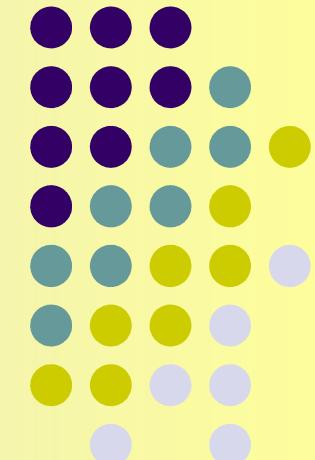


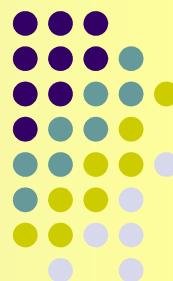


Background study for MMT-DY process at SPD ($\mu\mu$ case)



A.N.Skachkova
(JINR, Dubna)





V.A. Matveev, R.M. Muradian, A.N. Tavkhelidze (MMT)

(V.A. Matveev, R.M. Muradian, A.N Tavkhelidze, JINR P2-4543, JINR, Dubna, 1969; SLAC-TRANS-0098, JINR P2-4543, Jun 1069; 27p.)

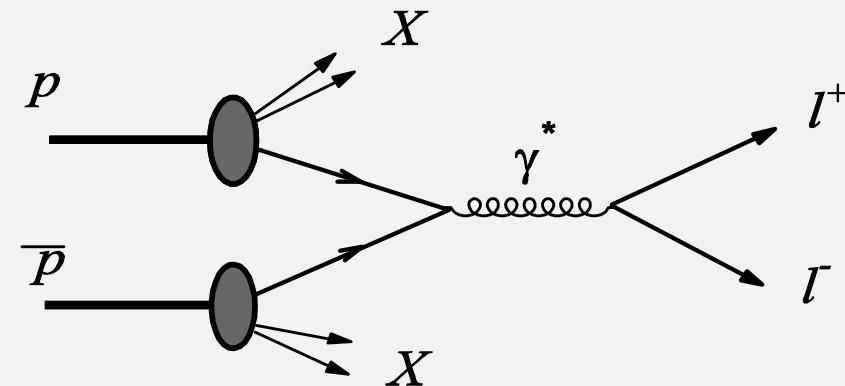
process, called also as Drell-Yan

(S.D. Drell, T.M. Yan, SLAC-PUB-0755, Jun 1970, 12p.; Phys.Rev.Lett. 25(1970)316-320, 1970)

The dominant mechanism
of the $|^+|^+$ production is
the perturbative QED/QCD
partonic $2 \rightarrow 2$ process

$$\bar{q}q \rightarrow \gamma^* / Z^0 \rightarrow |^+|^+$$

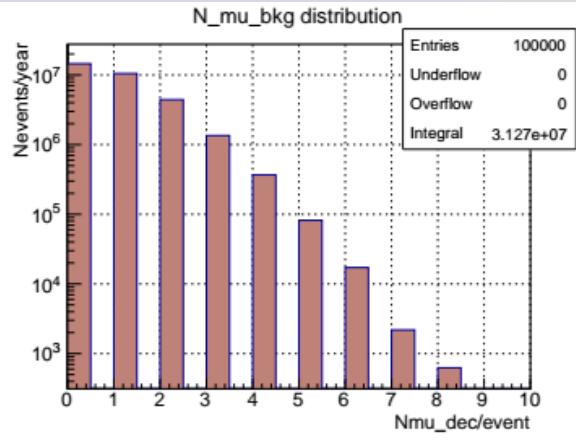
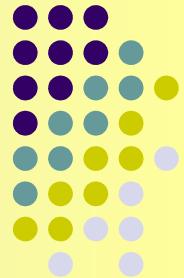
$$\sigma = 9.9 * 10^3 \text{ pb}$$



PYTHIA 6.4 simulation for the $E_{\text{cms}} = 27 \text{ GeV}$

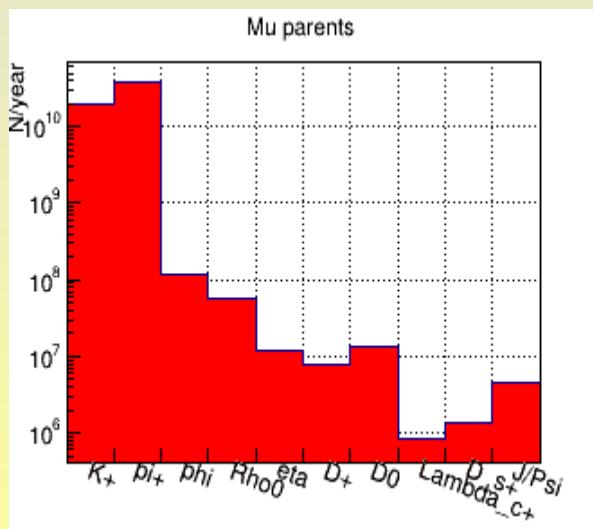
For the Luminosity $L = 1 \times 10^{32} \text{ cm}^{-2}\text{s}^{-1}$ with assumption of the full year beam operation
we expect up to 3.1×10^7 Drell-Yan events/year

Background muons in signal events



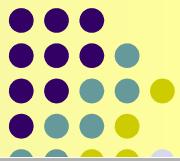
53.5 % of signal events contains >2 muons
 - up to 8 μ /event

We allow particles decay (and produce muons) in the volume before Muon (Range) System :
 cylindr radius **R = 2 400 mm**,
 size from the centre along Z axis **L = 4 000 mm**
 and search for muons in the angle region **9° < Θ < 171°**



The most probable parents of bkg muons - are charged π and K

The most probable grandparents of bkg muons - are «string» (Lund model), $\rho^0, \rho^+, K^0_s, K^{*0}, K^+, \eta'$

