

THE QUEST FOR PHASE TRANSITIONS IN STRONGLY INTERACTING MATTER

Anar Rustamov

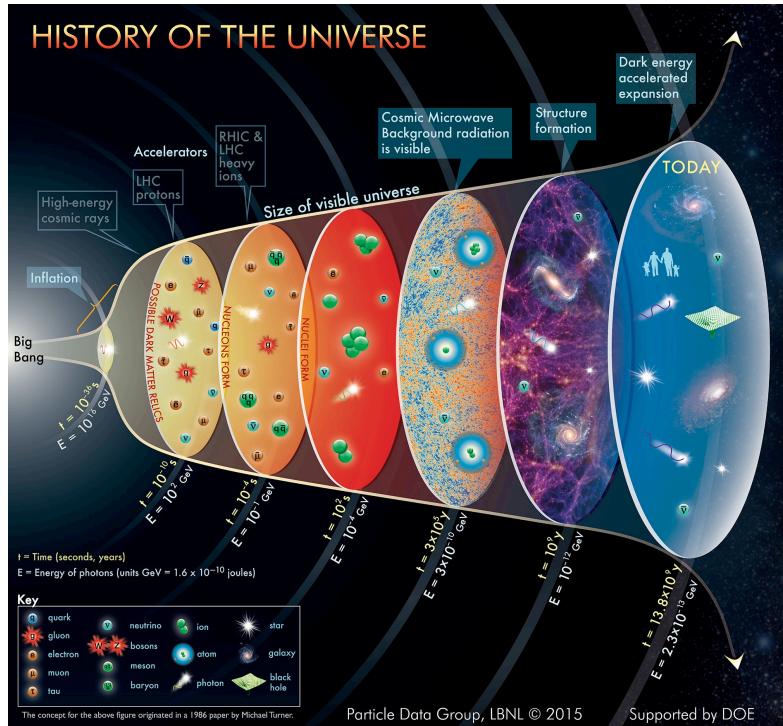
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- Phase transitions then and now
- Phases of EM interacting matter
- Phases of strongly interacting matter
- Experimental programs
 - Obtained results
- Summary
- Outlook

Phase transitions then and now



$$m_p \approx 937 \text{ MeV}$$

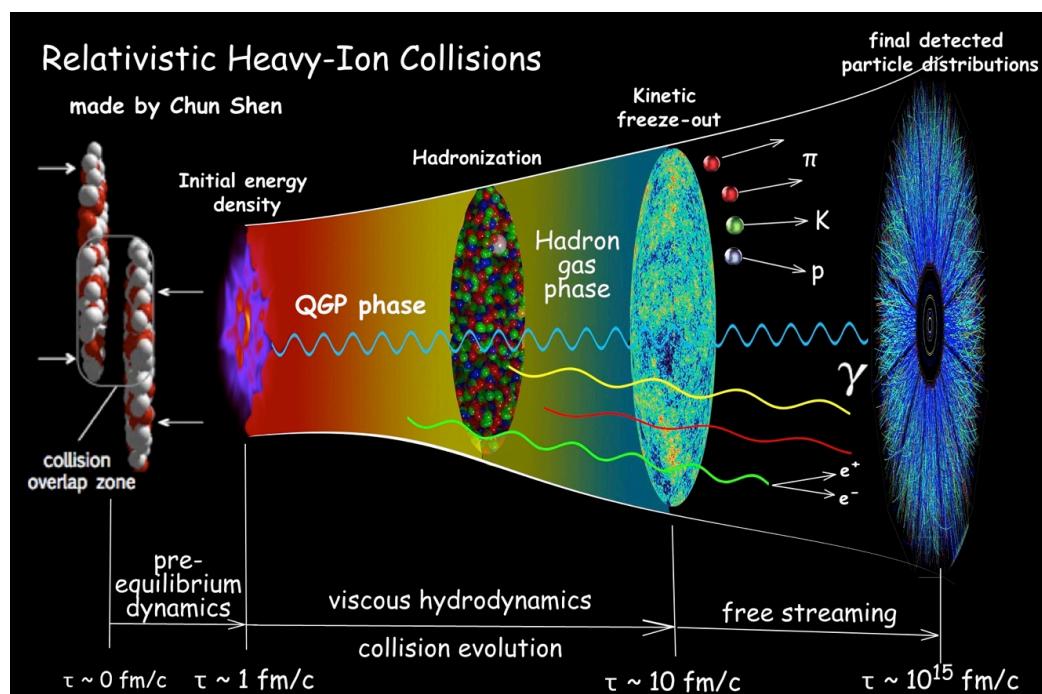
$$2m_u + m_d \approx 10 \text{ MeV}$$

(broken Chiral symmetry)

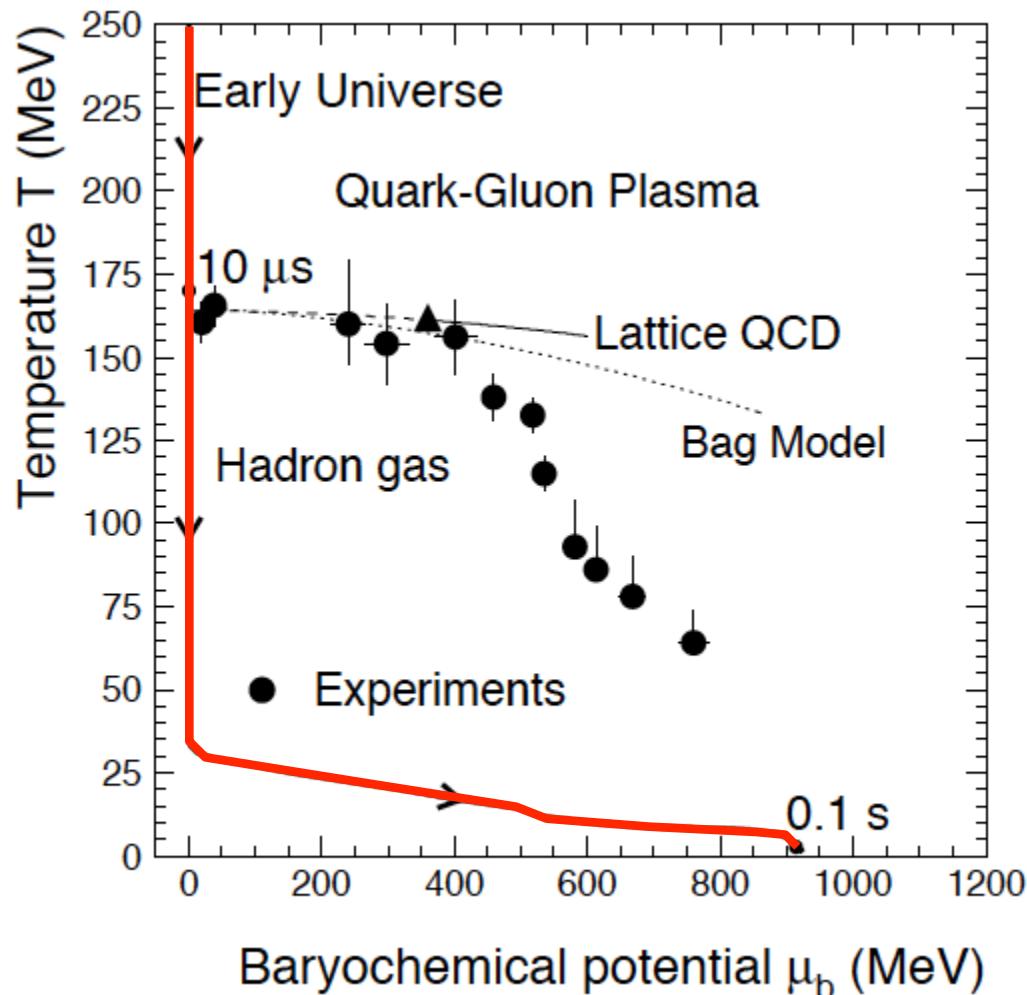
no isolated quarks seen thus far
(confinement)

1/100.000 seconds after the Big Bang
quarks and gluons recombine to hadrons

- recreating the Universe in laboratories
- exploring phase transitions



Bing Bang vs. Little Bangs



Ansatz:

- charge neutrality
- net-lepton number = net baryon number
- constant entropy per-baryon

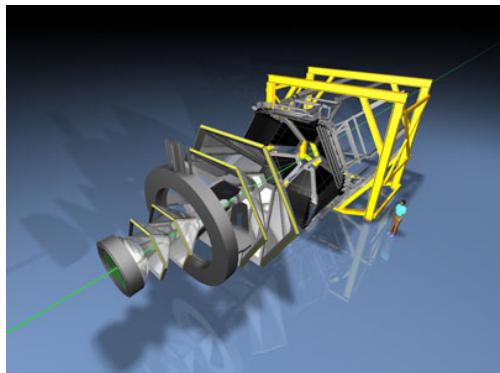
P. Braun-Munzinger, J. Wambach,
Rev. Mod. Phys. 81, (2009) , 1031

H. Schade, B. Kämpfer,
Phys. Rev. C79 (2009), 044909

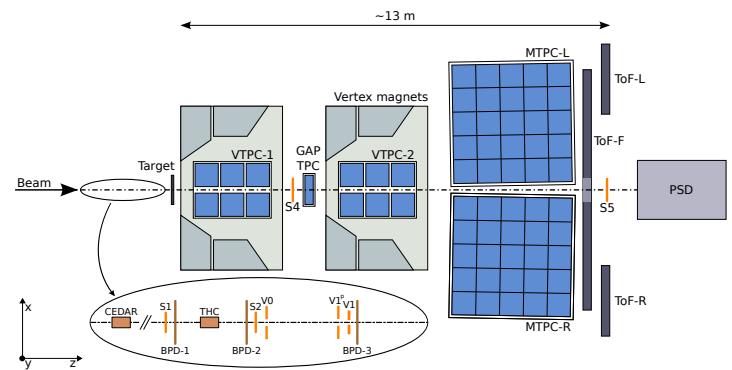
The Universe follows a different path!

Experimental campaigns in a wide energy range

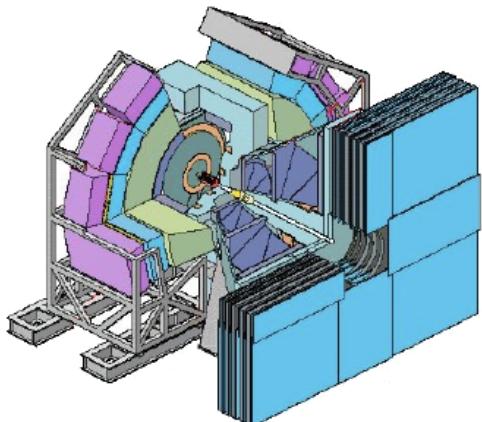
HADES (few GeV)



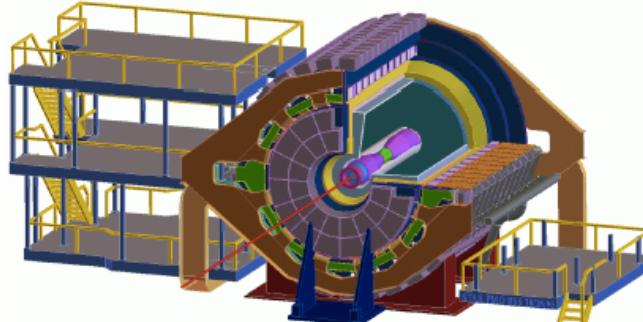
NA61/SHINE (5- 17 GeV)



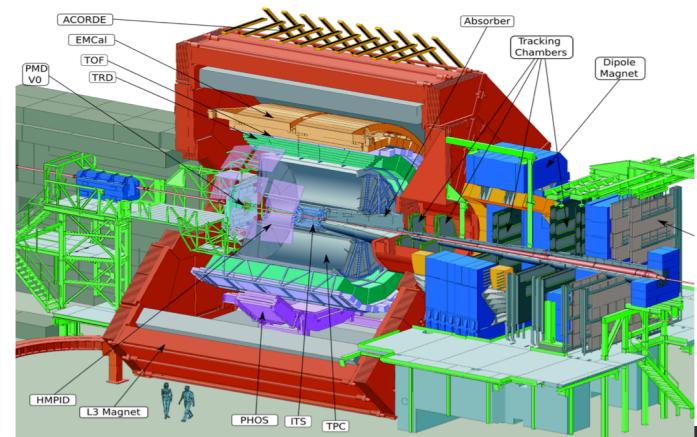
PHENIX (7.7- 62.4 GeV)



