

# Estimates for the single-spin asymmetries in $p^\uparrow p \rightarrow J/\psi X$ process at PHENIX RHIC and SPD NICA

A. V. Karpishkov<sup>1,2</sup>, M. A. Nefedov<sup>1</sup>, and V. A. Saleev<sup>1,2</sup>

<sup>1</sup> Samara National Research University

<sup>2</sup> Joint Institute for Nuclear Research

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Gluon content of proton and deuteron with the Spin Physics Detector at the  
NICA collider

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## The "incomplete" list of relevant recent articles

- U. D'Alesio, C. Flore, F. Murgia, C. Pisano and P. Tael, "Unraveling the Gluon Sivers Function in Hadronic Collisions at RHIC," Phys. Rev. D **99**, no.3, 036013 (2019)
- U. D'Alesio, L. Maxia, F. Murgia, C. Pisano and S. Rajesh, "Process dependence of the gluon Sivers function in  $p^\uparrow p \rightarrow J/\psi + X$  within a TMD approach in NRQCD," [arXiv:2007.03353 [hep-ph]].
- U. D'Alesio, F. Murgia, C. Pisano and S. Rajesh, "Single-spin asymmetries in  $p^\uparrow p \rightarrow J/\psi + X$  within a TMD approach: role of the color octet mechanism," Eur. Phys. J. C **79**, no.12, 1029 (2019)
- U. D'Alesio, F. Murgia, C. Pisano and P. Tael, "Probing the gluon Sivers function in  $p^\uparrow p \rightarrow J/\psi X$  and  $p^\uparrow p \rightarrow D X$ ," Phys. Rev. D **96**, no.3, 036011 (2017)
- R. M. Godbole, A. Kaushik, A. Misra, V. Rawoot and B. Sonawane, "Transverse single spin asymmetry in  $p + p^\uparrow \rightarrow J/\psi + X$ ," Phys. Rev. D **96**, no.9, 096025 (2017)

# Generalized Parton Model (GPM)

## Factorization schemes

The Collinear Parton Model (CPM) is applicable in a region of high- $p_T$  production

$$p_T \gg 1\text{GeV},$$

so we can neglect small intrinsic  $\mathbf{q}_T$  of initial partons ( $\langle q_T^2 \rangle \simeq 1 \text{ GeV}^2$ ).

If we're interested in particle production in a region of

$p_T \simeq \sqrt{\langle q_T^2 \rangle} \ll \mu_F \simeq m_{J/\psi}$ , we should take into account intrinsic  $q_T$  within TMD approach, [J. Collins, *Camb. Monogr., Part. Phys. Nucl. Phys. Cosmol.* 32, 1-624 (2011)].

Here we use phenomenological TMD-based approach, Generalized Parton Model (GPM), where simple prescription for TMD parton distribution functions (PDFs) is used:

$$F_a(x, q_T, \mu_F) = f_a(x, \mu_F) \times G_a(q_T), \quad (1)$$

where  $f_a(x, \mu_F)$  – corresponding collinear PDF,  $G_a(q_T)$  – Gaussian distribution

$$G_a(q_T) = \exp(-q_T^2 / \langle q_T^2 \rangle_a) / (\pi \langle q_T^2 \rangle_a)$$

# Factorization formula for the GPM

Within the GPM we can write the differential cross-section as follows

$$d\sigma(pp \rightarrow CX) = \int dx_1 \int d^2\mathbf{q}_{1T} \int dx_2 \int d^2\mathbf{q}_{2T} \times \\ \times F_g(x_1, q_{1T}, \mu_F) F_g(x_2, q_{2T}, \mu_F) d\hat{\sigma}(gg \rightarrow C), \quad (2)$$

where  $C = J/\psi, \psi(2S)$  or  $\chi_c(1P)$ .

For  $2 \rightarrow 1$  hard subprocess  $g(q_1) + g(q_2) \rightarrow C(k)$ :

$$d\hat{\sigma}(gg \rightarrow C) = (2\pi)^4 \delta^{(4)}(q_1 + q_2 - k) \frac{|\overline{M(gg \rightarrow C)}|^2}{2x_1 x_2 s} \frac{d^4 k}{(2\pi)^3} \delta_+(k^2 - m_C^2). \quad (3)$$

In a case of  $2 \rightarrow 2$  subprocess  $g(q_1) + g(q_2) \rightarrow C(k) + g(q_3)$ ,  $C = J/\psi, \psi(2S)$  :

$$d\hat{\sigma}(gg \rightarrow Cg) = (2\pi)^4 \delta^{(4)}(q_1 + q_2 - k - q_3) \frac{|\overline{M(gg \rightarrow Cg)}|^2}{2x_1 x_2 s} \frac{d^3 k}{(2\pi)^3 2k_0} \frac{d^4 q_3}{(2\pi)^3} \delta_+(q_3^2). \quad (4)$$

