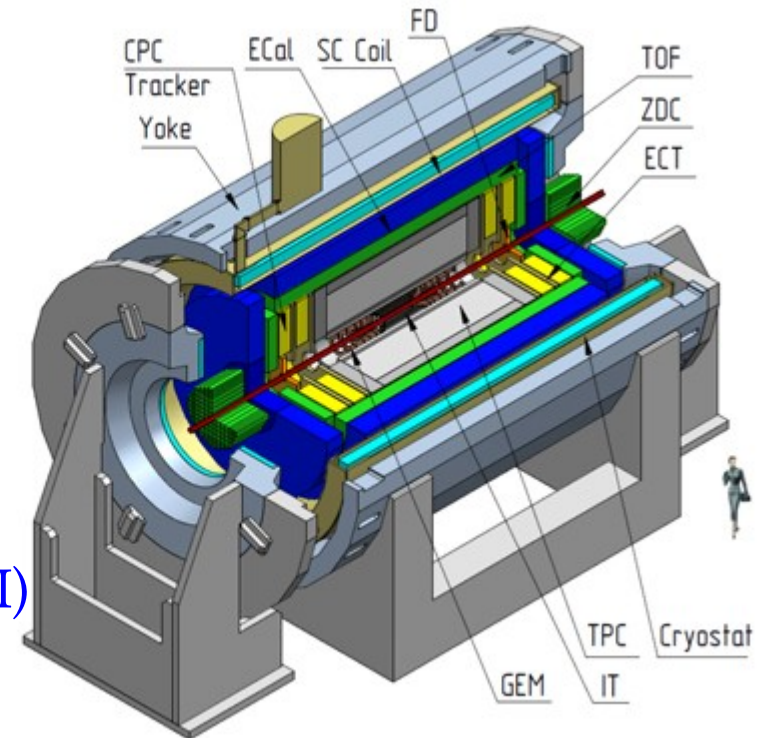




# Influence of methodological effects on femtoscopy in MPD within the RFBR Mega Grant # 18-02-40044

## People:

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- Konstantin Mikhaylov (ITEP & JINR), convener
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- Olga Kodolova (SINP MSU),
- Igor Lokhtin (SINP MSU),
- Gleb Romanenko (PhD student, MSU),
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- Yevheniia Khyzniak (PhD student, NRNU MEPhI)
- Alexei Chernishov (student, MSU)
- Egor Alpatov (PhD student, NRNU MEPhI)



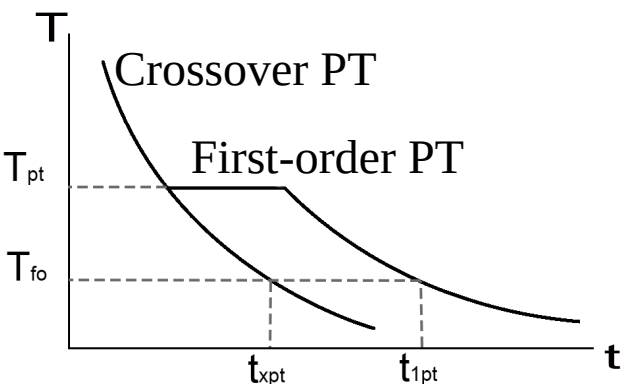
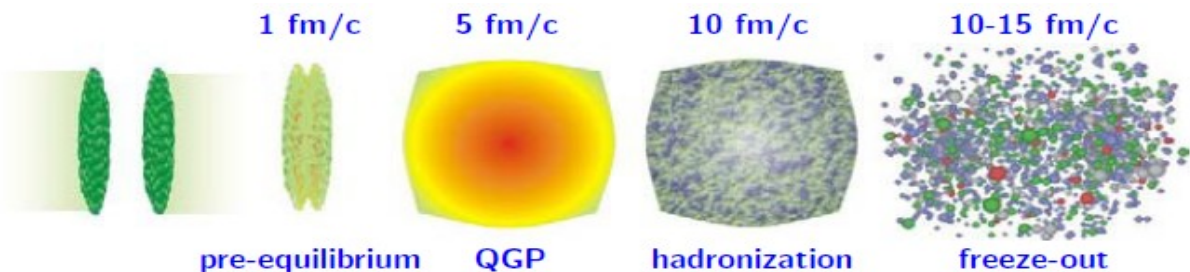
# Outline

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- Femtoscopy & Motivation
- Analysis details
- Influence of single- and two-track resolution on Correlation Functions (Cfs)
- PID study
- Momentum resolution studies
- Two-tracks effects studies

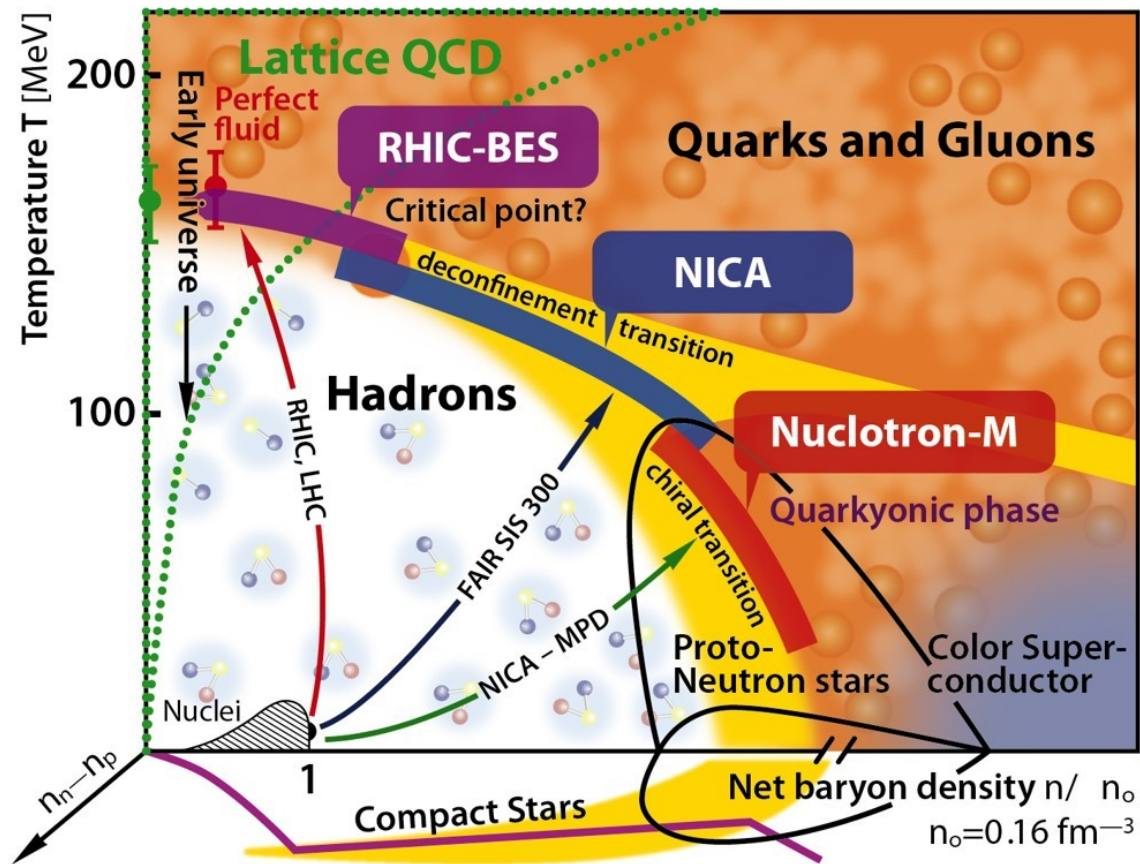
# Motivation: Phase diagram QCD

- Crossover phase transition (XPT) to QGP occurs at RHIC & LHC energies
- The 1<sup>st</sup>-order phase transition (1PT) to QGP occurs at lower energies (?)



**It is important to extract space-time information -> femtoscopy**

- BES RHIC ( $\sqrt{s_{NN}} = 3-39 \text{ GeV}$ )
- BES-II + FXT ( $\sqrt{s_{NN}} = 3-27 \text{ GeV}$ )
- NA61@SPS ( $E_{lab} = 10-158 \text{ AGeV}$ );
- projects: CBM@FAIR (GSI), MPD and BM@N @ NICA (JINR)



# Femtoscscopy

## Correlation femtoscopy :

Measurement of space-time characteristics  $\mathbf{R}$ ,  $\mathbf{c\tau}$  of particle production using particle correlations due to the effects of quantum statistics ( QS ) and final state interactions ( FSI )

## Two-particle correlation function:

theory:

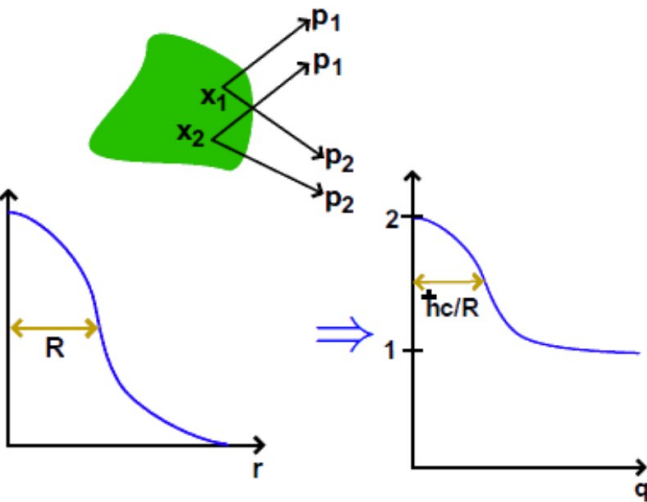
$$C(q) = \frac{N_2(p_1, p_2)}{N_1(p_1) \cdot N_2(p_1)}, C(\infty) = 1$$

experiment:

$$C(q) = \frac{S(q)}{B(q)}, q = p_1 - p_2$$

$S(q)$  – distribution of pair momentum difference from same event

$B(q)$  – reference distribution built by mixing different events



## Parametrizations used:

1D CF:  $C(q_{inv}) = 1 + \lambda e^{-R^2 q_{inv}^2}$

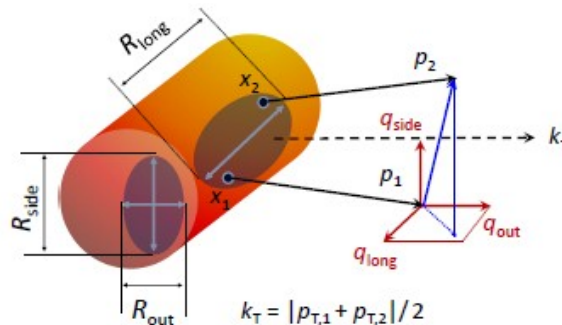
$R$  – Gaussian radius in PRF,

$\lambda$  – correlation strength parameter

3D CF:  $C(q_{out}, q_{side}, q_{long}) = 1 + \lambda e^{-R_{out}^2 q_{out}^2 - R_{side}^2 q_{side}^2 - R_{long}^2 q_{long}^2}$

$R$  and  $q$  are in Longitudinally Co-Moving Frame (LCMS)

long || beam; out || transverse pair velocity  $\mathbf{v}_T$ ; side normal to out, long



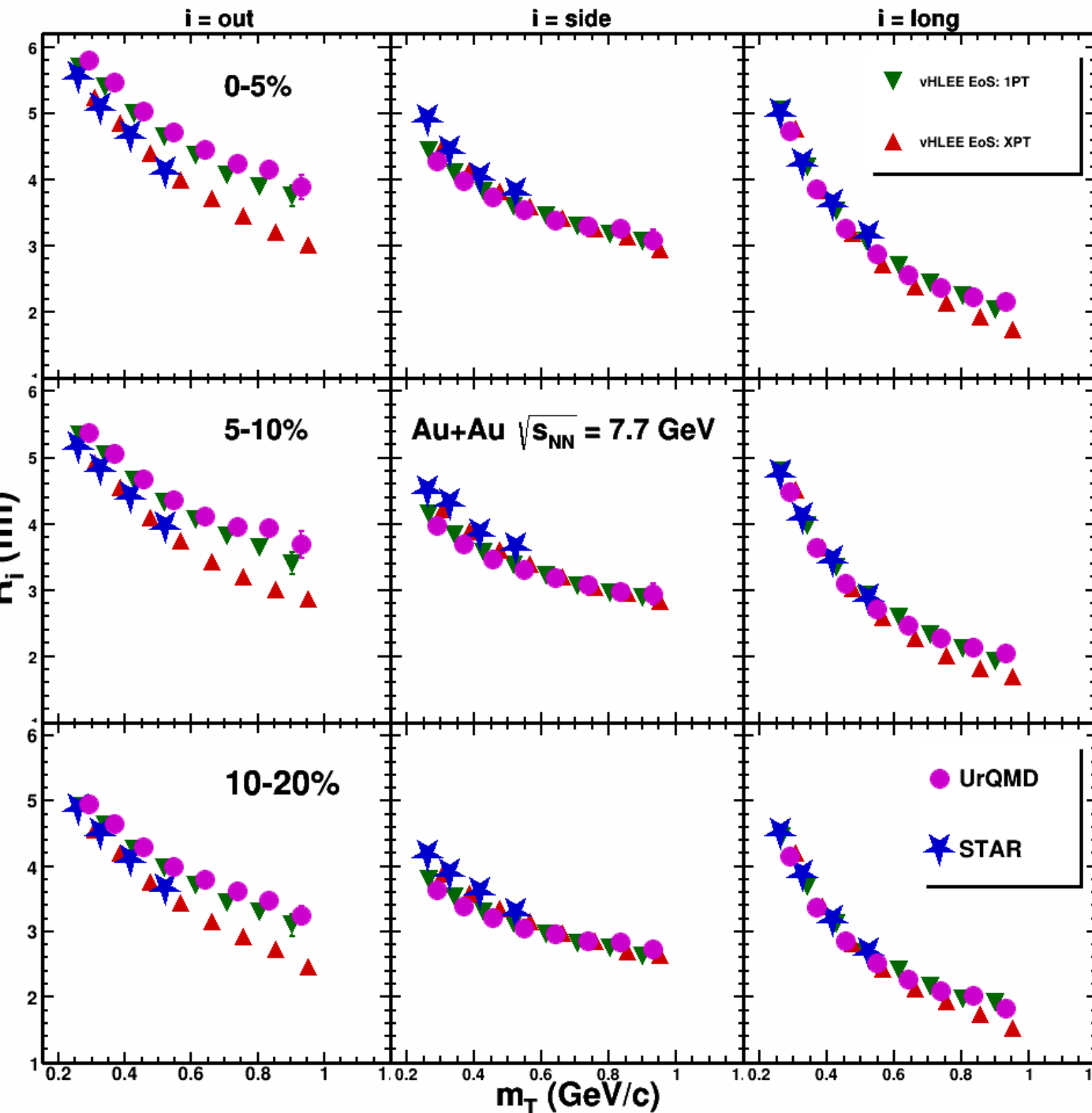
## 3D analysis:

$R_{side}$  sensitive to geometrical transverse size.

$R_{long}$  sensitive to time of freeze-out.

$R_{out} / R_{side}$  sensitive to emission duration.

# Pion radii with the vHLE and UrQMD models

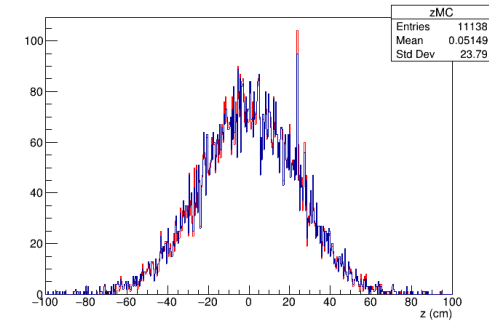
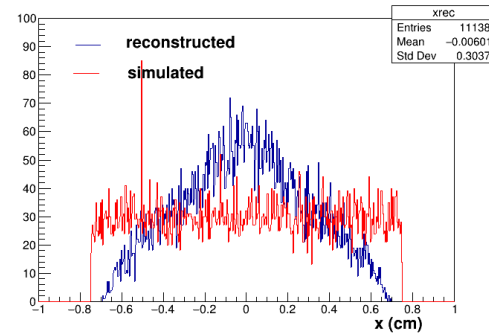


- Au+Au,  $\sqrt{s_{NN}} = 7.7$  GeV
- It is important to study femtosopic radii dependence in the broad  $k_T(m_T)$  range
- Difference between different models demonstrates it self more clearly.
- $k_T(m_T)$ -dependence allows to study evolution of the system
- Radii decrease with  $m_T \rightarrow$  radial flow
- Increase size with increasing centrality  $\rightarrow$  simple geometric picture of collisions
- Cross over EoS describes  $R_{out}(m_T)$  better than the 1st-order phase transition
- $R_{out,long}(1PT) > R_{out,long}(XPT)$
- Radii obtained from UrQMD are close to those from vHLE with the 1PT

# **Analysis of reconstructed data in MPD**

# Details of analysis

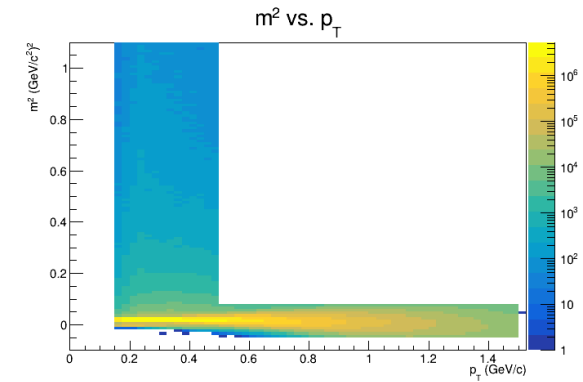
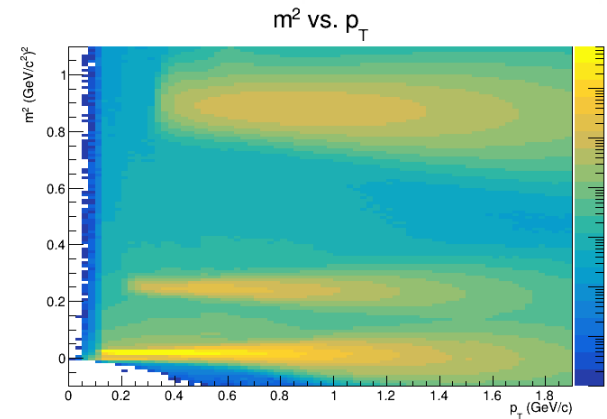
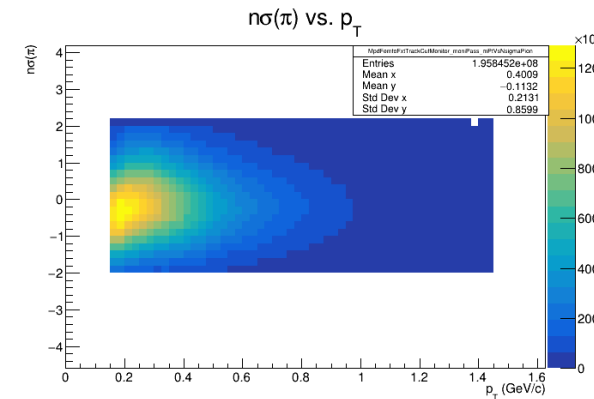
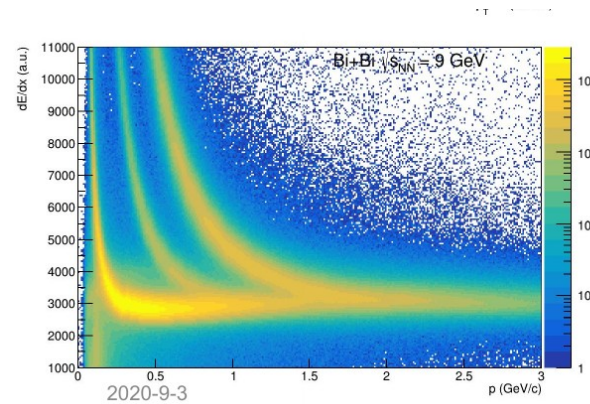
- Dataset (UrQMD → Geant4 → reconstruction) :  
 $\text{Bi+Bi } \sqrt{s_{\text{NN}}} = 9 \text{ GeV}$ :  
[/eos/nica/mpd/sim/data/MiniDst/dst-BiBi-09](#)  
[GeV-mp07-20-pwg3-250ev/BiBi/](#)  
[09.0GeV-0-14fm/UrQMD/](#)



- Track Cuts:  
 $0.15 < p_T < 1.5 \text{ GeV/c}$   
 $|\eta| < 1.0$   
 $N_{\text{hits}}(\text{TPC}) > 15$   
 $\text{DCA} < 5 \text{ cm}$

- PID  
 TPC+TOF,  
 - TOF starts at  $p > 0.5 \text{ GeV/c}$   
 - Pion nSigma for TPC+TOF identification (details will be shown)

