Naturalness of the Standard Model and Higgs boson

Victor T. Kim

Petersburg Nuclear Physics Institute NRC KI, Gatchina
St. Petersburg Polytechnic University

Outline:

- **Running masses in the standard model (SM)**
- **Higgs boson mass evolution and naturalness problem**
- **the standard model: naturalness, hierarchy & fine-tuning and new physics**
- **Summary**

In collaboration with G. Pivovarov (INR RAS, Moscow)

Running masses in the standard model

Running couplings: α_{QCD}, α_{EW}

Running masses

Different mass parameterizations
(different approaches to include higher orders):

- **pole (on-shell) mass**
- **running mass**

SM running masses

- **fermions and vector bosons: logarithmic**
- **scalar Higgs boson: logarithmic or/and quadratic ?**

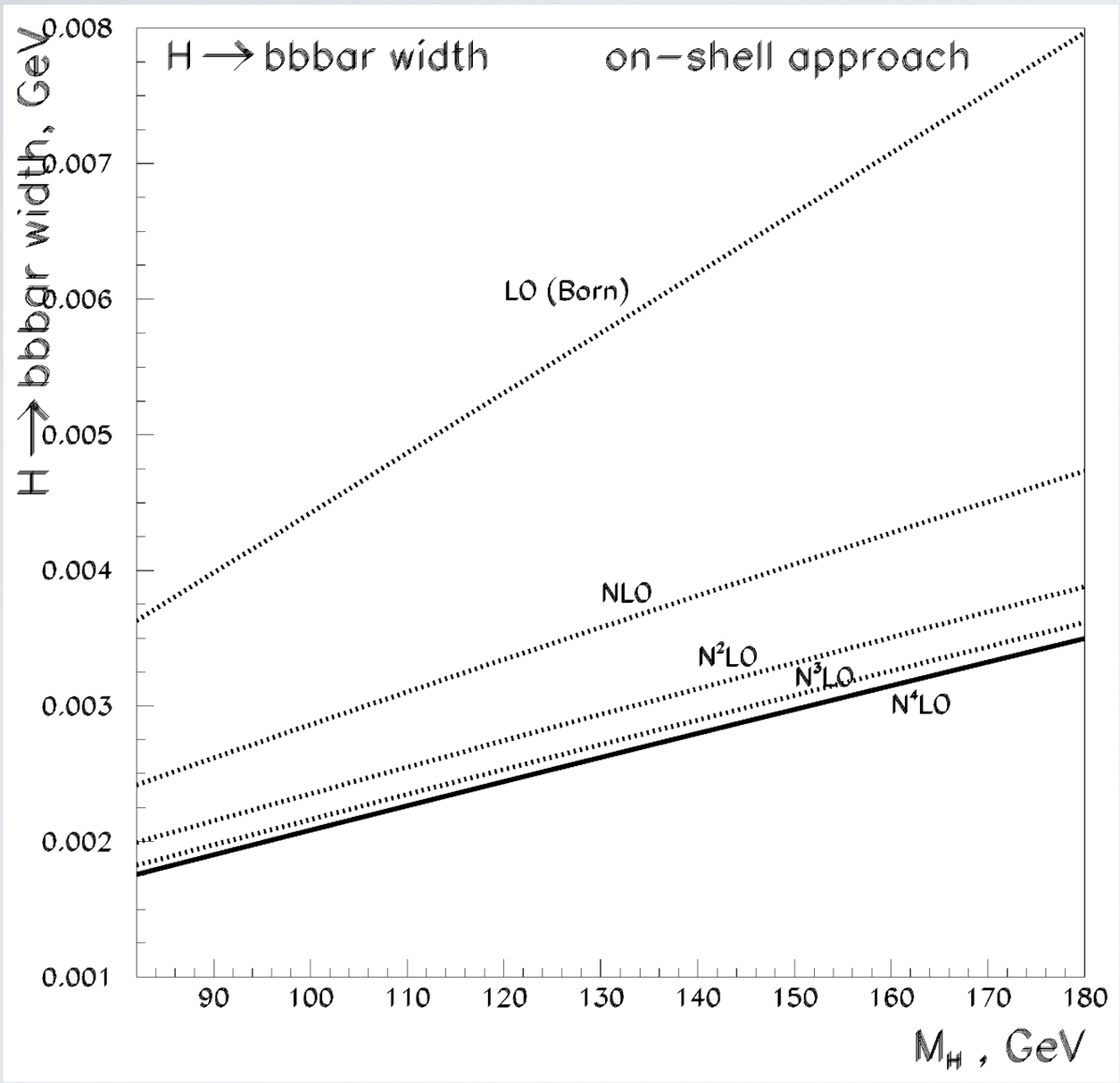
quadratic -> “non-naturalness”

