

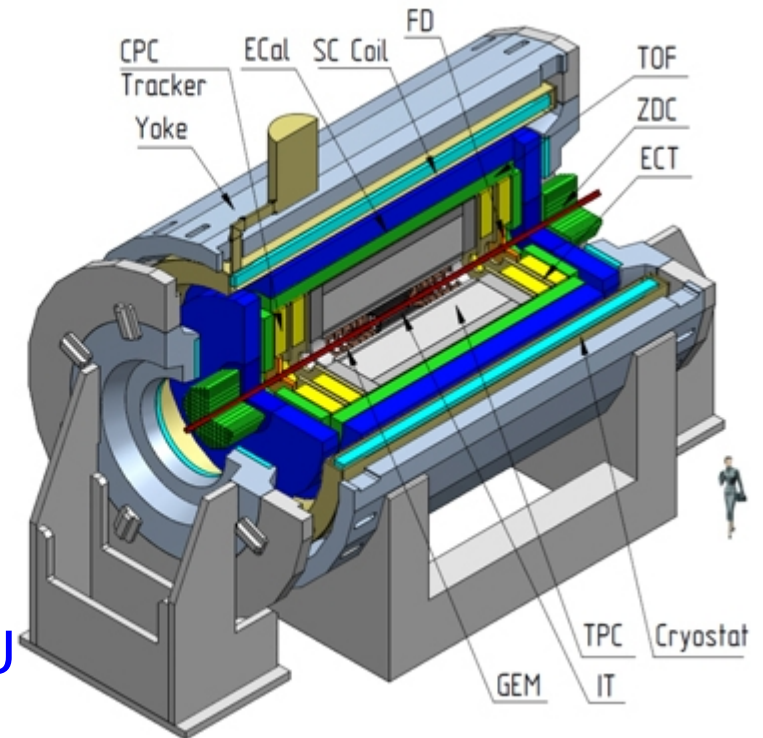


# Study of strongly interacting matter properties at the energies of the NICA collider using the methods of femtoscopy and factorial moments

within the RFBR Mega Grant # 18-02-40044

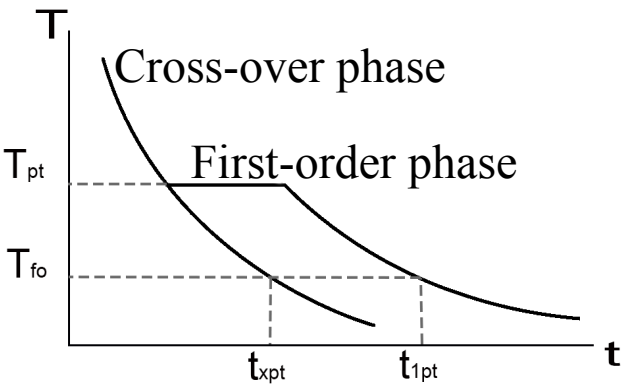
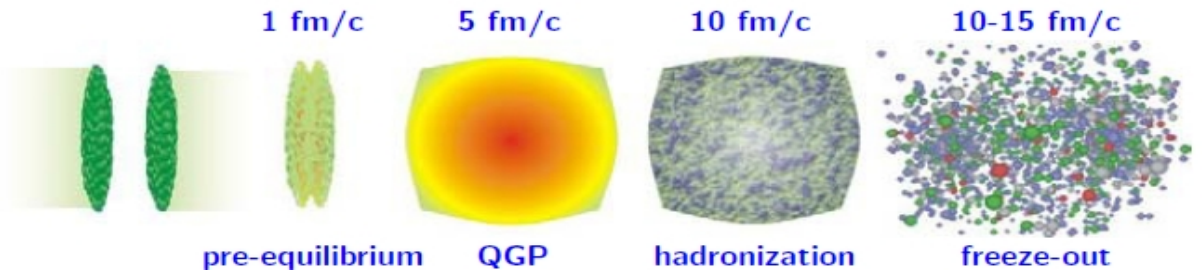
## People:

- Ludmila Malinina (SINP MSU, JINR),
- Konstantin Mikhaylov (ITEP & JINR), convener
- Grigory Nigmatkulov (NRNU MEPhI),
- Olga Kodolova (SINP MSU),
- Igor Lokhtin (SINP MSU),
- Gleb Romanenko (student, MSU),
- Marya Cheremnova (student, MSU)
- Yevheniia Khyzniak (PhD student, NRNU MEPhI)
- Chernishov Alexey (student MSU)
- Egor Alpatov (student NRNU MEPhI)



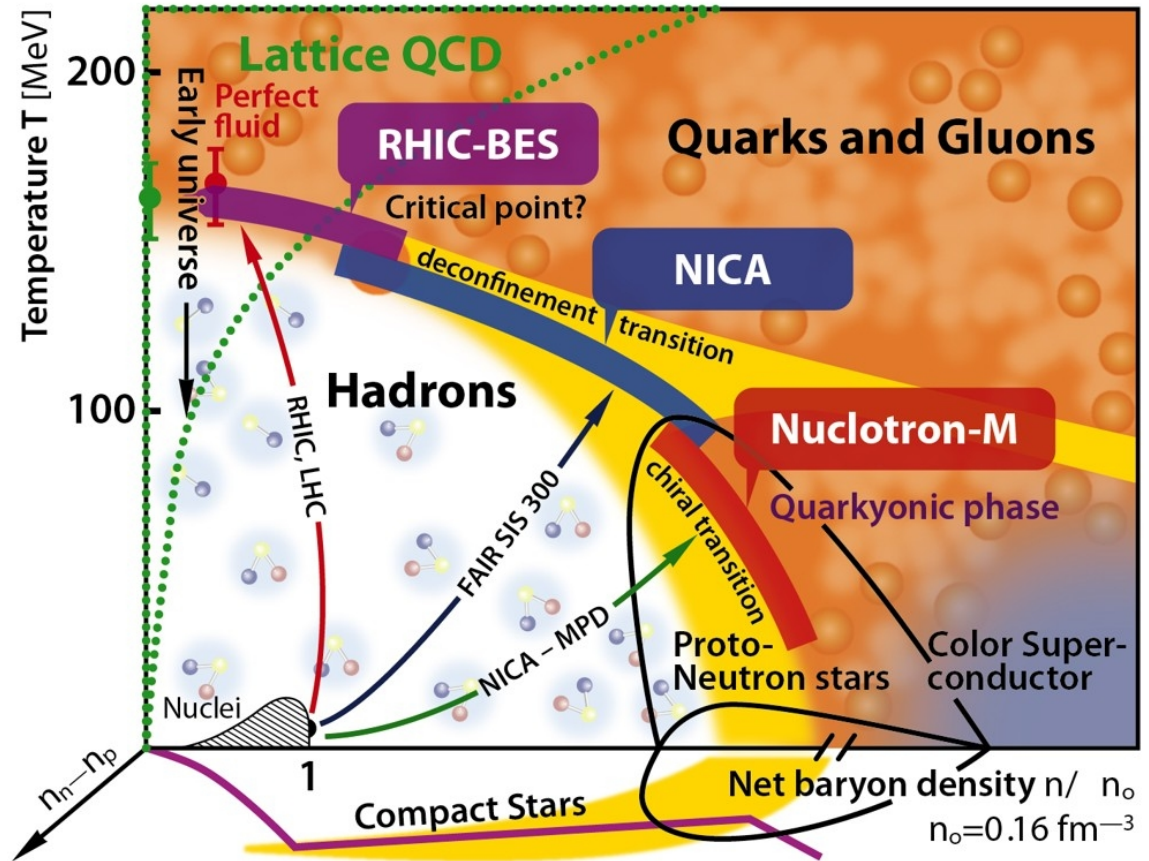
# Motivation: Phase diagram QCD

- Crossover transition to QGP occurs at RHIC & LHC
- 1st order phase transition to QGP occurs at lower energies (?)