Pions:  $2 \cdot 2.0 \cdot 10^8$



# Influence of track reconstruction on CF

## Track reconstruction influences the shape of CF

### • Single-track effects:

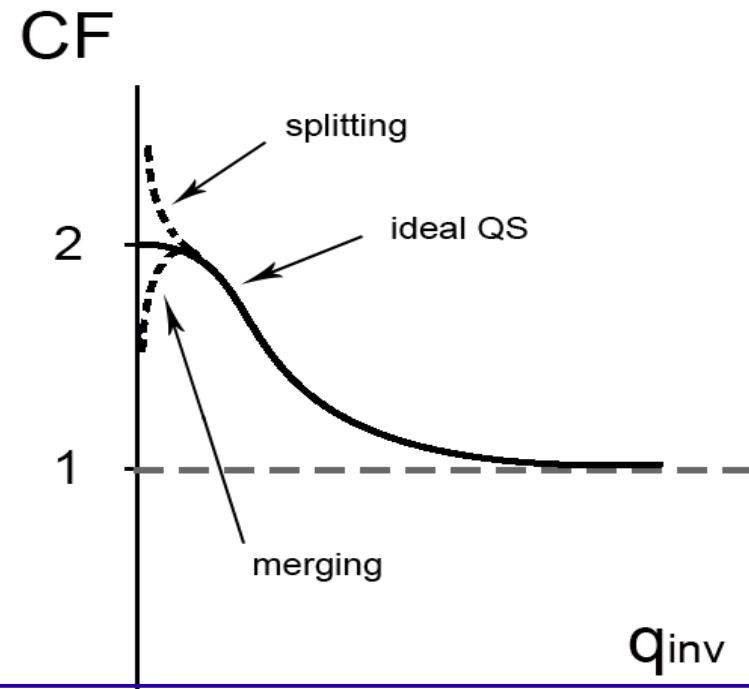
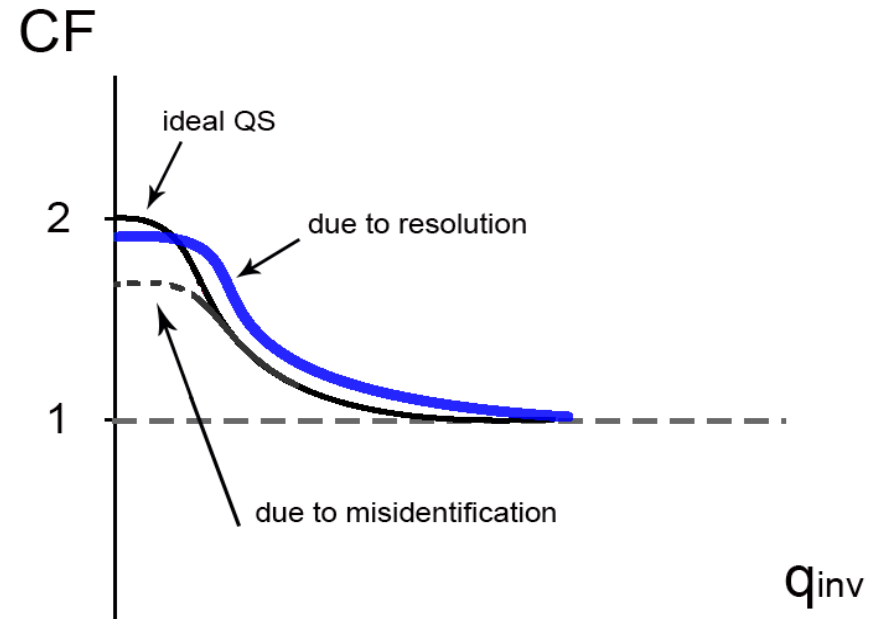
- The momentum resolution effect smears CF, making it wider and extracted radii smaller
- CFs should be corrected for single-track momentum resolution

### • Particle misidentification:

- Influences only  $\lambda$  parameter of CF, radii do not change
- CF should be corrected by pair purity. Pair purity is obtained from particle purity

### • Two-track effects:

- Track splitting (one track is reconstructed as two)
- Track merging (two tracks are reconstructed as one)
- These effects are studied and the specific pair cuts that will be applied in the femtoscopic analysis

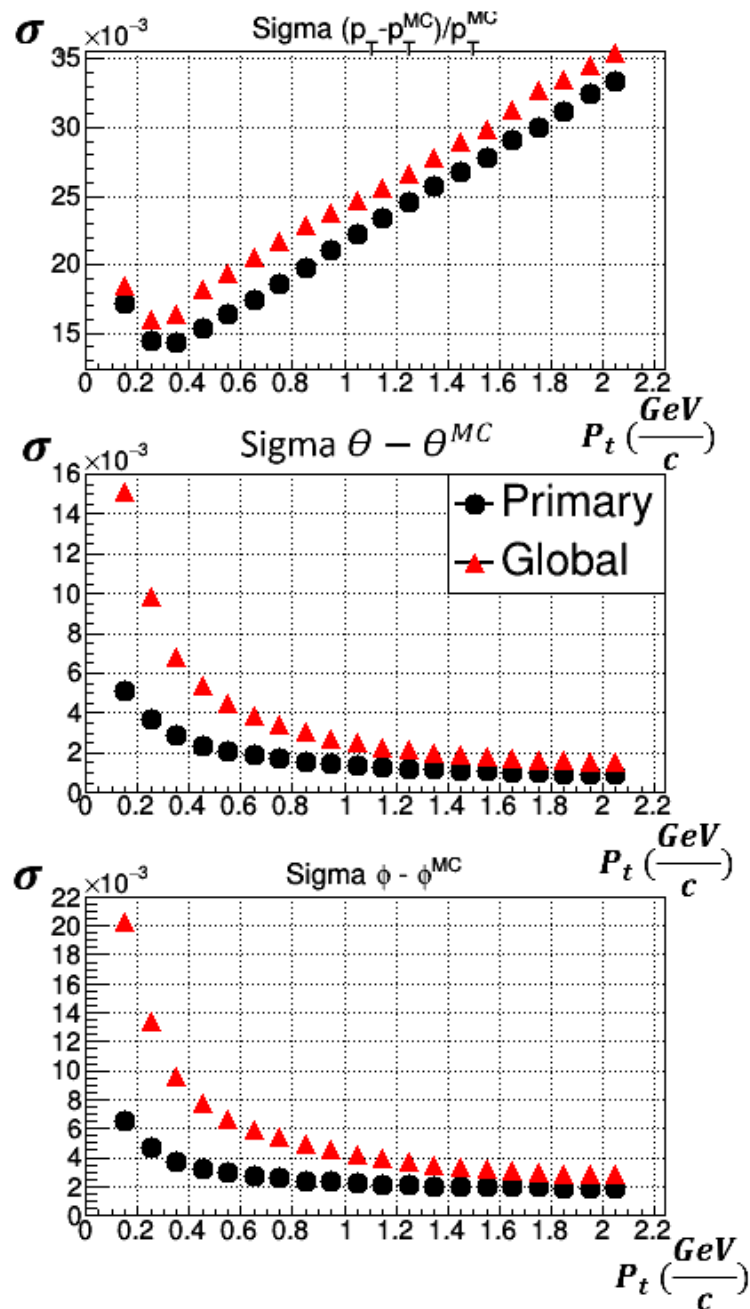




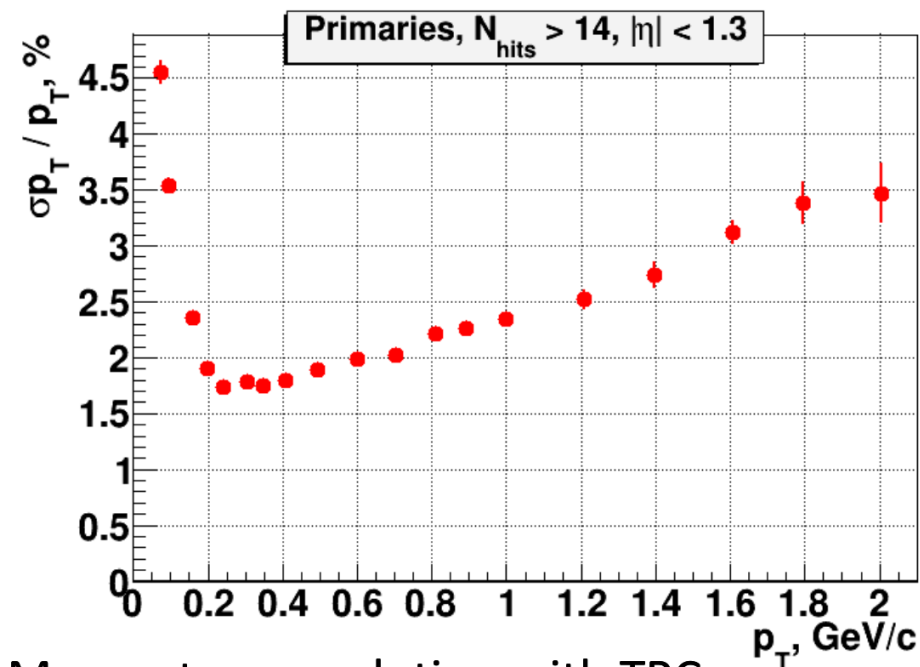
# Single-track effects in femtoscopy

- Single-track momentum resolution smears two-particle correlation function

# Momentum resolution for primary and global tracks



$|\eta| < 1$   
 $N_{hits} > 15$



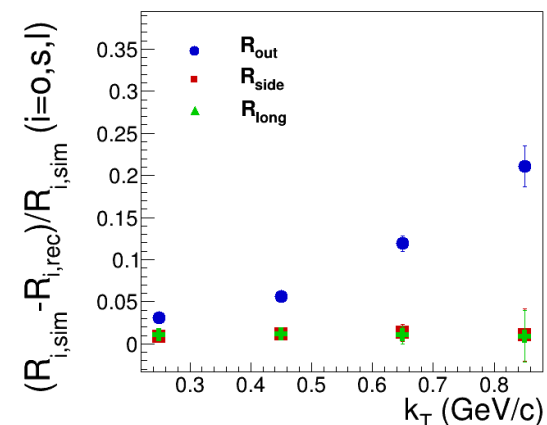
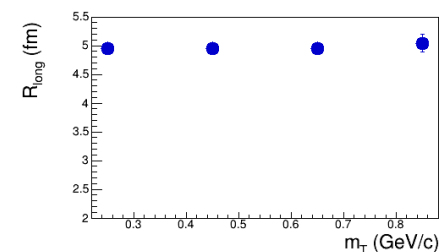
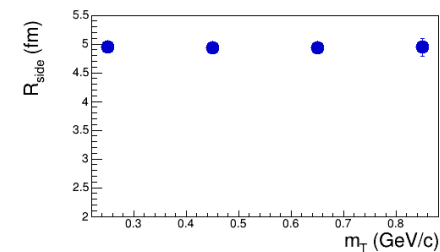
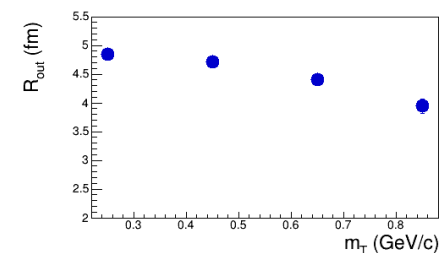
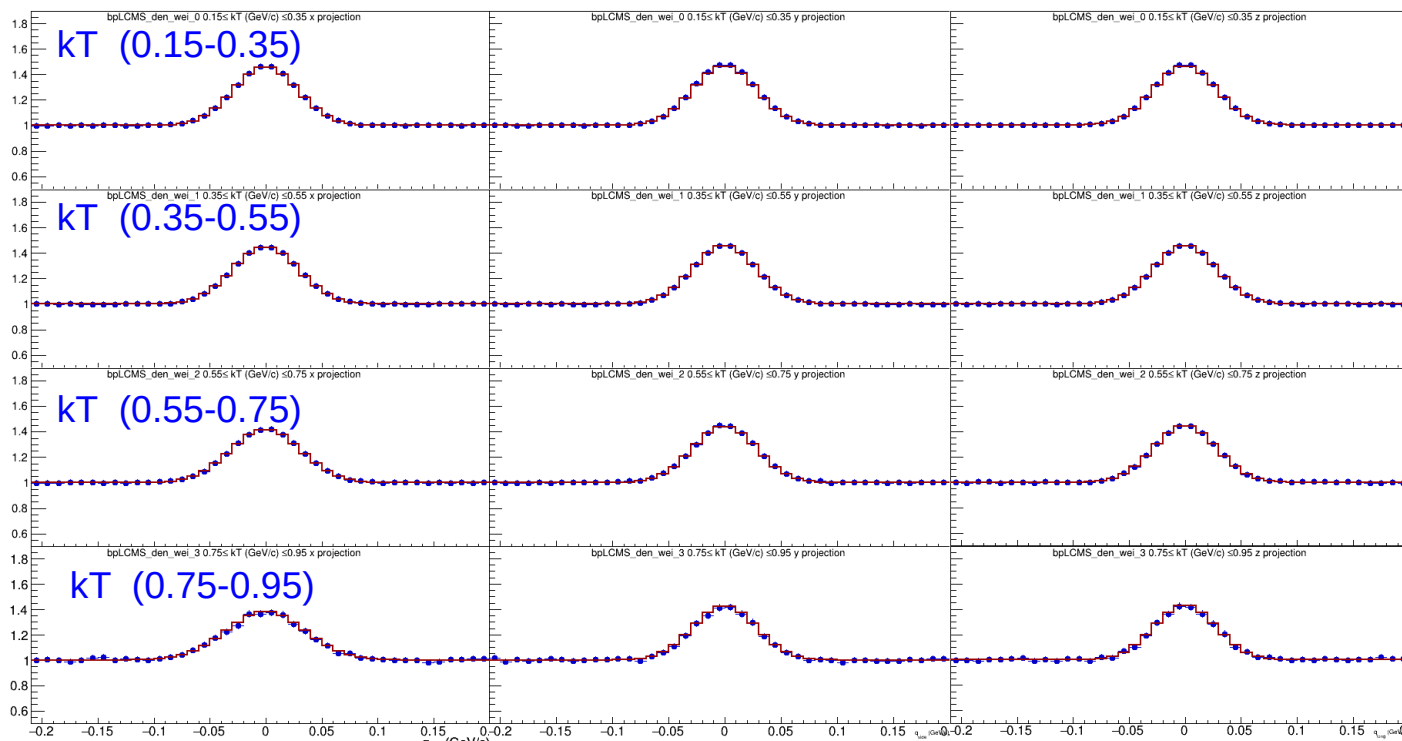
Momentum resolution with TPC

Egor Alpatov (student, NRNU MEPhI)  
 For tracks with vertex constrain (Primary tracks) momentum resolution is better

# Influence of momentum resolution on 3D CFs in LCMS

3D Gauss in LCMS  $R_{o1} = 5 \text{ fm}$  ;  $pdg1=211$  &  $pdg2=211$   
 $k_T$  (0.15-0.95) GeV/c & 4  $k_T$  bins

CF = (Dmixed, weight=QS)/ Dmixed



CFs become wider with increasing  $k_T$

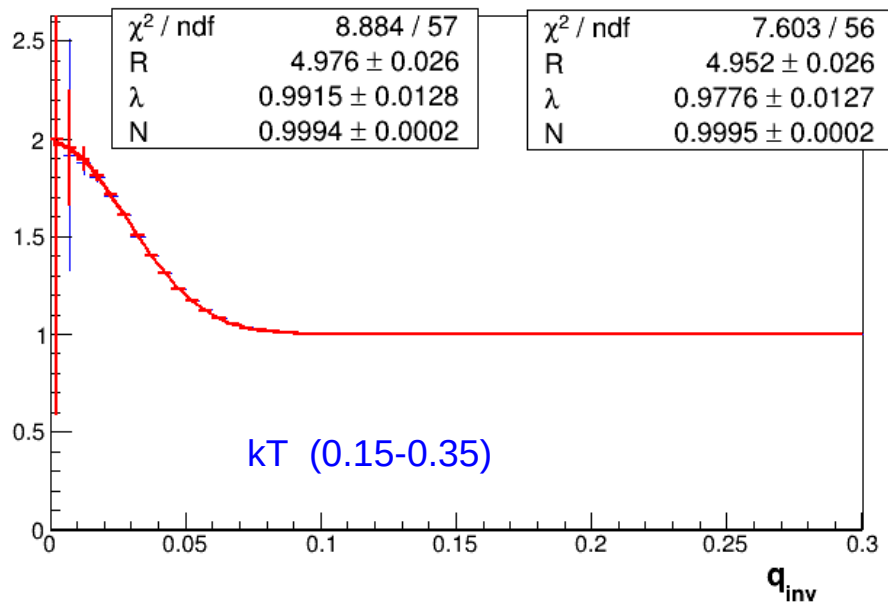
Resolution effect on  $R_{out}$  is strong at large  $k_T$

Calculations were performed for each (Ro,Rs,RI) combination. When projecting on one axis the other two components were required to be within  $(-0.04, 0.04)$  GeV/c.

# Influence of momentum resolution on 1D/3D CFs

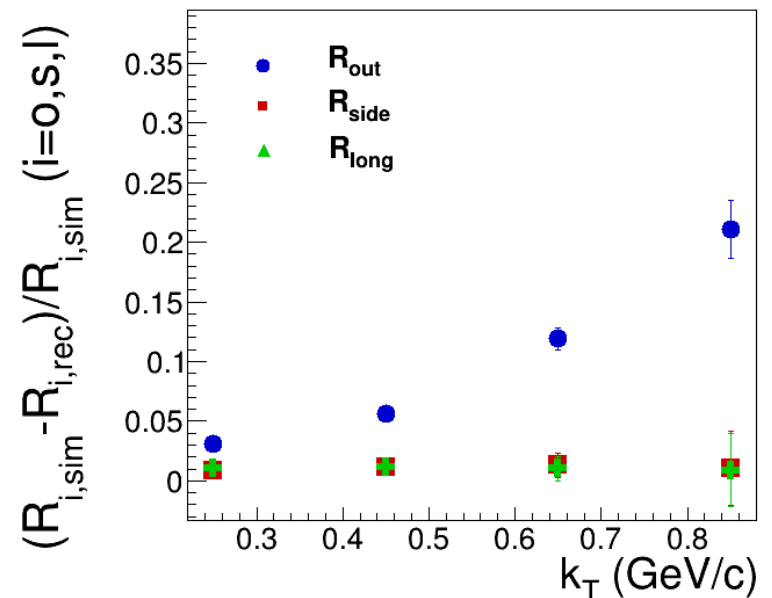
1D Gauss in PRF  $R_{inv} = 5$  fm  
 $k_T$  (0.15-0.95) GeV/c & 4  $k_T$  bins

$$CF = (D_{mixed}, \text{weight}=QS) / D_{mixed}$$



- Resolution effects for  $R_{inv}$ ,  $R_{side}$ ,  $R_{long}$  are small
- Resolution effect for  $R_{out}$  increases linearly with  $k_T$ .
- It is understandable because “out” component depends linearly on  $p_T$
- Similar effect is observed in ALICE data (effect in MPD ~1.5 times worse than in ALICE)

## MPD



## ALICE TDR

$K_t$ range (MeV/c)	Resolution (r.m.s.) (MeV/c)			
	$q_{inv}$	$q_o$	$q_s$	$q_l$
$100 < p_t < 300$	0.95	2.70	0.34	0.95
$300 < p_t < 600$	0.99	3.62	0.40	1.12
$p_t > 600$	1.17	6.33	0.62	1.42

