

ADDITIONAL VIEW IN THE MOSS TECHNIQUE BY EMPLOYING SOME SIMPLE STATISTICS

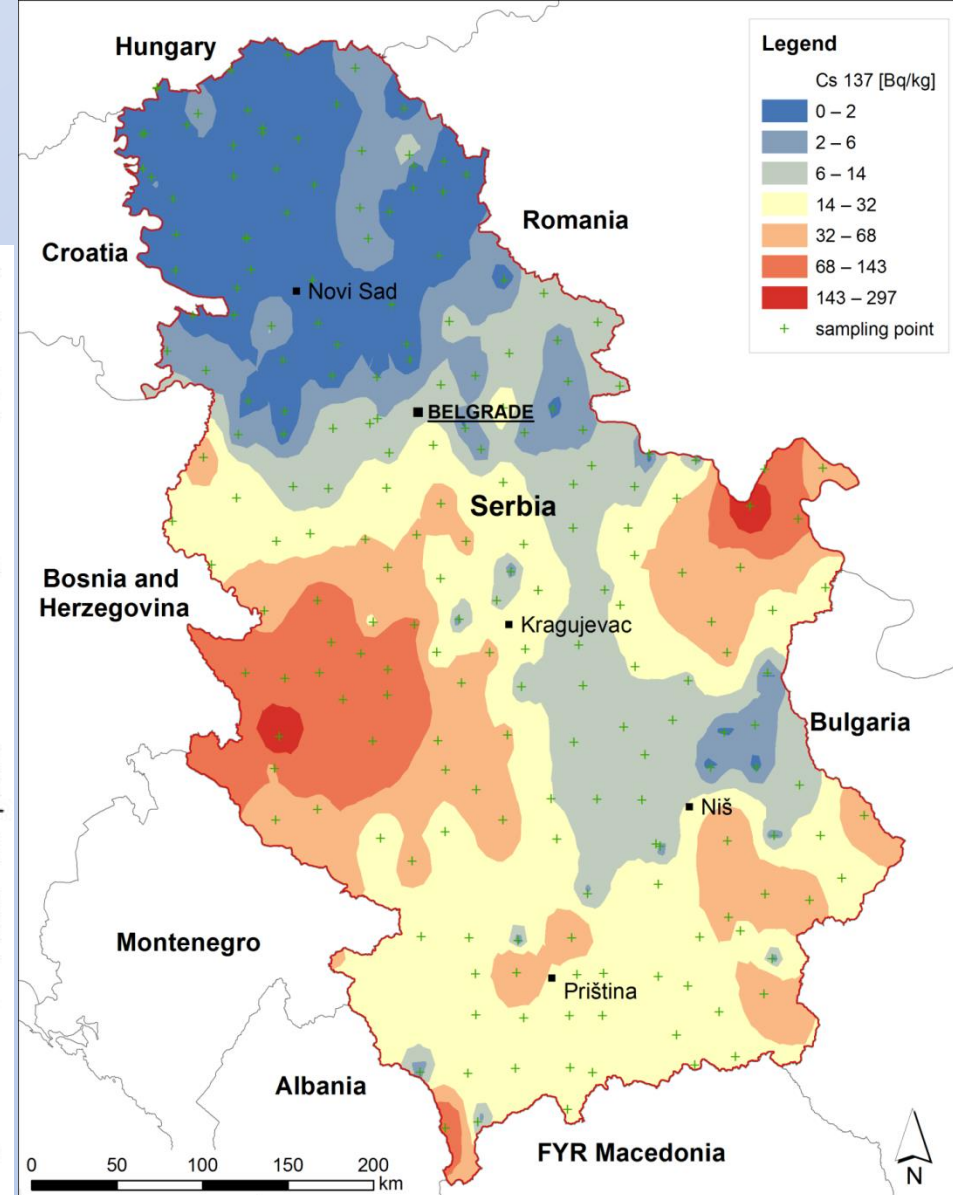
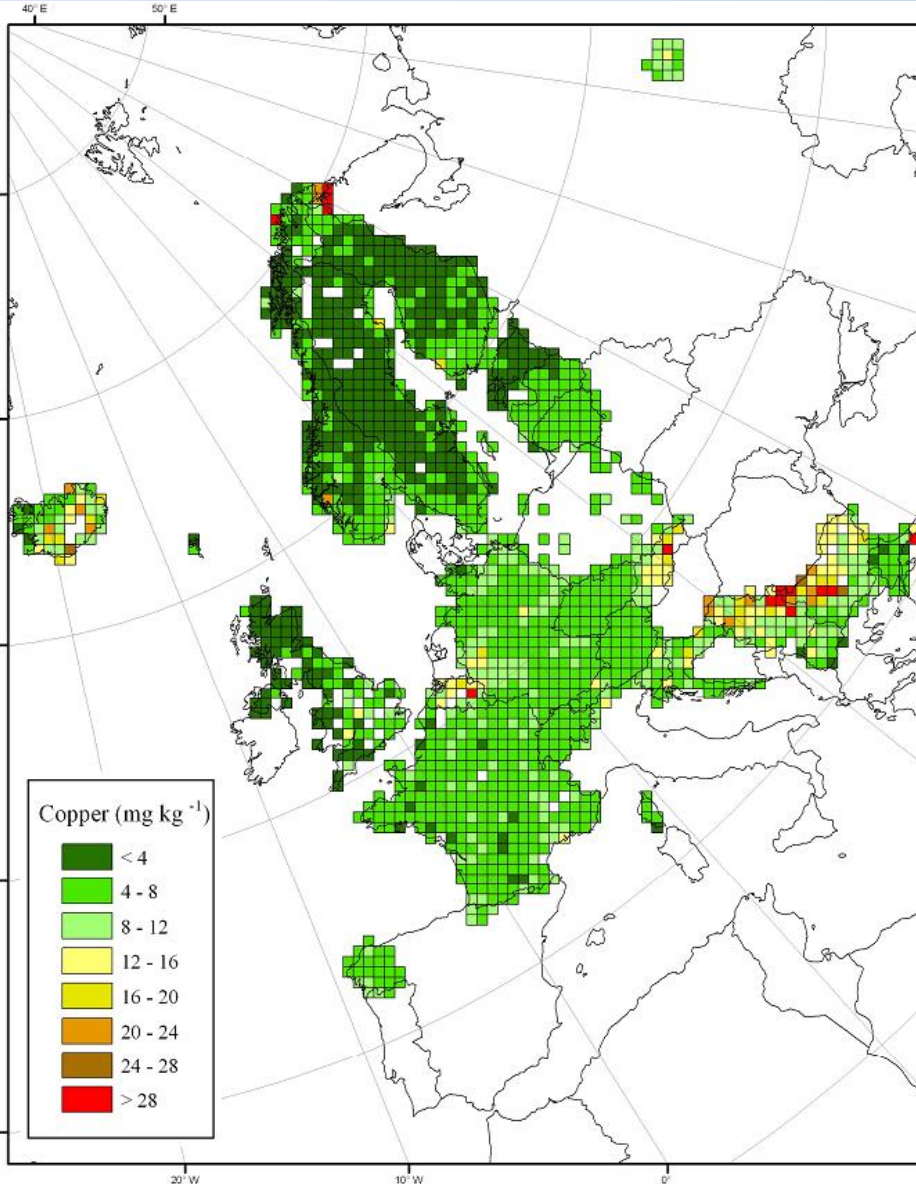
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Excellent maps showing spatial distribution of some heavy metals or radionuclide can be obtained using biomonitors (mosses).



| Country | Parameter | As (mg/kg) | Cd (mg/kg) | Cr (mg/kg) | Cu (mg/kg) | Fe (mg/kg) | Hg (mg/kg) | Ni (mg/kg) | Pb (mg/kg) | V (mg/kg) | Zn (mg/kg) | Al (mg/kg) | Sb (mg/kg) | N (%) |
|-----------------|-----------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|--------------|---------------|---------------|---------------|----------|
| Poland | Number | | 272 | | 273 | 273 | | 272 | 272 | | 272 | | | |
| Poland | Min | | 0.01 | | 3.34 | 98 | | 0.13 | 0.01 | | 18.4 | | | |
| Poland | Max | | 1.94 | | 13.10 | 1210 | | 4.63 | 17.49 | | 124.2 | | | |
| Poland | Median | | 0.25 | | 6.58 | 300 | | 1.64 | 4.17 | | 34.1 | | | |
| Poland | Mean | | 0.33 | | 6.88 | 354 | | 1.65 | 5.11 | | 37.8 | | | |
| Poland (Marina) | Number | 30 | | 30 | | 30 | | 30 | | 30 | 30 | 30 | 30 | |
| Poland (Marina) | Min | 0.30 | | 1.00 | | 112 | | 0.83 | | 1.07 | 26.5 | 490 | 0.13 | |
| Poland (Marina) | Max | 3.12 | | 10.29 | | 3086 | | 6.36 | | 11.66 | 125.2 | 7406 | 0.68 | |
| Poland (Marina) | Median | 0.90 | | 2.74 | | 775 | | 2.56 | | 2.61 | 64.3 | 1237 | 0.36 | |
| Poland (Marina) | Mean | 1.03 | | 3.42 | | 868 | | 2.57 | | 2.93 | 66.8 | 1503 | 0.36 | |
| Russia (all) | Number | 220 | 74 | 220 | 76 | 220 | | 220 | | 220 | 220 | 220 | 220 | |
| Russia (all) | Min | 0.02 | 0.03 | 0.21 | 3.41 | 26 | | 0.43 | | 0.08 | 11.4 | 79 | 0.02 | |
| Russia (all) | Max | 2.47 | 1.06 | 48.06 | 22.48 | 23490 | | 22.78 | | 68.51 | 331.1 | 12865 | 2.47 | |
| Russia (all) | Median | 0.23 | 0.24 | 3.64 | 8.94 | 679 | | 2.74 | | 2.27 | 40.1 | 850 | 0.23 | |
| Russia (all) | Mean | 0.28 | 0.30 | 5.12 | 9.74 | 1212 | | 3.53 | | 3.64 | 47.7 | 1296 | 0.28 | |
| Serbia | Number | 193 | 193 | 193 | 193 | 193 | | 193 | 193 | 193 | 193 | 193 | 193 | |
| Serbia | Min | 0.22 | 0.04 | 2.00 | 3.04 | 670 | | 1.70 | 1.03 | 1.94 | 13.2 | 1117 | 0.06 | |
| Serbia | Max | 21.60 | 1.11 | 78.81 | 451.04 | 16100 | | 23.83 | 248.64 | 32.67 | 258.6 | 31180 | 1.37 | |
| Serbia | Median | 1.41 | 0.26 | 6.44 | 11.11 | 2267 | | 4.43 | 16.73 | 5.76 | 29.0 | 3946 | 0.24 | |
| Serbia | Mean | 2.01 | 0.34 | 9.69 | 17.69 | 3174 | | 5.38 | 20.74 | 7.48 | 34.0 | 5572 | 0.29 | |

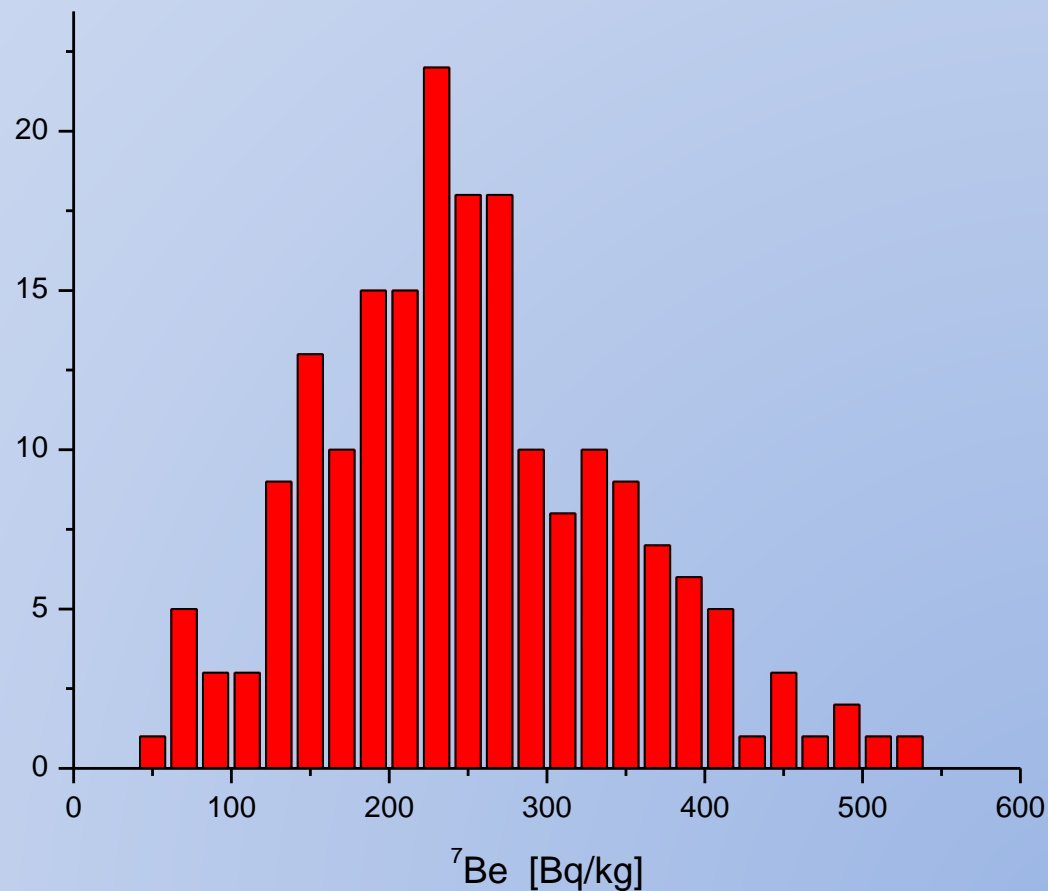
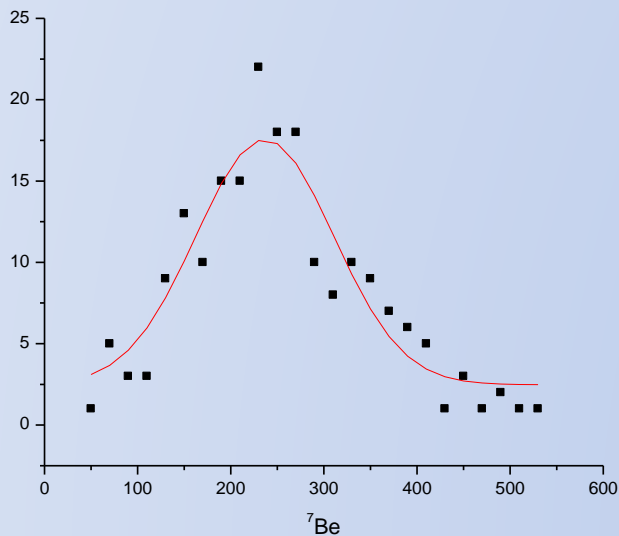
Several statistical parameters as Minimal value, Maximal value, Mean and Median are usually given.