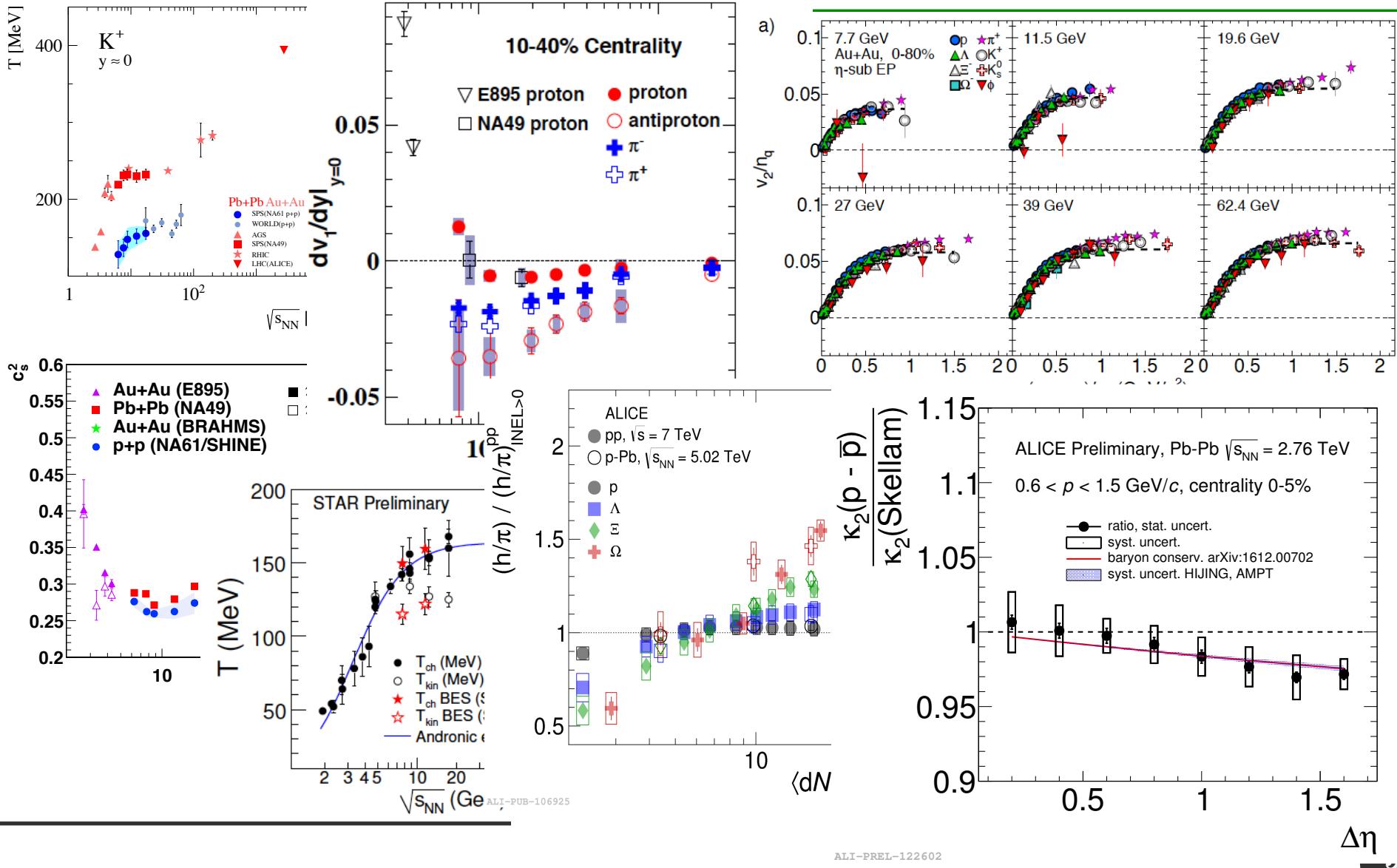
STAR (7.7- 62.4 GeV)



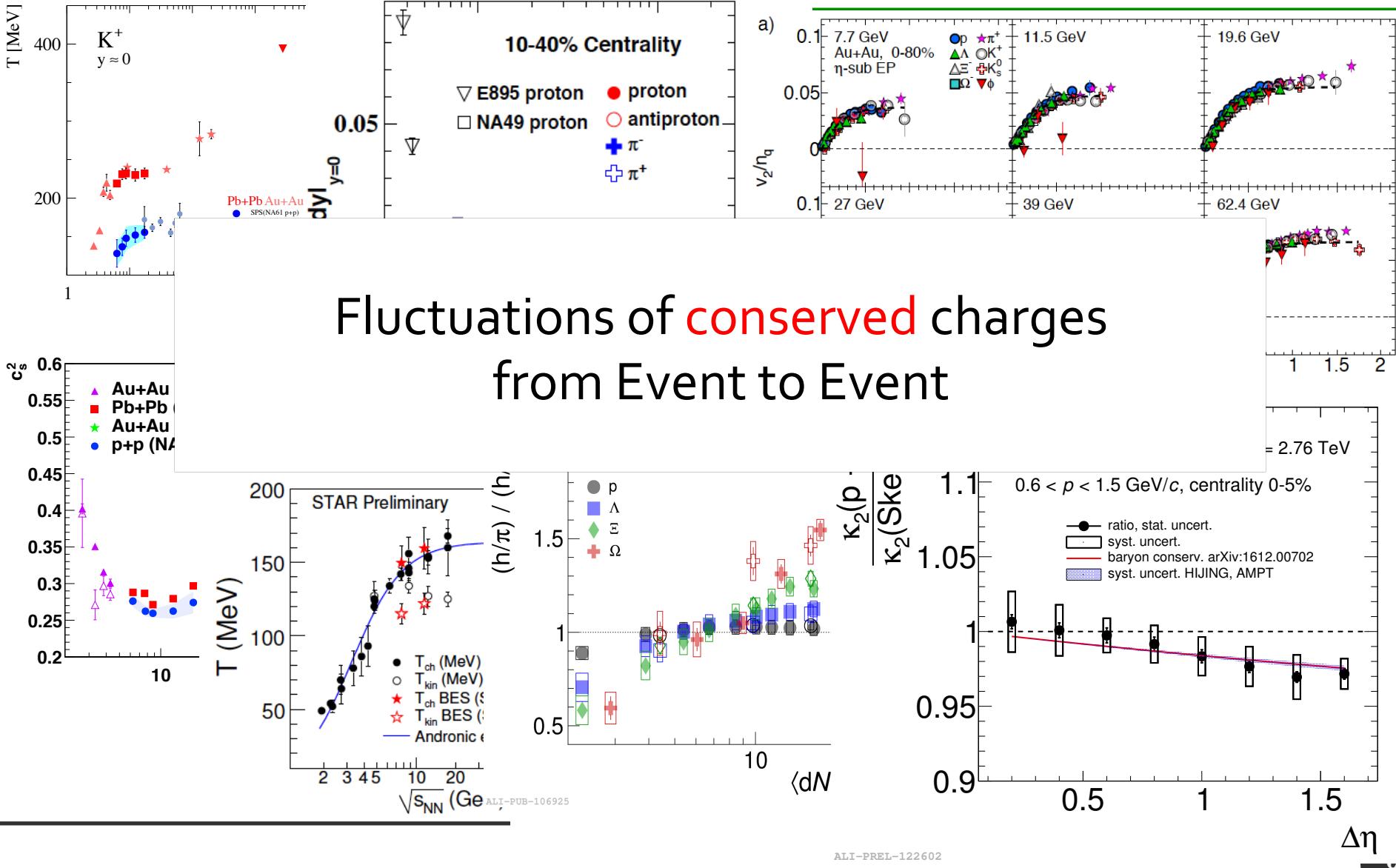
ALICE (few TeV)



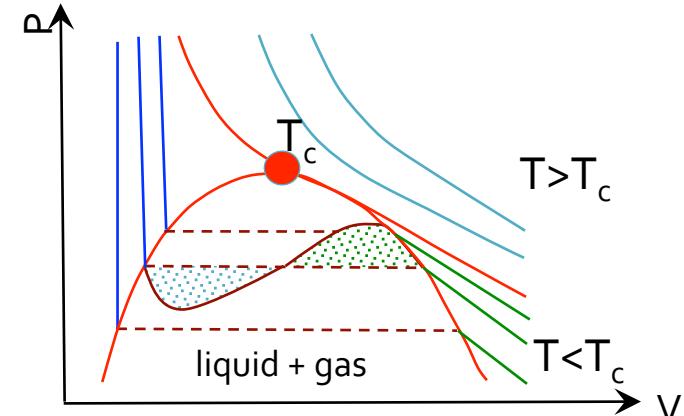
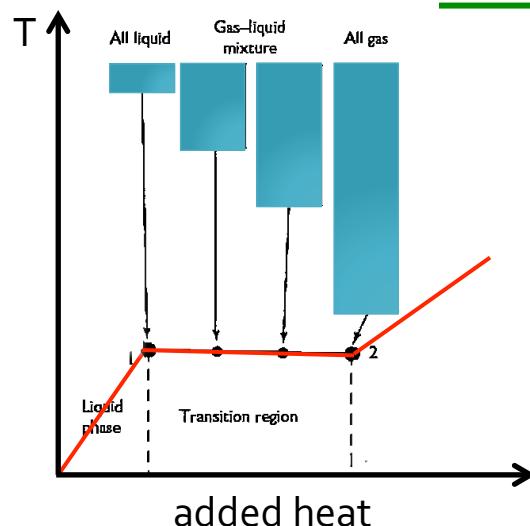
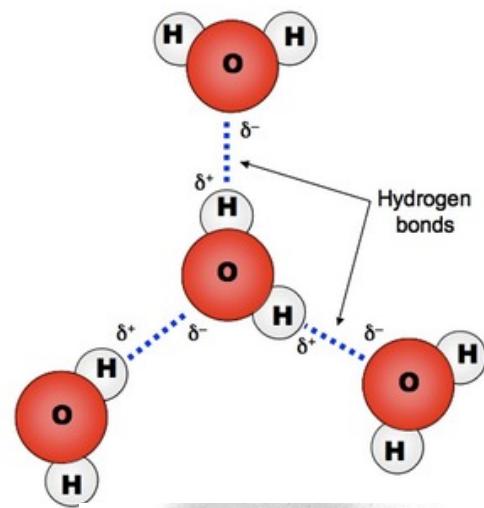
Measured signals



Exposed in this talk



Phase transitions, importance of interactions



$$(V - Nb) \left(P + \frac{N^2 a}{V^2} \right) = NT$$

$$\frac{\langle (N - \langle N \rangle)^2 \rangle}{\langle N \rangle^2} = \frac{T k_T}{V}$$

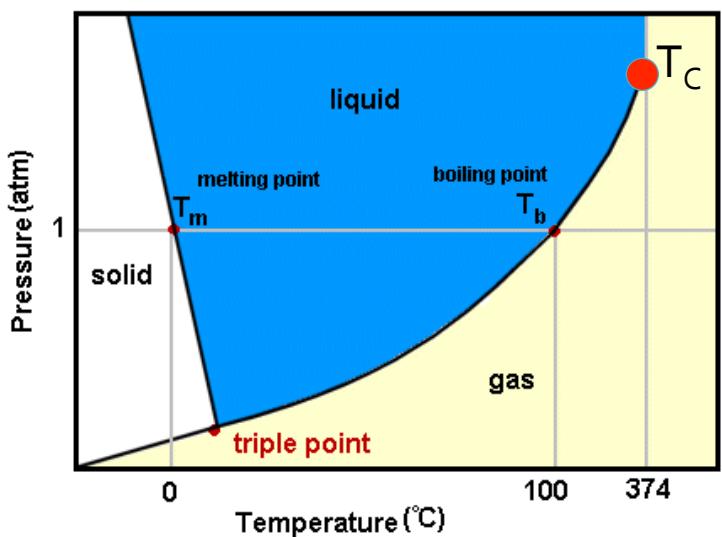
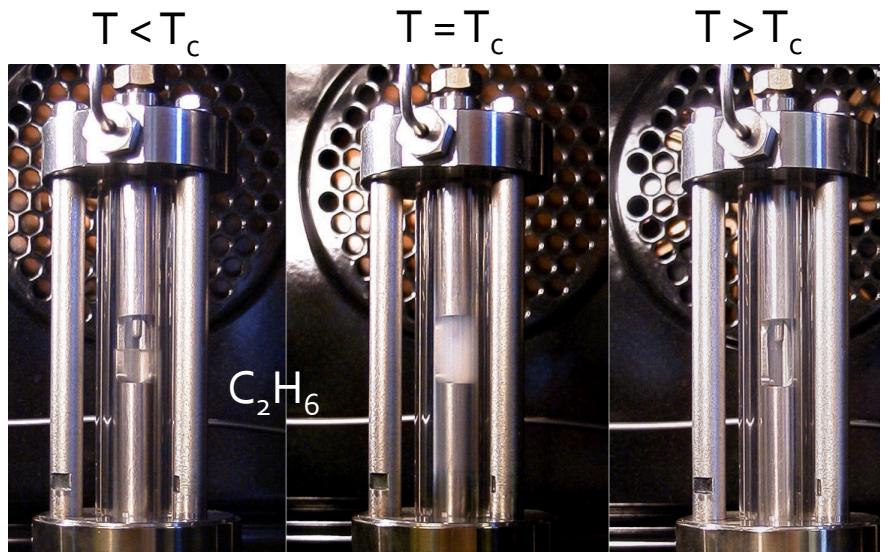
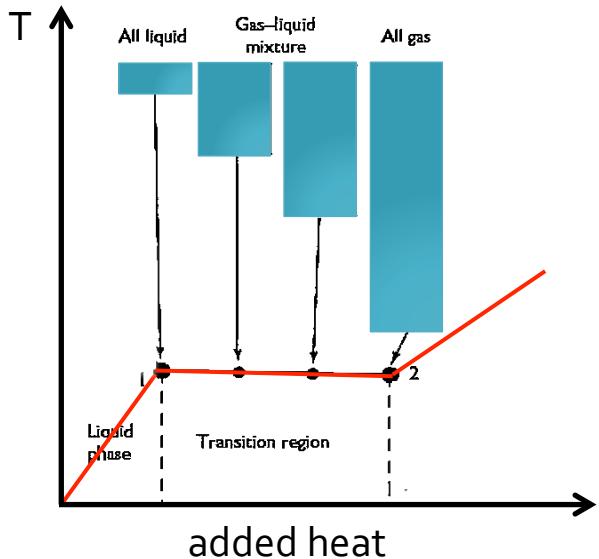
$$k_T = -\frac{1}{V \left(\frac{\partial P}{\partial V} \right)}$$

- Interactions are important for phase transitions
- Large fluctuations close to the critical point

Ideal gas: $\langle (N - \langle N \rangle)^2 \rangle \xrightarrow{PV=NT} \langle N \rangle$ (Poisson)

The Nobel Prize in Physics, 1910

Electromagnetically Interacting matter



$$\frac{\langle \rho^2 \rangle - \langle \rho \rangle^2}{\langle \rho \rangle^2} = \frac{T\chi}{V}, \quad \chi = -\frac{1}{V} \frac{\partial V}{\partial P}$$

Einstein, 1910

Rayleigh Ratio $\propto \chi$

probing phase transitions
with fluctuations

Strongly Interacting matter, ultimate temperature

1965: Hagedorn's mass spectrum

$$\rho(m) \propto e^{m/T_H}$$

partition sum for a resonance gas
in equilibrium

$$Z(T, V) \approx \exp \left[\frac{VT}{2\pi^2} \int_0^\infty m^2 K_2 \left(\frac{m}{T} \right) \rho(m) dm \right]$$