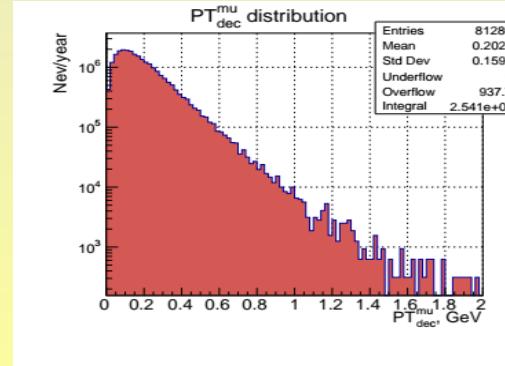
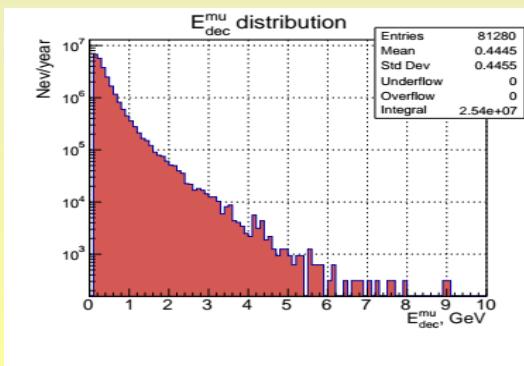
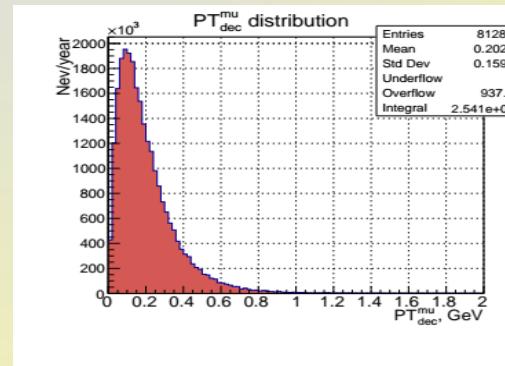
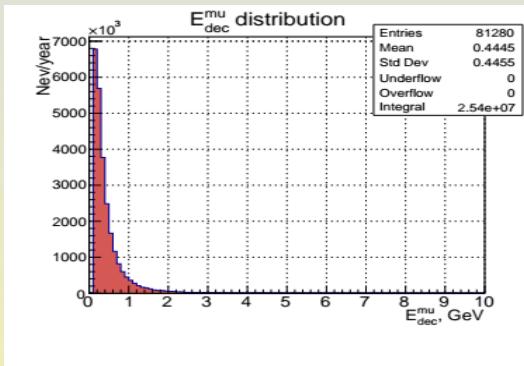
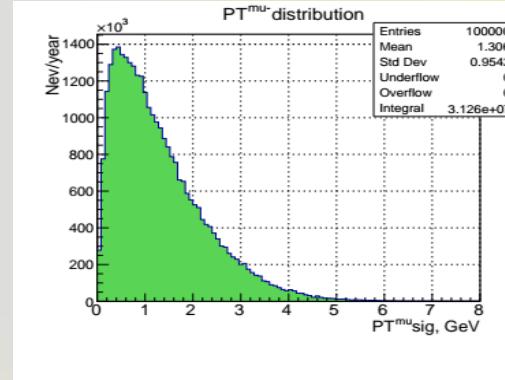
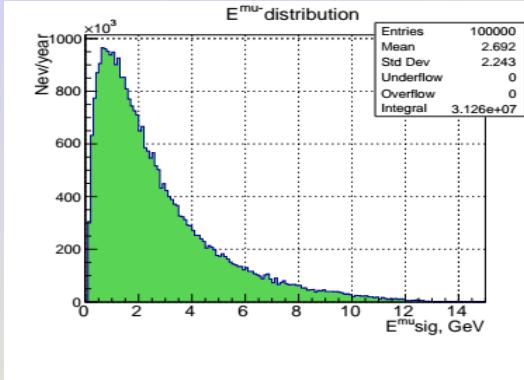


Decay muons in signal events

S
I
G

d
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c

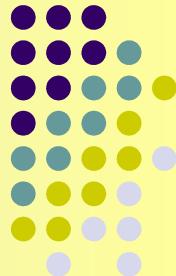
d
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Cuts : exactly 2 muons	E > 0.8 GeV	PT > 0.4 GeV
Reminder of signal events	54.1%	23.5%

Fraction of initial signal events with additional muons	2.1%	0.08%
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Fraction of remaining signal events with additional muons	3.9 %	0.3%
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Another situation when we have exactly 2 μ — first signal, the second — survived fake one.

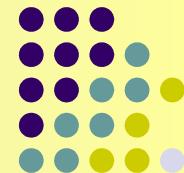
We have 2 situations -

1. Muons are of the same sign — easy to cut off
2. Muons are of different signs

After cutting off the events with additional (>2) muons we have

Cuts: exactly 2 muons with opposite signs	$E > 0.8 \text{ GeV}$ $\text{PT} > 0.4 \text{ GeV}$	$E > 1.0 \text{ GeV}$ $\text{PT} > 1.0 \text{ GeV}$
Reminder of signal events	51.9%	23.4%
Fraction of initial signal events with fake muons of the same sign	0.9%	0.09%
Fraction of remaining signal events with muons of the same sign	1.7 %	0.4%
Reminder of signal events after cut off the events with the muons of the same sign	51.0%	23.4%
Fraction of initial signal events with fake muons of different sign	0.9%	0.1%
Fraction of remaining signal events with muons of different sign	1.8 %	0.4%

Here we consider 2 kinds of backgrounds: QCD and Minimum-bias events



The generation was done with the use of more than 20 QCD subprocesses existed in PYTHIA

The main contributions come from the following partonic subprocesses:

- $q + g \rightarrow q + g$ (gives 2.8% of events with the $\sigma = 4.83$ mb);
- $g + g \rightarrow g + g$ (gives 2.5% of events with the $\sigma = 4.31$ mb);
- $q + q' \rightarrow q + q'$ (gives 0.7% of events with the $\sigma = 1.17$ mb);

