

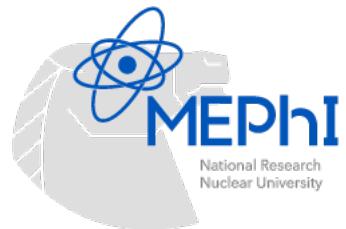
# Anisotropic flow at Nuclotron-NICA energy range

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IX Collaboration Meeting of the MPD Experiment at the NICA Facility  
25 – 27 April 2022

This work is supported by: the RFBR grant No. 18-02-40086

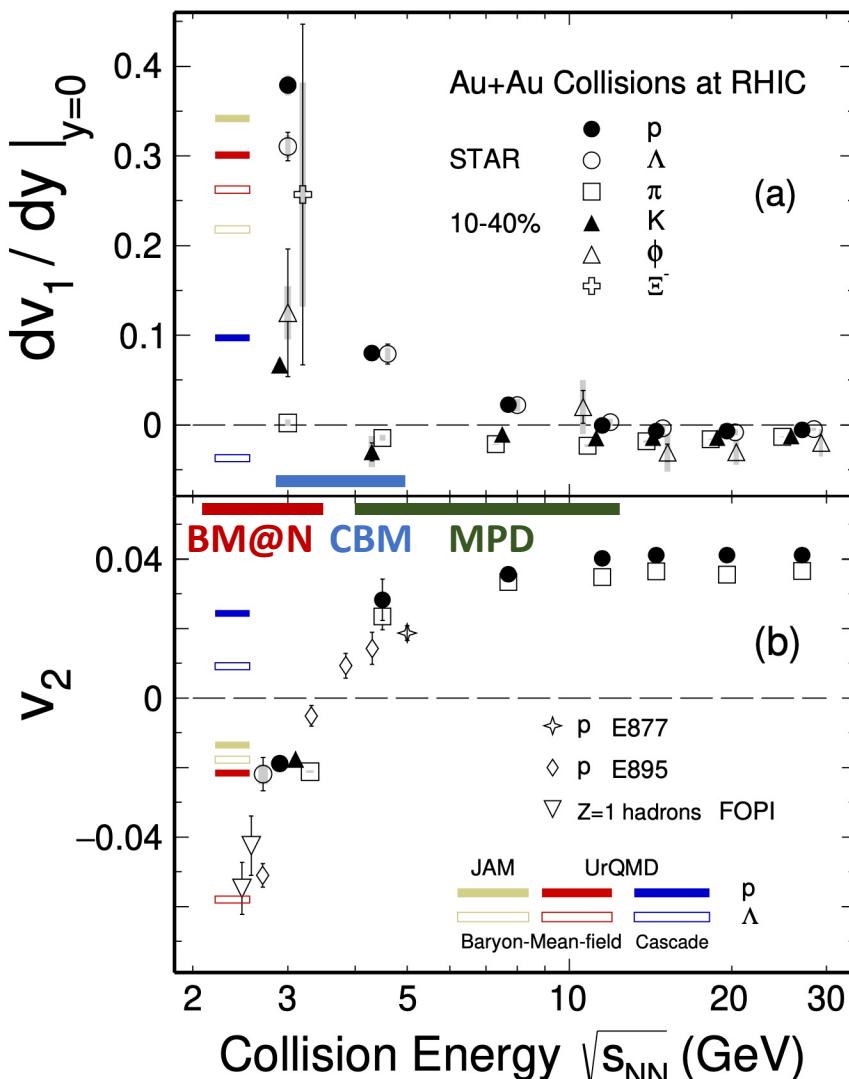


# Outline

- Introduction
- Anisotropic flow at  $\sqrt{s_{NN}} = 4.5 - 11.5$  GeV: hybrid and pure hadronic models vs. existing data
- Anisotropic flow at  $\sqrt{s_{NN}} = 2.4 - 4.5$  GeV: hadronic models with different EOS vs. data from HADES and STAR BES FXT
- What to expect from detailed  $v_n(p_T, y)$  measurements at Nuclotron-NICA energies?
- Summary and outlook

# Anisotropic flow in Au+Au collisions at Nuclotron-NICA energies

M. Abdallah et al. [STAR Collaboration] 2108.00908 [nucl-ex]



$$\frac{dN}{d\phi} \propto 1 + 2 \sum_{n=1} v_n \cos[n(\phi - \Psi_{RP})], \quad v_n = \langle \cos[n(\phi - \Psi_{RP})] \rangle$$

Strong energy dependence of  $dv_1/dy$  and  $v_2$  at  $\sqrt{s_{NN}}=2-11$  GeV