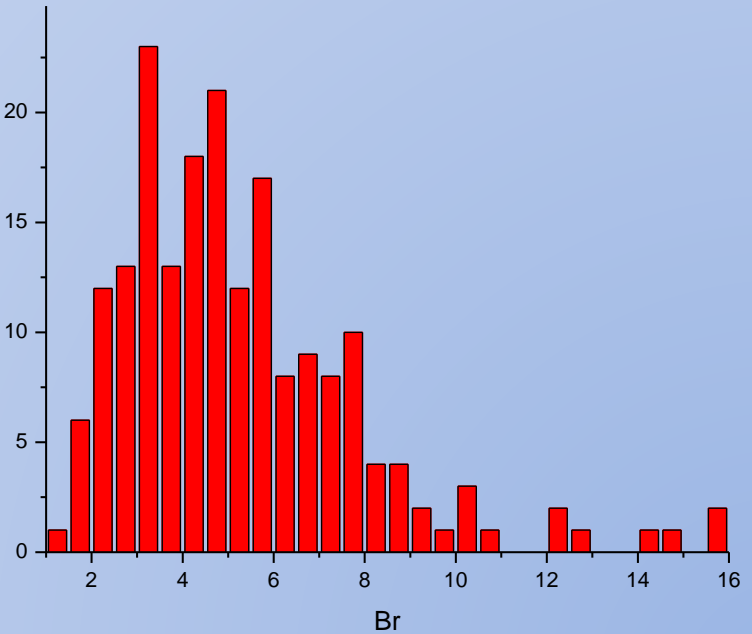
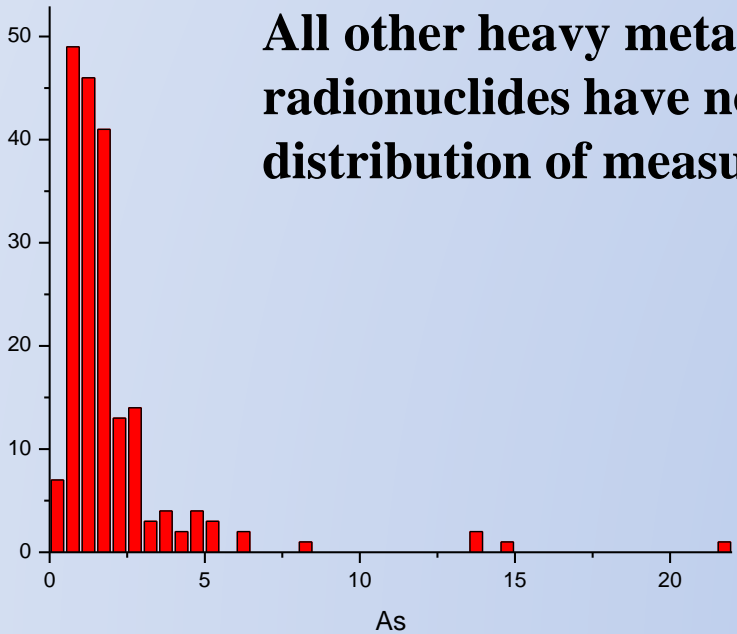
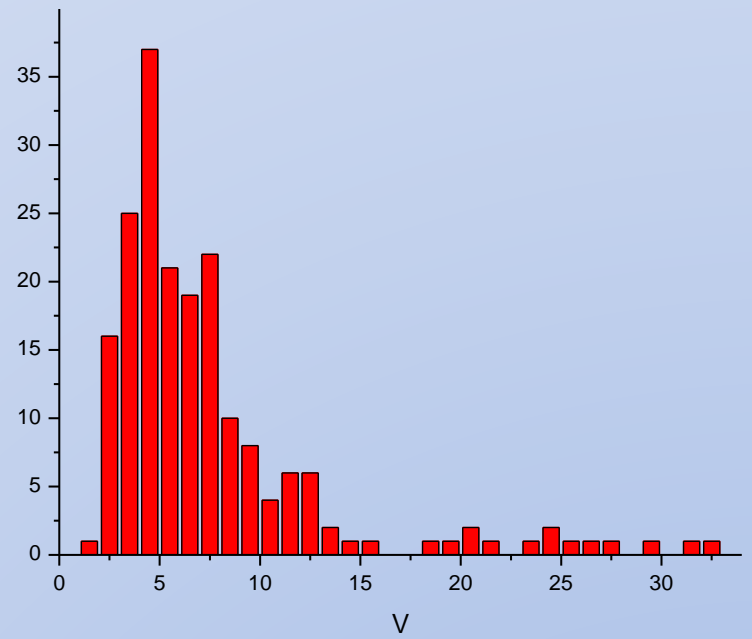
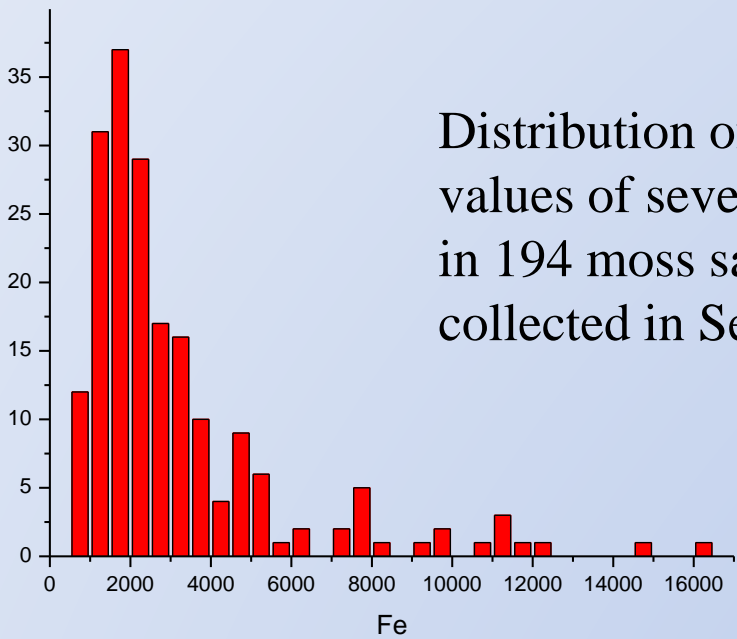
Mean is always higher than Median. It is consequence of specific distribution of measured values.

Let us see the distribution of measured values!!!!

| radionuclide | range [Bq kg ⁻¹] | Arithmetic mean [Bq kg ⁻¹] | Median [Bq kg ⁻¹] |
|-------------------|---------------------------------|---|----------------------------------|
| ⁷ Be | 60 - 538 | 251(94) | 244 |
| ⁴⁰ K | 128 - 2235 | 465(268) | 400 |
| ¹³⁷ Cs | mda - 296 | 23(43) | 8 |
| ²¹² Pb | 3 - 259 | 58(40) | 50 |
| ²¹⁴ Bi | mda - 793 | 114(116) | 79 |

Only one symmetric distribution (Gauss - like) is obtained between all measurements of moss samples. It was in analysis of ^7Be activity concentrations measured in 196 moss samples collected in Serbia.

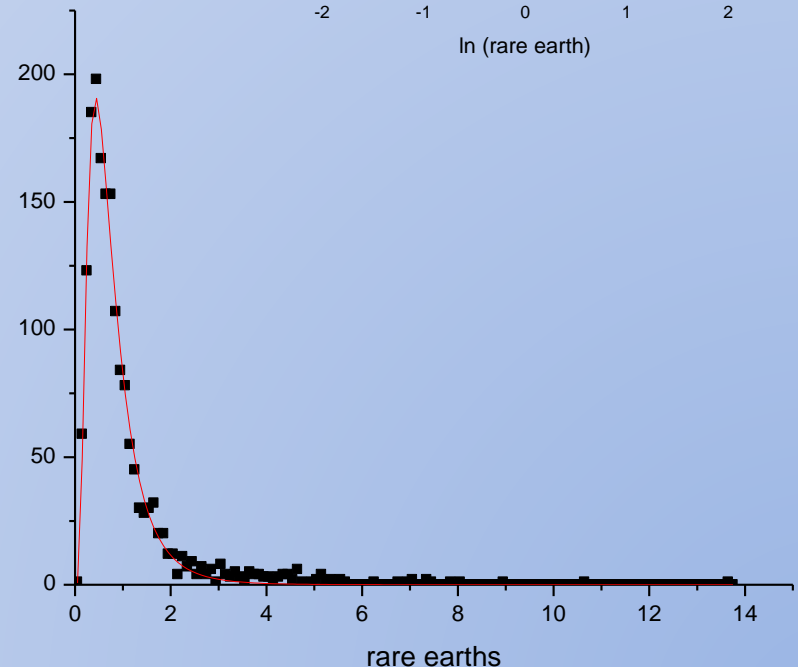
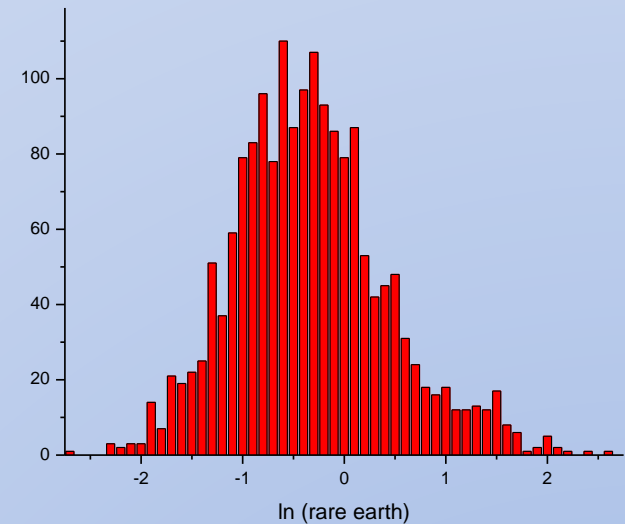
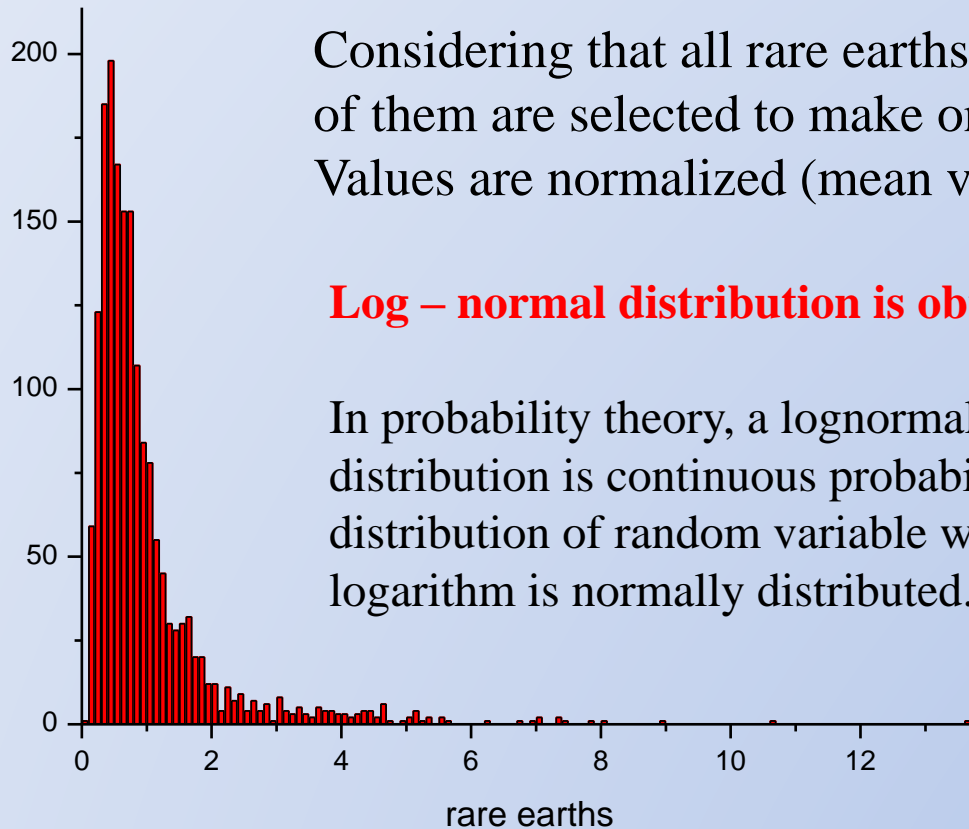




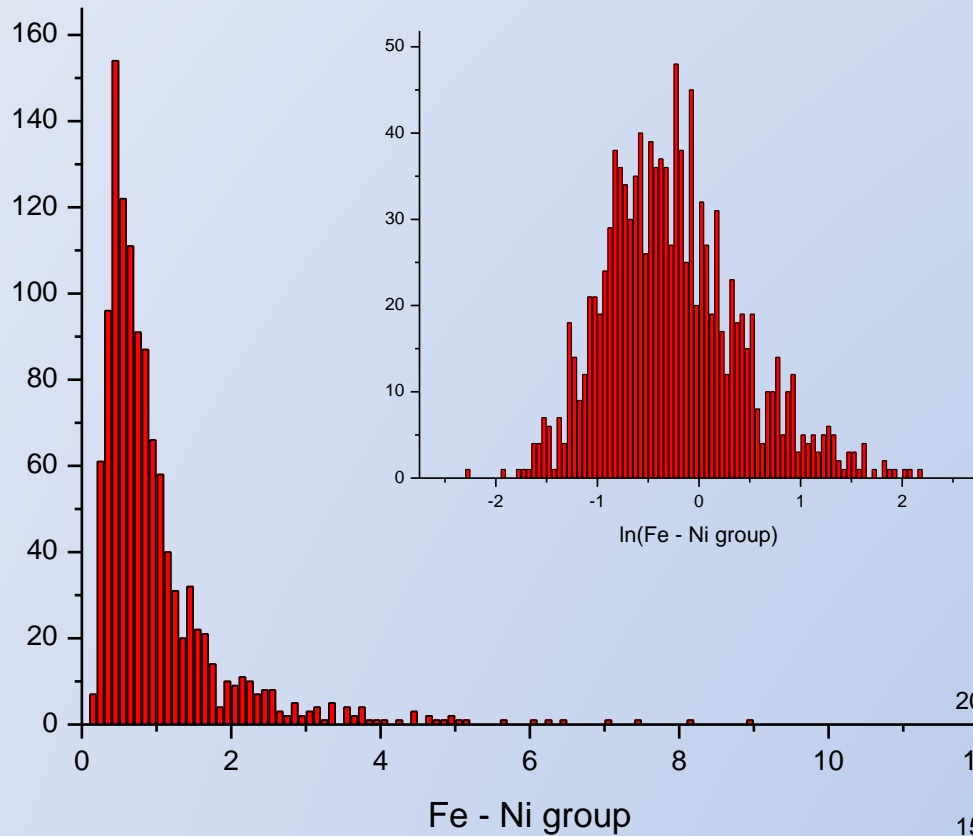
Considering that all rare earths have similar distribution, eight of them are selected to make one data set (1738 values). Values are normalized (mean value = 1)

Log – normal distribution is obtained

In probability theory, a lognormal distribution is continuous probability distribution of random variable whose logarithm is normally distributed.

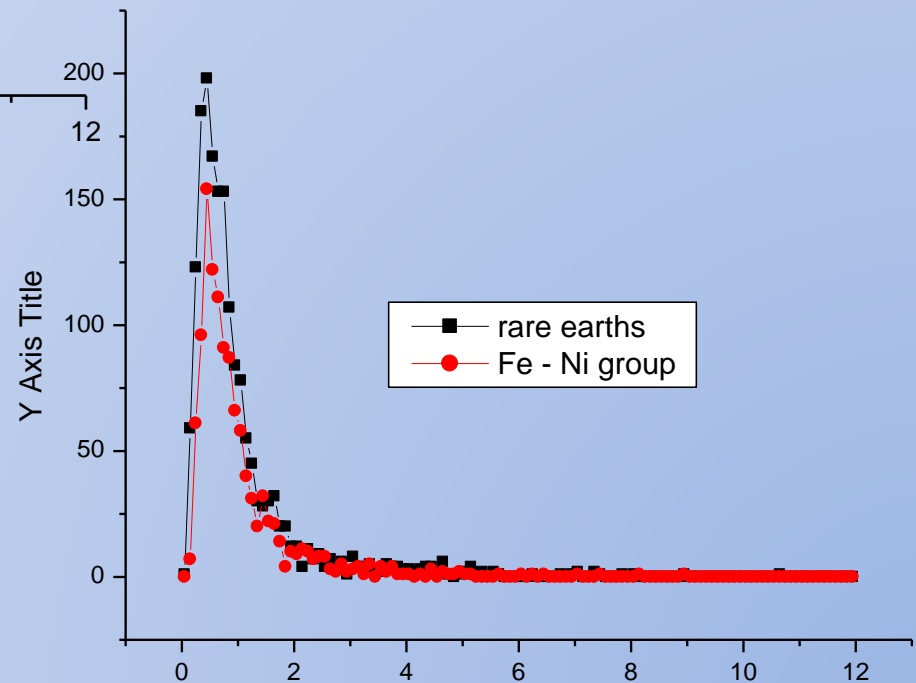


$$y = 165 \frac{\exp\left(-\frac{\left(\ln \frac{x}{0.657}\right)^2}{0.645}\right)}{\sqrt{2\pi \cdot 0.645 \cdot x}}$$

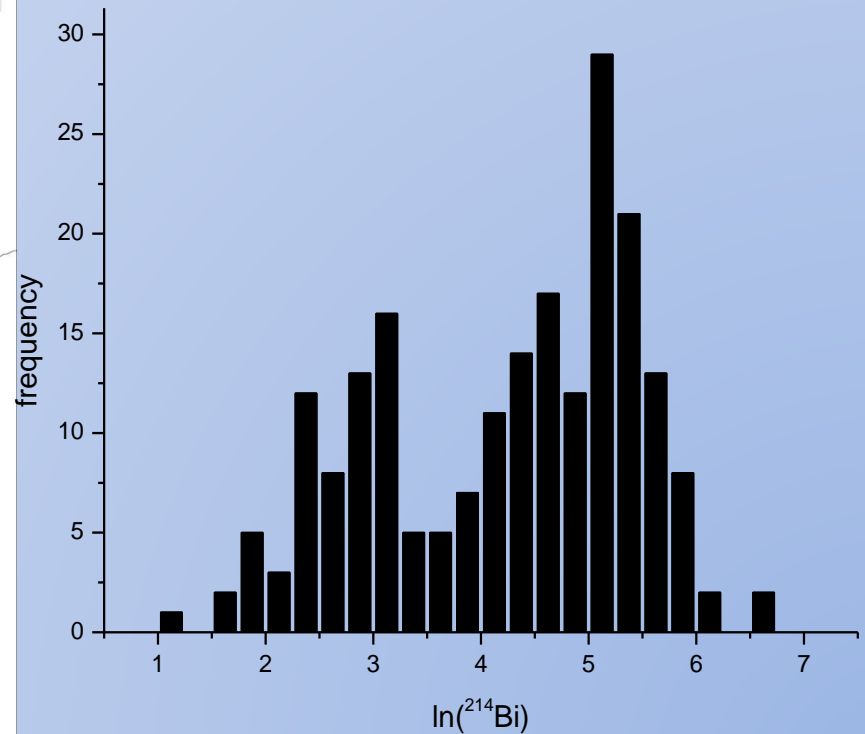
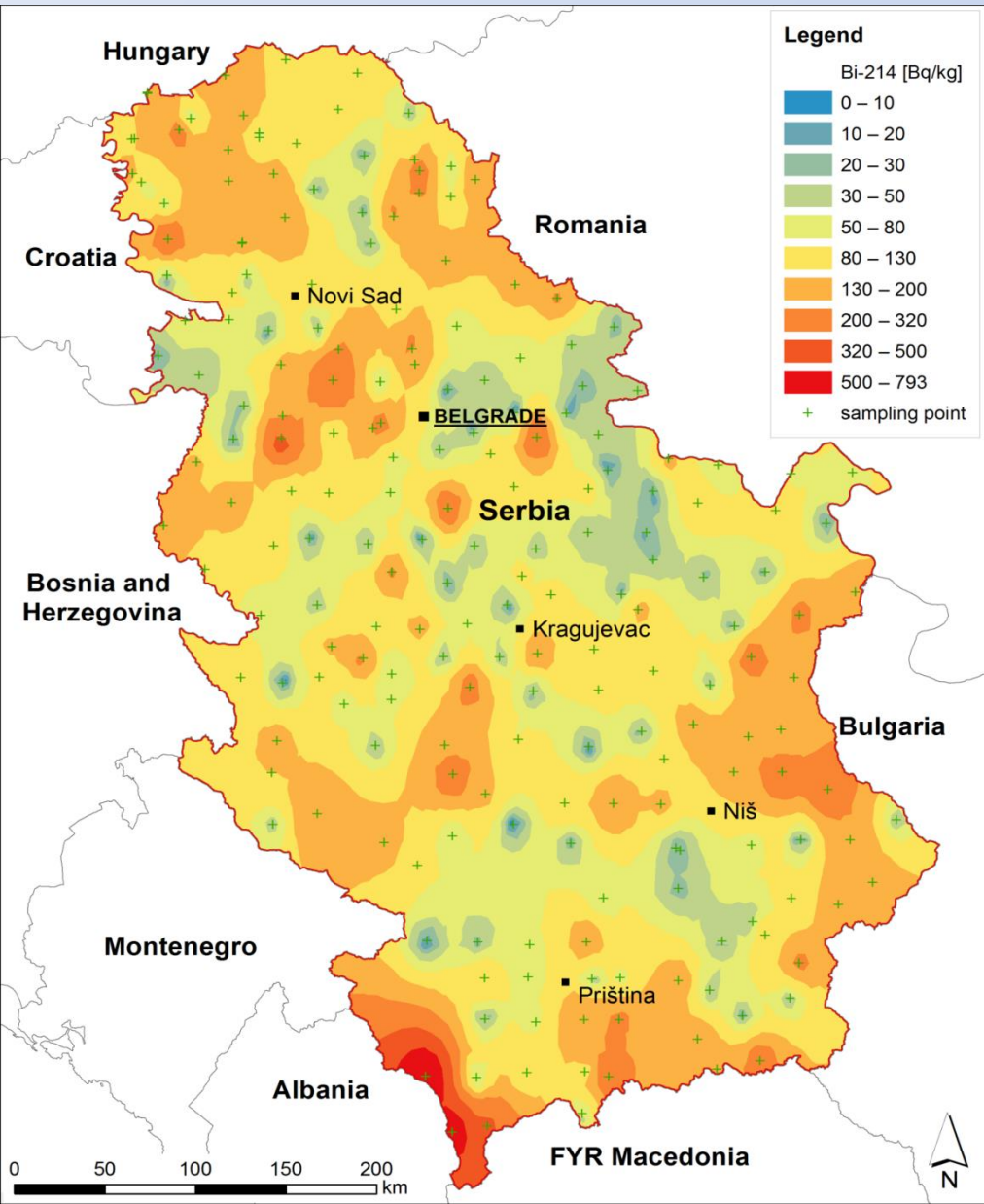