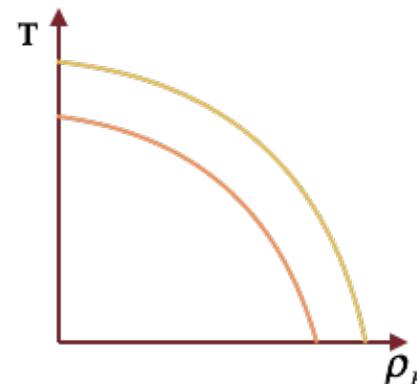
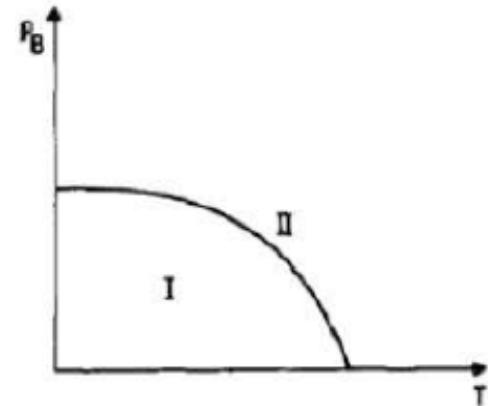
$$K_2(m/T) \sim (T/m)^{1/2} \exp(-m/T)$$

in the hadronic phase ($m/T \gg 1$)

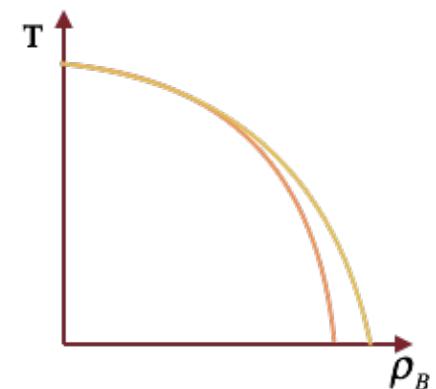
$$Z(V, T) \rightarrow \infty, \quad T \rightarrow T_H$$

1970: K. Huang and S. Weinberg;
Our present theoretical apparatus is
really inadequate to deal with much
earlier times, say when $T > 100$ MeV

1975: Cabibbo & Parisi;
exponential hadronic
spectrum and
quark liberation

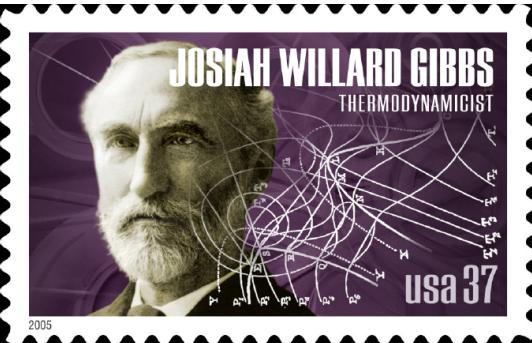


1982: G. Baym;
deconfinement and chiral
phase boundaries



1983: Lattice Monte Carlo;
deconfinement and chiral
phase boundaries coincide

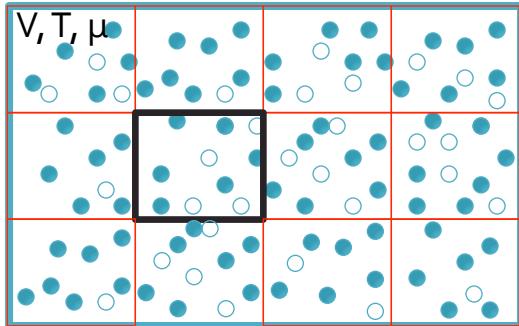
Fluctuations, Ensemble averaging



Ergodicity hypothesis: Averaging over time is equivalent to the averaging over ensembles.

Ensemble is an idealisation consisting of a large number of mental copies of a system, considered all at once, each represents a possible state that the real system!

Grand Canonical Ensemble



probability of a given state with E_j and N_j

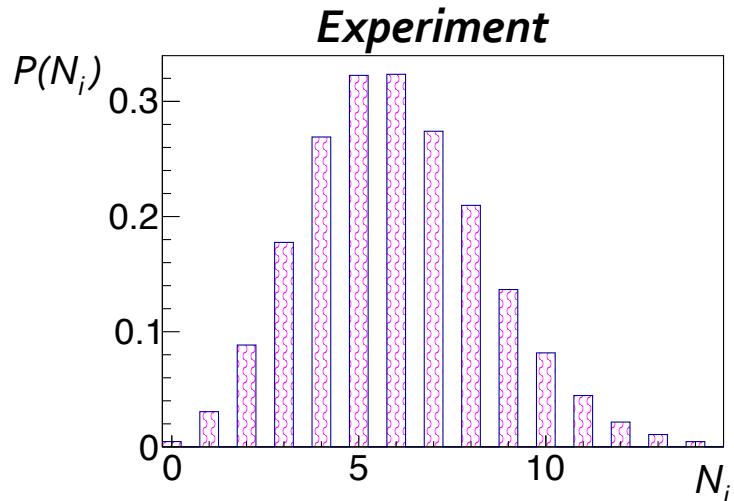
$$p_j = \frac{\exp\left[-(E_j - \mu N_j)/T\right]}{Z_{GCE}}$$

$$Z_{CGE}(T, V, \mu) = \sum_j \exp\left[-\frac{E_j - \mu N_j}{T}\right] \text{ partition function}$$

$$\langle N \rangle = \sum_j N_j p_j = T \frac{\partial \ln Z_{CGE}}{\partial \mu} \Big|_V$$

$$k_B \langle N \rangle = \langle N^2 \rangle - \langle N \rangle^2 = \sum_j N_j^2 p_j = T^2 \frac{\partial^2 \ln Z_{CGE}}{\partial \mu^2} \Big|_V$$

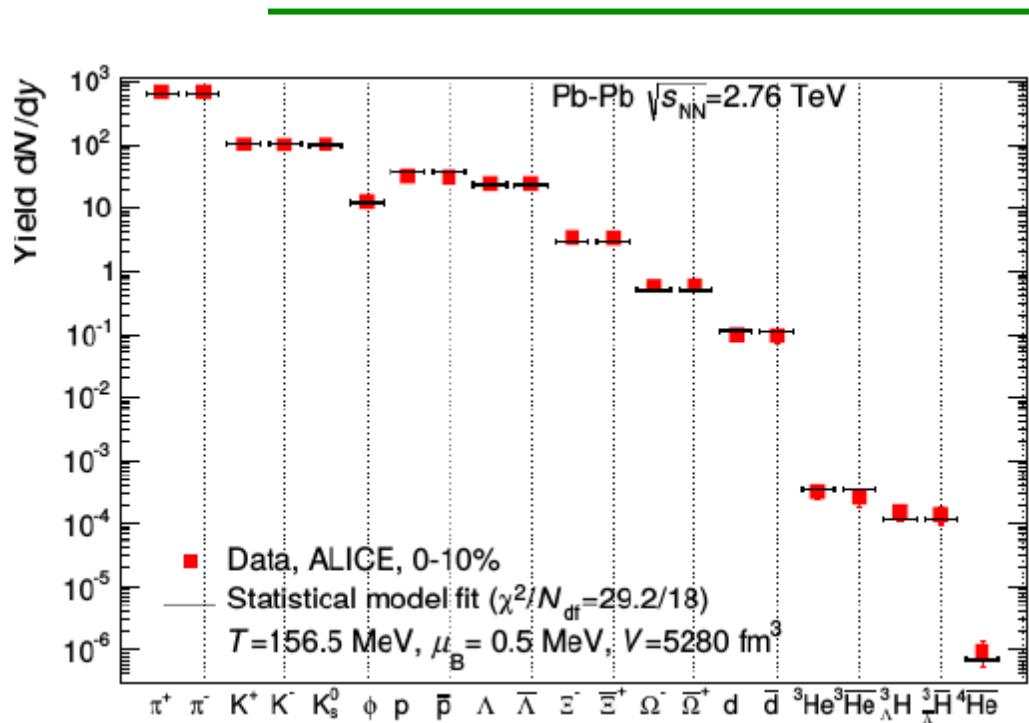
Phase boundaries from first moments



$$\langle N_i \rangle = V \frac{g_i}{2\pi^2} \int_0^\infty \frac{p^2 dp}{\exp[(E_i - \mu_i)/T] \pm 1}$$

$$\mu_i = \mu_B B_i + \mu_s S_i + \mu_I I_i$$

$$\chi^2 = \sum_{k=1}^n \frac{(\langle N_k^{\text{exp}} \rangle - \langle N_k^{\text{HRG}} \rangle)^2}{\sigma_k^2}$$

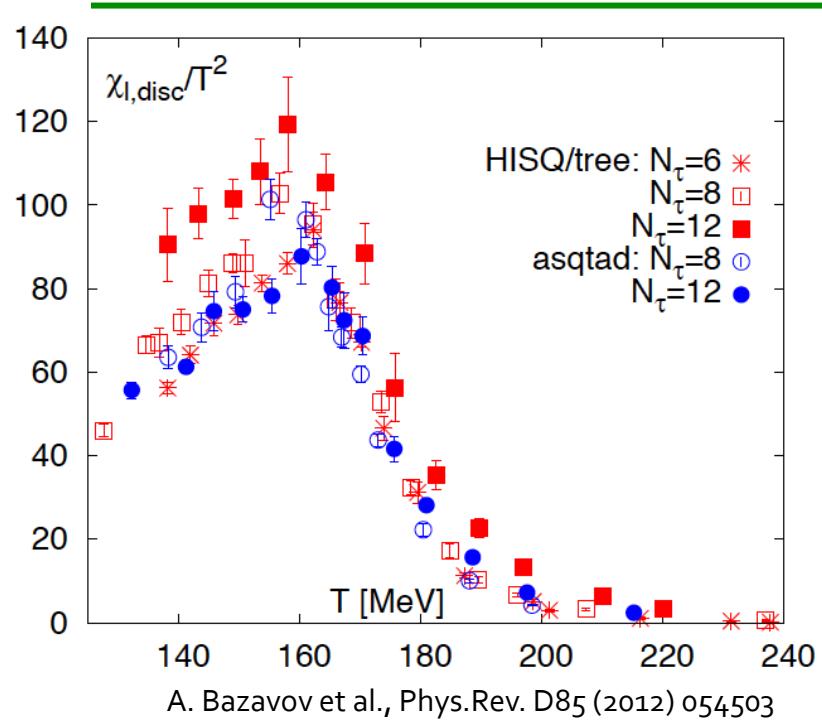
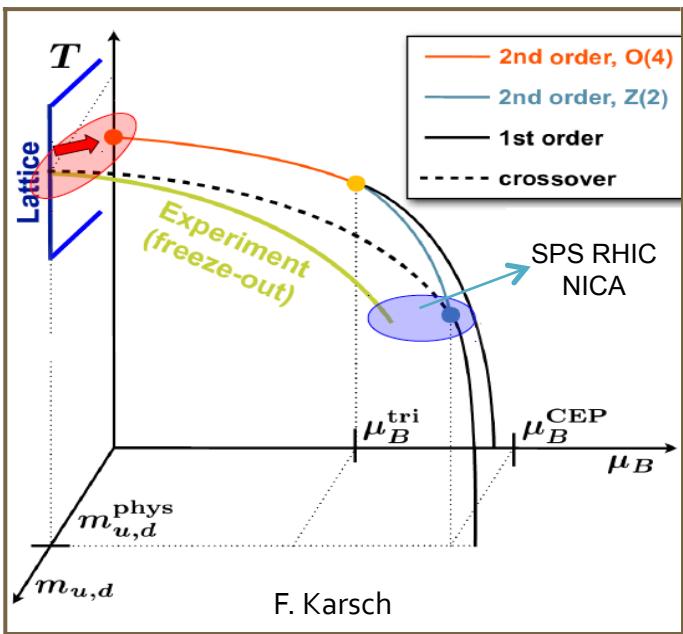


ALICE, PLB 726 (2013) 610

J. Stachel, A. Andronic, P. Braun-Munzinger and K. Redlich
J. Phys. Conf. Ser. 509 (2014) 012019

works in the energy range spanning by 3 orders of magnitude! y axis: 9 orders of magnitude!

Dynamics of phase transitions



freeze-out at the phase boundary!

$$T_c^{\text{lattice}} = 154 \pm 9 \text{ MeV}, \quad T_{\text{fo}}^{\text{ALICE}} = 156 \pm 3 \text{ MeV}$$

- *E-by-E fluctuations:*
 - To study dynamics of the phase transitions
 - To locate phase boundaries

Bridge from experiment to theory

for a thermal system in a fixed volume V
within the Grand Canonical Ensemble

$$\hat{\chi}_2^B = \frac{\langle \Delta N_B^2 \rangle - \langle \Delta N_B \rangle^2}{VT^3} = \frac{\kappa_2(\Delta N_B)}{VT^3}$$

$$\hat{\chi}_n^{N=B,S,Q} = \frac{\partial^n P/T^4}{\partial(\mu_N/T)^n} \quad \frac{P}{T^4} = \frac{1}{VT^3} \ln Z(V, T, \mu_{B,Q,S})$$

- *In experiments*
 - Volume (participants) fluctuates from E-to-E
 - Global conservation laws are important