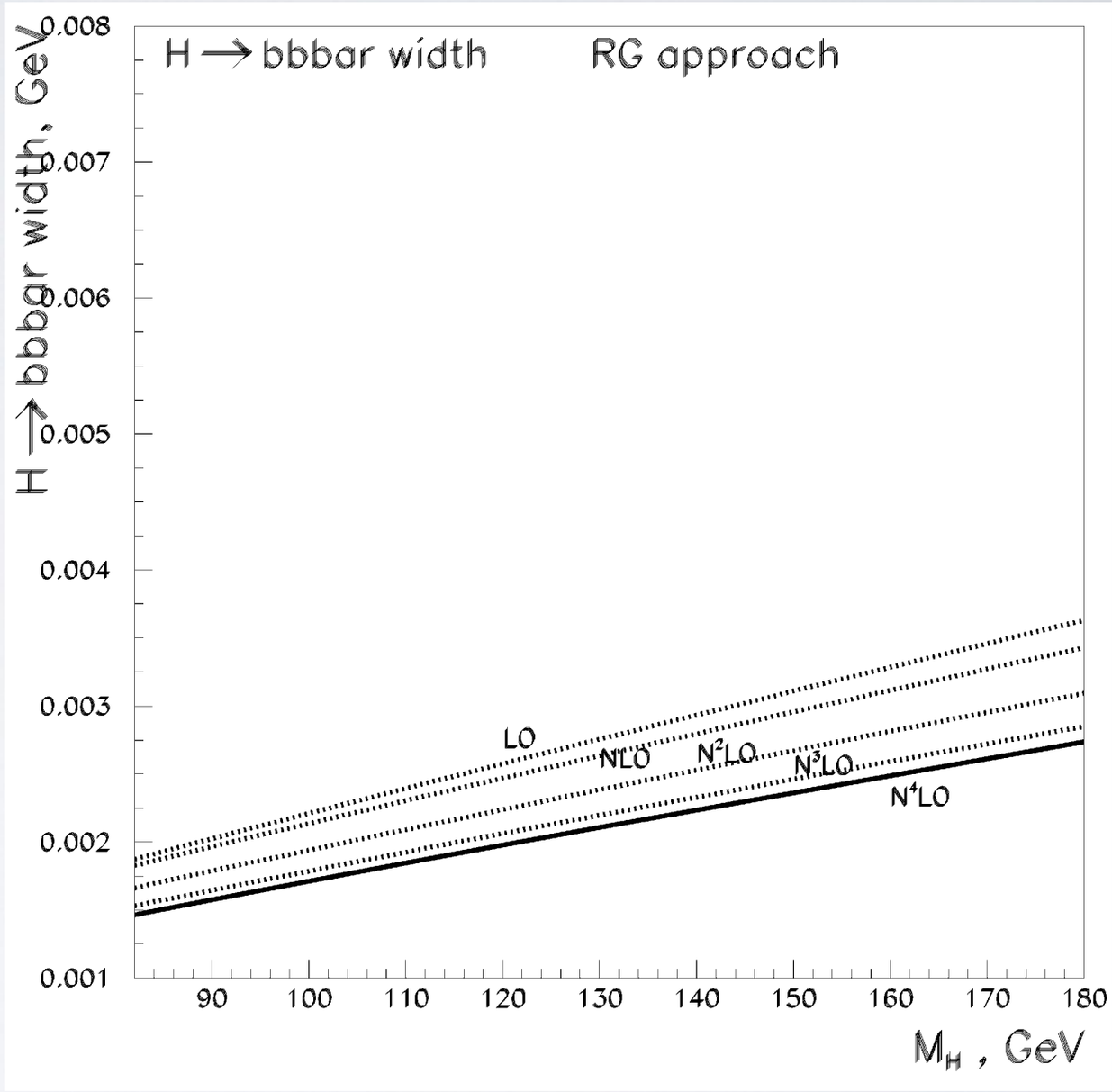
Higgs boson decay width

Width of Higgs boson decay into b-quarks (up to N⁴LO)

P. Baikov, K. Chetyrkin, J. Kuhn (2006)

A. Kataev, V. K. (2008)





b-quark mass - 4.5 GeV Upsilon

- 2.8 GeV Higgs boson

Higgs boson of Standard Model

Higgs boson discovery of CMS and ATLAS in 2012 is most important physics result at LHC upto now

ATLAS, Phys. Lett. B 716 (2012) 1
CMS, Phys. Lett. B 716 (2012) 30

Brout-Englert-Higgs-Guralnik-Hagen-Kibble mechanism of spontaneous symmetry breaking

R. Brout, F. Englert, Phys. Rev. Lett. 13 (1964) 321
P.W. Higgs, , Phys. Lett. 12 (1964) 132; Phys. Rev. Lett. 13 (1964) 508
G.S. Guralnik, C.R. Hagen, T.W.B. Kibble, Phys. Rev. Lett. 13 (1964) 585

P. Higgs & F. Englert: Nobel Prize (2013)

Higgs boson is only scalar elementary particle known up to now

Standard Model with 125 GeV Higgs boson

Higgs boson: if logarithmic mass evolution

Higgs boson defines electroweak vacuum density
(meta)stable vacuum up to Planck scales

F. Bezrukov, M. Kalmykov, B. Kiehl & M. Shaposhnikov, JHEP 10 (2012) 140

One may conclude:
(Almost) no need for a New Physics up to Planck scales
Only needs:
- (~ 1 GeV) BSM neutral leptons to explain Dark Matter
- strong CP-problem
- neutrino masses
- baryon-antibaryon asymmetry

...

- and still explain why there is naturalness (New Physics?!)

