

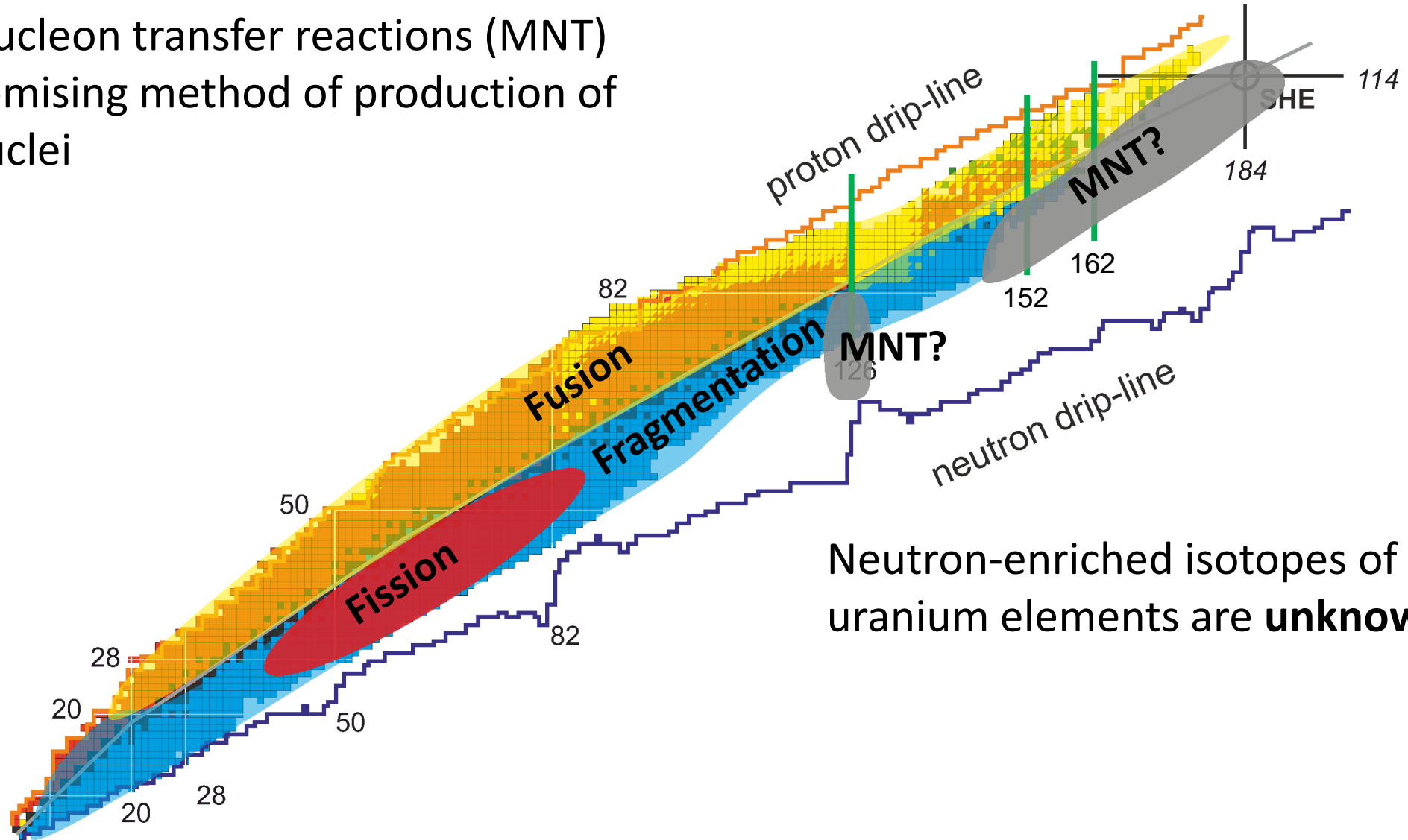
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**Multinucleon transfer reactions as
a method of production of
neutron-enriched isotopes of
transuranium elements**

Vyacheslav Saiko and Alexander Karpov

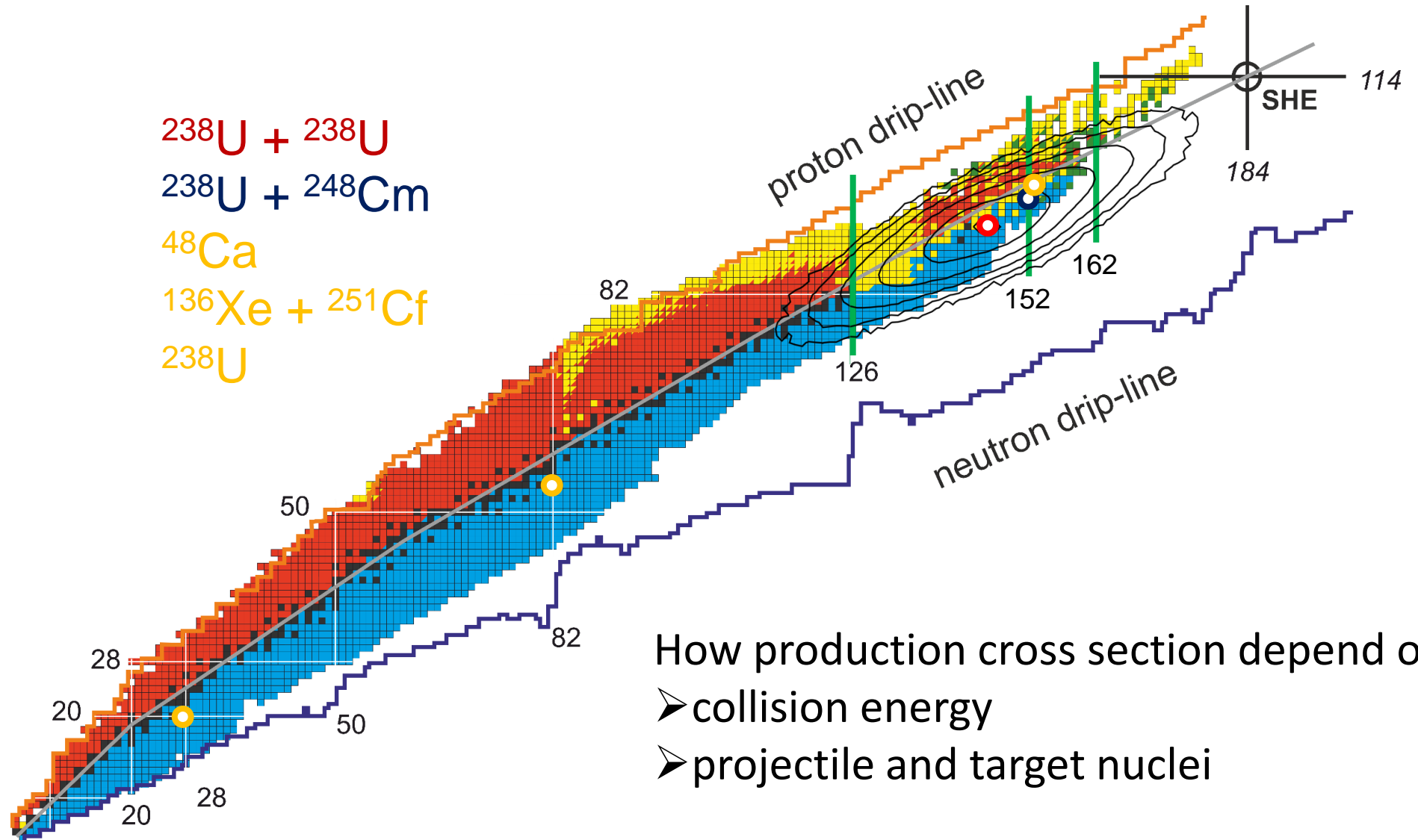
Methods of production of new nuclei

Multinucleon transfer reactions (MNT) is a promising method of production of new nuclei