• Beam Energy Scan (BES) program: search for location of transition point from Crossover (XPT) to 1<sup>st</sup> order (1PT) phase transitions

- BES RHIC ( $\sqrt{s}=3-60$  GeV)
- NA61@SPS ( $E_{lab}=10-158$  GeV);
- projects: CBM@FAIR (GSI) и MPD@NICA (JINR)



# Hybrid (hydro+hadron gas) vHLLE+UrQMD model

Pre-thermal phase

UrQMD

hydrodynamic phase

vHLLE

(3+1)-D viscous hydrodynamics

hadronic cascade

UrQMD

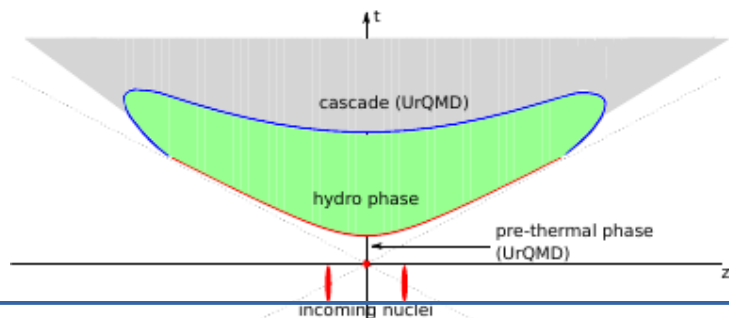
Iu. Karpenko, P. Huovinen, H. Petersen, M. Bleicher, Phys. Rev. C 91, 064901 (2015), arXiv:1502.01978, 1509.3751, talk QM2015

vHLLE code: free and open source, <https://github.com/yukarpenko/vhllle>, Comput. Phys. Commun. 185 (2014), 3016

The transition to hydrodynamical description occurs at a hyper-surface of constant longitudinal proper time  $\tau_0$ . The minimal value of the starting time  $\tau_0$  is taken to be equal to the average time for the two colliding nuclei to completely pass through each other:

$$\tau_0 = 2R / \sqrt{(\sqrt{s_{NN}}/2m_N)^2 - 1},$$

At  $\tau = \tau_0$  energy, momentum and baryon/electric charges of hadrons are distributed to fluid cells  $ijk$  around each hadron's position according to Gaussian

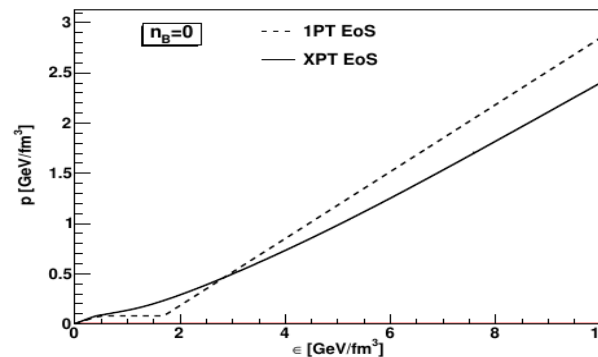


## VHLLE (3+1)-D viscous hydrodynamics

HadronGas + Bag Model  $\rightarrow$  1<sup>st</sup> order PT (1PT) P.F. Kolb, et al, PR C 62, 054909 (2000)

Chiral EoS  $\rightarrow$  crossover PT (XPT) J. Steinheimer, et al, J. Phys. G 38, 035001 (2011)

Thermodynamic pressure as a function of energy density, evaluated at zero baryon density from the equations of state used in the hydrodynamic stage XPT & 1PT



Fluid to particle transition, or particlization, is set to happen at a hypersurface of constant (hydrodynamic) energy density  $\epsilon_w = 0.5 \text{ GeV/fm}^3$ ,

The particlization hypersurface is reconstructed with the CORNELIUS subroutine.

At this hypersurface, individual hadrons are sampled using the Cooper-Frye formula including shear viscous corrections to the distribution functions. The hadronic rescatterings and decays are treated with the UrQMD cascade.

# Femtoscropy with vHLLE

Iu. Karpenko, P. Huovinen, H. Petersen, M. Bleicher, Phys.Rev. C.91, 2015, 064901

Pre-thermal phase

UrQMD

The transition to hydrodynamics occurs at a hyper-surface of constant longitudinal proper time  $\tau_0$ . Minimal value of the starting time  $\tau_0$  is taken to be equal to the average time for the two colliding nuclei to completely pass through each other:

Parameters  $\tau_0$ ,  $R_\perp$ ,  $R_\eta$  and  $\eta/s$  adjusted using basic observables in the RHIC BES-I region.

Model tuned by matching with existing experimental data from SPS and BES-I RHIC

Hydrodynamic phase

vHLLE

(3+1)-D viscous hydrodynamics

## EoS to be used in the model

- Chiral EoS — crossover transition  
J. Steinheimer et al., J. Phys. G 38, 035001 (2011)
- Hadron Gas + Bag Model 1st-order phase transition  
P. F. Kolb et al., Phys.Rev. C 62, 054909 (2000)

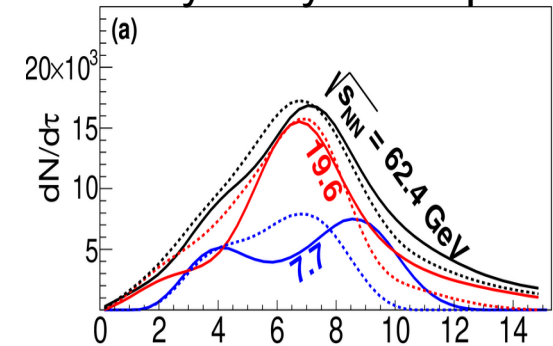
Hydrodynamic phase lasts longer with 1PT, especially at lower energies but cascade smears this difference.