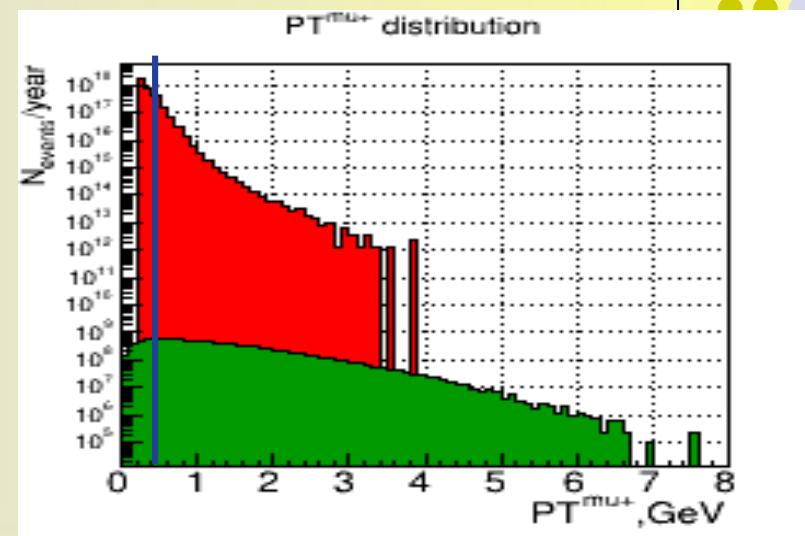
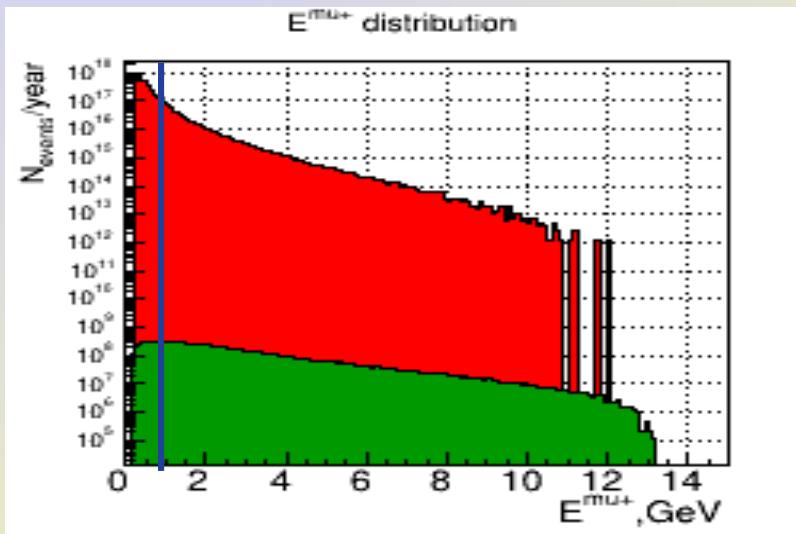
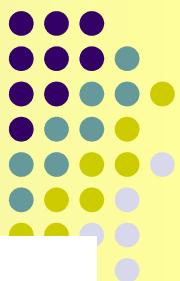
For QCD background $S/B \approx 10^{-6}$

The main source of background for the $\bar{q} q \rightarrow \gamma^* \rightarrow \mu^+ \mu^-$ are the Minimum-Bias processes:

- *Low - PT scattering* (gives 65% of events with the $\sigma = 13.0$ mb);
- *Single diffractive* (gives 22.3% of events with the $\sigma = 7.35$ mb);
- *Double diffractive* (gives 6.4% of events with the $\sigma = 2.12$ mb);
- $\bar{q} + q \rightarrow l^+ + l^-$ (has 0.000028% of events with the $\sigma = 9.9 \times 10^{-6}$ mb);

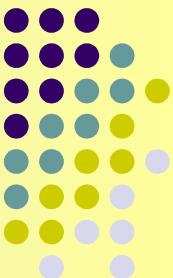
For Mini-bias background $S/B \approx 3 \times 10^{-7}$

First cuts — on E and PT

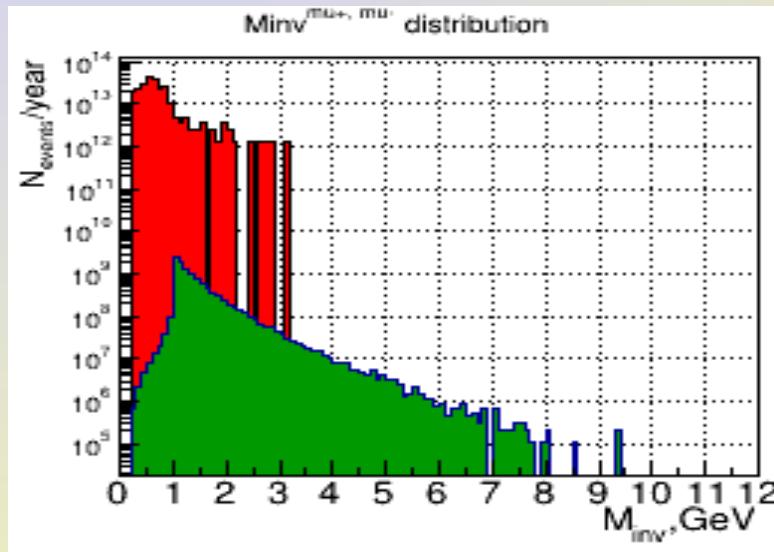


Effective cut off on E(P) only in the region $E_{\text{bkg}}^{\mu} < 1.5 \text{ GeV}$ ($E_{\text{bkg}}^{\mu} = 0.8 \text{ GeV}$) where is the maximum gradient in E_{bkg}^{μ} distribution

The most effective cuts off are in the region $PT_{\text{bkg}}^{\mu} < 1.5 \text{ GeV}$ ($PT_{\text{bkg}}^{\mu} = 0.4 \text{ GeV}$)



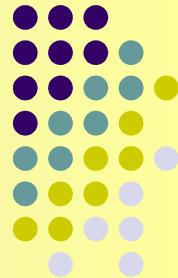
Invariant mass cut



The most effective cut is in the region < 0,9 — 1 GeV.

Further increase of Minv cut has no sense for Minimum-bias background events (it leads to significant loss of signal events without real improvement of S/B ratio) except backgrounds in the regions of J/ Ψ and other resonances production.

Efficiency of $M_{inv} (\mu^+, \mu^-)$ cut

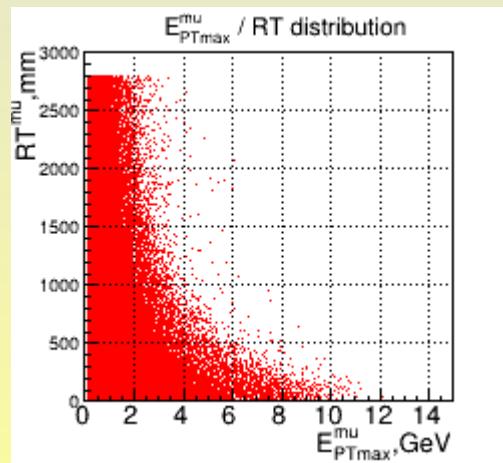
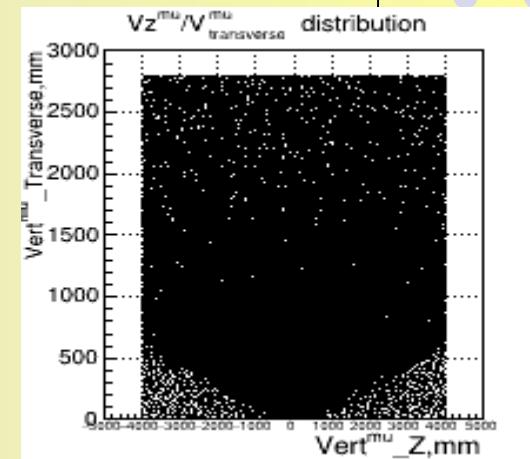
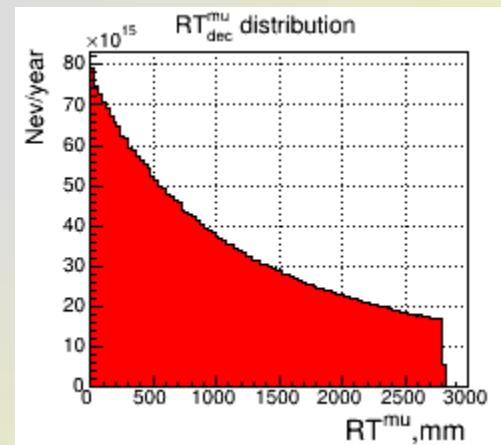
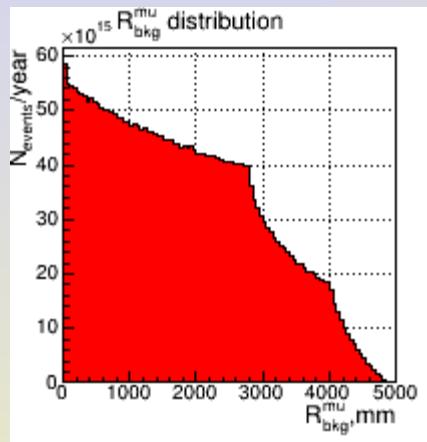
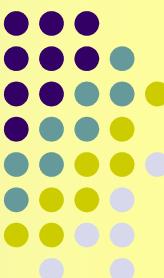