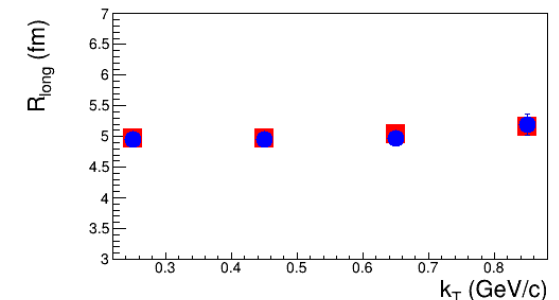
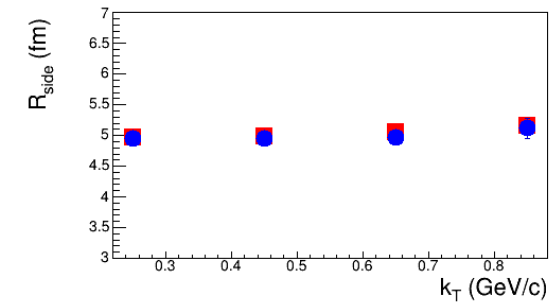
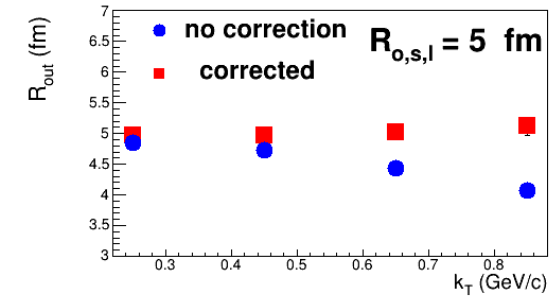
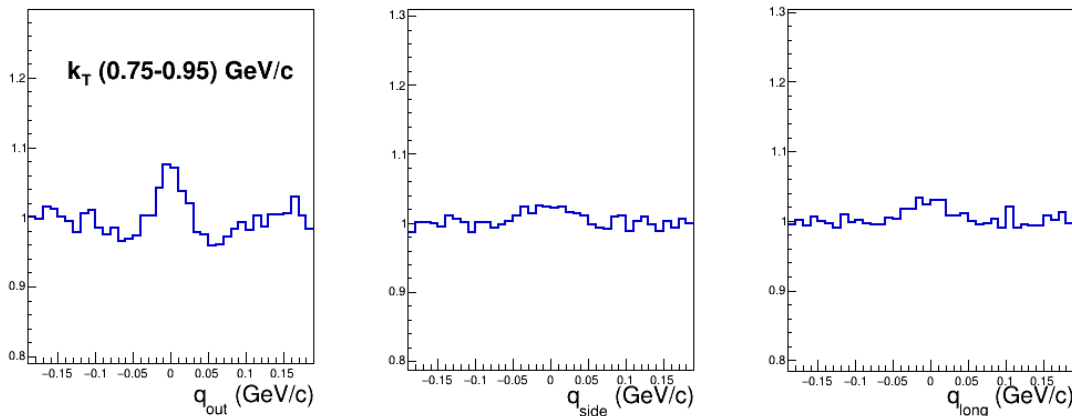
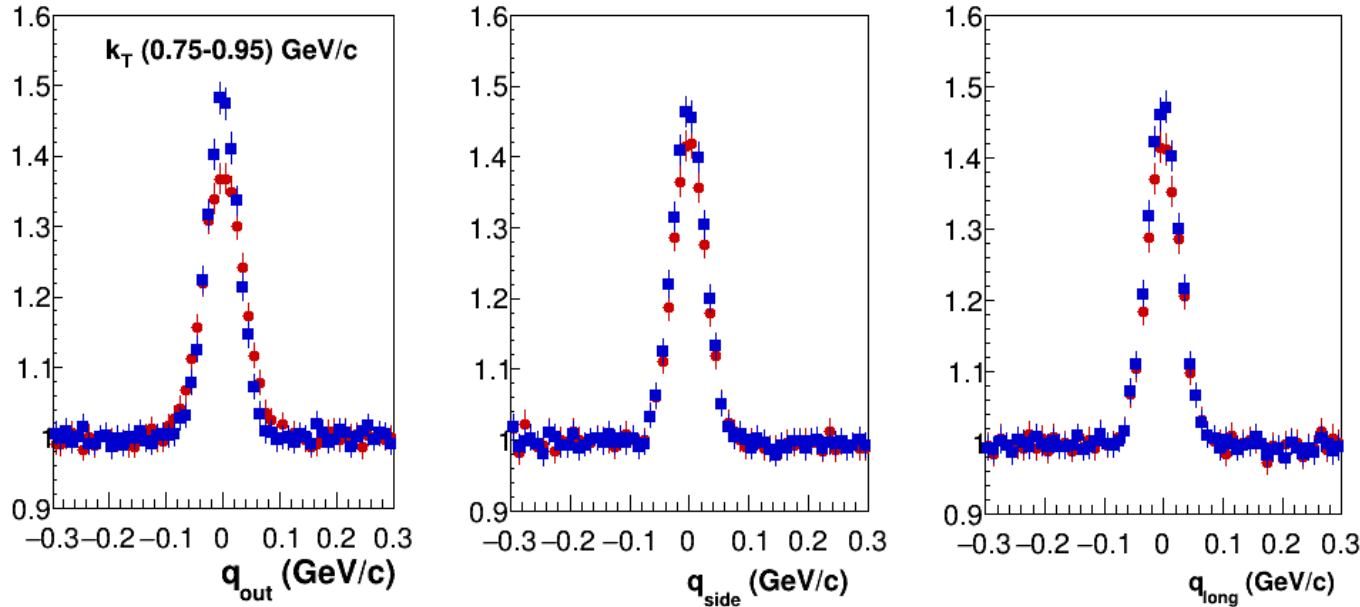
(a)

# Momentum resolution correction for 3D CFs in LCMS

3D Gauss in LCMS  $R_{osl} = 5 \text{ fm}$  ;  $CF = (D_{mixed}, \text{weight}=QS) / D_{mixed}$

Correction factor ( $q_{osl}$ ) =  $CF(q_{osl} \text{ simulated}) / CF(q_{osl} \text{ reconstructed})$

Example  $k_T$  (0.75-0.95) GeV/c



Resolution effect on  $R_{out}$  is strong at large  $k_T$ , but it is possible to correct CFs by momentum resolution

# Single-track effects in femtoscopy

- n-Sigma method was tested and applied  
(Alexei Chernishov (MSU student))
- Particle misidentification  
Influences only  $\lambda$  parameter of CF, radii do not change  
CF should be corrected by pair purity, determined using  
single particle purity

# $n_\sigma$ in TPC

Measured  
distribution

Extracted  
parameter

Applied cut

$$\frac{dE/dx_{TPC} - \langle dE/dx \rangle}{\sigma_E}$$



Mean  $\mu_E$



$$\left| \frac{dE/dx_{TPC} - \langle dE/dx \rangle}{\sigma_E} - \mu_E \right| < n_\sigma$$

Since sigma-based cut is applied, it is denoted as  $n_\sigma$  in TPC.

***NB.** Mean value  $\mu_E$  is meant to correct some systematic errors, if they are present. Otherwise it equals zero.*

# $n_\sigma$ in TOF

Measured  
distribution

$$\frac{1/\beta_{TOF} - 1/\beta}{1/\beta}$$



Extracted  
parameters

Mean  $\mu_\beta$   
Std. dev.  $\sigma_\beta$



Applied cut

$$\left| \frac{1/\beta_{TOF} - 1/\beta}{1/\beta} - \mu_\beta \right| < n_\sigma \sigma_\beta$$

$$\frac{m_{TOF}^2 - m^2}{m^2}$$



Mean  $\mu_m$   
Std. dev.  $\sigma_m$



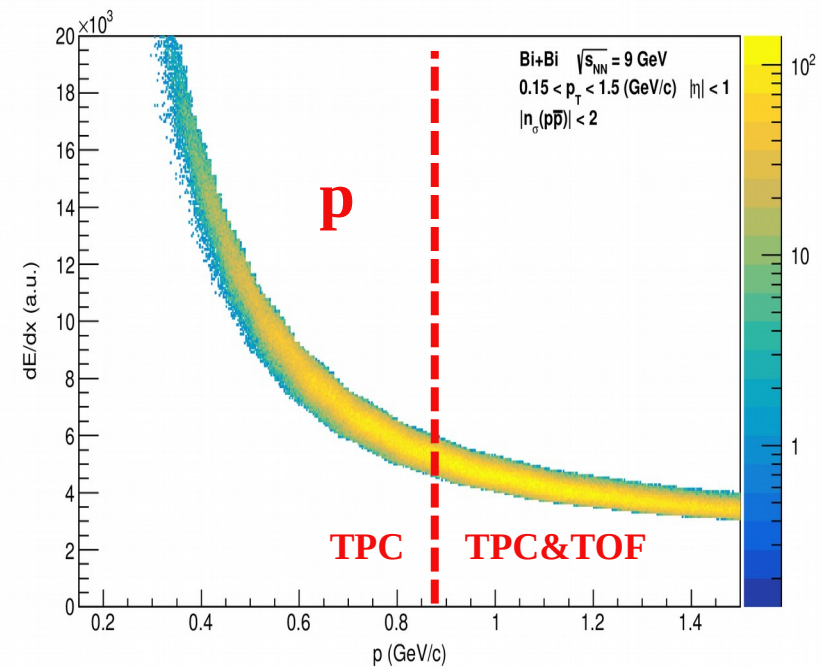
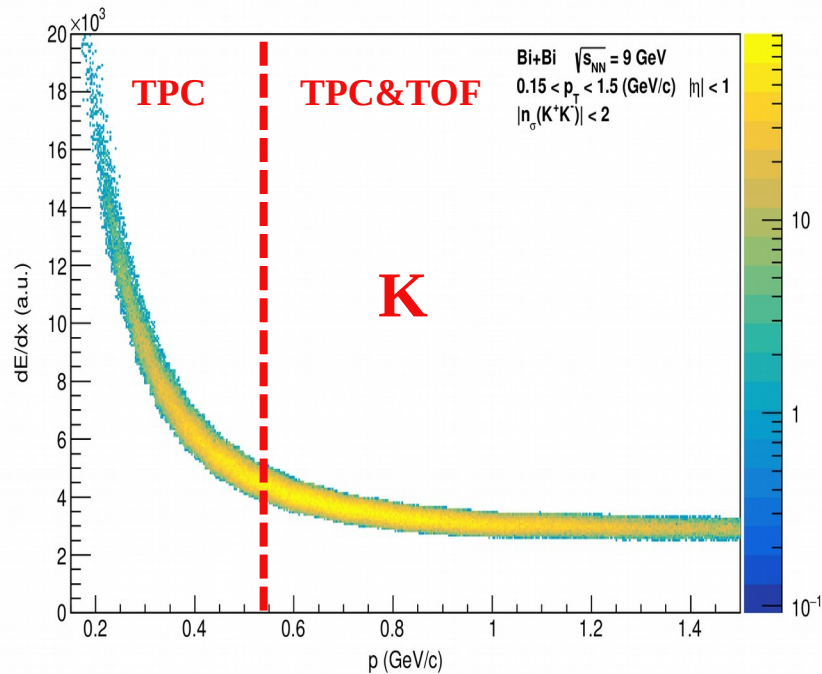
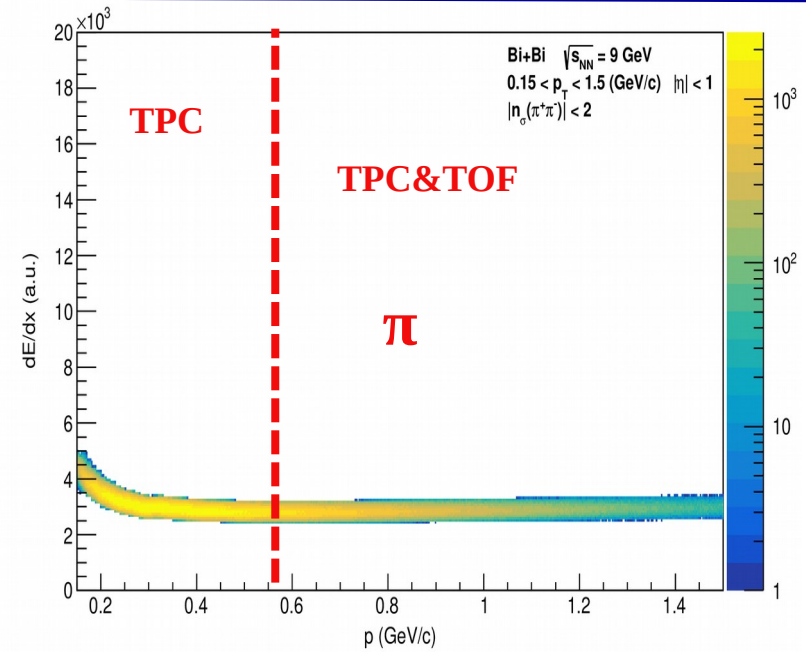
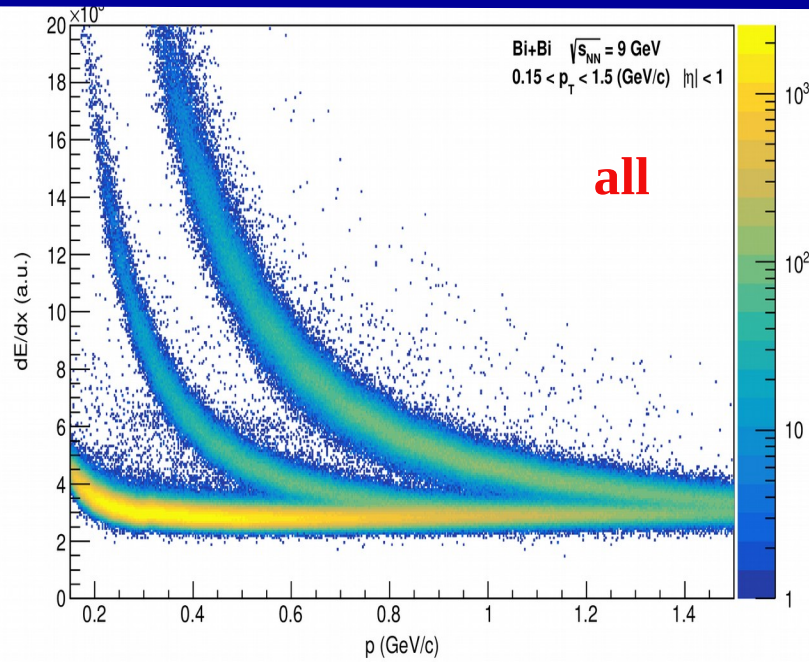
$$\left| \frac{m_{TOF}^2 - m^2}{m^2} - \mu_m \right| < n_\sigma \sigma_m$$

Since sigma-based cut is applied, it is denoted as  $n_\sigma$  in TOF.

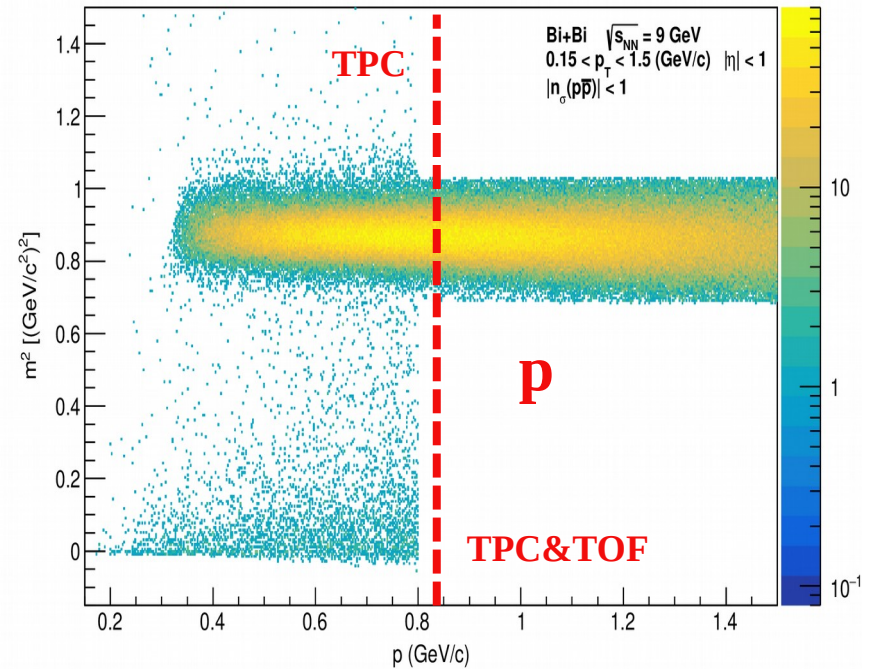
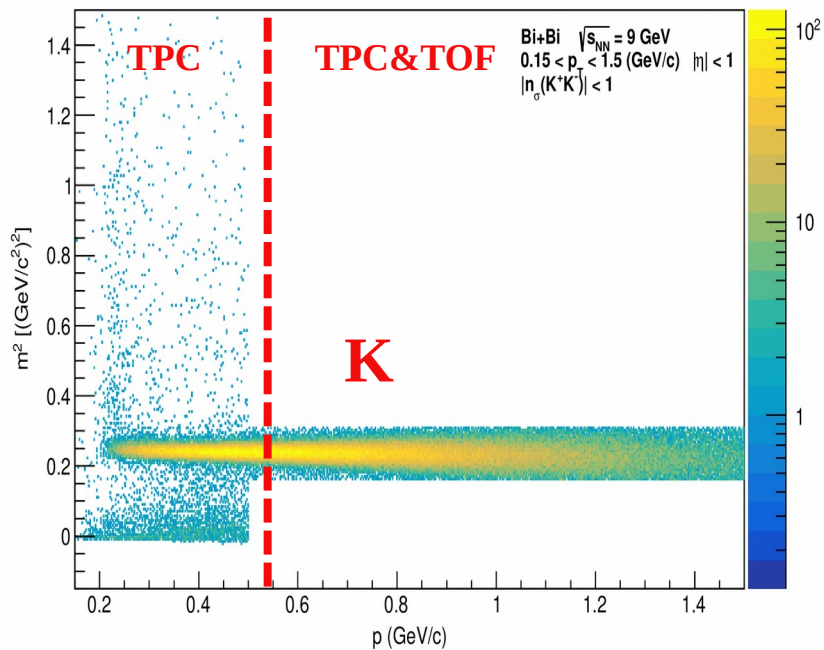
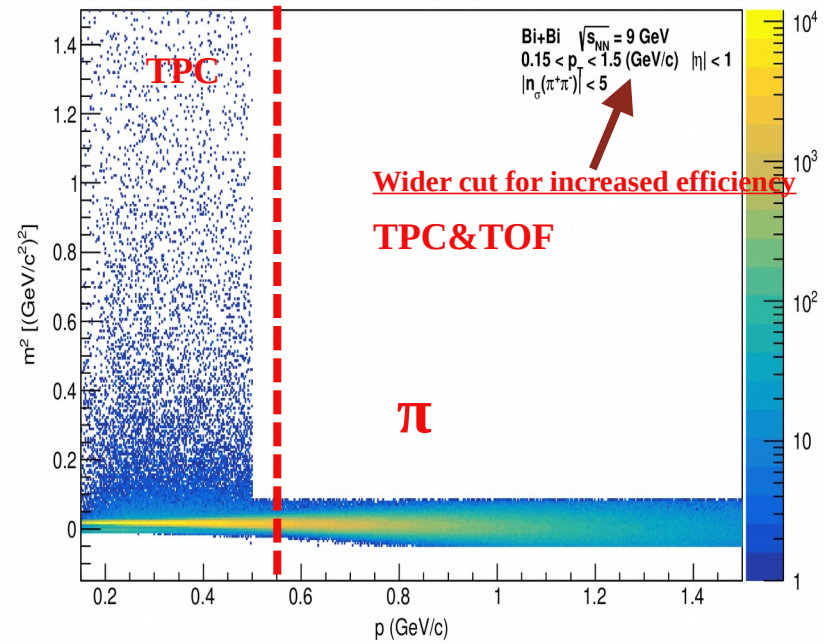
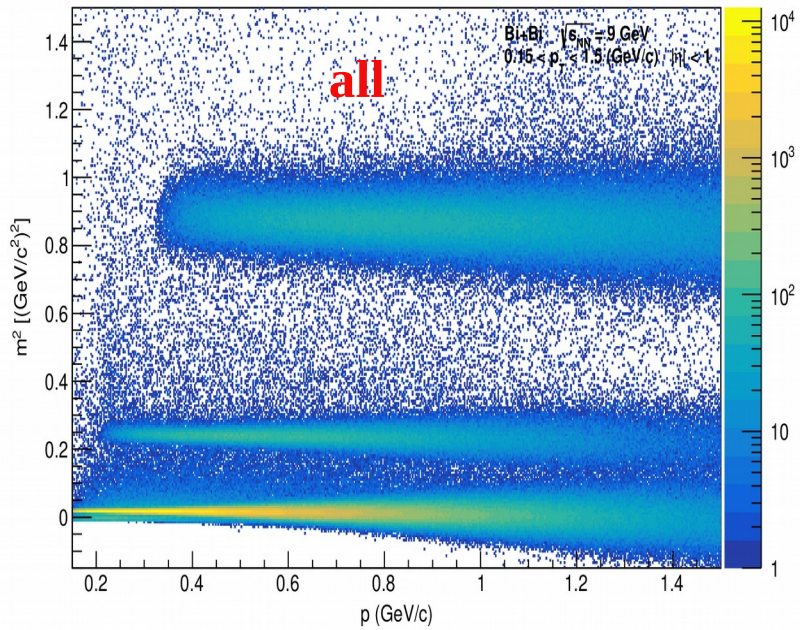
**NB.** Mean values  $\mu_\beta$  and  $\mu_m$  are meant to correct some systematic errors, if they are present. Otherwise they equal zero.