# Transverse Single Spin Asymmetry

In inclusive process  $p^\uparrow p \rightarrow CX$   $C = J/\psi, \chi_c, \psi(2S)$ ) TSSA is defined as:

$$A_N = \frac{d\sigma^\uparrow - d\sigma^\downarrow}{d\sigma^\uparrow + d\sigma^\downarrow} = \frac{d\Delta\sigma}{2d\sigma}. \quad (5)$$

The numerator and denominator of  $A_N$  have the form:

$$d\sigma \propto \int dx_1 \int d^2 q_{1T} \int dx_2 \int d^2 q_{2T} F_g(x_1, q_{1T}, \mu_F) F_g(x_2, q_{2T}, \mu_F) d\hat{\sigma}(gg \rightarrow CX), \quad (6)$$

$$d\Delta\sigma \propto \int dx_1 \int d^2 q_{1T} \int dx_2 \int d^2 q_{2T} [\hat{F}_g^\uparrow(x_1, \mathbf{q}_{1T}, \mu_F) - \hat{F}_g^\downarrow(x_1, \mathbf{q}_{1T}, \mu_F)] \\ \times F_g(x_2, q_{2T}, \mu_F) d\hat{\sigma}(gg \rightarrow CX), \quad (7)$$

where  $\hat{F}_g^{\uparrow,\downarrow}(x, q_T, \mu_F)$  is the distribution of unpolarized gluon (or quark) in polarized proton.

Following the Trento conventions [A. Bacchetta, U. D'Alesio, M. Diehl and C. A. Miller, *Phys. Rev. D* **70**, 117504 (2004)], the gluon Sivers function (GSF) can be introduced as

$$\begin{aligned} \Delta\hat{F}_g^\uparrow(x_1, \mathbf{q}_{1T}, \mu_F) &\equiv \hat{F}_g^{(\uparrow)}(x_1, \mathbf{q}_{1T}, \mu_F) - \hat{F}_g^{(\downarrow)}(x_1, \mathbf{q}_{1T}, \mu_F) \\ &= \Delta^N F_g^\uparrow(x_1, \mathbf{q}_{1T}^2, \mu_F) \cos(\phi_1). \end{aligned} \quad (8)$$

## Parameterizationa for GSF

Gluon Sivers function may be presented in the form

$$\Delta^N F_g^\uparrow(x, q_T^2, \mu_F) = 2 \frac{\sqrt{2}e}{\pi} N_g(x) f_g(x, \mu_F) \sqrt{\frac{1 - \rho_g}{\rho_g}} \frac{q_T}{\langle q_T^2 \rangle_g^{3/2}} e^{-q_T^2 / \rho_g \langle q_T^2 \rangle_g}. \quad (9)$$

GSF set	$N_g$	$\alpha_g$	$\beta_g$	$\rho_g$	$\langle q_T^2 \rangle_g, \text{ GeV}^2$
SIDIS1	0.65	2.8	2.8	0.687	0.25
SIDIS2	0.05	0.8	1.4	0.576	0.25
D'Alesio <i>et al.</i>	0.25	0.6	0.6	0.1	1.0

Table: Parameters of GSFs



# Models of $J/\psi$ production: NRQCD and ICEM

## Basics of NRQCD factorization

The NRQCD framework [G. T. Bodwin, E. Braaten, and G. P. Lepage, *Phys. Rev. D* **51**, 1125 (1995)] describes heavy quarkonium in terms of Fock state decomposition:

$$|\mathcal{H}\rangle = \mathcal{O}(v^0)|Q\bar{Q}[{}^3S_1^{(1)}]\rangle + \mathcal{O}(v)|Q\bar{Q}[{}^3P_J^{(8)}]g\rangle + \mathcal{O}(v^2)|Q\bar{Q}[{}^1S_0^{(8)}]g\rangle \quad (10)$$

$$+ \mathcal{O}(v^2)|Q\bar{Q}[{}^3S_1^{(1,8)}]gg\rangle + \dots \quad (11)$$

In the NRQCD effects of short and long distances are separated, and cross-section of heavy-quarkonium production via a partonic subprocess  $a + b \rightarrow \mathcal{H} + X$  can be presented in a factorized form:

$$d\hat{\sigma}(a + b \rightarrow \mathcal{H} + X) = \sum_n d\hat{\sigma}(a + b \rightarrow Q\bar{Q}[n] + X) \times \langle \mathcal{O}^{\mathcal{H}}[n] \rangle, \quad (12)$$

where  $n$  denotes the set of quantum numbers of the  $Q\bar{Q}$  pair, and its transitions into  $\mathcal{H}$  is described by the Long-Distance Matrix Elements (LDMEs)  $\langle \mathcal{O}^{\mathcal{H}}[n] \rangle$ .

