



VIth MPD Collaboration meeting
28-30 October 2020, JINR, Dubna



Femtoscopia correlations with MPD at NICA

on behalf of PWG3 (Correlations and Fluctuations)
Supported by the RFBR grant 18-02-40044



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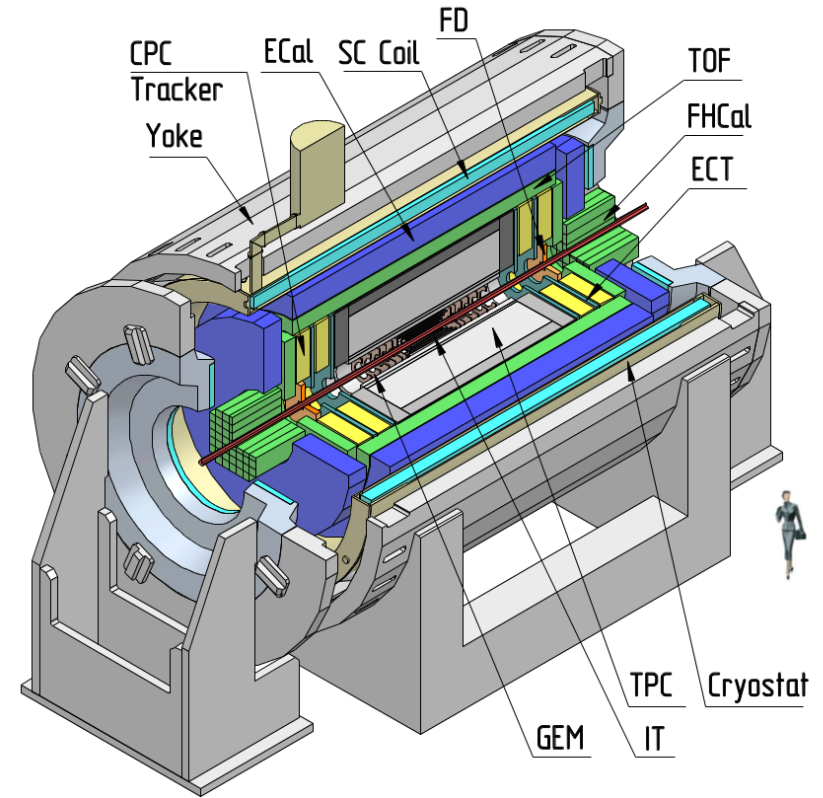
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Outline

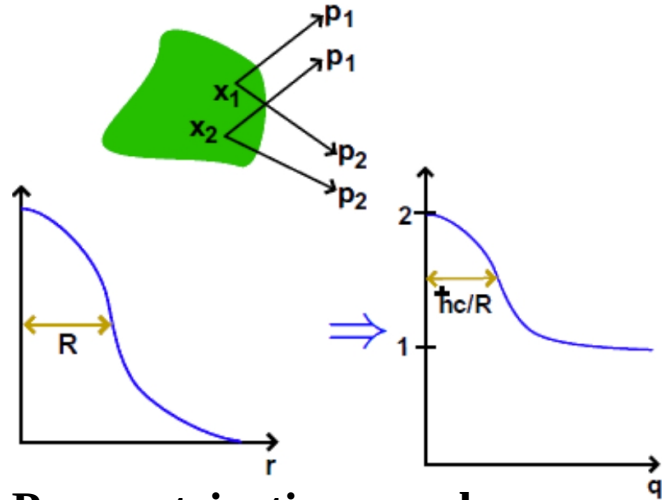
- Activities
- Femtoscopy & Motivation
- Hybrid vHLLE model
- New kaon results
- Tests with reconstructed data
- Factorial Moments
- Femto software
- Conclusions



Activities within RFBR grant 18-02-40044

- Three Master and 1 PhD student in Femto group
- PWG3 Meetings: about 20 events(2020) → <https://indico.jinr.ru/category/346/>
- MPD Physics Seminars(+3 in 2019):
 - G.Nigmatkulov. «The MpdMiniDst data format (Part 1)». 16 July 2020
 - G.Nigmatkulov. «The MpdMiniDst data format (Part 2)». 6 Aug 2020
- Conferences(+3 in 2019):
 - ICPPA-2020: 3 talks
 - NUCLEUS-2020: 1 talk
 - RFBR Grants for NICA: 3 talks
 - VI MPD Collaboration meeting: 2 talks
- Publications(+1 in 2019):
 - P. N. Batyuk, L. V. Malinina, K. R. Mikhaylov, and G. A. Nigmatkulov,
«Femtoscopia with Identified Charged Particles for the NICA Energy Range», Physics of Particles and Nuclei,
2020, Vol. 51, No. 3, pp. 252–257
 - + 5 proceedings(ICPPA, NUCLEUS and RFBR) will be published

Femtoscscopy



Correlation femtoscopy :

Measurement of space-time characteristics \mathbf{R} , \mathbf{ct} of particle production using particle correlations due to the effects of quantum statistics (QS) and final state interactions (FSI)

Two-particle correlation function:

theory:
$$C(q) = \frac{N_2(p_1, p_2)}{N_1(p_1) \cdot N_2(p_1)}, C(\infty) = 1$$

experiment:
$$C(q) = \frac{S(q)}{B(q)}, q = p_1 - p_2$$

$S(q)$ – distribution of pair momentum difference from same event
 $B(q)$ – reference distribution built by mixing different events

Parametrizations used:

1D CF:
$$C(q_{inv}) = 1 + \lambda e^{-R^2 q_{inv}^2}$$

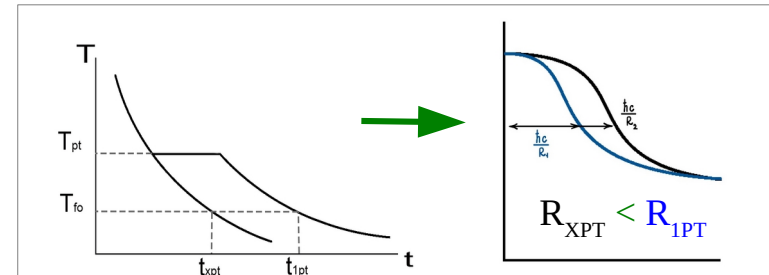
R – Gaussian radius in PRF,

λ – correlation strength parameter

3D CF:
$$C(q_{out}, q_{side}, q_{long}) = 1 + \lambda e^{-R_{out}^2 q_{out}^2 - R_{side}^2 q_{side}^2 - R_{long}^2 q_{long}^2}$$

R and q are in Longitudinally Co-Moving Frame (LCMS)

long || beam; out || transverse pair velocity \mathbf{v}_T ; side normal to out, long



Motivation

● Femtосcopy allows one:

- To obtain spatial and temporal information on particle-emitting source at kinetic freeze-out
- To study collision dynamics depending on EoS

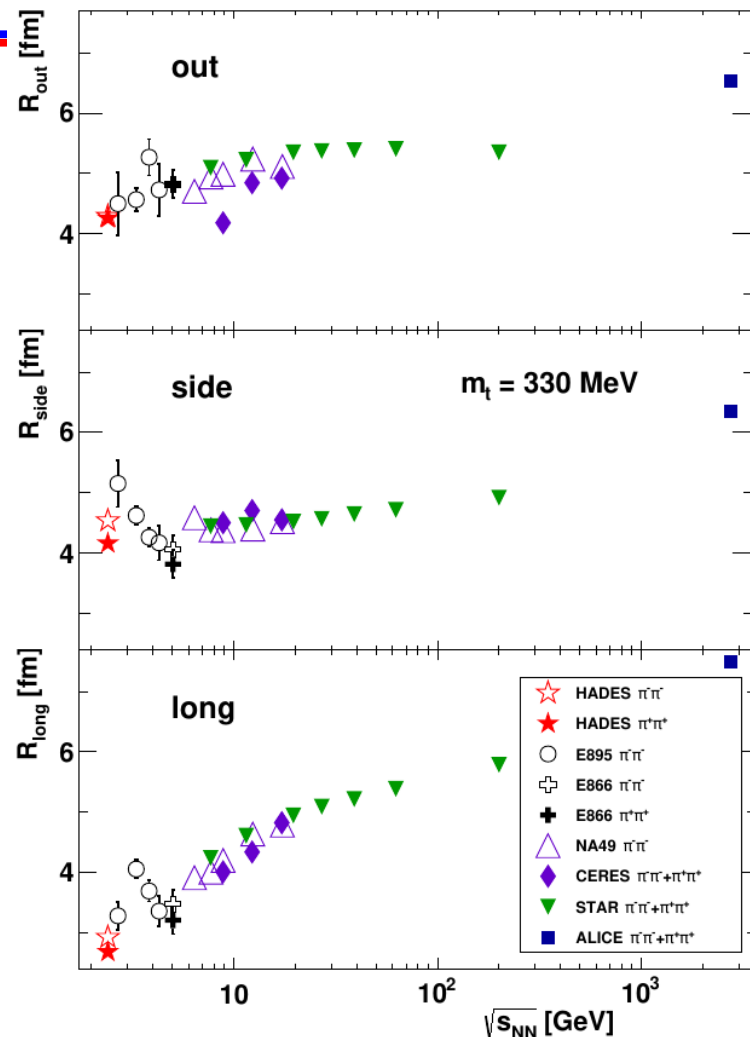
● RHIC Beam Energy Scan program (BES-I):