# Particle selection by TPC dE/dx(p)



# Particle selection by TOF $m^2(p)$



# Efficiency & Purity & Contamination

$$\epsilon_i = \frac{dN_{ii}^{meas}/dp}{dN_i/dp} - \text{efficiency}$$

$$f_i(p) = \frac{dN_{ii}^{true}/dp}{dN_i^{meas}/dp} - \text{purity}$$

$$cont_{ij}(p) = \frac{dN_j^{false}/dp}{dN_i^{meas}/dp} - \text{contamination}$$

$N_i$ : all generated particles of specie  $i$

$N_{ii}^{meas}$ : particles identified as specie  $i$  (within  $N_i$ )

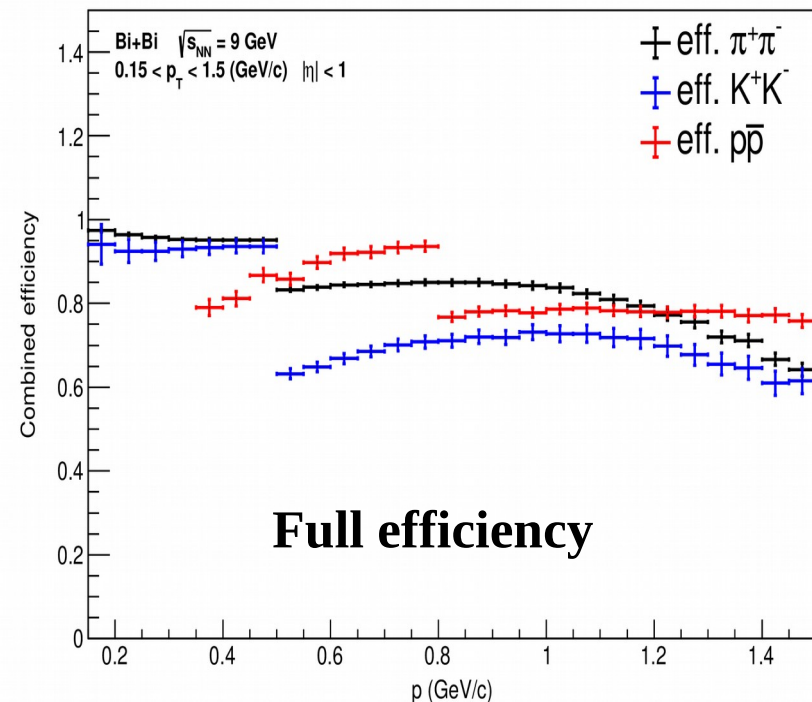
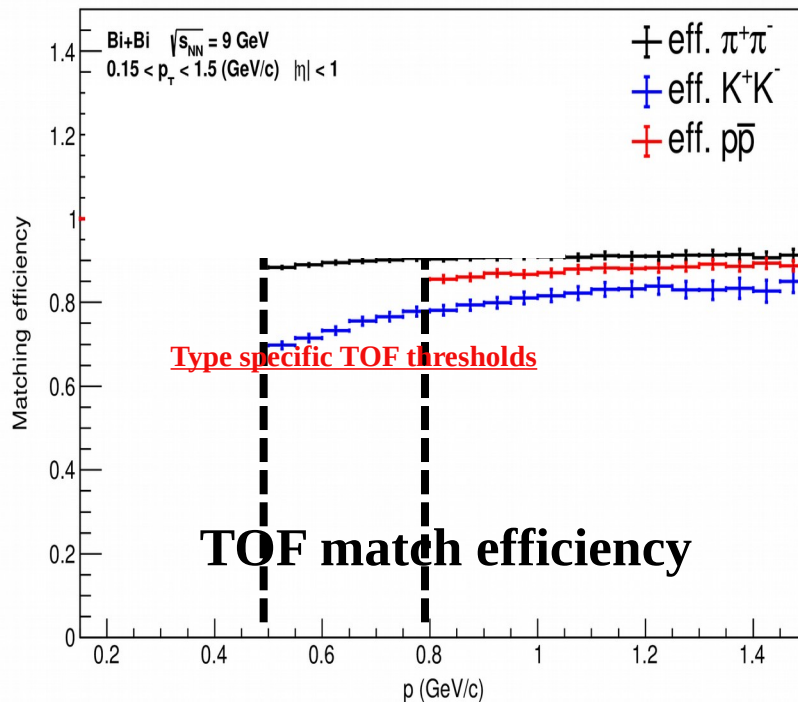
$N_i^{meas}$ : all particles identified as specie  $i$

$N_{ii}^{true}$ : particles identified as specie  $i$ ,  
are actually  $i$  (within  $N_i^{meas}$ )

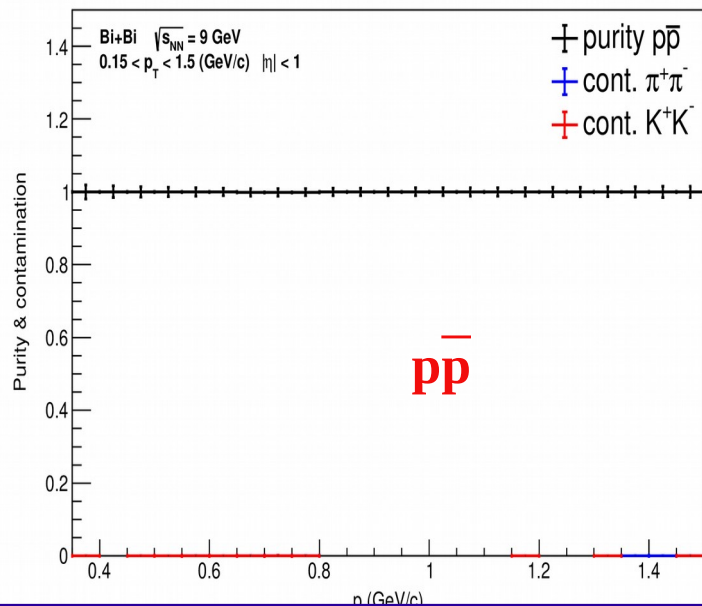
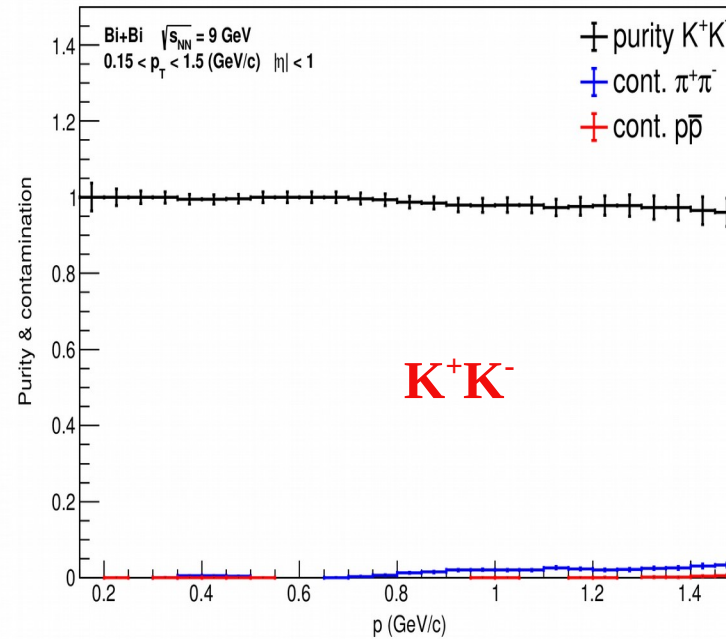
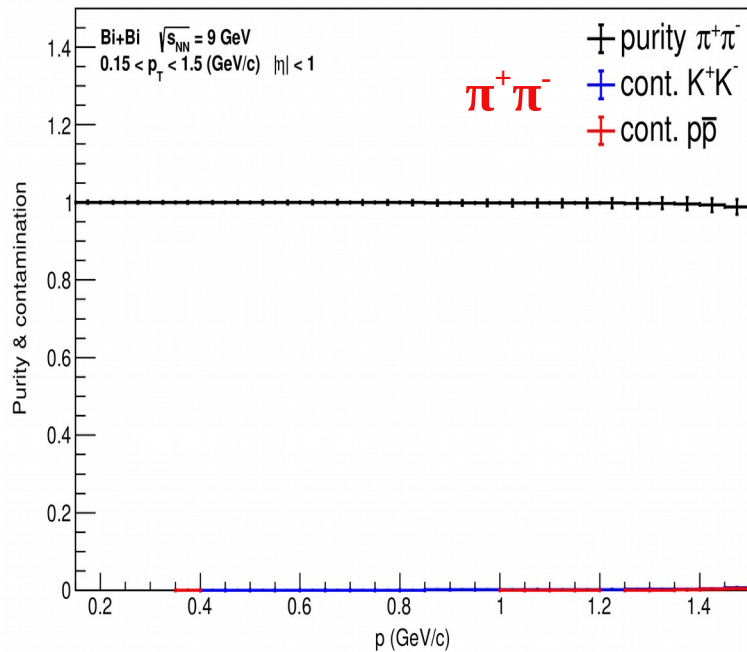
$N_i^{false}$ : particles misidentified as specie  $j$

$N_{ii}^{meas}$ : all particles identified as specie  $i$

Tracks are required to match TOF hit for track with momentum greater than the threshold.



# Purity & contamination



- n-Sigma method (used by ALICE & STAR) was successfully tested;
- Obtained small particle misidentifications are non-realistic;
- But n-sigma procedure can be applied for any realistic simulations;
- CF can be corrected by pair purity, determined using single particle purity

# Two-track effects in femtoscopy

- *Track merging (two tracks are reconstructed as one)*
- *Track splitting (one track is reconstructed as two)*

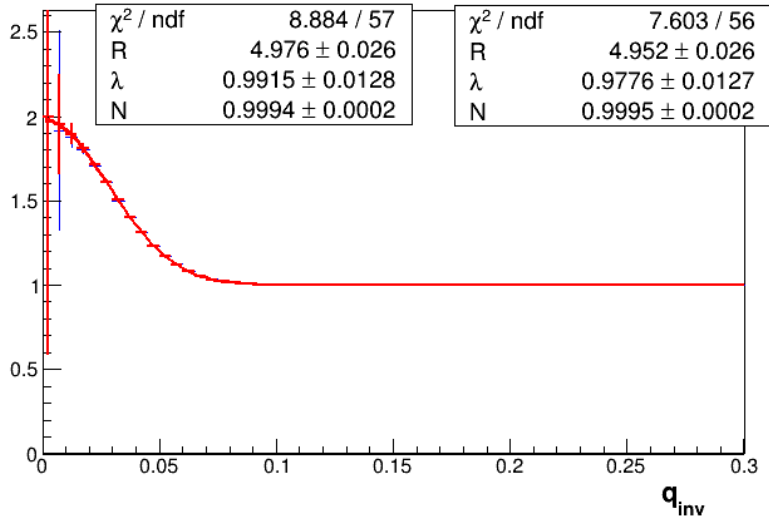
Communication with tracking group is ongoing  
(many thanks to Alexander Zinchenko !)

# 1D Correlation Function $CF(q_{inv})$

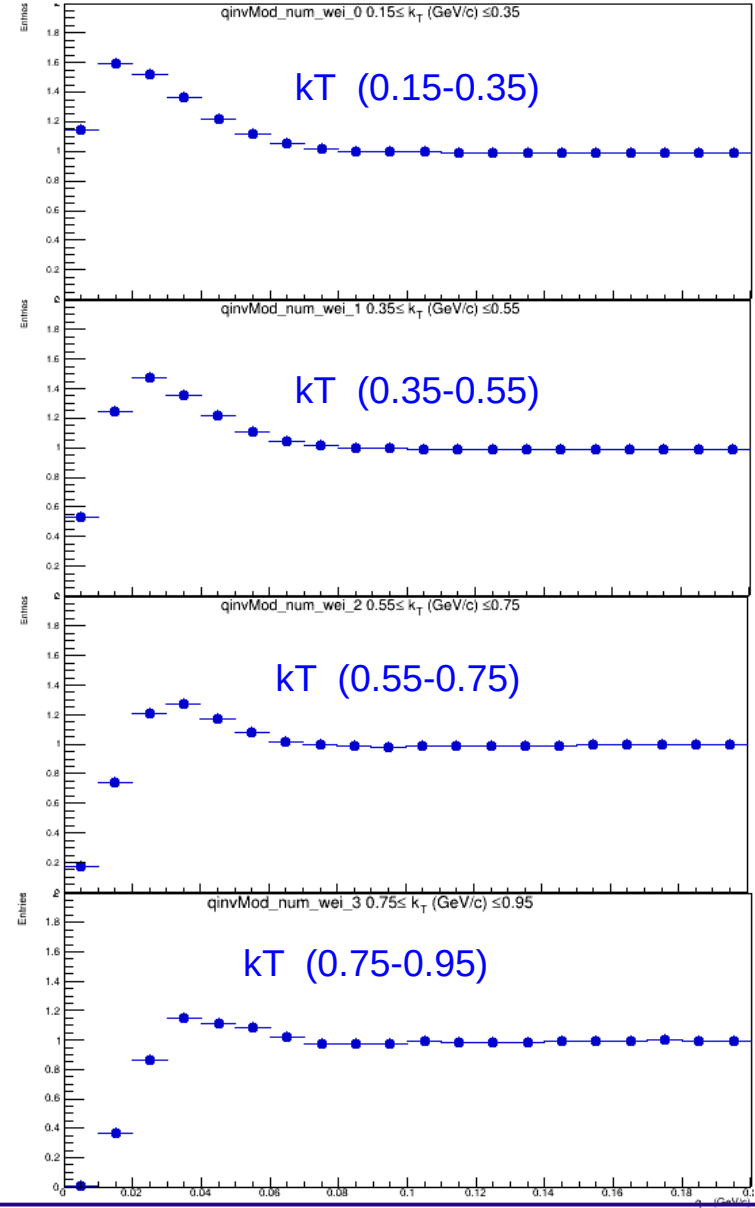
**Simulated** : Gauss in PRF,  $R_{inv} = 5$  fm

**Reconstructed**

$$CF = (N_{same}, \text{weight}=QS) / D_{mixed}$$



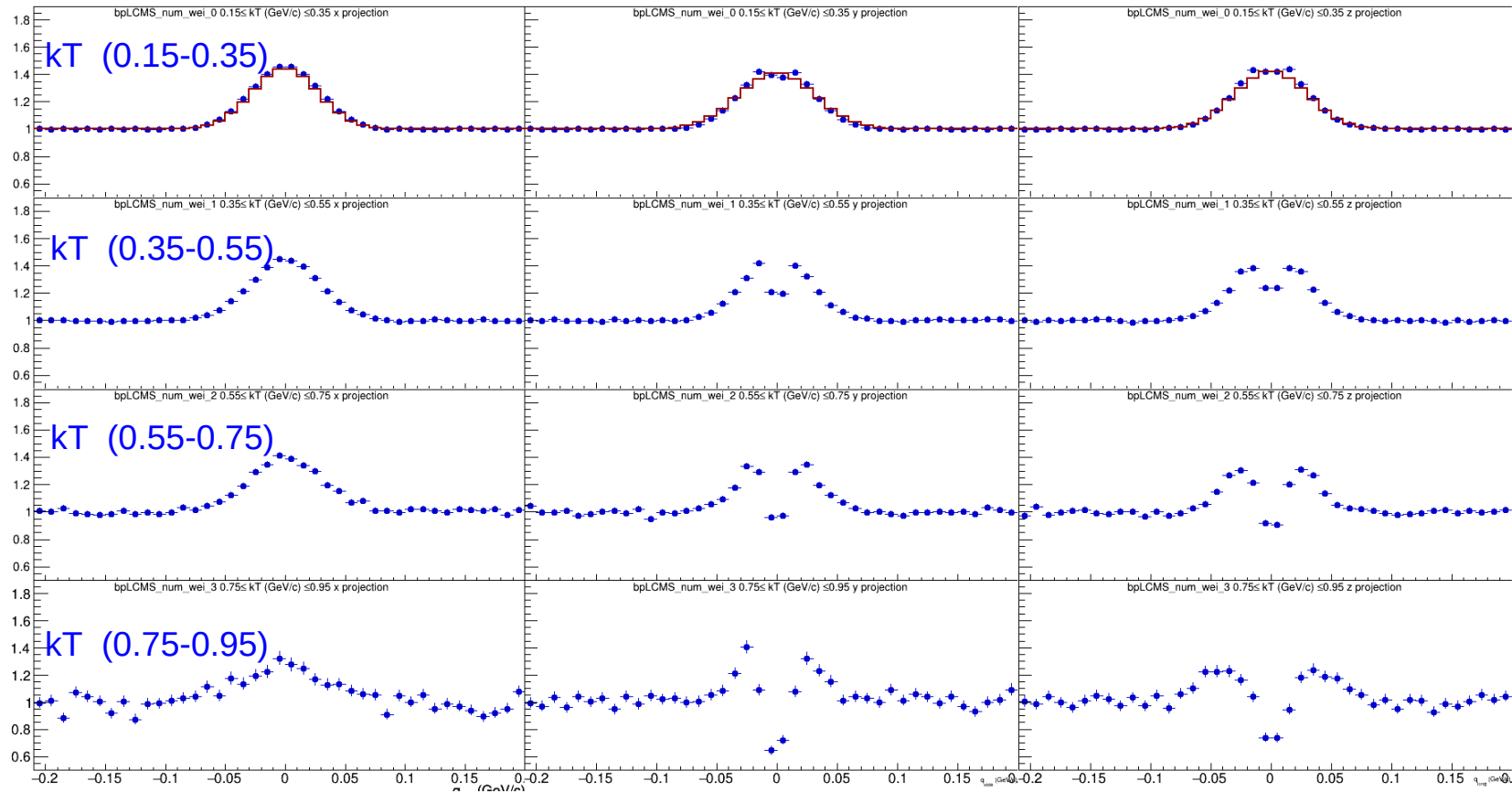
- The deep in CF due to the track-merging effect increases with  $k_T$
- Influence of the track-merging effect is extremely strong (especially at  $k_T > 0.55$  GeV/c)



# 3D Correlation Function

**Simulated** : Gauss in LCMS,  $R_{\text{iout}} = R_{\text{side}} = R_{\text{ilong}} = 5 \text{ fm}$

**CF = (Nsame, weight=QS) / Dmixed**

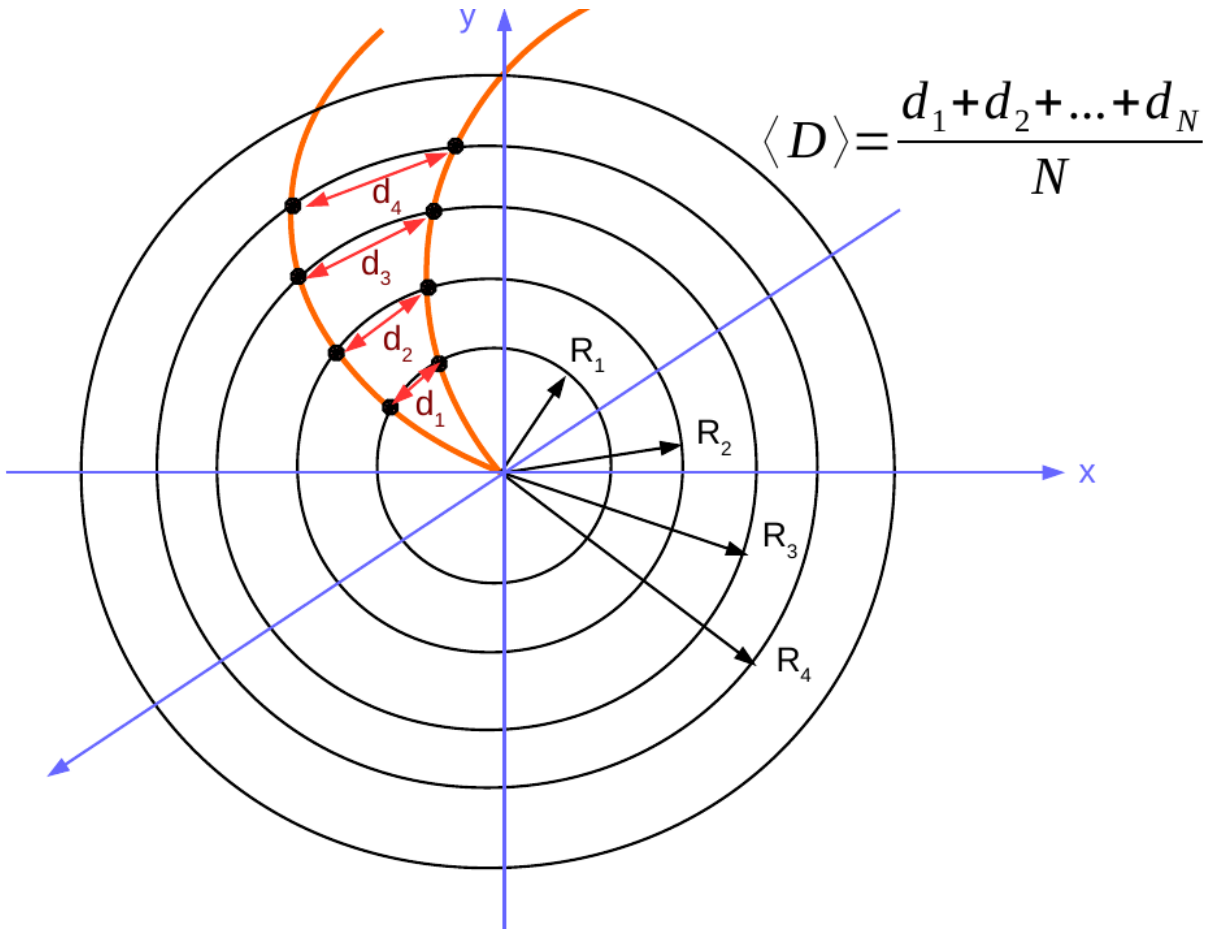
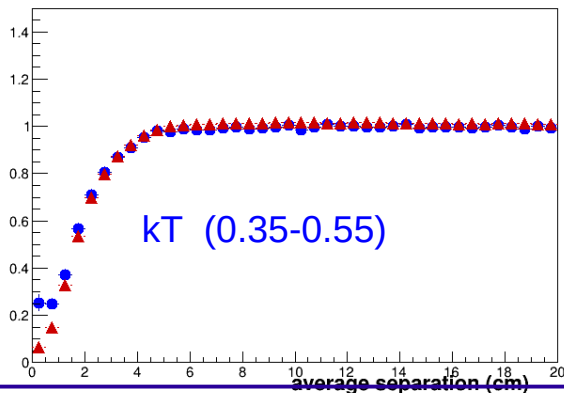
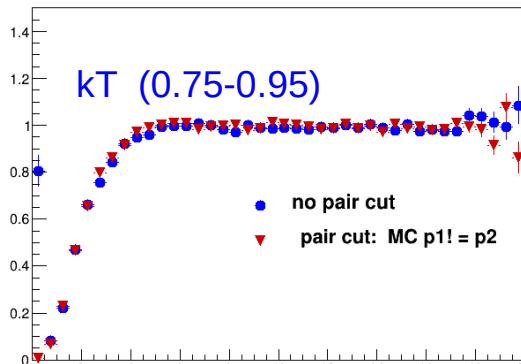
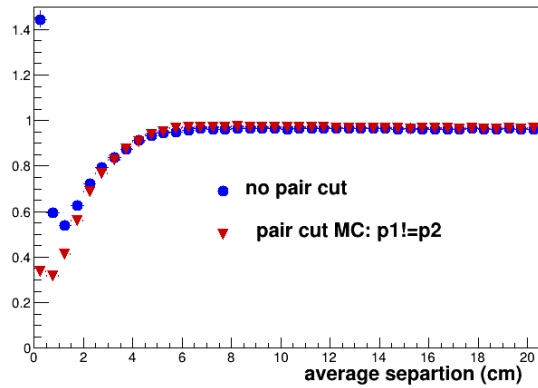


Projections of the three-dimensional  $\pi\pi$ -correlation functions. When projecting on one axis the other two components were required to be within  $(-0.04, 0.04) \text{ GeV}/c$ .