The partonic cross-section of quarkonium production from the  $Q\bar{Q}$  Fock state  $n = {}^{2S+1}L_J^{(1,8)}$  has the form:

$$d\hat{\sigma}(a + b \rightarrow Q\bar{Q}[{}^{2S+1}L_J^{(1,8)}] \rightarrow \mathcal{H}) = d\hat{\sigma}(a + b \rightarrow Q\bar{Q}[{}^{2S+1}L_J^{(1,8)}]) \times \frac{\langle \mathcal{O}^{\mathcal{H}}[{}^{2S+1}L_J^{(1,8)}] \rangle}{N_{col}N_{pol}},$$

where  $N_{col} = 2N_c$  for color-singlet state,  $N_{col} = N_c^2 - 1$  for color-octet state, and  $N_{pol} = 2J + 1$ .

## Amplitude of specified state

The definition of partonic cross-section of  $Q\bar{Q}[^{2S+1}L_J^{(1,8)}]$  production is following:

$$d\hat{\sigma}(a+b \rightarrow Q\bar{Q}[^{2S+1}L_J^{(1,8)}]) = \frac{1}{2x_1x_2S} \overline{|\mathcal{A}(a+b \rightarrow Q\bar{Q}[^{2S+1}L_J^{(1,8)}])|^2} d\Phi. \quad (13)$$

The projectors on spin-zero and spin-one states:

$$\Pi_0 = \frac{1}{8m^3} \left( \frac{\hat{p}}{2} - \hat{q} - m \right) \gamma^5 \left( \frac{\hat{p}}{2} + \hat{q} + m \right), \Pi_1^\alpha = \frac{1}{8m^3} \left( \frac{\hat{p}}{2} - \hat{q} - m \right) \gamma^\alpha \left( \frac{\hat{p}}{2} + \hat{q} + m \right).$$

The projectors on color-singlet and color-octet states:

$$C_1 = \frac{\delta_{ij}}{\sqrt{N_c}}, \quad C_8 = \sqrt{2}T_{ij}^a,$$

respectively, where  $T^a$  with  $a = 1, \dots, N_c^2 - 1$  are the generators of the color gauge group  $SU(N_c)$ .

## Long-distance matrix elements

We adopt the following values of color-singlet LDMEs

Color-singlet LDMEs can be determined from measured decay widths of charmonia using the known next-to-leading-order (NLO) QCD result or from calculations in potential models:

$$\langle \mathcal{O}^{J/\psi} [^3S_1^{(1)}] \rangle = 1.3 \text{ GeV}^3,$$

$$\langle \mathcal{O}^{\psi'} [^3S_1^{(1)}] \rangle = 6.5 \times 10^{-1} \text{ GeV}^3$$

$$\langle \mathcal{O}^{\chi_{cJ}} [^3P_J^{(1)}] \rangle = (2J+1) \times 8.9 \times 10^{-2} \text{ GeV}^5.$$

Color-octet LDMEs should be universal and process-independent parameters.

However, their numerical values strongly depend on approach which is used to describe  $c\bar{c}$ -pair production and data included into the fit.

Nevertheless, the hierarchy expected from velocity-scaling rules is respected by all the fits:

$$\langle \mathcal{O}^C [^3P_0^{(1)}] \rangle \gg \langle \mathcal{O}^C [^3P_0^{(8)}] \rangle$$

,

$$\langle \mathcal{O}^C [^3S_1^{(1)}] \rangle \gg \langle \mathcal{O}^C [^3P_J^{(8)}] \rangle \gg \left( \langle \mathcal{O}^C [^3S_1^{(8)}] \rangle, \langle \mathcal{O}^C [^1S_0^{(8)}] \rangle \right)$$

.

## Short-distance coefficients

Squared LO in  $\alpha_s$  amplitudes for  $2 \rightarrow 1$  subprocesses in CPM are well-known