The very same procedure was repeated for sum of normalized values of Sc, Ti, Cr, Fe, Co and Ni (1159 values). Very similar lognormal distribution was obtained

$$y = 108 \frac{\exp\left(-\frac{\ln \frac{x}{0.688}}{0.571}\right)}{\sqrt{2\pi} 0.571 x}$$

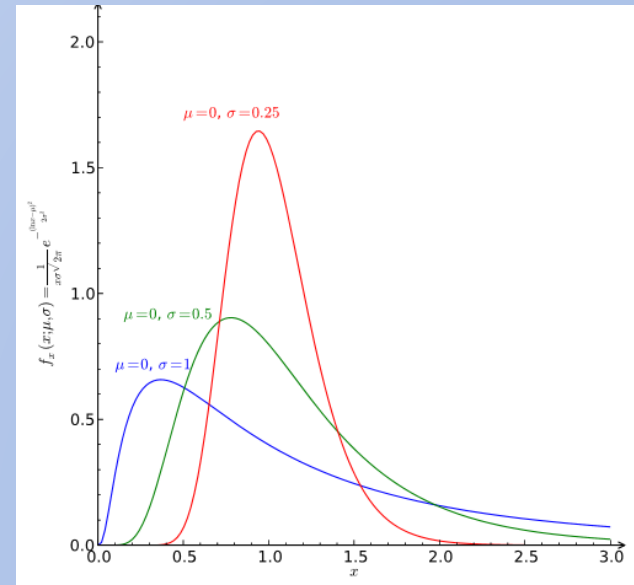
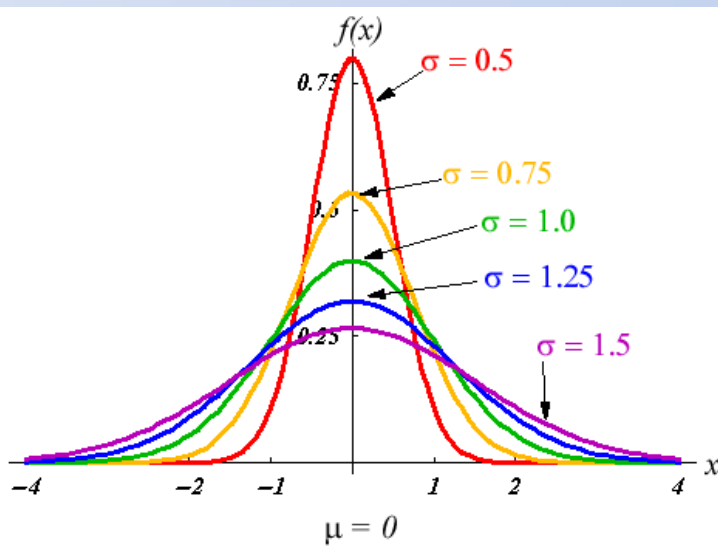


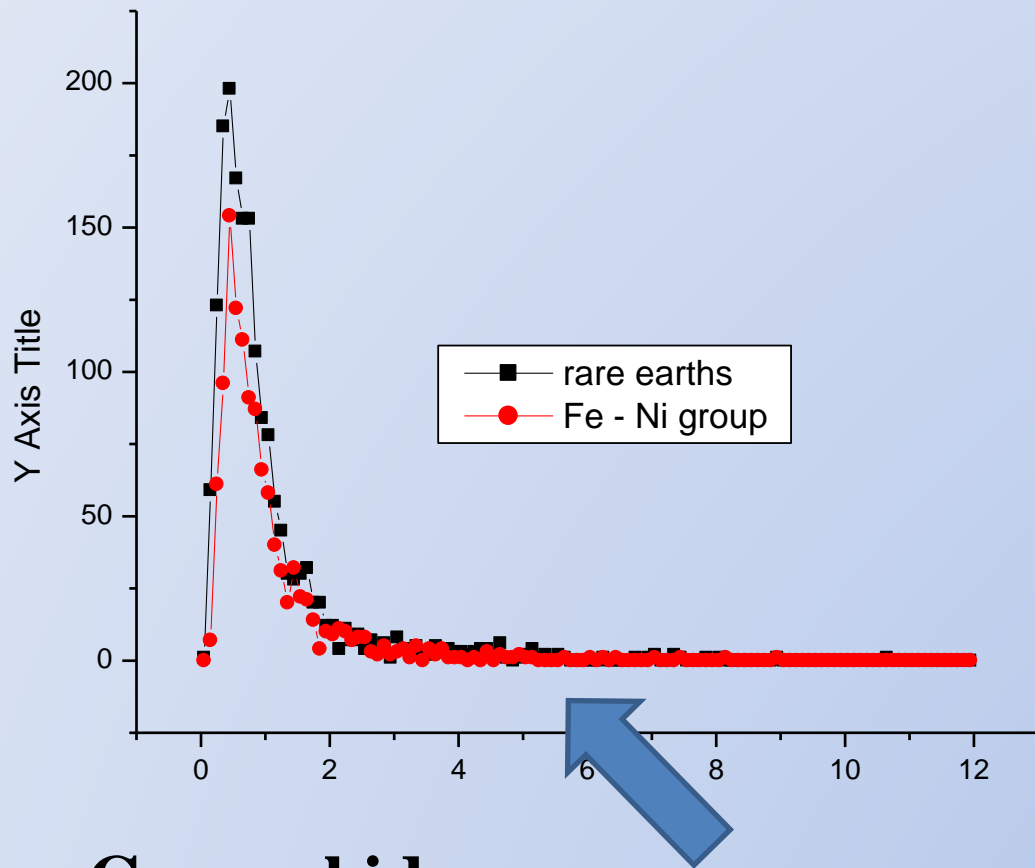
Distribution of values of ^{214}Bi (^{238}U) measured by gamma spectroscopy in 217 moss samples from Serbia.



A lognormal process is statistical realization of the multiplicative product of many independent random variables. Many natural processes are driven by the accumulation of many small (differential) changes. These become additive on a log scale and transformation onto the linear scale makes the distribution lognormal.

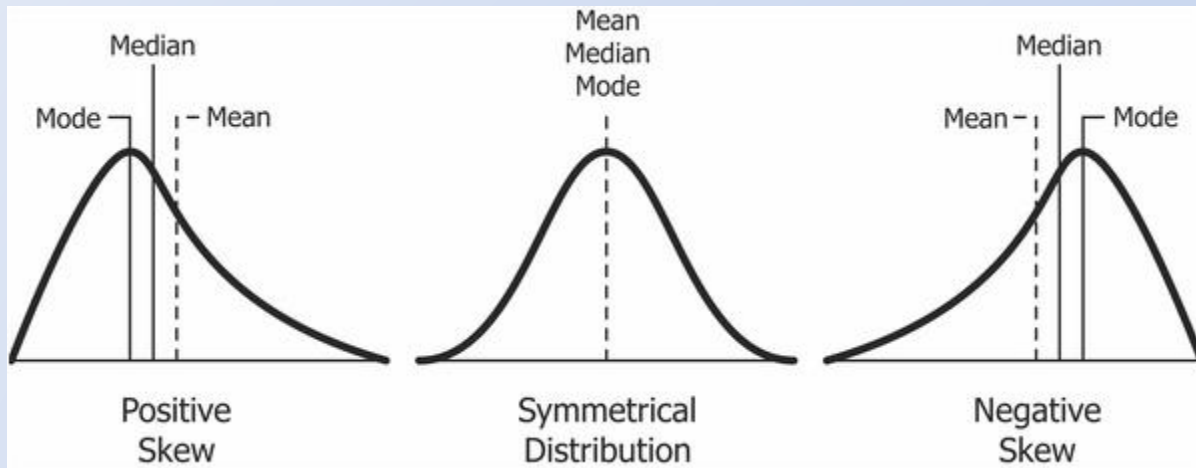
Physical quantities that are expected to be the sum of many independent processes have normal distributions.





General idea:

If the lognormal distribution is characteristic distribution of measured values of heavy elements or radionuclides in moss samples, possible pollution and detection of unusually elevated values could be observed at the tail of distribution.

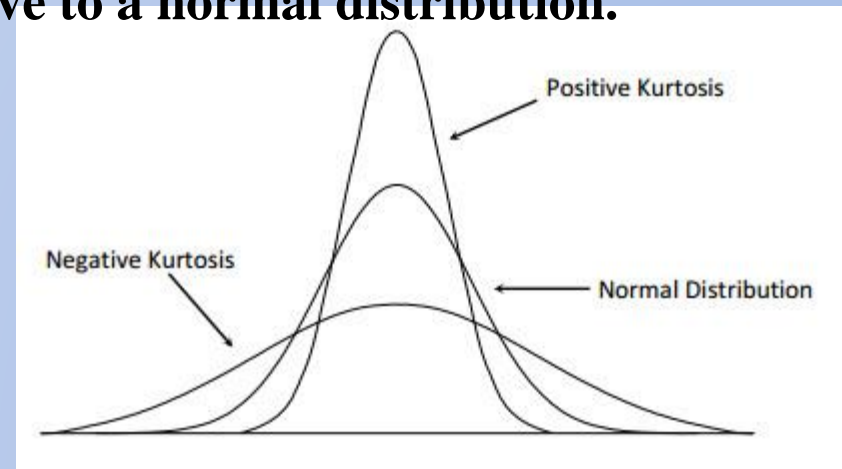


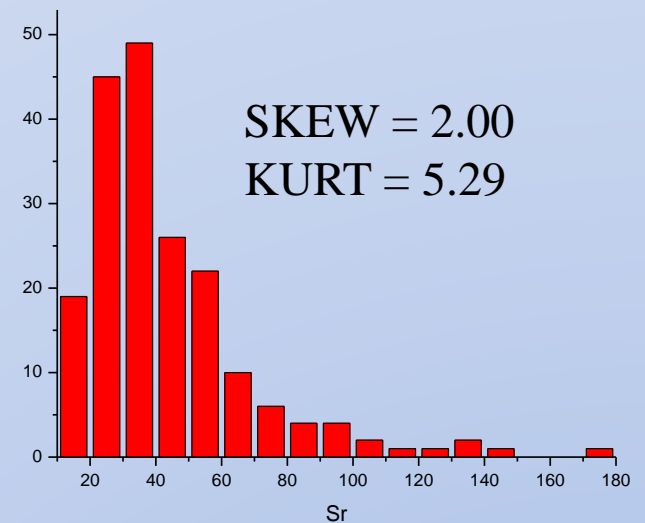
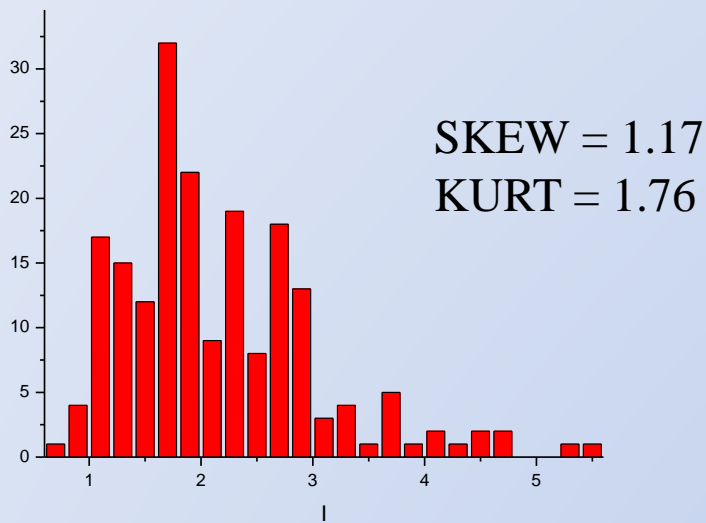
$$S = \frac{1}{n} \frac{\sum_{i=1}^n (X_i - X_{avg})^3}{\sigma^3}$$

Skewness is a measure of the asymmetry of some distribution of a real valued variable about its mean.

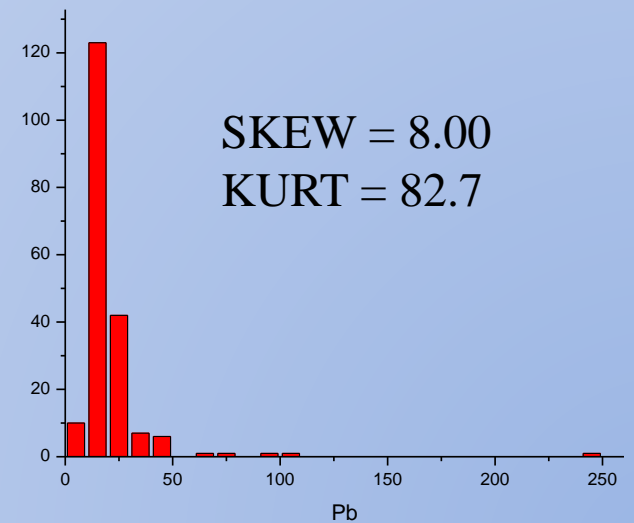
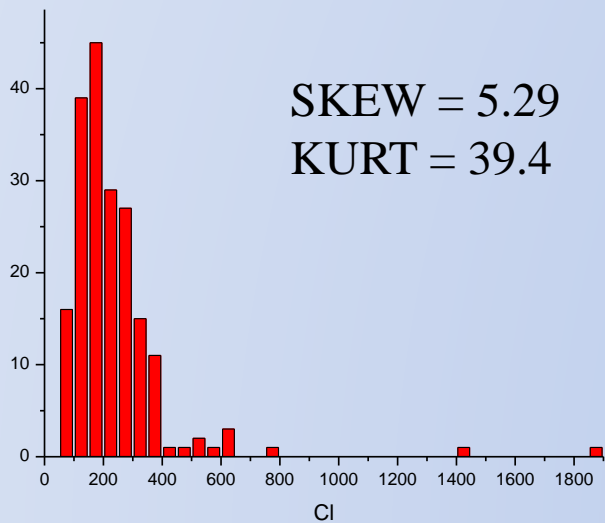
$$K = n \frac{\sum_{i=1}^n (X_i - X_{avg})^4}{(\sum_{i=1}^n (X_i - X_{avg})^2)^2} - 3$$

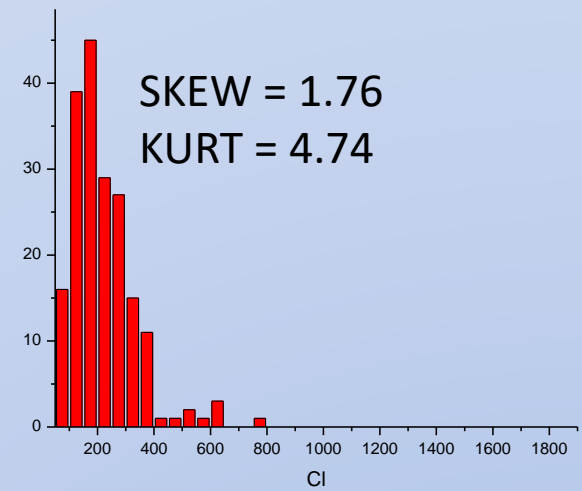
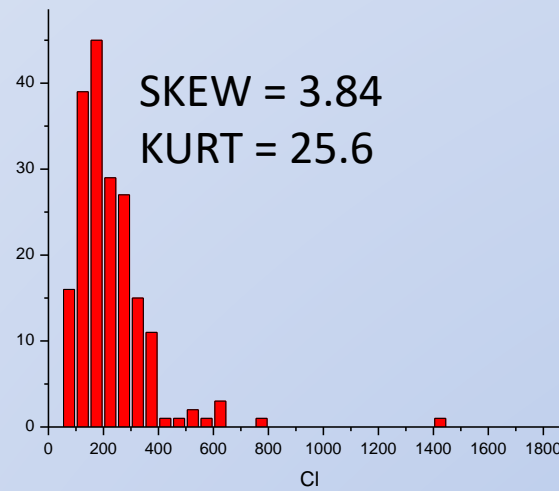
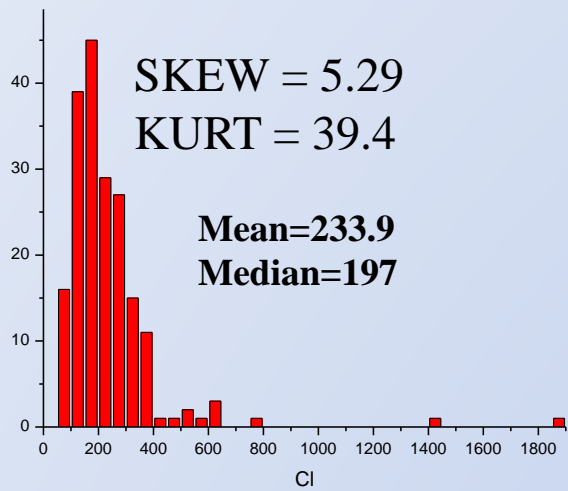
Kurtosis is a measure of whether the data are heavy-tailed or light-tailed relative to a normal distribution.