● **Strong “merging-like” effect increases with  $k_T$**

# Average separation in TPC

CF = Nsame/ Dmixed



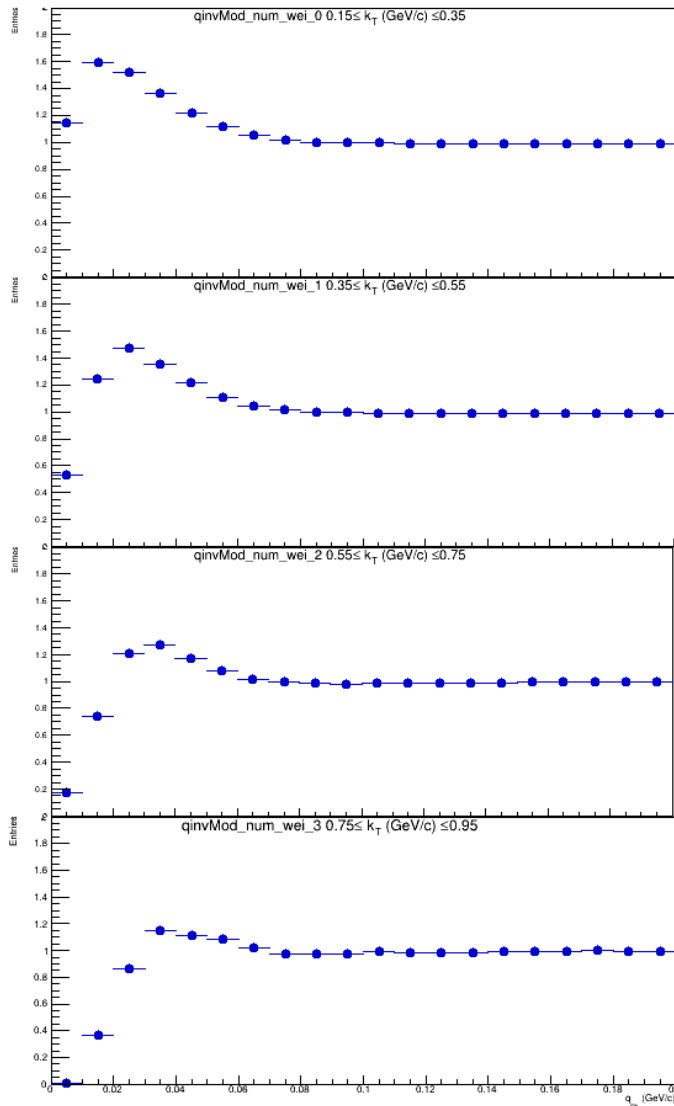
● average separation cut (>6 cm) was chosen for all  $k_T$  intervals



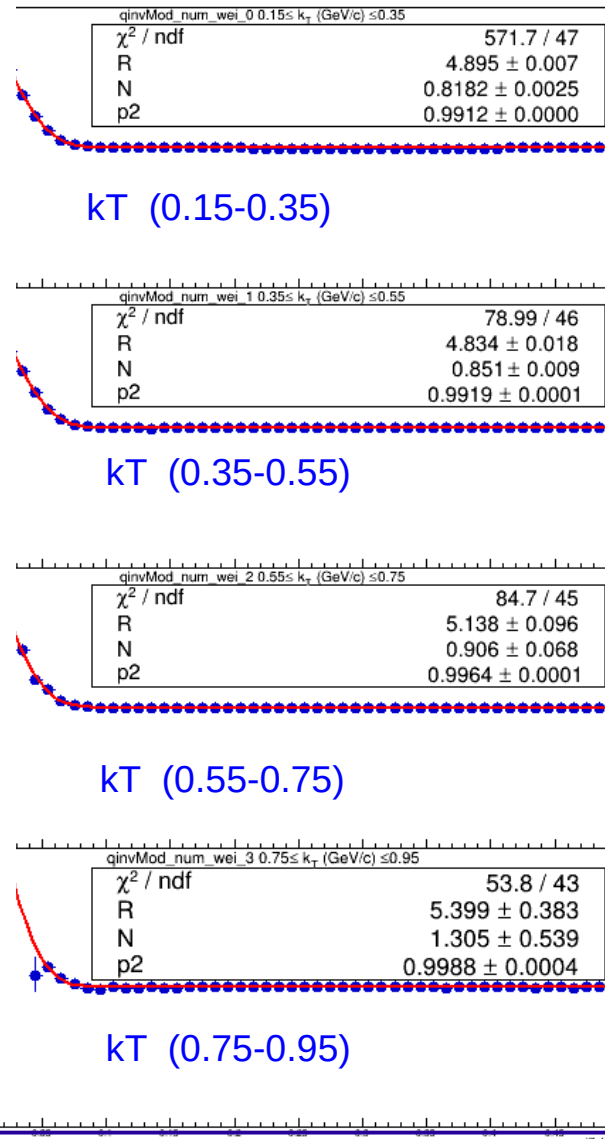
# 1D CF( $q_{inv}$ ) with two-track spatial average separation cut

CF = (Nsame, weight=QS) / Dmixed    Gauss in PRF     $R_{inv} = 5$  fm

No two-track cuts (No TTC)



Average separation > 6 cm



- Influence of the track-merging effect is extremely strong (especially at  $k_T > 0.55$  GeV/c)

- Average separation cut significantly removes pairs at small  $q_{inv}$  especially at  $k_T > 0.55$  GeV/c

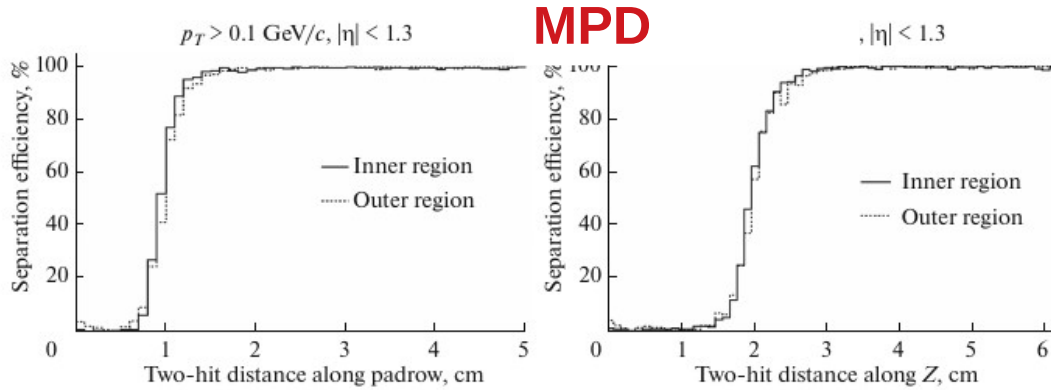
- For a moment impossibility to perform even 1D femtosopic analysis at  $k_T > 0.55$  GeV/c

**Why ?**

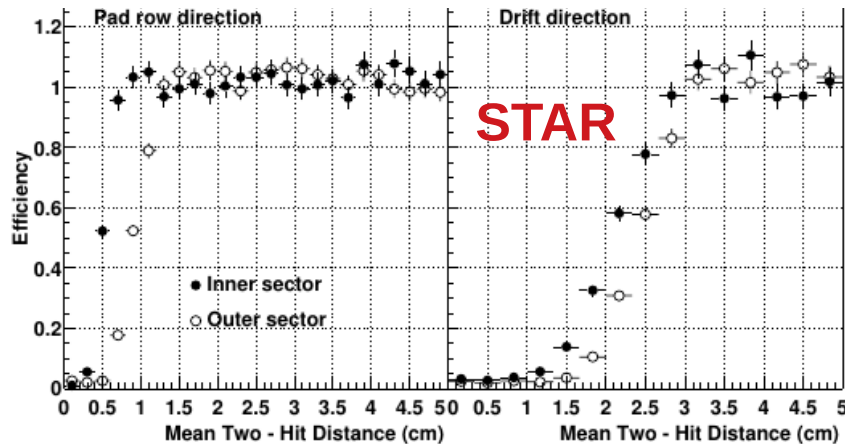
- two-hit resolution (comparable with STAR)
- two-track resolution ?

# Two Hits Separation Efficiency ( STAR / MPD )

Parameter	MPD	STAR
Magnetic field	0.5 T	same
Drift gas	P10 (90% Argon + 10% Methane)	same
Drift velocity	5.45 cm/ $\mu$ s	same
Transverse diffusion ( $\sigma_T$ )	185 $\mu$ m/ cm	230 $\mu$ m/ cm
Longitudinal diffusion ( $\sigma_L$ )	320 $\mu$ m/ cm	360 $\mu$ m/ cm
Pad size	5 $\times$ 12 mm <sup>2</sup> (27 rows) + 5 $\times$ 18 mm <sup>2</sup> (26 rows)	2.85 x 11.5 mm <sup>2</sup> (13 rows) + 6.20 x 19.5 mm <sup>2</sup> (32)
Outer radius of the drift volume	133 cm	200 cm
Inner radius the drift volume	34 cm	50 cm
Length of drift volume	170 cm (each half)	210 cm (each half)



“Towards of a Realistic Monte Carlo Simulation the MPD Detector at NICA”  
 V. Kolesnikov, A. Mudrokh, V. Vasendina, and A. Zinchenko  
 Physics of Particles and Nuclei Letters, 2019, Vol. 16, No. 1, pp. 6



“The STAR time projection chamber: a unique tool for studying high multiplicity events at RHIC”  
 Nuclear Instruments and Methods in Physics Research A 499 (2003) 659–678

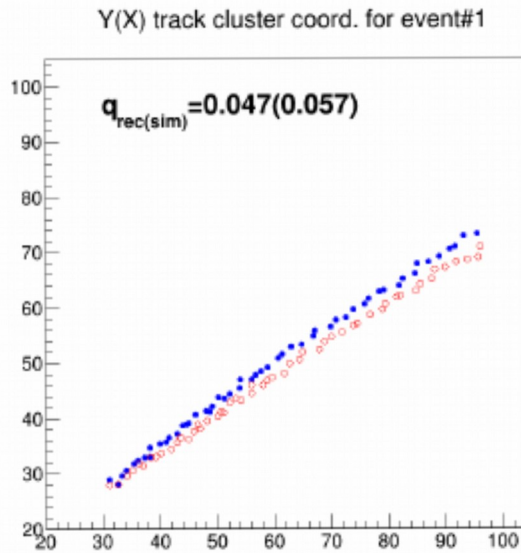
**Characteristics of MPD TPC are comparable with STAR TPC → two hits resolutions are comparable**

# Two-track efficiency with pair of isolated tracks

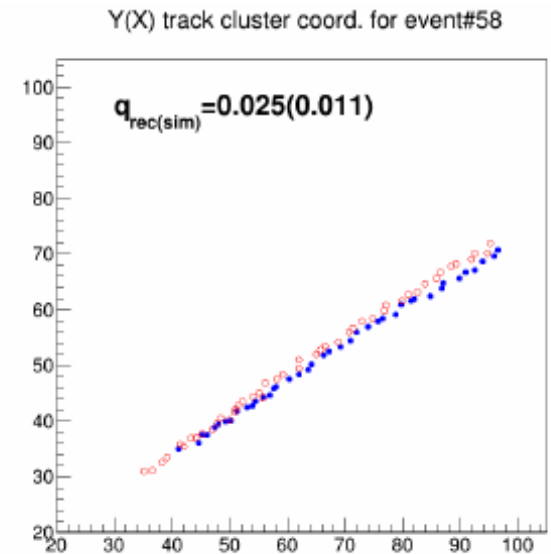
- Box generator was used to simulate  $\pi\pi$  pair with close momenta

- Efficiency of two-pair reconstruction strongly decrease with pair  $p_T$ 
  - Global tracks (no vertex constrains)
  - Primary (vertex constrained tracks)

Well reconstructed as 2 tracks



Still reconstructed as 2 tracks

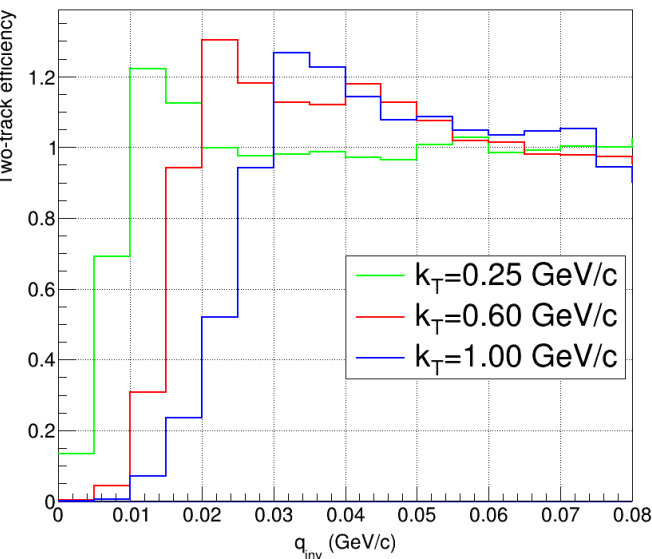


Efficiency of two-tracks reconstruction with:

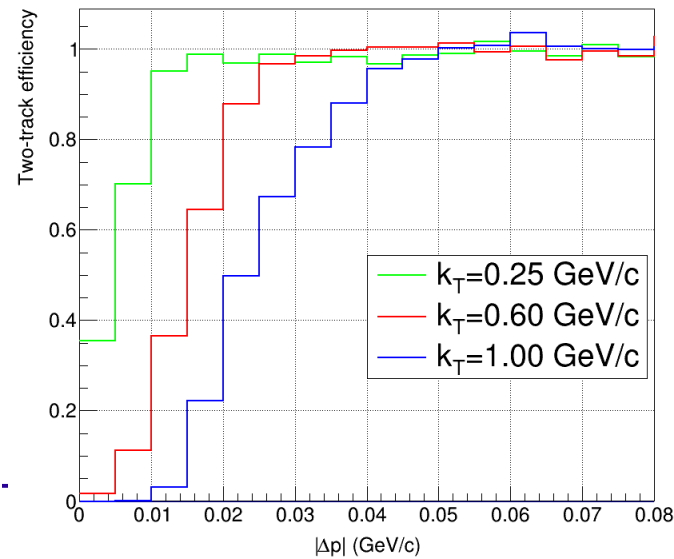
Global tracks

Primary tracks

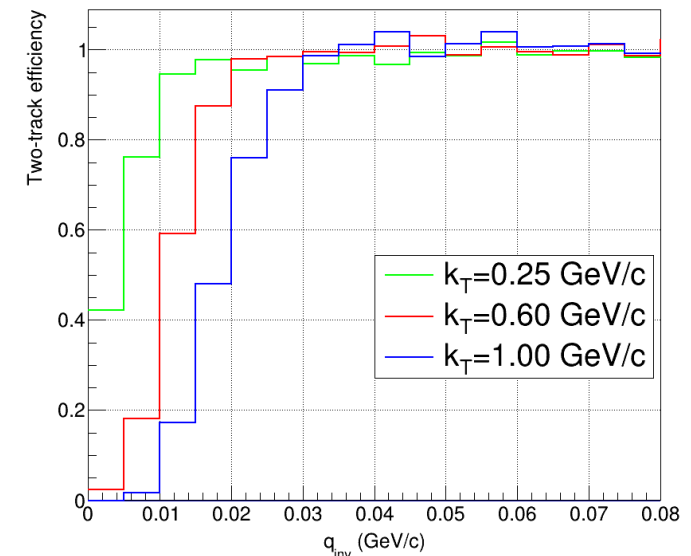
BOX: two  $\pi^+$  with close momenta(w/o Vertex constrain)



BOX: two  $\pi^+$  with close momenta



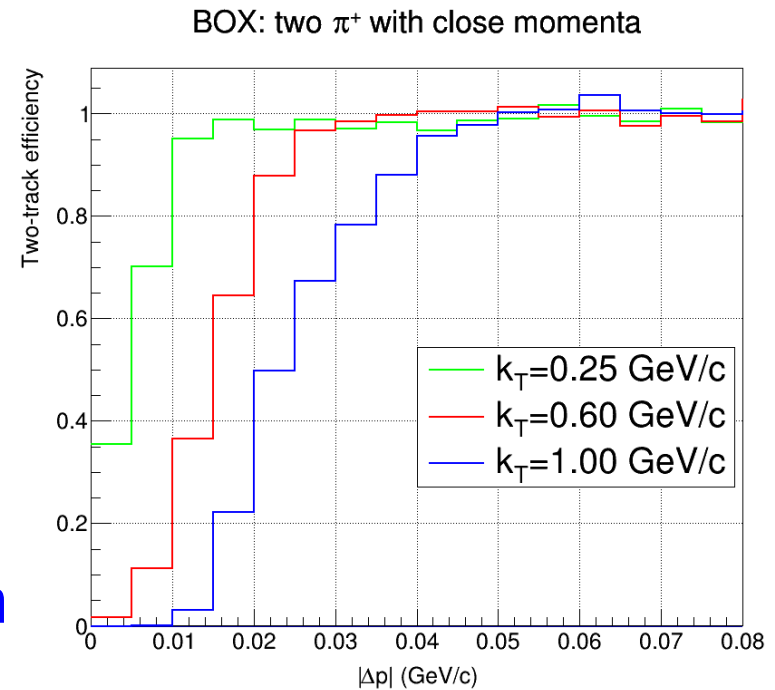
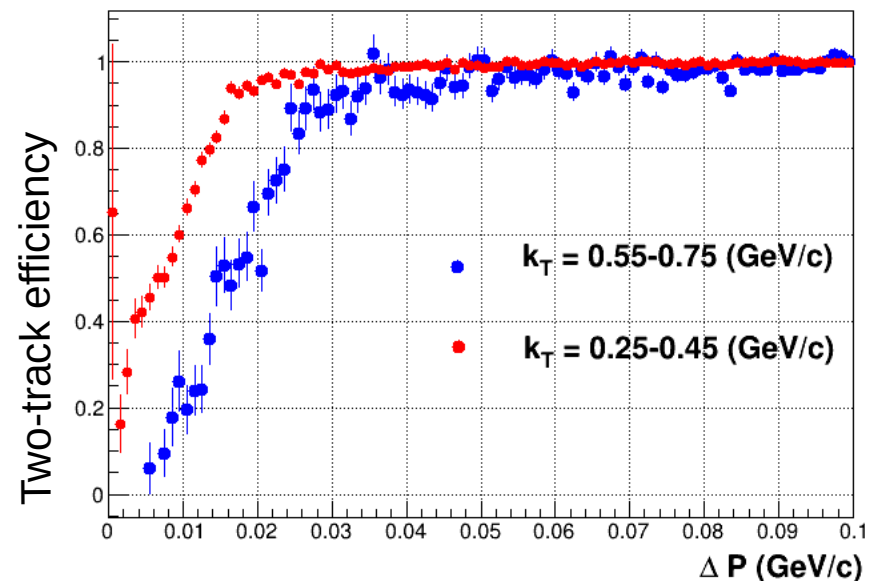
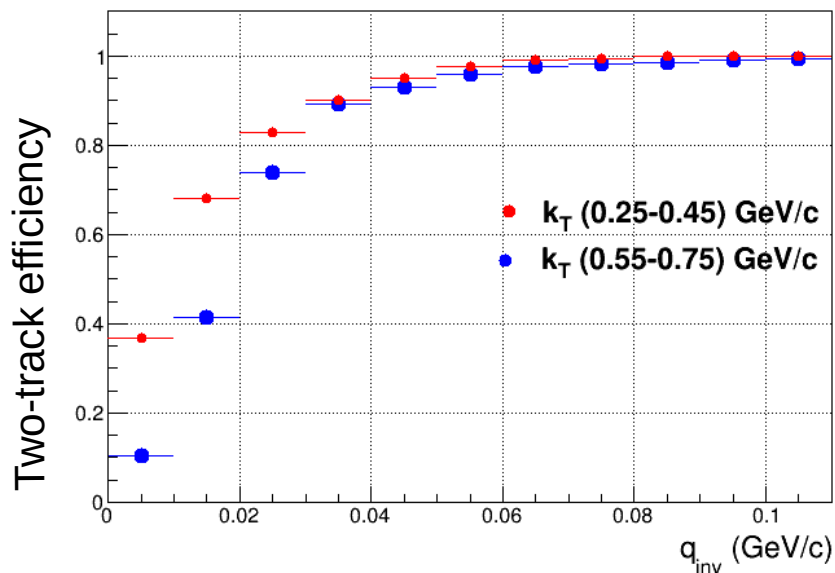
BOX: two  $\pi^+$  with close momenta



