

Study of $d^*(2380)$ in a chiral quark model

Yubing Dong

(董宇兵)

Collaborators: Fei Huang, Qifang Lv,
Pengnian Shen, Zhongye Zhang

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Content

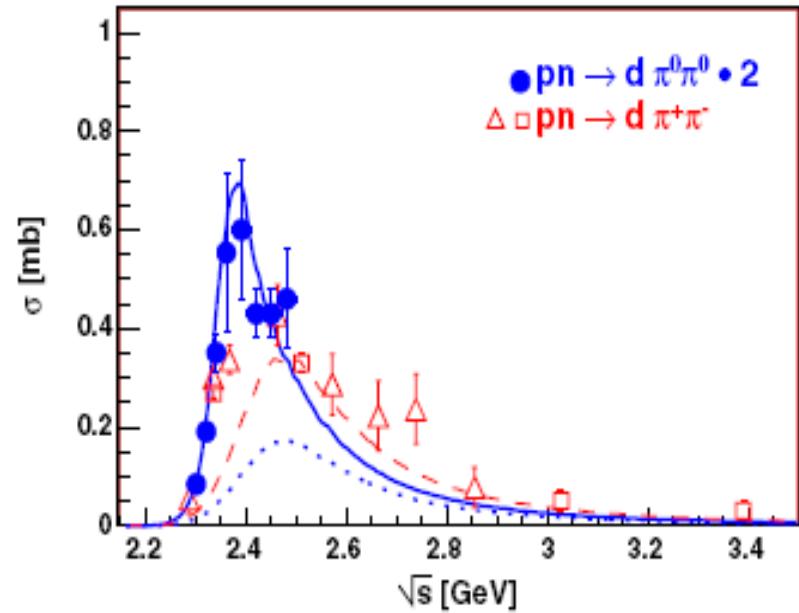
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1. Observation of $d^*(2380)$



cerncourier.com/cws/article/cern/57836

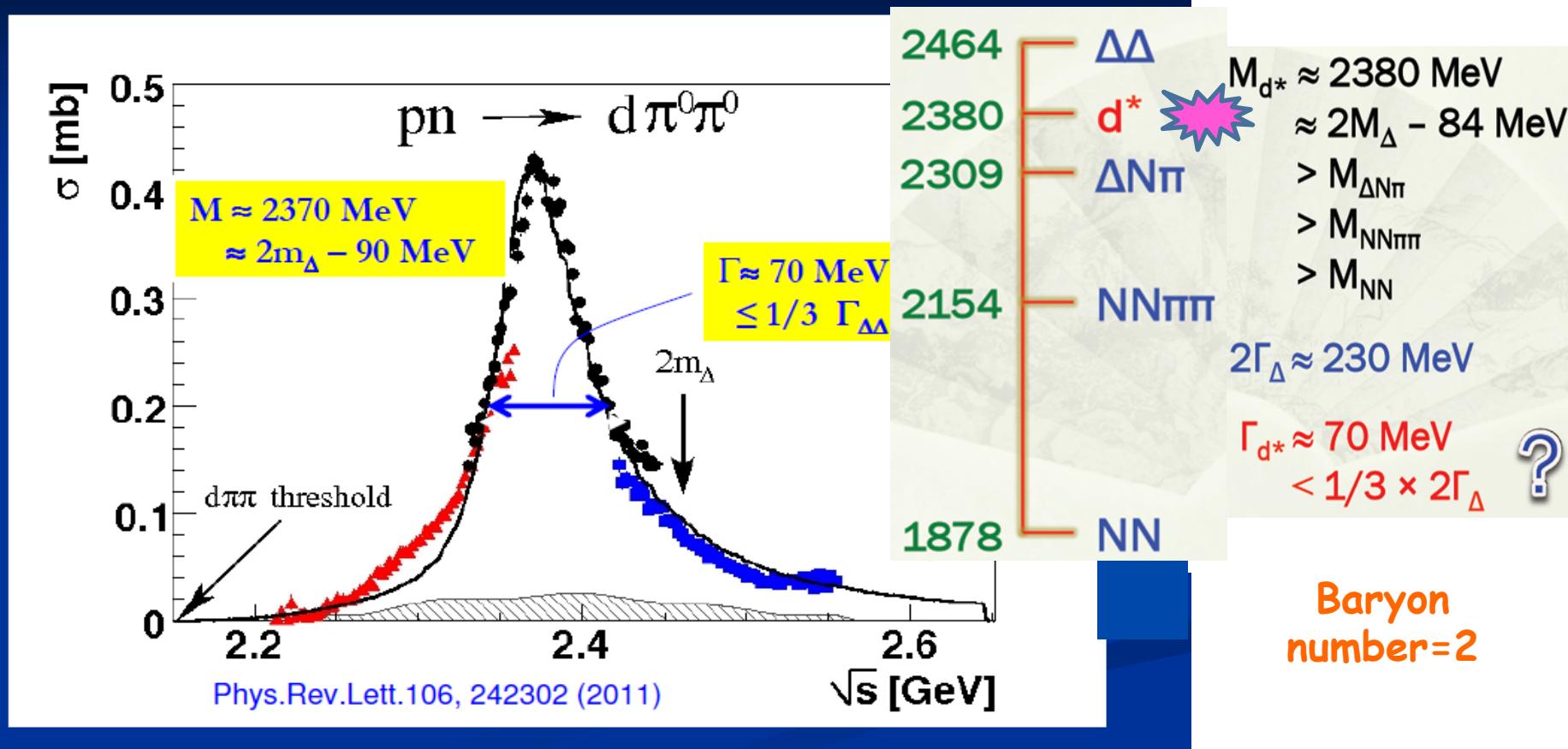
PRL 112 (2014) 202301



Experiments at the Jülich Cooler Synchrotron (COSY) have found compelling evidence for a new state in the two-baryon system, with a mass of 2380 MeV, width of 80 MeV and quantum numbers $I(J^P) = 0(3^+)$.