Hadronic cascade

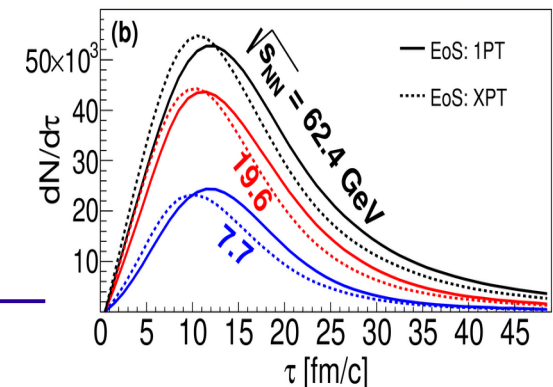
UrQMD

Fluid to particle transition at energy density = 0.5 GeV/fm<sup>3</sup>

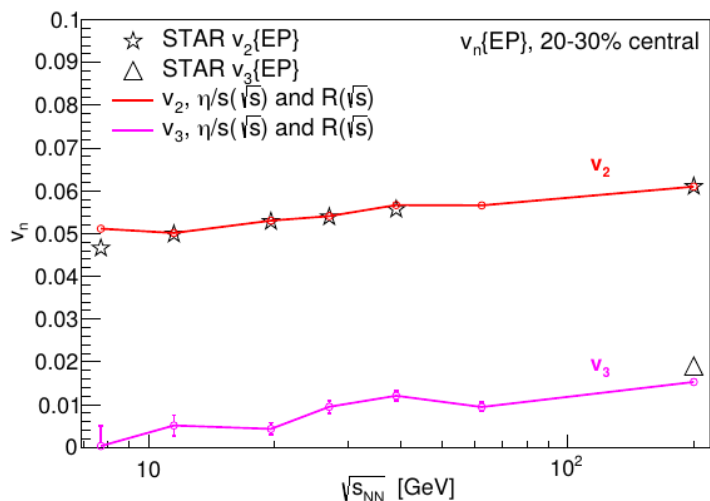
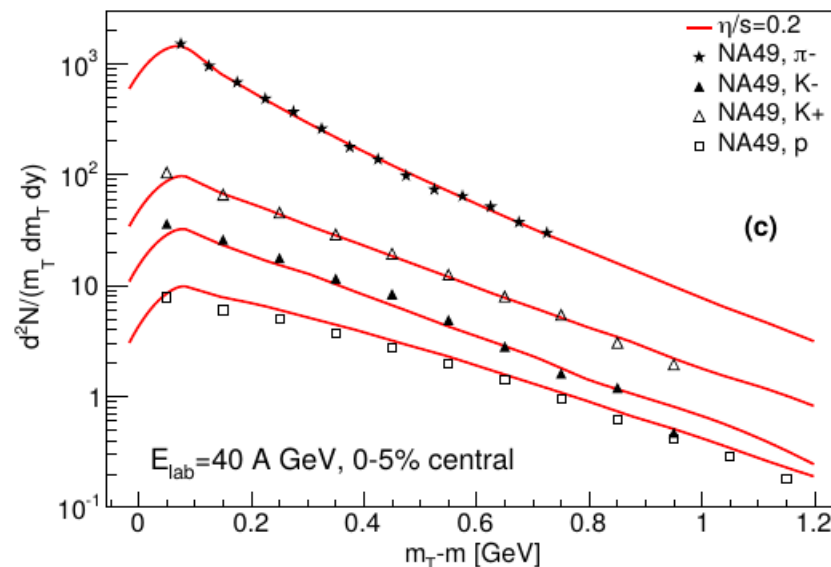
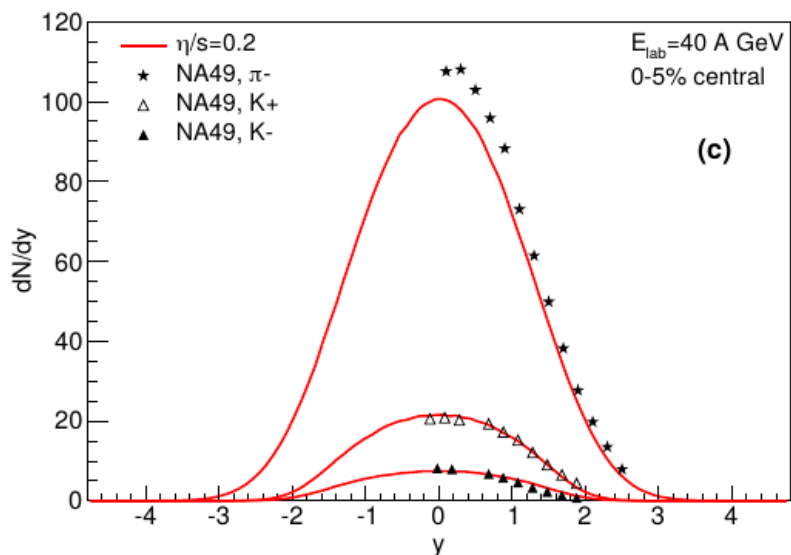
Pion emission time  
after hydrodynamic phase



after cascade



# Examples of vHLEE+UrQMD with XPT calculations for bulk observables



Adjustment to experimental data suggests  
 $\eta/s = 0.2 \rightarrow 0.08$  when  
 $\sqrt{s} = 7.7 \rightarrow 200 \text{ GeV}$ , modulo initial state  
 (UrQMD) and EoS (Chiral model) used.

Iu. Karpenko, P. Huovinen, H. Petersen, M. Bleicher, Phys.Rev. C 91, 064901 (2015), arXiv:1502.01978,1509.3751, talk QM2015

# Femtoscscopy

## Correlation femtoscscopy :

Measurement of space-time characteristics  $\mathbf{R}$ ,  $\mathbf{c\tau}$  of particle production using particle correlations due to the effects of quantum statistics ( QS ) and final state interactions ( FSI )

## Two-particle correlation function:

theory:

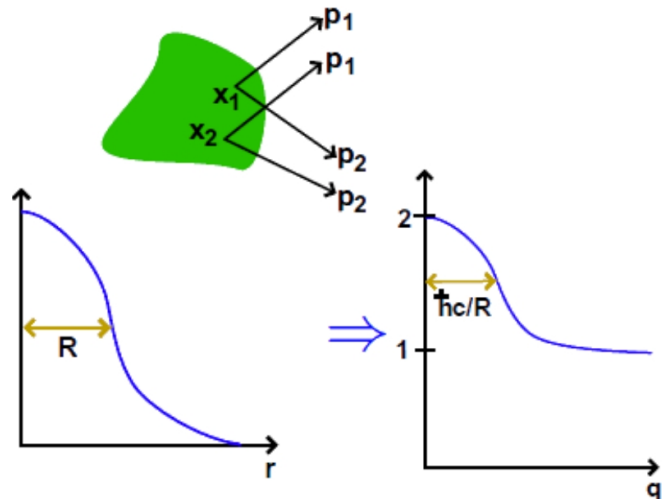
$$C(q) = \frac{N_2(p_1, p_2)}{N_1(p_1) \cdot N_2(p_1)}, C(\infty) = 1$$

experiment:

$$C(q) = \frac{S(q)}{B(q)}, q = p_1 - p_2$$

$S(q)$  – distribution of pair momentum difference from same event

$B(q)$  – reference distribution built by mixing different events



## Parametrizations used:

1D CF:  $C(q_{inv}) = 1 + \lambda e^{-R^2 q_{inv}^2}$

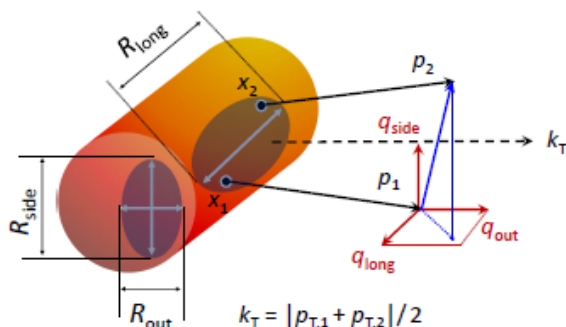
$R$  – Gaussian radius in PRF,

$\lambda$  – correlation strength parameter

3D CF:  $C(q_{out}, q_{side}, q_{long}) = 1 + \lambda e^{-R_{out}^2 q_{out}^2 - R_{side}^2 q_{side}^2 - R_{long}^2 q_{long}^2}$

$R$  and  $q$  are in Longitudinally Co-Moving Frame (LCMS)

long || beam; out || transverse pair velocity  $\mathbf{v}_T$ ; side normal to out, long



## 3D analysis:

$R_{side}$  sensitive to geometrical transverse size.