[P.L. Cho, A.K. Leibovich (1996)]:

$$\overline{|\mathcal{A}(g + g \rightarrow \chi_{c0}[{}^3P_0^{(1)}])|^2} = \frac{8}{3}\pi^2\alpha_s^2 \frac{\langle \mathcal{O}^{\chi_{c0}}[{}^3P_0^{(1)}] \rangle}{M^3}, \quad (14)$$

$$\overline{|\mathcal{A}(g + g \rightarrow \chi_{c1}[{}^3P_1^{(1)}])|^2} = 0, \quad (15)$$

$$\overline{|\mathcal{A}(g + g \rightarrow \chi_{c2}[{}^3P_2^{(1)}])|^2} = \frac{32}{45}\pi^2\alpha_s^2 \frac{\langle \mathcal{O}^{\chi_{c2}}[{}^3P_2^{(1)}] \rangle}{M^3}, \quad (16)$$

$$\overline{|\mathcal{A}(g + g \rightarrow \mathcal{C}[{}^3S_1^{(8)}])|^2} = 0, \quad (17)$$

$$\overline{|\mathcal{A}(g + g \rightarrow \mathcal{C}[{}^1S_0^{(8)}])|^2} = \frac{5}{12}\pi^2\alpha_s^2 \frac{\langle \mathcal{O}^{\mathcal{C}}[{}^1S_0^{(8)}] \rangle}{M}, \quad (18)$$

$$\overline{|\mathcal{A}(g + g \rightarrow \mathcal{C}[{}^3P_0^{(8)}])|^2} = 5\pi^2\alpha_s^2 \frac{\langle \mathcal{O}^{\mathcal{C}}[{}^3P_0^{(8)}] \rangle}{M^3}, \quad (19)$$

$$\overline{|\mathcal{A}(g + g \rightarrow \mathcal{C}[{}^3P_1^{(8)}])|^2} = 0, \quad (20)$$

$$\overline{|\mathcal{A}(g + g \rightarrow \mathcal{C}[{}^3P_2^{(8)}])|^2} = \frac{4}{3}\pi^2\alpha_s^2 \frac{\langle \mathcal{O}^{\mathcal{C}}[{}^3P_2^{(8)}] \rangle}{M^3}, \quad (21)$$

$$\overline{|\mathcal{A}(q + \bar{q} \rightarrow \mathcal{C}[{}^3S_1^{(8)}])|^2} = \frac{16}{27}\pi^2\alpha_s^2 \frac{\langle \mathcal{O}^{\mathcal{C}}[{}^3S_1^{(8)}] \rangle}{M}. \quad (22)$$

## Short-distance coefficients

The leading  $\alpha_S$   $2 \rightarrow 2$  partonic subprocess, which describes direct production of  $J/\psi$  or  $\psi(2S)$  via color-singlet intermediate state  $[^3S_1^{(1)}]$ , is  $g + g \rightarrow \mathcal{C}[^3S_1^{(1)}] + g$ . The squared amplitude for this partonic subprocess reads [\[R. Gastmans, W. Troost and T. T. Wu, Phys. Lett. B \*\*184\*\*, 257-260 \(1987\)\]](#):

$$\begin{aligned} \overline{|\mathcal{A}(g + g \rightarrow \mathcal{C}[^3S_1^{(1)}] + g)|^2} &= \pi^3 \alpha_s^3 \frac{\langle \mathcal{O}^{\mathcal{C}}[^3S_1^{(1)}] \rangle}{M^3} \frac{320M^4}{81(M^2 - \hat{t})^2(M^2 - \hat{u})^2(\hat{t} + \hat{u})^2} \times \\ &\times (M^4 \hat{t}^2 - 2M^2 \hat{t}^3 + \hat{t}^4 + M^4 \hat{t} \hat{u} - 3M^2 \hat{t}^2 \hat{u} + 2\hat{t}^3 \hat{u} + M^4 \hat{u}^2 - \\ &\quad - 3M^2 \hat{t} \hat{u}^2 + 3\hat{t}^2 \hat{u}^2 - 2M^2 \hat{u}^3 + 2\hat{t} \hat{u}^3 + \hat{u}^4). \quad (23) \end{aligned}$$

## Improved Color Evaporation Model (ICEM)

In the ICEM [Y.Q. Ma and R. Vogt, Phys. Rev. D **94** (2016) 114029], it is assumed that all  $c\bar{c}$  pairs with invariant masses below the  $D\bar{D}$ -threshold hadronize to charmonia with some probability, which is independent from angular momentum and spin quantum numbers of the pair:

$$\frac{d\sigma^{\mathcal{C}}}{d^3k} = F_{\mathcal{C}} \times \int_{m_C^2}^{4m_D^2} dM_{c\bar{c}}^2 \frac{d\sigma^{c\bar{c}}}{dM_{c\bar{c}}^2 d^3k}, \quad (24)$$

where  $F_{\mathcal{C}}$  is the process-independent hadronization probability to the charmonium state  $\mathcal{C}$ .