Standard Model with 125 GeV Higgs boson

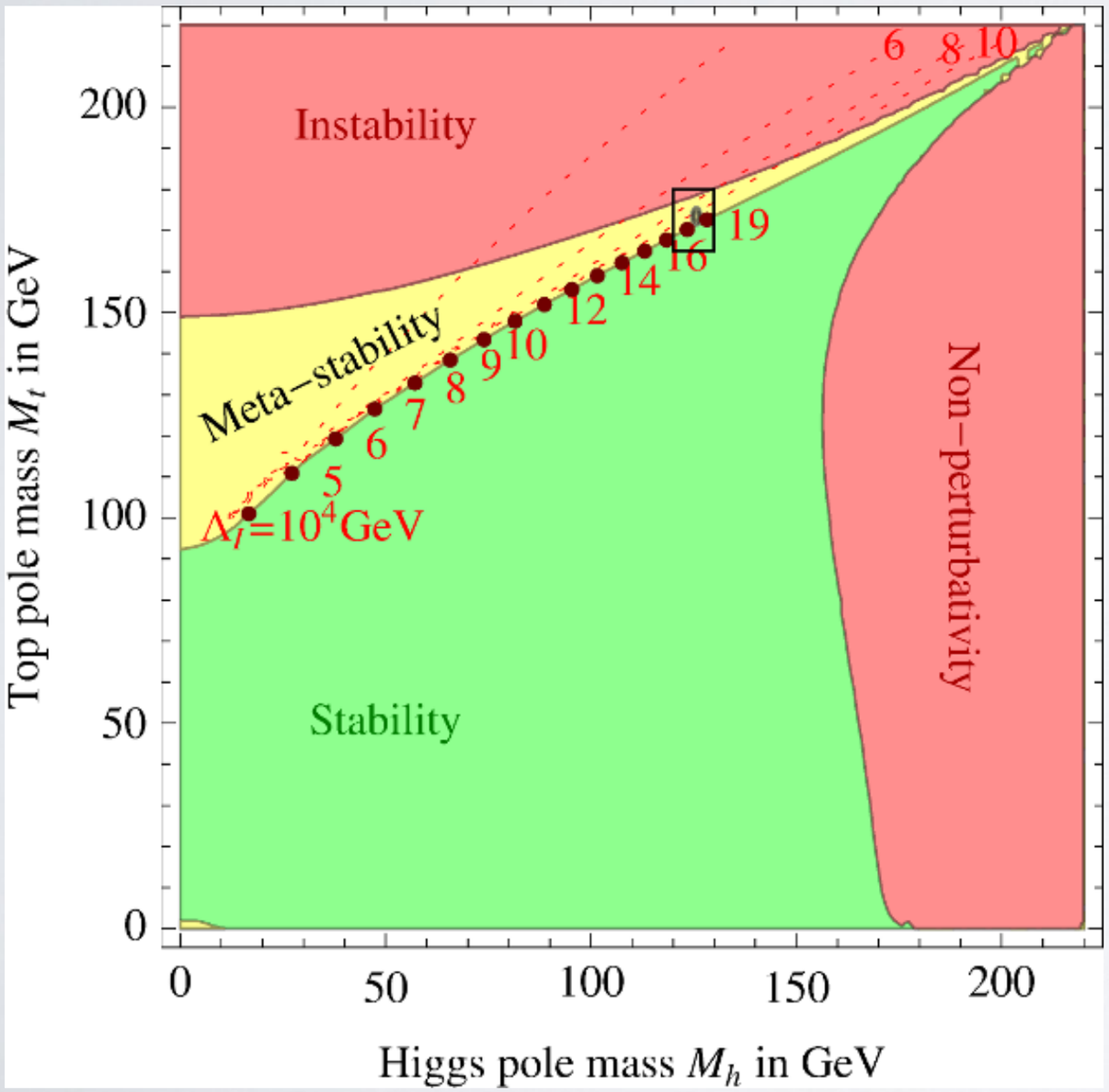
Higgs boson mass defines electroweak vacuum density