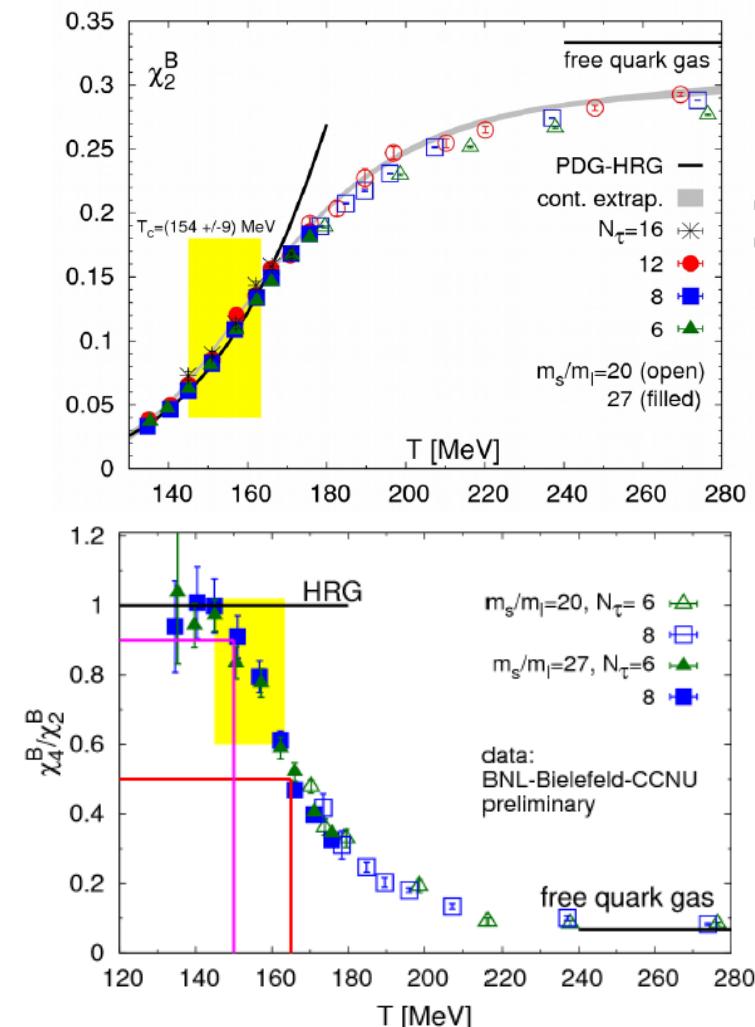
$$\hat{\chi}_n^B \neq \frac{\kappa_n(\Delta N_B)}{VT^3} \quad \frac{\kappa_4(\Delta N_B)}{\kappa_2(\Delta N_B)} \equiv \gamma_2 \sigma^2 \neq \frac{\hat{\chi}_4^B}{\hat{\chi}_2^B}$$

V. Skokov, B. Friman, and K. Redlich, Phys. Rev. C88 (2013) 034911

P. Braun-Munzinger, A. R., J. Stachel, arXiv:1612.00702, NPA 960 (2017) 114

At $s^{1/2} > 10$ GeV net-proton is a reasonable proxy for the net-baryon

M. Kitazawa, and M. Asakawa, Phys. Rev. C86 (2012) 024904



smaller than in HRG for $T > 150$ MeV

F. Karsch, QM17, arXiv:1706.01620

O. Kaczmarek, QM17, arXiv:1705.10682

Net-particle cumulants, definitions

$$\kappa_1(X) = \langle X \rangle$$

$$\kappa_2(X) = \left\langle (X - \langle X \rangle)^2 \right\rangle$$

$$\kappa_3(X) = \left\langle (X - \langle X \rangle)^3 \right\rangle$$

$$\kappa_4(X) = \left\langle (X - \langle X \rangle)^4 \right\rangle - 3\kappa_2^2(X)$$

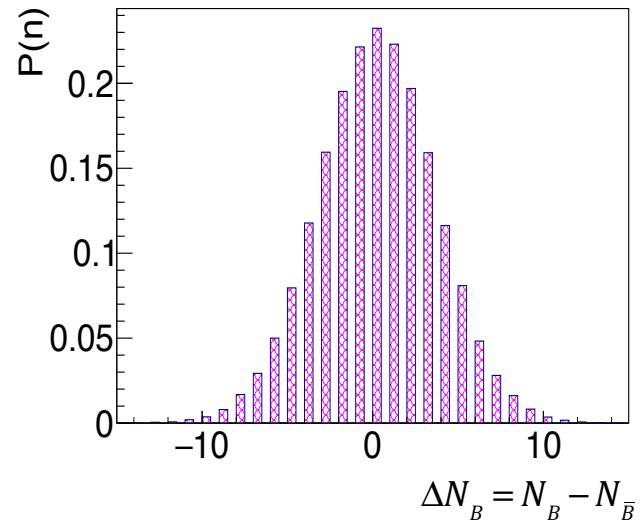
e.g., second cumulant of net-baryons

$$\kappa_2(N_B - N_{\bar{B}}) = \left\langle (N_B - N_{\bar{B}})^2 \right\rangle - \langle N_B - N_{\bar{B}} \rangle^2$$

$$\kappa_2(N_B - N_{\bar{B}}) = \kappa_2(N_B) + \kappa_2(N_{\bar{B}}) - 2(\langle N_B N_{\bar{B}} \rangle - \langle N_B \rangle \langle N_{\bar{B}} \rangle)$$

Correlation term may arise from:

1. Resonance contributions
2. Global conservation laws



Poisson limit:

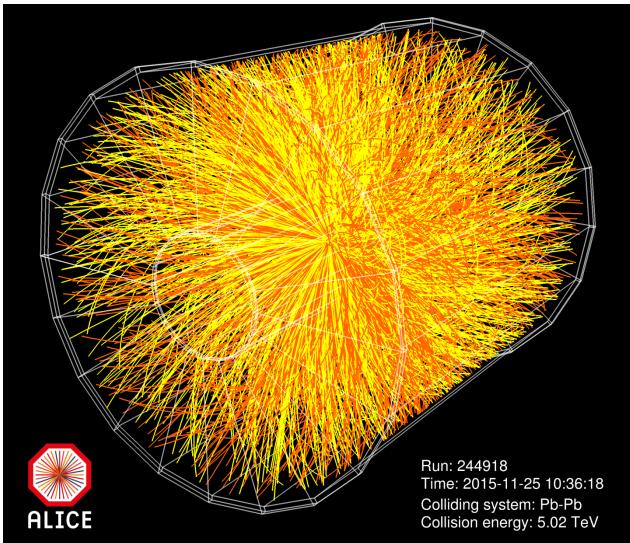
$$\kappa_2(N_B) = \langle N_B \rangle$$

$$\kappa_2(N_{\bar{B}}) = \langle N_{\bar{B}} \rangle$$

$$\kappa_2(N_{\bar{B}} - N_B) \xrightarrow{\langle N_B N_{\bar{B}} \rangle = \langle N_B \rangle \langle N_{\bar{B}} \rangle} \langle N_B \rangle + \langle N_{\bar{B}} \rangle$$

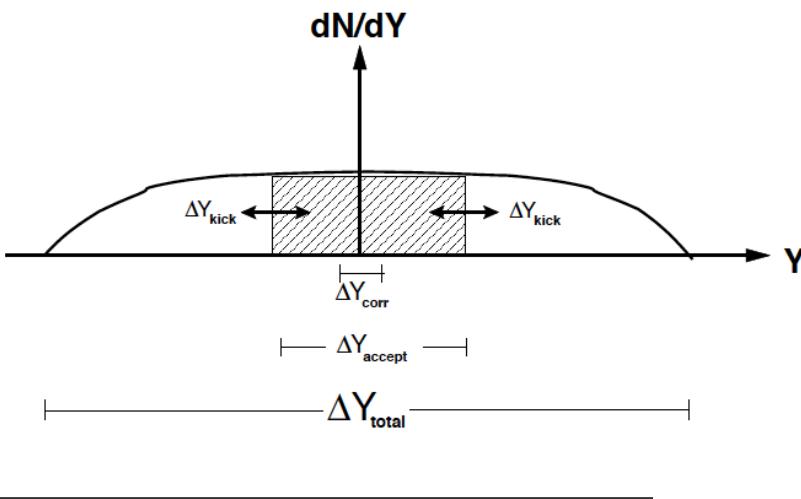
Skellam

Experimental trick: cuts on y and/or p_t



Large $\frac{\Delta y_{accept}}{\Delta y_{total}}$: conservations dominate

Small $\frac{\Delta y_{accept}}{\Delta y_{total}}$: dynamical fluctuations may disappear

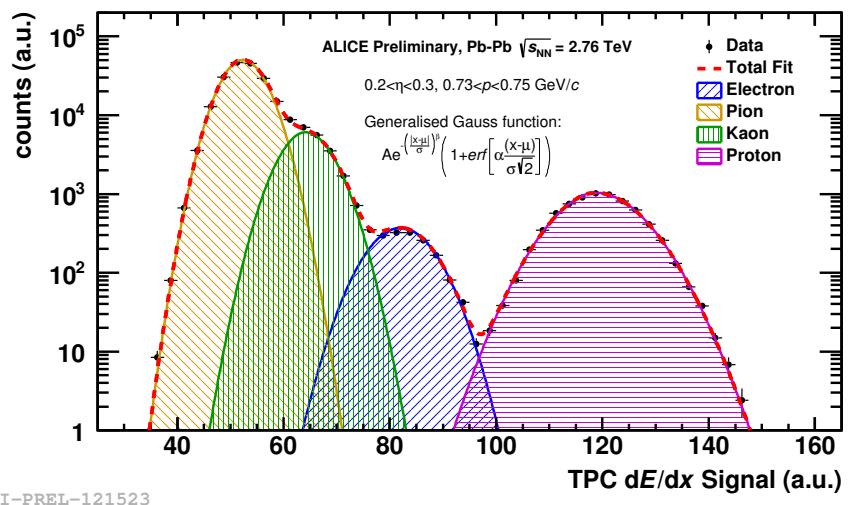
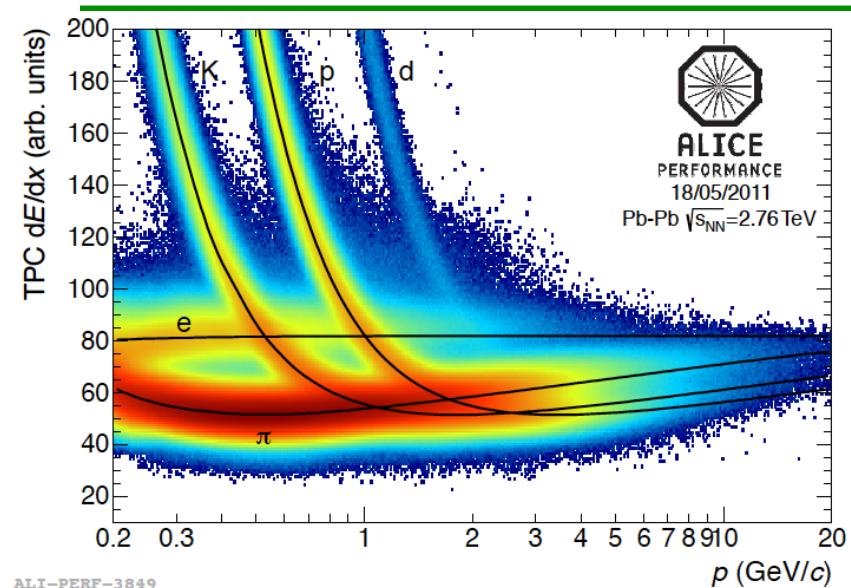
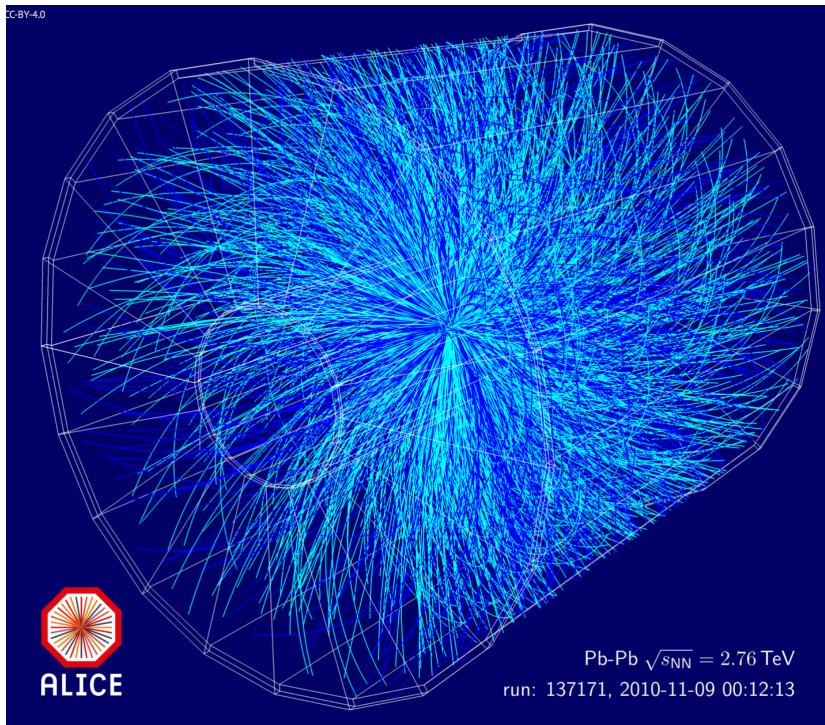


- Our approach:
 - Estimation of non-dynamical fluctuations
 - Selection of optimum acceptance
 - Correction for conservation laws