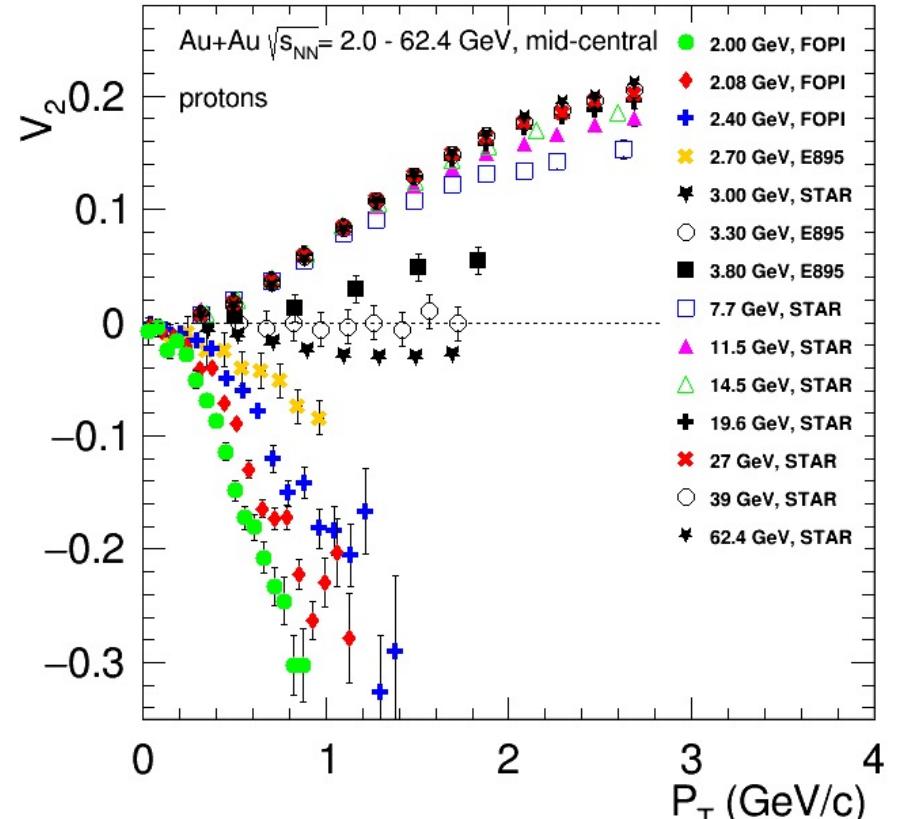
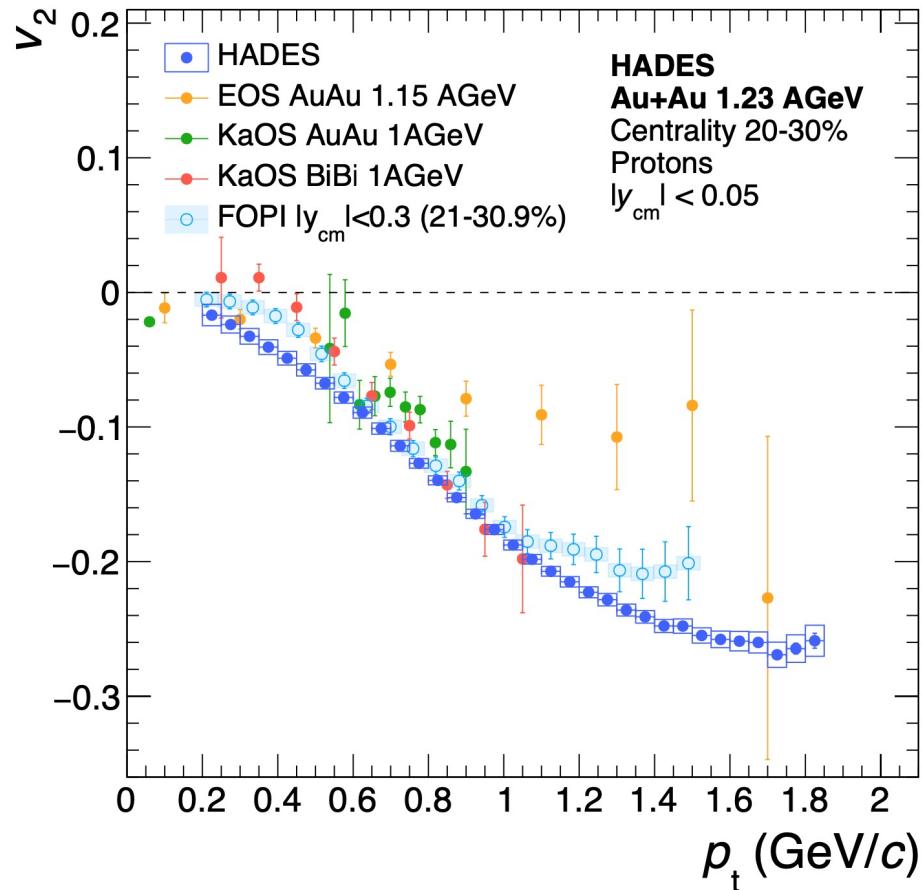
**Anisotropic flow at FAIR/NICA energies is a delicate balance between:**

- I. The ability of pressure developed early in the reaction zone and
- II. The passage time for removal of the shadowing by spectators

**Goal of this work:**

- Perform simulation with different models and make comparison with STAR BES (3, 4.5, 7.7, 11.5 GeV) and HADES (2.4 GeV) published experimental data
- Make predictions for the anisotropic flow measurements  $v_n(p_T, y)$  at BM@N ( $\sqrt{s_{NN}}=2.3-3.3$  GeV), CBM ( $\sqrt{s_{NN}}=2.7-4.9$  GeV), and MPD ( $\sqrt{s_{NN}}=4-11$  GeV) energies

# Why do we need new measurements at BM@N and MPD?



- The main source of existing systematic errors in  $v_n$  measurements is the difference between results from different experiments (for example, FOPI and HADES)
- New data from the future BM@N ( $\sqrt{s_{NN}}=2.3\text{-}3.3$  GeV) and MPD ( $\sqrt{s_{NN}}=4\text{-}11$  GeV) experiments will provide more detailed and robust  $v_n$  measurements

# Hybrid models for anisotropic flow at RHIC/LHC

## 1. UrQMD + 3D viscous hydro model vHLLE+UrQMD

Iurii Karpenko, Comput. Phys. Commun. 185 (2014), 3016

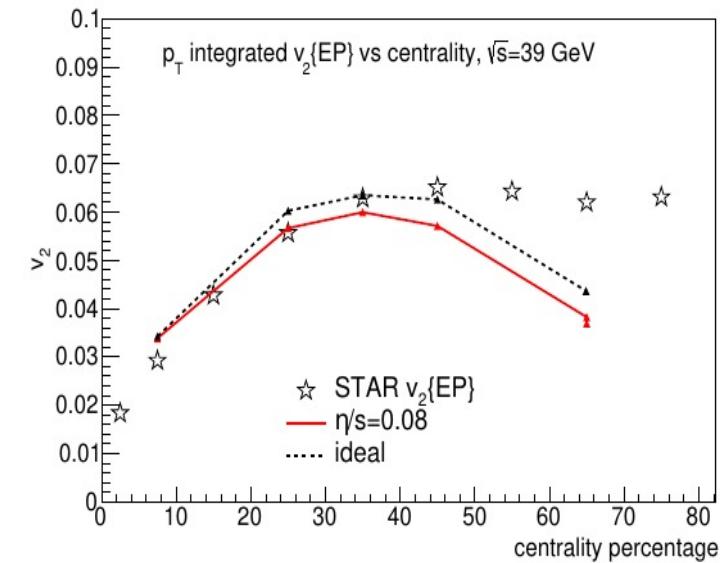
<https://github.com/yukarpenko/vhlle>

Parameters: from Iu. A. Karpenko, P. Huovinen, H. Petersen, M. Bleicher, Phys. Rev. C91 (2015) no.6, 064901 – good description of STAR BES results for  $v_2$  of inclusive charged hadrons (7.7-62.4 GeV)

Initial conditions: model UrQMD

QGP phase: 3D viscous hydro (vHLLE) with crossover EOS (XPT)