## Cross section of the ICEM

Cross section in GPM and ICEM reads:

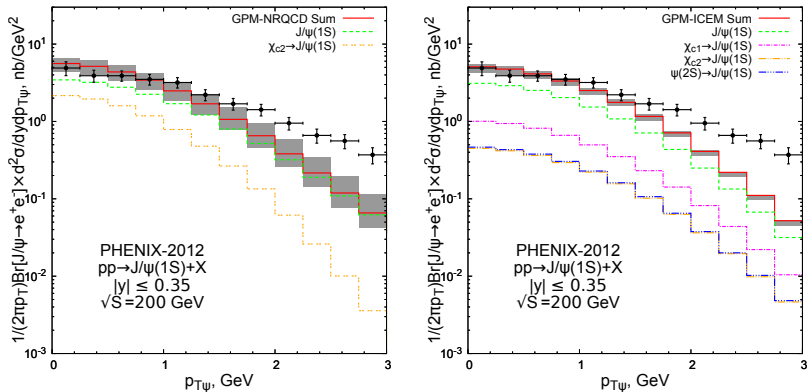
$$\begin{aligned} \frac{d\sigma^C}{d^3k} &= F_C \times \int dx_1 \int d^2q_{1T} \int dx_2 F_g(x_1, q_{1T}, \mu_F) F_g(x_2, q_{2T}, \mu_F) \hat{\sigma}(\hat{s}, ij \rightarrow c\bar{c}) \\ &\times \delta(q_1^3 + q_2^3 - k^3) [\theta(\hat{s} - m_C^2) - \theta(\hat{s} - 4m_D^2)], \end{aligned} \quad (25)$$

where  $\hat{\sigma}(\hat{s}, ij \rightarrow c\bar{c})$  is just a well-known total cross section of one of the subprocesses:  $gg \rightarrow c\bar{c}$  or  $q\bar{q} \rightarrow c\bar{c}$ , correspondingly.



# TSSA in charmonium production at RHIC and NICA

# PHENIX-2012 data, $|y| \leq 0.35$ , $\sqrt{s} = 200$ GeV.



**Figure:** Differential cross-section of prompt  $J/\psi$  production as function of transverse momentum at  $\sqrt{s} = 200$  GeV,  $|y| \leq 0.35$ . The theoretical results are obtained in GPM with  $\langle q_T^2 \rangle = 1$  GeV<sup>2</sup>. Left panel: NRQCD-factorization prediction with only color-singlet channels included. Right panel: ICEM-prediction. In the left panel, contributions from decays  $\chi_{c0} \rightarrow J/\psi$  and  $\psi(2S) \rightarrow J/\psi$  are not shown. Experimental data are from the Ref. [A. Adare *et al.* [PHENIX], Phys. Rev. D **85**, 092004 (2012)].

PHENIX-2012 data,  $|y| \leq 0.35$ ,  $\sqrt{S} = 200$  GeV.

**Table:** The relative contributions of direct and feed-down production within NRQCD and ICEM. Experimental data of the PHENIX collaboration for  $\sqrt{s} = 200$  GeV are from [A. Adare *et al.* [PHENIX], Phys. Rev. D **85**, 092004 (2012)].

$\sqrt{s}$	Model/Source of data	$\sigma^{\text{direct}} : \sigma_{\chi_c \rightarrow J/\psi} : \sigma_{\psi(2S) \rightarrow J/\psi}$
24 GeV	NRQCD	0.58 : 0.39 : 0.03
24 GeV	ICEM	0.68 : 0.25 : 0.07
200 GeV	NRQCD	0.61 : 0.34 : 0.05
200 GeV	ICEM	0.61 : 0.30 : 0.09
200 GeV	PHENIX collab.	0.58 : 0.32 : 0.10

**Table:** The values of hadronization probabilities of ICEM, which had been obtained via the fit of total cross-section of  $J/\psi$ -production at PHENIX. The fit of LHC data are taken from [V. Cheung and R. Vogt, Phys. Rev. D **98**, 114029 (2018)].

$F_C$	Our fit	The fit of LHC data
$F_{J/\psi}$	0.02	0.02
$F_{\chi_{c1}}$	0.06	0.18
$F_{\chi_{c2}}$	0.06	0.2
$F_{\psi'}$	0.08	0.12

PHENIX-2018 data,  $1.2 \leq |y| \leq 2.2$ ,  $\sqrt{S} = 200$  GeV.