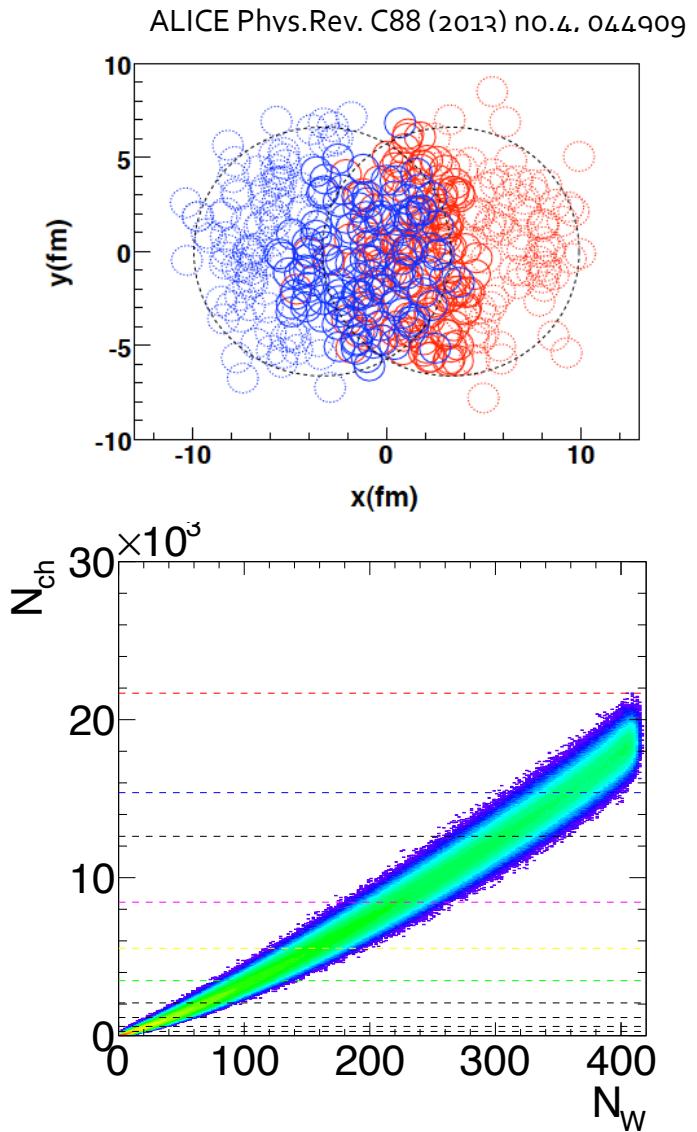
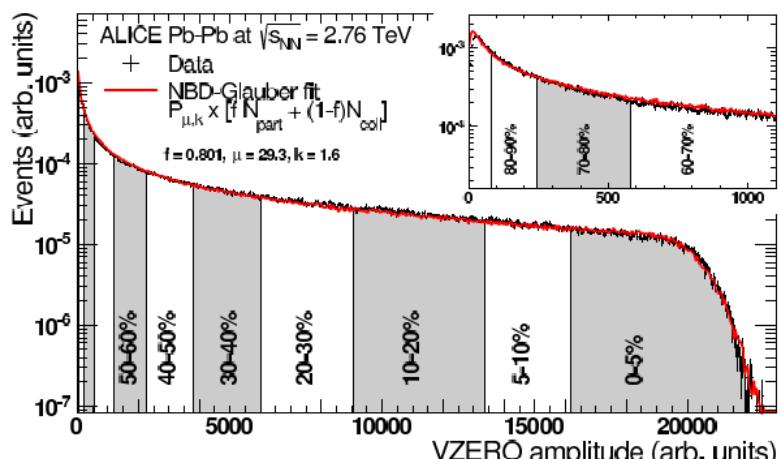
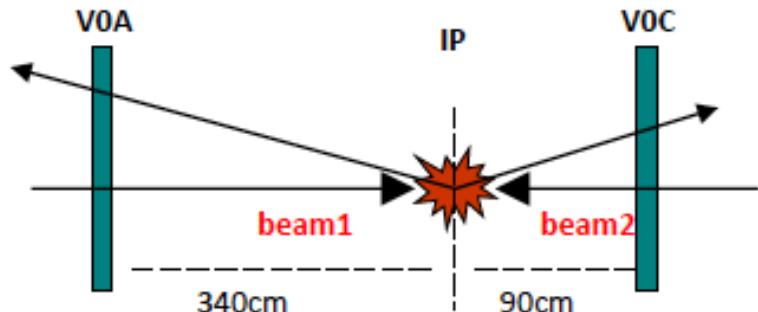
P. Braun-Munzinger, A. R., J. Stachel, in preparation

A. R. SQM 2017

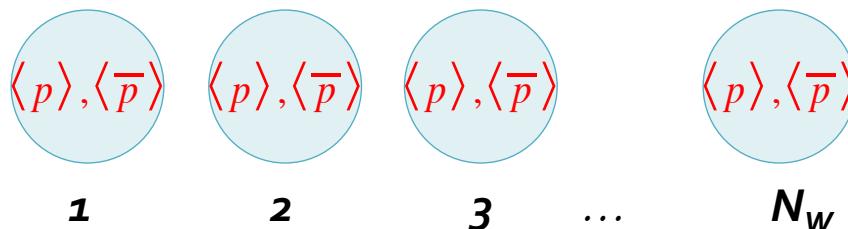
Particle Identification, ALICE example



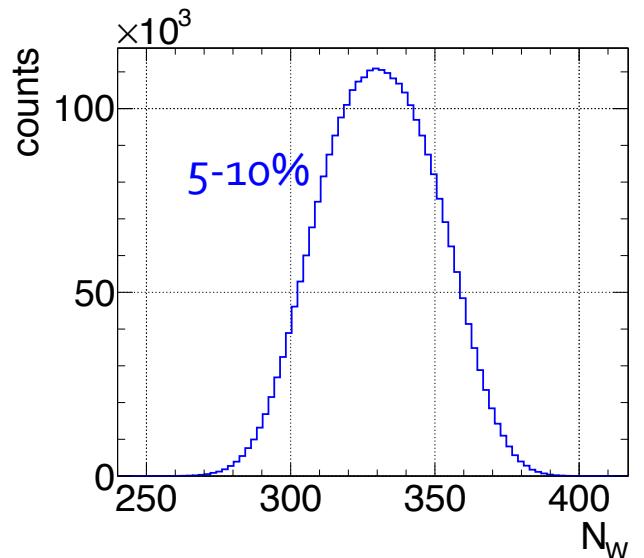
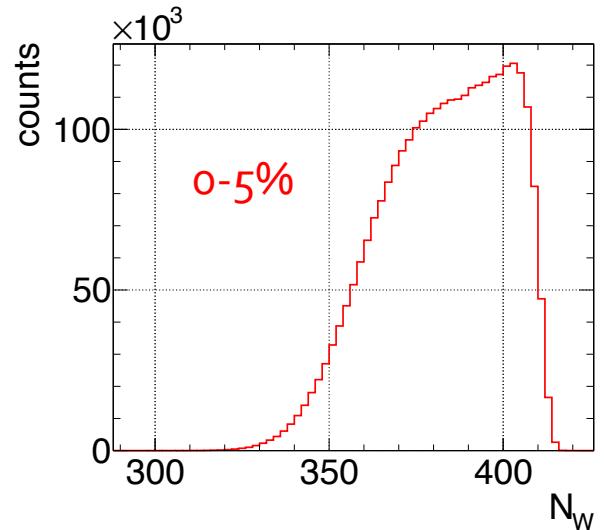
Centrality determination



Non-dynamical fluctuations

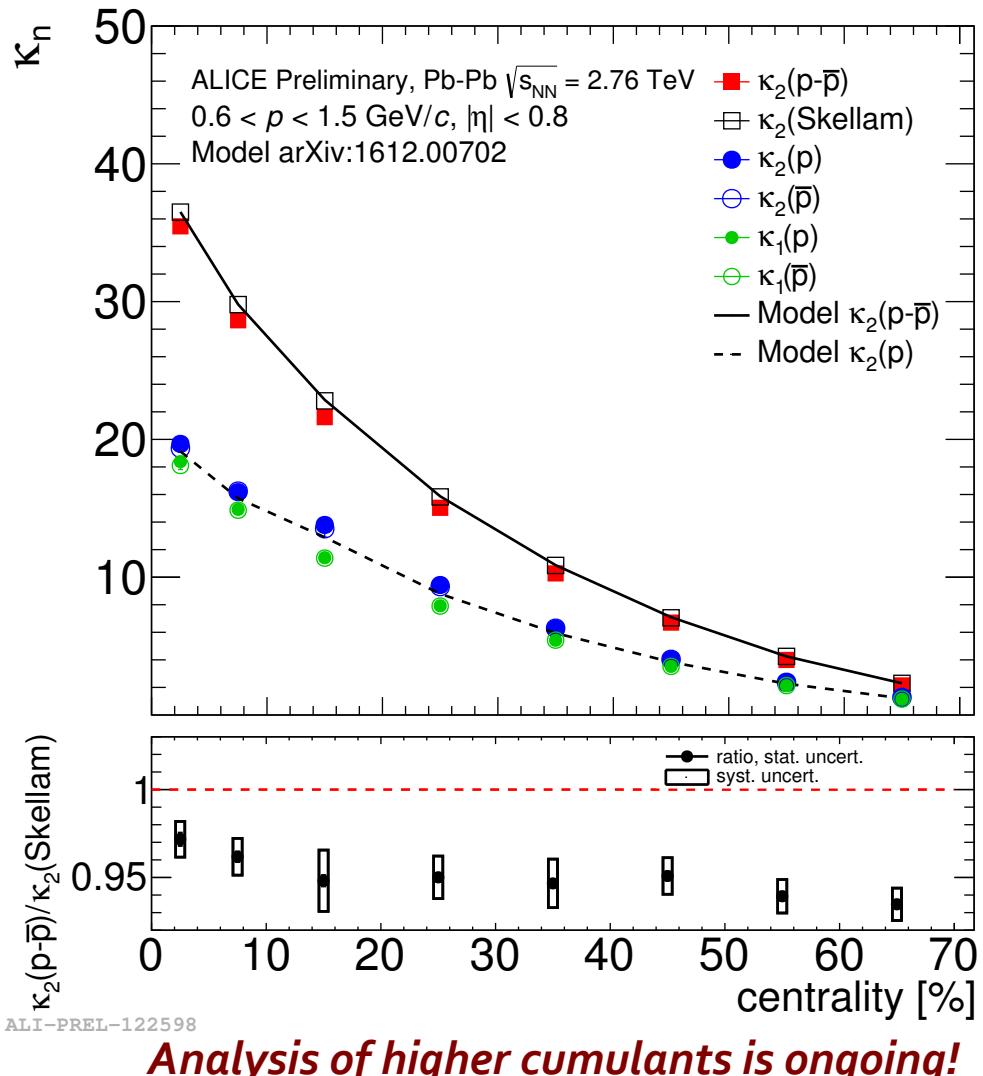


- ◎ N_w fluctuates with MC Glauber initial conditions
- ◎ Particles are produced from each source
- ◎ Inputs:
 - ◎ Mean proton multiplicities $\langle p \rangle, \langle \bar{p} \rangle$
 - ◎ Centrality selection like in experimental data



P. Braun-Munzinger, A. R., J. Stachel, arXiv:1612.00702, NPA 960 (2017) 114

Results from ALICE



$$\kappa_2(n_B - n_{\bar{B}}) = \kappa_2(n_B) + \kappa_2(n_{\bar{B}}) - 2(\langle n_B n_{\bar{B}} \rangle - \langle n_B \rangle \langle n_{\bar{B}} \rangle)$$

Input to the Model

$$\kappa_1(p), \kappa_1(\bar{p})$$

centrality selection procedure

Predictions

— $\kappa_2(p-\bar{p})$
--- $\kappa_2(p)$

$$\kappa_2(N_B - N_{\bar{B}}) = \langle N_w \rangle \kappa_2(n_B - n_{\bar{B}}) + \langle n_B - n_{\bar{B}} \rangle^2 \kappa_2(N_w)$$

participants (red arrow)
vanishes at LHC (green arrow)
from single participant (red arrow)

**Second cumulants of net-particles
at LHC are not affected by
participant fluctuations
easy control of systematics**

Results from ALICE

Contribution from global baryon number conservation

$$\frac{\kappa_2(p - \bar{p})}{\kappa_2(\text{Skellam})} = 1 - \alpha \quad \alpha = \frac{\langle p \rangle^{\text{measured}}}{\langle B \rangle^{4\pi}}$$

P. Braun-Munzinger, A. R., J. Stachel,
arXiv:1612.00702, NPA 960 (2017) 114

Inputs for $\langle B \rangle^{\text{acc}}$ from:

Phys. Lett. B 747, 292 (2015)

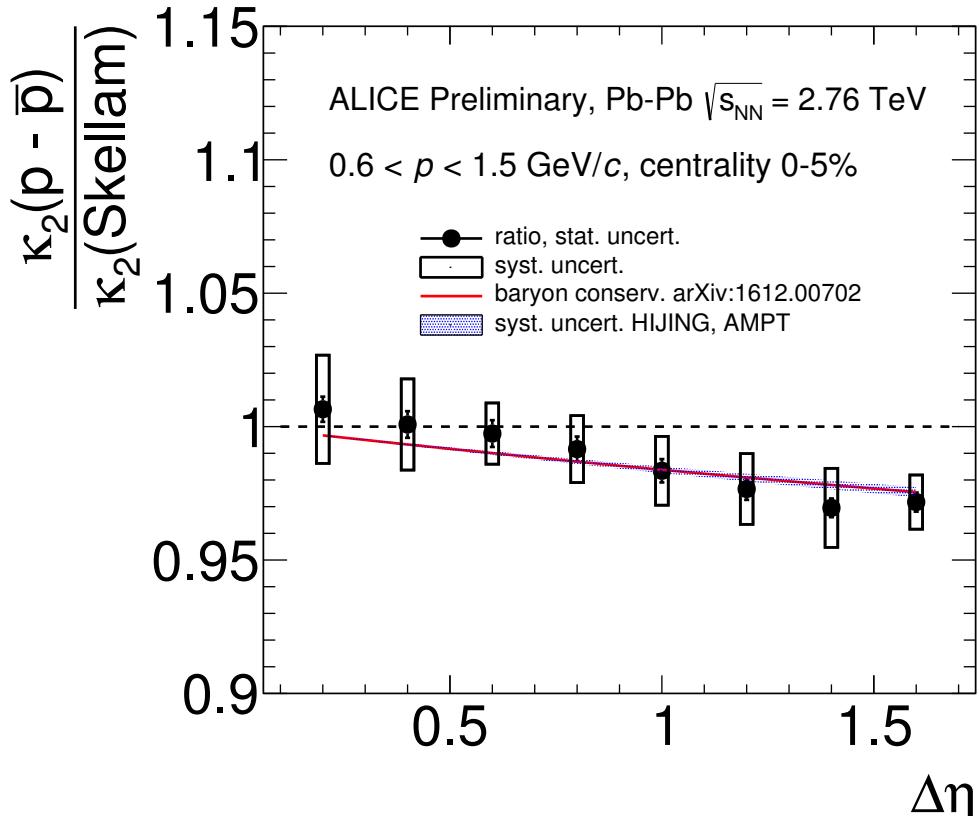
P. Braun-Munzinger, A. Kalweit, K. Redlich, J. Stachel

extrapolation from $\langle B \rangle^{\text{acc}}$ to $\langle B \rangle^{4\pi}$