Hadronic phase: model UrQMD



## 2. A Multi-Phase Transport model (AMPT) for high-energy nuclear collisions

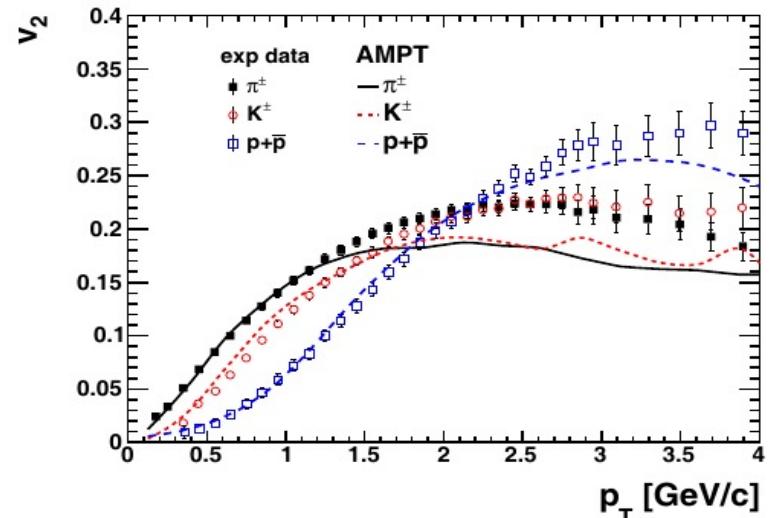
The main source code (Zi-Wei Lin):

<https://myweb.ecu.edu/linz/ampt/v1.26t9b/v2.26t9b>

Initial conditions: model HIJING

QGP phase: Zhang's parton cascade for modeling partonic scatterings

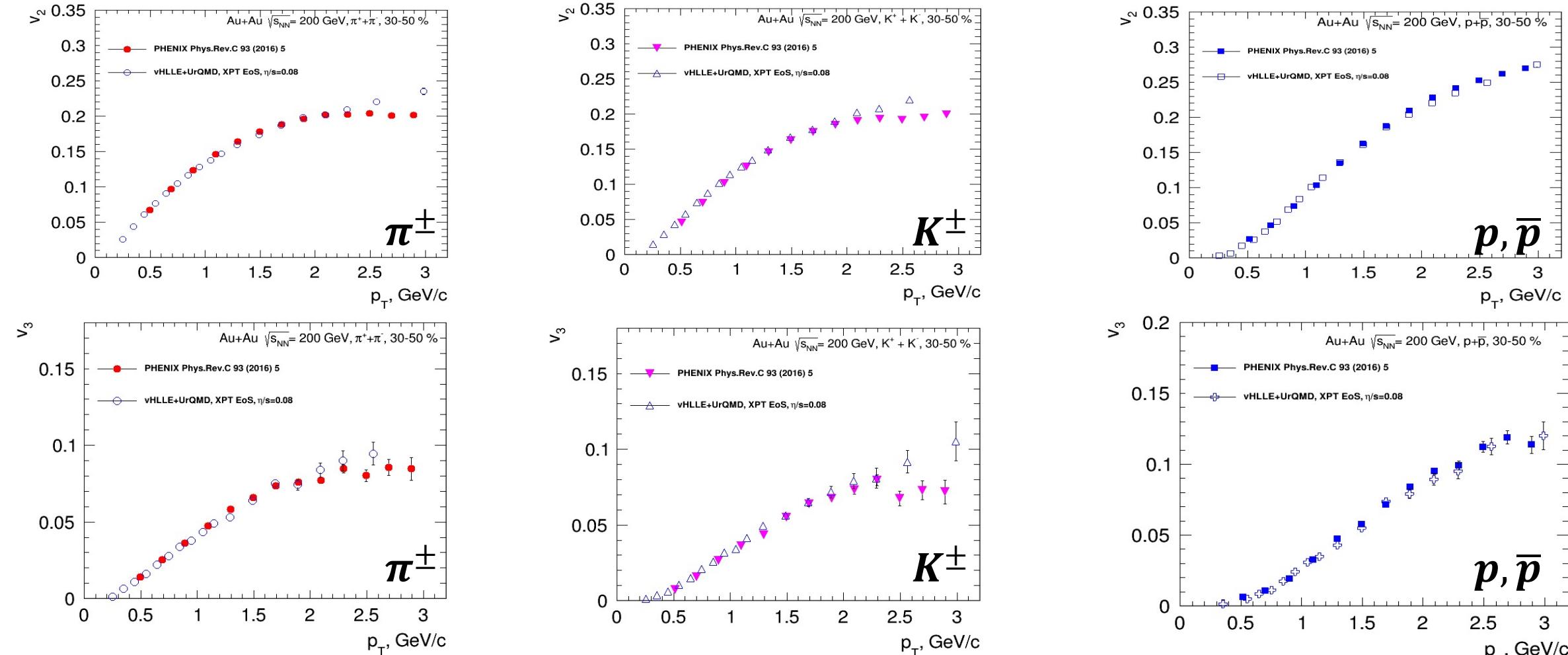
Hadronic phase: model ART



Z.W. Lin, C. M. Ko, B.A. Li, B. Zhang and S. Pal:

Physical Review C 72, 064901 (2005).