$$\sqrt{s_{NN}} = 7.7, 11.5, 19.6, 27, 39 \text{ GeV}$$

- The search for the onset of a first-order phase transition in Au + Au collisions
- Measured pion and kaon femtoscopic parameters:
 - m_T -dependence of radii,
 - flow-induced $x - p$ correlations

● NICA energy range: $\sqrt{s_{NN}} = 4 - 11 \text{ GeV}$

- first collider measurements below 7.7 GeV
- including K and heavier



Femtoscropy with vHLLE

Iu. Karpenko, P. Huovinen, H. Petersen, M. Bleicher, Phys.Rev. C.91, 2015, 064901

Pre-thermal phase

UrQMD

Parameters τ_0 , R_{\perp} , R_{η} and η/s adjusted using basic observables in the RHIC BES-I region.

$\sqrt{s_{NN}}$ [GeV]	τ_0 [fm/c]	R_{\perp} [fm]	R_{η} [fm]	η/s
7.7	3.2	1.4	0.5	0.2
8.8 (SPS)	2.83	1.4	0.5	0.2
11.5	2.1	1.4	0.5	0.2
17.3 (SPS)	1.42	1.4	0.5	0.15
19.6	1.22	1.4	0.5	0.15
27	1.0	1.2	0.5	0.12
39	0.9	1.0	0.7	0.08
62.4	0.7	1.0	0.7	0.08
200	0.4	1.0	1.0	0.08

Model tuned by matching with existing experimental data from SPS and BES-I RHIC

Hydrodynamic phase

vHLLE

(3+1)-D viscous hydrodynamics

EoS to be used in the model

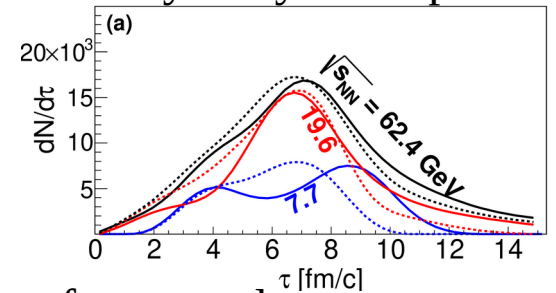
- Chiral EoS — crossover transition
J. Steinheimer et al., J. Phys. G 38, 035001 (2011)
- Hadron Gas + Bag Model
1st-order phase transition
P. F. Kolb et al., Phys.Rev. C 62, 054909 (2000)

Hydrodynamic phase lasts longer with 1PT, especially at lower energies but cascade smears this difference.

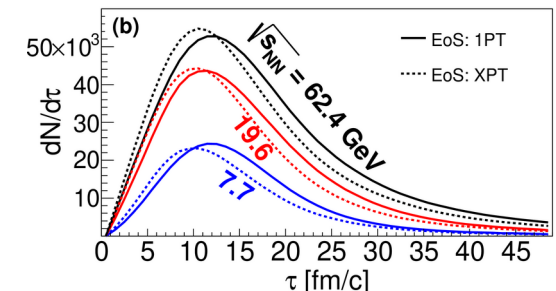
Hadronic cascade

UrQMD

Pion emission time
after hydrodynamic phase

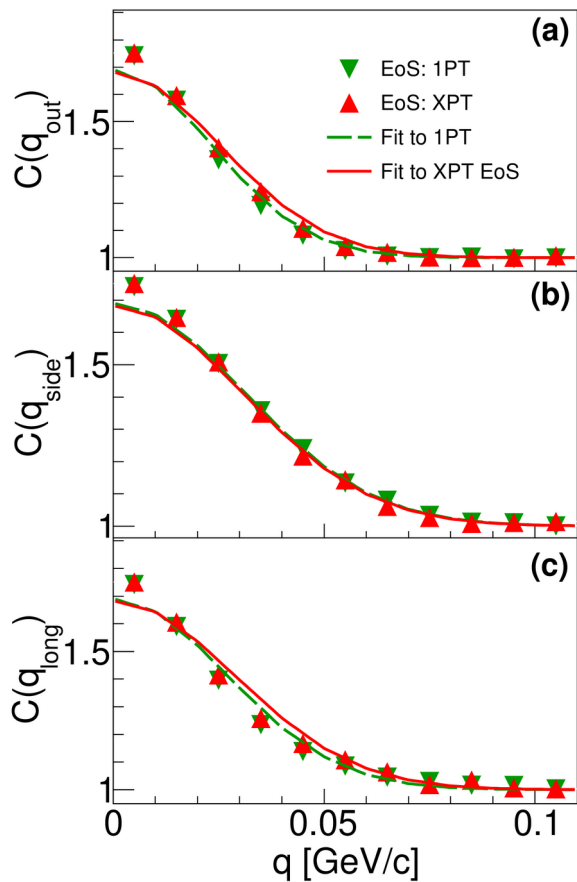


after cascade

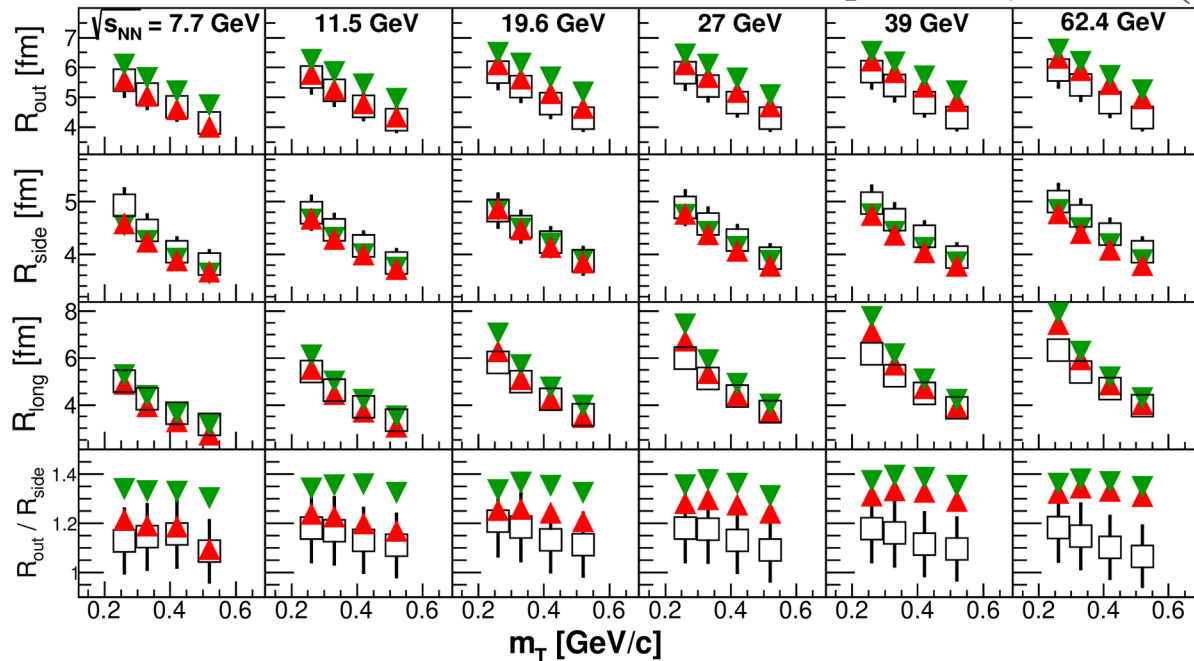


3D Pion radii versus m_T with vHLLE

Model CF



Comparison of extracted radii with the STAR data [PRC 96, 024911(2017)]



- Femtoscopic radii are sensitive to the type of the phase transition
- **Crossover EoS** does better job at lowest collision energies.
- R_{out} (XPT) at high energies and R_{out} (1PT) at all energies are slightly overestimated
- $R_{out, long}$ (1PT) $>$ $R_{out, long}$ (XPT) by value of $\sim 1-2$ fm.