using HIJING and AMPT models

A. R., QM2017, arXiv:1704.05329

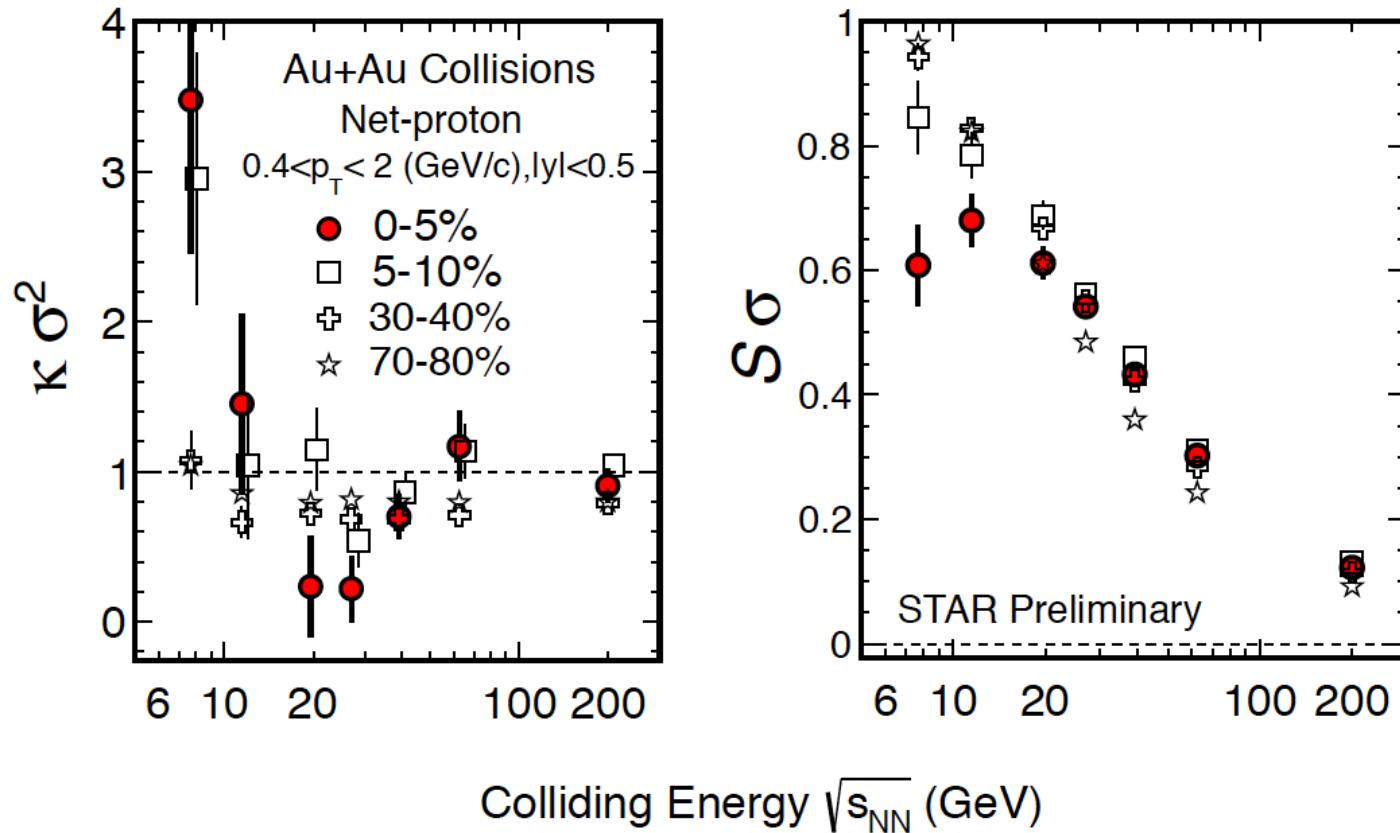
A. R., CPOD 2016



The deviation from Skellam is due to the global baryon number conservation.

Analysis of higher cumulants is ongoing!

Results from STAR



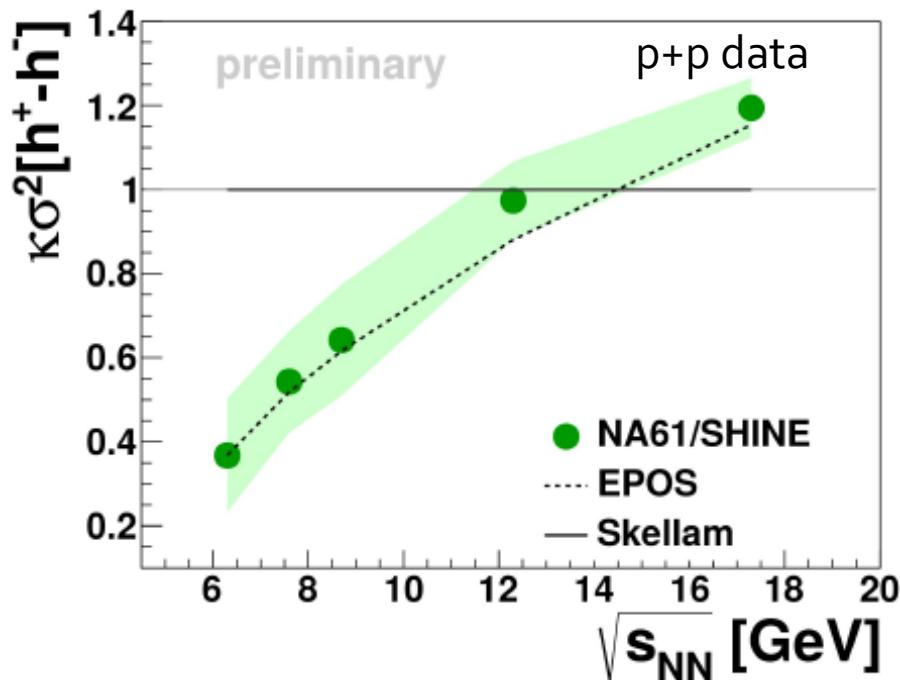
- Close to unity for peripheral collisions
- Below 39 GeV hints for a non-monotonic behavior
- ***More statistics and precise control of systematics are needed to explore this region***

Drop at 7.7 GeV for central events

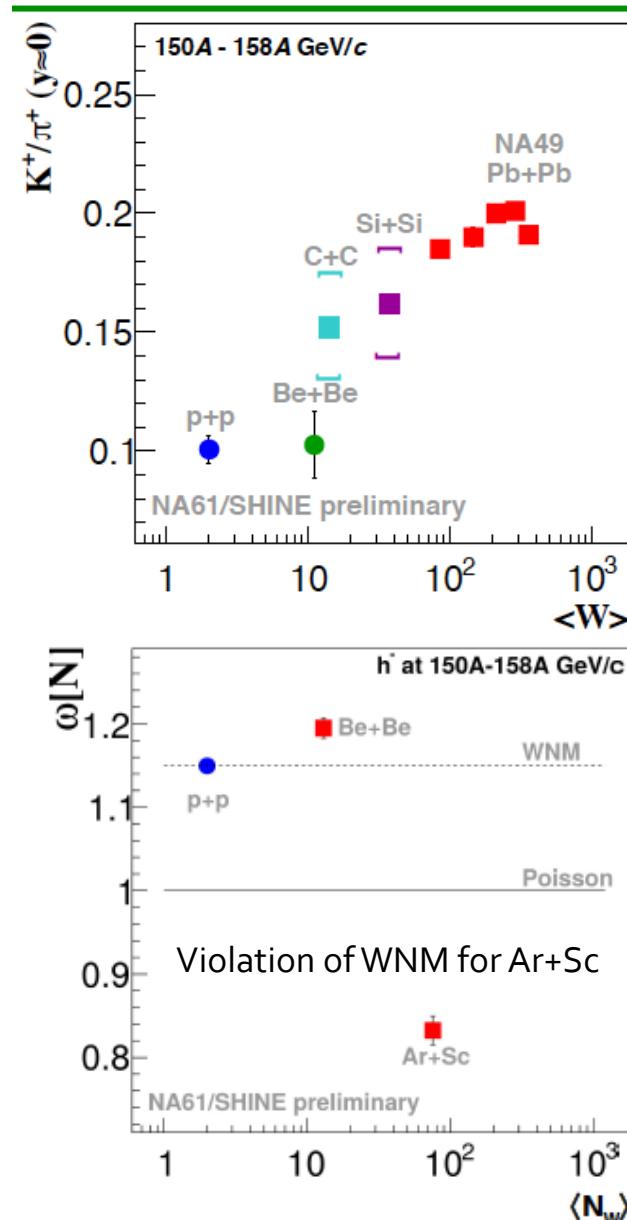
X. Luo, PoS CPOD2014, 019 (2015)
STAR: PRL 112, 032302 (2014)

NOTE: Only statistical uncertainties are presented!

Results from NA61/SHINE/NA49

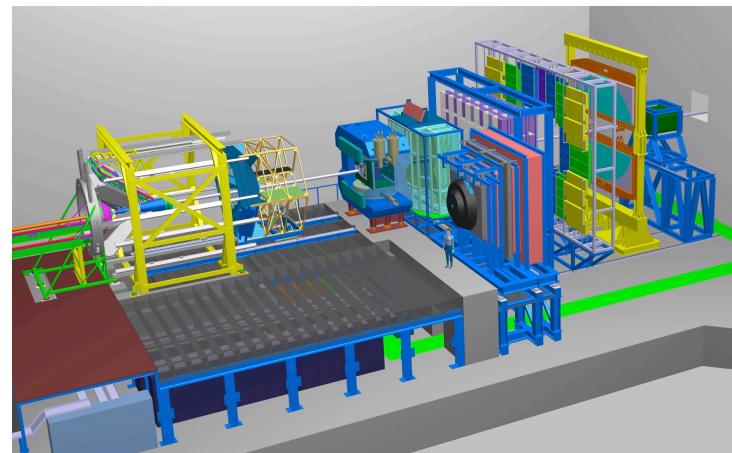
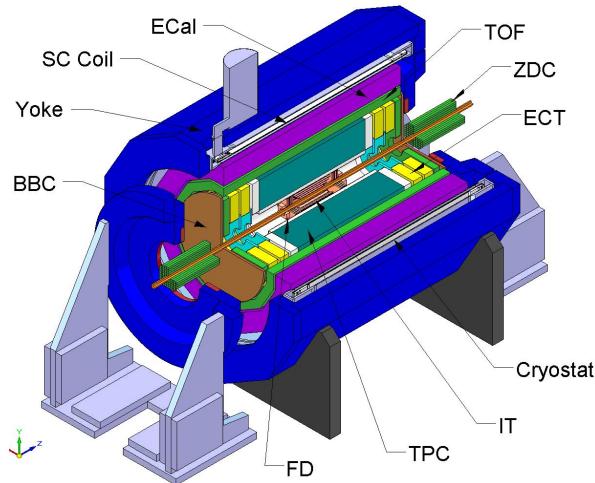


- reproduced by EPOS
- Skellam is not a proper baseline

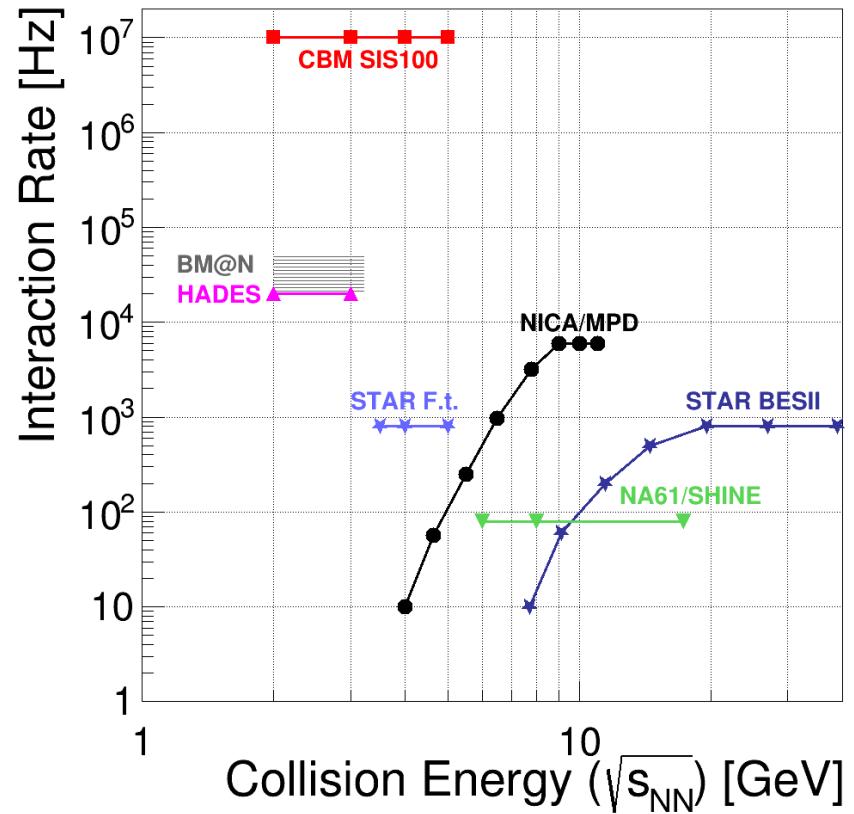


Near Future Experiments

MPD at NICA (collider mode)



CBM at FAIR (fixed target)