# vHLLE+UrQMD: Elliptic and triangular flow in Au+Au collisions at 200 GeV

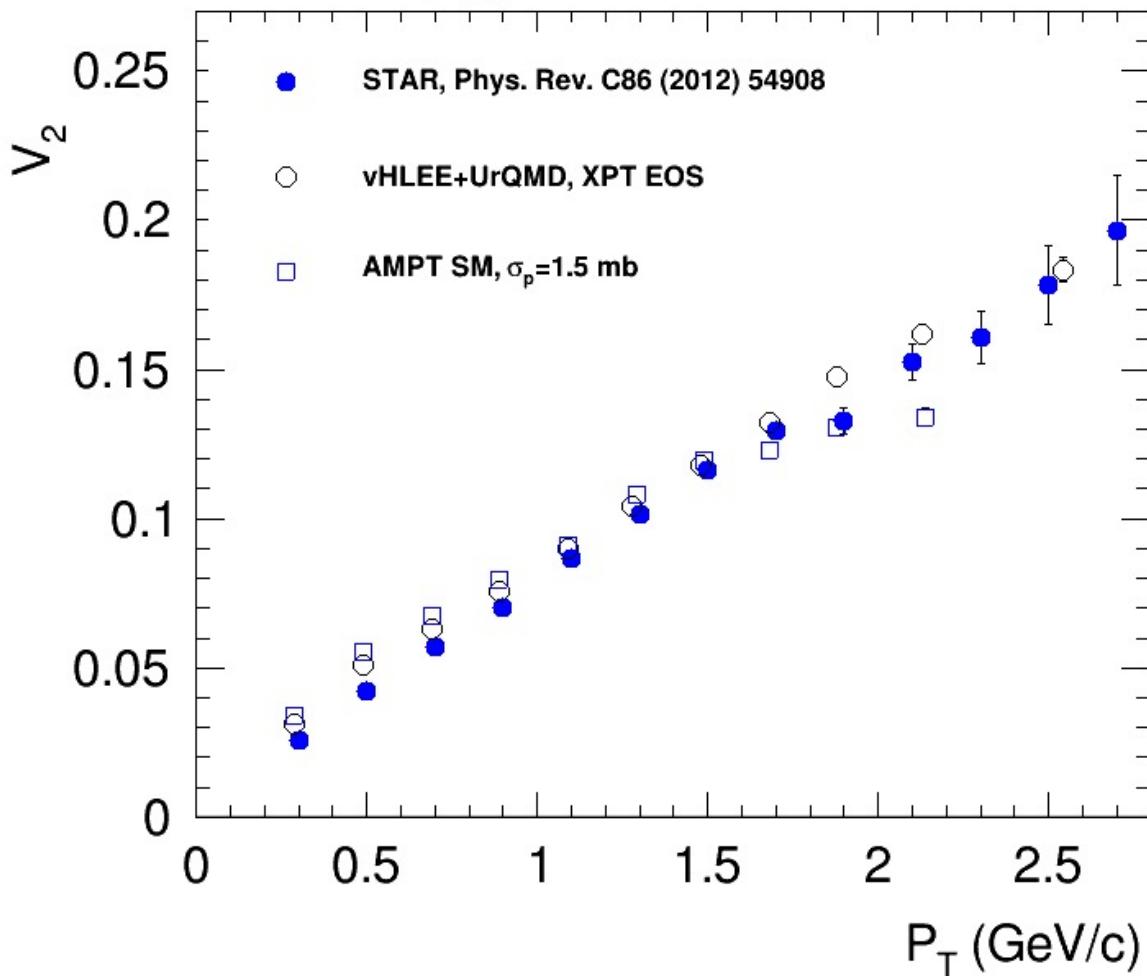


3D hydro model vHHLE + UrQMD (XPT EOS),  $\eta/s = 0.08$  + param from Iu.A. Karpenko, P. Huovinen, H. Petersen, M. Bleicher , Phys.Rev. C91 (2015) no.6, 064901

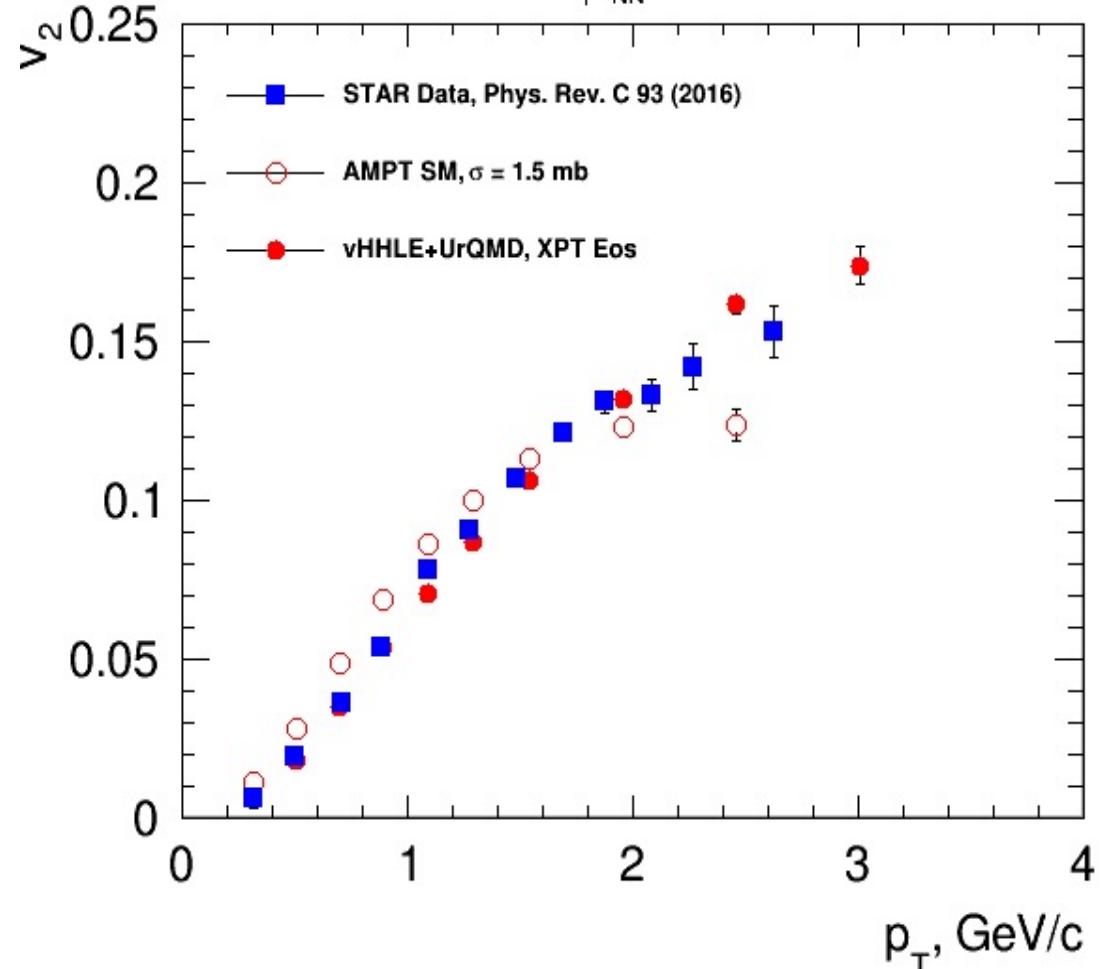
**Reasonable agreement between results of vHLLE+UrQMD model and published PHENIX data**