# Two-track efficiency in AuAu (BiBi)

- UrQMD generator was used
- Efficiency of two-track reconstruction strongly decrease with pair  $p_T$
- Efficiency of two-track reconstruction only slightly depends on colliding system, but is mainly determined by the efficiency of reconstruction of two isolated tracks

## Efficiency of two-tracks reconstruction



BOX: two  $\pi^+$  with close momenta

# Conclusions

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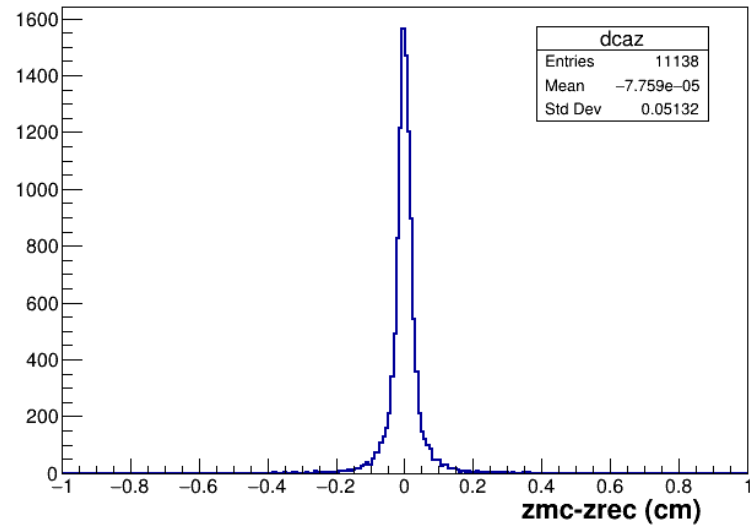
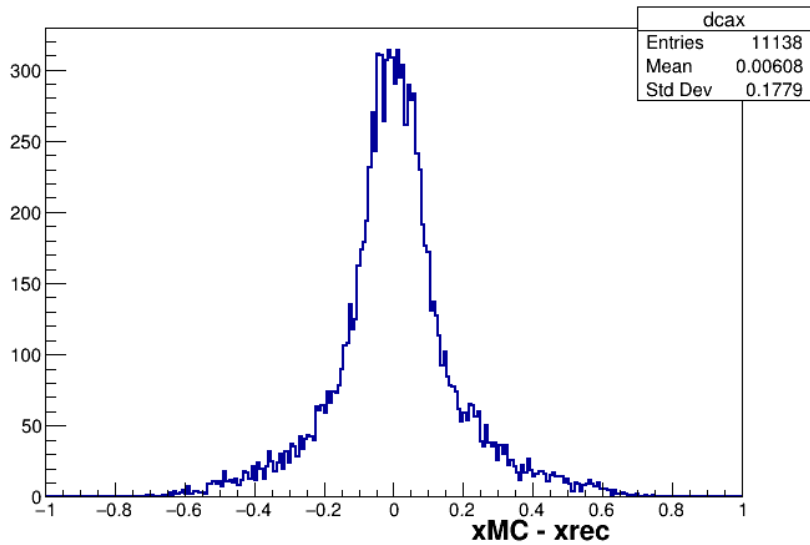
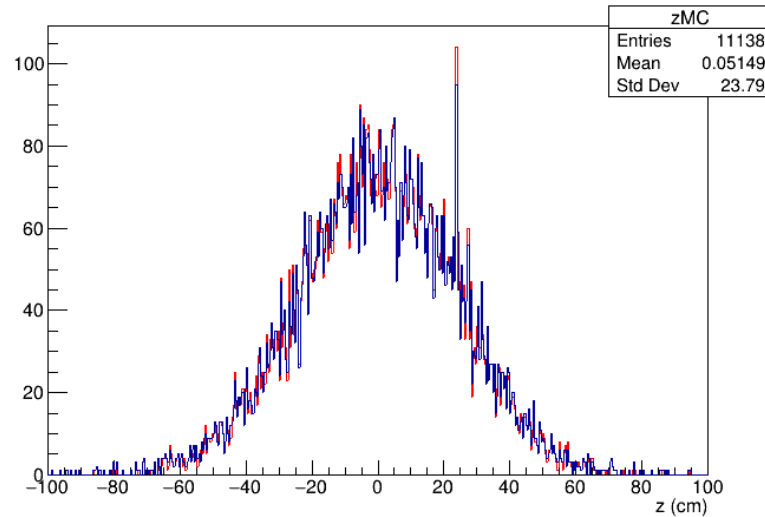
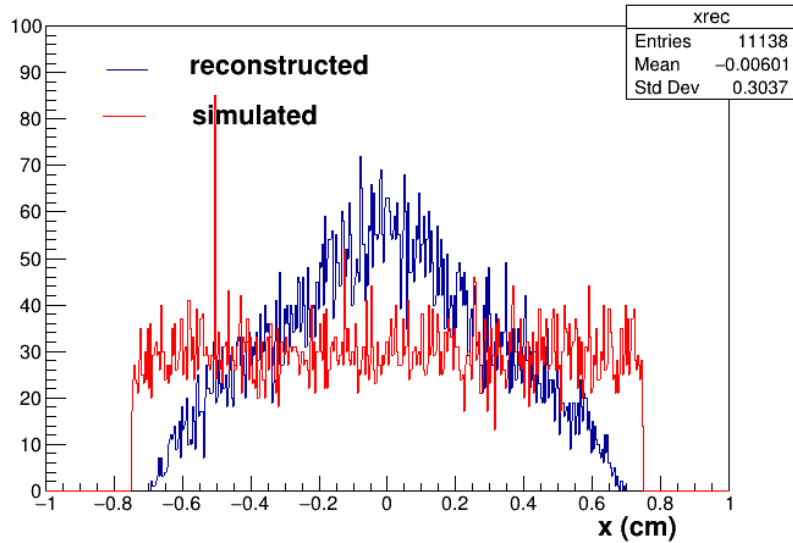
- **Single-track momentum resolution:**
  - Influence on the femtoscopic correlation function depends on pair transverse momentum
  - Strong influence on outward component,  $R_{out}$  (sensitive to the extraction of the particle emission duration)
  - Effect is strong but can be corrected for
- **Misidentification**
  - n-Sigma PID method was successfully tested
  - CF can be corrected by pair purity, determined using single particle purity
- **One track is reconstructed as two (track splitting):**
  - Observed at small relative momentum
- **Two tracks reconstructed as one (track merging):**
  - Strong effect & Depends on  $k_T$  of the pair
  - To study femtoscopic correlation for pions at  $k_T > 0.55$  GeV/c the modification of tracking procedure for close tracks is needed

Communication with tracking group is ongoing many thanks to Alexander Zinchenko !

**MPD provides a good opportunity to study sophisticated femtoscopic observables: e.g. rare particle pairs more sensitive to EoS**

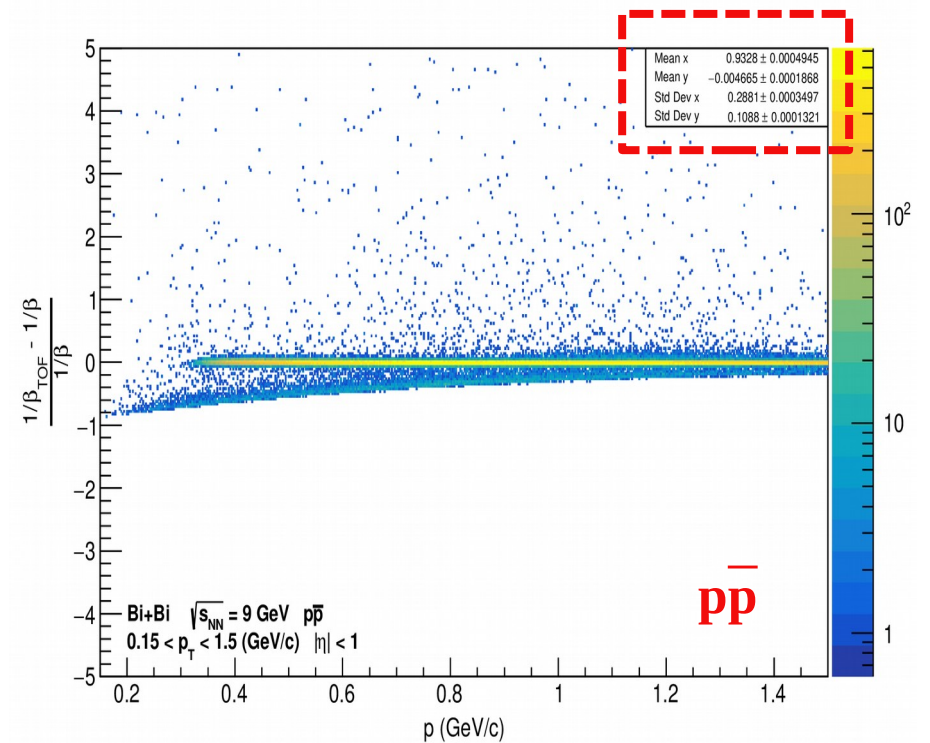
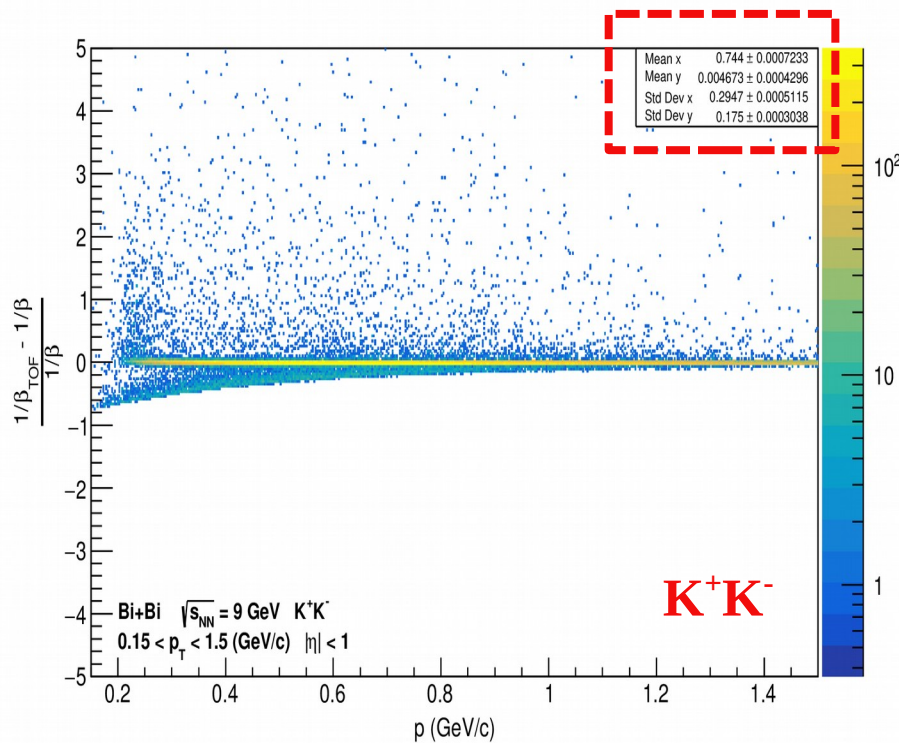
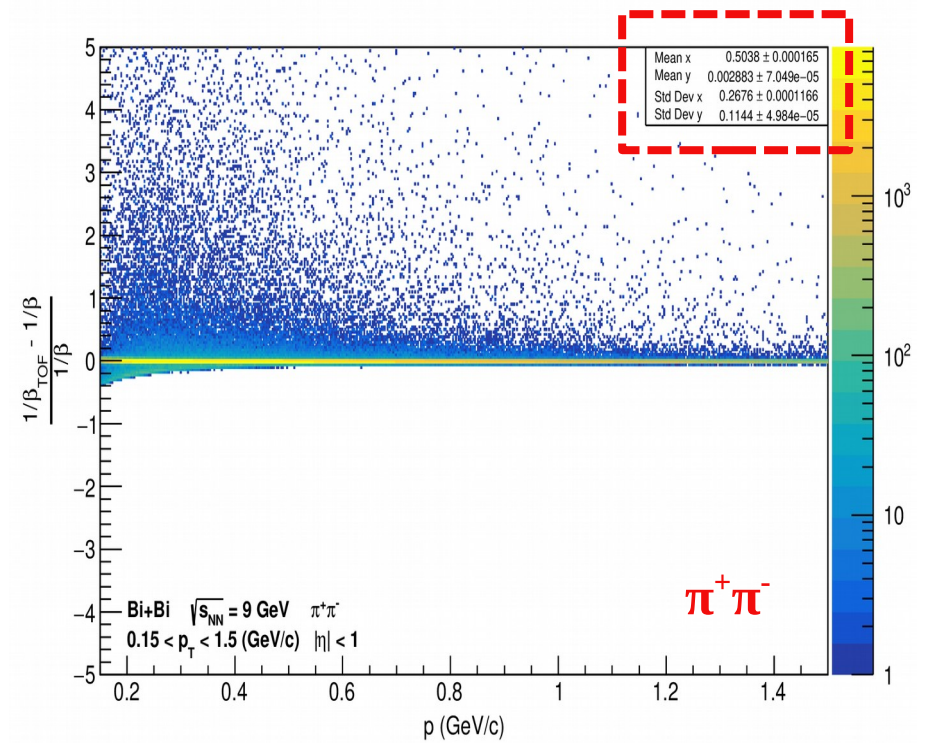
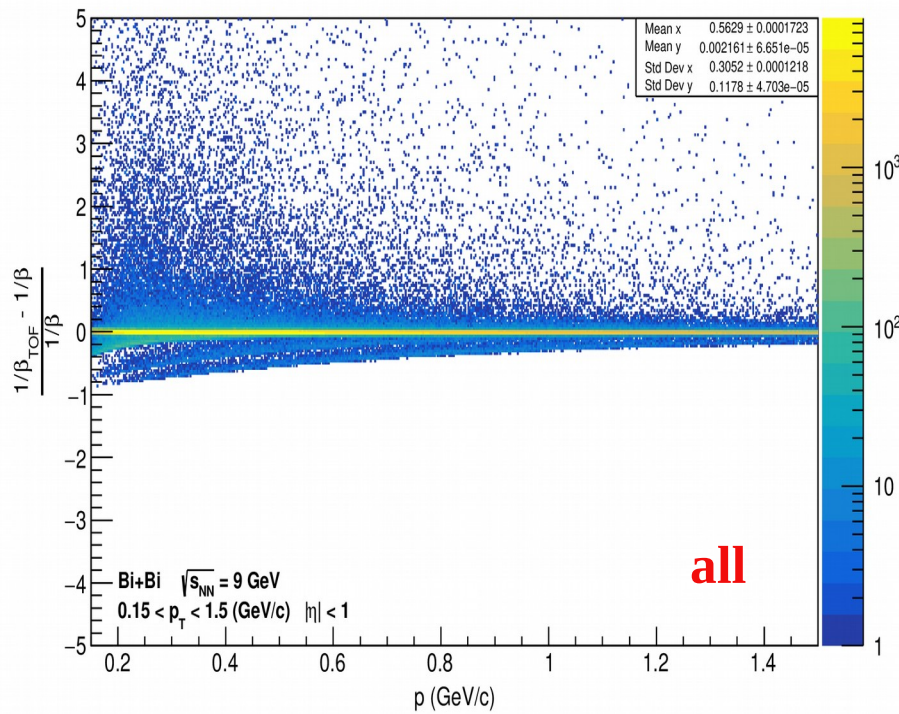
# **Additional slides**

# Vertex {X,Y,Z} – distributions

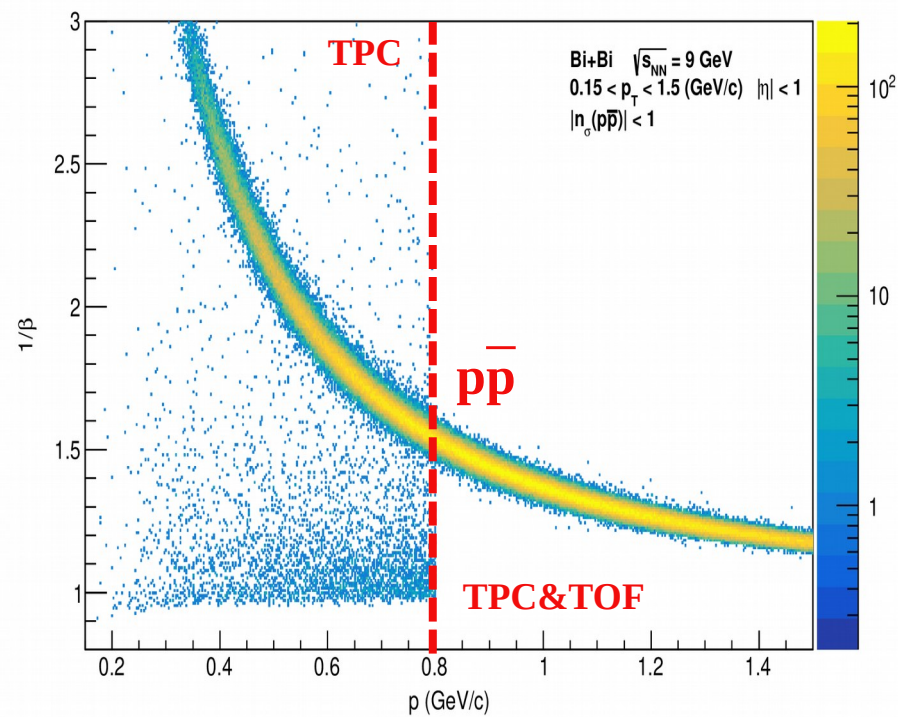
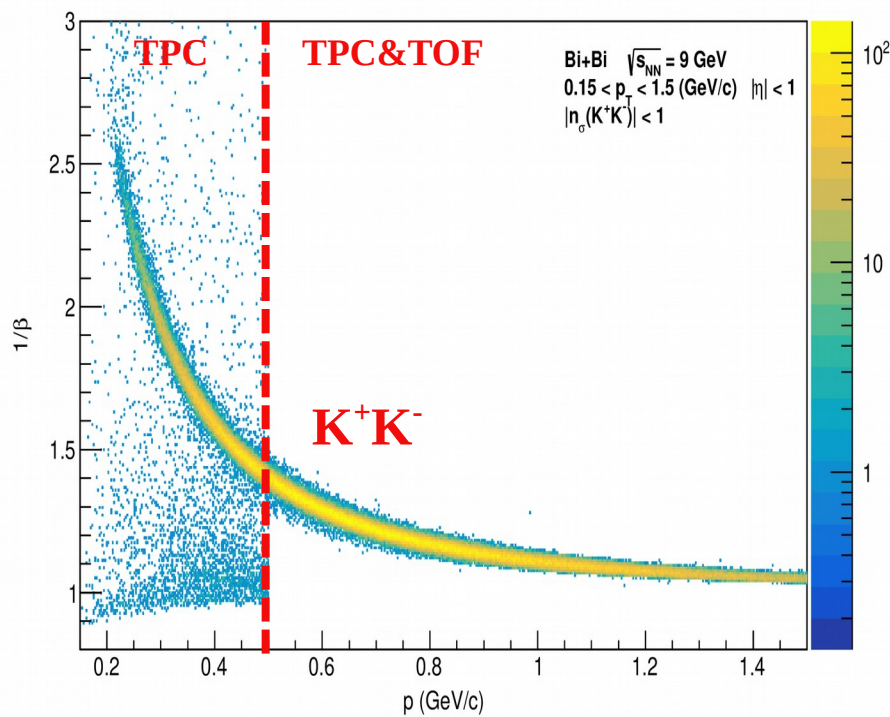
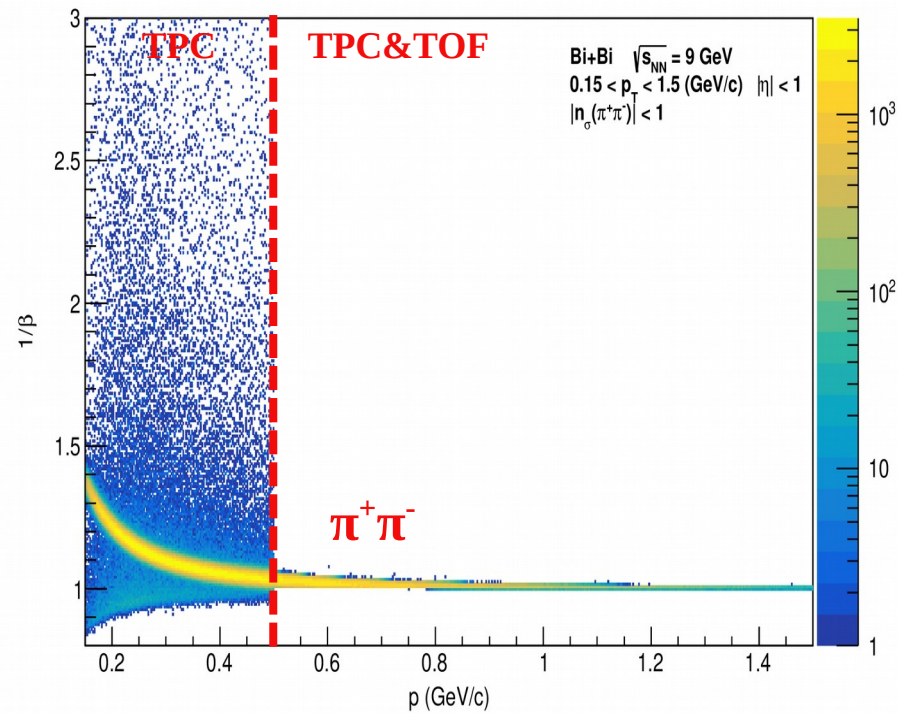
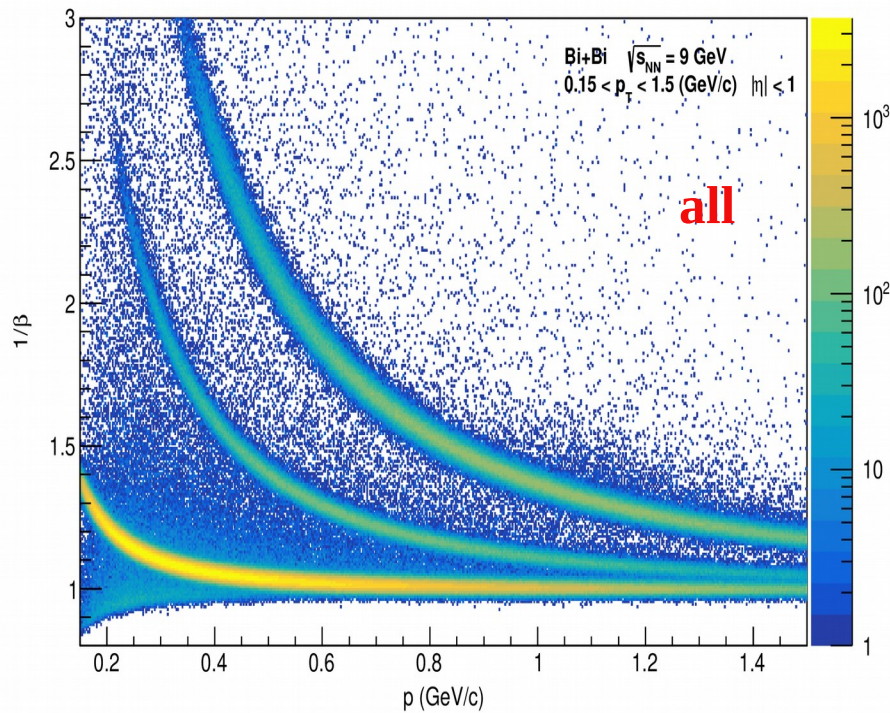