V. Kekelidze, QM2017

P. Senger, QM2017

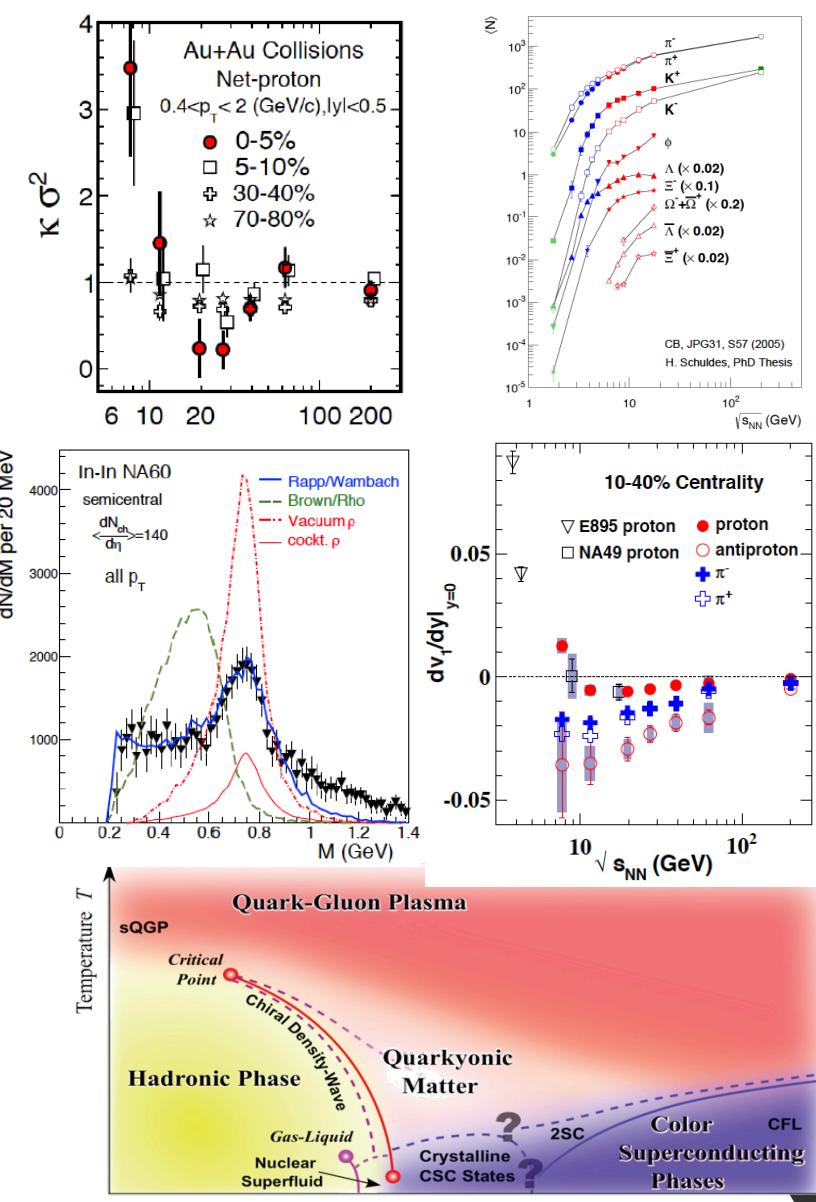
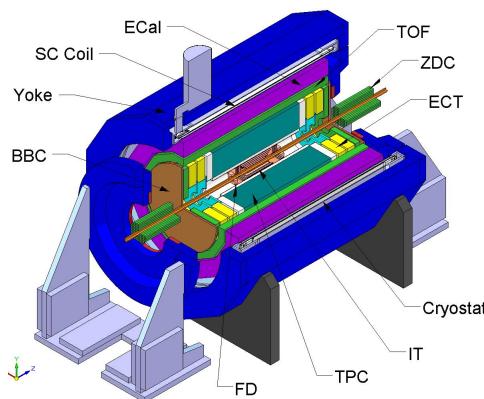
Summary

- The measured second cumulants of net-protons at ALICE are, after accounting for baryon number conservation, in agreement with the corresponding second cumulants of the Skellam distribution.
 - LQCD predicts a Skellam behavior for κ_2 of net-baryons at 150 MeV.
- Net-proton measurements from STAR hints for a non-monotonic behavior for energies below 39 GeV. More statistics and control of systematics are needed.
- NA61 data shows violation of the WNM model for Ar+Sc data
- *The analysis of higher cumulants are ongoing in ALICE, which is extremely important for understanding the nature of transition at vanishing μ_B*

Outlook

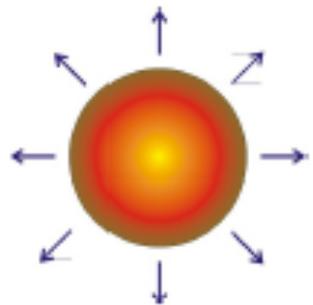
- **No clear signals for critical point**
- **No direct evidence for chiral symmetry restoration**
- **Missing hadron yields and spectra in the NICA energy range**
- **Additional phases at lower baryon chemical potential?**

All these and other unresolved issues can and should be explored at the upcoming MPD@NICA



Probing the equation of state

spherical (radial)

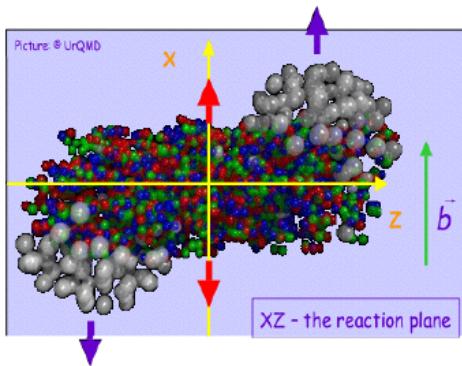


probes EoS

$$\frac{1}{m_T} \frac{d^2n}{dm_T dy} = \alpha e^{-\frac{m_T}{T}}$$

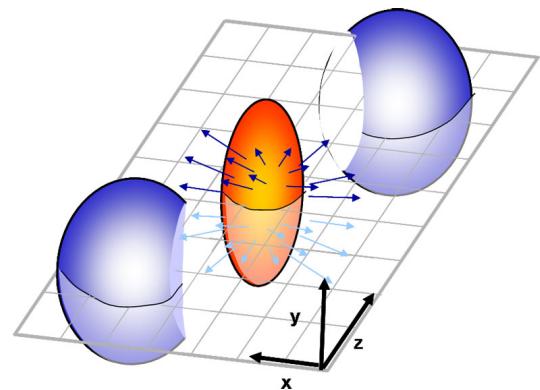
$$T = T_F + m \langle \beta_T \rangle^2, p_T < 2 GeV$$

directed



Spectators deflected from
dense reaction zone
probes EoS
sensitive to pressure

elliptic

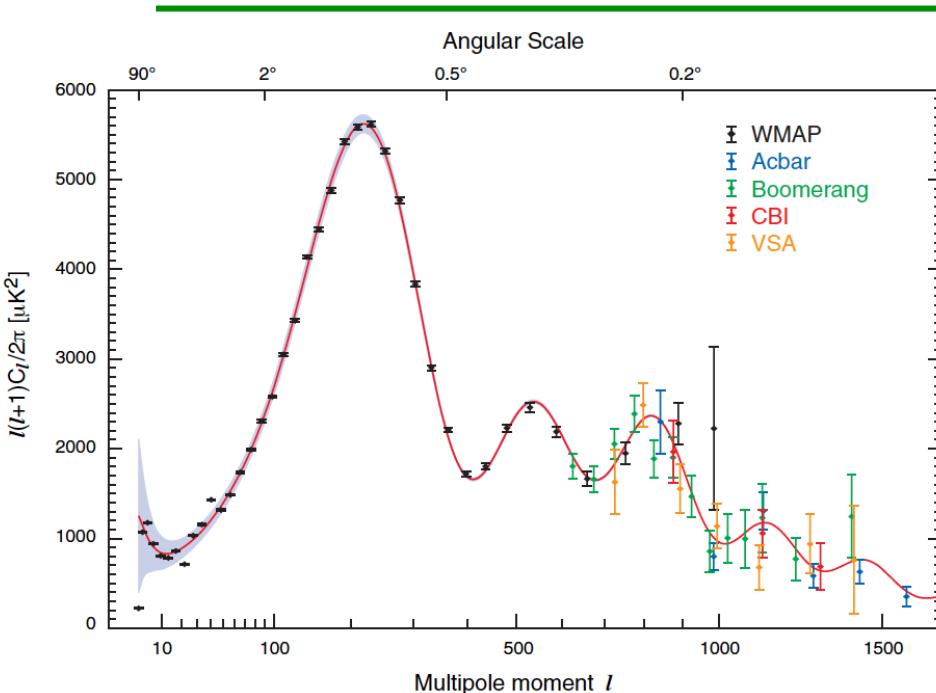
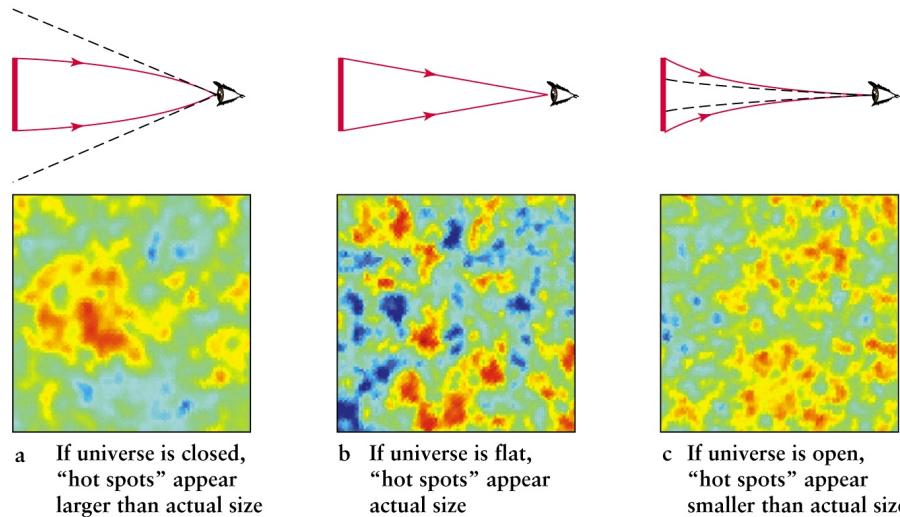


Asymmetry out vs. in-plane
sensitive to EoS
measure of perfect fluid

$$v_n = \langle \cos(n(\phi - \psi_{RP})) \rangle$$

$$E \frac{d^3N}{d^3\vec{p}} = \frac{1}{2\pi} \frac{d^2N}{p_T dp_T dy} \left[1 + 2v_1 \cos(\phi - \psi_{RP}) + 2v_2 \cos(2(\phi - \psi_{RP})) + \dots \right]$$

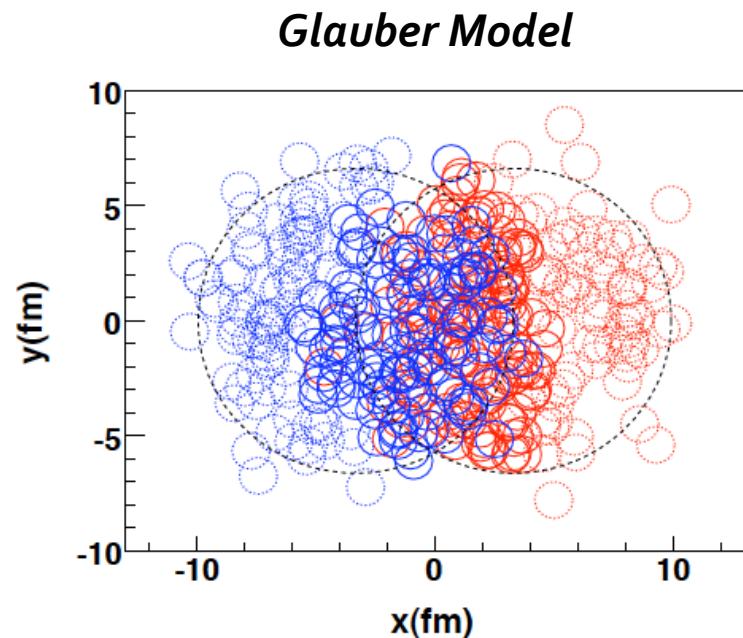
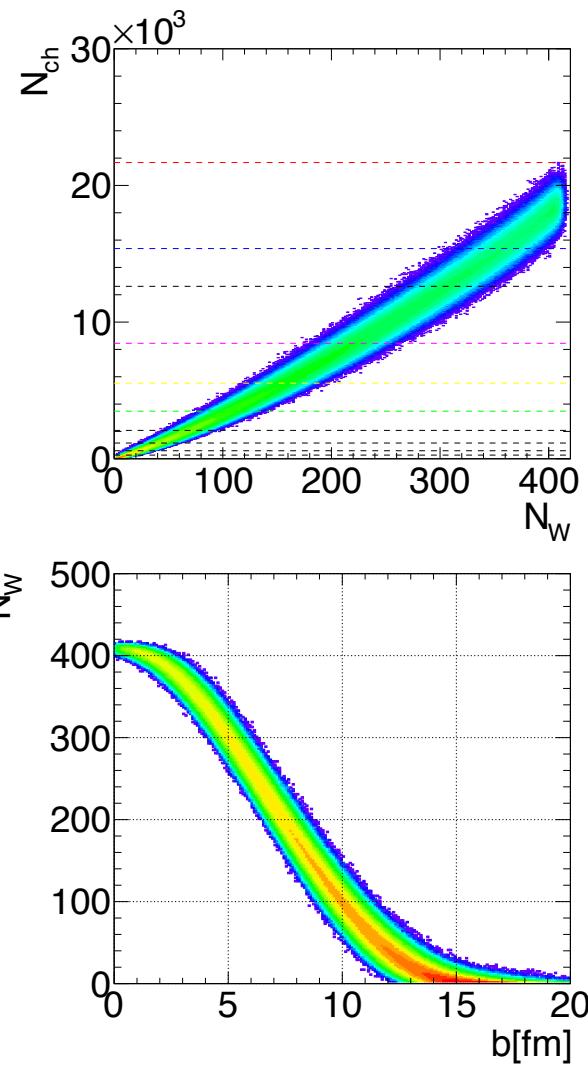
Fluctuations in the Early Universe



Age of the Universe: 13.77 billion years
The Universe if flat within 0.4 %
Ordinary matter ~ 4.6 %
Dark matter ~ 24%
Dark energy ~ 71.4 %
...