# Elliptic flow at NICA energies: Models vs. Data comparison

Au+Au at  $\sqrt{s_{NN}} = 7.7$  GeV, 20-30%, ch. hadrons

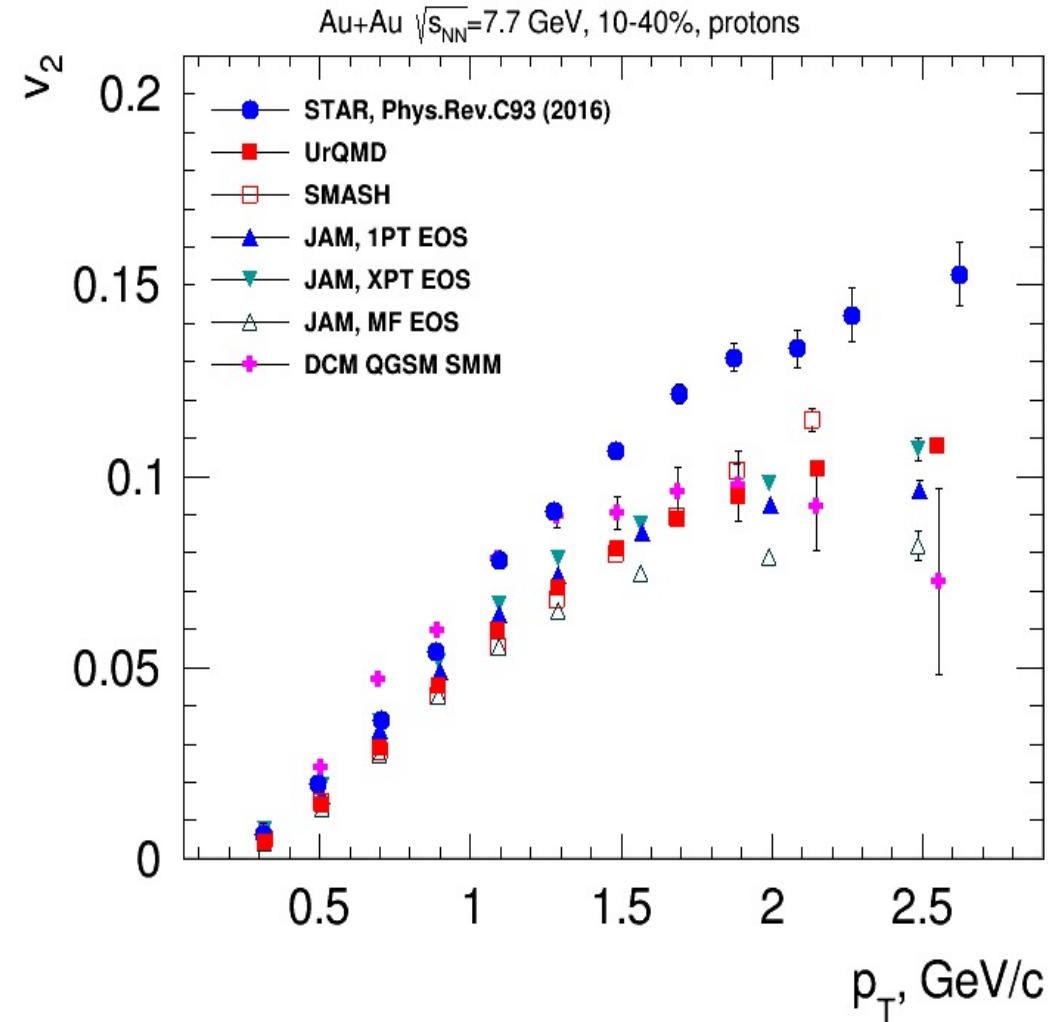
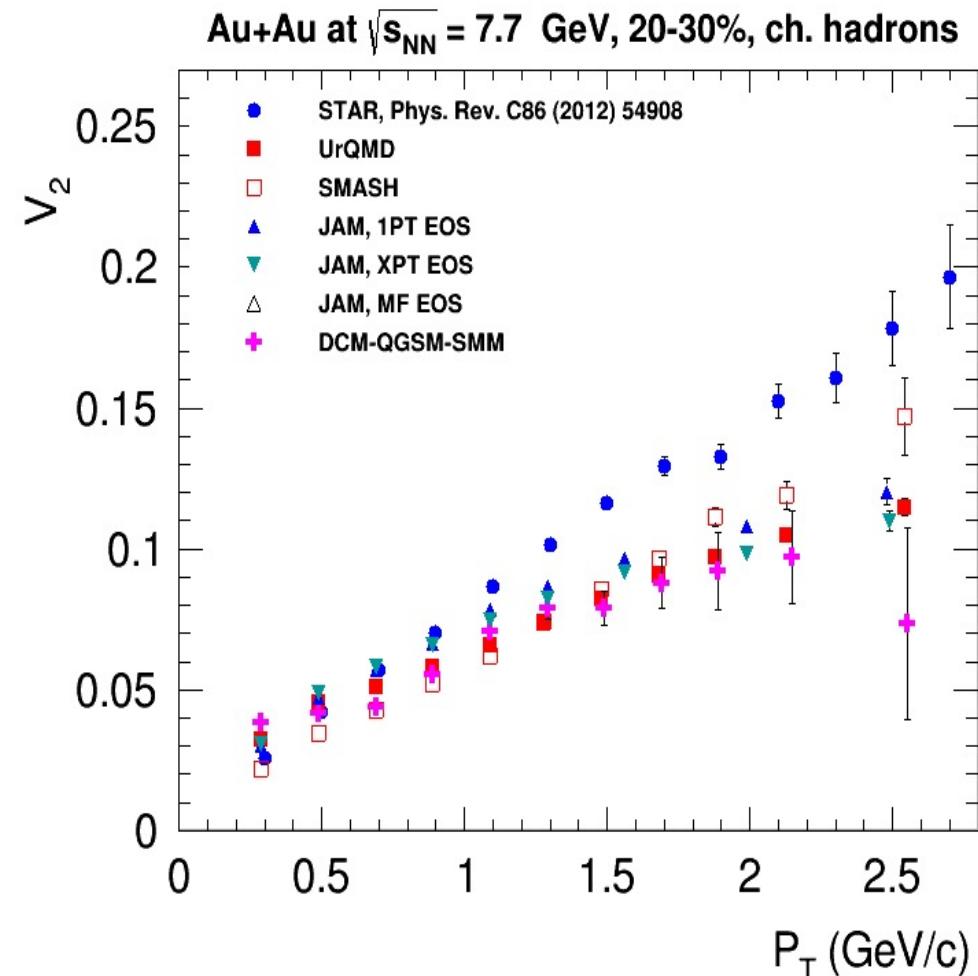


Protons, Au+Au  $\sqrt{s_{NN}}=7.7$  GeV, 10-40 %



Good agreement between vHLLGE+UrQMD ( $\eta/s = 0.2$ , XPT EOS), AMPT models and STAR data for  $\sqrt{s_{NN}} \geq 7.7$  GeV