- The same effect is seen for y-coordinate of primary vertex.

# Extracted parameters

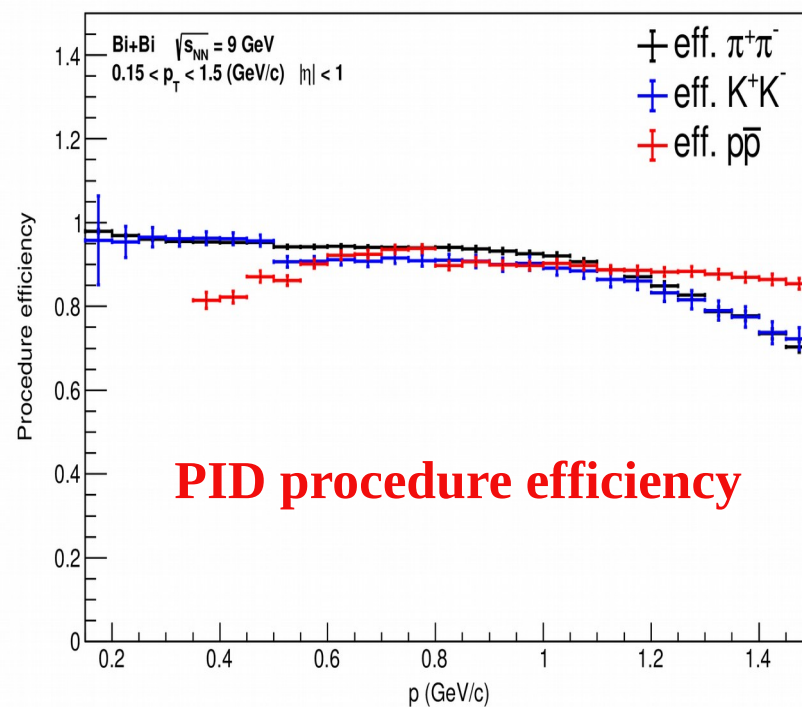
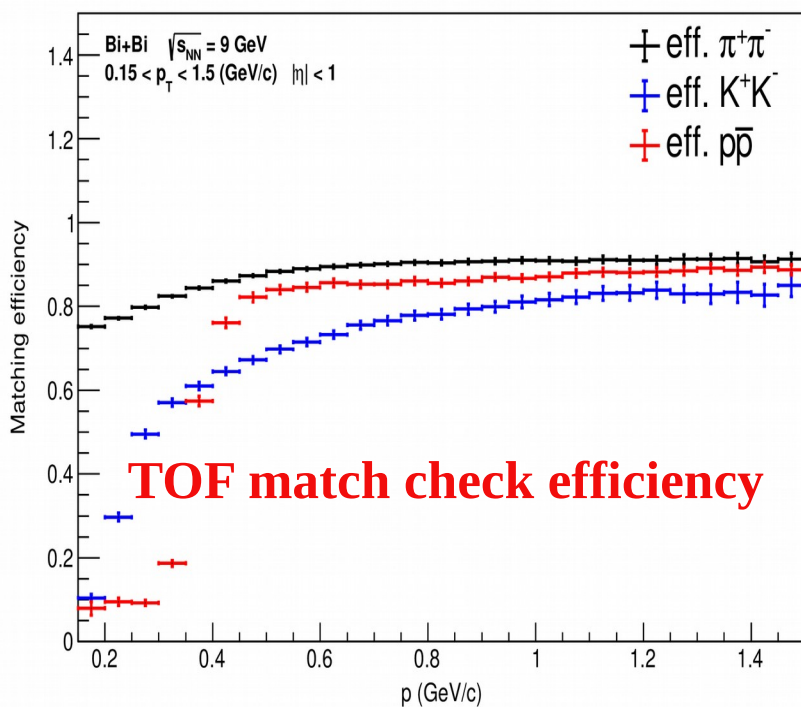
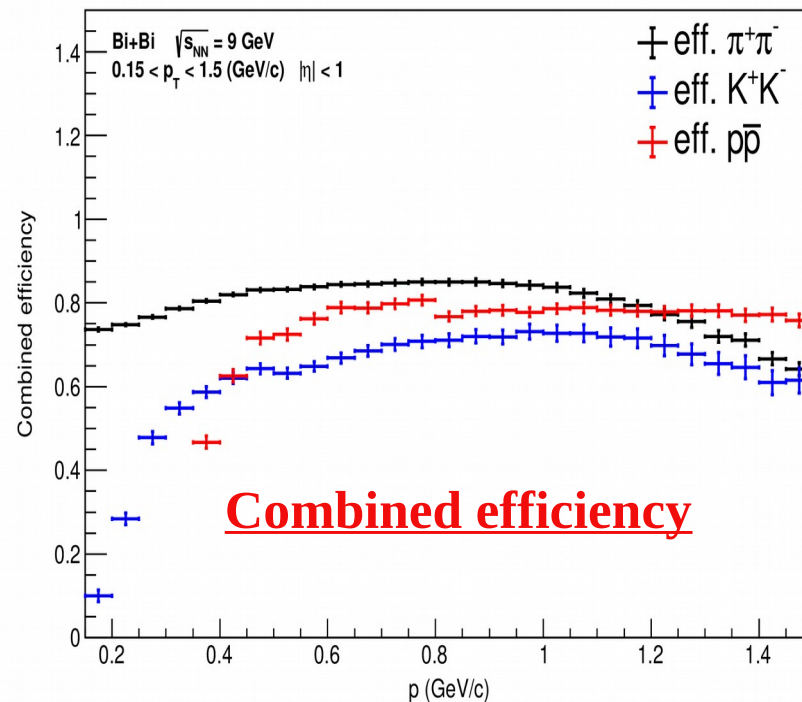






# «Crude» TOF match check

All tracks are required to have a TOF match – significantly decreases combined efficiency at low momenta, not preferred.



# ALICE $\Delta\eta\Delta\phi^*$ min – distributions

Diploma Thesis, “Azimuthally Sensitive Hanbury Brown–Twiss Interferometry measured with the ALICE Experiment”, J.L. Gramling CERN-THESIS-2012-08813/12/20

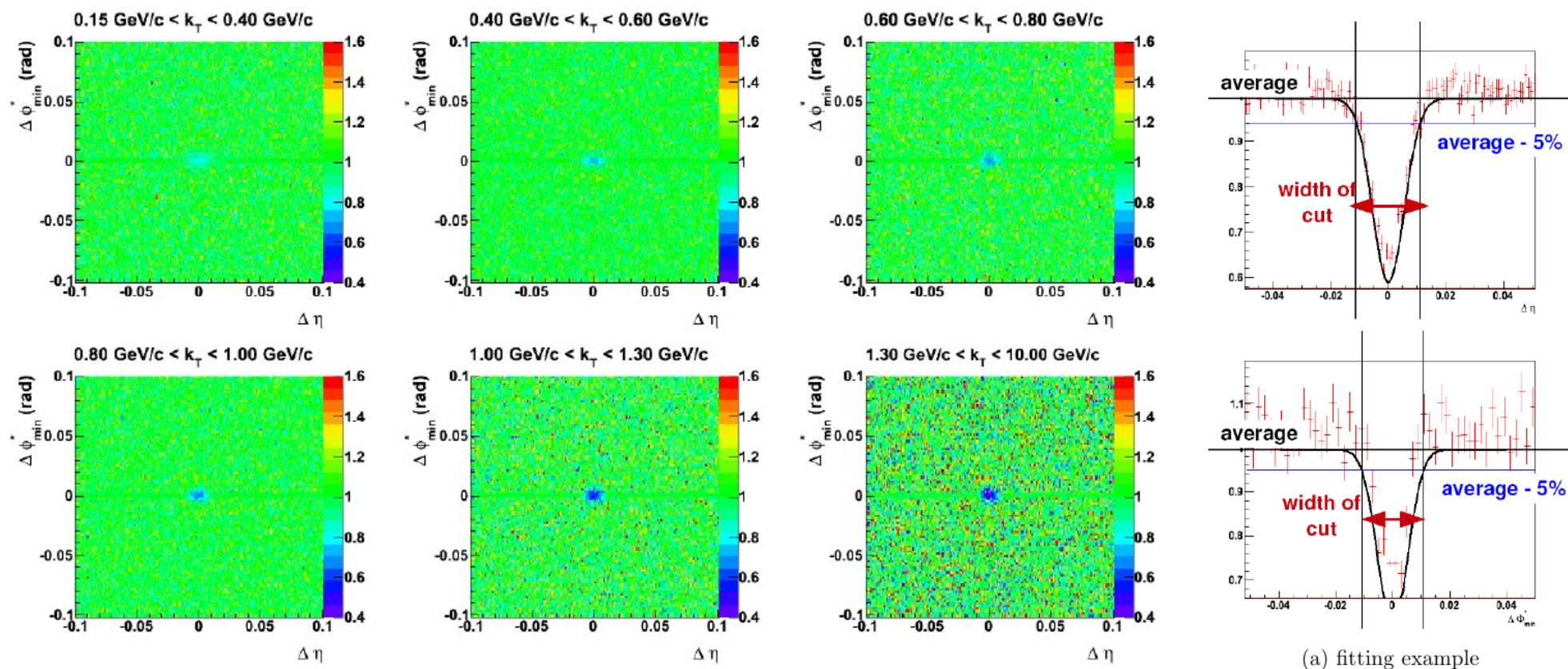


Fig. 7: Two-dimensional ratio in  $\Delta\eta$  and  $\Delta\phi^*_{min,TPC}$ , with the minimum in  $\Delta\phi^*$  determined inside the TPC, TPC-only tracks.

# No TTC : $\Delta\eta\Delta\phi^*$ distributions (TPC+TOF $p>0.5\text{GeV}/c$ )

$\Delta\eta\text{-}\Delta\phi^*$  with MPD reconstructed tracks

$$\Delta\phi^* = \phi_1 - \phi_2 + \arcsin\left(\frac{z \cdot e \cdot B_z \cdot R}{2p_{T1}}\right) - \arcsin\left(\frac{z \cdot e \cdot B_z \cdot R}{2p_{T2}}\right)$$

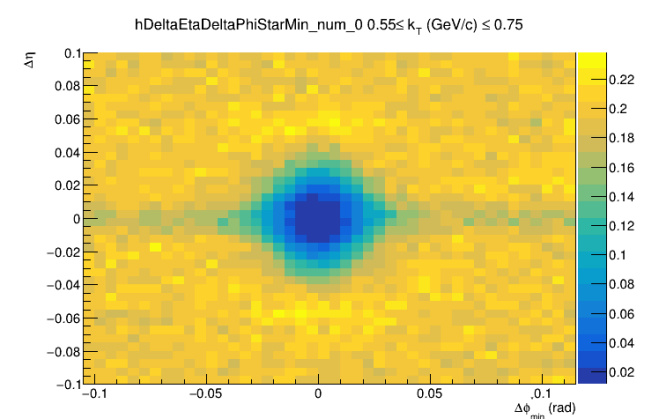
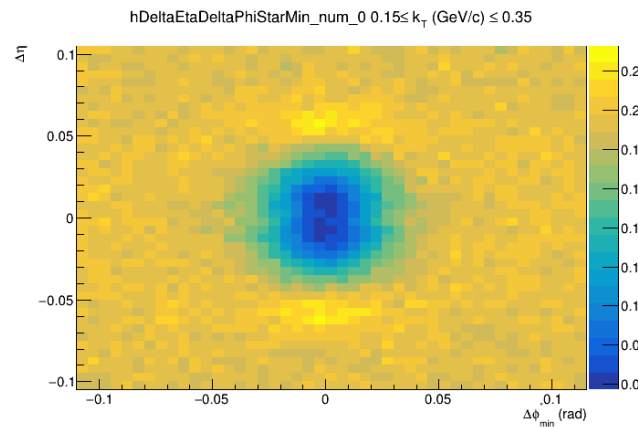
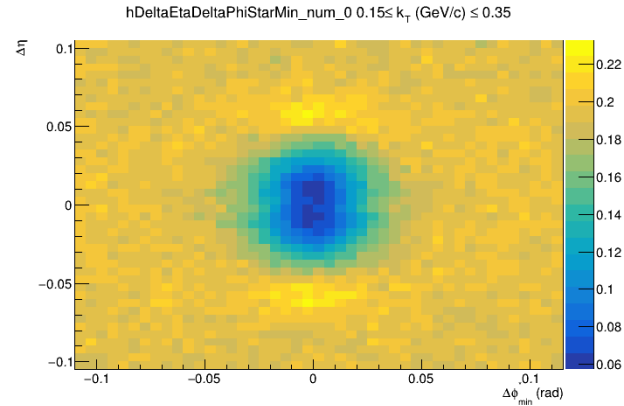
R is a given cylindrical radius

$\phi_{1,2}$  are azimuthal angles of track at reconstructed vertex

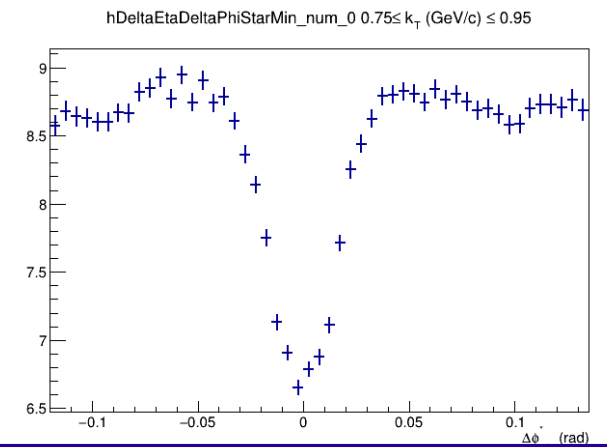
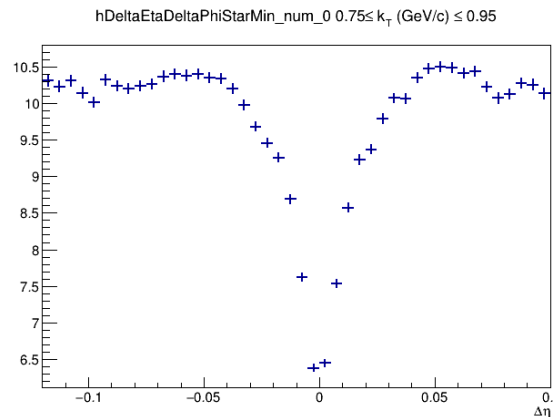
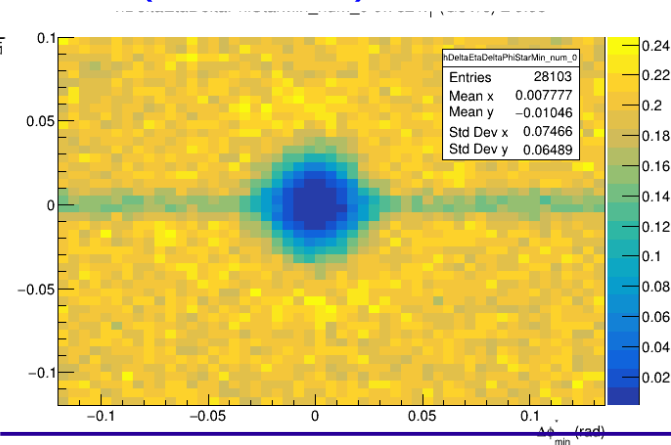
kT (0.15-0.35) GeV/c, R=0.65 m

kT (0.15-0.35) GeV/c

kT (0.55-0.75) GeV/c



kT (0.75-0.95) GeV/c



# No TTC : $\Delta\eta\Delta\phi^*$ distributions (TPC+pdg)

$\Delta\eta\text{-}\Delta\phi^*$  with MPD reconstructed tracks

$$\Delta\phi^* = \phi_1 - \phi_2 + \arcsin\left(\frac{z \cdot e \cdot B_z \cdot R}{2p_{T1}}\right) - \arcsin\left(\frac{z \cdot e \cdot B_z \cdot R}{2p_{T2}}\right)$$