Correlation Functions from UrQMD

- Examples of the correlation functions of pions and kaons obtained for Au+Au collisions at $\sqrt{s_{NN}}=11.5$ GeV (UrQMD)
- Correlation functions were fitted with:

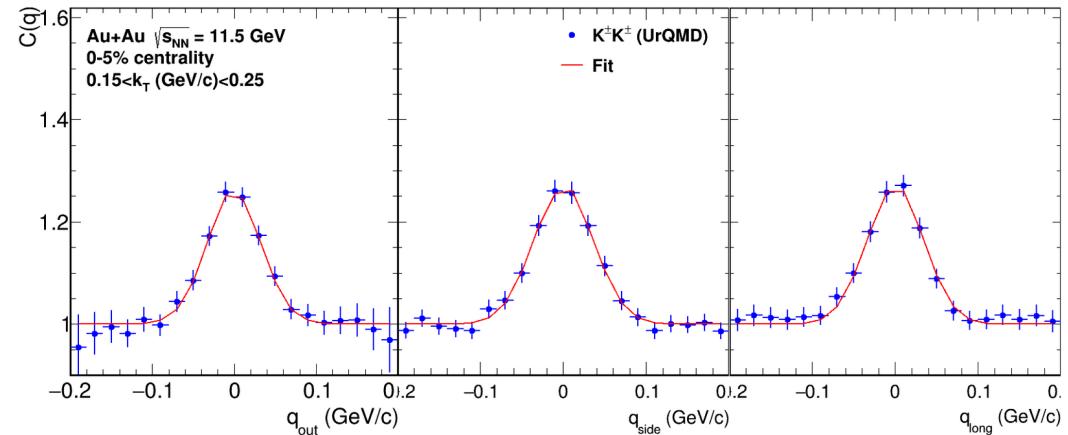
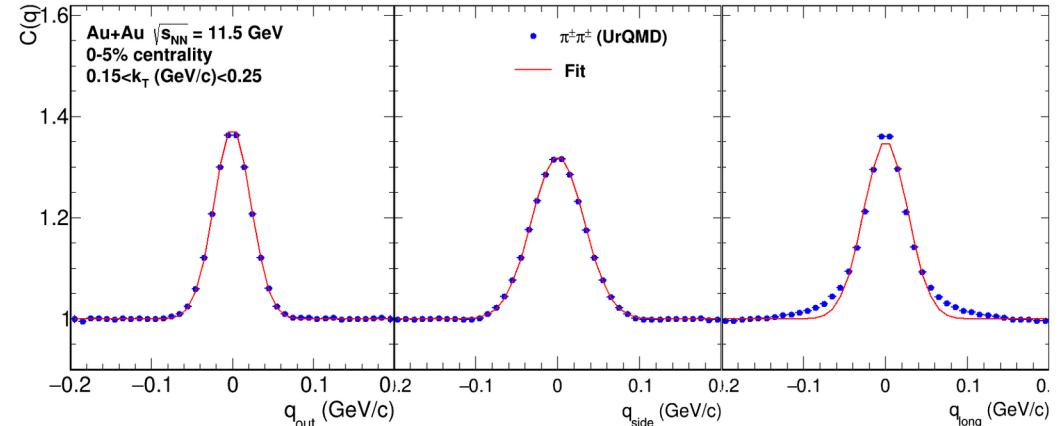
$$C(q_{out}, q_{side}, q_{long}) = 1 + \lambda e^{-R_{out}^2 q_{out}^2 - R_{side}^2 q_{side}^2 - R_{long}^2 q_{long}^2}$$

where:

R_{side} – size of the emission region

R_{out} – sensitive to the emission duration

R_{long} – proportional to the system lifetime



Correlation Functions from vHLLLE

- Examples of the correlation functions of pions and kaons obtained for Au+Au collisions at $\sqrt{s_{NN}}=11.5$ GeV (vHLLLE)
- Correlation functions were fitted with:

$$C(q_{out}, q_{side}, q_{long}) = 1 + \lambda e^{-R_{out}^2 q_{out}^2 - R_{side}^2 q_{side}^2 - R_{long}^2 q_{long}^2}$$

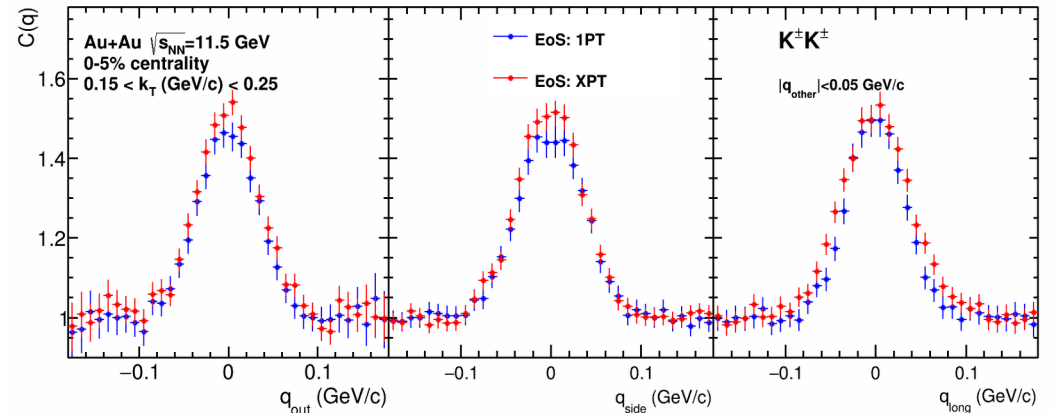
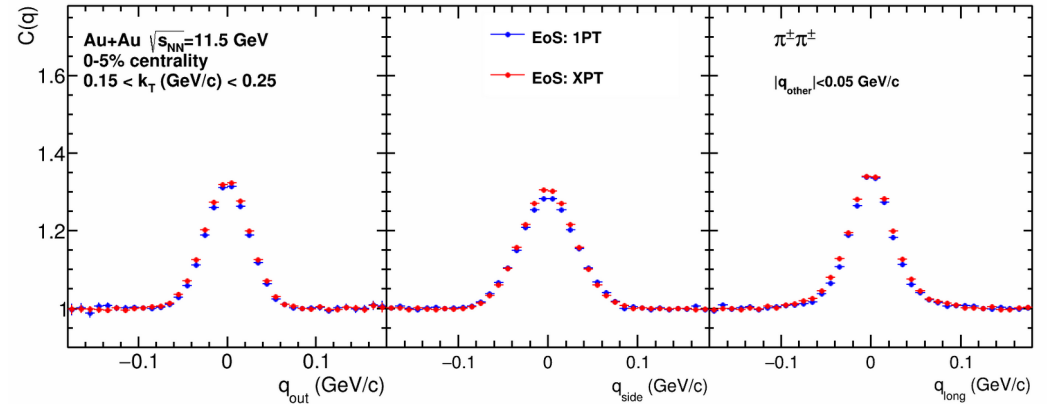
where:

R_{side} – size of the emission region

R_{out} – sensitive to the emission duration

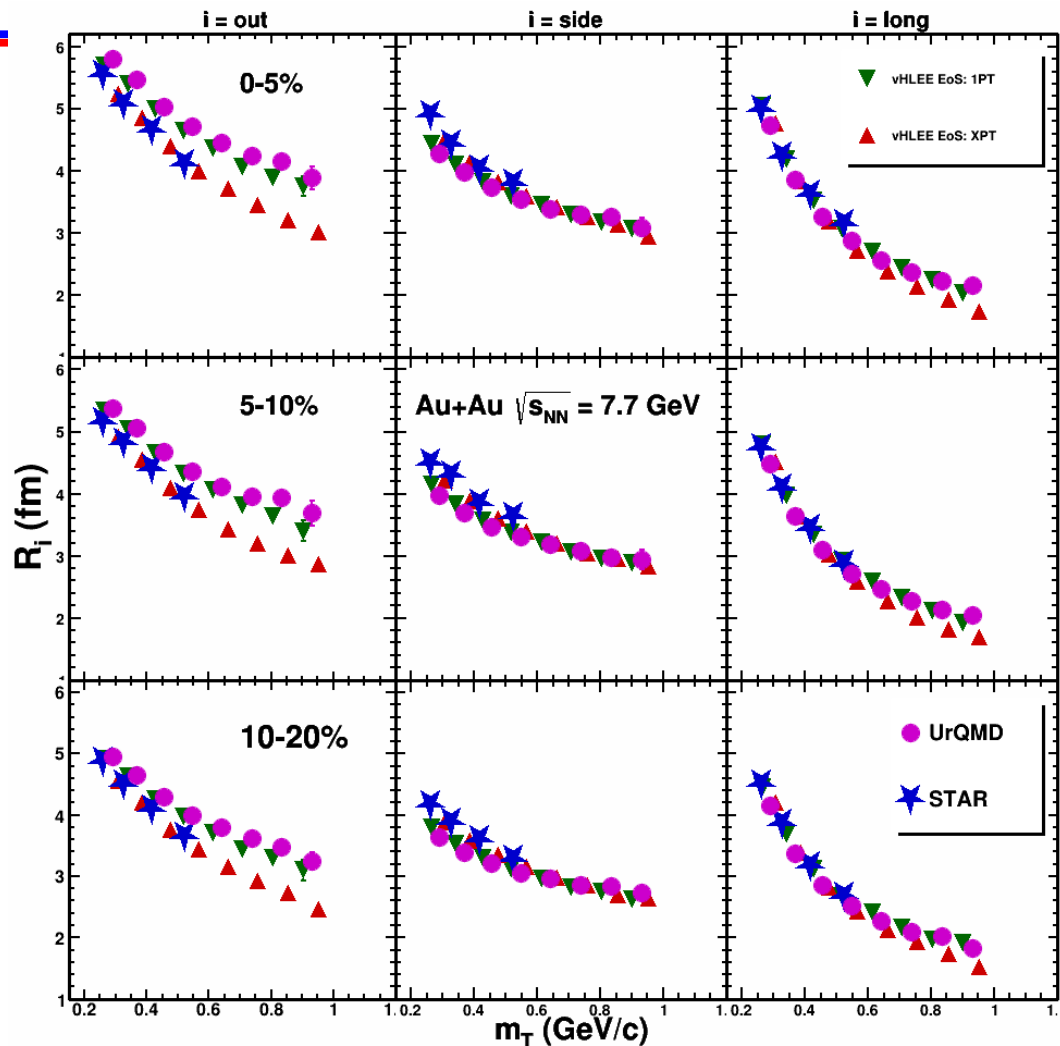
R_{long} – proportional to the system lifetime

- Both K and π CF **XPT** wide than 1XP
 \rightarrow **XPT** size smaller than 1XP



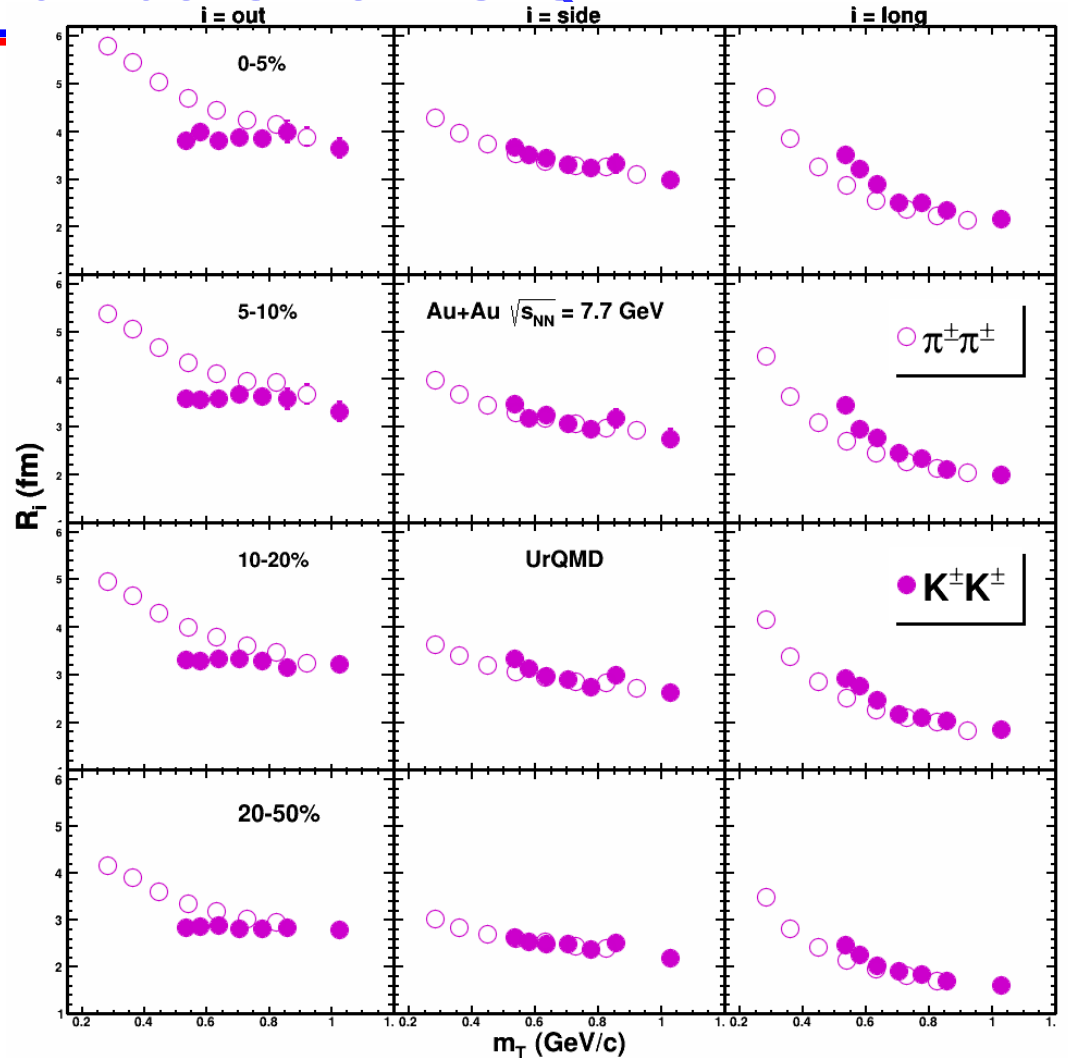
Femtoscopic R_π from UrQMD and vHLLE

- Femtoscopic radii of pions decrease with increasing transverse mass
→ Influence of radial flow
- R_{side} increases going from peripheral to central collisions
→ Geometrical picture of ion-ion collision
- UrQMD shows similar results to vHLLE with 1PT
- vHLLE with XPT reasonably describe STAR data