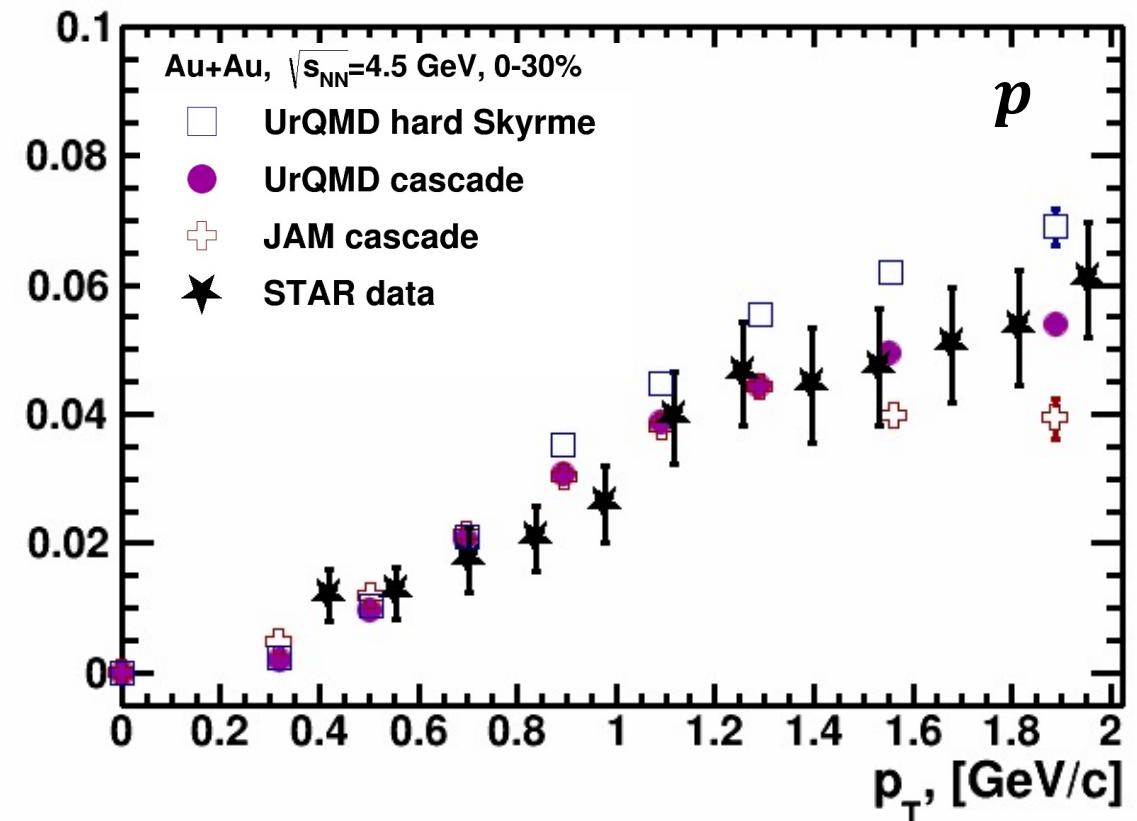
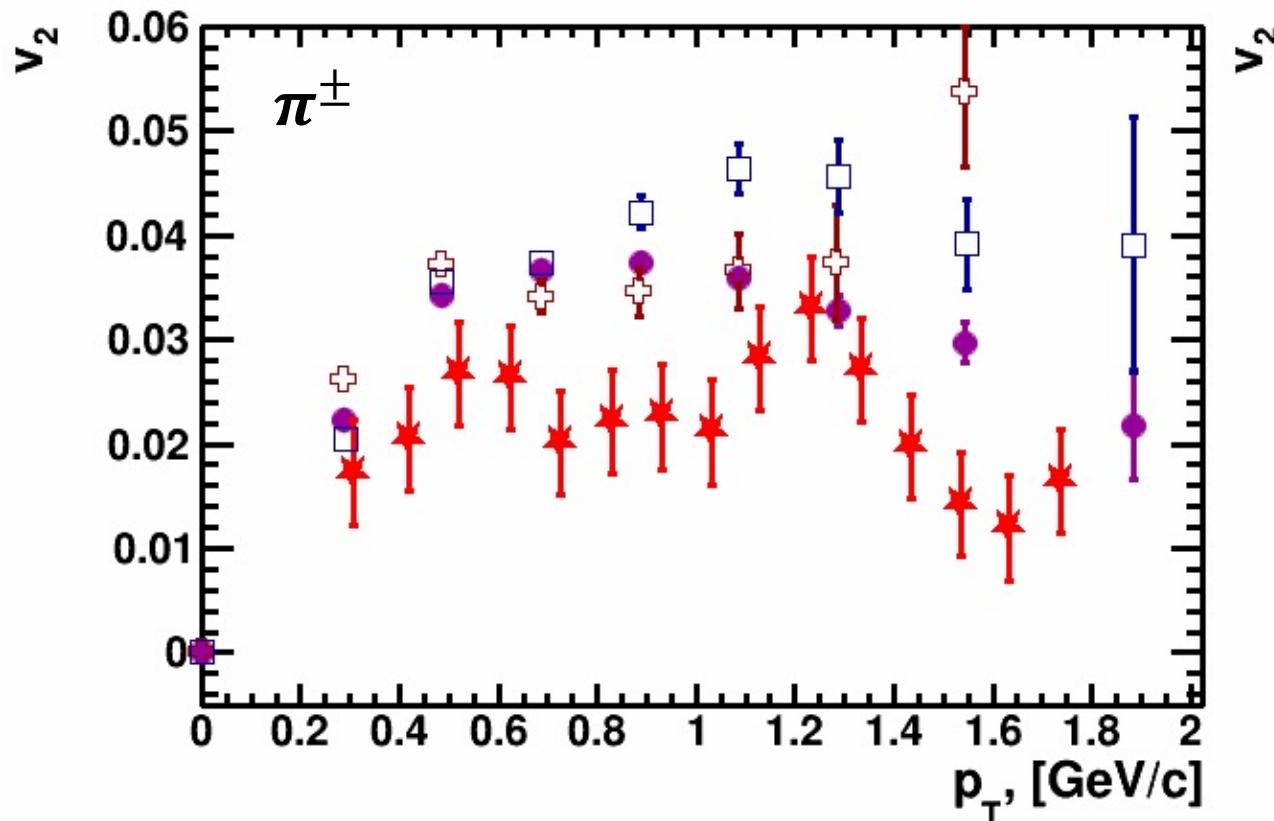
# Elliptic flow at NICA energies: Models vs. Data comparison



Pure String/Hadronic Cascade models give smaller  $v_2$  signal compared to STAR data for  $\sqrt{s_{NN}} \geq 7.7$  GeV