Together with the cut $E, PT > 1$ GeV

Supposing 100 % - without Minv cut

M_{inv} cut	Rest of BKG	Cut efficiency	Rest of sig	Cut efficiency	S/B
$M_{inv}^{\mu\mu} > 0.9$ GeV	76.7 %	1.3	100 %	1	0.038
$M_{inv}^{\mu\mu} > 1.0$ GeV	73.8 %	1.35	99.4 %	1.006	0.039
$M_{inv}^{\mu\mu} > 1.5$ GeV	64.4 %	1.55	39.2 %	2.55	0.021
$M_{inv}^{\mu\mu} > 2.0$ GeV	55.8 %	1.79	21.1 %	4.73	0.013
$M_{inv}^{\mu\mu} > 2.5$ GeV	35.9 %	2.78	12.6 %	7.9	0.010
$M_{inv}^{\mu\mu} > 3.0$ GeV	19.7 %	5.06	7.6 %	13.1	0.014
$M_{inv}^{\mu\mu} > 3.5$ GeV	9.7 %	10.3	4.5 %	21.9	0.019
$M_{inv}^{\mu\mu} > 4.0$ GeV	5.2 %	19.1	2.7 %	36.7	0.018
$M_{inv}^{\mu\mu} > 4.5$ GeV	3.1 %	31.6	1.6 %	61.6	0.030
$M_{inv}^{\mu\mu} > 5.0$ GeV	2.0 %	48.5	1.0 %	101.5	0.046

Vertex distributions

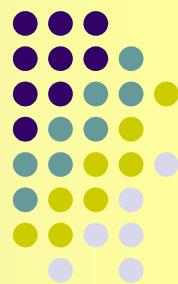


$$R = \sqrt{x^2 + y^2 + z^2}$$

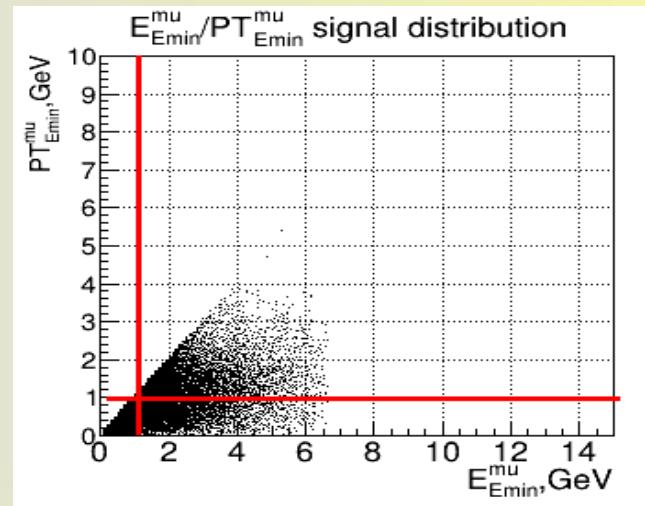
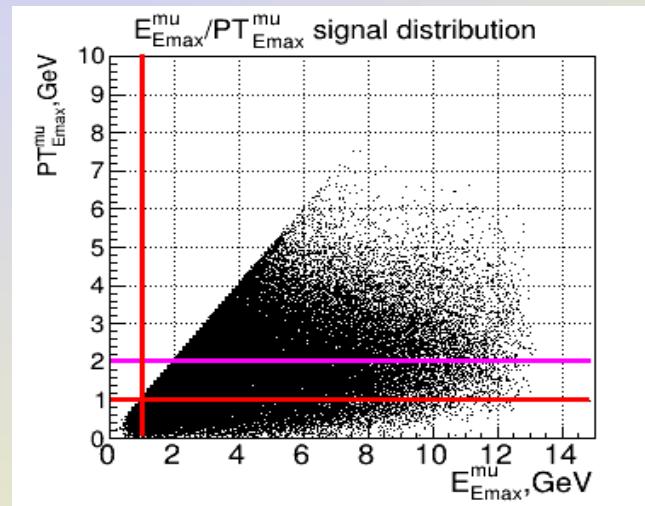
$$RT = \sqrt{x^2 + y^2}$$