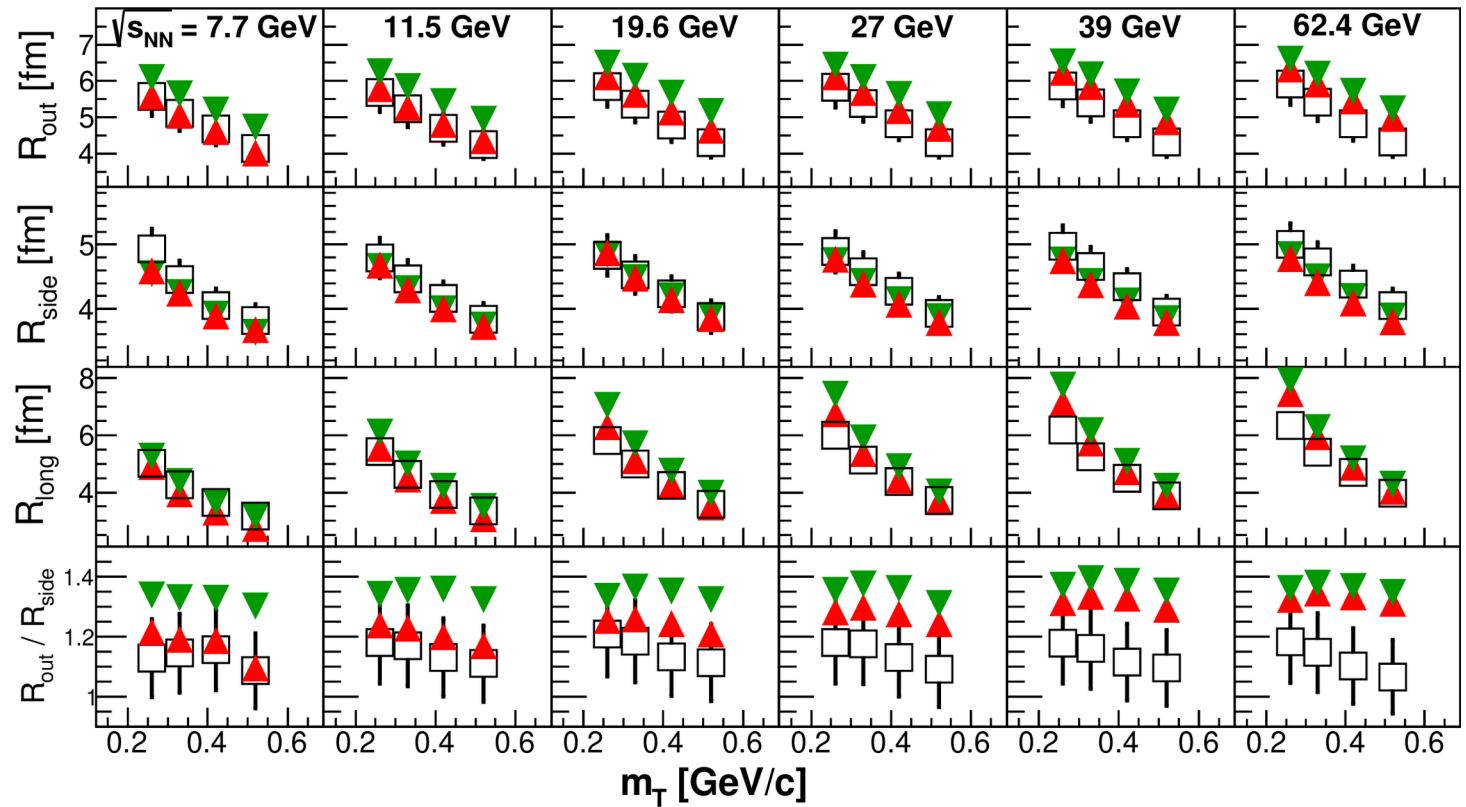
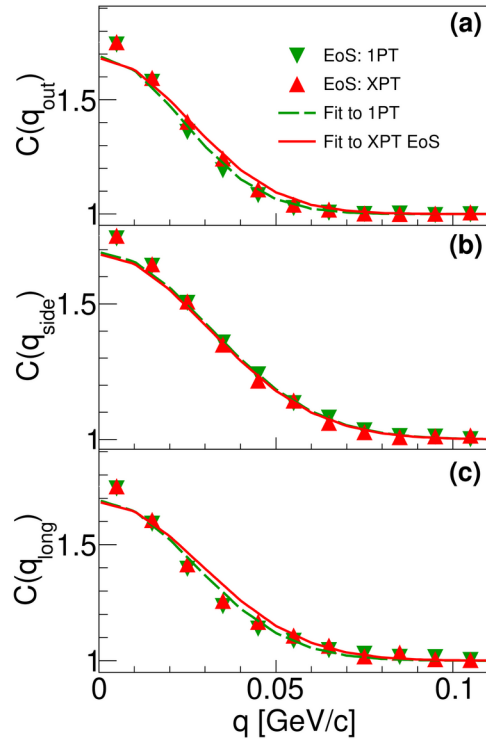
$R_{long}$  sensitive to time of freeze-out.

$R_{out} / R_{side}$  sensitive to emission duration.

# 3D Pion radii with vHLE model

Phys.Rev. C96 (2017) no.2, 024911

## Projections of 3D Model CF



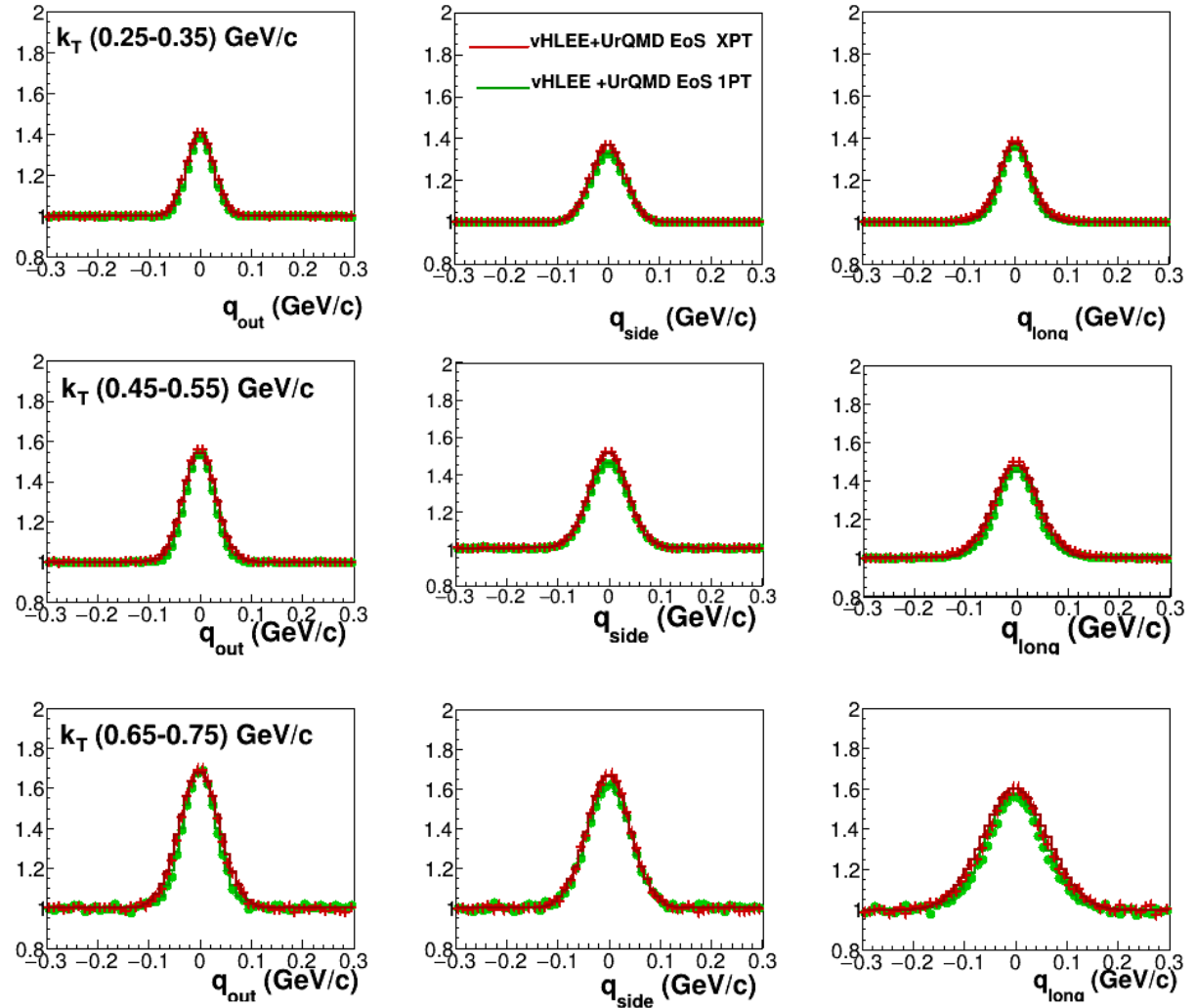
- Femtoscopic radii are sensitive to the type of the phase transition
- **Crossover EoS** describes better  $R(m_T)$  dependencies
- $R_{out, long}$  (1PT) >  $R_{out, long}$  (XPT) by value of  $\sim 1-2$  fm.
- $R_{out}/R_{side}$  (XPT) agrees with STAR data points at 7.7 and 11.5 GeV, but then increases with increasing collision energy while ratio in data is independent with collision energy;  $R_{out}/R_{side}$  for 1PT systematically overestimate data and is independent on collision energy.