Neutron-enriched isotopes of trans-uranium elements are **unknown**

MNT reactions with actinides

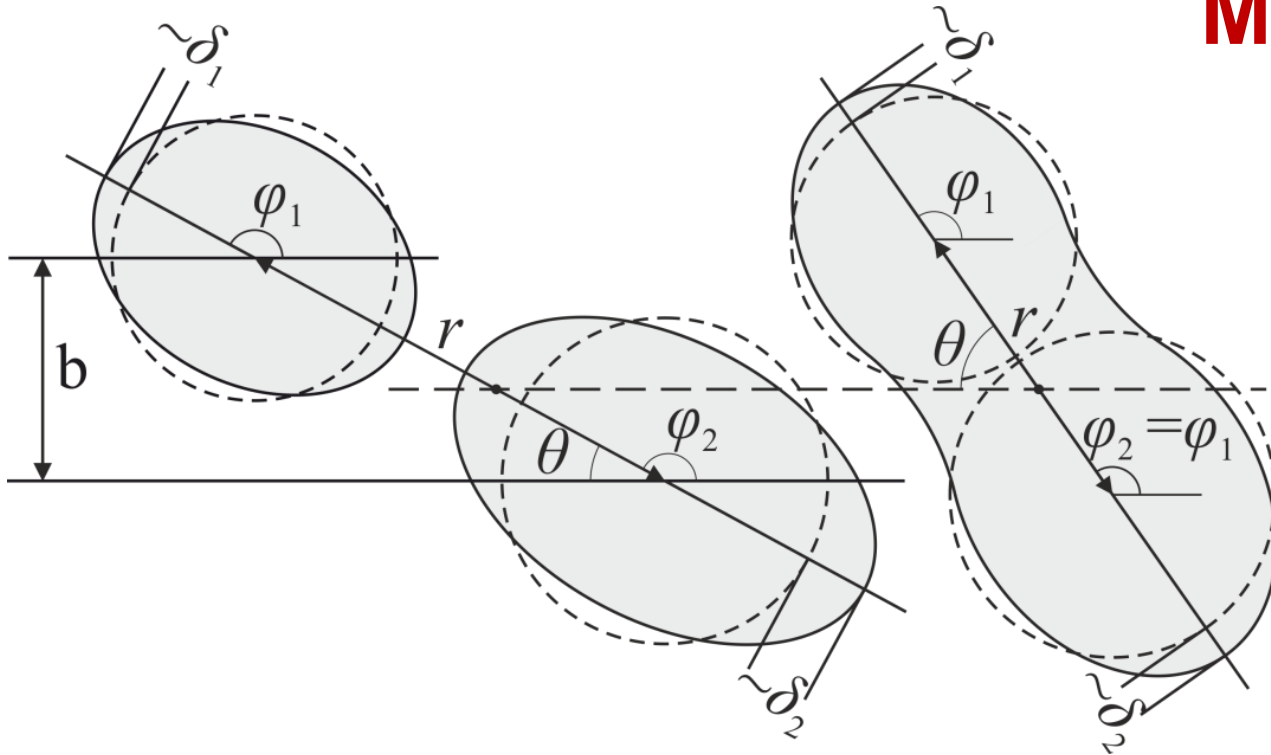


How production cross section depend on

- collision energy
- projectile and target nuclei

Model

A.V. Karpov and V.V. Saiko,
Phys. Rev. C 96, 024618 (2017)
Phys. Rev. C 99, 014613 (2019)



r – distance between centers of nuclei

$\delta_{1,2}$ – ellipsoidal deformations

η_A – mass asymmetry

η_Z – charge asymmetry

θ – angle between symmetry axis and beam direction

$\varphi_{1,2}$ – angles of rotation of nuclei in the reaction plane

$$\eta_A = \frac{A_1 - A_2}{A_{CN}} \quad \eta_Z = \frac{Z_1 - Z_2}{Z_{CN}}$$

$$\begin{aligned} \dot{q}_i &= \mu_{ij} p_j, \\ \dot{p}_i &= T \left(\frac{\partial S}{\partial q_i} \right)_{E_{tot}} - \sum_{j,k} \gamma_{ij} \mu_{jk} p_k + \sum_j \theta_{ij} \xi_j \end{aligned} \quad \begin{array}{l} \text{system of} \\ \text{Langevin equations} \end{array}$$