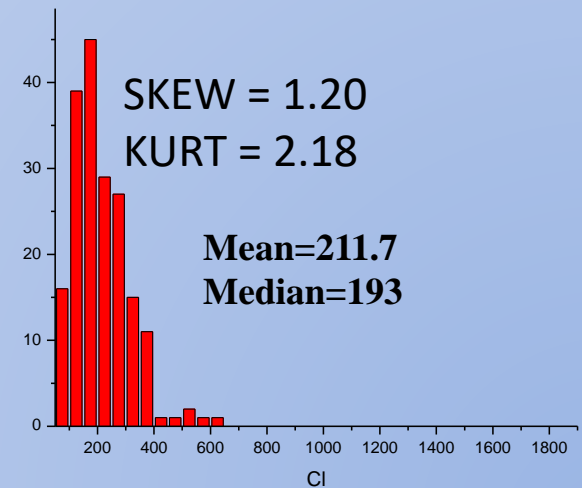
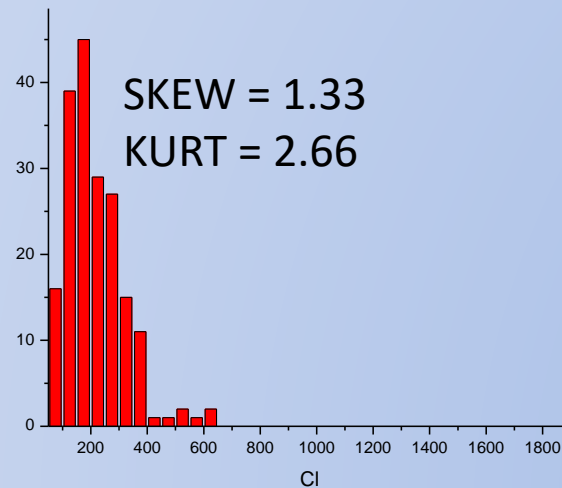
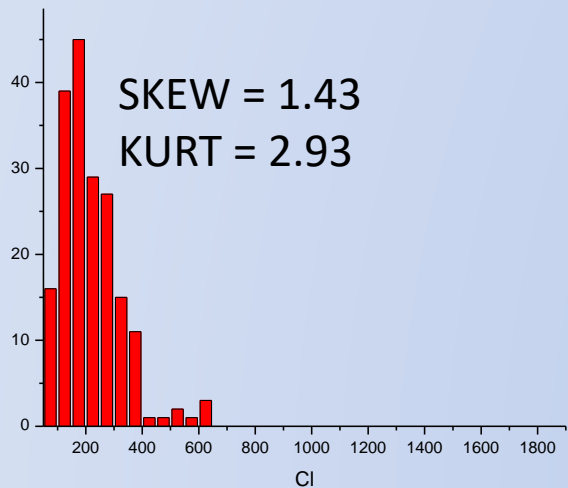


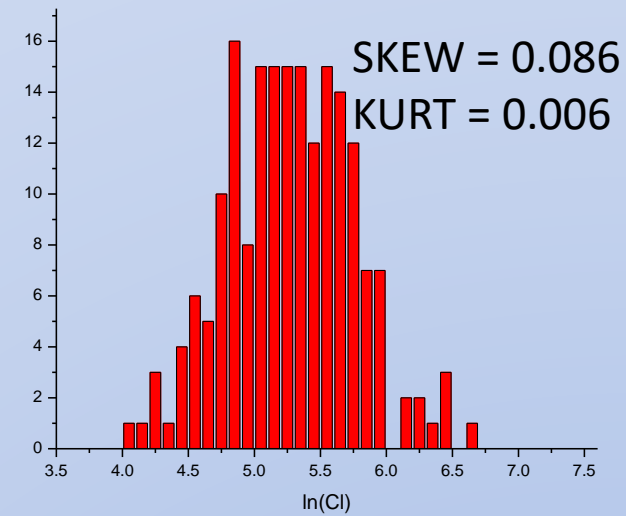
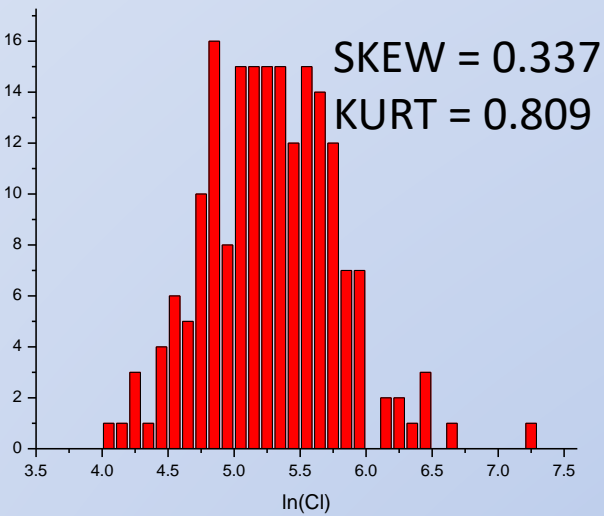
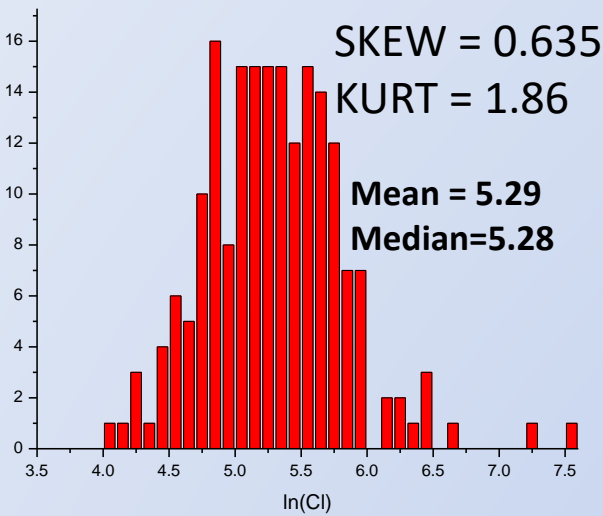
Skewness, kurtosis and distributions of several elements measured in moss samples collected 2005 in Serbia. There were 194 moss samples.



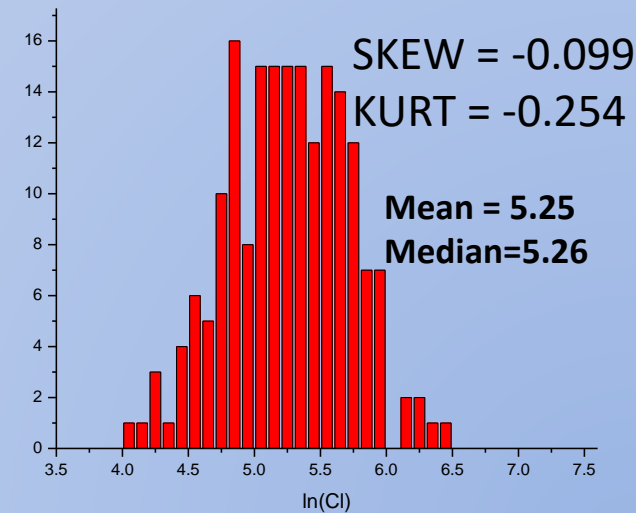
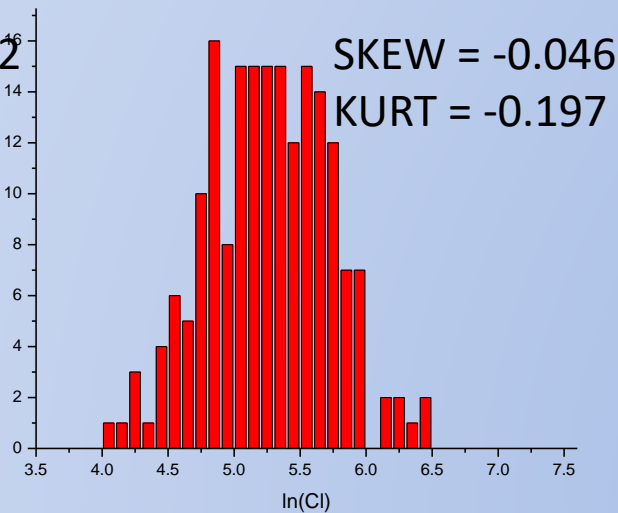
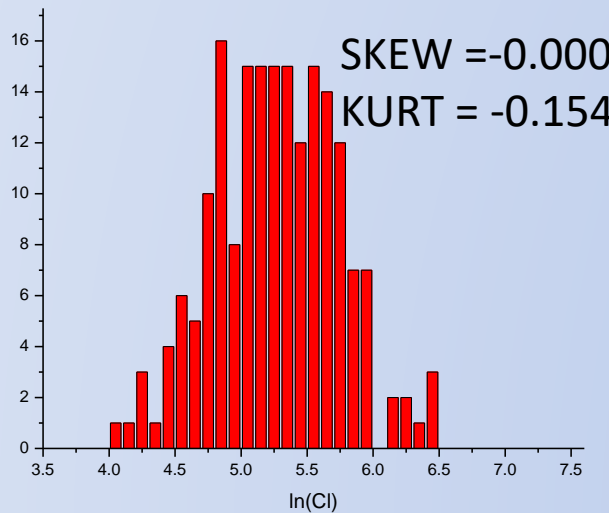


Skewness of the distribution of measured values of CI in 194 moss samples collected in 2005 in Serbia. The highest measured values are successively deleted.

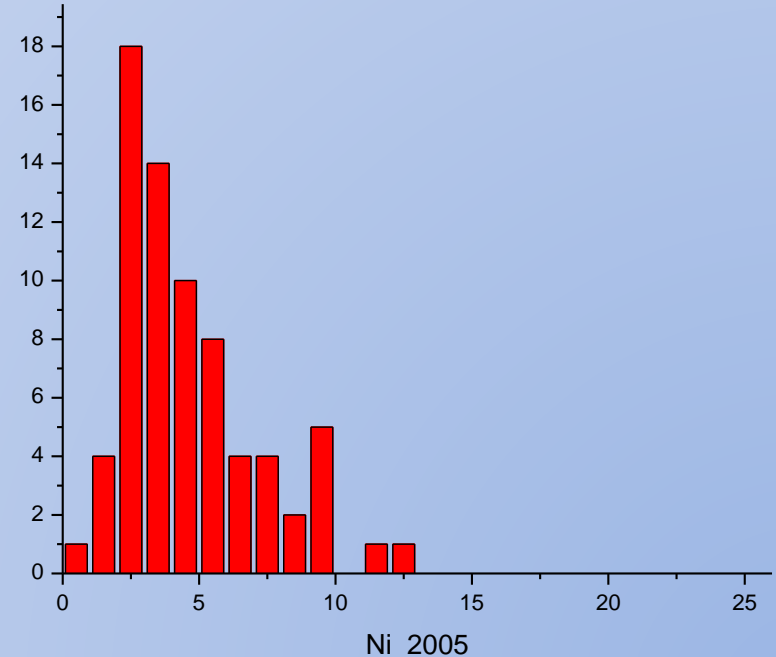
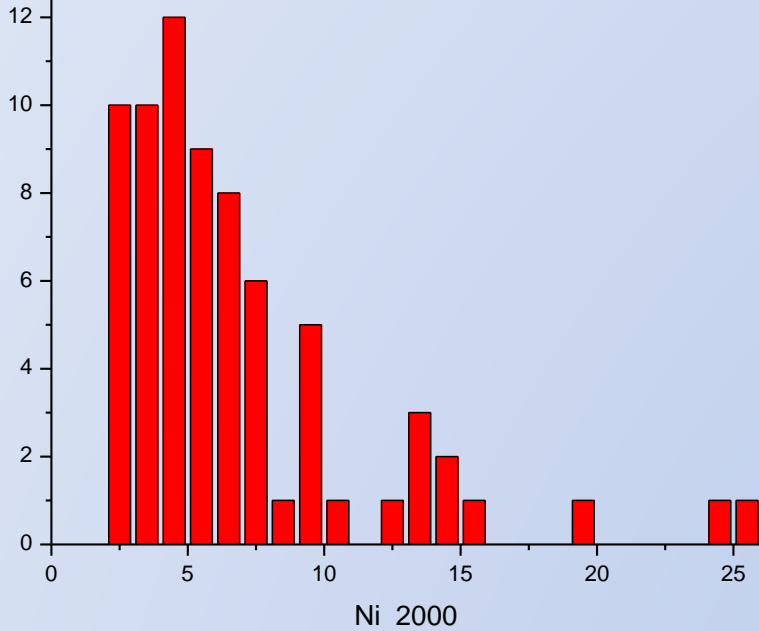




Very same calculation was repeated using logarithm values of measured concentrations of Cl in 194 moss samples.



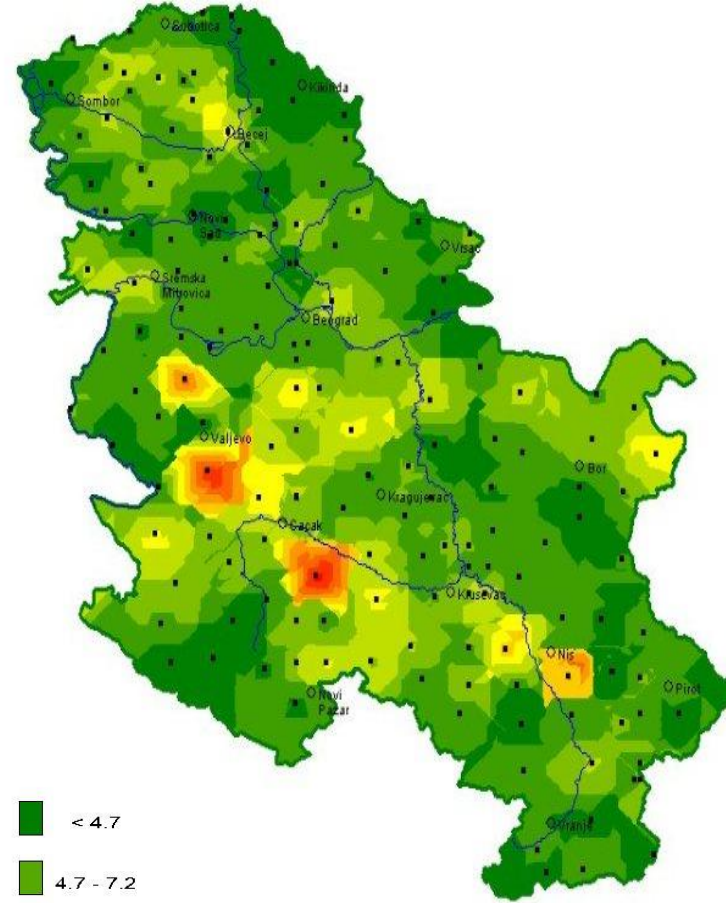
Let us compare two sets of data: moss survey 2000 and moss survey 2005. There were 75 moss samples taken from very same location in the area of north Serbia.



| | Ni 2000 | Ni 2005 |
|---------------|-------------|--------------|
| Min | 2.09 | 0.915 |
| Max | 25.7 | 12.2 |
| Mean | 6.87 | 4.61 |
| Median | 5.60 | 3.81 |
| Skew | 2.10 | 1.08 |
| Kurt | 5.10 | 0.736 |

NI

2005

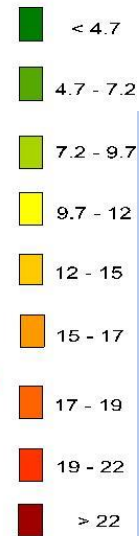
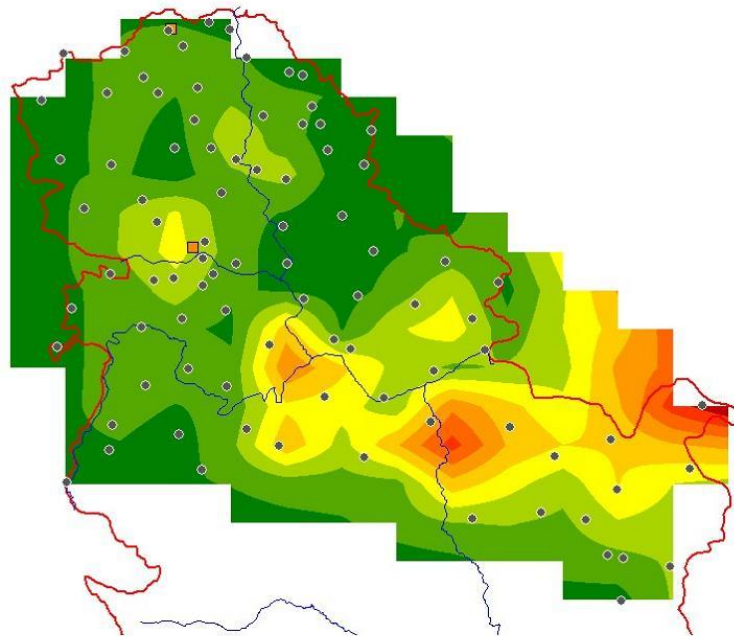