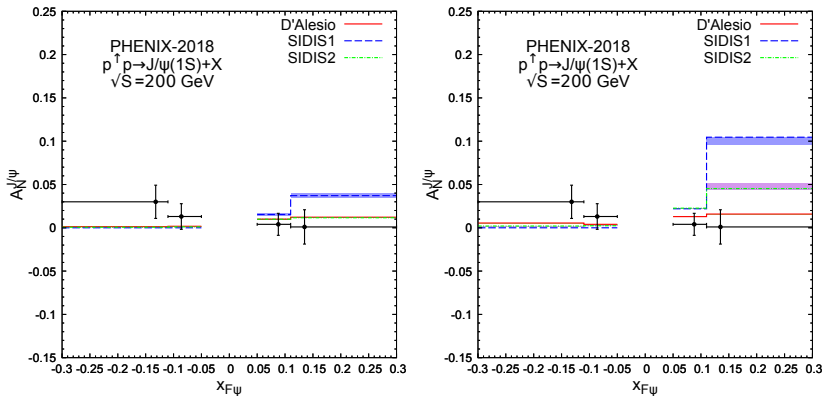


Figure: SSA  $A_N^{J/\psi}$  as function of  $x_F$  at  $\sqrt{s} = 200$  GeV. The theoretical results are obtained with SIDIS1 and D'Alesio *et al.* parameterizations of GSFs. Experimental data are from Ref. [C. Aidala *et al.* [PHENIX], Phys. Rev. D **98**, 012006 (2018)]. Left panel: NRQCD-prediction. Right panel: ICeM prediction.

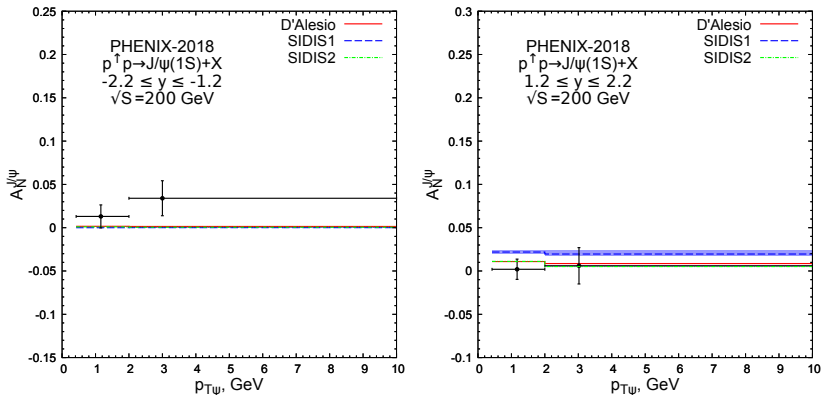
PHENIX-2018 data,  $1.2 \leq |y| \leq 2.2$ ,  $\sqrt{S} = 200$  GeV.

Figure: NRQCD predictions for SSA  $A_N^{J/\psi}$  as function of  $J/\psi$ -transverse momentum at  $\sqrt{s} = 200$  GeV. The theoretical results are obtained with SIDIS1 and D'Alesio et al. parameterizations of GSFs. Left panel – backward production ( $-2.2 \leq y \leq -1.2$ ), right panel – forward production ( $1.2 \leq y \leq 2.2$ ). Experimental data are from Ref. [C]. Aidala *et al.* [PHENIX], Phys. Rev. D **98**, 012006 (2018)].

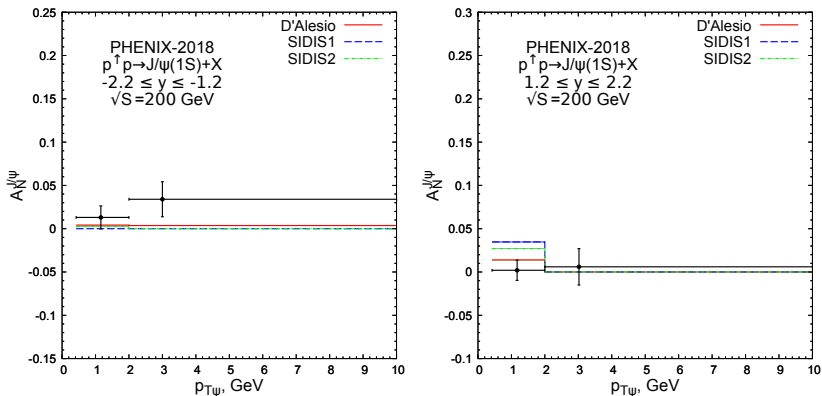
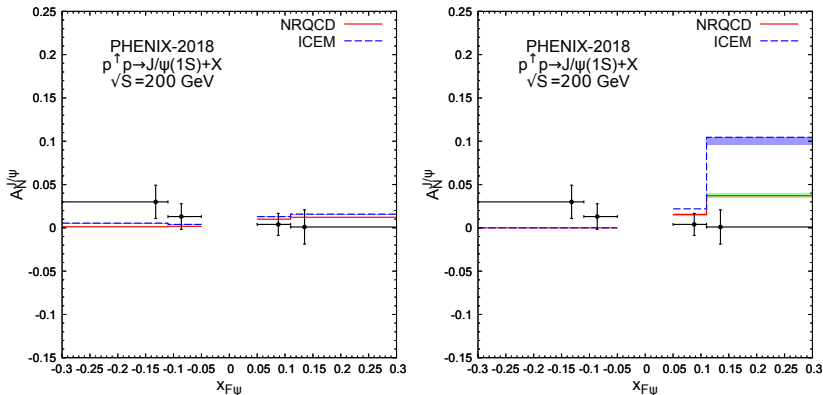
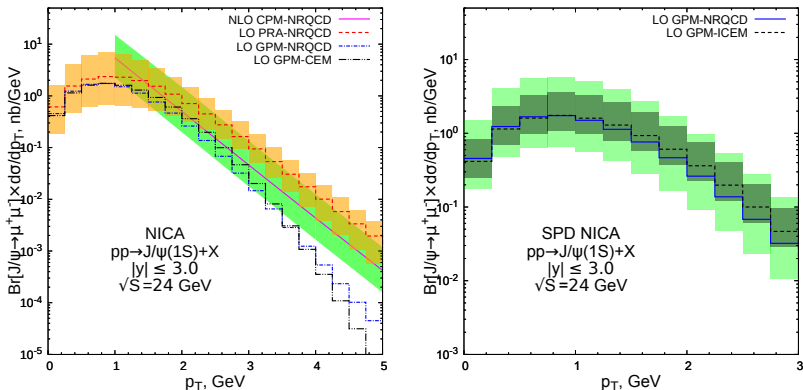
PHENIX-2018 data,  $1.2 \leq |y| \leq 2.2$ ,  $\sqrt{S} = 200$  GeV.