driving, friction and random forces

$\mu_{ij} = m_{ij}^{-1}$ – mass tensor

γ_{ij} – dissipation tensor

θ_{ij} – amplitude of random force

ξ_i – random value

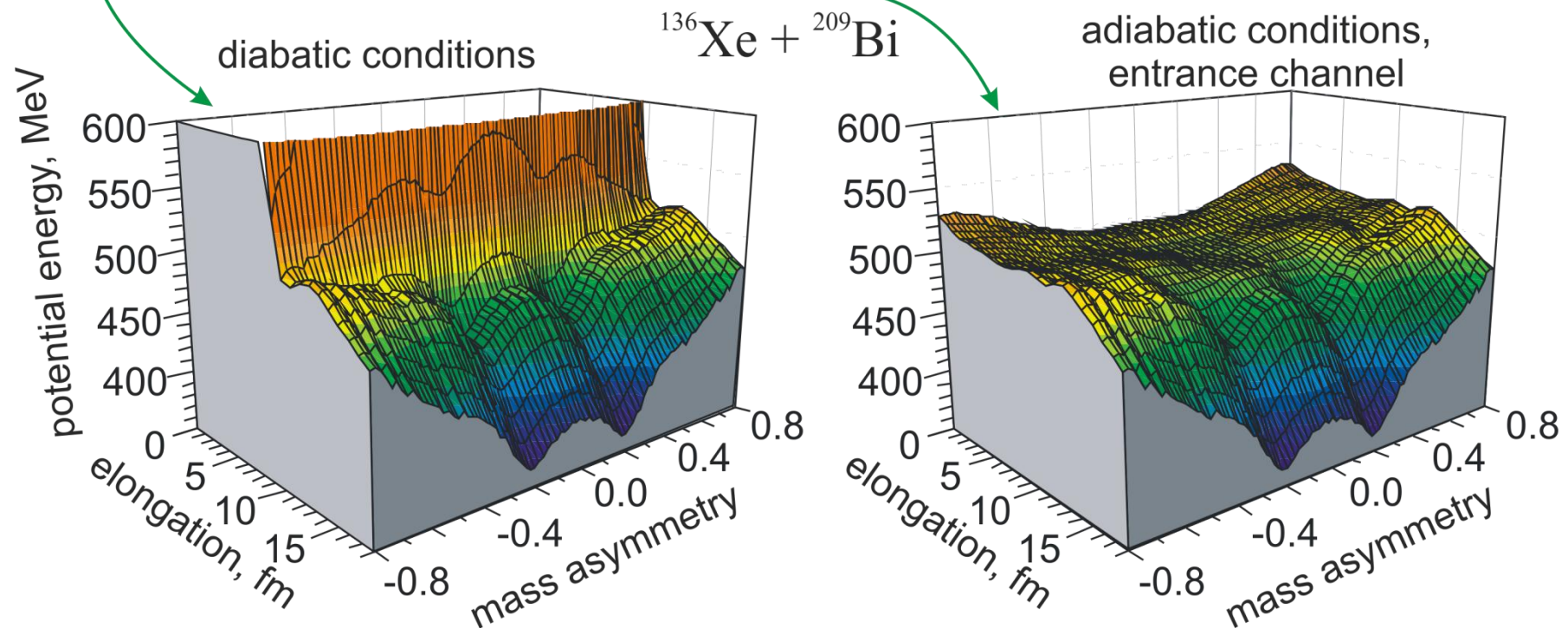
Potential energy

V. Zagrebaev, A. Karpov et al., Phys. Part. Nucl. 38, 469 (2007)

<http://nr.v.jinr.ru>

$$V(t) = V_{\text{diab}} \exp\left(-\frac{t}{\tau_{\text{DA}}}\right) + V_{\text{adiab}}(t) \left(1 - \exp\left(-\frac{t}{\tau_{\text{DA}}}\right)\right), \quad \tau_{\text{DA}} = 10^{-22} \text{ s}$$

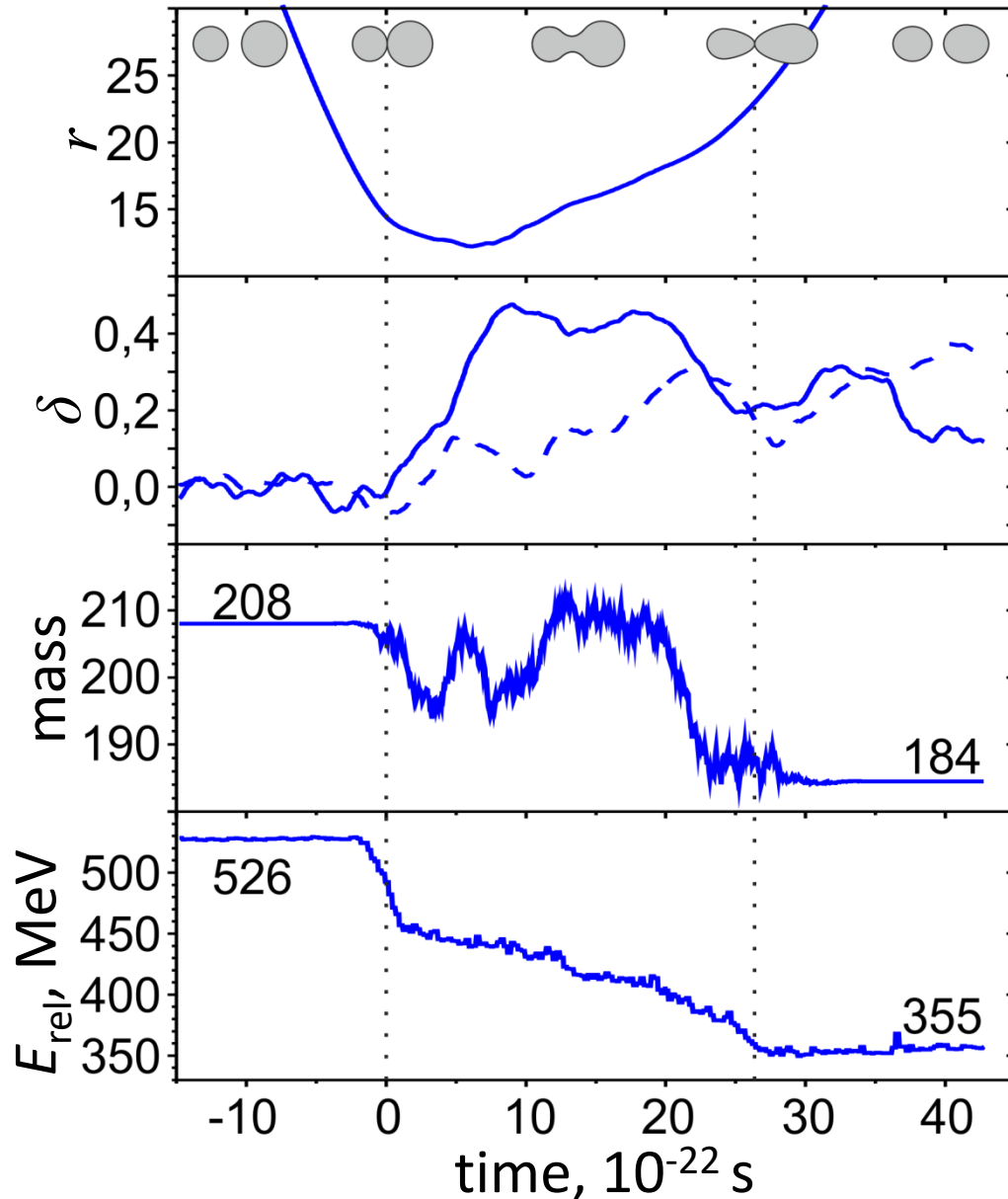
$$V_{\text{adiab}}(t) = V_{\text{adiab}}^{\text{in}} \exp\left(-\frac{t}{\tau_{\varepsilon}}\right) + V_{\text{adiab}}^{\text{out}} \left(1 - \exp\left(-\frac{t}{\tau_{\varepsilon}}\right)\right), \quad \tau_{\varepsilon} = 10^{-20} \text{ s}$$



Model

*A.V. Karpov and V.V. Saiko,
Phys. Rev. C 96, 024618 (2017)
Phys. Rev. C 99, 014613 (2019)*

a collision of $^{136}\text{Xe} + ^{208}\text{Pb}$



each **trajectory** of a collision provides:

- Z and A of fragments,
- excitation energy,
- scattering angle,
- reaction time,
- kinetic energy,
- ...