# 3D Pion Correlation Functions with vHLE model

1PT -green dots; XPT – red dots

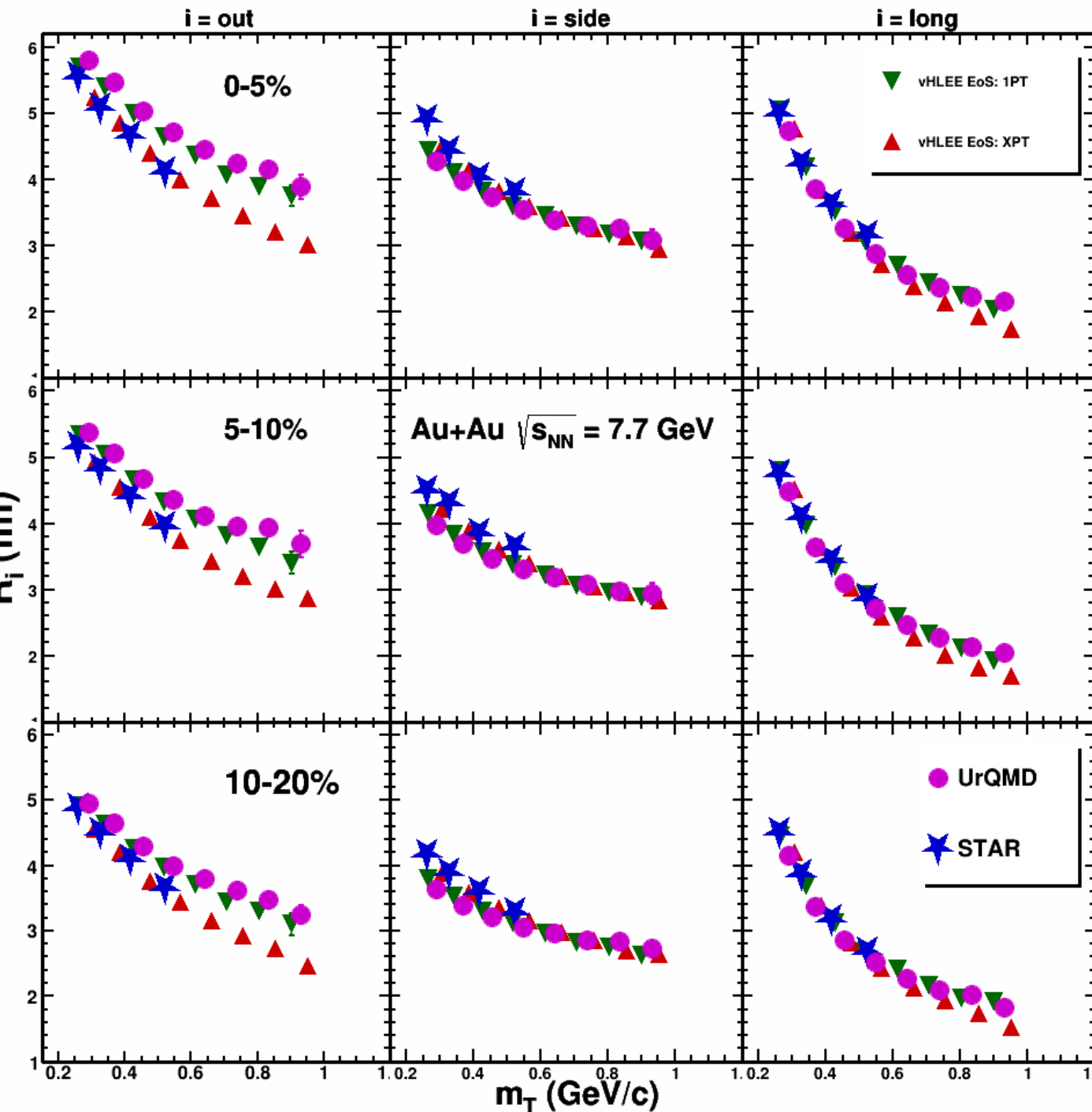
## Analysis

- MDP femto package (see Grigory Nigmatkulov's talk)
- We performed analysis of pion and kaon correlations for vHLE and UrQMD for different centrality ranges
- Au+Au,  $\sqrt{s_{NN}} = 11.5$  GeV central events vHLE
- Standard 3D Gaussian fit used
- Projections of 3D pion correlation functions on out-side-long
- XPT CF projections on long direction are wider than 1PT ones
- CF become wider with increasing  $k_T$