The d^* Resonance $I(J^P) = 0(3^+)$

Unusual
narrow width



$$\Gamma_{d^*} \approx 70 \text{ MeV}$$

$$M_{\Delta N\pi} = 2310 \text{ MeV}$$

$$M_{d^*} \approx 2380 \text{ MeV}$$

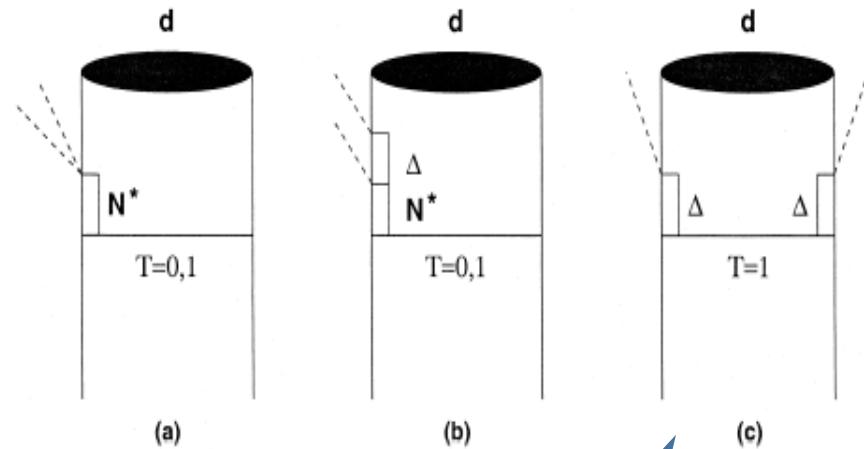
$$M_{\Delta\Delta} = 2464 \text{ MeV}$$

Fusion $2\pi^0$ production

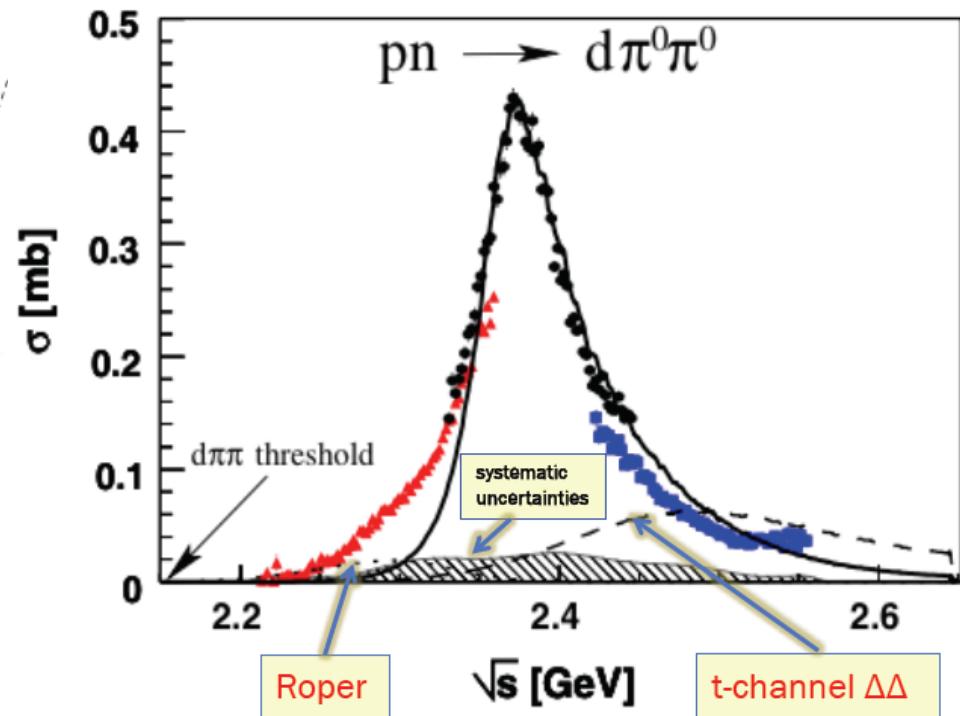
$pd \rightarrow p_{\text{spectator}} d \pi^0 \pi^0$

Possible understandings

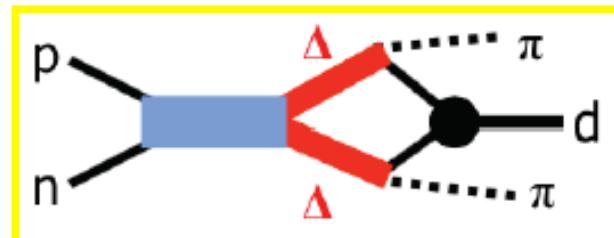
WASA-at-COSY: PRL106(2011)242302



$\Delta\Delta$ resonance?



Neither NN
(Roper), nor $\Delta\Delta$
Intermediate state



24/7/17

$$I(J^P) = 0(3^+)$$

$$M \approx 2380 \text{ MeV}$$

$$\Gamma \approx 70 \text{ MeV}$$

Signals in other reactions @ COSY

fusion 2π processes

Measured also in fusion reactions
to helium isotopes:



Non-fusion 2π processes



PRC88 (2013)055208



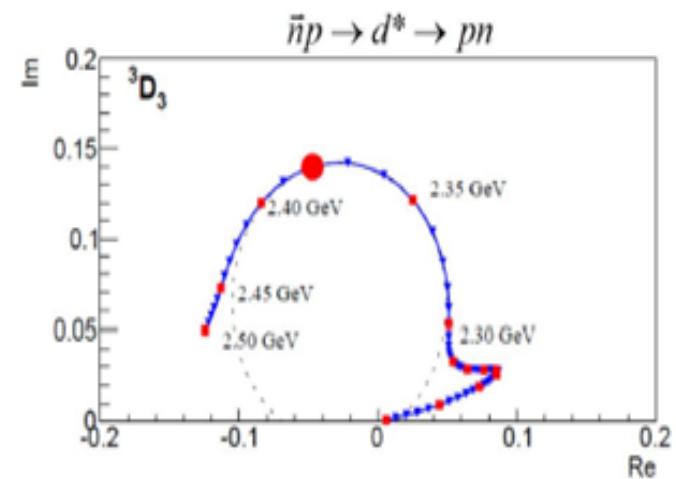
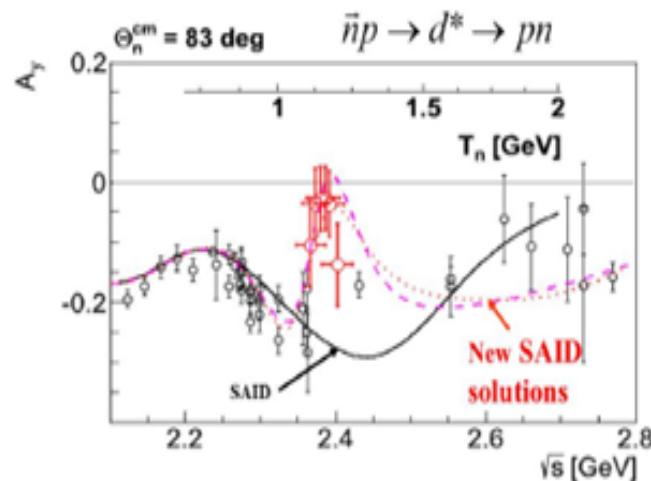
PLB 743 (2015) 325