Final fragments are simulated by means of

- **statistical model** of decay of heavy excited nuclei,

- **GEF code**

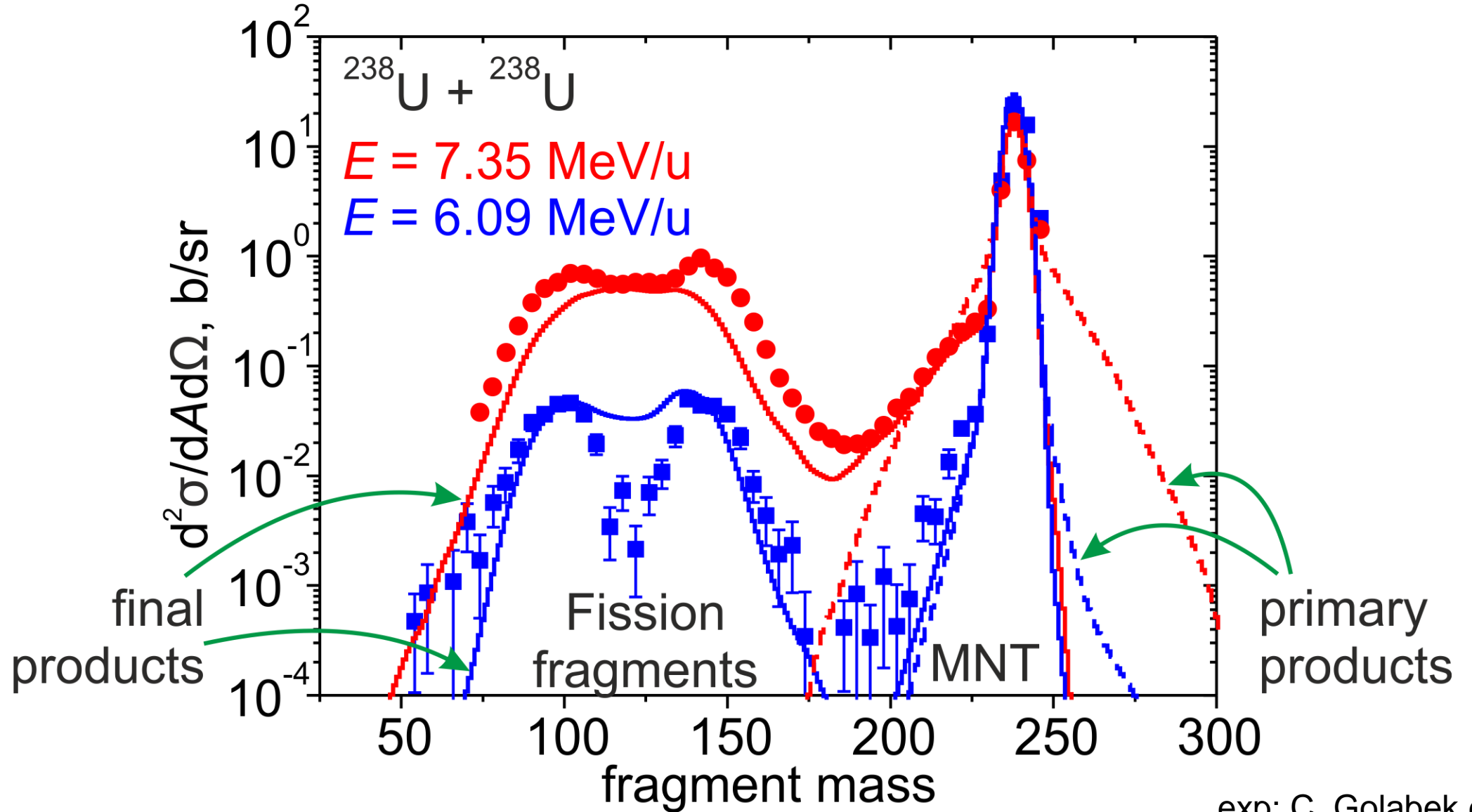
<http://nrv.jinr.ru>

<http://www.khschmidts-nuclear-web.eu/GEF.html>

differential reaction cross section:

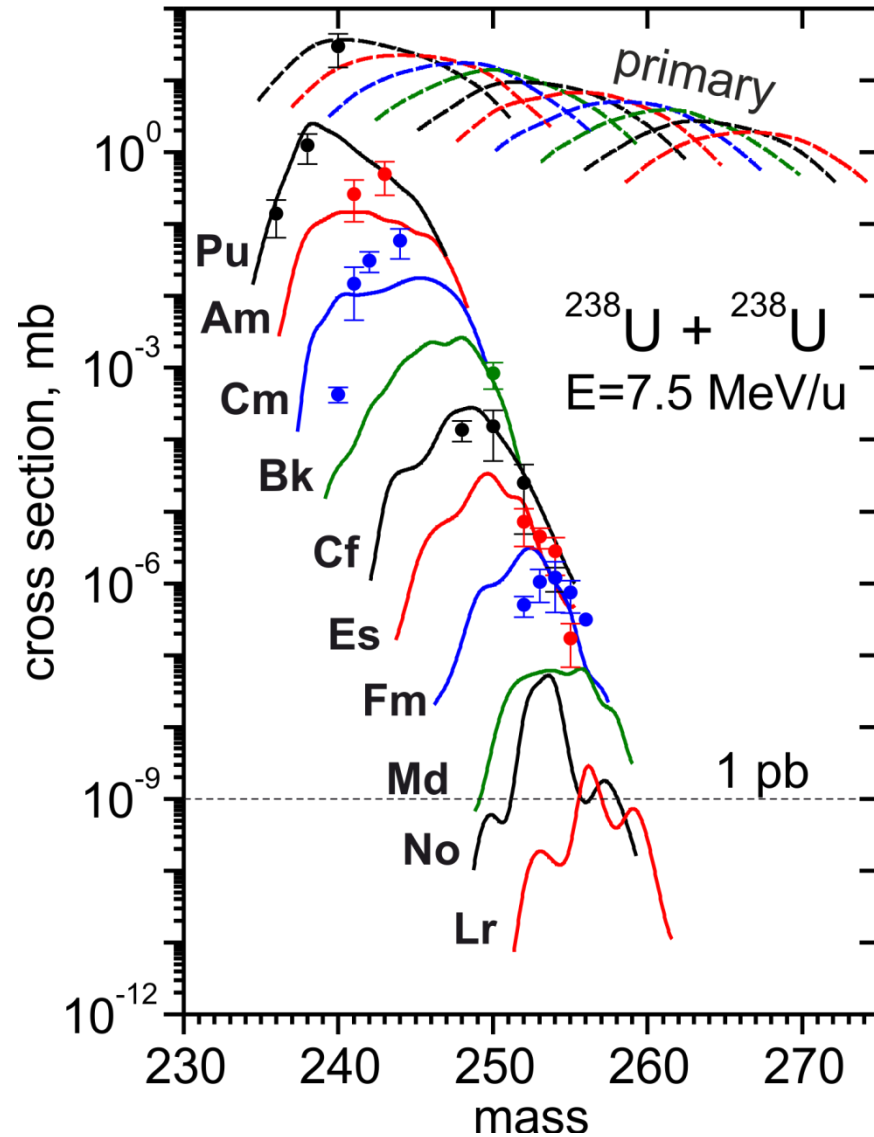
$$\frac{d^4\sigma}{dZdAd\Omega dE}(Z, A, E, \theta) = \int_0^{b_{\max}} \frac{\Delta N(b, Z, A, E, \theta) b db}{N_{\text{tot}}(b) \Delta Z \Delta A \sin\theta \Delta\theta \Delta E}$$