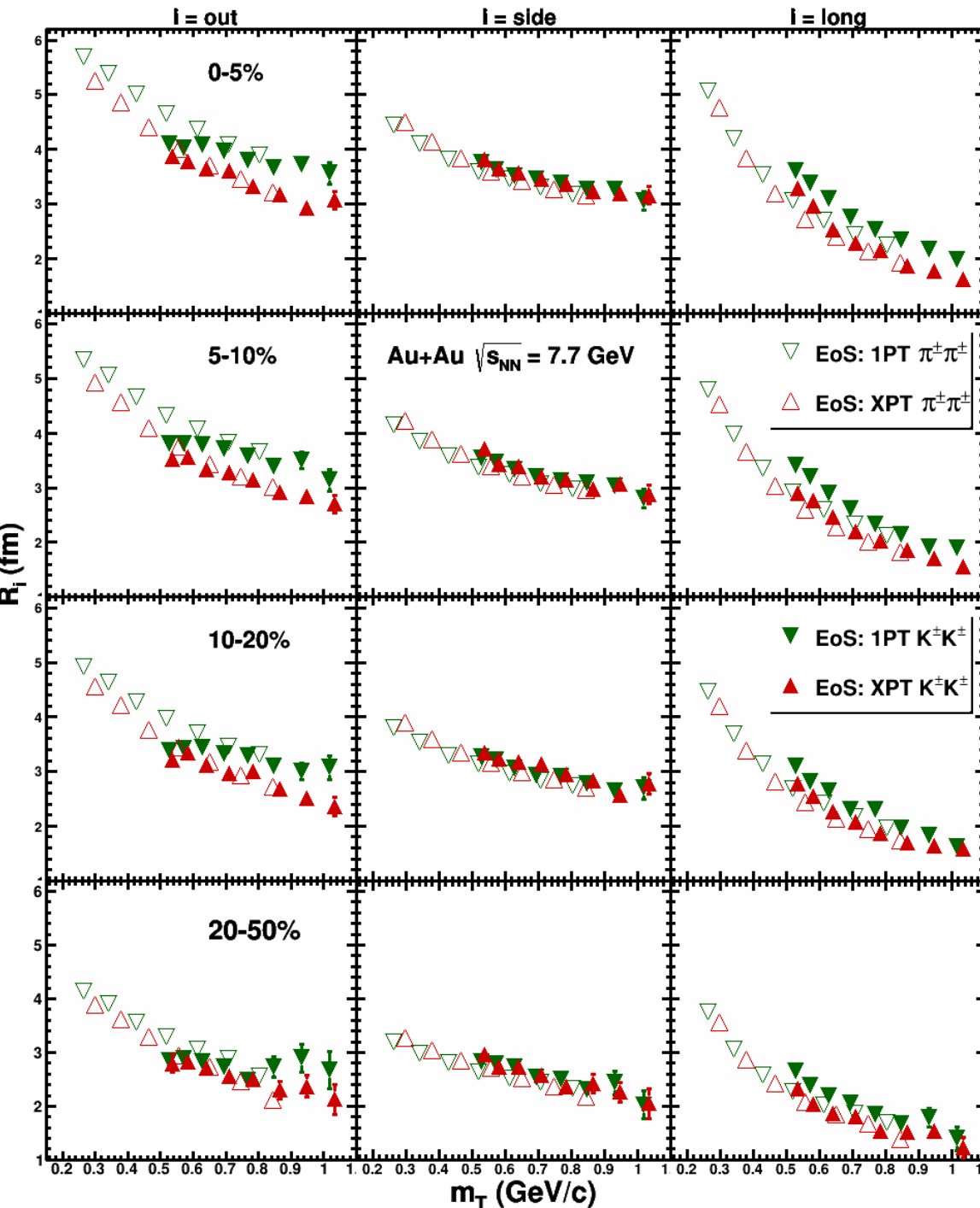


# Pion radii with vHLEE and UrQMD models



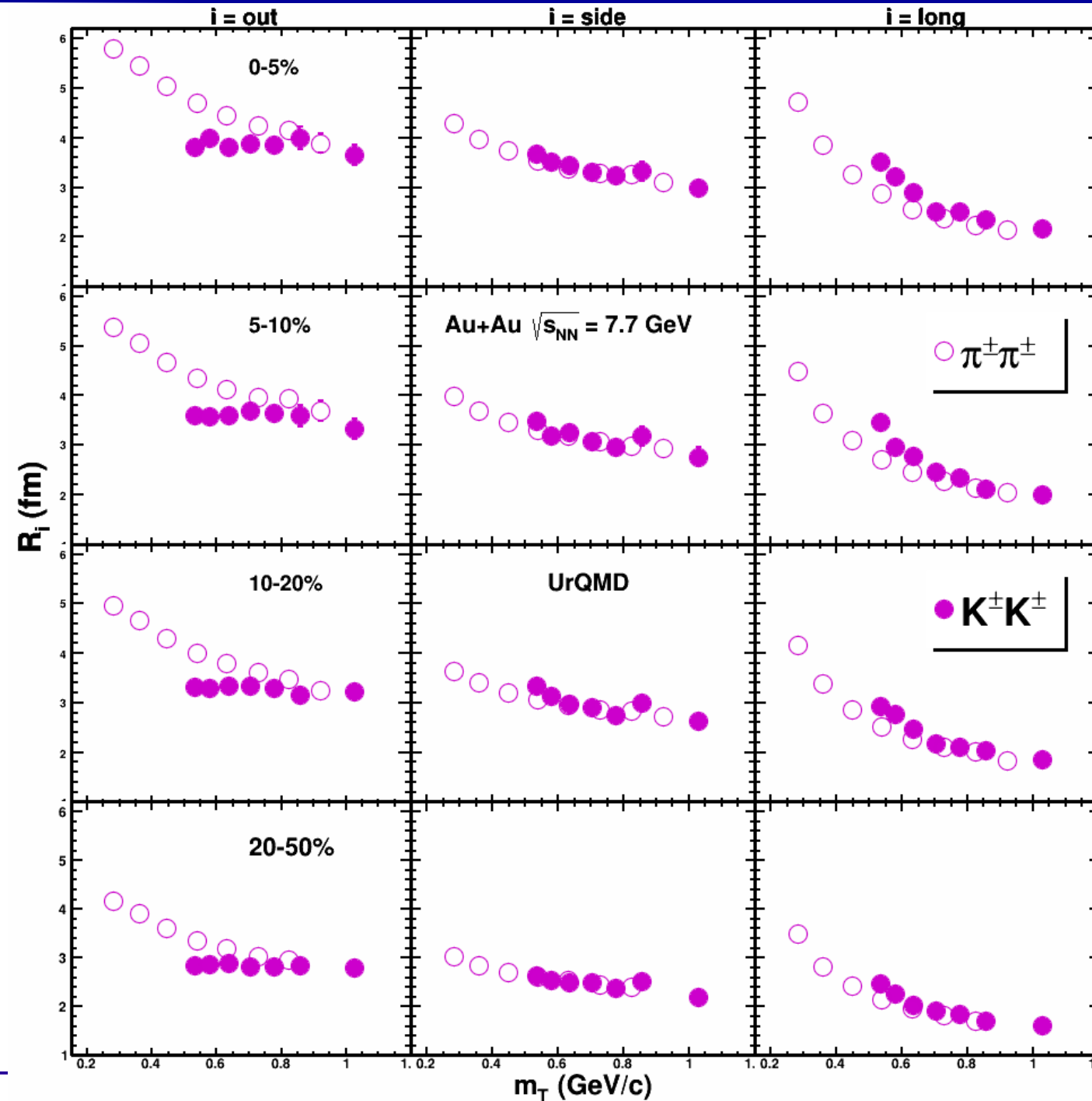
- Au+Au,  $\sqrt{s_{NN}} = 7.7$  GeV
- It is important to study  $k_T$  ( $m_T$ ) dependence in larger interval than STAR
- Radii decrease with  $m_T \rightarrow$  radial flow
- Increase size with increasing centrality  $\rightarrow$  simple geometric picture of the collisions.
- Crossover EoS describes better  $R_{\text{out}}(m_T)$
- $R_{\text{out,long}}(1\text{PT}) > R_{\text{out,long}}(\text{XPT})$
- UrQMD is closed to 1PT
- The similar trends is observed for AuAu 11.5 GeV