Figure: **ICEM predictions** for SSA  $A_N^{J/\psi}$  as function of  $J/\psi$ -transverse momentum at  $\sqrt{s} = 200$  GeV. The theoretical results are obtained with SIDIS1 and D'Alesio et al. parameterizations of GSFs. Left panel – backward production ( $-2.2 \leq y \leq -1.2$ ), right panel – forward production ( $1.2 \leq y \leq 2.2$ ). Experimental data are from Ref. [C]. Aidala *et al.* [PHENIX], Phys. Rev. D **98**, 012006 (2018)].

# Predictions for TSSA in $J/\psi$ production at PHENIX , $\sqrt{s} = 200$ GeV.



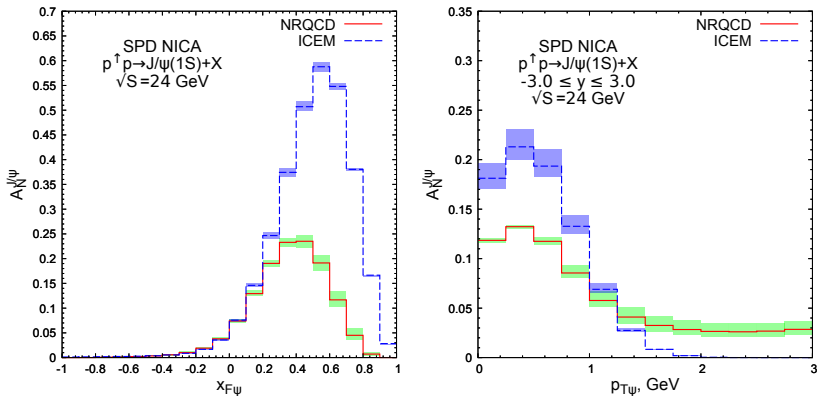
**Figure:** Comparison of predictions for SSA  $A_N^{J/\psi}$  as function of  $x_F$  with the D'Alesio *et al.* parameterization of GSF (left panel) and SIDIS1 (right panel) at  $\sqrt{s} = 24$  GeV in NRQCD (solid histogram) and ICEM (dashed histogram) approaches.  $s$  is used.

Predictions for NICA (in different models),  $|y| \leq 3$ ,  $\sqrt{s} = 24$  GeV.