$^{238}\text{U} + ^{238}\text{U}$ reaction



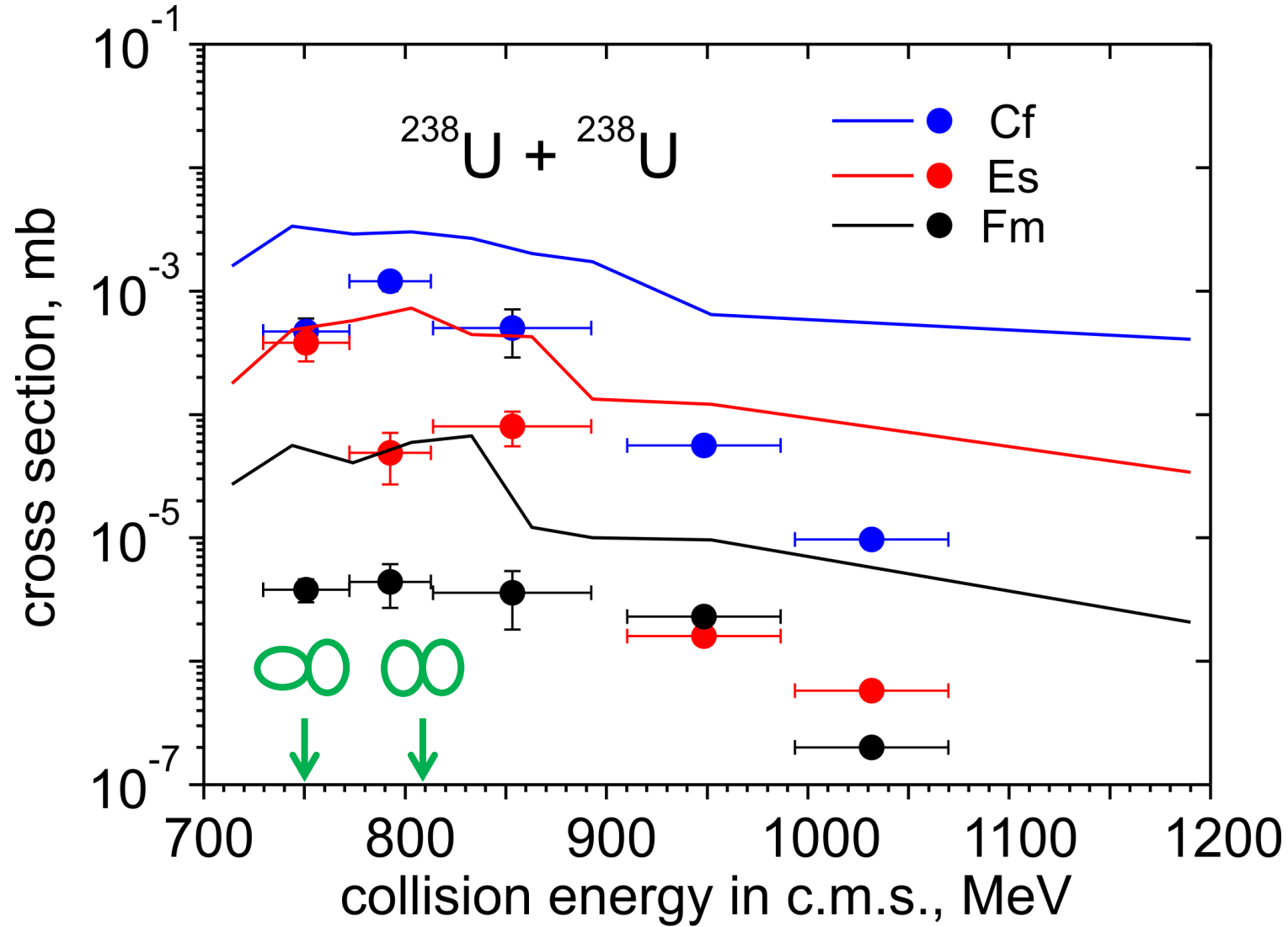
exp: C. Golabek et al.,
Eur. Phys. Jour. A 43, 251 (2010)

$^{238}\text{U} + ^{238}\text{U}$ reaction



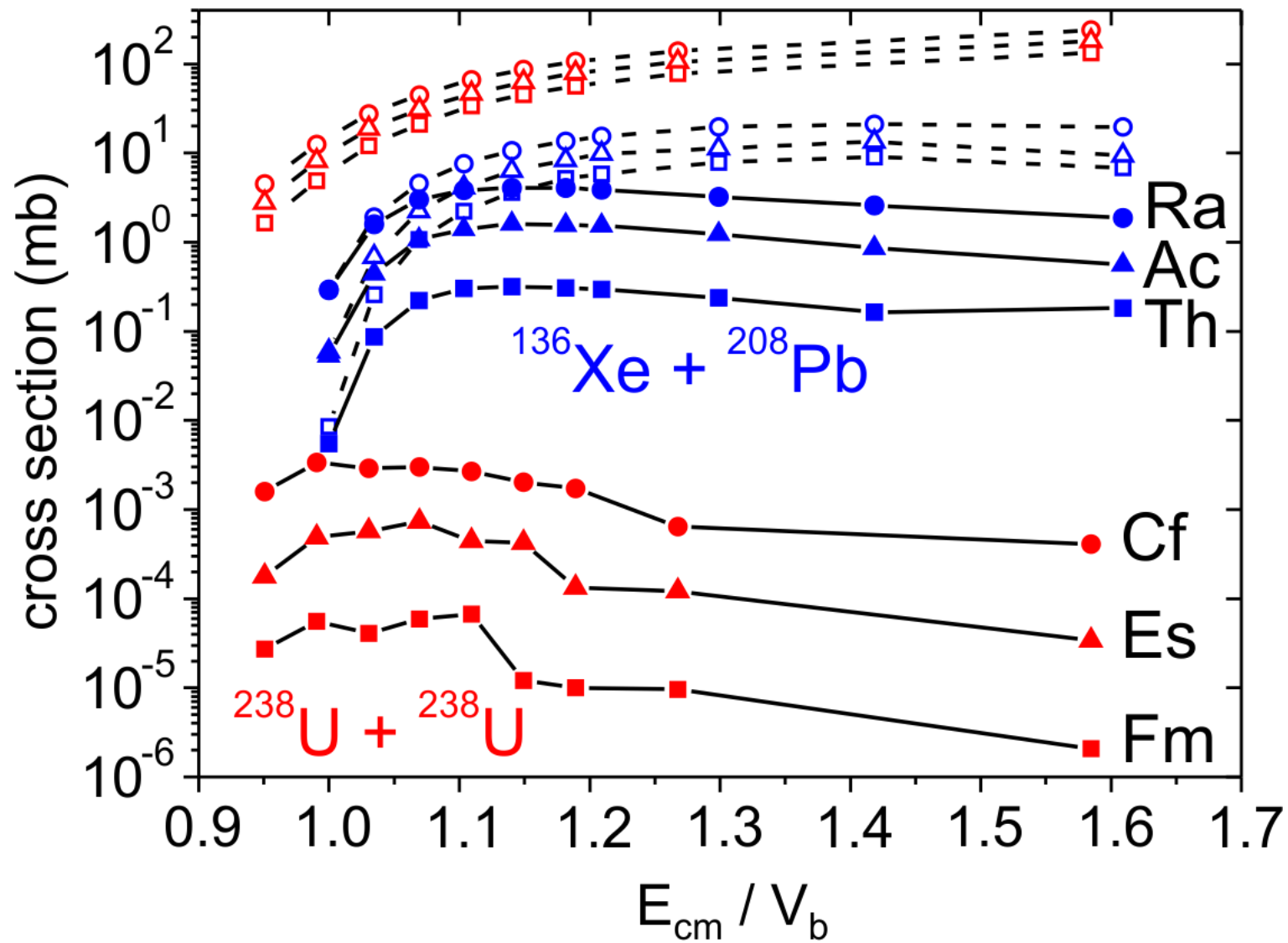
exp.: M. Schadel et al., Phys. Rev. Lett. 41, 469 (1978)