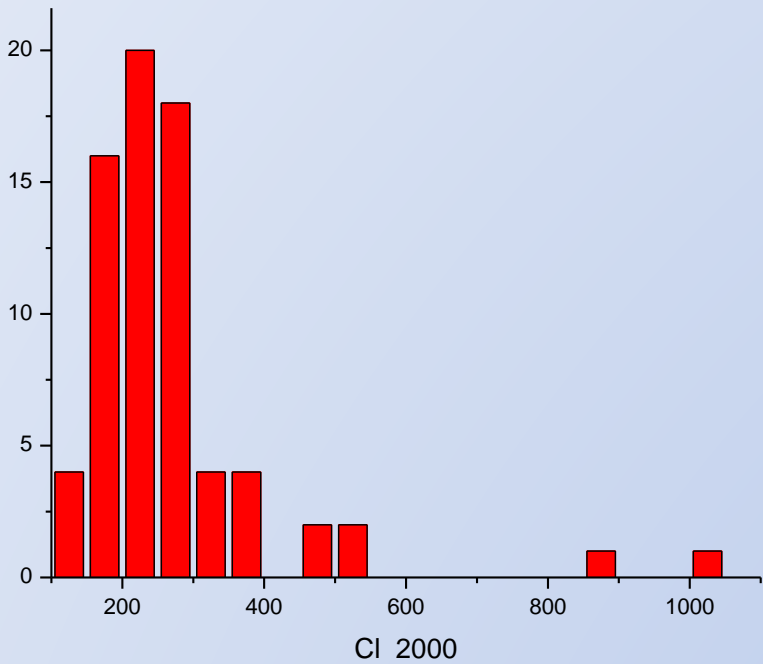
Concentration [ppm]



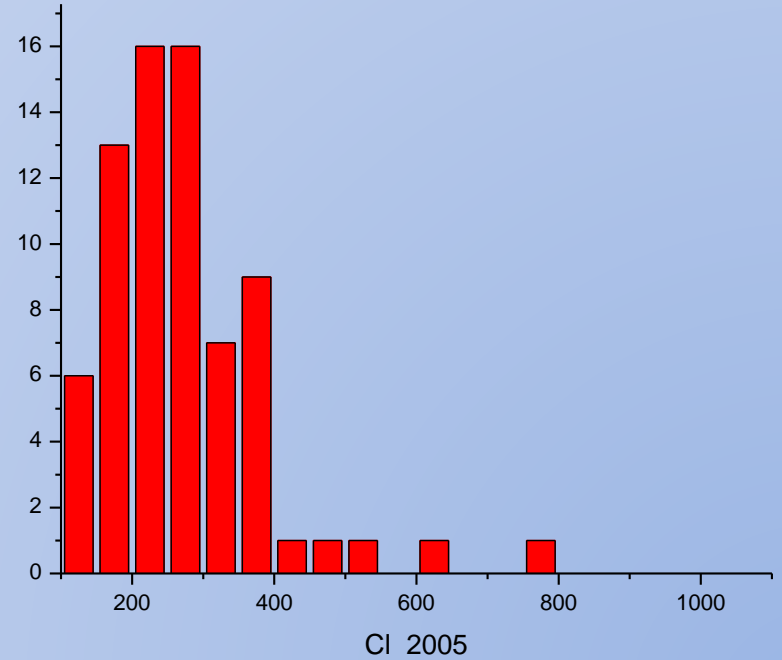
2000

Ni



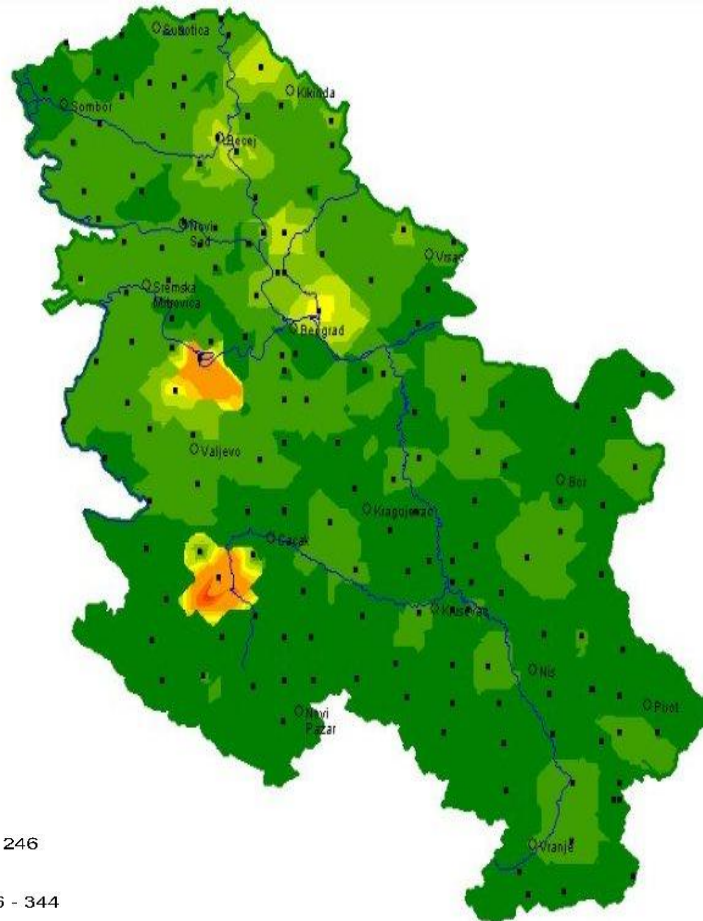


| | CI 2000 | CI 2005 |
|---------------|----------------|----------------|
| Min | 131.3 | 104.1 |
| Max | 1032 | 793.2 |
| Mean | 269.6 | 269 |
| Median | 235.7 | 251 |
| Skew | 3.32 | 1.92 |
| Kurt | 13.8 | 6.09 |



CL

2005

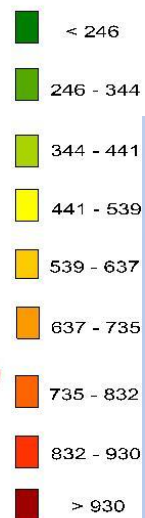
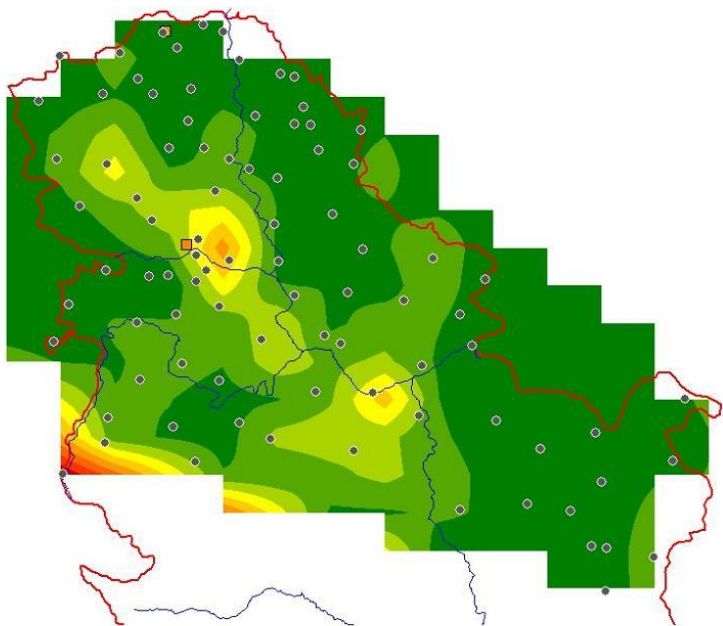


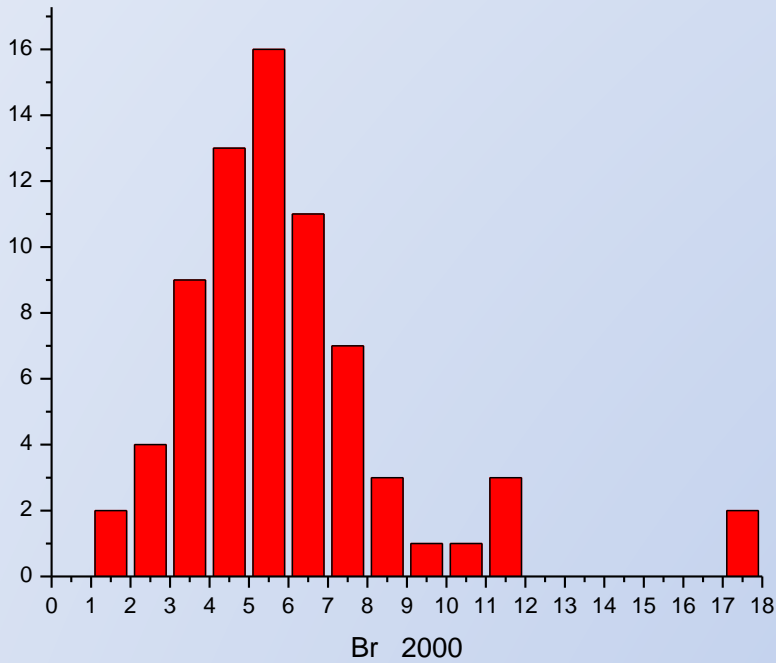
Concentration [ppm]



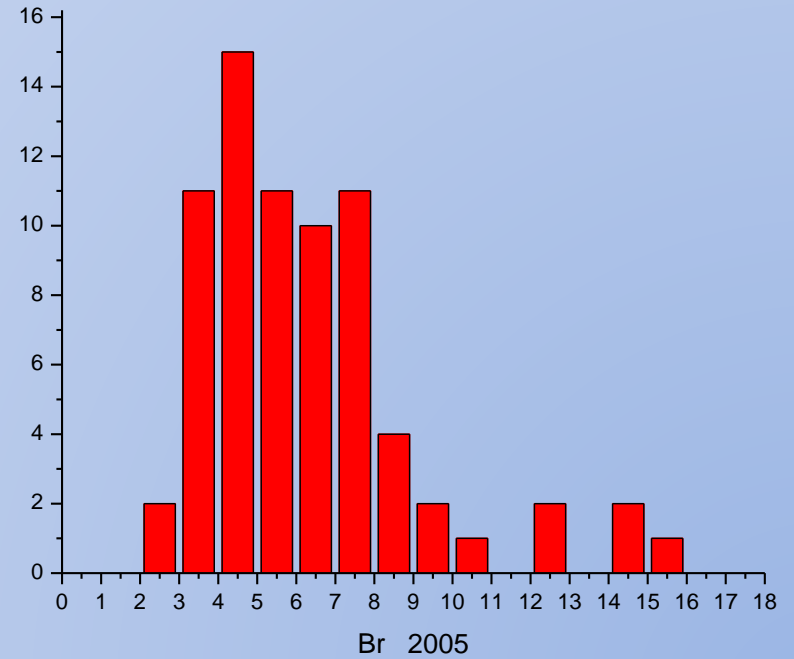
2000

CI

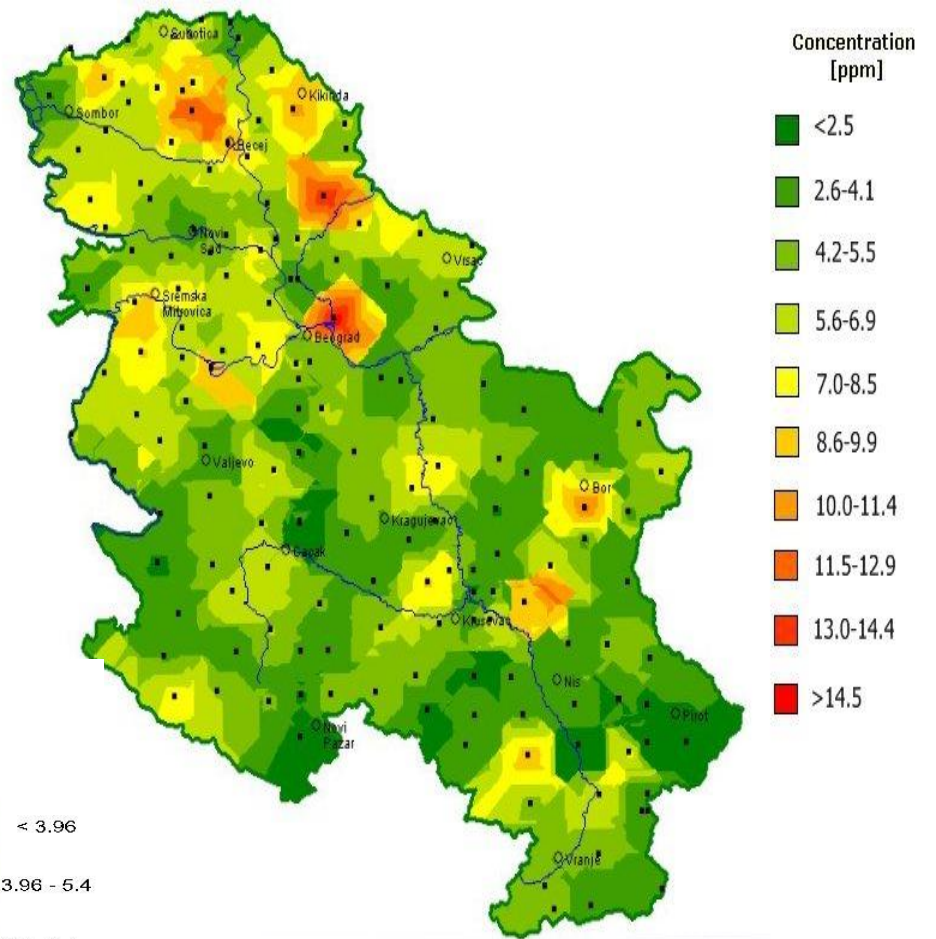




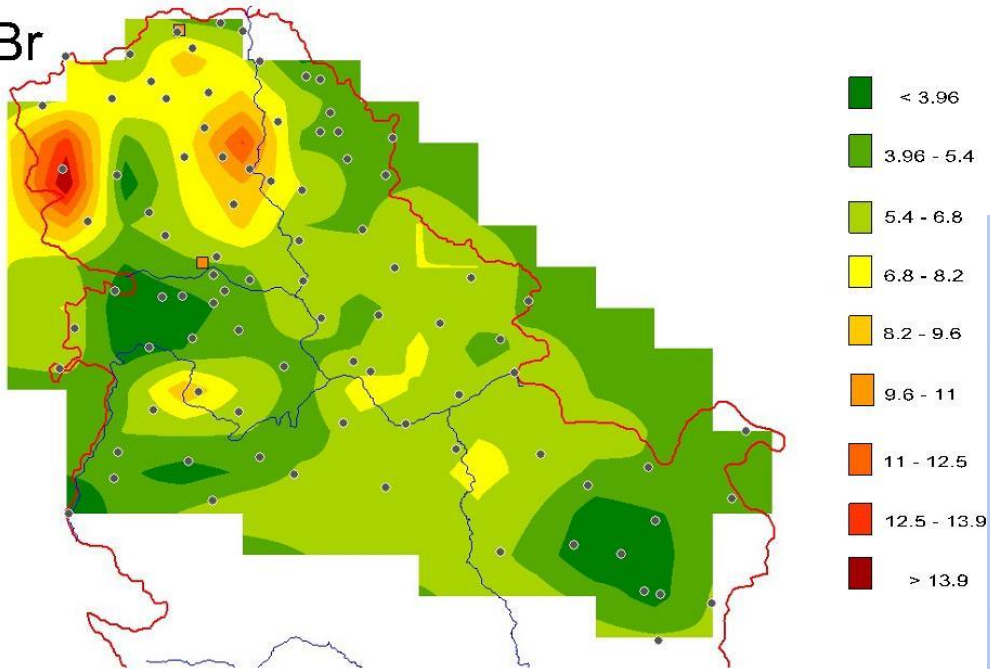
| | Br 2000 | Br 2005 |
|---------------|----------------|----------------|
| Min | 1.83 | 2.32 |
| Max | 17.6 | 15.9 |
| Mean | 3.56 | 6.31 |
| Median | 5.47 | 5.77 |
| Skew | 1.97 | 1.51 |
| Kurt | 5.69 | 2.68 |



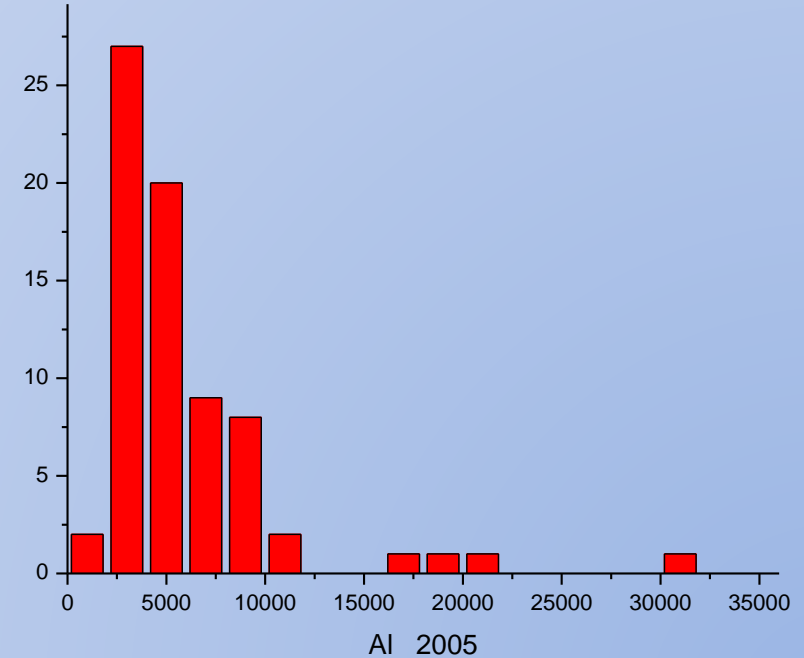
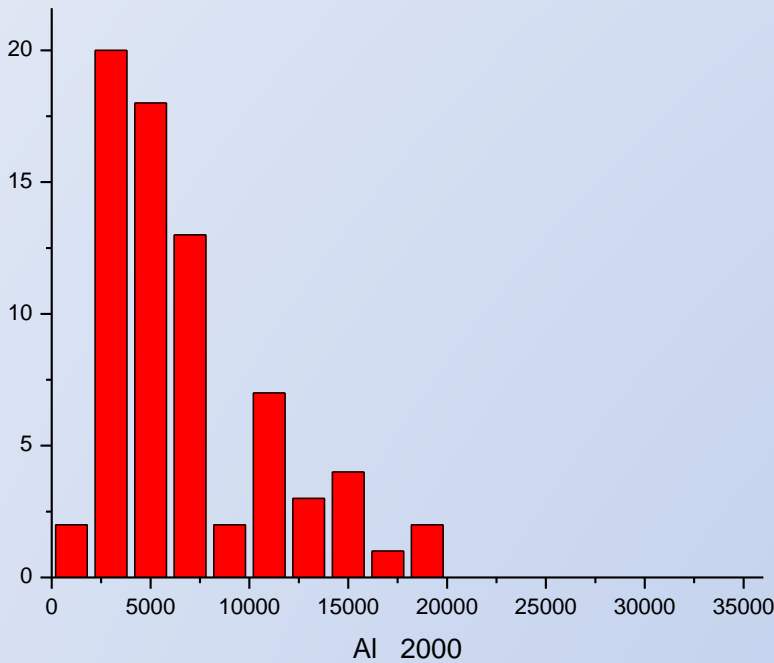
BR