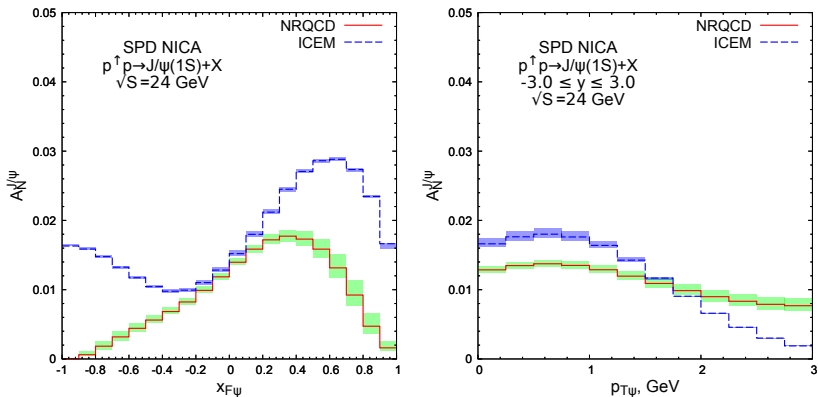
**Figure:** Prompt  $J/\psi$  transverse momentum distribution at  $\sqrt{s} = 24$  GeV,  $|y| \leq 3$ . Left panel: GPM results with  $\langle q_T^2 \rangle = 1$  GeV<sup>2</sup> are shown by dash-dotted (NRQCD) and dash-double-dotted (ICEM) histograms. Solid and dashed histograms with uncertainty bands are PRA [A.V. Karpishkov, M.A. Nefedov and V.A. Saleev, J. Phys. Conf. Ser. **1435**, 012015 (2020)] and NLO CPM [M. Butenschön and B.A. Kniehl, private communication] predictions respectively. Right panel: GPM predictions in NRQCD (solid histogram with light green uncertainty band) and ICEM (dashed histogram with dark-green uncertainty band) approaches with their uncertainty bands shown.



# Predictions for SSA at NICA (SIDIS1), $|y| \leq 3$ , $\sqrt{s} = 24$ GeV.

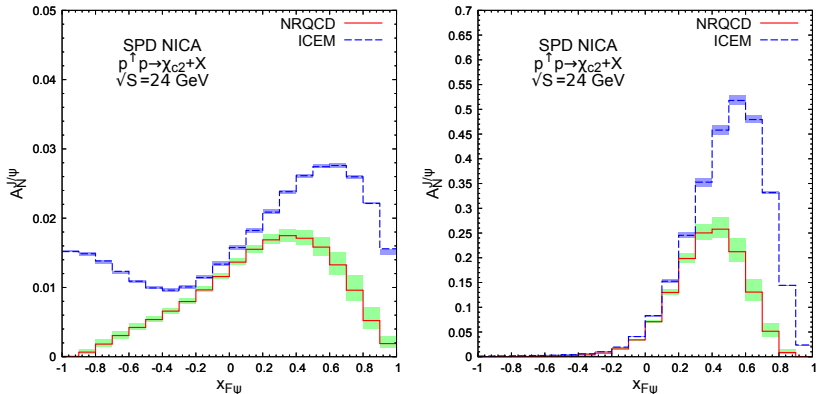


**Figure:** Comparison of predictions for SSA  $A_N^{J/\psi}$  as function of  $x_F$  (left panel) and transverse momentum (right panel) at  $\sqrt{s} = 24$  GeV in NRQCD (solid histogram) and ICEM (dashed histogram) approaches. The SIDIS1 parametrisation of GSFs is used.

Predictions for TSSA at NICA (D'Alesio),  $|y| \leq 3$ ,  $\sqrt{S} = 24$  GeV.

**Figure:** Comparison of predictions for SSA  $A_N^{J/\psi}$  as function of  $x_F$  (left panel) and transverse momentum (right panel) at  $\sqrt{s} = 24$  GeV in NRQCD (solid histogram) and ICEM (dashed histogram) approaches. The D'Alesio *et al.* parametrisation of GSFs is used.

# Predictions for TSSA in $\chi_{c2}$ production at NICA , $|y| \leq 3$ , $\sqrt{s} = 24$ GeV.



**Figure:** Comparison of predictions for SSA  $A_N^{\chi_{c2}}$  as function of  $x_F$  with the D'Alesio *et al.* parameterization of GSF (left panel) and SIDIS1 (right panel) at  $\sqrt{s} = 24$  GeV in NRQCD (solid histogram) and ICEM (dashed histogram) approaches.  $s$  is used.

## Conclusions

- Prompt  $J/\psi$  transverse momentum spectra at small  $k_{TJ/\psi} < m_{J/\psi}$  can be described well in GPM, as in the Color Singlet Model of NRQCD, as in the ICEM. The total cross-section ratios of direct and feed-down contributions in good agreement with experimental data too.
- We find, that parametrization of D'Alesio *et al.* for GSF leads to reasonable predictions for magnitude,  $J/\psi$  transverse momentum and  $x_F$  dependence of the TSSA at PHENIX RICH.
- We demonstrate measurable differences in predictions of TSSAs obtained in NRQCD versus ICEM, especially at SPD NICA experiment.
- The predictions for TSSAs at the planned SPD NICA experiment are presented for the first time.

For details, see [A.V. Karpishkov, M.A. Nefedov, V.A. Saleev, arXiv:2008.07232].

Thank you for your attention!