Optimal energy *for heavier elements*

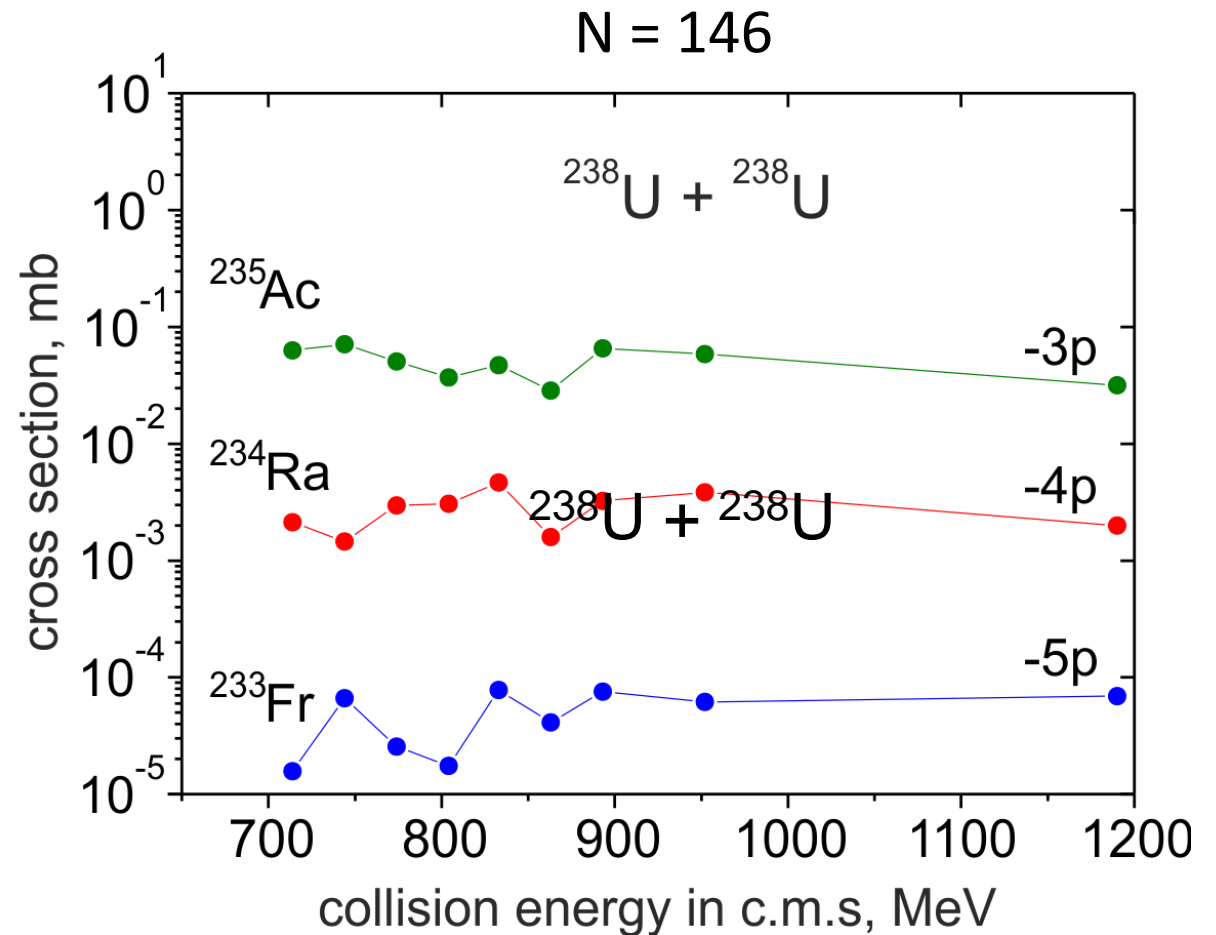
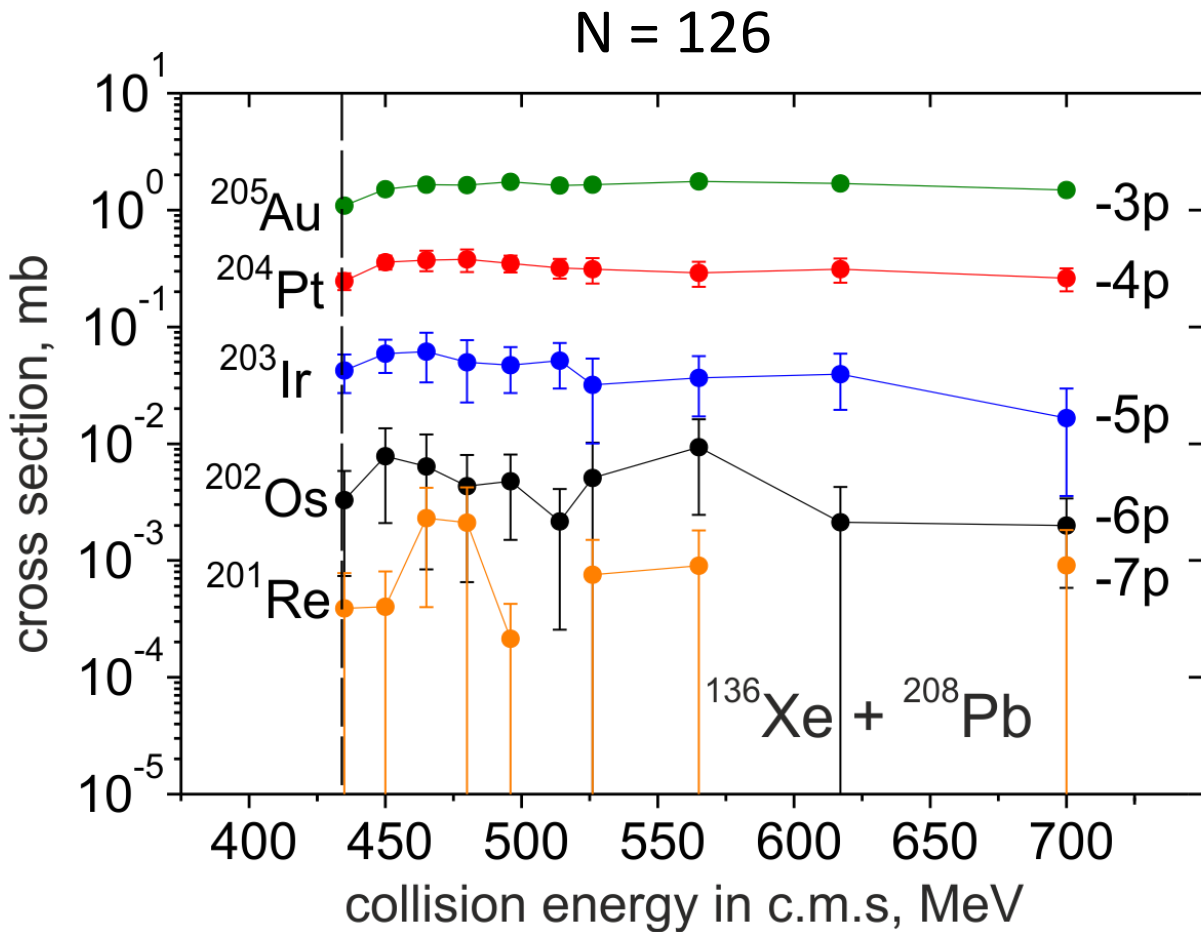