Br

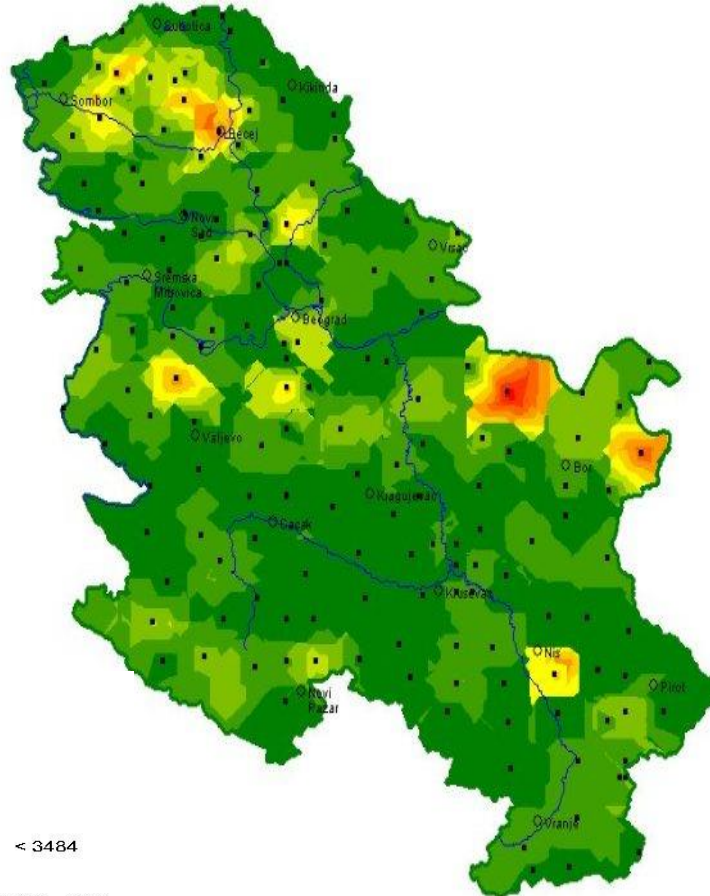


Couple examples when Skewness and Kurtosis are higher in 2005 than in 2000 moss samples.



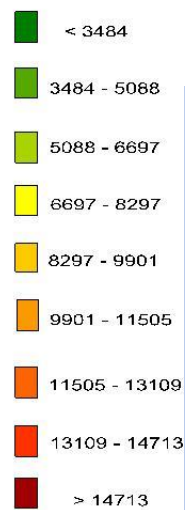
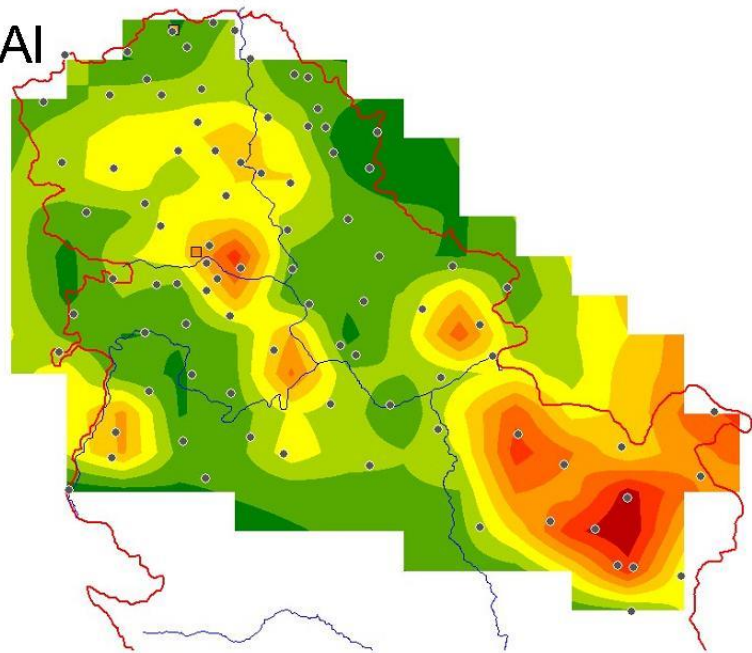
| | AI 2000 | AI 2005 |
|---------------|----------------|----------------|
| Min | 1275 | 1938 |
| Max | 18660 | 31180 |
| Mean | 6841 | 5905 |
| Median | 5521 | 4628 |
| Skew | 1.18 | 3.23 |
| Kurt | 0.615 | 13.1 |

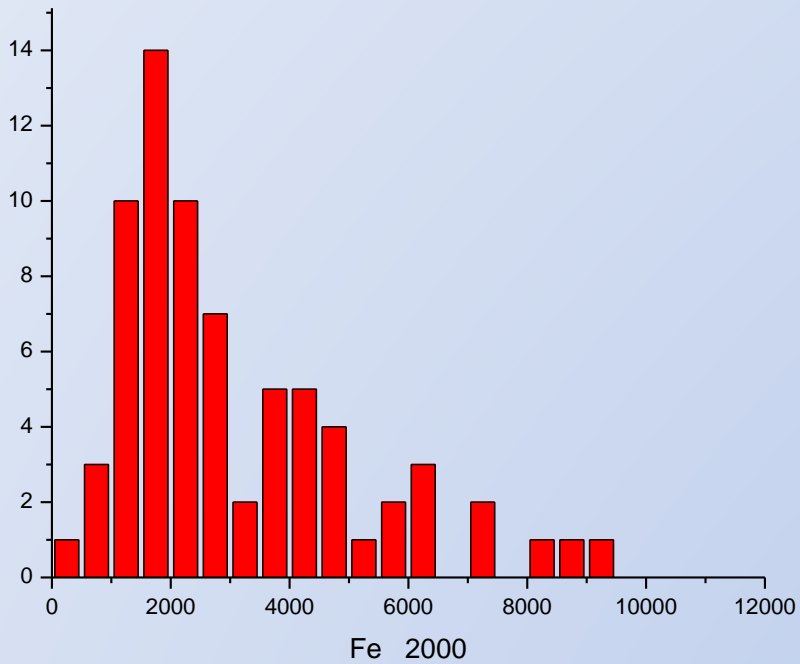
AL
2005



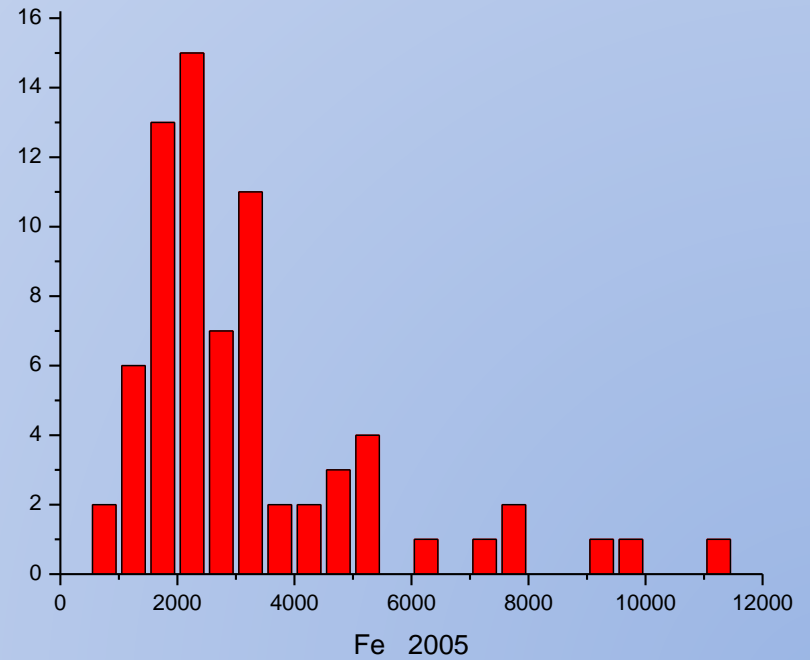
2000

AI



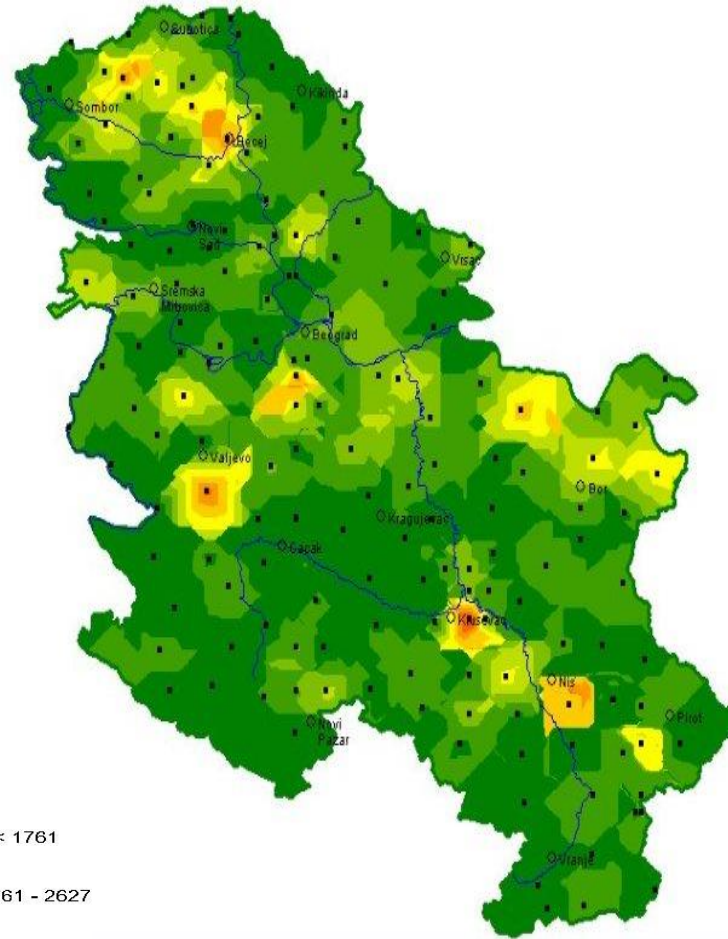


| | Fe 2000 | Fe 2005 |
|---------------|----------------|----------------|
| Min | 337 | 675 |
| Max | 9229 | 11320 |
| Mean | 3086 | 3192 |
| Median | 2298 | 2540 |
| Skew | 1.21 | 1.88 |
| Kurt | 0.876 | 3.75 |



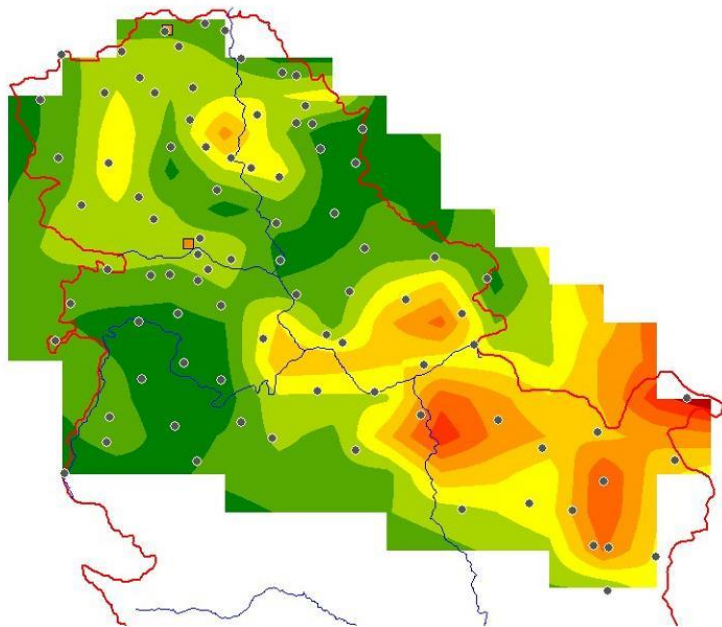
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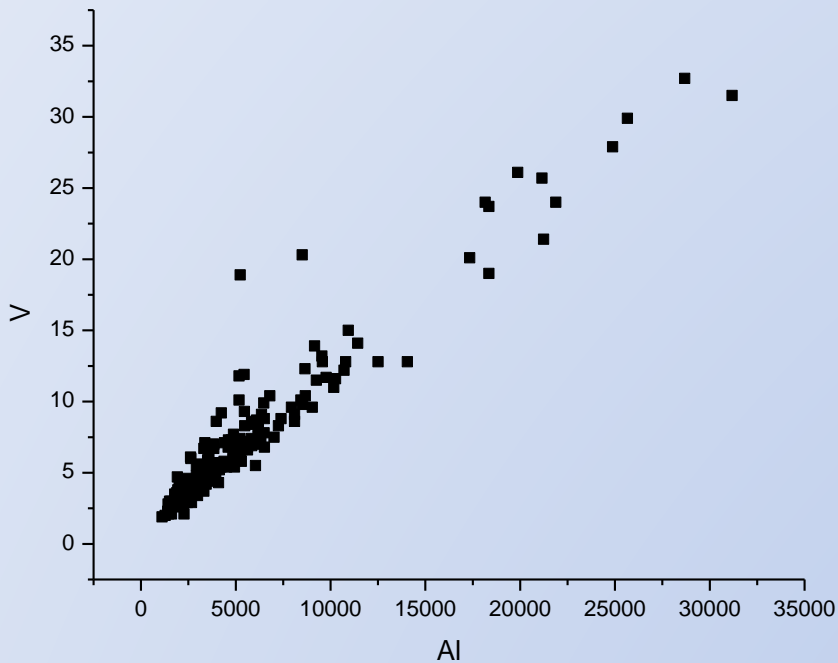
2005



2000

Fe





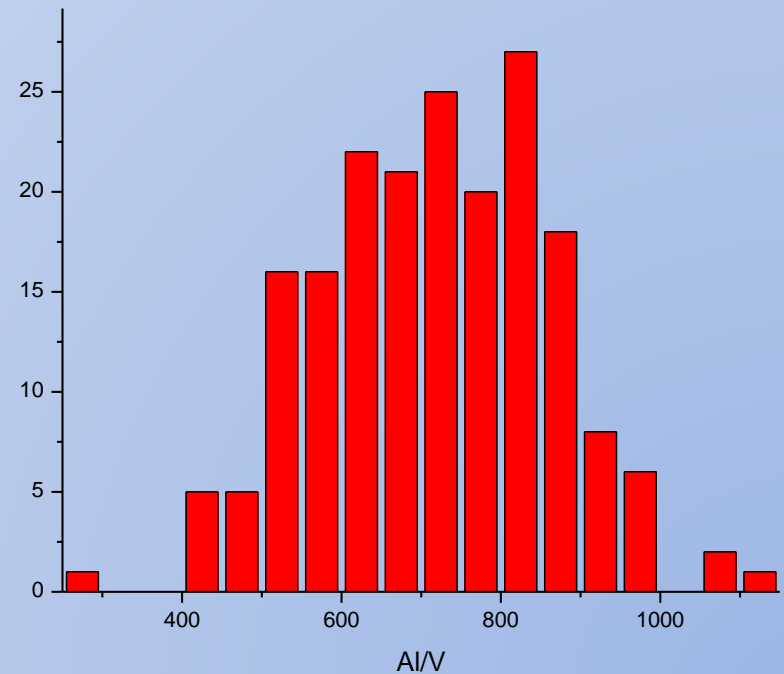
What about correlation between two elements measured in mosses?

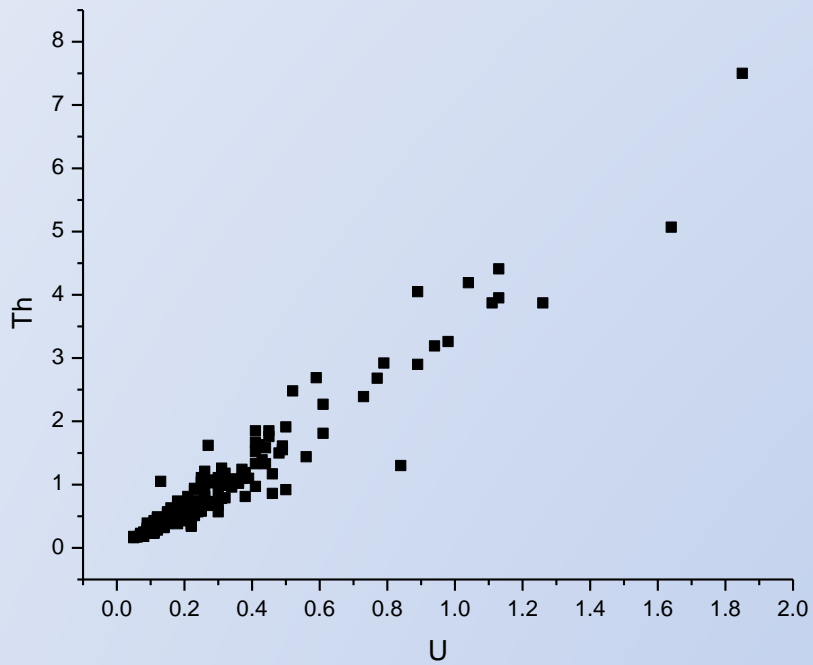
Ratio of two elements was calculated for all moss samples and distribution of obtained ratios was analyzed.