Proc. STORI 2015



Scattering $pn \rightarrow pn$

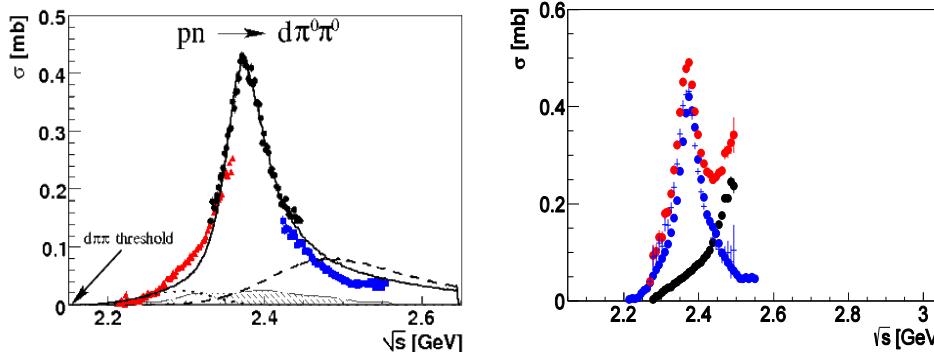


the Argand diagram of the $3D_3$
partial wave in pn scattering

d^* Strong decays

PRL 106 (2011) 242302

PLB 721 (2013) 229



● ● ● WASA data

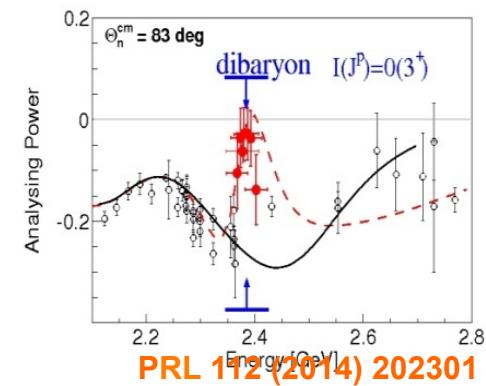
$pn \rightarrow d^*(2380)$

$pp\pi^-\pi^0$

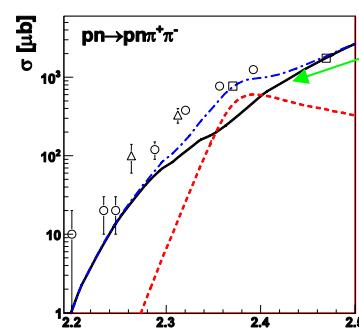
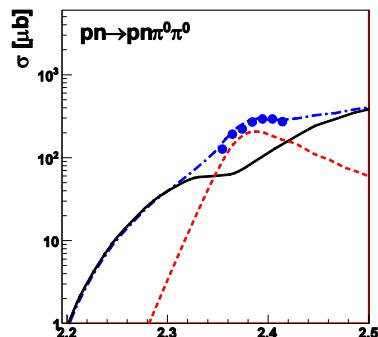
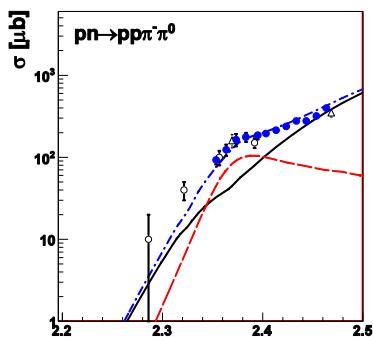
$pn\pi^0\pi^0$

$d\pi^+\pi^-$

pn



PRL 112 (2014) 202301



HADES

PRC 88 (2013) 055208

PLB 743 (2015) 325

Proc. STORI 2015

d* Characters:

- d* mass locates between $\Delta\Delta$ and $\Delta N\pi$
Effect from threshold is expected small
- d* narrow width → Possible 6q structure
might be different from normal hadrons

d*(2380) size

P.R.L.103(2009)162001

$$r \approx \frac{\hbar c}{\sqrt{2m\epsilon}}$$

d* Binding energy ~ 80 MeV

d* rms is about 0.5fm ($m = m_\Delta = 1.232\text{GeV}$)

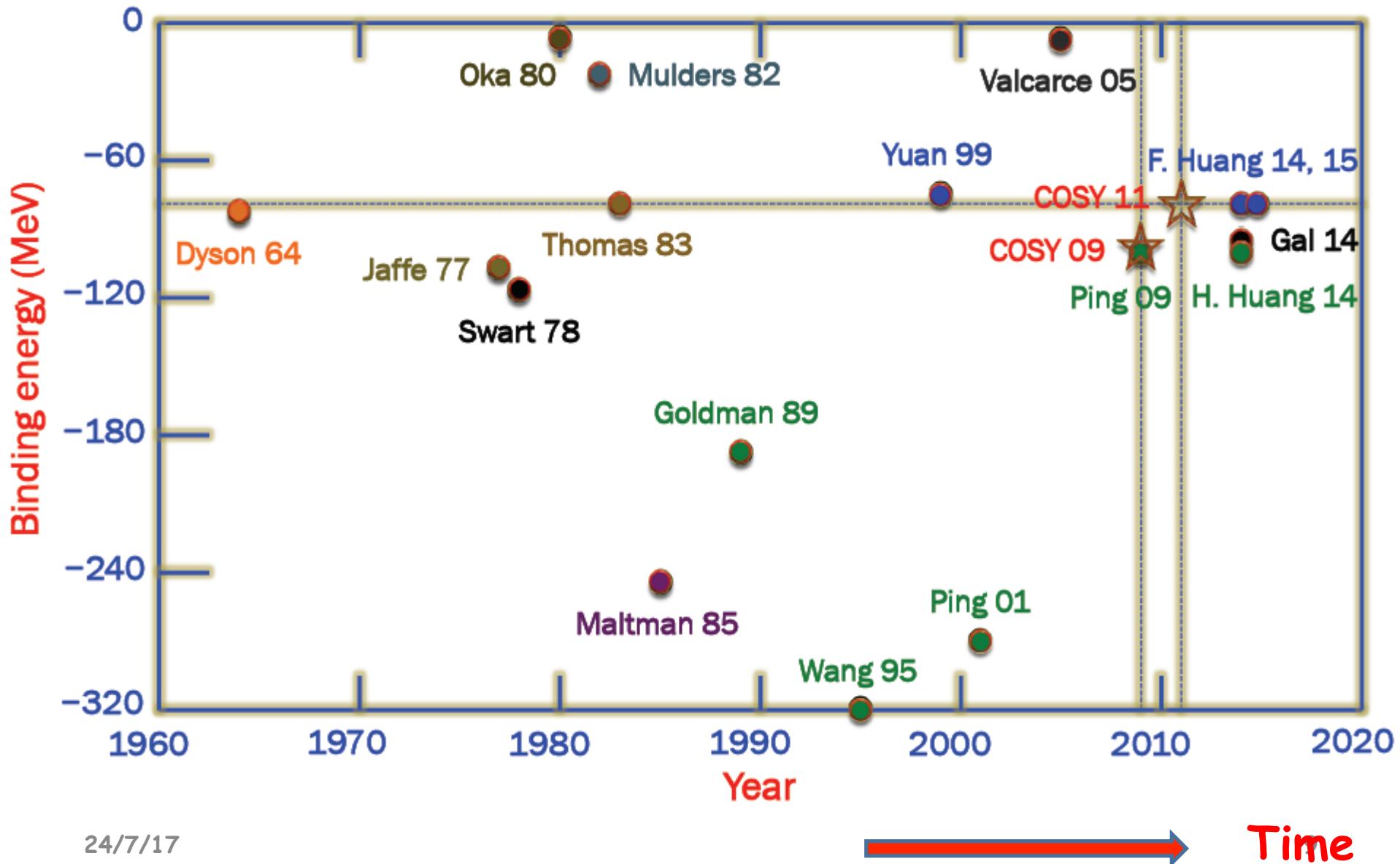


Probably a compact structure

Heinz Clement, Progress in Particle and Nuclear Physics,

93 (2017), 195-142

2. Possible interpretations *



Before the discovery of d*

- A pioneer discussion from symmetry: J.Dyson, PRL 13, 815 (1964)

Two baryon systems
SU(6) classification :

Anti-symmetric representations:
Non-strange states

$$(I, J) = (3,0)(2,1)(1,0)(1,2)(0,1)(0,3) \text{ 6 states}$$

Casmir operator reduced
a mass formula

$$M = A + B' (T(T+1)) + B'' (J(J+1))$$

If $B' = B'' = B$, the obtained deuteron mass 1876MeV, and then, obtain A,

Choose $B = 50\text{MeV}$, then, $M_{d^*} = 2376\text{MeV}$

• Chiral SU(3) Quark Model

X.Q.Yuan, Z.Y.Zhang, Y.W.Yu, P.N.Shen, PRC 60, 045203 (1999)

$\Delta\Delta + CC$ structures

- ✓ Parameters: from NN phase shifts, YN cross sections, deuteron binding & radius
- ✓ dynamical calculation for its binding $d^*(\Delta\Delta + CC \text{ (IS=03)})$

- ✓ • predict: d^* binding

$BE \approx 40-80 \text{ MeV} [\text{SU}(3)]$

(Present data: 84 MeV)

- Conclusions: CC channel is important, suppress the binding about 20MeV.

