### $\eta_c$ -production at SPD NICA

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### Outline

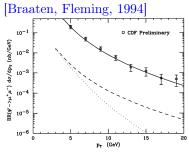
- ► Short theoretical introduction: NRQCD-factorization and Color-Evaporation model
- $\blacktriangleright$  Measurement of  $\eta_c$ -production at LHCb, HQSS-puzzle
- ▶ Predictions for SPD-NICA

# A bit of history

Historically, the first model of heavy-quarkonium production was the **color-singlet model**: The production of state  $X_Q$   $(J/\psi, \chi_{cJ}, ..., \Upsilon(nS), \chi_{bJ}, ...)$  is dominated by production of **color-singlet**  $Q\bar{Q}$ -pair with L and S quantum numbers given by NR potential model for this state. Probability of hadronization is proportional to  $|\Psi^{(k)}(0)|^2$ , (k=0,1,...) from potential model.

This model has two problems:

- Leads to a wrong shape of  $p_T$ -spectrum at high energies (Tevatron, LHC) both at LO and NLO of CPM and in  $k_T$ -factorization, which **under-estimates** the cross-section for  $p_T > 10$  GeV by factor of 30 (Tevatron  $\psi(2S)$  puzzle).
- ► Is theoretically inconsistent at NLO for production of *P*-wave states: In QCD, non-cancelling IR-divergences arise at NLO.



Dotted line – LO CPM color-singlet contribution. Solid line –  ${}^3S_1^{(8)}$ .

# NRQCD and Color-Evaporation model

To solve above-mentioned problems, two approaches have been proposed: NRQCD-factorization and Color-Evaporation Model. Both models are well-defined to all orders in  $\alpha_s$ , but NRQCD-factorization is viewed as more "rigorous" approach by the community.

- ▶ In (Improved-)Color-Evaporation Model: all  $Q\bar{Q}$  states with  $M_X < M_{Q\bar{Q}} < 2M_{\text{(open flav. Q-meson)}}$  hadronize to quarkonium X with the same probability  $F_X$ , independent on  $Q\bar{Q}$ -quantum numbers
- ▶ Optionally [Ma, Vogt, 2016] ICEM takes into account kinematic (soft-gluon recoil) corrections from the difference of masses  $M_{Q\bar{Q}}$  and  $M_X$  using simple relation  $p_T(X) = p_T(Q\bar{Q}) \times M_X/M_{Q\bar{Q}}$ .
- ▶ ICEM can be viewed as NRQCD-factorization without velocity-scaling rules for probabilities  $F_X$ .

## NRQCD and Color-Evaporation model

To solve above-mentioned problems, two approaches have been proposed: NRQCD-factorization and Color-Evaporation Model.

- ▶ NRQCD-factorization: Different L, S and color states of  $Q\bar{Q}$ -pair hadronize to X with different "probability" long-distance matrix element (LDME):  $\left\langle \mathcal{O}^{X} \left[^{2S+1}L_{J}^{(\text{color})}\right] \right\rangle$ .
- LDME-s of states different from CSM-state are suppressed by powers of  $v^2$  ( $\sim 0.3$  for  $J/\psi$ ,  $\sim 0.1$  for  $\Upsilon$ ) velocity-scaling rules for LDMEs. E.g. for  $J/\psi$  and  $\psi(2S)$ : CSM= $^3S_1^{(1)} = O(1)$  and  $^3P_J^{(8)}$  and  $^3S_1^{(8)}$ ,  $^1S_0^{(8)}$ , contribute up to  $O(v^4)$ .

# Velocity-scaling rules and HQSS-relations

Velocity-scaling rules for LDMEs:

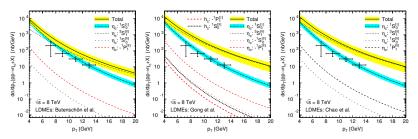
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	$^{1}S_{0}^{(1)}$	$^{3}S_{1}^{(1)}$	$^{-1}S_0^{(8)}$	$^{3}S_{1}^{(8)}$	$^{1}P_{1}^{(1)}$	$^{)} {}^{3}P_{0}^{(1)}$	$^{)} {}^{3}P_{1}^{(1)}$	$^{)} {}^{3}P_{2}^{(1)}$	$^{1}P_{1}^{(8)}$	$^{3}P_{0}^{(8)}$	$^{3}P_{1}^{(8)}$	$^{3}P_{2}^{(8)}$
$\eta_c$	1		$v^4$	$v^3$					$v^4$			
$J/\psi$		1	$v^3$	$v^4$	ì					$v^4$	$v^4$	$v^4$
$h_c$			$v^2$		$v^2$							
$\chi_{c0}$				$v^2$	ì	$v^2$						
$\chi_{c1}$				$v^2$	ı		$v^2$					
$\chi_{c2}$				$v^2$				$v^2$				
, 0												

