

Directed, elliptic, and triangular flow of protons in Au+Au collisions at HADES energy

$$E_{lab} = 1.23 \text{ A GeV}$$

A theoretical analysis of the recent HADES data

Based on: P. Hillmann *et al.*, J. Phys. G **45**, no. 8, 085101 (2018), doi:10.1088/1361-6471/aac96f, arXiv:1802.01951 [nucl-th].

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Matter under Extreme Conditions in Heavy-Ion Collisions and
Astrophysics, Dubna, Russia, 2018

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Motivation

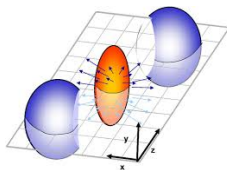
- At low energy Au+Au collisions baryon density is 3-4 times higher than the ground state density can be reached. One expects to find exotic particles or maybe even super conducting matter and a phase transition to the Quark Gluon Plasma.
- The dynamics are sensitive to the initial density and potential interactions and therefore the nuclear equation of state (EoS).
- Being sensitive to initial pressure gradients the collective flow is a promising variable to study the EoS.
- The HADES experiment performed Au+Au collisions at $E_{lab} = 1.23$ A GeV with a huge amount of data and is able to measure even higher order flow components.

- Collective flow as Fourier-series of momentum distribution:

$$E \frac{d^3 N}{d^3 p} = \frac{1}{2\pi} \frac{d^2 N}{p_T dp_T dy} \left(1 + 2 \sum_{n=1}^{\infty} v_n \cos[n(\varphi - \Psi_{RP})] \right) \quad (1)$$

- Calculation of the flow components as average over events in a given centrality class ($\Psi_{RP} = 0$):

$$v_n(p_T, y) = \langle \cos[n\varphi] \rangle \quad (2)$$



The equation of state in UrQMD

- UrQMD is based on a geometrical interpretation of the nuclear cross section and therefore includes string and resonance dynamics, scattering and strangeness exchange.
- To create two different EoS, potential interactions have to be taken into account.
- 1 The electromagnetic Coulomb potential V_C^{ij} with Z being the charge number of the particles, e the elementary charge and $|\mathbf{r}_i - \mathbf{r}_j|$ their relative distance:

$$V_C^{ij} = \frac{Z_i Z_j e^2}{|\mathbf{r}_i - \mathbf{r}_j|} \quad (3)$$

- 2 The strong force Yukawa potential V_Y^{ij} with $V_0^Y = -0.498$ MeV and $\gamma_Y = 1.4$ fm:

$$V_Y^{ij} = V_0^Y \cdot \frac{\exp(-|\mathbf{r}_i - \mathbf{r}_j|/\gamma_Y)}{|\mathbf{r}_i - \mathbf{r}_j|} \quad (4)$$

The equation of state in UrQMD

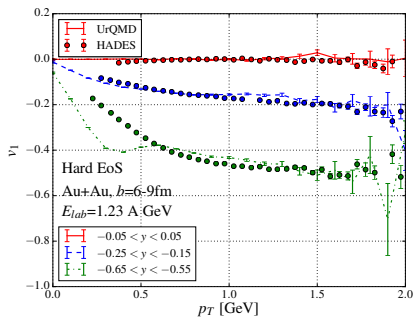
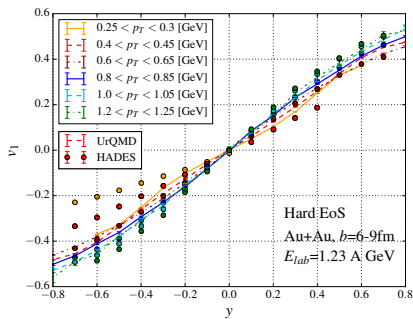
- ③ The hadronic Skyrme potential V_{Sk} to change the stiffness of the EoS with ρ_{int} the baryon density ρ_0 being the ground state baryon density:

$$V_{Sk} = \alpha \cdot \left(\frac{\rho_{int}}{\rho_0} \right) + \beta \cdot \left(\frac{\rho_{int}}{\rho_0} \right)^\gamma \quad (5)$$