# Elliptic flow at NICA energies: Models vs. Data comparison

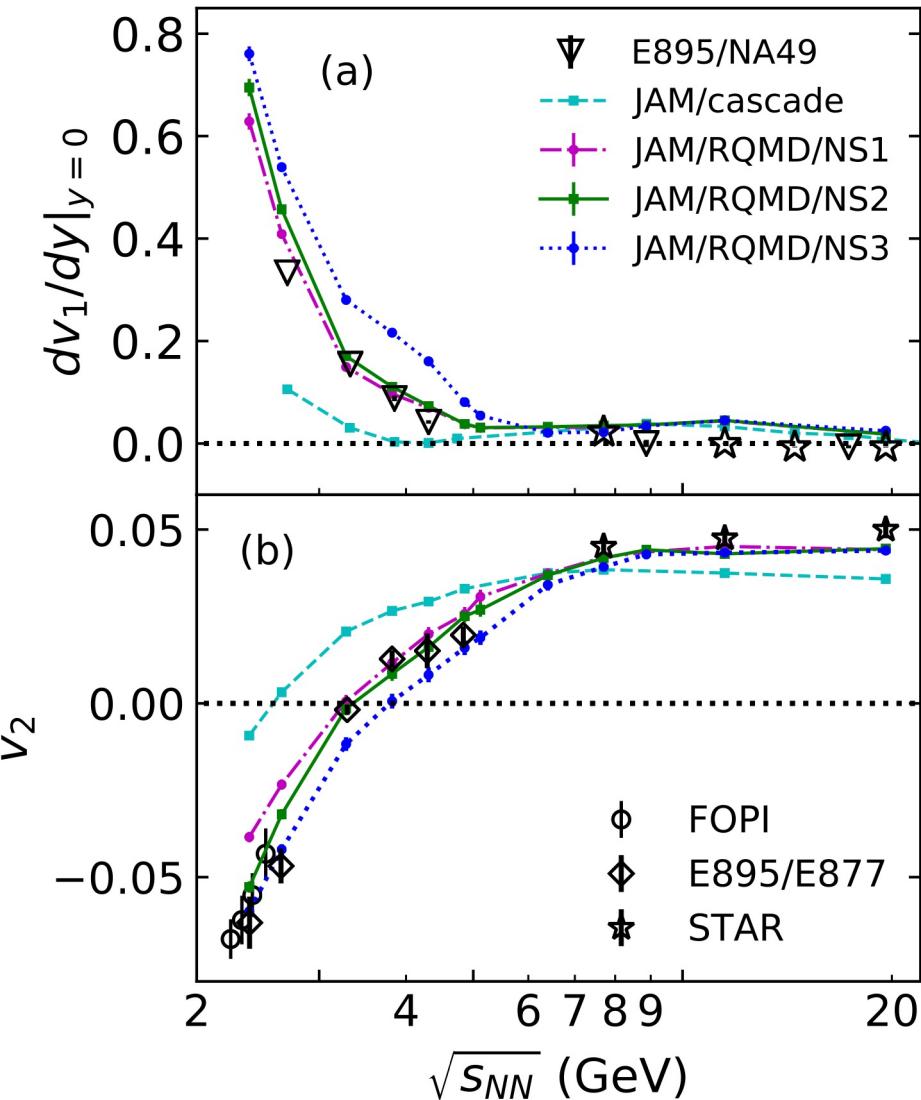
Experimental data is taken from: *Phys.Rev.C* 103 (2021) 3, 034908



Pure String/Hadronic Cascade models give similar  $v_2$  signal  
compared to STAR data for Au+Au  $\sqrt{s_{NN}} = 4.5$  GeV

# Anisotropic flow study at $\sqrt{s_{NN}}=2\text{-}4.5 \text{ GeV}$ with JAM model

Y.Nara, et al., Phys. Rev. C 100, 054902 (2019)



To study energy dependence of  $v_n$ , JAM microscopic model was selected (ver. 1.90597)

NN collisions are simulated by:

- $\sqrt{s_{NN}} < 4 \text{ GeV}$ : resonance production
- $4 < \sqrt{s_{NN}} < 50 \text{ GeV}$ : soft string excitations
- $\sqrt{s_{NN}} > 10 \text{ GeV}$ : minijet production

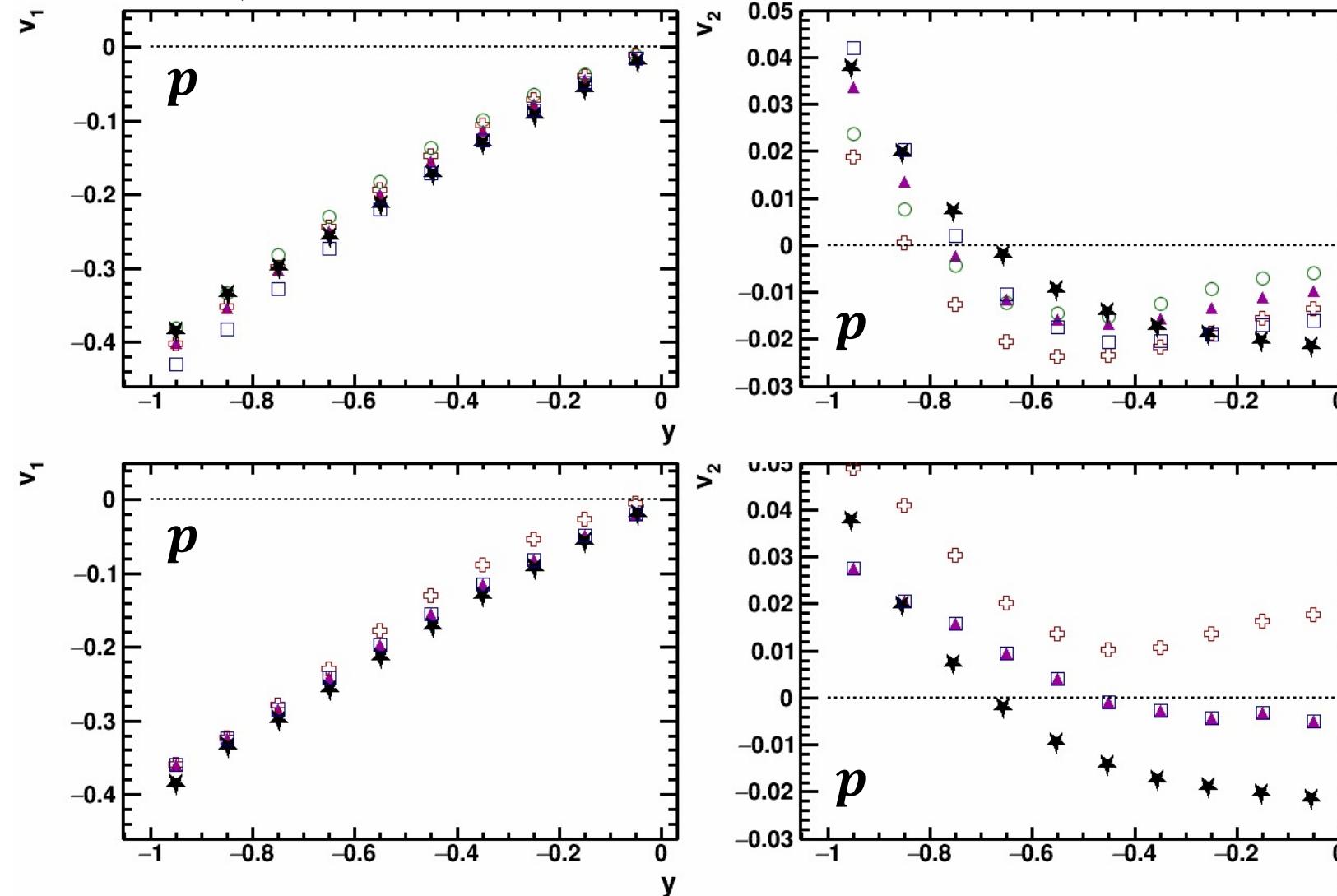
We use RQMD with relativistic mean-field theory (non-linear  $\sigma\text{-}\omega$  model) implemented in JAM model