$E_{\text{PTmax}}^{\mu\mu}$ - energy of leading μ with max PT

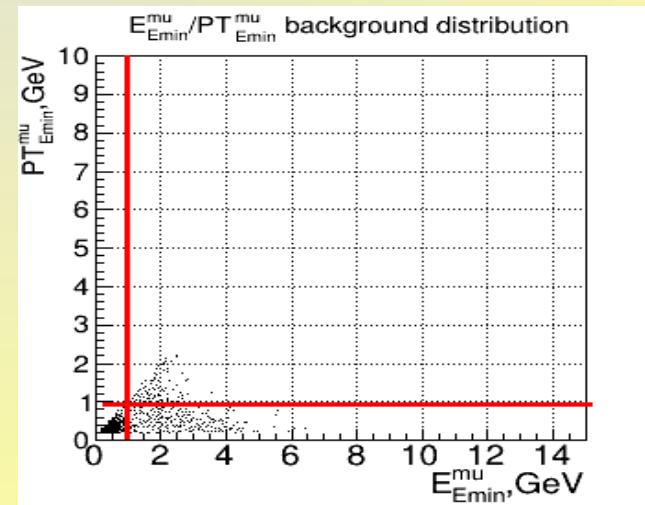
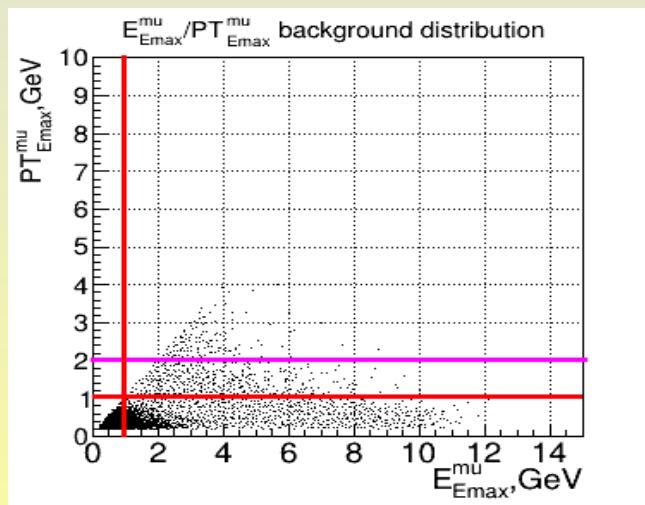
E^μ/PT^μ correlations for muons with max(fast)/min(slow) E^μ in the pair



S
I
G



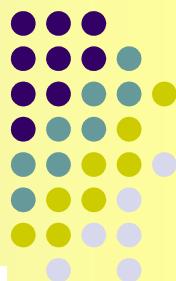
B
K
G



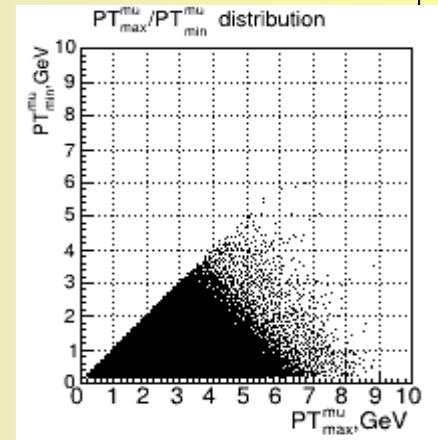
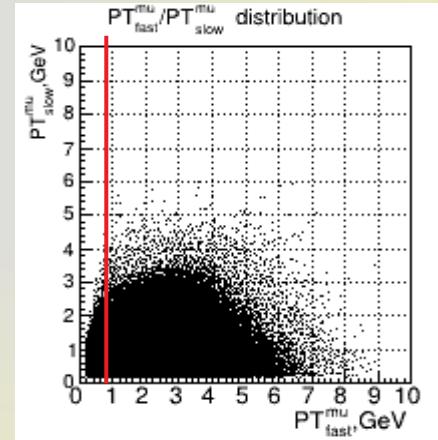
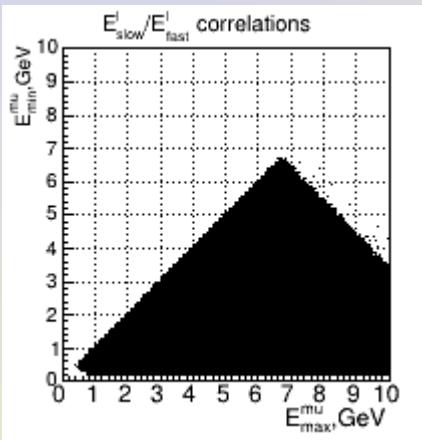
$PT_{E\text{max}}^{\mu} > 2.0$ GeV can also be considered

Cut on $PT_i > 1.0$ GeV and $E\mu > 1.0$ GeV

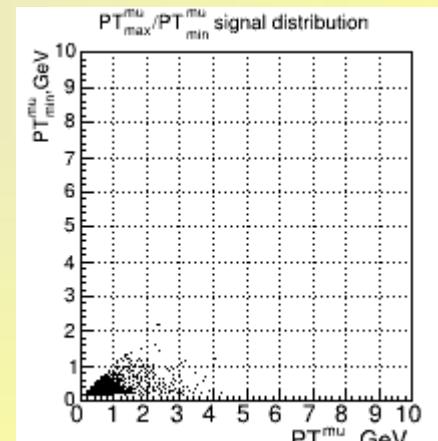
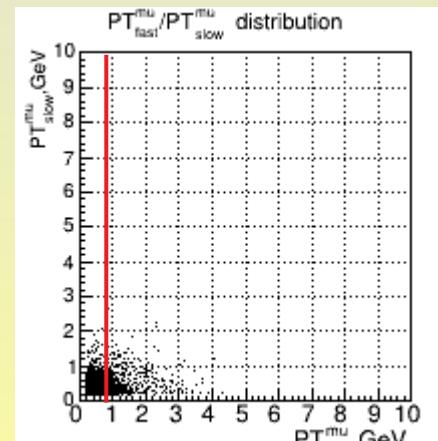
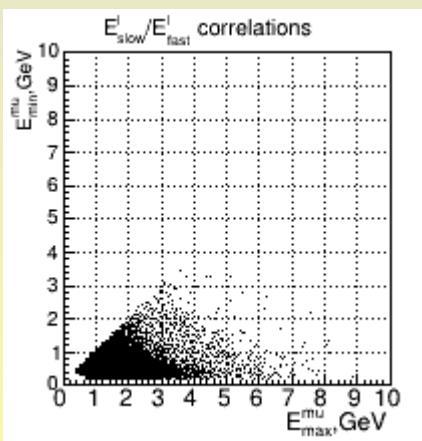
$E_{\max}^{\text{fast}} / E_{\min}^{\text{slow}}$, $\text{PT}_{\text{fast}} / \text{PT}_{\text{slow}}$, $\text{PT}_{\max} / \text{PT}_{\min}$ distributions