# Pion and kaon radii with vHLE model



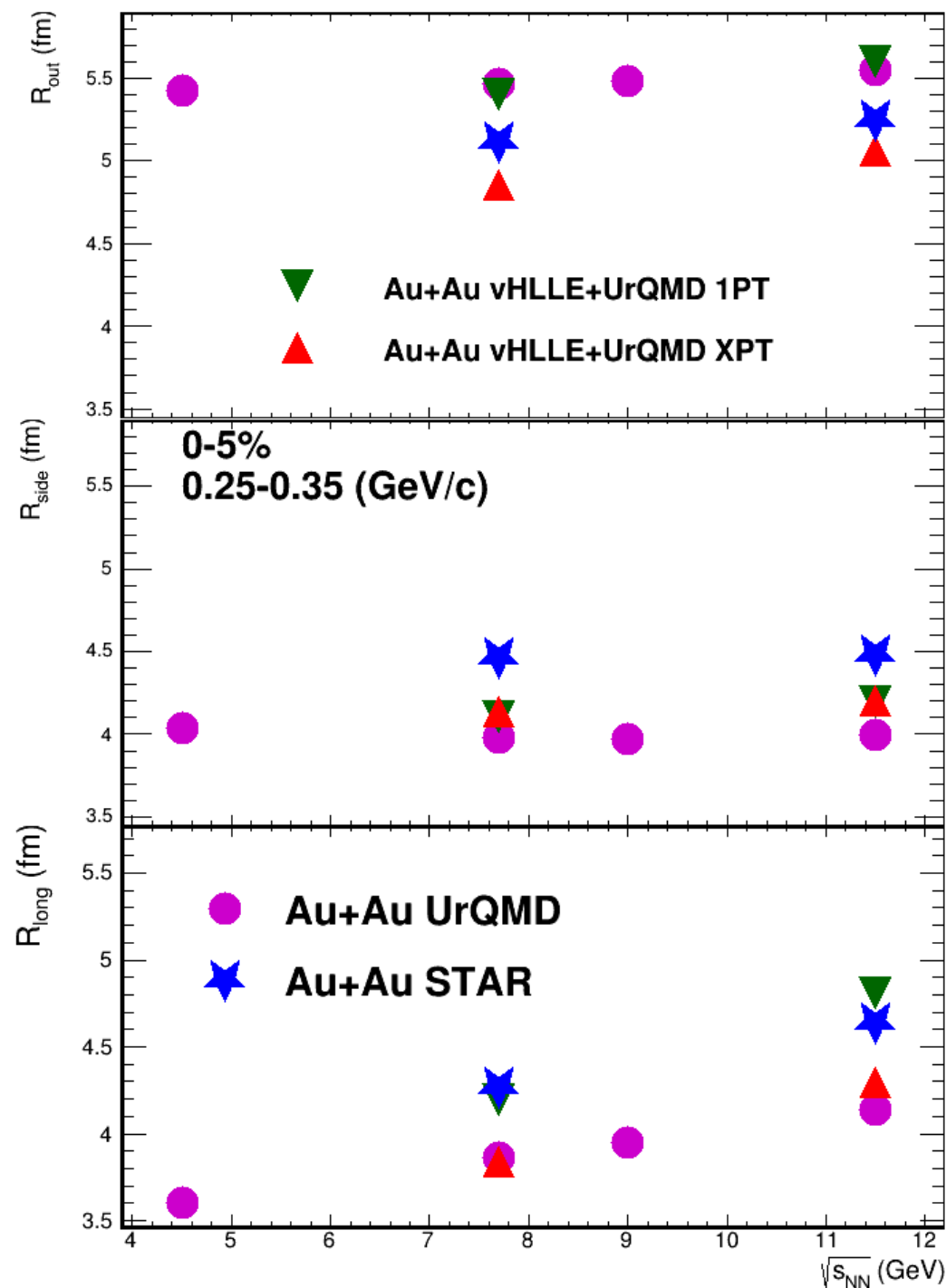
- Au+Au,  $\sqrt{s_{NN}} = 7.7$  GeV
- Approximate  $m_T$  scaling for  $R_{\text{side}}$
- Similarly to pions : kaon radii decrease with  $m_T \rightarrow$  radial flow ;
- for 1PT EoS almost flat dependence  $R_{\text{out}}(m_T)$  is observed  $\rightarrow$  weaker flow
- $R_{\text{out, long}}(1PT) > R_{\text{out, long}}(XPT)$
- $R_{\text{long}}$  kaon radii for XPT  $>$   $R_{\text{long}}$  pion similarly to experiment (LHC & RHIC)
- Very different predictions of vHLE model for different EoS  $\rightarrow$  importance to study heavier than pions particles  $\rightarrow$  kaons
- The similar trend is observed for AuAu 11.5 GeV

# Pion and kaon radii with UrQMD model



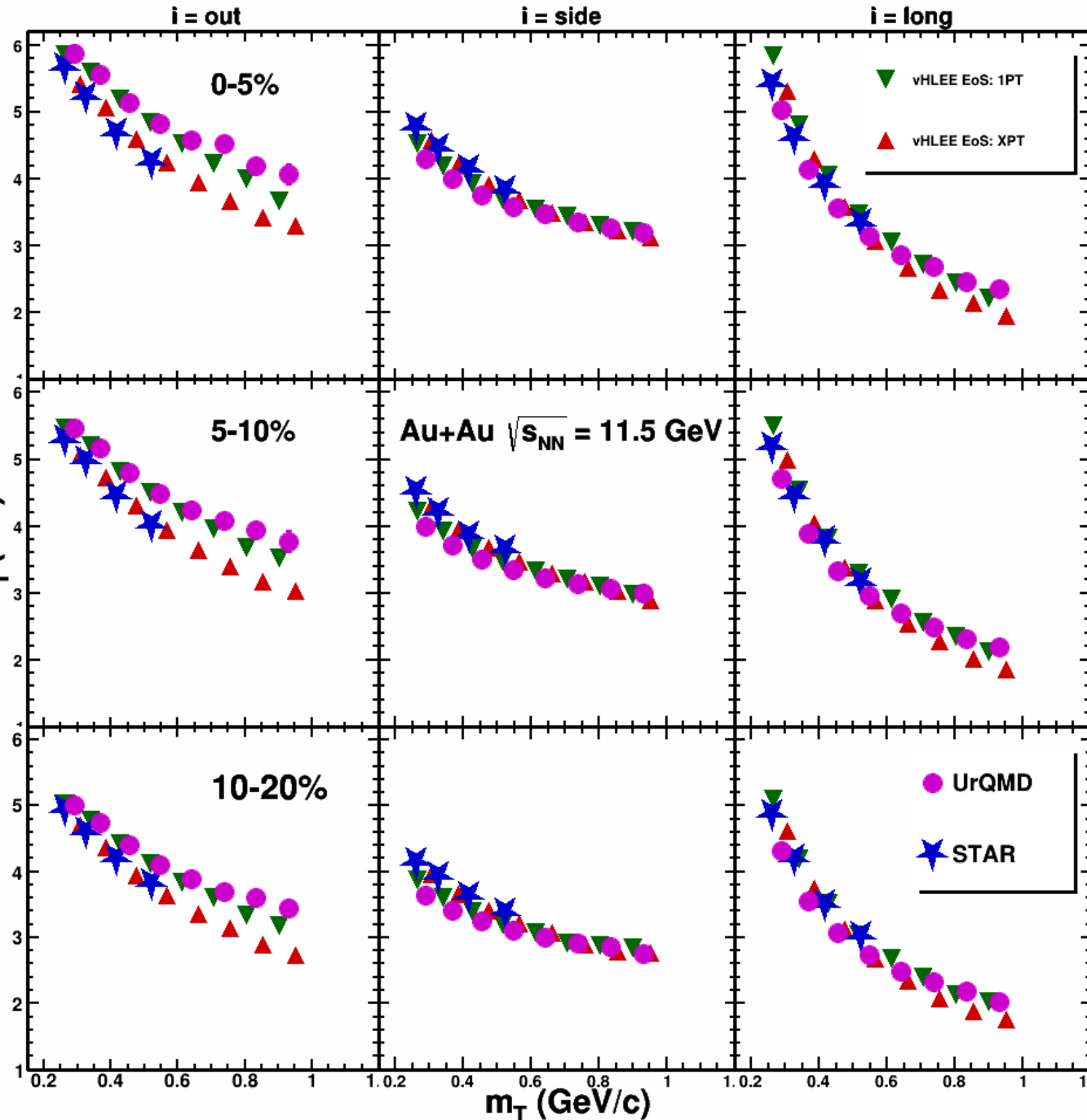
- Au+Au,  $\sqrt{s_{NN}} = 7.7$  GeV
- kaon radii demonstrate almost flat behavior similarly to vHLEE with the 1PT EoS  $\rightarrow$  weak flow
- $R_{\text{long}}$  kaon radii are larger than pion ones similarly to experiment (LHC & RHIC)
- The similar trend is observed for AuAu 11.5 GeV

# Energy dependence of pion radii



- NICA energy range:  
 $\sqrt{s_{NN}} = 4 - 11$  GeV
- We performed femtoscopic analysis of pions in this energy range using vHLEE and UrQMD models
- There is a lack of systematical high accuracy and high statistics studies of QGP phase transition for this region in the world !