R is a given cylindrical radius

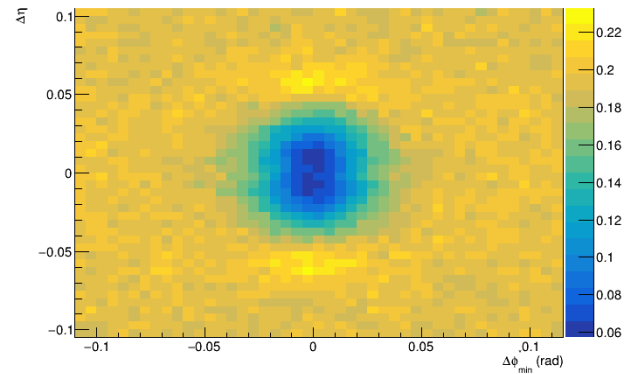
$\phi_{1,2}$  are azimuthal angles of track at reconstructed vertex

kT (0.15-0.35) GeV/c, R=0.65 m

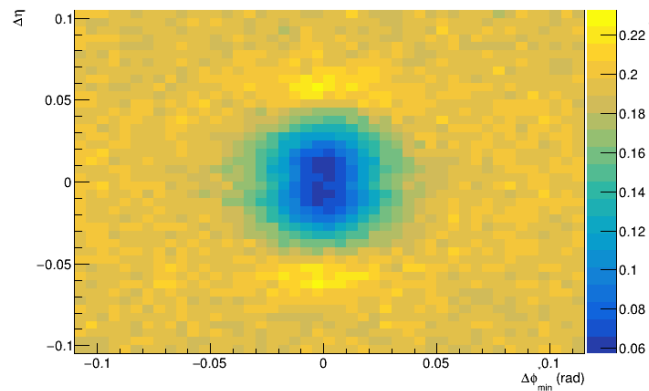
kT (0.15-0.35) GeV/c

kT (0.55-0.75) GeV/c

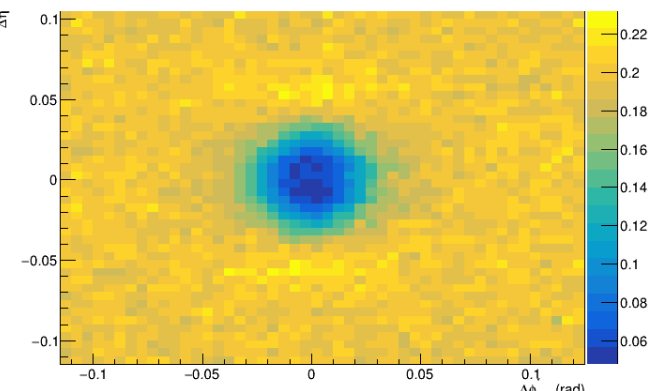
hDeltaEtaDeltaPhiStarMin\_num\_0 0.15 ≤ k<sub>T</sub> (GeV/c) ≤ 0.35



hDeltaEtaDeltaPhiStarMin\_num\_0 0.15 ≤ k<sub>T</sub> (GeV/c) ≤ 0.35

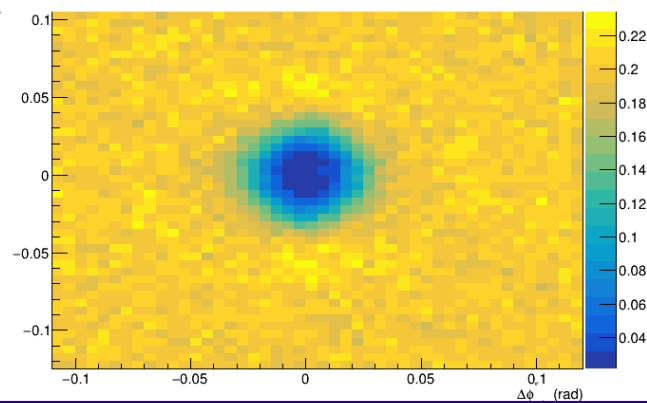


hDeltaEtaDeltaPhiStarMin\_num\_0 0.55 ≤ k<sub>T</sub> (GeV/c) ≤ 0.75

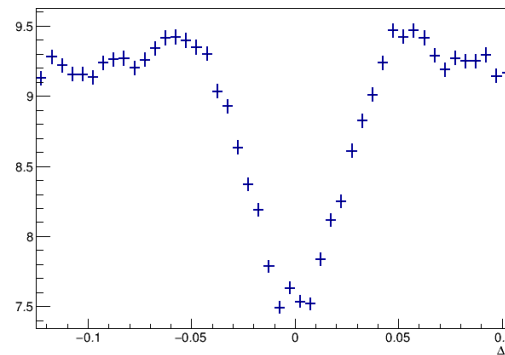


kT (0.75-0.95) GeV/c

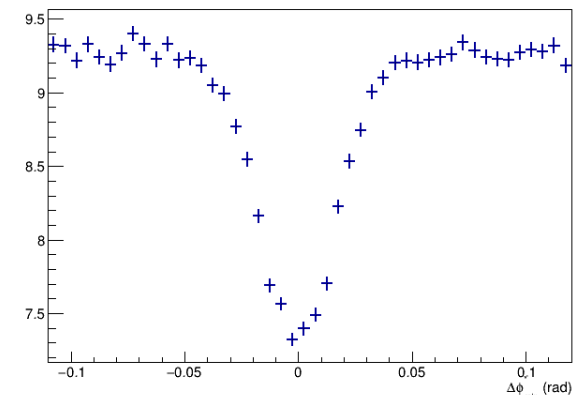
hDeltaEtaDeltaPhiStarMin\_num\_0 0.75 ≤ k<sub>T</sub> (GeV/c) ≤ 0.95



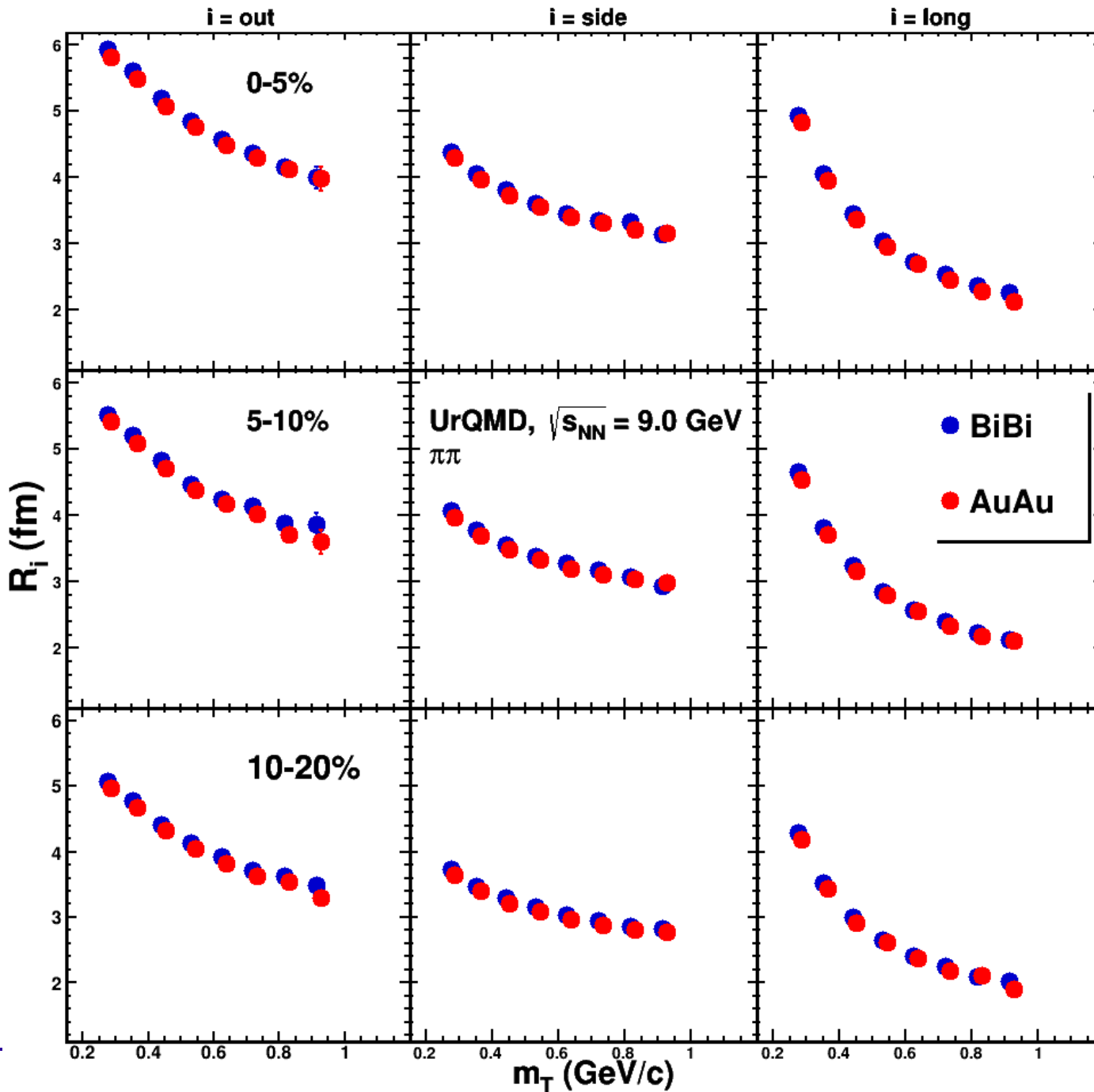
hDeltaEtaDeltaPhiStarMin\_num\_0 0.75 ≤ k<sub>T</sub> (GeV/c) ≤ 0.95



hDeltaEtaDeltaPhiStarMin\_num\_0 0.75 ≤ k<sub>T</sub> (GeV/c) ≤ 0.95



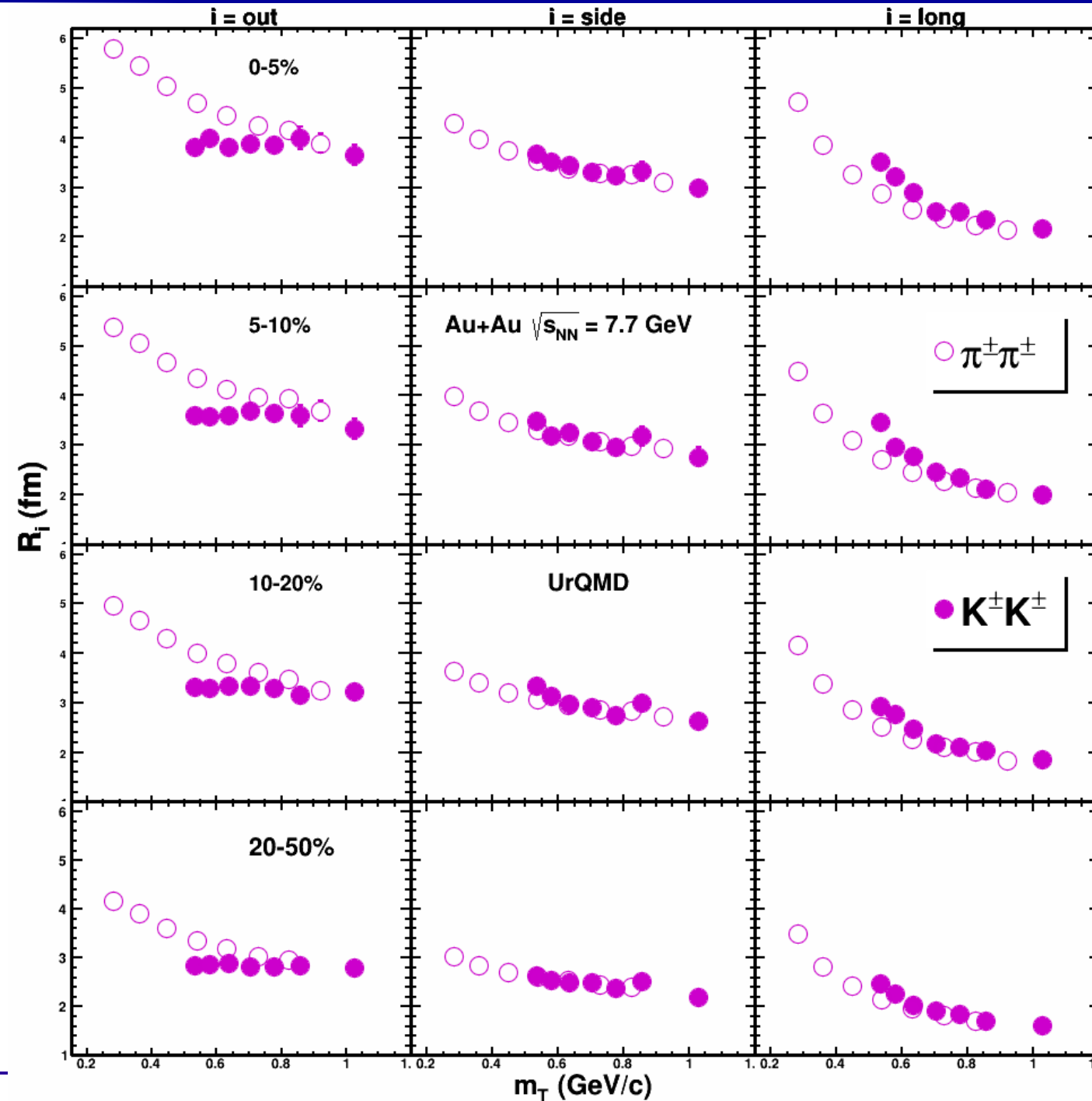
# Comparison of AuAu and BiBi (UrQMD)



● Au+Au, and Bi+Bi at  $\sqrt{s_{NN}} = 9$  GeV

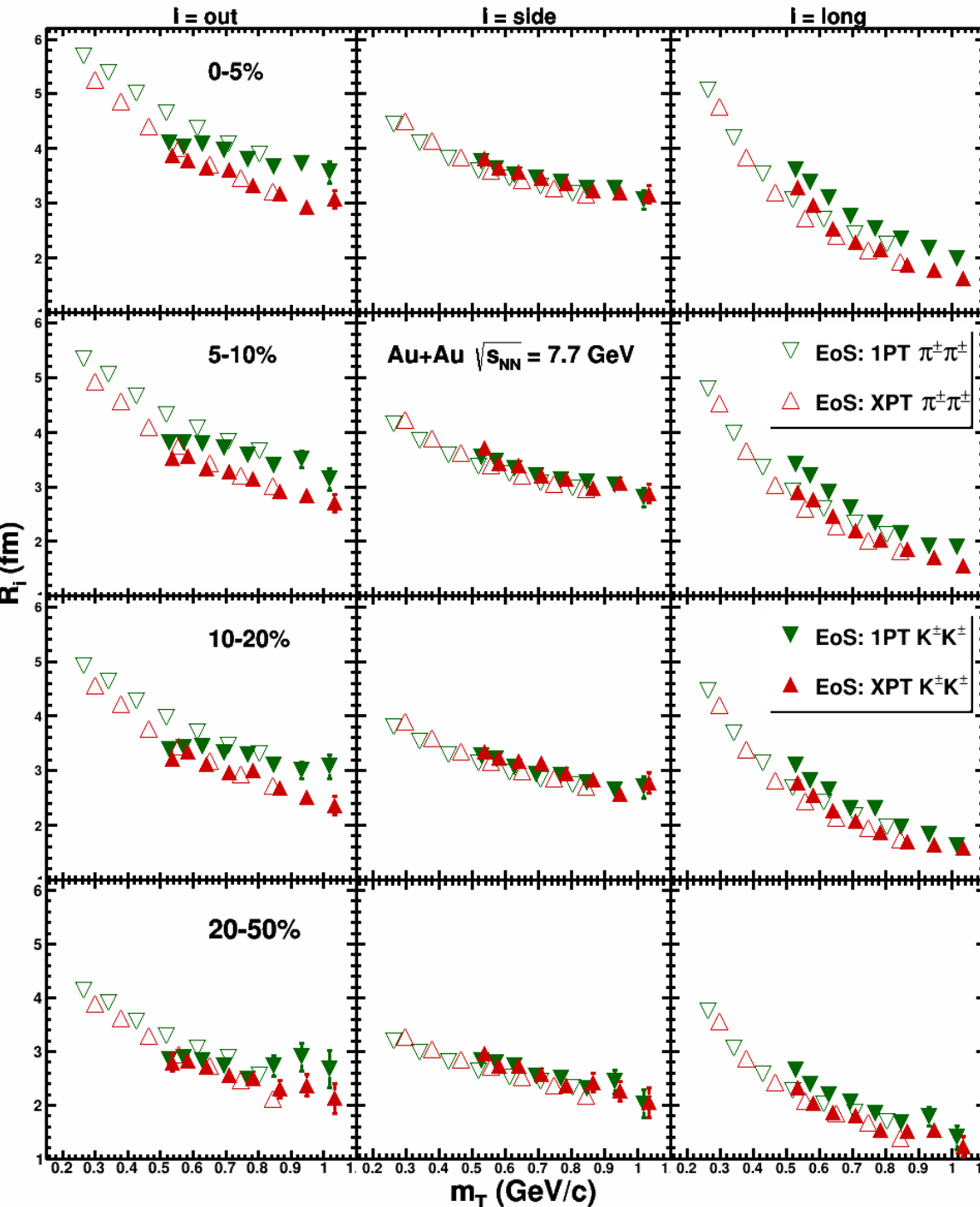
● Pion femtoscopy radii of Bi+Bi are larger than Au+Au ones by  $\sim 2-6\%$

# Pion and kaon radii with UrQMD model



- Au+Au,  $\sqrt{s_{NN}} = 7.7$  GeV
- kaon radii demonstrate almost flat behavior similarly to vHLEE with the 1PT EoS  $\rightarrow$  weak flow
- $R_{\text{long}}$  kaon radii are larger than pion ones similarly to experiment (LHC & RHIC)
- The similar trend is observed for AuAu 11.5 GeV

# Pion and kaon radii with vHLE model

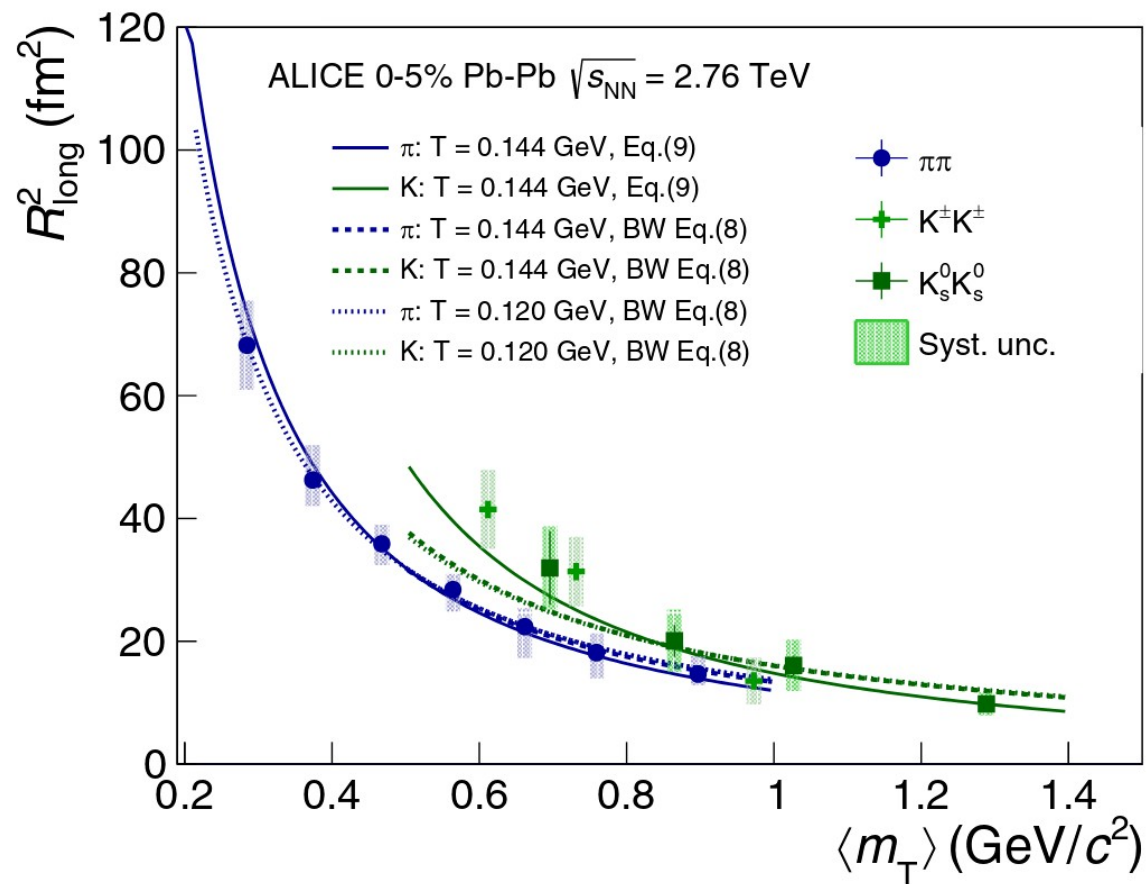


- Au+Au,  $\sqrt{s_{NN}} = 7.7$  GeV
- Approximate  $m_T$  scaling for  $R_{\text{side}}$
- Similarly to pions : kaon radii decrease with  $m_T \rightarrow$  radial flow ;
- for 1PT EoS almost flat dependence  $R_{\text{out}}(m_T)$  is observed  $\rightarrow$  weaker flow
- $R_{\text{out, long}}(1PT) > R_{\text{out, long}}(XPT)$
- $R_{\text{long}}$  kaon radii for XPT  $>$   $R_{\text{long}}$  pion similarly to experiment (LHC & RHIC)
- Very different predictions of vHLE model for different EoS  $\rightarrow$  importance to study heavier than pions particles  $\rightarrow$  kaons
- The similar trend is observed for AuAu 11.5 GeV



# Emission delay in ALICE data

- ALICE kaon data in hydro-based parameterization: kaons emitted on average later than pions.
- It comes from rescattering via  $K^*$  resonance
- $R_{\text{long}}^2 \sim \tau / \sqrt{m_T}$
- Measured values:  $\tau_{\pi} = 9.5 \pm 0.2$  fm/c  
 $\tau_K = 11.6 \pm 0.1$  fm/c



# Single-track momentum resolution in MPD