- WFs and decays not calculated.

TABLE III. Deltaron binding energy $B(\text{MeV})$ with different parameters. $B = -(E_{\text{deltaron}} - 2M_\Delta)$.

	$(\Delta\Delta+CC)$	$(L=0+L=2)$		
$B(\text{OGE}+\pi,\sigma)$	79.7	97.1	97.9	113.4
$B[\text{OGE}+\text{SU}(3)]$	37.3	64.2	52.4	79.2
$b_N(\text{fm})$	0.505	0.60	0.505	0.60
$m_\sigma(\text{MeV})$	625	625	550	550

- Binding energy: 40 ~ 80 MeV
- CC: 10 ~ 20 MeV increase in binding energy

Understanding d^* after the discovery

- 6q dominant (quark-level)

* Argument

M.Bashkanov, S.J.Brodsky H.Clement, PLB727, 438(2013)

* $\Delta\Delta+CC$ Interpretations

- a, arXiv: 1408.0458 [nucl-th] (CPC 39 (2015) 071001]
- b, SCIENCE CHINA 59 (2016) 622002
- c, PRC 91 (2015) 064002
- d, arXiv: 1603.08748 [hep-ph], PRC 94, 014003 (2016)

Binding energy, wave functions, decays

We conclude from such observations that d^* must be of an unconventional origin, possibly indicating a genuine six-quark nature. With the predominant decay of d^* being $d^* \rightarrow \Delta\Delta$ ($BR(d^* \rightarrow \Delta\Delta)/BR(d^* \rightarrow pn) = 9 : 1$), one could naively expect d^* to be a so-called a "deltaron" denoting a deuteron-like bound state of two Δ s. However, the narrow width of d^* contradicts this simple assumption. A deltaron would need to have 90 MeV binding energy, i.e. 45 MeV per Δ , which would lead to a reduction of width from $\Gamma_{\Delta\Delta} = 230$ MeV to $\Gamma_{\Delta\Delta} = 160$ MeV, using the known momentum dependence of the width of the Δ resonance. This is more than twice what is observed.

Ansatz

$$|\Psi_{d^*}\rangle = \sqrt{\frac{1}{5}}|\Delta\Delta\rangle + \sqrt{\frac{4}{5}}|6Q\rangle$$

$$|\Psi_{d^*}\rangle = \sqrt{\frac{4}{5}}|\Delta\Delta\rangle - \sqrt{\frac{1}{5}}|6Q\rangle.$$

Here $\Delta\Delta$ means the asymptotic $\Delta\Delta$ configuration and $6Q$ is the genuine "hidden color" six-quark configuration. The first solution denotes a S^6 quark structure (all six quarks in the S-shell).

$\Delta\Delta$ width:

$$\Gamma_{\Delta\Delta} = 230 \text{ MeV}$$

Binding about 90MeV

$$\Gamma_{\Delta\Delta} = 160 \text{ MeV}$$

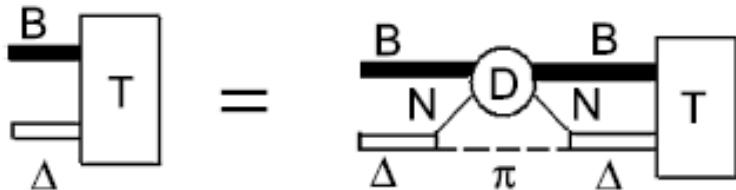
The observed d^* must be of an unconventional origin, probably 6q structure.

- d^* narrow width

- **$\Delta N\pi$ 3-body bound state (π induced $D_{12}\pi$ scenario)**

$$B = \Delta' (\Delta (\Gamma=0))$$

A. Gal et al. NPA 928, 73(2014)



S-matrix pole equation for $D_{03}(2370)$ $\Delta\Delta$ dibaryon



$N\Delta$ dibaryon's Lippmann-Schwinger equation

a). $\Delta' N$ is $NN\pi$ 3-body system:

$N\pi$ Interaction: P33 channel separable potential (Δ')

By solving Faddeev eq. to obtain $\Delta' N$ interaction,

D_{12} -Pole : (2165~2174) - i (64~60) MeV

b). Take $\Delta'\Delta$ as $\Delta' N \pi$ 3-body system:

$\Delta' N$ Interaction from solution a), $N\pi$ separable potential

Solving Faddeev eq. to get the $\Delta' N \pi$ resonance

$$M_{\Delta'N\pi} = 2383 \text{ MeV}$$

$$\Gamma_{\Delta'N\pi} \approx 82 \sim 94 \text{ MeV}$$

$$m_\Delta = (1211 + i X 49.5) \text{ MeV}$$

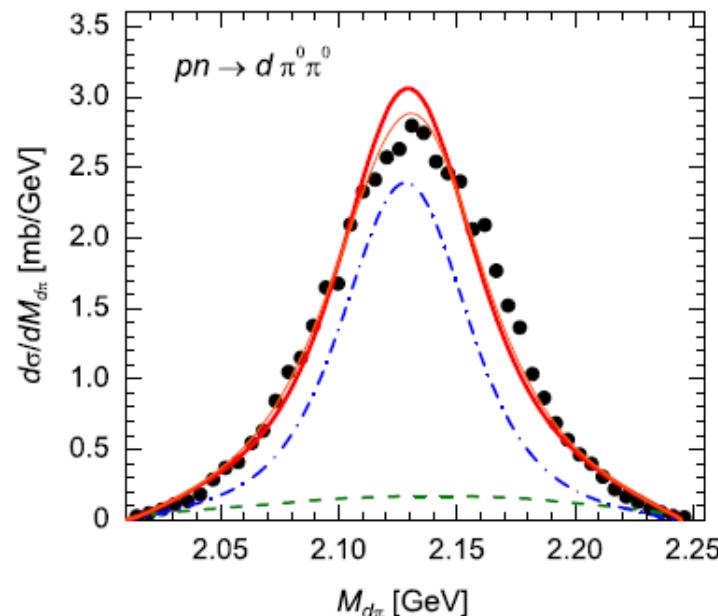
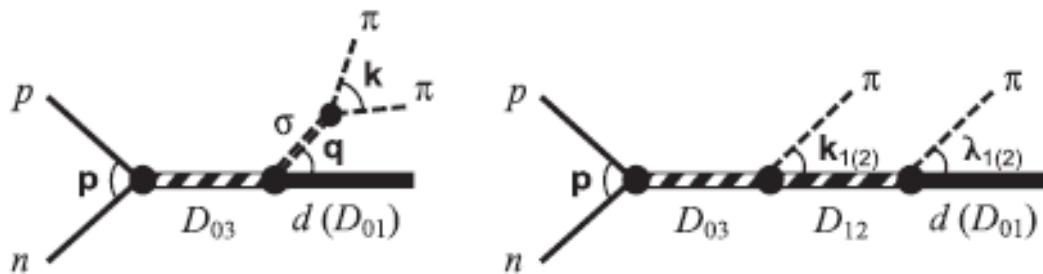
$$M_{\Delta'N\pi} = 2343 \text{ MeV}$$

$$\Gamma_{\Delta'N\pi} \approx 48 \sim 62 \text{ MeV}$$

Where $X = 1$ 或 $2/3$

- $d\sigma$ & $\mathcal{D}_{12}\pi$

Hadronic model



The dot-dashed line gives the "D12(2150) contribution to the two-body decay of D03(2380), and the dashed line gives a scalar-isoscalar sigma-meson emission contribution.