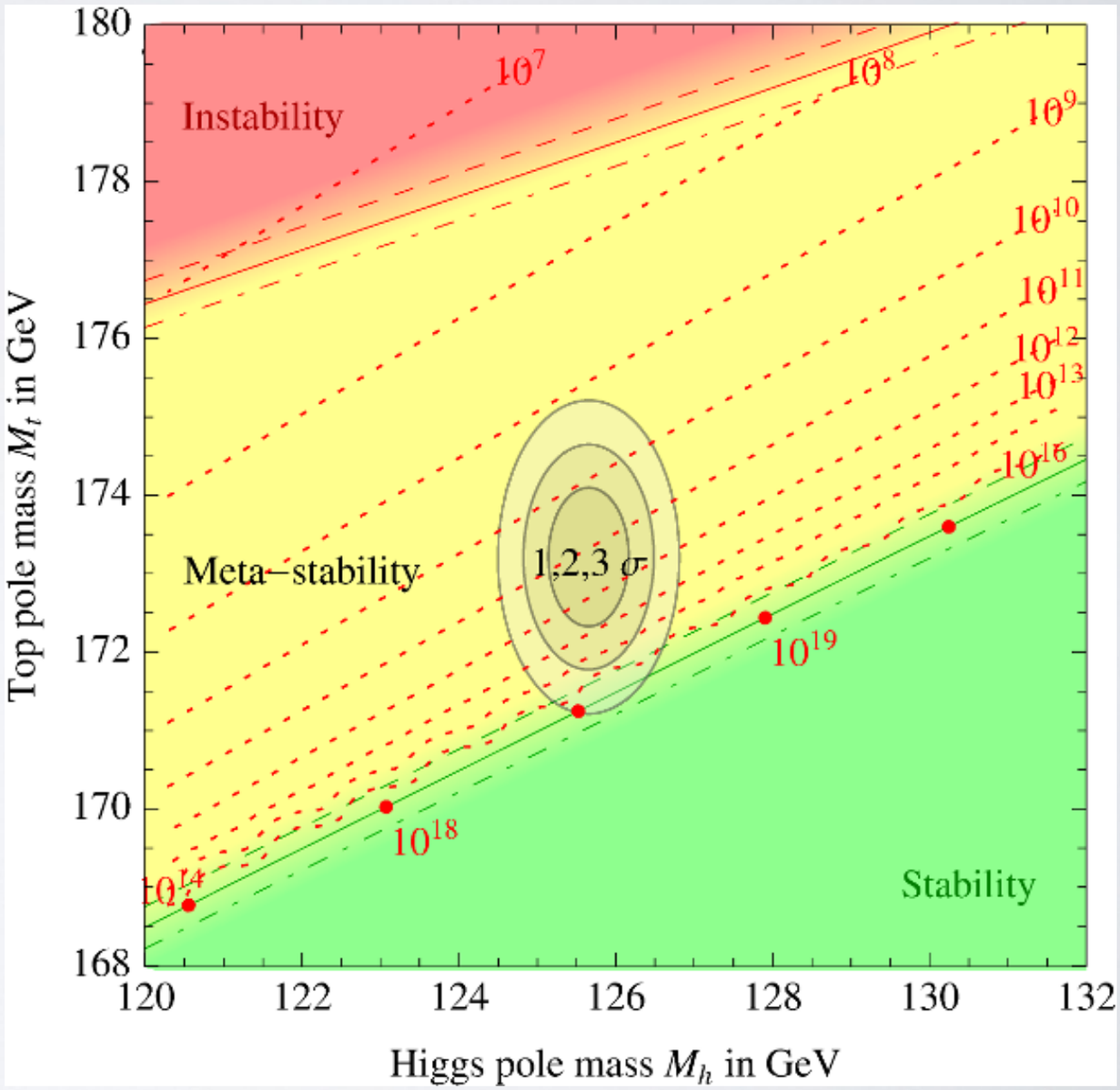
Meta-stable vacuum

G. Degrassi et al., JHEP 08 (2012) 098

D. Butazzo et al., JHEP 12 (2013) 089

A. Bednyakov et al., Phys. Rev. Lett. 115 (2015) 201802

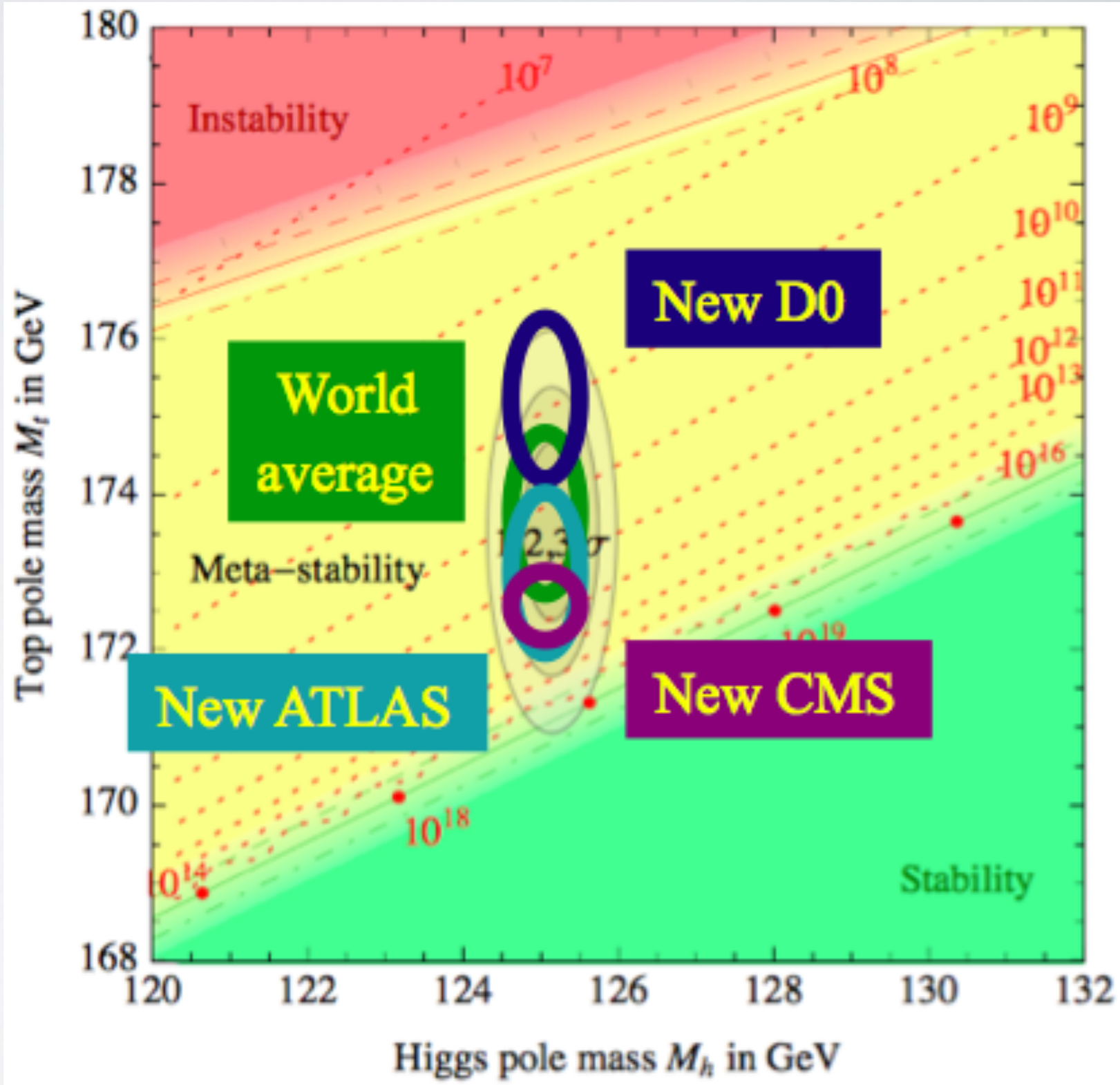




Standard Model vacuum stability vs new LHC data

J. Ellis, arXiv: 1702.05436 (2017)

D. Butazzo et al., JHEP 12 (2013) 089



(Non-)Naturalness of the standard model

Logarithmic evolution of theory parameters:
weak dependence between low and very large scales
-> concept of ”Naturalness”