Skewness = - 0.02527

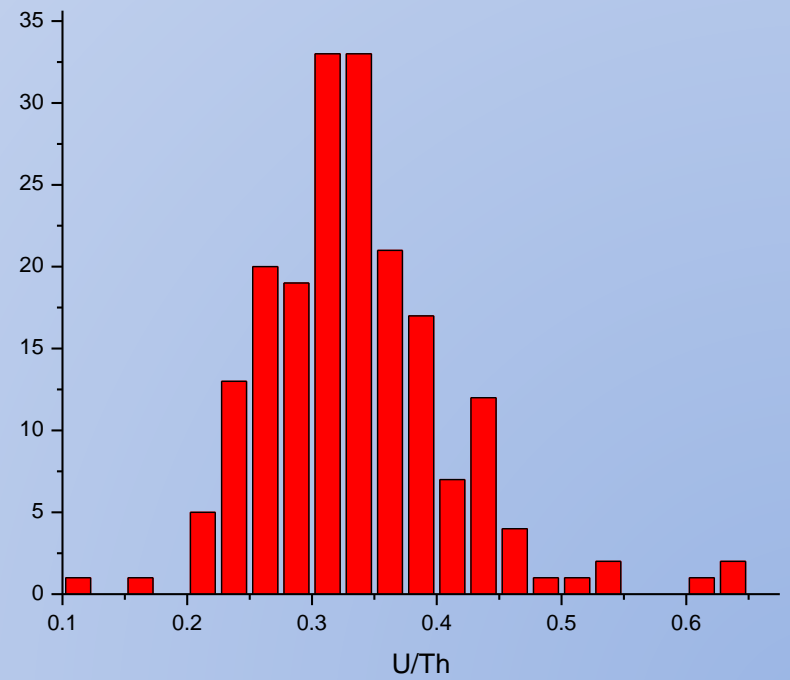
Kurtosis = - 0.1755

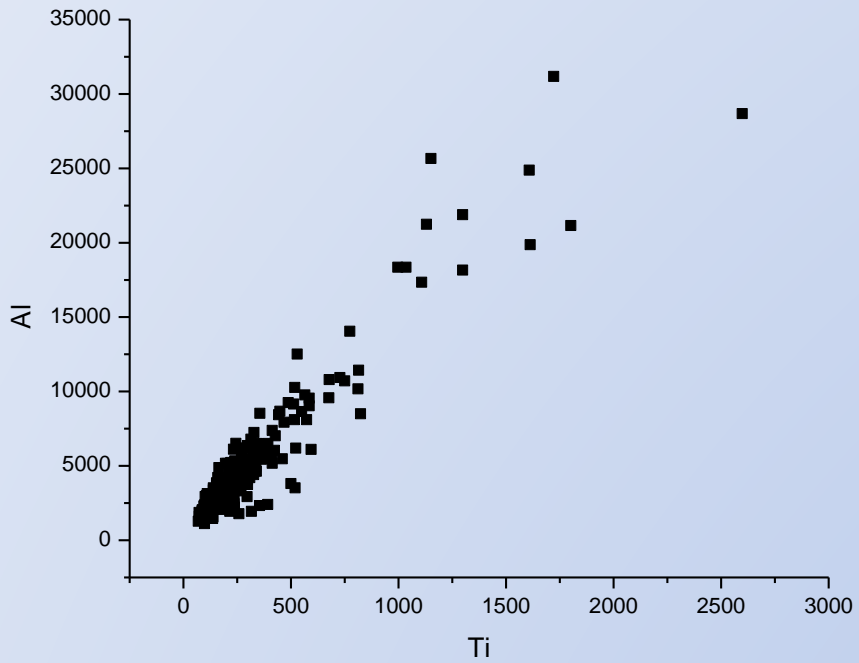
Good correlation – almost Gauss shape of distribution of calculated ratio.



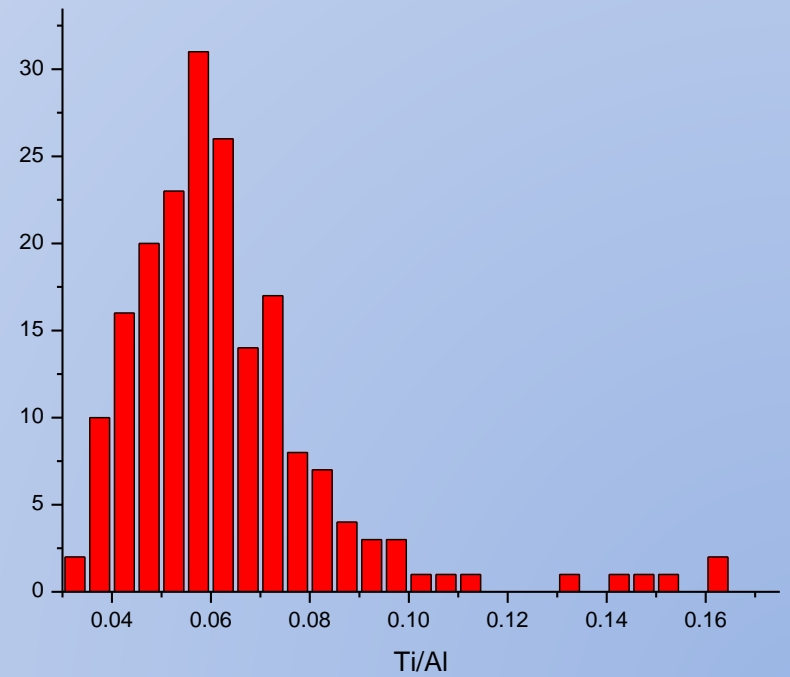


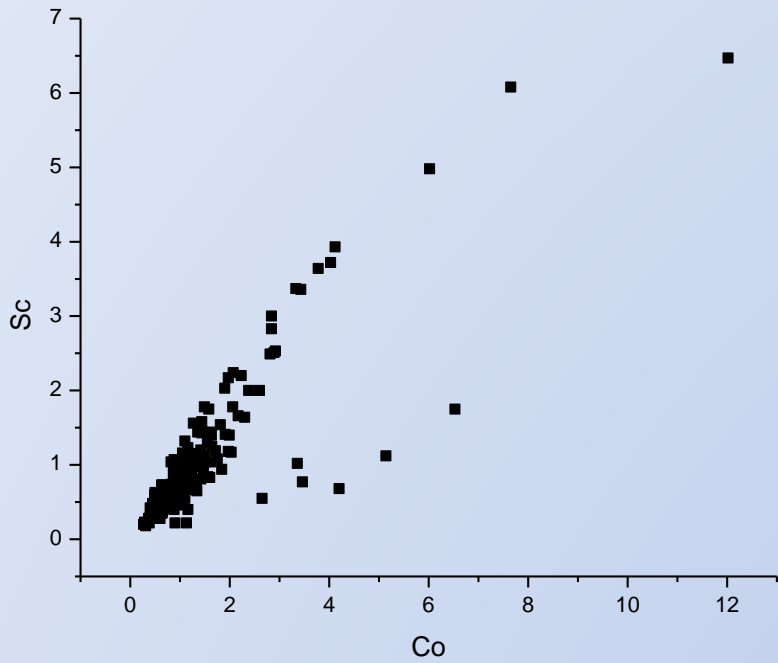
Skewness = 1.028
Kurtosis = 2.886



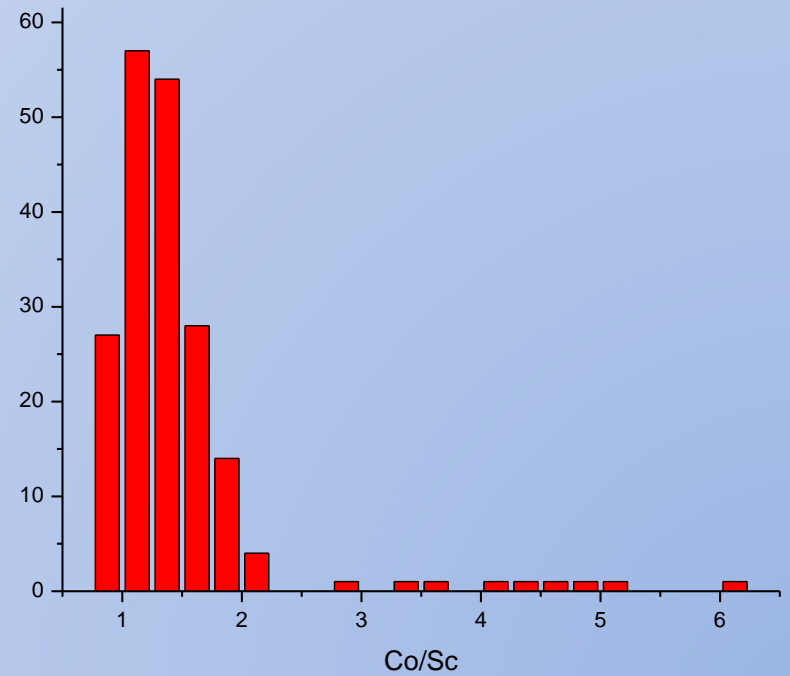


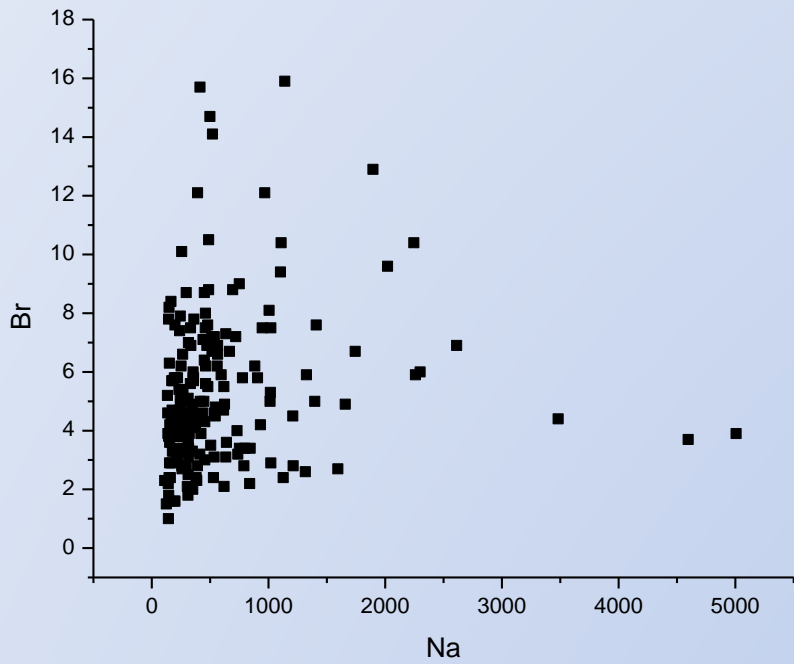
Skewness = 2.214
Kurtosis = 6.927



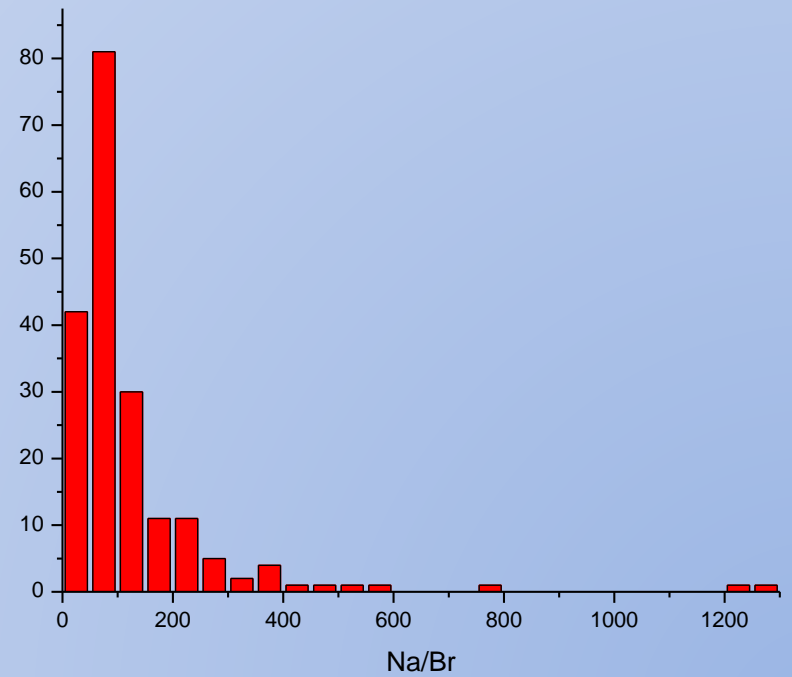


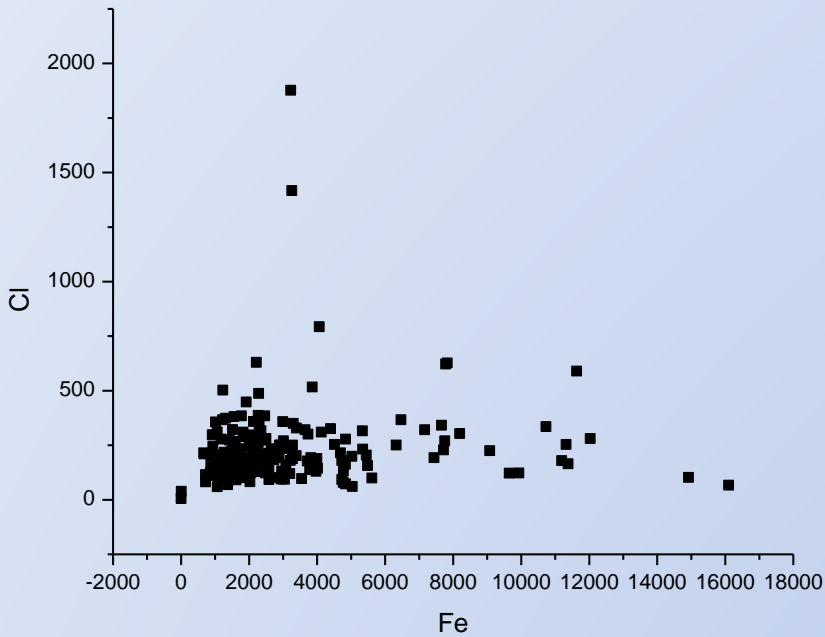
Skewness = 3.771
Kurtosis = 16.83





Skewness = 4.705
Kurtosis = 28.477



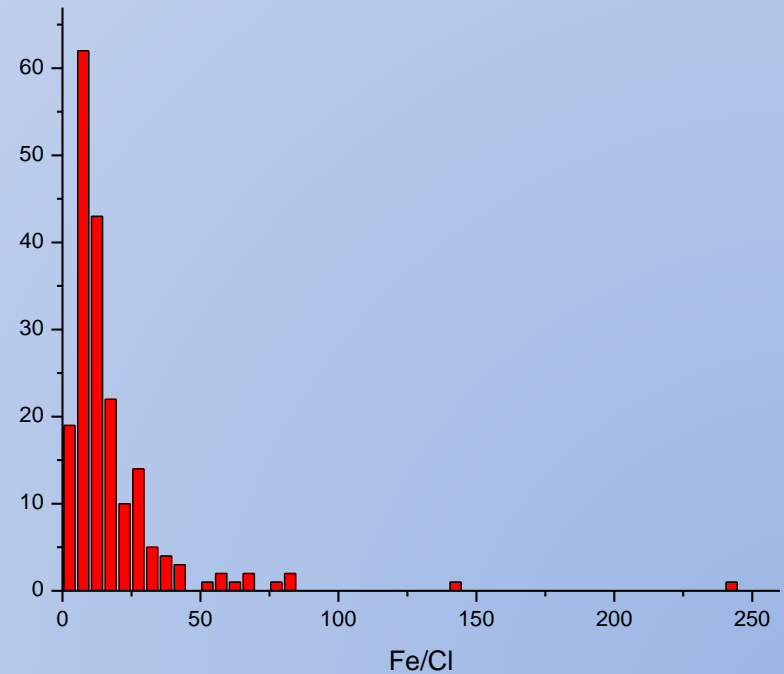


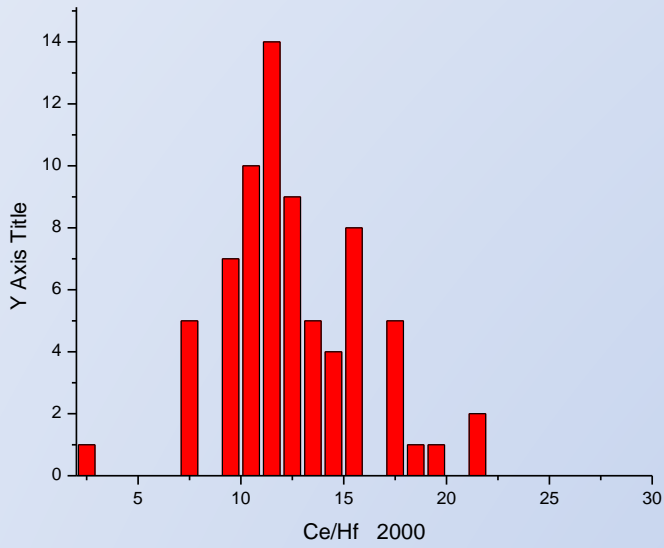
Very bad correlation – lognormal distribution of obtained ratios showing high values of skewness and kurtosis.

Skewness = 5.752

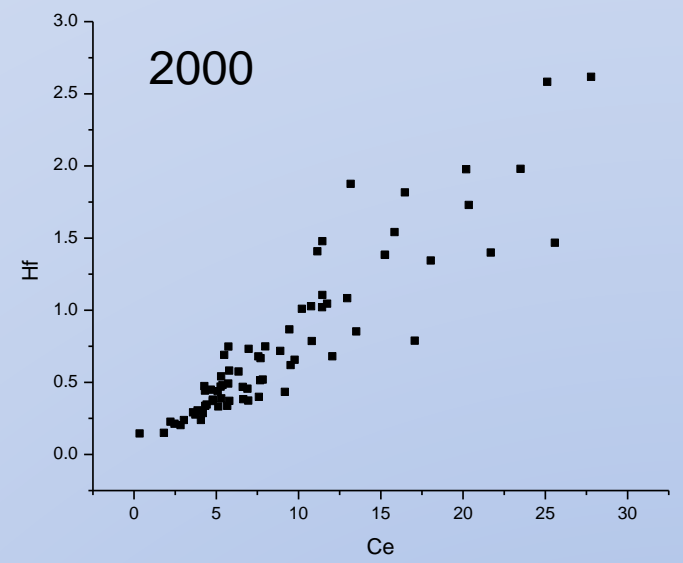
Kurtosis = 45.81

Skewness and kurtosis of ratio of two element concentration can be confident index of correlation.