- QCD Sum rule (6q) H.X.Chen, PRC 91, 025204 (2015)

$$M_{d^*} = 2.4 \pm 0.2 \text{ GeV}$$

.....

3. d^* structures in chiral constituent quark model

q-q Interactions

$$V_{ij} = V_{ij}^{\text{conf}} + V_{ij}^{\text{OGE}} + V_{ij}^{\text{ch}} + V_{ij}^{\text{chv}}$$

$$V_{ij}^{\text{ch}} = \sum_a (V_{ij}^{s(a)} + V_{ij}^{ps(a)})$$

Scalar

Pseudoscalar

vector

Interactive Lagrangian

$$\mathcal{L}_I = -g_{ch} \bar{\Psi} \left(\sum_{a=0}^8 \sigma_a \lambda_a + i \sum_{a=0}^8 \pi_a \lambda_a \gamma_5 \right) \Psi$$

b_u , m_σ are determined by fitting to the experimental data for NN systems

$$\text{BE}_d^{\text{exp't}} = 2.22 \text{ MeV}$$



	SU(3)	Ext. SU(3) (f/g=0)	Ext. SU(3) (f/g=2/3)
Deuteron Binding energy(MeV)	2.09	2.24	2.20
Fraction of Wave Function (%)	NN (L=0)	93.68	94.66
	NN (L=2)	6.32	5.34

$$b_u = 0.5 \text{ fm}$$

$$b_u = 0.45 \text{ fm}$$

$$m_\sigma = 595 \text{ MeV}$$

$$m_\sigma = 535 \sim 547 \text{ MeV}$$

NN Phase shifts: Good



- **a, RGM method for WFs:** $I(J^P) = 0(3^+)$

$$\Psi_{6q} = \mathcal{A} [\phi_\Delta(\xi_1, \xi_2) \phi_\Delta(\xi_4, \xi_5) \eta_{\Delta\Delta}(r) + \\ \phi_C(\xi_1, \xi_2) \phi_C(\xi_4, \xi_5) \eta_{CC}(r)]_{S=3, I=0, C=(00)}.$$

$\Delta : (0s)^3 [3]_{\text{orb}}, S = 3/2, I = 3/2, C = (00),$

$C : (0s)^3 [3]_{\text{orb}}, S = 3/2, I = 1/2, C = (11),$

\mathcal{A} : Anti-symmetrized operator

ϕ : Internal cluster WF

η : Relative WF from RGM with interactions

$\mathcal{A} = 1 - 9P_{36}, \quad P_{36}$ Quark Exchange Operator

• **b**, Hadronization

Due to the exchange operator, functions are not orthogonal

$$\Psi_{6q} = (1 - 9P_{36})[\phi_\Delta \phi_\Delta \eta_{\Delta\Delta}(r)]_{SIC=30(00)} + (1 - 9P_{36})[\phi_C \phi_C \eta_{CC}(r)]_{SIC=30(00)}$$

(1) (2)
↓ ↓
↑ ↑
(3) (4)

$$I(J^P) = 0(3^+)$$

Using the projection method to integrate out the internal coordinates inside the clusters (or Hadronization)

Relative Wave function (or Channel Wave function)

$$\chi_{\Delta\Delta}(r) \equiv \langle \phi_\Delta(\xi_1, \xi_2) \phi_\Delta(\xi_4, \xi_5) | \Psi_{6q} \rangle, \quad \text{Contains (1), (2),(4) terms}$$

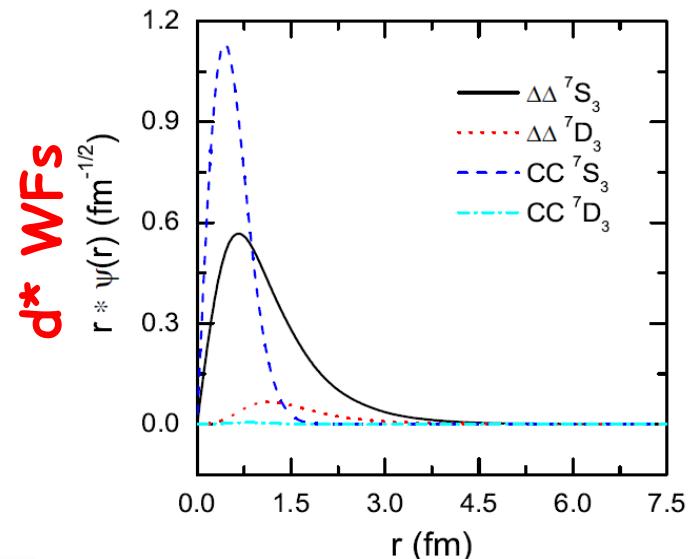
$$\chi_{CC}(r) \equiv \langle \phi_C(\xi_1, \xi_2) \phi_C(\xi_4, \xi_5) | \Psi_{6q} \rangle, \quad \text{Contains (3), (2),(4) terms}$$

$$\Psi_{d^*} = |\Delta\Delta\rangle \chi_{\Delta\Delta}(r) + |CC\rangle \chi_{CC}(r) \quad \chi_{\Delta\Delta} \text{ and } \chi_{CC} \text{ orthogonal}$$

Quark exchange effect is included

• Binding energy and relative wave function

Parameters are determined by fitting to the data, then the binding and wave functions are calculated.



	SU(3)		Ext. SU(3) (f/g=0)		Ext. SU(3) (f/g=2/3)	
	$\Delta\Delta$ (L=0,2)	$\Delta\Delta\text{-CC}$ (L=0,2)	$\Delta\Delta$ (L=0,2)	$\Delta\Delta\text{-CC}$ (L=0,2)	$\Delta\Delta$ (L=0,2)	$\Delta\Delta\text{-CC}$ (L=0,2)
d^* Binding Energy(MeV)	28.9	47.9	62.3	83.9	47.9	70.3
Fraction of Wave Function (%)	ΔΔ (L=0)	97.18	33.11	98.01	31.22	97.71
	ΔΔ (L=2)	2.82	0.62	1.99	0.45	2.29
	CC (L=0)	0	66.25	0	68.33	0
	CC (L=2)	0	0.02	0	0.00	0

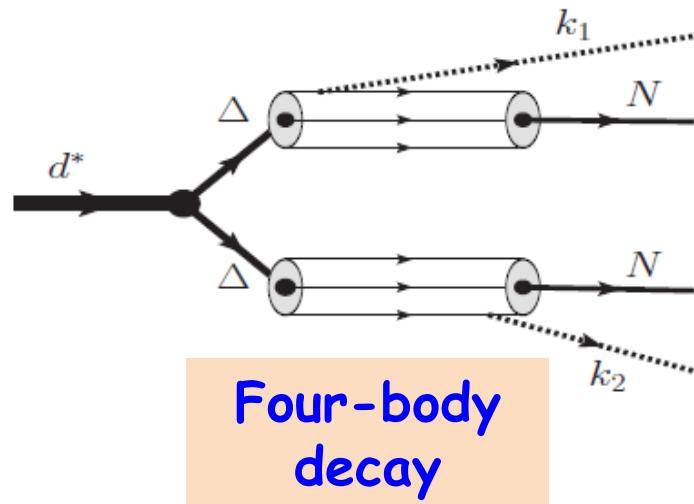
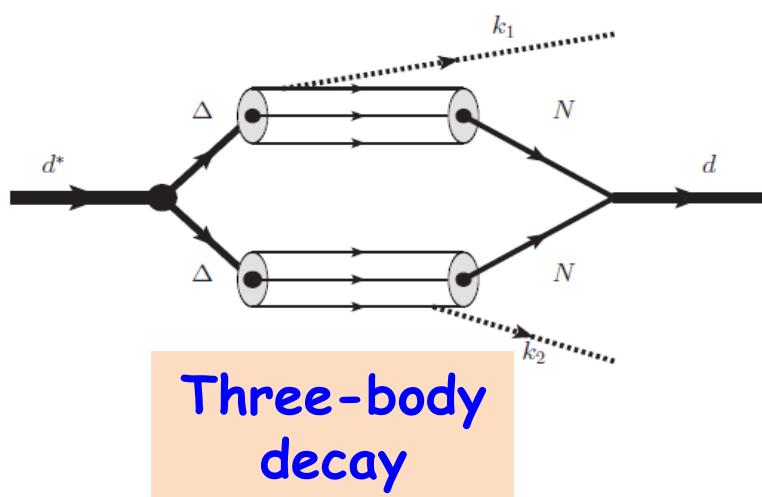
• d^* decay widths