- **Scalar field is simple, but “non-natural”:**
  scalar mass evolution is quadratic, not logarithmic

  K. Wilson, Phys. Rev. D3 (1971) 1818
  L. Susskind, Phys. Rev. D20 (1979) 2619

- **Scalar field is not protected by a symmetry,**
  while fermions are protected by chiral symmetry

  G. ‘t Hooft, Proc. Cargese Summer Inst. (1980)

  for reviews see G. Giudice, (2008)

Standard Model: Higgs boson mass evolution

The previously discussed calculations were done within MSbar renormalization: based on popular dimensional regularization (DR)

-> no quadratic mass divergences in “standard” prescription

Also, used as an argument for a necessity of SUSY

R. Barbieri, G.F. Giudice, Nucl. Phys. B306 (1988) 63

Physical renormalization: momentum substraction (MOM) scheme

-> there are quadratic mass divergences

Naturalness of the Standard Model in 1-loop

M. Veltman, Acta Phys. Pol. B12 (1981) 437

renormalization scheme dependence for scalar particles:

$$m_H^2 = m_{0H}^2 + C_L(\lambda_i, m_i) \cdot \log(\frac{\Lambda_{UV}^2}{m^2}) + C_X(\lambda_i, m_i) \cdot \Lambda_{UV}^2$$