S
I
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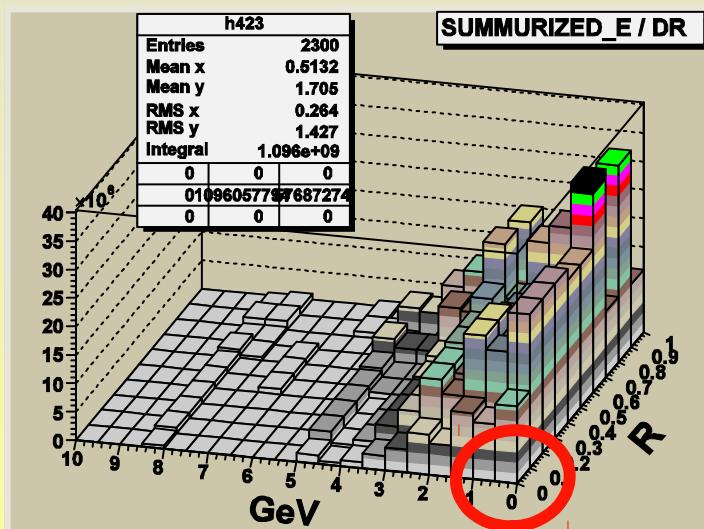
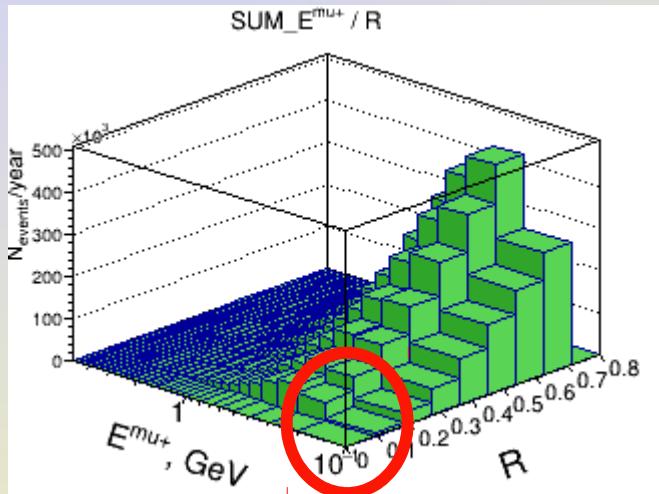


B
K
G



Proposed cuts

- 1. Events with only 2 muons with $\text{PT}_l > 1.0 \text{ GeV}$,
 $E_l > 1.0 \text{ GeV}$ ($\text{PT}_l > 0.4 \text{ GeV}$, $E_l > 0.8 \text{ GeV}$)**
- 2. Muons are of the *opposite sign***
- 3. $\text{Minv}(l^+, l^-) > 0.9 \text{ GeV}$**
- 4. The vertex of origin lies within the
distance from the interaction point $< 1 \text{ mm}$**
- 5. Isolation criteria $E_{(R \text{ isolation} = 0.2)}^{\text{sum}} > 0.5 \text{ GeV}$**



The plots show the distributions over **summarized energy** of the final state charged particles in the cones of radius

$R_{\text{isolation}} = \sqrt{\eta^2 + \phi^2}$ respect to the
(η — *pseudorapidity*, ϕ — *azimuthal angle*)

upper plot **signal events**

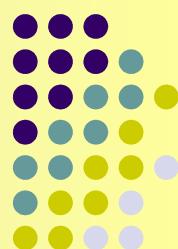
bottom plot **Mini-bias background**

Isolation criteria ($R_{\text{isolation}} = 0.2$)
 E (of particles) > 0.5 GeV

allows to separate most part
of Mini-bias & QCD bkg muons
with the loss of 0.7 % of signal events

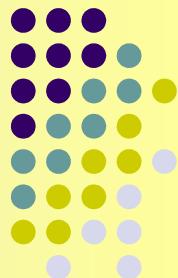
after applied 4 cuts discussed above

Cuts separate efficiency for mini-bias and QCD background events (10^9)



$$\text{Efficiency } \text{Eff } (K,N) = \text{Nev(cut}N\text{)} / \text{Nev(cut}K\text{)}$$

N of cuts	S/B ratio	Efficiency for BKG	Rest of BKG	Efficiency for SIG	Rest of SIG- 3.1×10^7 /year
1 <i>Exactly 2μ with $P_{T,\mu} > 1.0 \text{ GeV}$, $E_T > 1.0 \text{ GeV}$</i>	$1.7 * 10^{-2}$	Eff (1,init) = 286041	$3.5 \times 10^{-4} \text{ %}$	4.8	20.9 %
2 ⁺¹ <i>2μ are of the opposite sign</i>	$2.9 * 10^{-2}$	Eff (2,1) = 1.67	$2.1 \times 10^{-4} \text{ %}$	1	20.9 %
3 ⁺²⁺¹ <i>$M_{inv}(\mu_1, \mu_2) > 0.9 \text{ GeV}$</i>	$3.8 * 10^{-2}$	Eff (3,2) = 1.3	$1.6 \times 10^{-4} \text{ %}$	1	20.9 %
4 ⁺³⁺²⁺¹ <i>The vertex is in $R < 1 \text{ mm}$</i>	2.8	Eff (4,3) = 72.8	$2.2 \times 10^{-6} \text{ %}$	1	20.9 %
5 ⁺³⁺²⁺¹ <i>$P_{T,\mu}^{max} > 2.0 \text{ GeV}$</i>	0.415	Eff (5,3) = 30.2	$5.3 \times 10^{-6} \text{ %}$	2.8	7.5 %
6 ⁺³⁺²⁺¹ <i>Isolation criterium</i>	> 59	Eff (6,3) > 1602	< $8.6 \times 10^{-8} \text{ %}$	1.03	20.2 %



Cuts separate efficiency for mini-bias and QCD background events (10^9 - not enough)

$M^{\mu+\mu^-}_{inv} > 4.3 \text{ GeV}$ $S/B = 1.7 \times 10^{-9}!$

N of cuts	S/B ratio	Efficiency for BKG	Rest of BKG	Efficiency for SIG	Rest of SIG — 1.4×10^5 /year
1 Exactly 2 μ with $PT_1 > 1.0 \text{ GeV}, E_1 > 1.0 \text{ GeV}$	$3.9 * 10^{-4}$	Eff (1,init) = 293599	$3.4 \times 10^{-4} \%$	1.26	79.4 %
2 ⁺¹ 2 μ are of the opposite sign	$6.6 * 10^{-4}$	Eff (2,1) = 1.7	$2.0 \times 10^{-4} \%$	1	79.3 %
3 ⁺²⁺¹ $M_{inv}(\mu_1, \mu_2) > 4.3 \text{ GeV}$	$1.2 * 10^{-2}$	Eff (3,2) = 18	$1.2 \times 10^{-5} \%$	~1	79.3 %
4 ⁺³⁺²⁺¹ The vertex is in $R < 1 \text{ mm}$	> 1.3	Eff (4,3) > 113	$< 10^{-7} \%$	1	79.3 %
5 ⁺³⁺²⁺¹ $PT^\mu_{Emax} > 2.0 \text{ GeV}$	$5.0 * 10^{-2}$	Eff (5,3) = 6.6	$1.7 \times 10^{-6} \%$	1.58	50.1 %
6 ⁺³⁺²⁺¹ Isolation criterium	> 0.8	Eff (6,3) > 113	$< 10^{-7} \%$	1.63	48.6 %