$$d^* \rightarrow d\pi^0\pi^0 (d\pi^+\pi^-)$$

$$d^* \rightarrow pp\pi^-\pi^0$$

$$d^* \rightarrow np\pi^0\pi^0 (np\pi^+\pi^-)$$

$$d^* \rightarrow nn\pi^0\pi^+$$



$qq\pi$ Interaction

$$\mathcal{H}_{qq\pi} = g_{qq\pi} \vec{\sigma} \cdot \vec{k}_\pi \tau \cdot \phi \frac{1}{(2\pi)^{3/2} \sqrt{2\omega_\pi}},$$

Simon Capstick, PRD46, 2864

$\Delta \rightarrow N\pi$ Coupling & form factor

$$\Gamma_{\Delta \rightarrow \pi N} = \frac{4}{3\pi} k_\pi^3 (g_{qq\pi} I_o)^2 \frac{\omega_N}{M_\Delta},$$

Calculated widths: PRC91,064002; 94,014003

Discussions:

	Theor.(MeV)	Expt.(MeV)
$d^* \rightarrow d\pi^+\pi^-$	16.8	16.7
$d^* \rightarrow d\pi^0\pi^0$	9.2	10.2
$d^* \rightarrow pn\pi^+\pi^-$	20.6	21.8
$d^* \rightarrow pn\pi^0\pi^0$	9.6	8.7
$d^* \rightarrow pp\pi^0\pi^-$	3.5	4.4
$d^* \rightarrow nn\pi^0\pi^+$	3.5	4.4
$d^* \rightarrow pn$	8.7	8.7
Total	71.9	74.9

*Isospin breaking

$$\frac{\Gamma(d^* \rightarrow d\pi^+\pi^-)}{\Gamma(d^* \rightarrow d\pi^0\pi^0)} \sim 1.8 \quad (1.6, \quad 2.0)$$

Ideal

$$\frac{\Gamma(d^* \rightarrow pn\pi^+\pi^-)}{\Gamma(d^* \rightarrow pn\pi^0\pi^0)} \sim 2.2 \quad (2.5, \quad 2.5)$$

M_{d^*} (MeV)	(100%) $\Delta\Delta$ 2374	Expt 2375
Decay channel	Γ (MeV)	Γ (MeV)
$d^* \rightarrow d\pi^0\pi^0$	17.0	10.2
$d^* \rightarrow d\pi^+\pi^-$	30.8	16.7
Total	132.8	74.9

*The narrow width is due to large component CC

This channel might provide a test for different interpretations.
Experiment gives 9% up-limit; the result of three-body ($\Delta\pi N$) is about 18%.

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Decay width of the $d^*(2380) \rightarrow NN\pi$ process in a chiral constituent quark model



Yubing Dong ^{a,b,c,*}, Fei Huang ^c, Pengnian Shen ^{d,a,b}, Zongye Zhang ^{a,b,c}

^a Institute of High Energy Physics, Chinese Academy of Sciences, Beijing 100049, China

^b Theoretical Physics Center for Science Facilities (TPCSF), CAS, Beijing 100049, China

^c School of Physical Sciences, University of Chinese Academy of Sciences, Beijing 101408, China

^d College of Physics and Technology, Guangxi Normal University, Guilin 541004, China

Very recently

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ABSTRACT

The width of three-body single-pion decay process $d^* \rightarrow NN\pi^{0,\pm}$ is calculated by using the d^* wave function obtained from our chiral SU(3) constituent quark model calculation. The effect of the dynamical structure on the width of d^* is taken into account in both the single $\Delta\Delta$ channel and coupled $\Delta\Delta + CC$ two-channel approximations. Our numerical result shows that in the coupled-channel approximation, namely, the hidden-color configuration being considered, the obtained partial decay width of $d^* \rightarrow NN\pi$ is about several hundred keV, while in the single $\Delta\Delta$ channel it is just about 2 ~ 3 MeV. We, therefore, conclude that the partial width in the single-pion decay process of d^* is much smaller than the widths in its double-pion decay processes. Our prediction may provide a criterion for judging different interpretations of the d^* structure, as different pictures for the d^* may result quite different partial decay width.