"physical" schemes $\rightarrow C_X \neq 0$
schemes with dim. regularization ($\overline{\text{MS}}$, ...) $\rightarrow C_X = 0$

MSbar reproduces quadratic divergence at D = 2, L=1

$$m_H^2 = m_{H0}^2 + \delta m_H^2 \qquad v = 246\,\text{GeV}$$

$$\delta m_H^2 \approx \frac{\Lambda^2}{16\pi^2}\left(24y_t^2 - 6(2y_W^2 + y_Z^2 + y_H^2)\right) \sim 8.2\frac{\Lambda^2}{16\pi^2} \qquad y_i \equiv \frac{m_i}{v}$$

Non-naturalness of Higgs boson at Λ > 550 GeV (Veltman criterion):

$$\delta m_H^2 \approx m_H^2 \qquad (\Lambda = 550\,\text{GeV},\ m_H = 125\,\text{GeV})$$

Standard Model: Higgs boson mass evolution

M. Veltman, Acta Phys. Pol. B12 (1981) 437
quadratic mass divergences within MSbar renormalization:
Dim = 4 – 2/L

$$m_R^2 = m_B^2 + P\,\Lambda^2,$$

where P = P (mH, mt, mW, mZ)

Veltman condition for absence of quadratic mass divergences:

$$P = 0$$

Veltman condition holds up to 2-loops:
but in higher orders it cannot be hold in self-consistent way
M.S. Al-sarhi, I. Jack, D.R.T. Jones,
Nucl. Phys. B345 (1990) 431, Zeit fur Physik C55 (1992) 283

Veltman condition and Higgs effective potential
M.B. Einhorn, D.R.T. Jones, Phys. Rev. D42 (1992) 5206

Naturalness of Standard Model

Barbieri-Giudice (BG) condition:
sensitivity physical parameters for small variation of bare ones
R. Barbieri, G.F. Giudice, Nucl. Phys. B306 (1988) 63

Using BG condition with both quadratic and logarithmic contributions leads to extention of Naturalness domain of SM:
up ~ O(10 TeV) instead of ~ O (1 TeV)
VK, G. Pivovarov, Phys. Rev. D78 (2008) 016001

Regular way for scalar boson mass evolution with quadratic mass divergences
G. Pivovarov, Phys. Rev. D81 (2010) 076077

Landau pole like in λH^4:

$$\lambda(Q) \simeq \frac{\lambda(v)}{1 - \frac{3}{4\pi^2}\lambda(v)\ln\left(Q^2/v^2\right)}$$

Standard Model: Higgs boson roles

- provide mass to SM particles by
  Brout-Englert-Higgs mechanism

- restore unitarity for EW vector boson scattering:
  Higgs boson cancels quadratic growth
  of longitudinal components for EW vector bosons
  with collision energy

- if Higgs could be very light -> no noticeable growth
  with collision energy

- if Higgs could be very heavy ->
  strong growth of EW vector boson interaction ->
  New SM dynamics: nonpertubative strong EW interaction
  can lead to heavy EW resonances

SM with “non-natural” Higgs boson

Proper physical consideration with quadratic evolution for Higgs boson mass:

Higgs boson observables (mass, self-coupling, EW vacuum density) gets critical values at larger scales than in popular “standard” treatments with scale ~ O(1 TeV)

-> only at the scales ~ O(10 TeV) one should expect new physics manifestations:
- **new strong EW dynamics**
- **or/and New Physics beyond Standard Model**

Summary

- **Standard Model without quadratic evolution for Higgs boson mass requires (!) New Physics to have Naturalness**

- **Naturalness domain of Standard Model with quadratic evolution for Higgs boson mass may be larger than generally accepted: up ~ O(10 TeV) instead of ~ O (1 TeV)**

- **Present LHC physics: new physics is unavoidable either as a new dynamics of SM or/and a New Physics. Besides search direct search of New Physics it requires 'non-naturalness' studies (talk by M. Gouzevitch)**