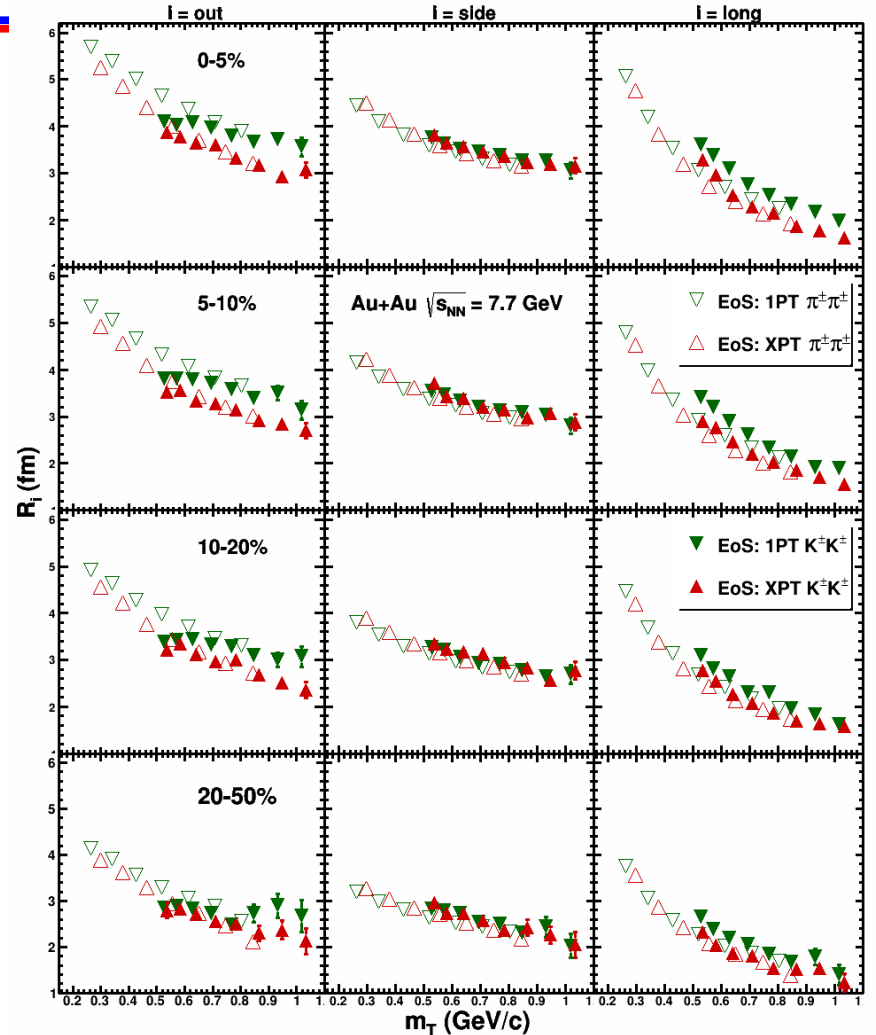
Femtoscopic Radii of Pions and Kaons from UrQMD

- Femtoscopic radii of pions decrease with increasing transverse mass
→ Influence of radial flow
- R_{side} values for pions and kaons are similar
→ Similar size of the particle-emitting region
- R_{long} for kaons is generally larger than that for pions at the same m_T
→ Influence of resonances?
- R_{out} pions and kaons behave differently
→ Different emission duration?
→ Change of the production mechanism?



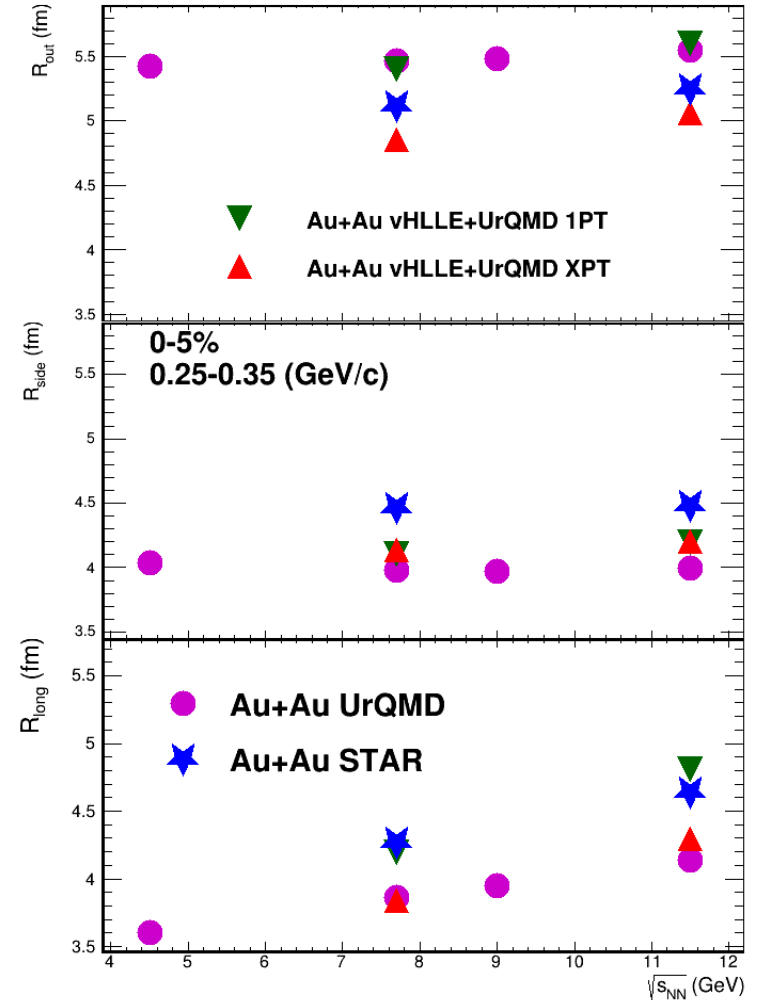
Femtoscopic Radii of Pions and Kaons from vHLE

- Pion and kaon results for the cross over (XPT) and 1st-order (1PT) phase transitions
- Femtoscopic radii of pions decrease with increasing transverse mass \rightarrow Influence of radial flow
- R_{side} values for pions and kaons are similar \rightarrow Similar size of the particle-emitting region
- R_{out} for both pions and kaons show similar behavior \rightarrow Similar particle emission duration?
- R_{long} for kaons is generally larger than that for pions at the same m_T \rightarrow Influence of resonances?



Energy dependence of pion femtoscopic radii

- Estimated pion radii for NICA energy range ($\sqrt{s_{NN}} = 4-11$ GeV)
- Pion radii slightly increase with increasing collision energy
- Excitation function of R_{long} suggests a slight increase of the system lifetime with increasing $\sqrt{s_{NN}}$



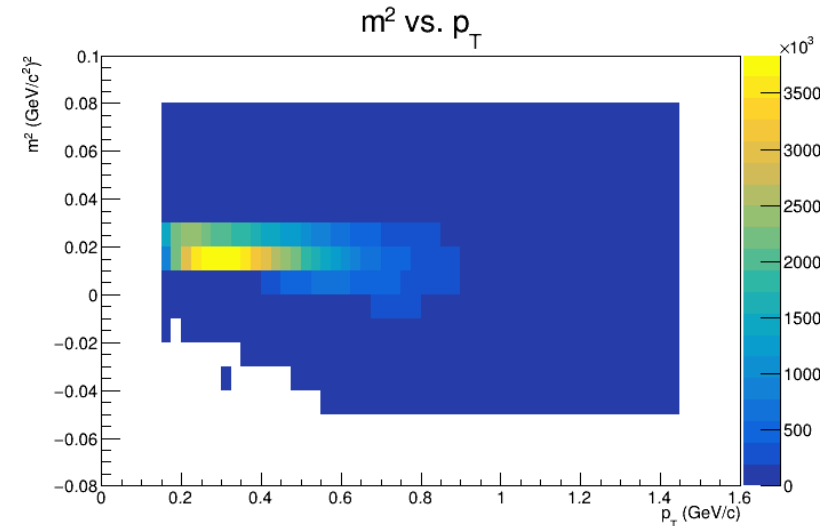
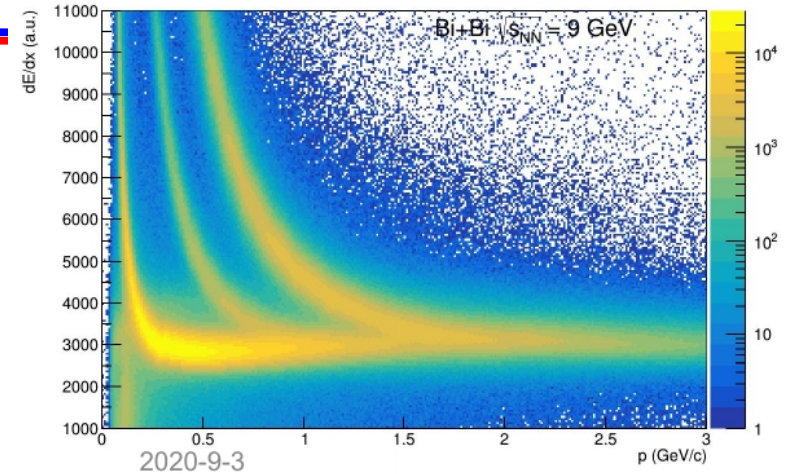
Monte-Carlo data

- Monte-Carlo simulation request
- UrQMD Minimal Bias 10 million evens
- BiBi at $\sqrt{s_{NN}}=9$ GeV
- MiniDST format