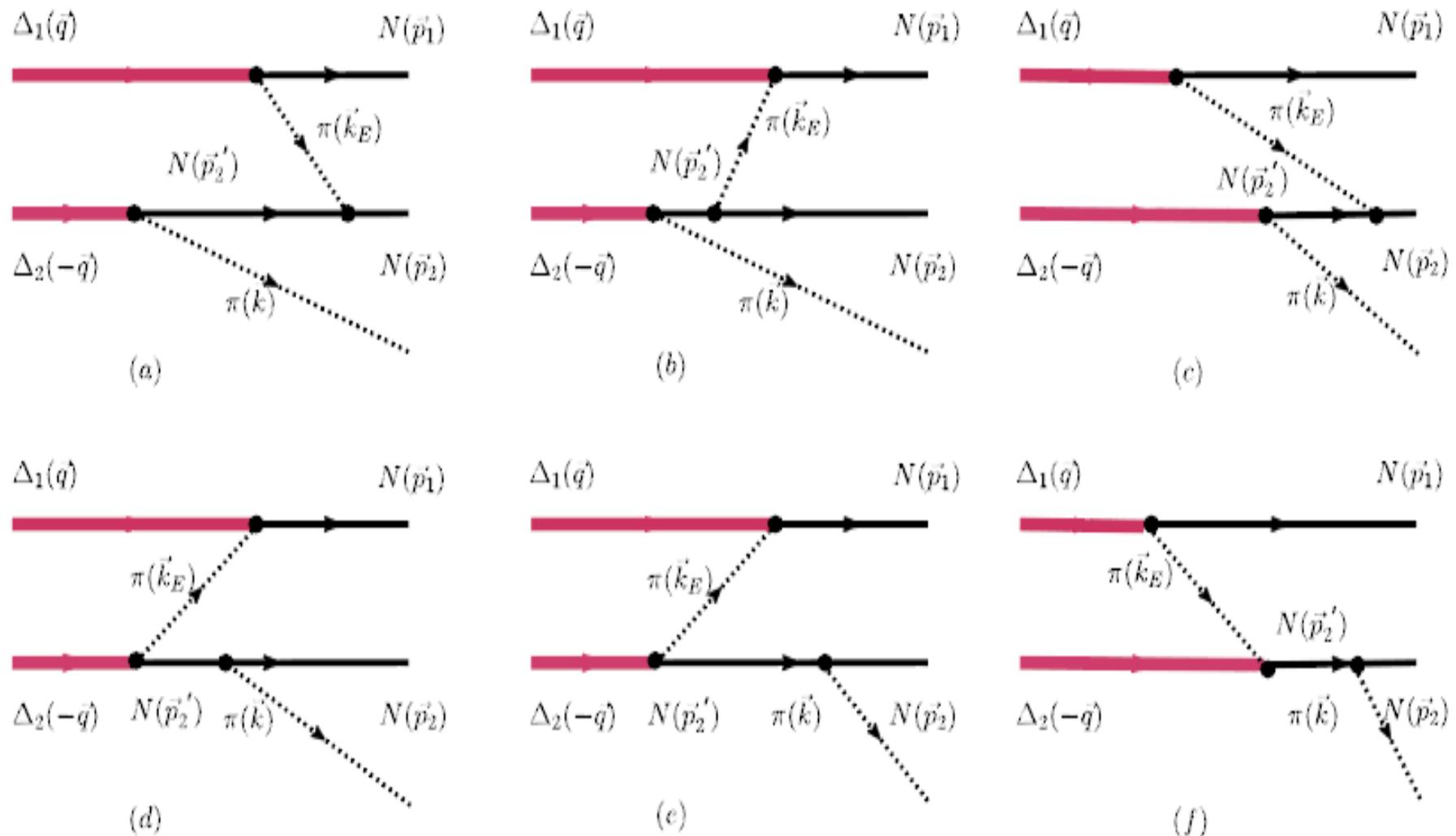
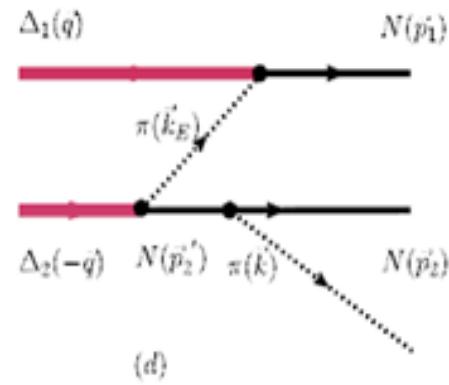


Fig. 1. Six possible ways to emit pion only from the $\Delta\Delta$ component of d^* in the $d^* \rightarrow NN\pi$ decay process. The outgoing pion with momenta \vec{k} is emitted from Δ_2 . The other six sub-diagrams with pion emitted from Δ_1 are similar, and then are not shown here for reducing the size of the figure.

$$L = L_{\pi NN} + L_{\Delta N \pi}$$



$$\Psi_{d^*} = |\Delta\Delta\rangle \chi_{\Delta\Delta}(r) + |CC\rangle \chi_{CC}(r)$$

Δ : $(0s)^3 [3]_{\text{orb}}, S = 3/2, I = 3/2, C = (00),$

C : $(0s)^3 [3]_{\text{orb}}, S = 3/2, I = 1/2, C = (11),$

From quark model $\frac{g_{\pi\Delta\Delta}^2}{4\pi} = \frac{1}{25} \frac{M_\Delta^2}{M_N^2} \frac{g_{\pi NN}^2}{4\pi}, g_{\pi\Delta\Delta}$ small

- 1, $C \rightarrow \Delta$, interaction should be color and isospin-dependent
- 2, $CC(SI=3,0) \rightarrow NN^*(1400)$, D-wave of OGE is required

The suppressions enable to ignore the contribution from the CC component in d^*

Our prediction
1%

Table 1

The calculated decay width of the $d^* \rightarrow NN\pi$ process and the widths contributed individually from the (a)-, (b)-, (c)-, (d)-, (e)-, and (f)-type diagrams (in units of MeV).

Case	Total width	(a)	(b)	(c)	(d)	(e)	(f)	sum of (a)-(f)
One ch. ($\Delta\Delta$ only)	2.276	0.550	0.306	0.267	0.0963	0.209	0.233	1.661
Two chs. ($\Delta\Delta + CC$)	0.670	0.154	0.0884	0.0789	0.0279	0.0687	0.0847	0.503

Recently Gal(arXiv:1612.05092)

In order to match the up-limit

$$\rightarrow |d^* \rangle \approx \sqrt{\frac{5}{7}} |\Delta\Delta\rangle + \sqrt{\frac{2}{7}} |N\Delta\pi\rangle$$

Of exp.

Intermediate states:

$(N, N^*, \Delta, \Delta^*)$

Low-lying resonances are considered

4. Summary

- Our understanding:

d^* with CC component dominant ($\sim 66\text{-}68\%$)

$$M \approx 2380 \text{ MeV} \quad \Gamma \approx 72 \text{ MeV}$$

$$(M^{\text{exp't}} \approx 2380 \text{ MeV} \quad \Gamma^{\text{exp't}} \approx 70\text{-}75 \text{ MeV})$$

- Other experimental measurements

$$e^+ + e^- \rightarrow \bar{d}^* + p + n \quad \Upsilon \rightarrow \bar{d} + d^*, \quad d + \bar{d}^*, \quad \bar{d}^* + d^*$$

$$\text{BR}(\Upsilon \rightarrow \bar{d} + X) \sim 2.86 \times 10^{-5}$$

- Short range interaction

If it is 6q dominant, one can get more information

Effective Δ - Δ short range interaction induced by OGE (VM)
are attractive

q-q short range int.



Thanks !

If the d^* is further confirmed by other experiments, we believe that our interpretation is reasonable. Thus, it is a resonance state with $6q$ structure dominant and moreover, the more information about the short range interaction is expected.

$\langle P_{36}^{\text{sfc}} \rangle$ exchange effect in spin-flavor-color spaces

Reason for the large component of CC (67%)

$(\Delta\Delta)_{SI=30}$	$(\Delta\Delta)_{SI=30}$	$(CC)_{SI=30}$
$(\Delta\Delta)_{SI=30}$	$(CC)_{SI=30}$	$(CC)_{SI=30}$
$\langle P_{36}^{\text{sfc}} \rangle$	$-\frac{1}{9}$	$-\frac{4}{9}$

$$P_{36} = P_{36}^r P_{36}^{\text{sfc}} \quad \text{if it large}$$

$\langle P_{36}^r \rangle: 1$ should also large

$\langle P_{36}^r \rangle$ is determined by the dynamical wave function

For d^* The effective Δ - Δ interaction induced by OGE and vector meson exchange enables the short range interaction attractive.

→ Two clusters $\Delta\Delta$ closer, $\langle P_{36}^r \rangle$ is not small

1). d^* special characters

spin-flavor-color spaces exchange effect: model independent

2). $\Delta\Delta$ ($SI=30$), Δ - Δ short range interaction is attractive

Dynamical effect — Model dependent

P_{36} Effect large, large CC component

d^* might be a 6q dominant state

→ d^* deep bounded and narrow width

Analysis: Large component of CC (67%) in d^* ?

$$\Psi_{6q} = (1 - 9P_{36})[\phi_{\Delta}\phi_{\Delta}\eta_{\Delta\Delta}(\mathbf{r})]_{\text{SIC}=30(00)}$$

$$+ (1 - 9P_{36})[\phi_C\phi_C\eta_{CC}(\mathbf{r})]_{\text{SIC}=30(00)}$$

$\chi_{\Delta\Delta}(r) \equiv \langle \phi_{\Delta}(\xi_1, \xi_2) \phi_{\Delta}(\xi_4, \xi_5) | \Psi_{6q} \rangle$, (1) (2) (4) terms

$\chi_{CC}(r) \equiv \langle \phi_C(\xi_1, \xi_2) \phi_C(\xi_4, \xi_5) | \Psi_{6q} \rangle$, (3) (4) (2) terms

$$\Psi_{d^*} = |\Delta\Delta\rangle \chi_{\Delta\Delta}(r) + |CC\rangle \chi_{CC}(r)$$

χ_{CC} contains the contri. From (2), from $\Delta\Delta$ exchanged terms.