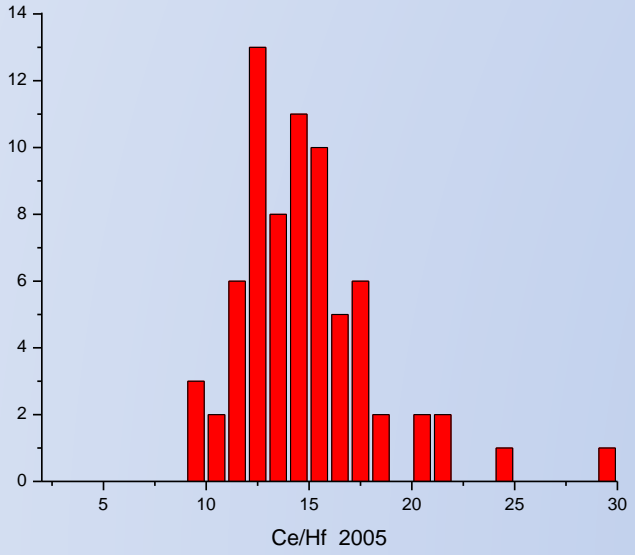




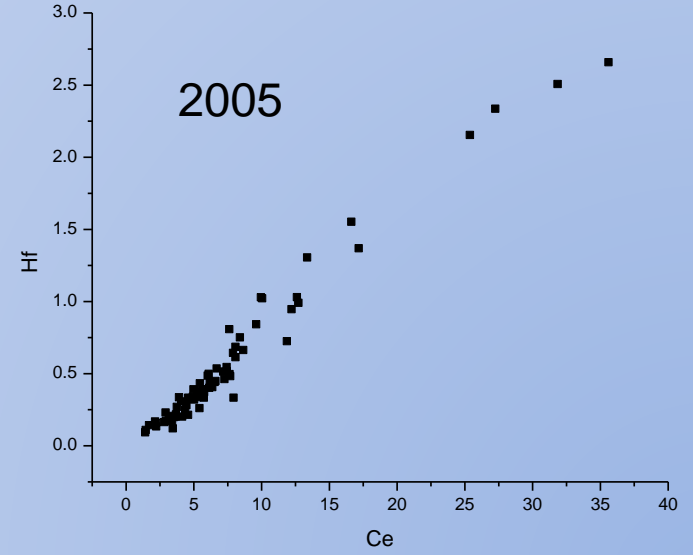
Mean = 12.6
 Median = 19
 Skew = 0.337
 Kurt = 0.958

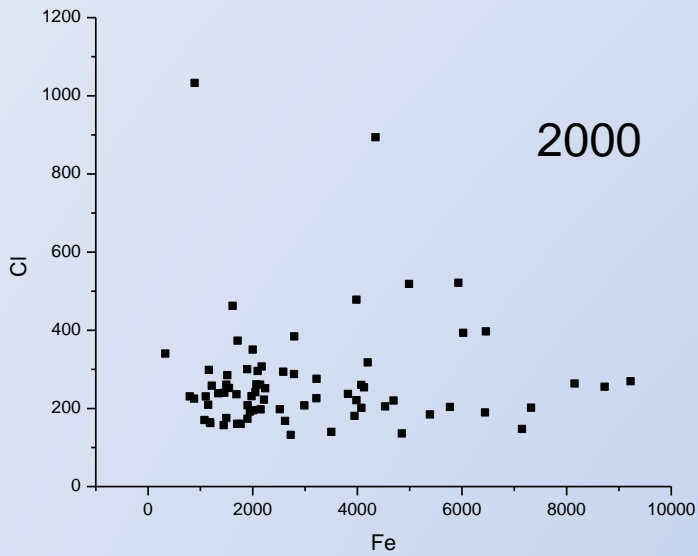


Skewness and kurtosis of ratios of two good correlated elements in two successive sampling.

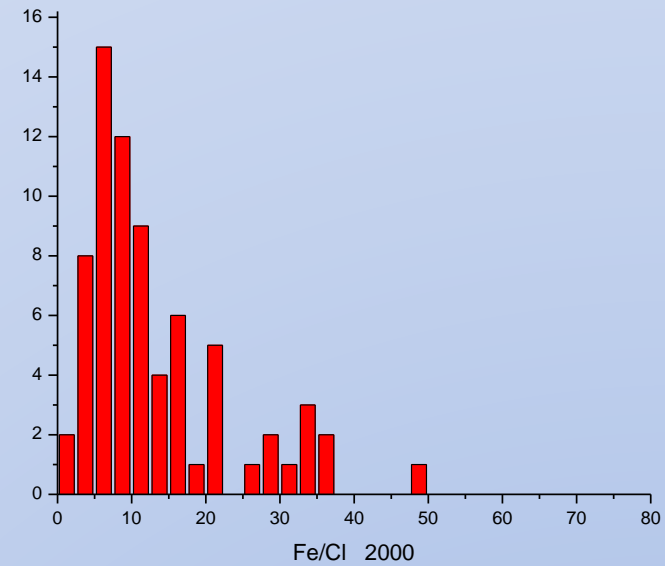


Mean = 14.8
 Median = 14.3
 Skew = 1.59
 Kurt = 4.52

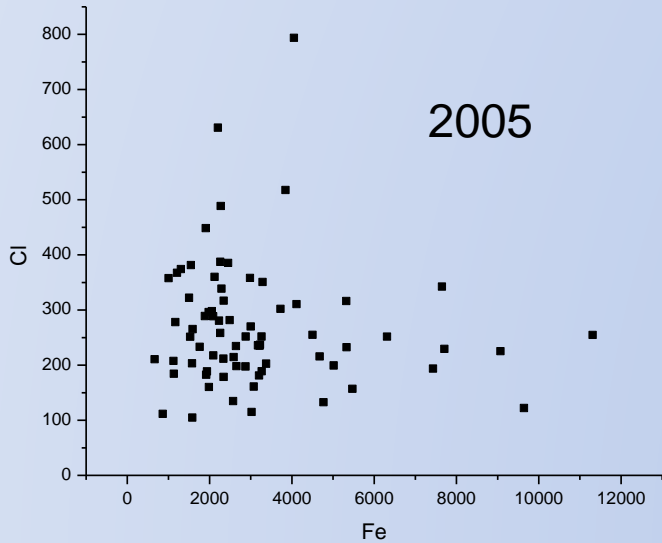




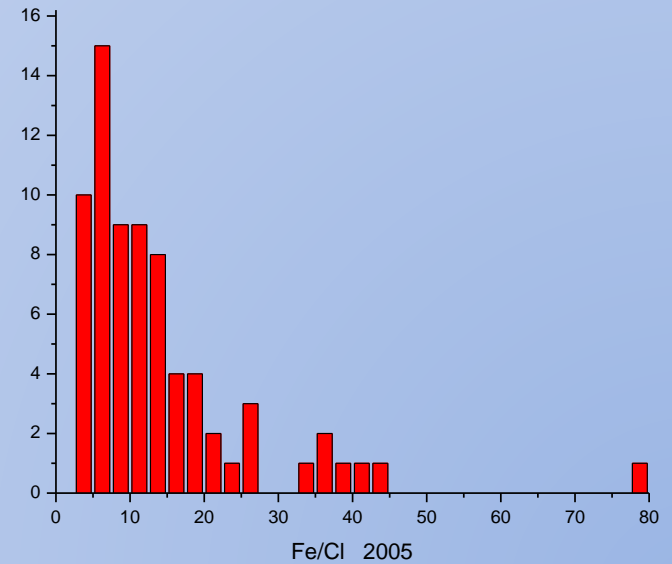
Mean = 13.2
 Median = 9.70
 Skew = 1.50
 Kurt = 1.94



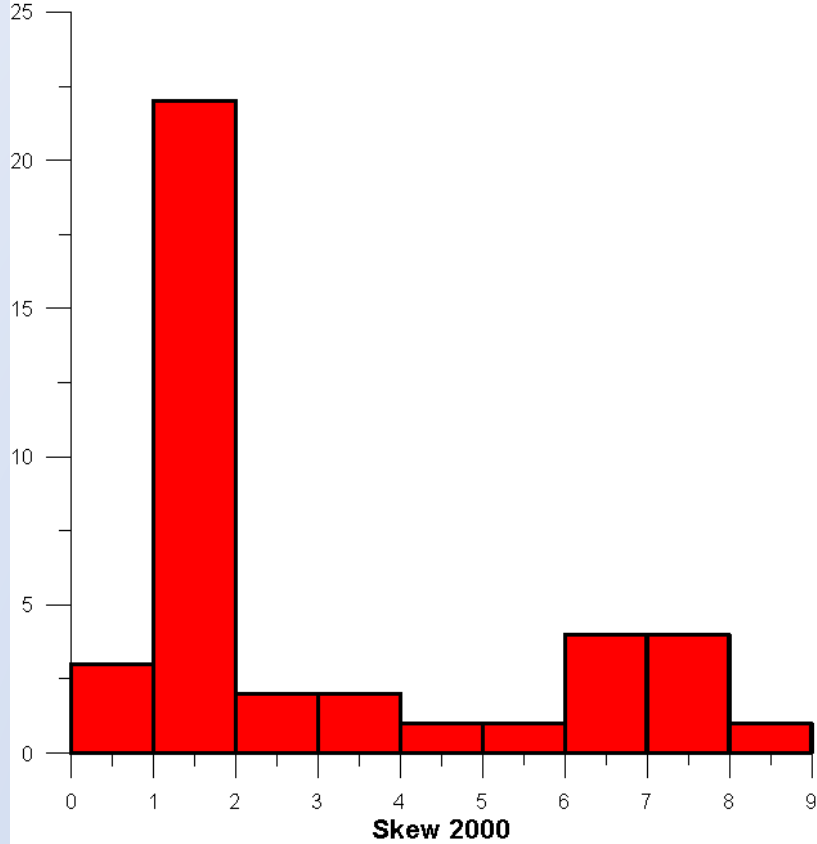
Skewness and kurtosis of ratios of two bad correlated elements in two successive sampling.



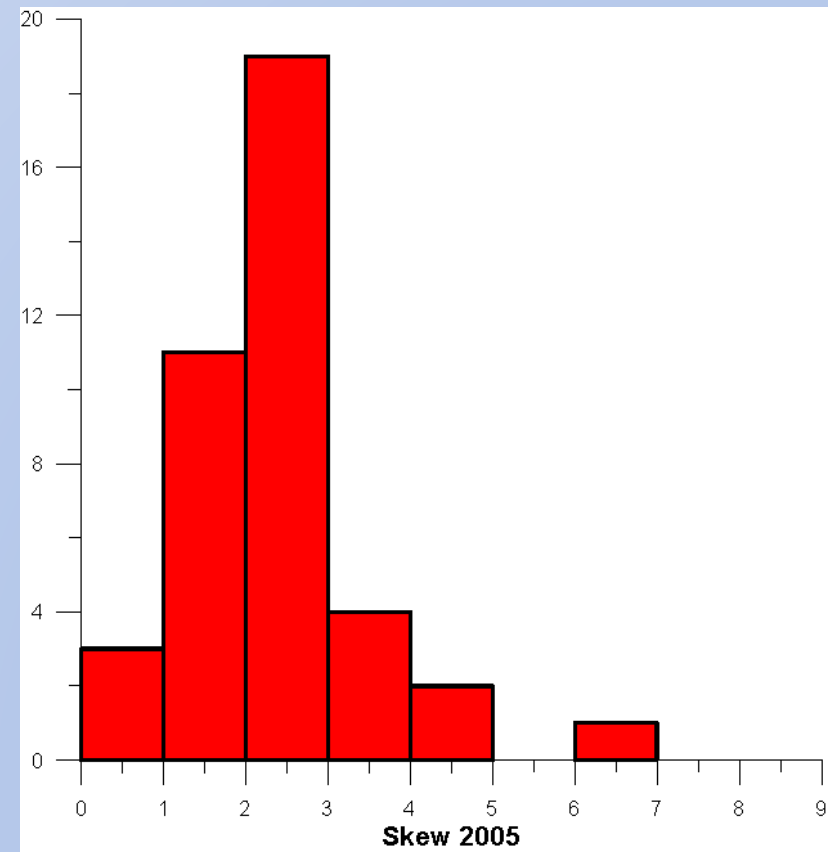
Mean = 14.1
 Median = 10.8
 Skew = 2.73
 Kurt = 10.5

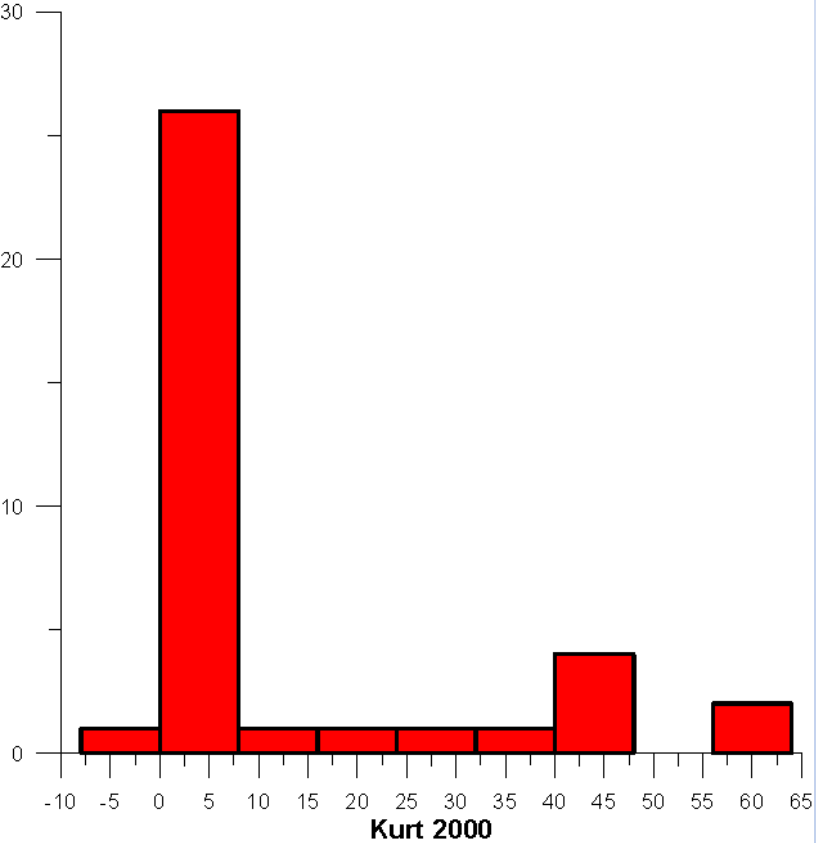


Distribution of skewness values obtained in two sets of data.



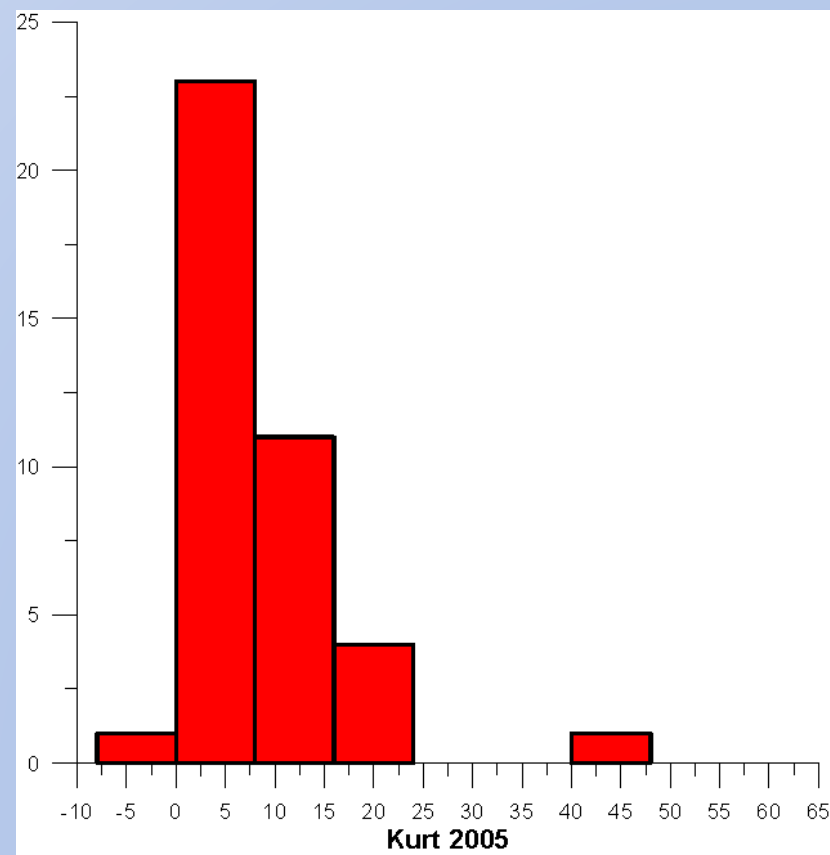
| | 2000 | 2005 |
|---------------|--------------|--------------|
| Min | 0.776 | 0.656 |
| Max | 8.10 | 6.42 |
| Mean | 2.96 | 2.44 |
| Median | 1.66 | 2.46 |





| | 2000 | 2005 |
|---------------|----------------|----------------|
| Min | - 0.355 | - 0.733 |
| Max | 67.5 | 47.7 |
| Mean | 16.34 | 8.39 |
| Median | 3.35 | 7.51 |

Distribution of kurtosis values obtained in two sets of data.



**It is just suggestion to think
together about it.**

Thank you!!!!