Non-dynamical contributions

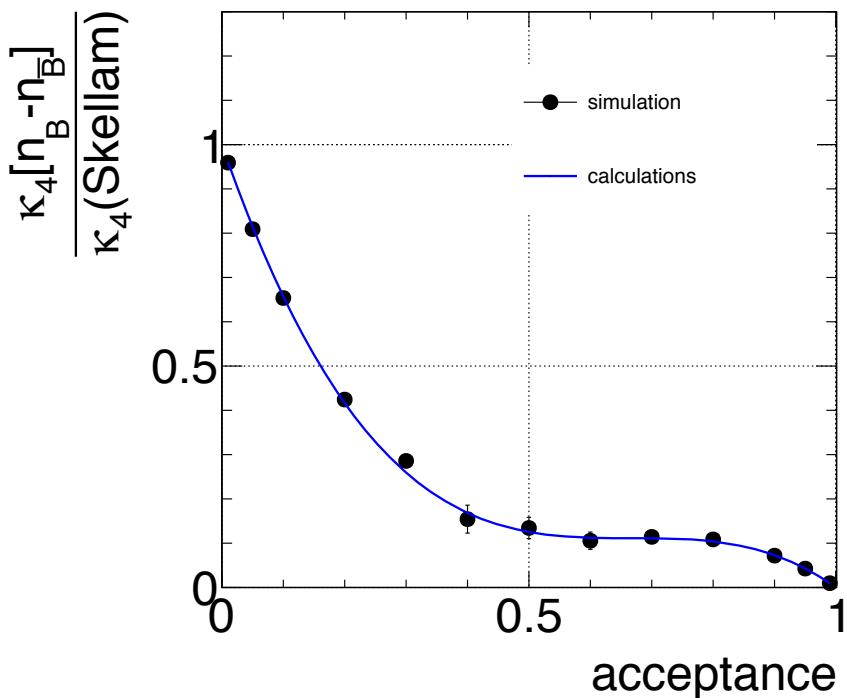
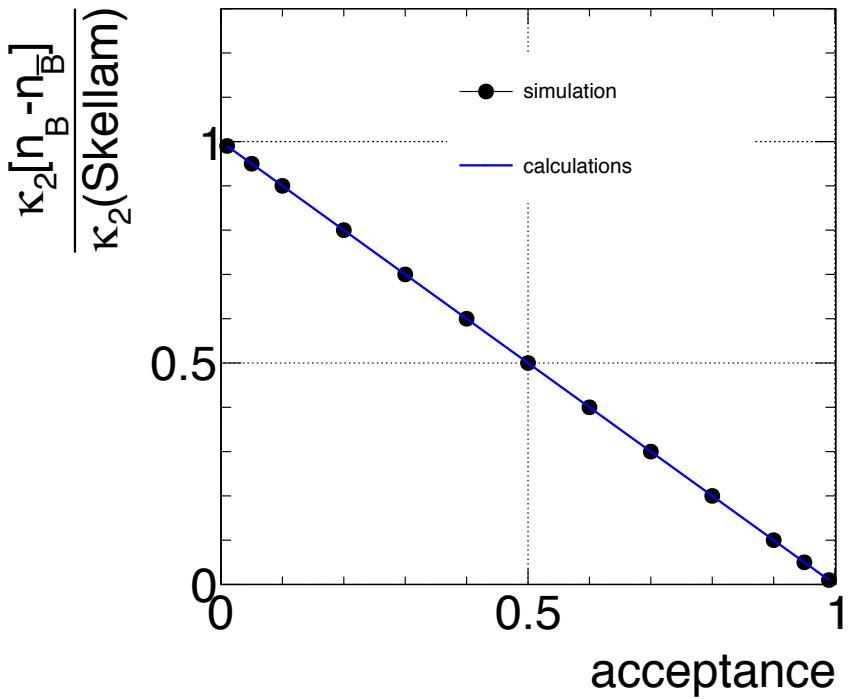
Experimental approaches:



- Each approach gives:
 - Similar $\langle N_w \rangle$
 - Very different $\langle N_w^n \rangle$

For higher moments centrality selection is crucial!

Acceptance is crucial

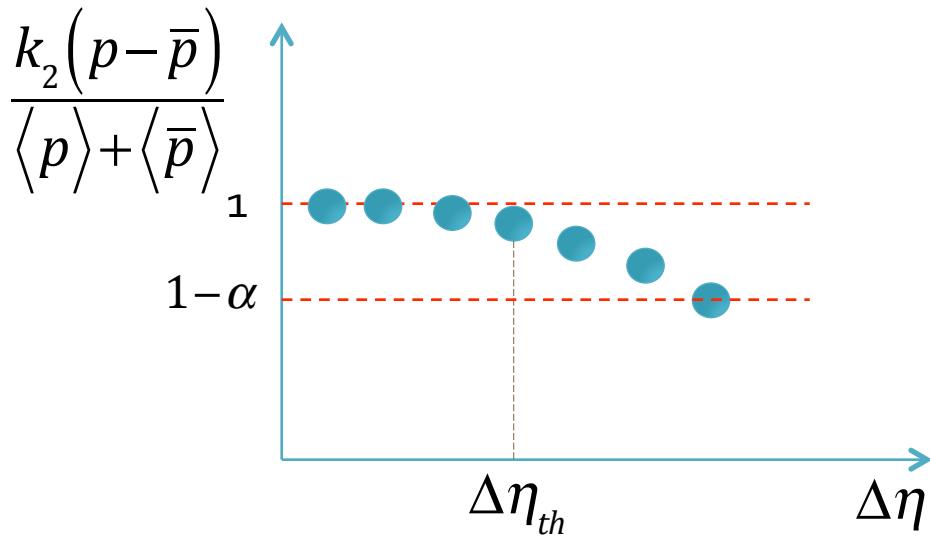


- Model assumption: full correlation in 4 pi (baryon number conservation)
- Approach to independent Poisson (Skellam) for a small acceptance
- Approach to zero for full acceptance
- Acceptance is more crucial for the 4th cumulant
- $\kappa_2/\text{Skellam} \rightarrow 1$ -acceptance

$$\kappa_2(n_B - n_{\bar{B}}) = \kappa_2(n_B) + \kappa_2(n_{\bar{B}}) - 2(\langle n_B n_{\bar{B}} \rangle - \langle n_B \rangle \langle n_{\bar{B}} \rangle)$$

P. Braun-Munzinger, A. R., J. Stachel, in preparation

Baryon number conservation



$$\frac{k_2(p - \bar{p})}{\langle p \rangle + \langle \bar{p} \rangle} = 1 - \alpha$$

$$\alpha = \frac{\langle n_p^{acc} \rangle}{\langle N_B^{4\pi} \rangle}$$

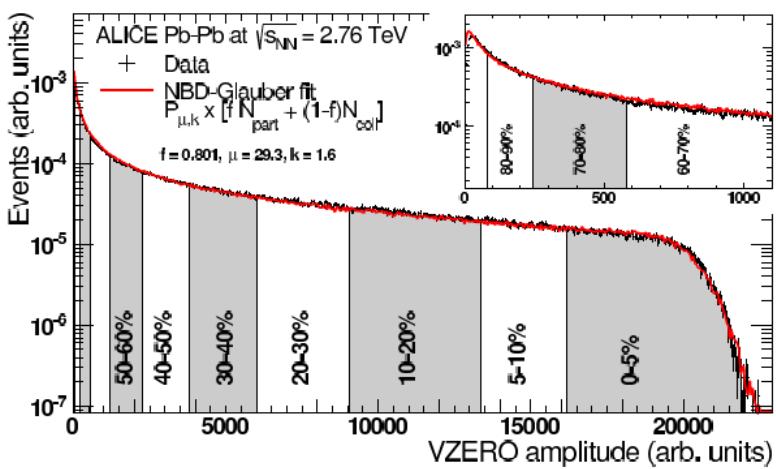
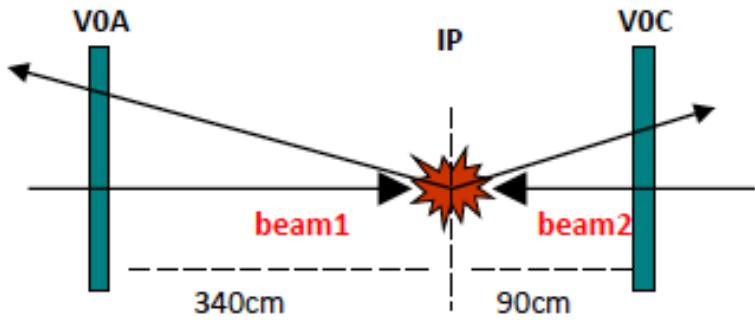
A. R. talk at CPOD 2016

Proposed comparison procedure:

- Eliminate volume dependence
- Perform analysis for $\Delta\eta > \Delta\eta_{th}$
- Calculate acceptance factors based on experimental data $\alpha(\Delta\eta) = \frac{p^{acc}}{B^{4\pi}}$
- Correct the experimental data
- Compare to LQCD

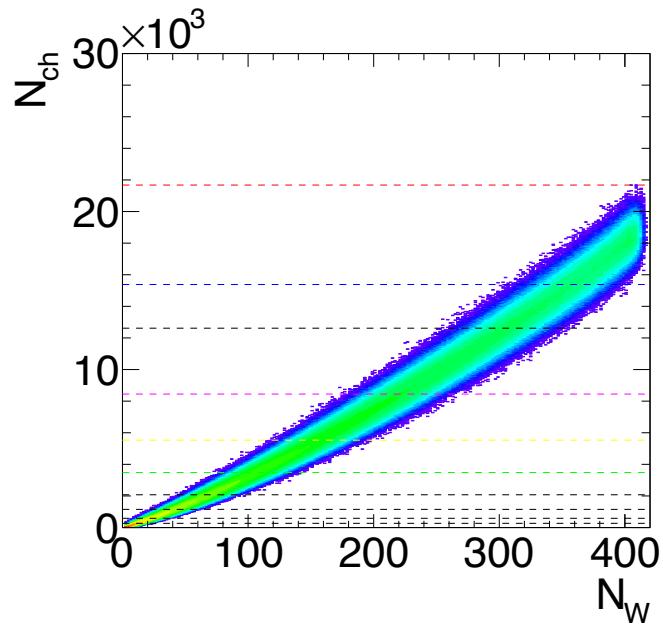
Centrality determination

ALICE Phys. Rev. C88 (2013) no.4, 044909

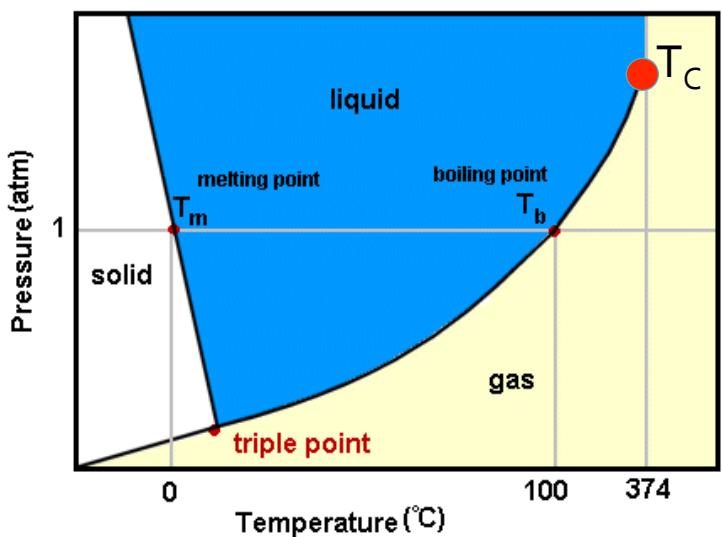
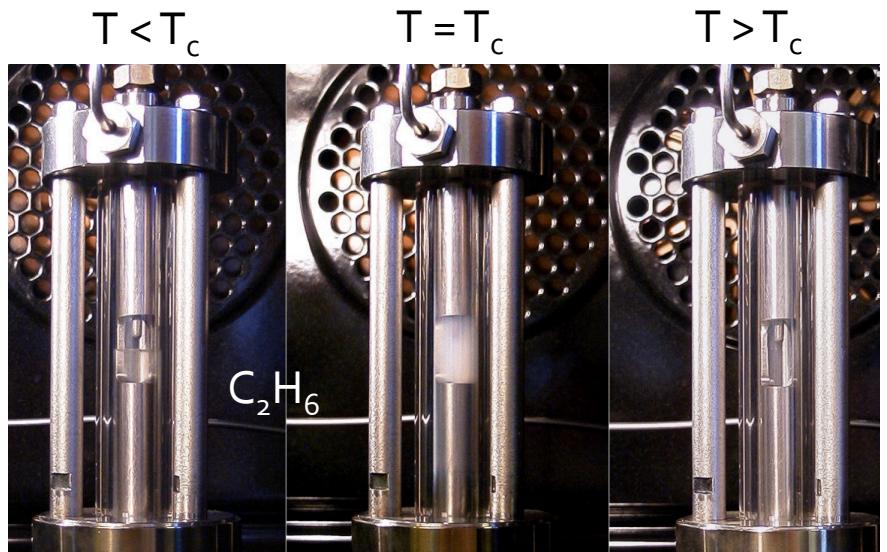
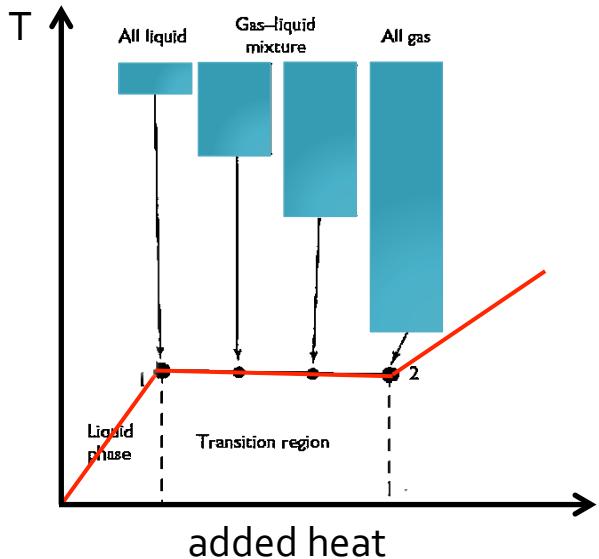


$$P_{\mu,k}(n) = \frac{\Gamma(n+k)}{\Gamma(n+1)\Gamma(k)} \frac{\left(\frac{\mu}{k}\right)^n}{\left(\frac{\mu}{k} + 1\right)^{n+k}}$$

$$N = fN_W + (1-f)N_{\text{coll}}$$



Electromagnetically Interacting matter



$$\frac{\langle \rho^2 \rangle - \langle \rho \rangle^2}{\langle \rho \rangle^2} = \frac{T\chi}{V}, \quad \chi = -\frac{1}{V} \frac{\partial V}{\partial P}$$

Einstein, 1910

Rayleigh Ratio $\propto \chi$

probing phase transitions
with fluctuations