Thus P_{36} Exchange is important!

$P_{36} = P_{36}^r P_{36}^{sfc}$ d^* has $\Delta\Delta$ and CC components

- $\Delta\Delta$ +coupled channels (in quark level)

J.L.Ping, F.Wang et al. PRC **89**, 034001 (2014)

ChQM (10 channels with hidden-color ones)

$IJ^P = 03^+$	1 $\Delta\Delta(^7S_3)$	2 $NN(^3D_3)$	3 $\Delta\Delta(^3D_3)$	4 $\Delta\Delta(^7D_3)$	5 $^2\Delta_8$	6 $^2\Delta_8(^3D_3)$	7 4N_8	8 $^2N_8(^3D_3)$	9 4N_8	10 $^4N_8(^7S_3)$	10 $^4N_8(^7D_3)$

$$BE = 71 \text{ MeV} \quad \Gamma = 150 \text{ MeV}$$

QDCSM (4 coupled channels)

$$\Delta\Delta^7S_3, NN^3D_3, \Delta\Delta^3D_3, \Delta\Delta^7D_3$$

$$BE = 107 \text{ MeV} \quad \Gamma = 110 \text{ MeV}$$

TABLE III. $\Delta\Delta$ or resonance mass M and decay width Γ , in MeV, in two quark models for the $IJ^P = 03^+$ state.

	QDCSM		ChQM		
	sc	4 cc	sc	4 cc	10 cc
M	2365	2357	2425	2413	2393
Γ_{NN}	—	14	—	14	14
Γ_{inel}	103	96	177	161	136
Γ	103	110	177	175	150

On the charge distribution of d*

Form factors: 2S+1 relative to size arXiv:1704.01253

Nucleon(1/
2):

$$\langle N(p') | J_N^\mu | N(p) \rangle = \bar{U}_N(p') \left[F_1(Q^2) \gamma^\mu + i \frac{\sigma^{\mu\nu} q_\nu}{2M_N} F_2(Q^2) \right] U(p),$$

$$G_E(Q^2) = F_1(Q^2) - \eta F_2(Q^2), \quad G_M(Q^2) = F_1(Q^2) + F_2(Q^2),$$

Breit frame

$$\langle N(\vec{q}/2) | J_N^0 | N(-\vec{q}/2) \rangle = (1 + \eta)^{-1/2} \chi_{s'}^+ \chi_s G_E(Q^2)$$

$$\langle N(\vec{q}/2) | \vec{J}_N | N(-\vec{q}/2) \rangle = (1 + \eta)^{-1/2} \chi_{s'}^+ \frac{\vec{\sigma} \times \vec{q}}{2M_N} \chi_s G_M(Q^2).$$

Deuteron(1):

$$J_{jk}^\mu(p', p) = \epsilon_j'^{*}\epsilon_k^\alpha(p') S_{\alpha\beta}^\mu \epsilon_k^\beta(p)$$

$$S_{\alpha\beta}^\mu = - \left[G_1(Q^2) g_{\alpha\beta} - G_3(Q^2) \frac{Q_\alpha Q_\beta}{2m_D^2} \right] P^\mu - G_2(Q^2) (Q_\alpha g_\beta^\mu - Q_\beta g_\alpha^\mu),$$

$$G_C(Q^2) = G_1(Q^2) + \frac{2}{3} \eta_D G_2(Q^2), \quad G_M(Q^2) = G_2(Q^2),$$

$$G_Q(Q^2) = G_1(Q^2) - G_2(Q^2) + (1 + \eta_D) G_3(Q^2),$$

Breit frame

$$G_C(Q^2) \longrightarrow \frac{1}{3} \sum_\lambda \langle p', \lambda | J^0 | p, \tilde{\lambda} \rangle.$$

d[★](3):

$$\mathcal{J}^\mu = (\epsilon^*)^{\alpha' \beta' \gamma'}(p') \mathcal{M}_{\alpha' \beta' \gamma', \alpha \beta \gamma}^\mu \epsilon^{\alpha \beta \gamma}(p)$$

$$\begin{aligned}
\mathcal{M}_{\alpha' \beta' \gamma', \alpha \beta \gamma}^\mu &= \left[G_1(Q^2) \mathcal{P}^\mu \left[g_{\alpha' \alpha} \left(g_{\beta' \beta} g_{\gamma' \gamma} + g_{\beta' \gamma} g_{\gamma' \beta} \right) + \text{permutations} \right] \right. \\
&\quad + G_2(Q^2) \mathcal{P}^\mu \left[q_{\alpha'} q_\alpha \left[g_{\beta' \beta} g_{\gamma' \gamma} + g_{\beta' \gamma} g_{\gamma' \beta} \right] + \text{permutations} \right] / (2M^2) \\
&\quad + G_3(Q^2) \mathcal{P}^\mu \left[q_{\alpha'} q_\alpha q_{\beta'} q_\beta g_{\gamma' \gamma} + \text{permutations} \right] / (4M^4) \\
&\quad + G_4(Q^2) \mathcal{P}^\mu q_{\alpha'} q_\alpha q_{\beta'} q_\beta q_{\gamma'} q_\gamma / (8M^6) \\
&\quad + G_5(Q^2) \left[\left(g_{\alpha'}^\mu q_\alpha - g_\alpha^\mu q_{\alpha'} \right) \left(g_{\beta' \beta} g_{\gamma' \gamma} + g_{\beta' \gamma} g_{\beta' \gamma} \right) + \text{permutations} \right] \\
&\quad + G_6(Q^2) \left[\left(g_{\alpha'}^\mu q_\alpha - g_\alpha^\mu q_{\alpha'} \right) \left(q_{\beta'} q_\beta g_{\gamma' \gamma} + q_{\gamma'} q_\gamma g_{\beta' \beta} + q_{\beta'} q_\gamma g_{\gamma' \beta} + q_{\gamma'} q_\beta g_{\gamma' \beta} \right) \right. \\
&\quad \quad \left. + \text{permutations} \right] / (2M^2) \\
&\quad + G_7(Q^2) \left[\left(g_{\alpha'}^\mu q_\alpha - g_\alpha^\mu q_{\alpha'} \right) q_{\beta'} q_\beta q_{\gamma'} q_\gamma + \text{permutations} \right] / (4M^4)
\end{aligned}$$

$$q_\mu \mathcal{M}_{\alpha' \beta' \gamma', \alpha \beta \gamma}^\mu = 0$$

$$G_E^{d^*}(Q^2) = \frac{1}{7} \sum_{m_{d^*}=-3}^3 \langle p', m_{d^*} | J^0 | p, m_{d^*} \rangle$$

$$J^0 = \sum_{i=1}^6 e_i \bar{q}_i \gamma^0 q_i = \sum_{i=1}^6 j_i^0.$$

Cases	$d^*(2380)$		D_{12}
	A1	A2	
$rms \ (fm)$	1.09	0.78	2.39