- 5 k_T bins (0.15-0.65) GeV/c, with step 100 MeV/c

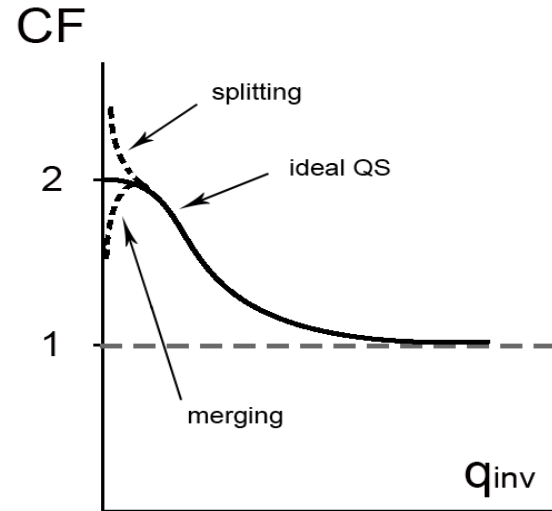
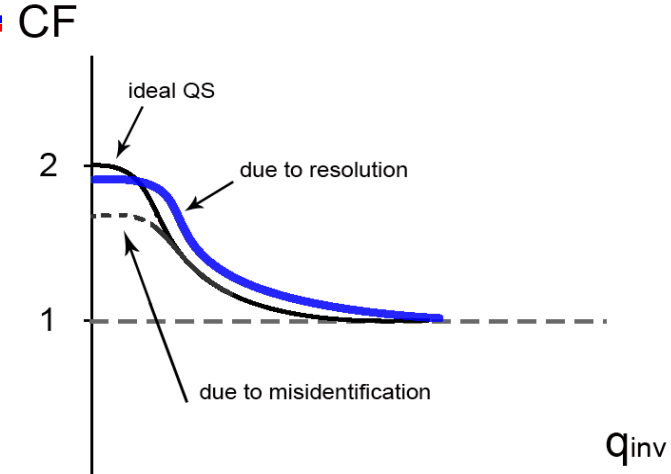
- Kinematic conditions for pions
 - $0.15 < p_T < 1.45$ GeV/c
 - $|\eta| < 1.0$

- Nhits TPC > 15
- DCA < 3 cm
- $|\text{VertexZ}| < 75$
- PID : Nsigma for pion selections in TPC & TOF = 2



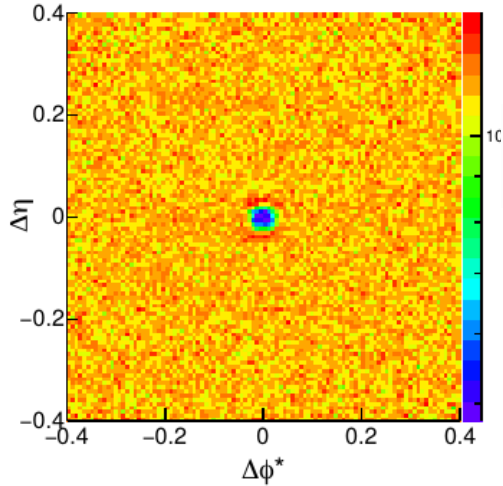
Detector effects affecting the correlation function

- Single track effects:
 - the momentum resolution effects smear CF, making it wider and extracted radii smaller
 - CFs should be corrected by resolution
 - the particle misidentification influences only λ -parameter of CF, radii do not change.
 - CF should be corrected by pair purity.
- Two track effects:
 - track splitting (one track is reconstructed as two)
 - track merging (two tracks are reconstructed as one)These effects are studied and the special pair cuts are used in the analysis.



Two track effects

$\Delta\eta$ vs $\Delta\phi^*$

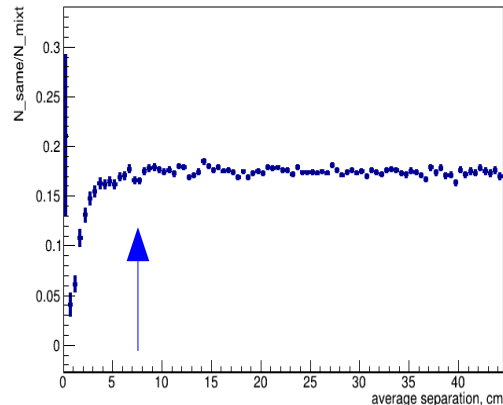


- $\Delta\eta$ - $\Delta\phi^*$ cut:

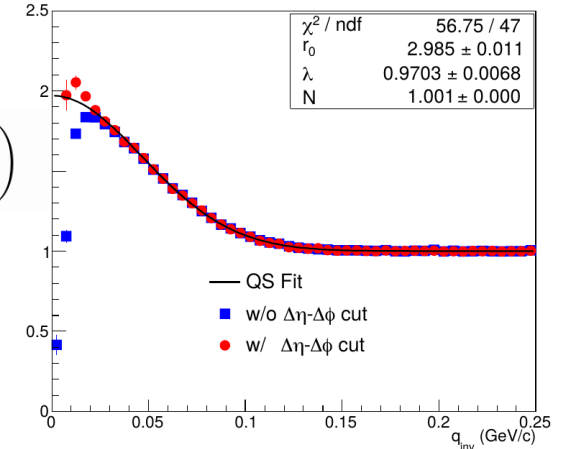
$$\Delta\phi^* = \phi_1 - \phi_2 + \arcsin\left(\frac{z \cdot e \cdot B_z \cdot R}{2p_{T1}}\right) - \arcsin\left(\frac{z \cdot e \cdot B_z \cdot R}{2p_{T2}}\right)$$

R is a given cylindrical radius,
 $\phi_{1,2}$ are azimuthal angles of track
 at reconstructed vertex

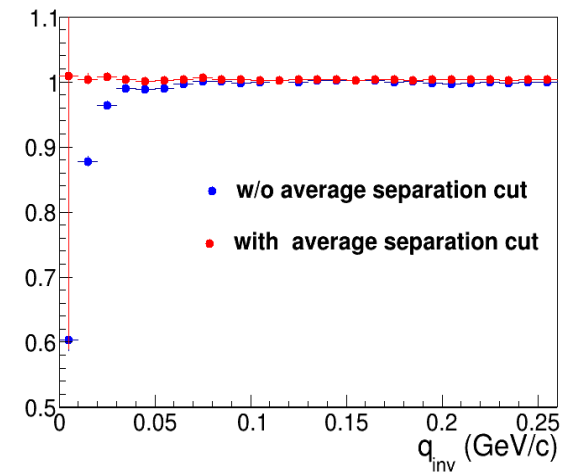
- Average track separation cut:
 - ratio real/mixed vs average distance
 - dip at low distance due to merging (or bump due to splitting)
- Cut on distance > 7 cm
 - remove the dip



$\pi\pi$ correlation function (QS, $r_0=3$ fm)



$\pi\pi$ correlation function w/o FSI



Factorial moments

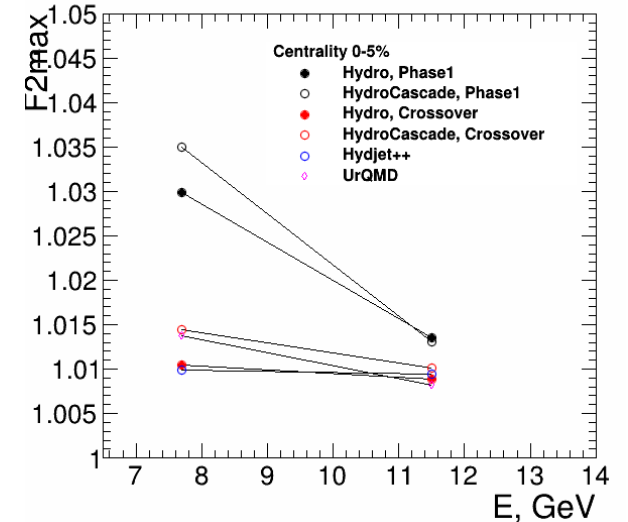
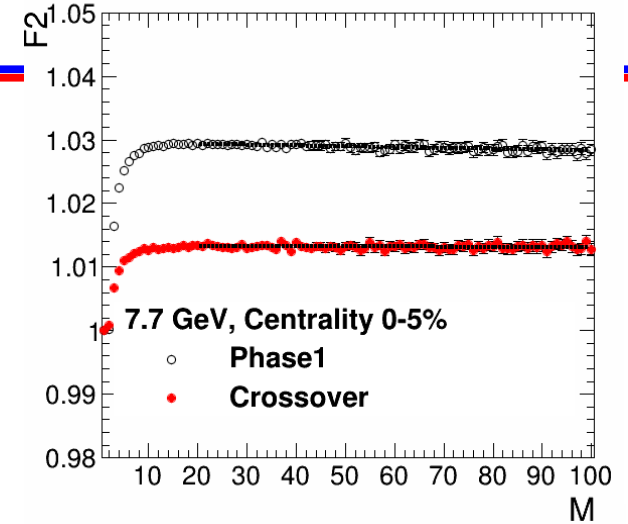
- Olga Kodolova and Maria Cheremnova (see talks at ICPPA, RFBR)
- A. Bialas and R. Peschanski(Nucl. Phys. B273 (1986) 703) to study the dependence of the normalized factorial moments of the rapidity distribution on the bin size δy :

$$F_i = M^{i-1} \times \left\langle \frac{\sum_{j=1}^M k_j \times (k_j - 1) \times \dots \times (k_j - i + 1)}{N \times (N - 1) \times \dots \times (N - i + 1)} \right\rangle$$