Parameters	hard EoS	soft EoS
α [MeV]	-124	-356
β [MeV]	71	303
γ	2.00	1.17

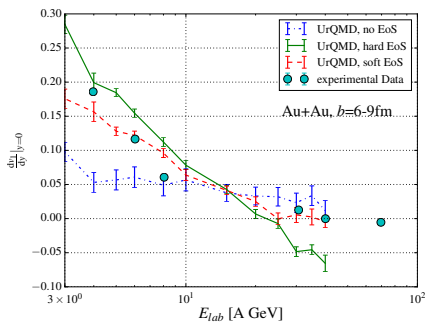
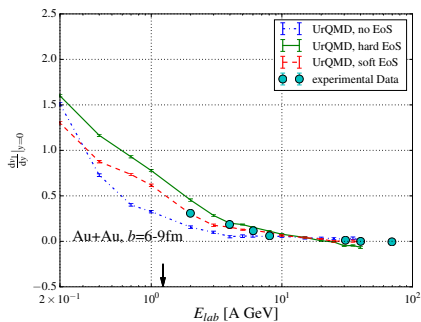
Table: Parameters used in the UrQMD Skyrme potential

Directed flow



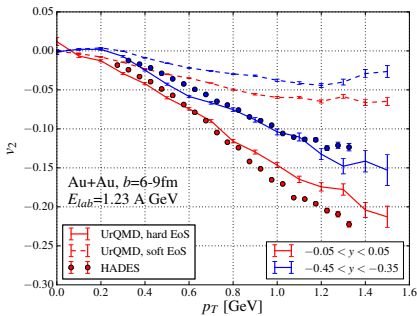
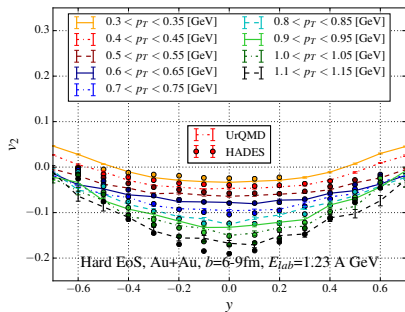
- No strong dependence on transverse momentum.
- Strong dependence on rapidity.
- Deviation at low p_T /higher y values maybe due to a lack of cluster formation.

Directed flow



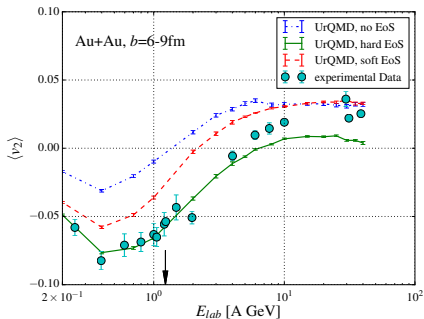
- At low energies hard EoS is preferred and at higher energies soft EoS.

Elliptic flow



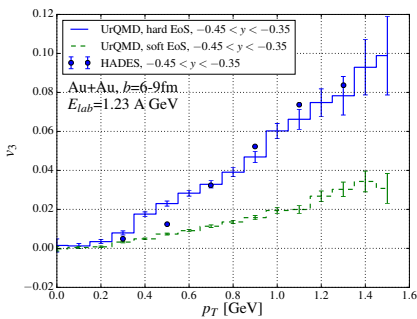
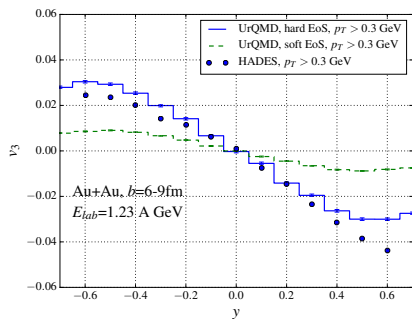
- Strong rapidity dependence.
- Strong transverse momentum dependence, decreasing with growing p_T .

Elliptic flow



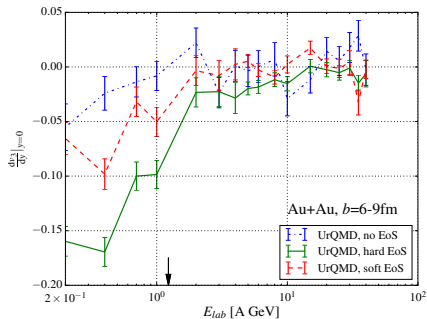
- At low energies a hard EoS is preferred, the flow is a consequence of the squeeze-out effect.
- With growing energy in-plane emission becomes more preferable and the flow turns positive. Also here the soft EoS becomes more preferable.