HQSS-relations between LDMEs of  $\eta_c$  and  $J/\psi$ :

$$\left\langle \mathcal{O}^{\eta_c} \left[ {}^{1}S_0^{(1/8)} \right] \right\rangle = \frac{1}{3} \left\langle \mathcal{O}^{J/\psi} \left[ {}^{3}S_1^{(1/8)} \right] \right\rangle + O(v^2), 
\left\langle \mathcal{O}^{\eta_c} \left[ {}^{3}S_1^{(8)} \right] \right\rangle = \left\langle \mathcal{O}^{J/\psi} \left[ {}^{1}S_0^{(8)} \right] \right\rangle + O(v^2), 
\left\langle \mathcal{O}^{\eta_c} \left[ {}^{1}P_1^{(8)} \right] \right\rangle = 3 \left\langle \mathcal{O}^{J/\psi} \left[ {}^{3}P_0^{(8)} \right] \right\rangle + O(v^2).$$

## Test of HQSS-relations

[Butenschön, Kniehl, He, 2014] Experimental data from [LHCb, 2014]:  $pp \to \eta_c(\to p\bar{p}) + X$  with  $\sqrt{S} = 7$  and 8 TeV.



#### Conclusions:

- ► CS-model ( ${}^1S_0^{(1)}$ ) describes LHCb data! CO-contrs. lead to significant overshoot.  $\Rightarrow$  HQSS-relations fail!
- ▶ Feeddown from  $h_c$  is negligible

### $\eta_c$ at SPD-NICA?

If pure-CS picture of  $\eta_c$ -production is correct, then only gluon-induced process contributes at LO:

$$g + g \rightarrow c\bar{c} \left[ {}^{1}S_{0}^{(1)} \right],$$

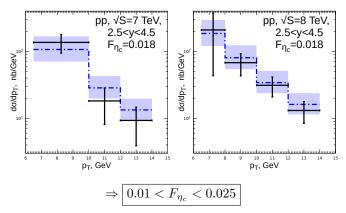
and it has no free-parameters:  $\left\langle \mathcal{O}^{\eta_c} \left[ {}^1S_0^{(1)} \right] \right\rangle \propto |\Psi(0)|^2.$ 

- ▶ LHCb has done measurement at high  $\sqrt{S}$  and forward rapidity. More measurements in other PS-regions needed to check CS hypothesis!
- ▶ LHCb used  $\eta_c \to p\bar{p}$ -decay with  $B = 1.45 \times 10^{-3}$ . What about  $\eta_c \to K\bar{K}\pi$  with B = 7.3%? At lower energy comb. background is lower, right? However neutral pion...

We decided to estimate  $\eta_c$   $p_T$ -spectrum in  $p_T$ -collisions with  $\sqrt{S} = 24$  GeV in ICEM and NRQCD (CS-model).

## Description of LHCb data in ICEM+LO PRA

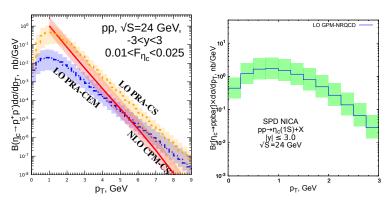
We use LO of Parton Reggeization Approach  $(R_{+}(\mathbf{q}_{T1}) + R_{-}(\mathbf{q}_{T2}) \rightarrow c + \bar{c})$  to compute  $c + \bar{c}$ -production cross-section and tune  $F_{\eta_c}$ :



For comparison,  $F_{J/\psi} \simeq 0.02$ .

### Results for SPD-NICA

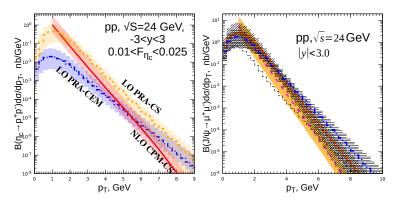
Predictions in NLO CPM CSM[Kniehl, Butenshön], LO PRA ICEM and LO PRA CSM shown in the left plot. Right plot – LO GPM CSM (with  $\langle k_T \rangle = 1$  GeV). Cross-section× $B(\eta_c \to p\bar{p})$ :



LO PRA CSM:  $\sigma \times B(\eta_c \to p\bar{p}) = 0.61^{+0.76}_{-0.43} \text{ nb.}$ 

# Comparison with $J/\psi$

Predictions in NLO CPM CSM[Kniehl, Butenshön], LO PRA ICEM and LO PRA CSM shown in the left plot. Cross-section× $B(\eta_c \to p\bar{p})$ :



Cross section is  $\sim 0.1$  compared with the  $J/\psi \times B(J/\psi \to \mu^+\mu^-)$ .

### Outlook

- Any measurement of  $\eta_c$  production, even with large errors, is useful for development of heavy-quarkonium production theory
- ▶ If CS-model is valid  $\Rightarrow \eta_c$  is the golden probe for proton structure. Couples to gluons, TMD-factorization is valid. One can study spin-asymmetries etc.
- ▶  $d\sigma/dp_T \times B(\eta_c \to p\bar{p}) \sim 1 \text{ nb/GeV}$  is obtained at  $\sqrt{S} = 24 \text{ GeV}$ .
- ► Any hope to see this?

### Thank you for your attention!