- $\delta y = \Delta y / M$; M - number of bins; Δy - size of mid rapidity window; N - number of particles in Δy ;
- k_j - the number of particles in bin j
- If fluctuations are purely statistical no variation of moments as a function of δy is expected
- Observation of variations indicates the presence of physics origin fluctuations

Sensitivity of factorial moments

- Different energy behavior F_2 vHLLLE (1PT and XPT EoS)
- No-phase transition (UrQMD, HYDJET++) do not reveal the energy dependence as vHLLLE



Packages for data storage and femtoscopic analysis

- Grigory Nigmatkulov and Pavel Batyuk (RFBR, VI MPD)

Summary

- The new data format ([MpdMiniDst](#)) that may satisfy most MPD physics needs:
 - Was developed and implemented in MpdRoot
 - Contains most of the detector subsystems
 - Easy to use
 - Already used in several analyses
- Package for femtoscopic analysis ([MpdFemtoMaker](#)):
 - Developed and implemented in MpdRoot
 - Applied to study identical pion and kaon correlations using the UrQMD and vHLLE models
 - Allowed us to study the influence of two-particle effects on correlation function in MPD and develop two-track selection criteria to suppress these parasitic effects

Conclusions

- We performed the first model estimation of kaons femtoscopic radii using the UrQMD and vHLLE models
- Kaon radii dependence as a function of transverse mass shows:
 R_{side} values for pions and kaons are similar for vHLLE and behaviour is different for UrQMD
 R_{long} for kaons is generally larger than that for pions
- Sensitivity of both pion and kaon source size to the nature of the phase transitions
- Factorial moments are sensitive to phase transition within vHLLE model
- Results were presented at ICPPA, NUCLEUS and RFBR conferences
- Proceedings will be published

Thank you for attention!

Backup

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Activities within RFBR grant 18-02-40044

Aim of the project:

Study of collective effects and dynamics of quark-hadron phase transitions via femtoscopic correlations of hadrons and factorial moments of particle multiplicity at NICA energies

Goals:

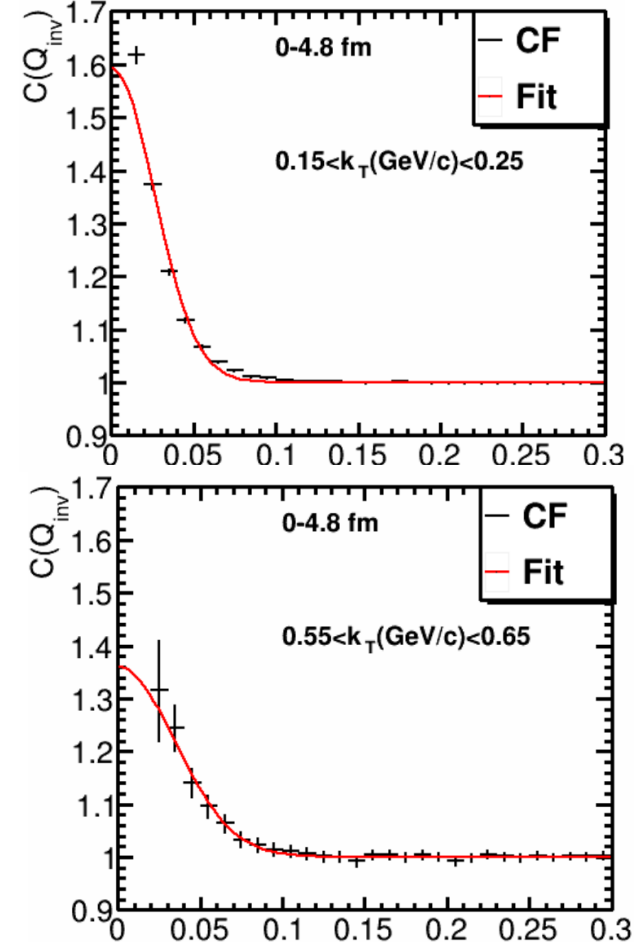
- Development of the data analysis methods and software that will be integrated in the Multi-Purpose Detector (MPD) software environment
- Analysis of the simulated with different event generators (in particular, UrQMD and vHLLE) Au+Au collisions at NICA energies
- Study the dependence of femtoscopic radii and scaled factorial moments of particle multiplicity on the initial conditions and properties of nuclear matter equation of state

2020:

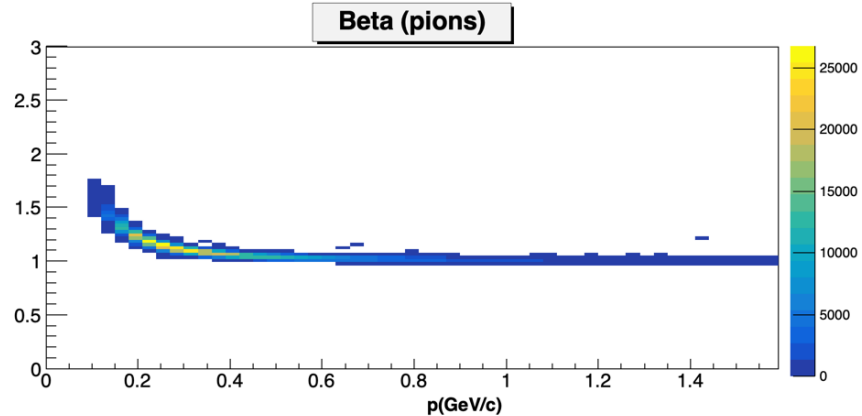
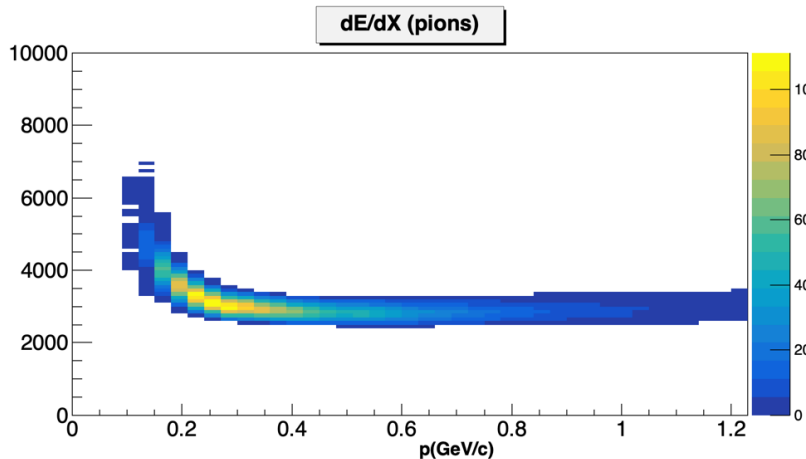
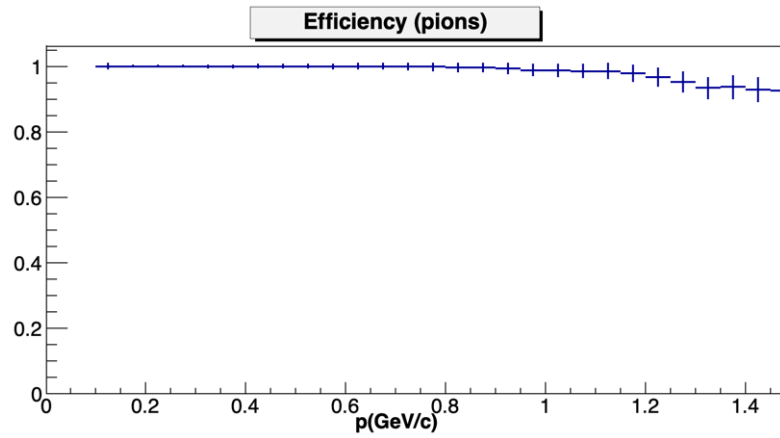
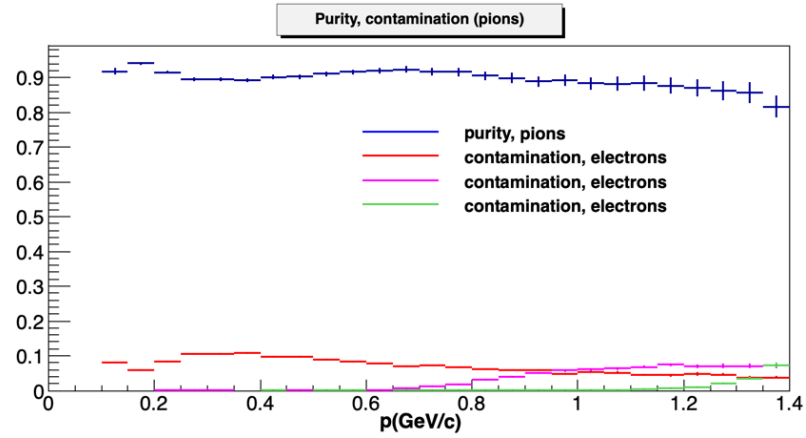
- Simulation of Au+Au collisions with UrQMD and vHLLE+UrQMD models for different collision energies (**done**)
- Software development for: (**done**)
 - femtoscopic analyses
 - factorial moments of multiplicity distributions
 - other activities
- Femtoscopic analysis and extraction of source functions for pions and kaons for models with different Equation of State (EoS): first-order phase transition (1PT), crossover (XPT), no phase transition (**done**)
- Investigation of the detector effects (track-merging and track-splitting in TPC) on femtoscopic measurements and factorial moments (**done**)