Processes with charmonium production – S/B $\sim 7,6 \cdot 10^{-3}$

86) $g g \rightarrow J/\Psi + g \rightarrow \mu^+ \mu^- + X$ R.Baier and R.Rücke, Z.Phys. **C19** (1983) 251
 106) $g g \rightarrow J/\Psi + \gamma \rightarrow \mu^+ \mu^- + X$ M.Drees and C.S.Kim, Z.Phys. **C53** (1991) 673

- 421) $g g \rightarrow cc^- [{}^3S_1 {}^{(1)}] g \rightarrow \mu^+ \mu^- + X$
- 422) $g g \rightarrow cc^- [{}^3S_1 {}^{(8)}] g \rightarrow \mu^+ \mu^- + X$
- 423) $g g \rightarrow cc^- [{}^3S_0 {}^{(8)}] g \rightarrow \mu^+ \mu^- + X$
- 424) $g g \rightarrow cc^- [{}^3P_J {}^{(8)}] g \rightarrow \mu^+ \mu^- + X$
- 425) $g q \rightarrow cc^- [{}^3S_1 {}^{(8)}] q \rightarrow \mu^+ \mu^- + X$
- 426) $g q \rightarrow cc^- [{}^3P_J {}^{(8)}] q \rightarrow \mu^+ \mu^- + X$
- 427) $g g \rightarrow cc^- [{}^3S_1 {}^{(1)}] q \rightarrow \mu^+ \mu^- + X$
- 428) $q q^- \rightarrow cc^- [{}^3S_1 {}^{(8)}] g \rightarrow \mu^+ \mu^- + X$
- 429) $q q^- \rightarrow cc^- [{}^1S_0 {}^{(8)}] g \rightarrow \mu^+ \mu^- + X$
- 430) $q q^- \rightarrow cc^- [{}^3P_J {}^{(8)}] g \rightarrow \mu^+ \mu^- + X$

- 431) $g g \rightarrow cc^- [{}^3P_0 {}^{(1)}] g \rightarrow \mu^+ \mu^- + X$
- 432) $g g \rightarrow cc^- [{}^3P_1 {}^{(1)}] g \rightarrow \mu^+ \mu^- + X$
- 433) $g g \rightarrow cc^- [{}^3P_2 {}^{(1)}] g \rightarrow \mu^+ \mu^- + X$
- 434) $g q \rightarrow cc^- [{}^3P_0 {}^{(1)}] q \rightarrow \mu^+ \mu^- + X$
- 435) $g q \rightarrow cc^- [{}^3P_1 {}^{(1)}] q \rightarrow \mu^+ \mu^- + X$
- 436) $g q \rightarrow cc^- [{}^3P_2 {}^{(1)}] q \rightarrow \mu^+ \mu^- + X$
- 437) $q q \rightarrow cc^- [{}^3P_0 {}^{(1)}] g \rightarrow \mu^+ \mu^- + X$
- 438) $q q \rightarrow cc^- [{}^3P_1 {}^{(1)}] g \rightarrow \mu^+ \mu^- + X$
- 439) $q q \rightarrow cc^- [{}^3P_2 {}^{(1)}] g \rightarrow \mu^+ \mu^- + X$

431, 433, 434, 436 – maximum contribution

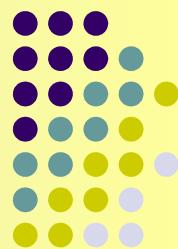
G.T.Badwin, E.Braten and G.P.Lepage, Phys.Rev. **D51** (1995) 1125 [Erratum: *ibid* **D55** (1997) 5883];

M.Beneke, MKrämer and M.Vänttinen, Phys.Rev. **D57** (1998) 4258;

B.A.Kniehl and I.Lee, Phys.Rev. **D62** (2000) 114027

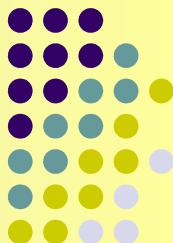
Cuts separate efficiency for charmonium background events (10^8)

$$\text{Efficiency } \text{Eff} (K,N) = \text{Nev (cutN)} / \text{Nev (cutK)}$$

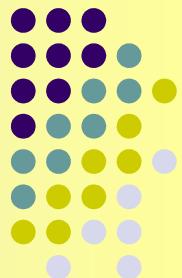


N of cuts	S/B ratio	Efficiency for BKG	Rest of BKG	Efficiency for SIG	Rest of SIG
1 Exactly 2 μ with $\text{PT}_\mu > 1.0 \text{ GeV}$, $E_\gamma > 1.0 \text{ GeV}$	0.306	Eff (1,init) = 170.8	$5.8 \times 10^{-1} \%$	4.27	23.4 %
2 ⁺¹ 2 μ are of the opposite sign	0.307	Eff (2,1) = 1.005	$5.8 \times 10^{-1} \%$	1,003	23.3 %
3 ⁺²⁺¹ $M_{inv}(\mu_1, \mu_2) > 0.9 \text{ GeV}$	0.307	Eff (3,2) = 1.001	$5.8 \times 10^{-1} \%$	1,003	23.2 %
4 ⁺³⁺²⁺¹ The vertex is in $R < 1 \text{ mm}$	0.302	Eff (4,3) = 1.007	$5.7 \times 10^{-1} \%$	1,02	22.7 %
5 ⁺³⁺²⁺¹ $\text{PT}^\mu > 2.0 \text{ GeV}$	0.374	Eff (5,3) = 3.8	$1.5 \times 10^{-1} \%$	3.11	7.5 %
6 ⁺³⁺²⁺¹ Isolation criterium	> 175138	Eff (6,3) > 577184	$< 1.01 \times 10^{-6} \%$	1.01	23.0 %

Cuts separate efficiency for charmonium background events (10^8)



N of cuts	S/B ratio	Efficiency for BKG	Rest of BKG	Efficiency for SIG	Rest of SIG
1 Exactly 2 μ with $PT_1 > 0.4 \text{ GeV}$, $E_1 > 0.8 \text{ GeV}$	0.32	Eff (1,init) = 79.9	1.2 %	1.92	52.1 %
2 ⁺¹ 2 μ are of the opposite sign	0.36	Eff (2,1) = 1.14	1.1 %	1.01	51.3 %
3 ⁺²⁺¹ $M_{inv}(l_1, l_2) > 0.9 \text{ GeV}$	0.37	Eff (3,2) = 1.004	1.05 %	1.00	51.0 %
4 ⁺³⁺²⁺¹ The vertex is in $R < 1 \text{ mm}$	0.27	Eff (4,3) = 1.16	0.9 %	1.60	31.8 %
5 ⁺³⁺²⁺¹ $PT^\mu > E_{max}$ 1.0 GeV	0.36	Eff (5,3) = 1.42	0.74 %	1.47	34.7 %
6 ⁺³⁺²⁺¹ Isolation criteria	> 377979	Eff (6,3) > 1044838	$< 1.01 \times 10^{-6} \%$	1.03	49.6 %