# Pion radii with vHLEE and UrQMD models



- Au+Au,  $\sqrt{s_{NN}} = 11.5$  GeV
- It is important to study  $k_T$  ( $m_T$ ) dependence in larger interval than STAR
- Radii decrease with  $m_T \rightarrow$  radial flow
- Increase size with increasing centrality  $\rightarrow$  simple geometric picture of the collisions.
- Crossover EoS describes better  $R_{\text{out}}(m_T)$
- $R_{\text{out,long}}(1\text{PT}) > R_{\text{out,long}}(\text{XPT})$
- URQMD is closed to 1PT
- The similar trends is observed for AuAu 11.5 GeV

# Introduction: Factorial Moments (intermittency)

## Factorial Moments (see Olga Kodolova's talk)

It was proposed by A. Bialas and R. Peschanski (Nucl. Phys. B 273 (1986) 703) to study the dependence of the normalized factorial moments

$$F_i = M^{i-1} \times \left\langle \frac{\sum_{j=1}^M k_j \times (k_j - 1) \times \dots \times (k_j - i + 1)}{N \times (N - 1) \times \dots \times (N - i + 1)} \right\rangle$$

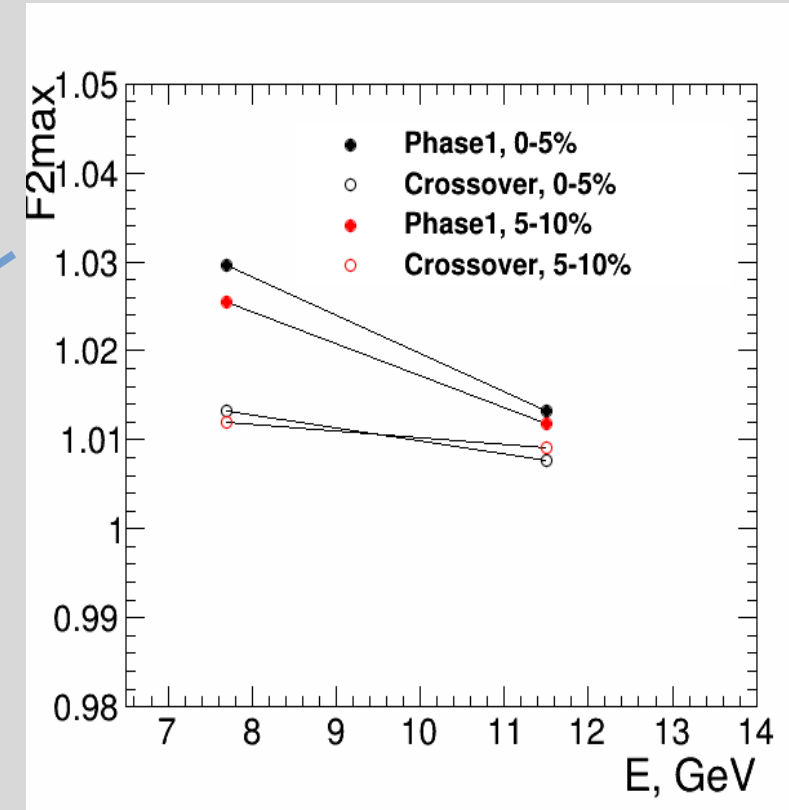
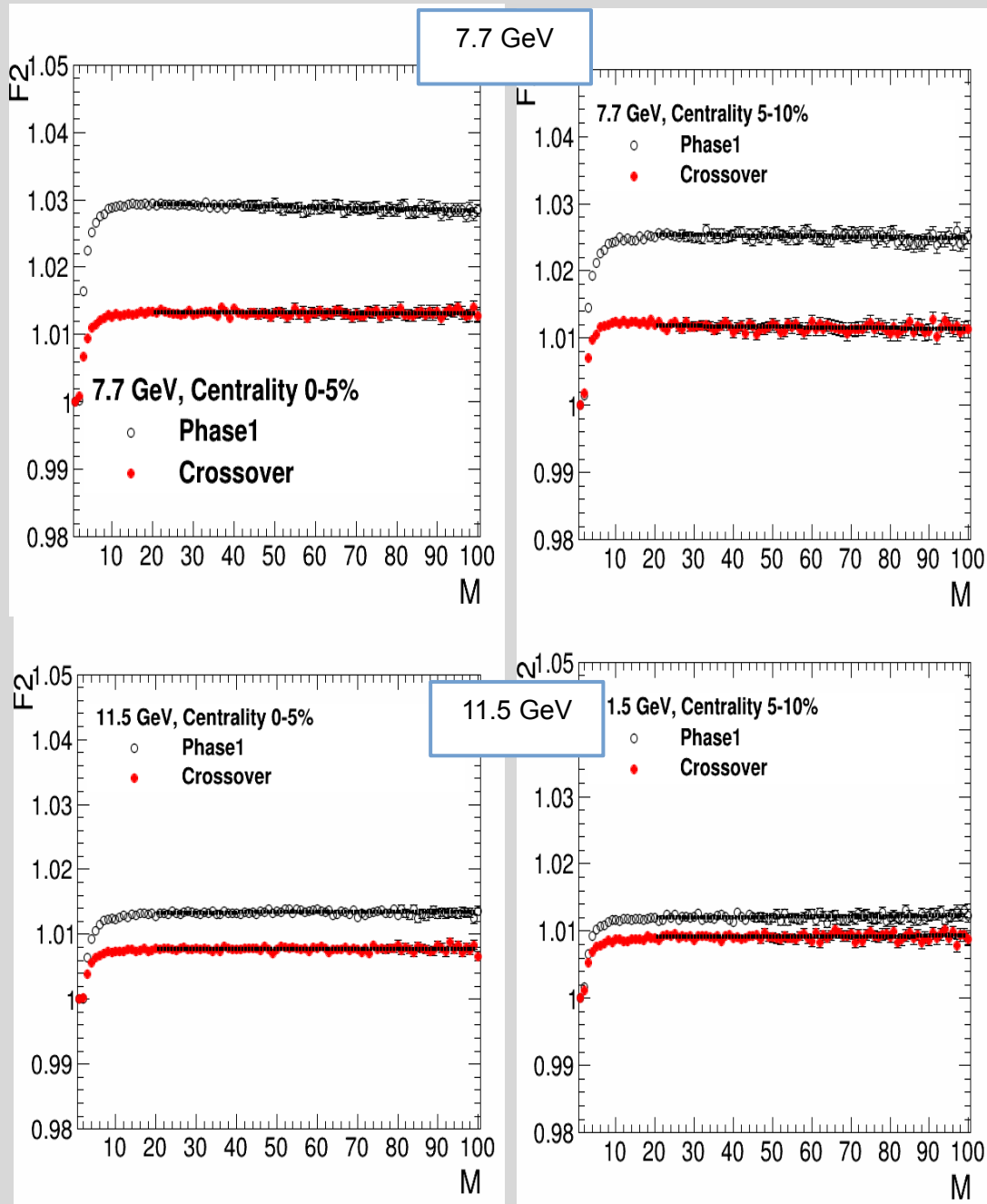
Note: there is a set of definitions of moments and cumulants.

of the rapidity distribution on the size  $\delta y$  ( $\Delta y/M$ ,  $M$  is the number of bins,  $\Delta y$  is the size of the mid rapidity window):

1. if fluctuations are purely statistical no variation of moments as a function of  $\delta y$  is expected
2. Observation of variations indicates the presence of physics origin fluctuations

Intermittency (fluctuations of various different sizes in 1D, 2D and 3D phase space) have been studied at LEP, Tevatron, Protvino in ee, hh, hA, AA interactions at the various energies.

# Au-Au, UrQMD+vHLLLE



- ◆ Different energy dependence is expected for Crossover and 1<sup>st</sup> order phase transition
- ◆ There is a mild dependence on centrality for 1<sup>st</sup> order phase transition