exp.: J.V. Kratz, et. al,
Phys. Rev. C 88, 054615 (2013)

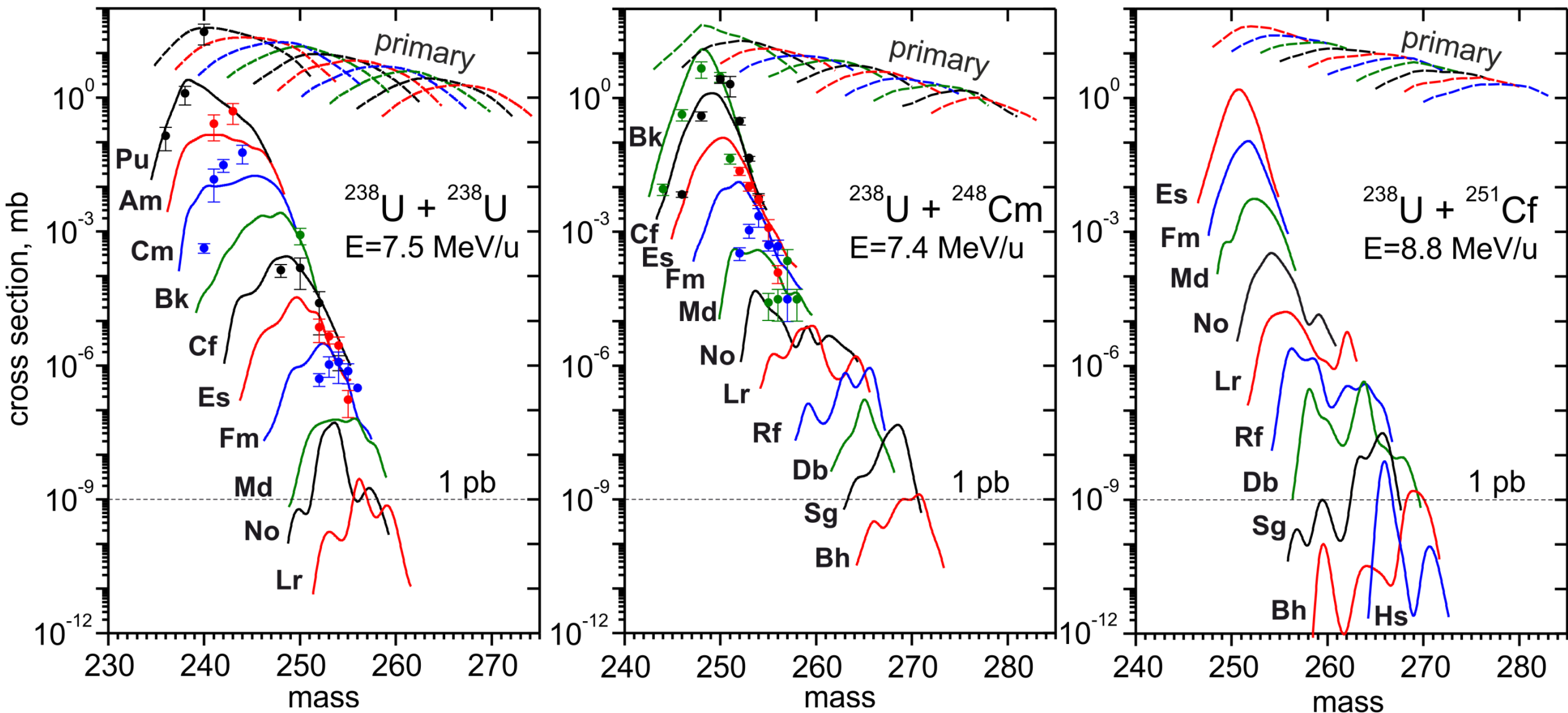
Optimal energy *for heavier elements*



Optimal energy *for neutron-rich nuclei*

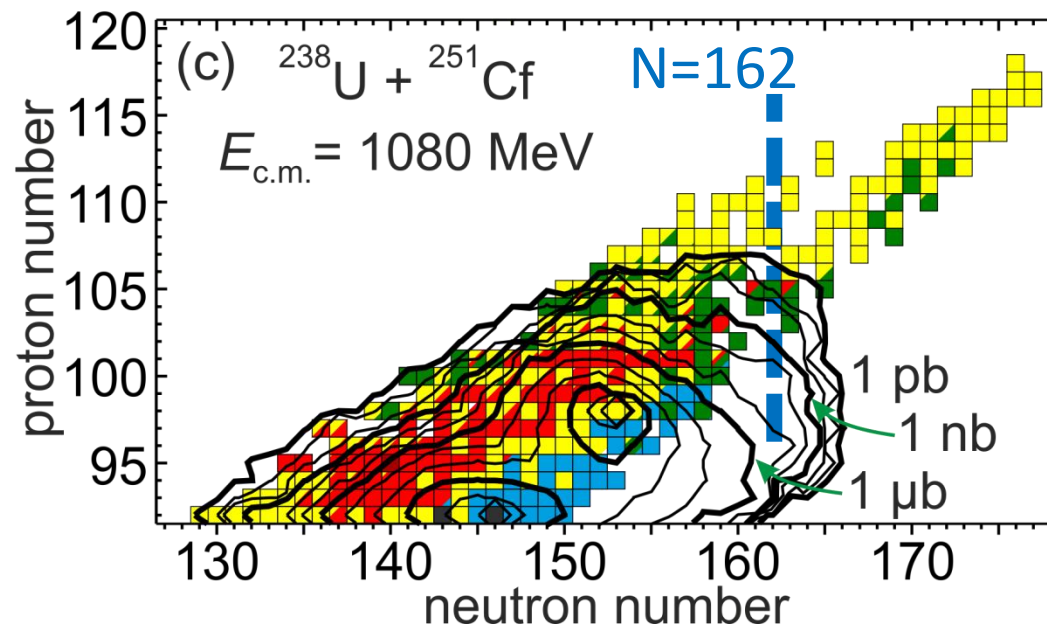
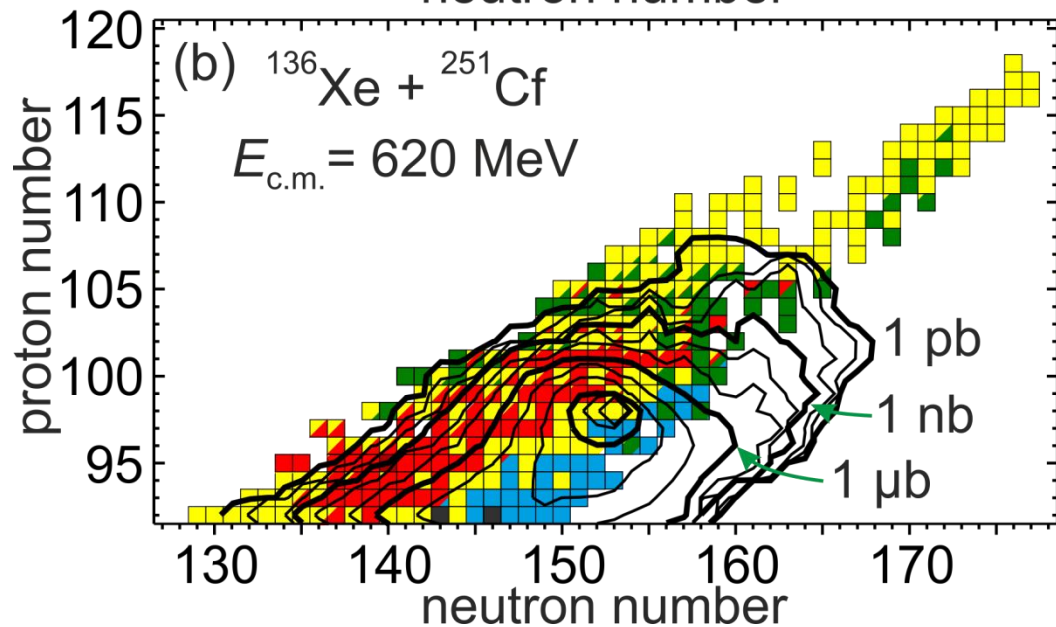
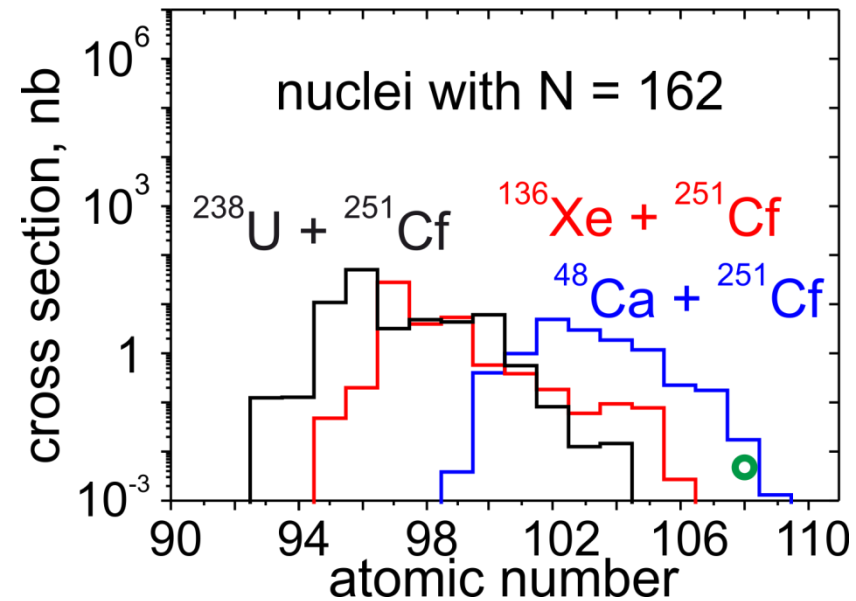
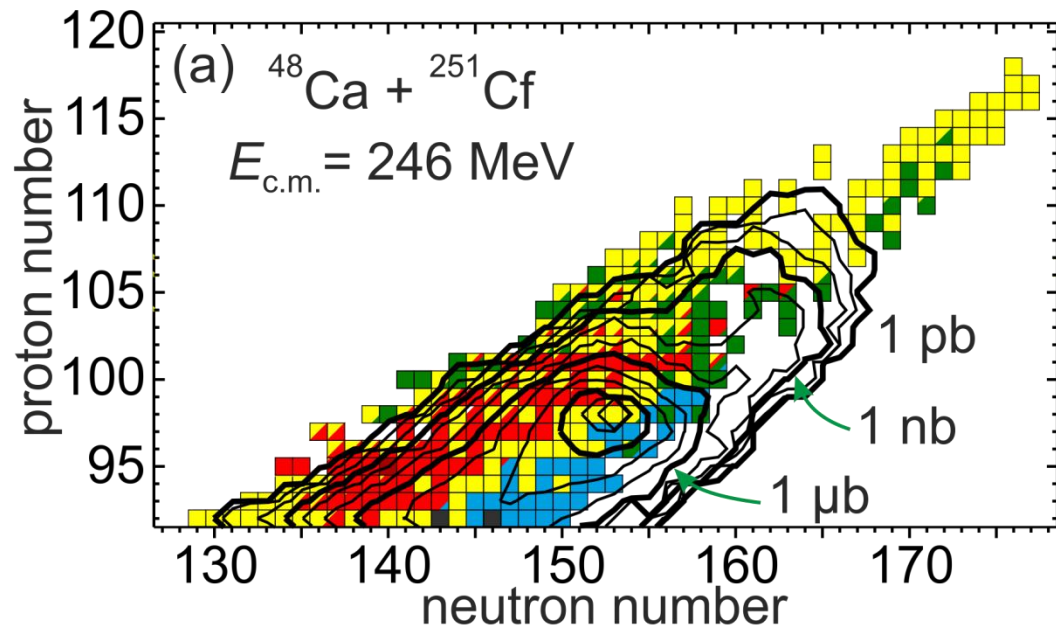


^{238}U -induced MNT reactions



exp.: M. Schadel et al., Phys. Rev. Lett. 41, 469 (1978), Phys. Rev. Lett. 48, 852 (1982)

MNT reactions with ^{251}Cf



Summary

Multidimensional dynamical approach based on Langevin equations is a powerful tool to simulate heavy-ion collisions at low energies. It can describe main characteristics of multinucleon transfer reactions and predict reaction cross sections.

Theoretical analysis of possibility to synthesize new neutron-rich nuclei in multinucleon transfer reactions with actinides was done in the framework of the dynamical model.

Neutron-rich isotopes of transuranium elements can be produced in a MNT reaction with neutron-rich actinide target combining with neutron-rich heavy projectile. Optimal collision energy is slightly above the coulomb barrier. For example, production cross sections of yet-unknown nuclei in the $^{238}\text{U} + ^{251}\text{Cf}$ reaction exceeds 1 μb level.

Thank you for attention!