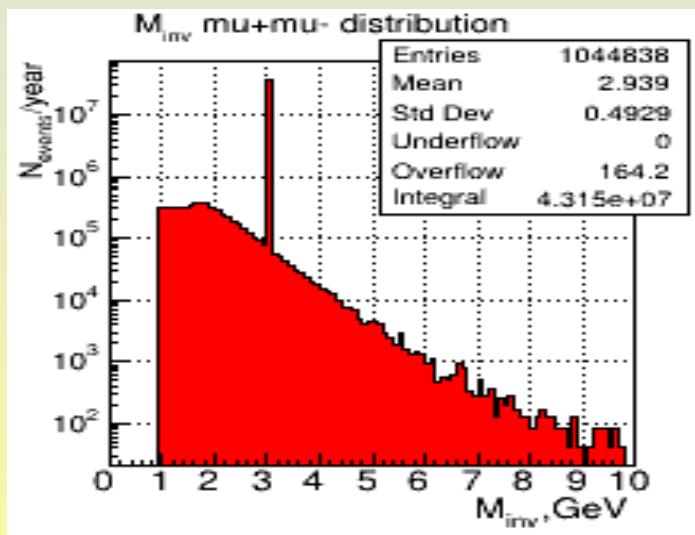


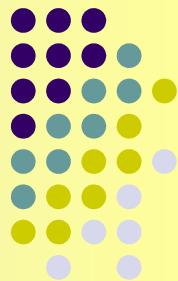
For charmoniums background Vertex information doesn't work.

Cut on PT of leading muon weakly helps.

The best criterium - the isolation criterium.

Additional S/B reduction can be achieved by excluding the resonance M_{inv} peaks.

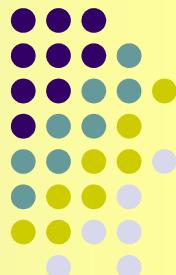




Cuts separate efficiency for mini-bias and QCD background events (10^9)

Efficiency Eff (K,N) = Nev(cutN) / Nev(cutK)

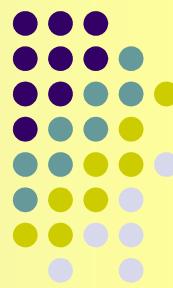
N of cuts	S/B ratio	Efficiency for BKG	Rest of BKG	Efficiency for SIG	Rest of SIG
1 Exactly 2 μ with $\text{PT}_{\mu} > 0.4 \text{ GeV}$, $E_{\nu} > 0.8 \text{ GeV}$	$2.1 * 10^{-4}$	Eff (1,init) = 1606	$6.2 \times 10^{-2} \%$	2.17	46 %
2⁺¹ 2 μ are of the opposite sign	$3.7 * 10^{-4}$	Eff (2,1) = 1.76	$3.5 \times 10^{-2} \%$	1.02	45 %
3⁺²⁺¹ $M_{inv}(\mu_1, \mu_2) > 0.9 \text{ GeV}$	$4.7 * 10^{-4}$	Eff (3,2) = 1.28	$2.7 \times 10^{-2} \%$	1.01	44.7%
4⁺³⁺²⁺¹ $\text{PT}_{\mu}^{\text{Emax}} > 1.0 \text{ GeV}$	$6.9 * 10^{-3}$	Eff (4,3) = 19.7	$1.4 \times 10^{-3} \%$	1.34	33.3 %
5⁺³⁺²⁺¹ The vertex is in $R < 1 \text{ mm}$	0.158	Eff (5,3) = 334	$8.2 \times 10^{-5} \%$	1	44.7%
6⁺³⁺²⁺¹ Isolation criterium	3.5	Eff (6,3) = 7656	$3.6 \times 10^{-6} \%$	1.03	43.3 %



Cuts summarized efficiency for mini-bias and QCD background events (10^9)

Efficiency Eff (K,N) = Nev(cutN) / Nev(cutK)

N of cuts	S/B ratio	Efficiency for BKG	Rest of BKG	Efficiency for SIG	Rest of SIG
1 <i>Exactly 2 μ with $PT_i > 0.4 \text{ GeV}$, $E_i > 0.8 \text{ GeV}$</i>	$2.1 * 10^{-4}$	Eff (1,init) = 1606	$6.2 \times 10^{-2} \text{ %}$	2.17	46 %
2 ⁺¹ <i>2μ are of the opposite sign</i>	$3.7 * 10^{-4}$	Eff (2,1) = 1.76	$3.5 \times 10^{-2} \text{ %}$	1.02	45 %
3 ⁺²⁺¹ <i>$M_{inv}(\mu_1, \mu_2) > 0.9 \text{ GeV}$</i>	$4.7 * 10^{-4}$	Eff (3,2) = 1.28	$2.7 \times 10^{-2} \text{ %}$	1.01	44%
4 ⁺³⁺²⁺¹ <i>$PT^\mu_{Emax} > 1.0 \text{ GeV}$</i>	$6.1 * 10^{-3}$	Eff (4,3) = 19.7	$1.4 \times 10^{-3} \text{ %}$	1.5	29 %
5 ⁺⁴⁺³⁺²⁺¹ <i>The vertex is in $R < 1 \text{ mm}$</i>	1.75	Eff (5,4) = 5625	$4.9 \times 10^{-6} \text{ %}$	1.5	29%
6 ⁺⁵⁺⁴⁺³⁺²⁺¹ <i>Isolation criterium</i>	> 86	Eff (6,5) > 275635	$< 1 \times 10^{-7} \text{ %}$	1.5	29 %



Conclusion

The proposed cuts:

- 1.** *Events with only 2 leptons of the opposite sign and $E_l > 0.8 \text{ GeV}$, $\text{PT}_l > 0.4 \text{ GeV}$*
- 2.** *The vertex of origin lies within the distance from the interaction point $< 1 \text{ mm}$*
- 3.** *$\text{Minv}(l^+, l^-) > 0.9 \text{ GeV}$*
- 4.** *Isolation criteria $E_{(R \text{ isolation} = 0.2)} > 0.5 \text{ GeV}$*

*Allow to suppress **for muons** QCD & Mini-bias bkgd up to **S/B > 80** with the **loss of signal** ~ 70%*

Further study with SPDRoot is needed