Triangular flow



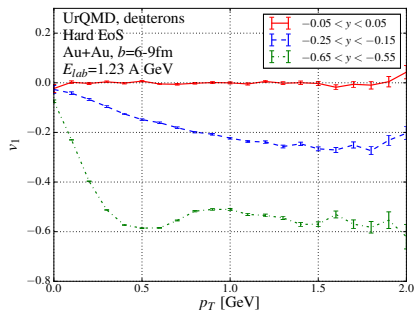
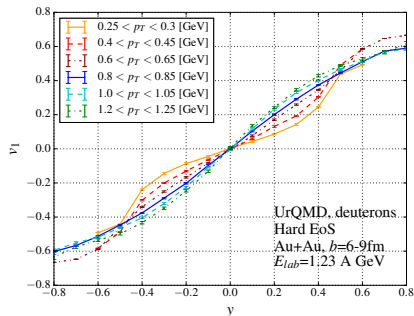
- Soft EoS underestimates the data.
- Measured $v_3 \neq 0$ with respect to the reaction plane makes separation of initial stage and expansion stage impossible at low energies.

Triangular flow



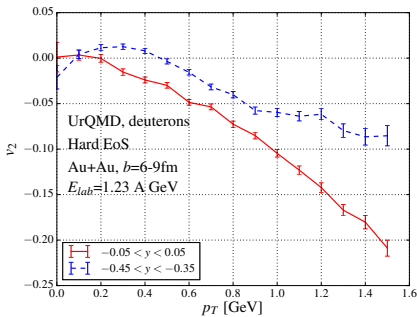
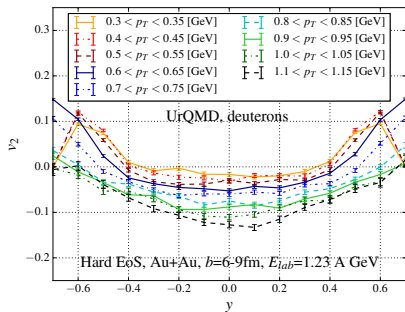
- Strong EoS dependence is observable.
- At higher energies v_3 vanishes.

Outlook: Preliminary directed flow of deuterons



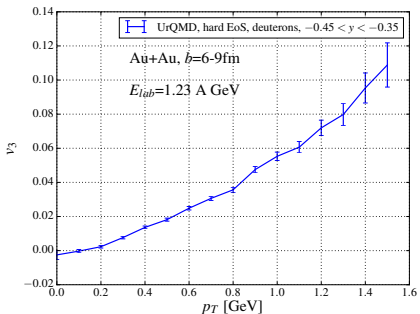
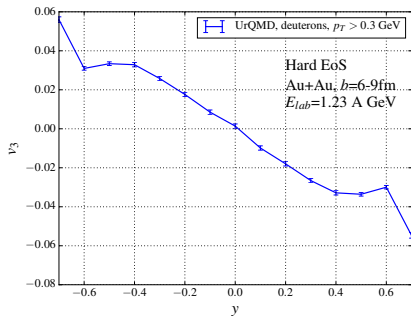
- Stronger dependence on transverse momentum.
- More negative flow as function of p_T .

Outlook: Preliminary elliptic flow of deuterons



- More negative elliptic flow as function of p_T due to higher p_y -component.

Outlook: Preliminary triangular flow of deuterons



Summary and Outlook

- UrQMD including two different equations of state was used to measure the collective flow of protons in Au+Au collisions at low and intermediate beam energies.
- The calculations agree with the data of different experiments. For low energies a hard EoS is preferred, for higher energies the soft EoS.
- The $v_3 \neq 0$ with respect to the reaction-plane indicates an interplay of initial stage and expansion stage.
- Cluster forming nucleons have a large effect to the collective proton flow. Therefore deuteron flow is now under investigation. Heavier nucleons will be included in near future.