First physics (very preliminary, UrQMD MC)

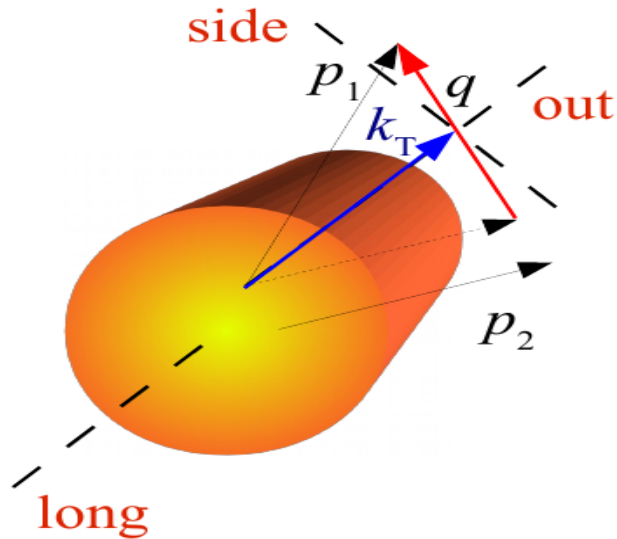
- First look with UrQMD
- Bi+Bi $\sqrt{s_{NN}} = 7.7$ GeV, 200K “good” events 0-10% centrality
- $\sqrt{s_{NN}} = 7.7$ GeV \rightarrow STAR data exists
- $\pi\pi$ one dimension correlation function for a few k_T ranges
0.15-0.25, 0.25-0.35,...,0.55-0.65 GeV/c
- Possible to study m_T dependence of 1D femtoscopic radius for a few centrality bins
- Need to have full simulation chain
(generator \rightarrow GEANT \rightarrow reconstruction) for realistic estimations



MPD response for femtoscopy(standard MPD PID)



LCMS reference frame



$$m_T = \sqrt{k_T^2 + m_\pi^2}$$

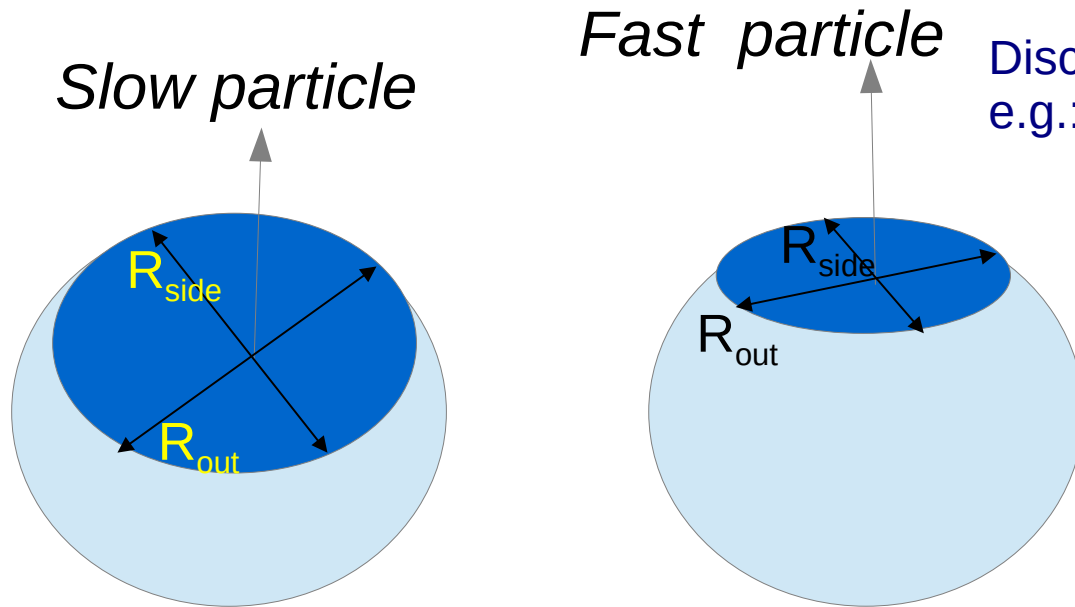
Longitudinally Co-Moving
System (LCMS):

$$p_{1,long} = -p_{2,long}$$

- For charged pions measurement in 3 dimensions, giving 3 independent sizes in Longitudinally Co-Moving System
- The Bertsch-Pratt decomposition of q :
 - Long along the beam: sensitive to longitudinal dynamics and evolution time
 - Out along k_T : sensitive to geometrical size, emission time and space-time correlation
 - Side perpendicular to Long and Out: sensitive to geometrical size
- For statistically challenged analyses, measurement in one dimension (giving only one size) in Pair Rest Frame

Femtoscscopy with expanding source $\rightarrow m_T$ -dependence

- $\mathbf{x-p}$ correlations \rightarrow interference dominated by particles from nearby emitters.
- Interference probes only parts of the source at close momenta – **homogeneity regions**.
- Longitudinal and transverse expansion of the source \rightarrow significant reduction of the radii with increasing pair velocity, consequently with k_T (or $m_T = (m^2 + k_T^2)^{1/2}$)



Discussed in
e.g.:

Kolehmainen, Gyulassy'86
Makhlin-Sinyukov'87
Pratt, Csörgö, Zimanyi'90

$$R_{\text{side}} \sim R / (1 + m_T \beta_T^2 / T)^{1/2}$$

β_T collective transverse flow
assuming a longitudinal boost
invariant expansion

$$R_{\text{long}} \sim \tau (T/m_T)^{1/2}$$

$$R_{\text{out}}^2 \sim R_{\text{side}}^2 + 1/2 (T/m_T)^2 \beta_T^2 \tau^2$$

Femtoscscopy with expanding source

Interference probes only parts of the source at close momenta – **homogeneity regions**.

[Yu.M. Sinyukov, Nucl. Phys. A 566, 589 (1994);]

Figures and consideration from A. Kisiel Phys.Rev. C81 (2010) 064906

- A particle emitted from a medium will have a collective velocity β_f and a thermal (random) one β_t
- As observed p_T grows, the region from where pairs with small relative momentum can be emitted gets smaller and shifted to the outside of the source