Different EOS were used:

- **MD3** (momentum-dependent potential):  $K=380 \text{ MeV}$ ,  $m^*/m=0.65$
- **MD2** (momentum-dependent potential):  $K=210 \text{ MeV}$ ,  $m^*/m=0.8$
- **MD4** (momentum-dependent potential):  $K=380 \text{ MeV}$ ,  $m^*/m=0.65$
- **NS1**:  $K=230 \text{ MeV}$ ,  $m^*/m=0.8$
- **NS2**:  $K=380 \text{ MeV}$ ,  $m^*/m=0.8$

Y.Nara, T.Maruyama, H.Stoecker Phys. Rev. C 102, 024913 (2020)  
Y.Nara, H.Stoecker Phys. Rev. C 100, 054902 (2019)

# $v_{1,2}(y)$ in Au+Au $\sqrt{s_{NN}}=3$ GeV: model vs. STAR data



JAM, Au+Au, 10-40%

- MD3 Kinematic cuts:  
 $v_1(y)$  of  $\pi^\pm$ :  $0.2 < pT < 1.6$  GeV/c
- ▲ MD2
- + NS1  $v_1(y)$  of  $K^\pm$ :  $0.4 < pT < 1.6$  GeV/c
- NS2  $v_1(y)$  of  $p$ :  $0.4 < pT < 2.0$  GeV/c
- ★ STAR data

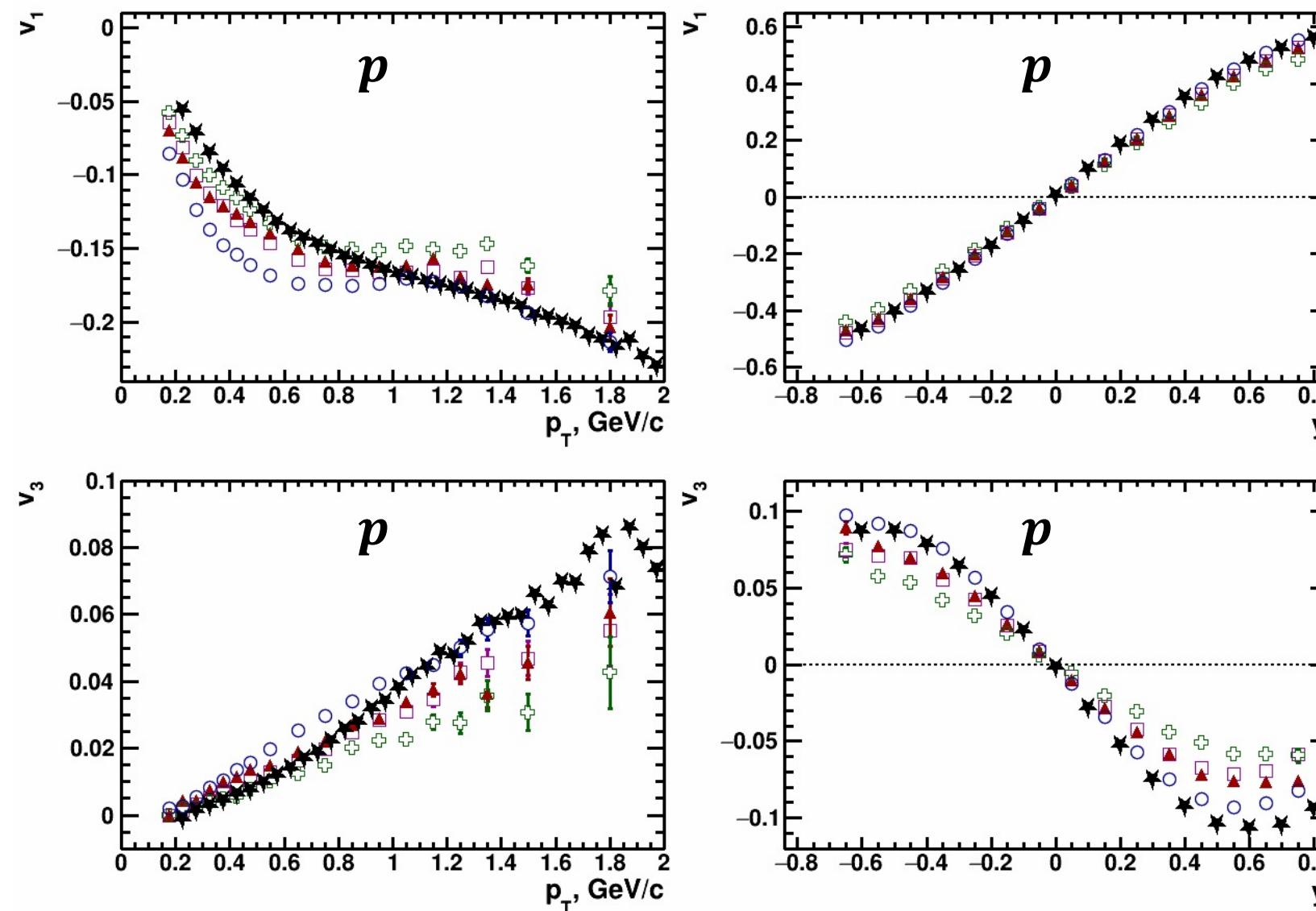
Au+Au, 10-40%

- PHQMD hard EoS
- ▲ PHQMD soft EoS
- + HSD
- ★ STAR data

JAM does not describe all particle species equally well  
 $v_1$  of pions is most sensitive to different EOS

Experimental data points were taken from:  
M. Abdallah et al. [STAR Collaboration] 2108.00908 [nucl-ex]

# $v_{1,3}(p_T, y)$ in Au+Au $\sqrt{S_{NN}}=2.4$ GeV: model vs. HADES data



JAM, Au+Au, 20-30% (6< $b$ <9 fm)

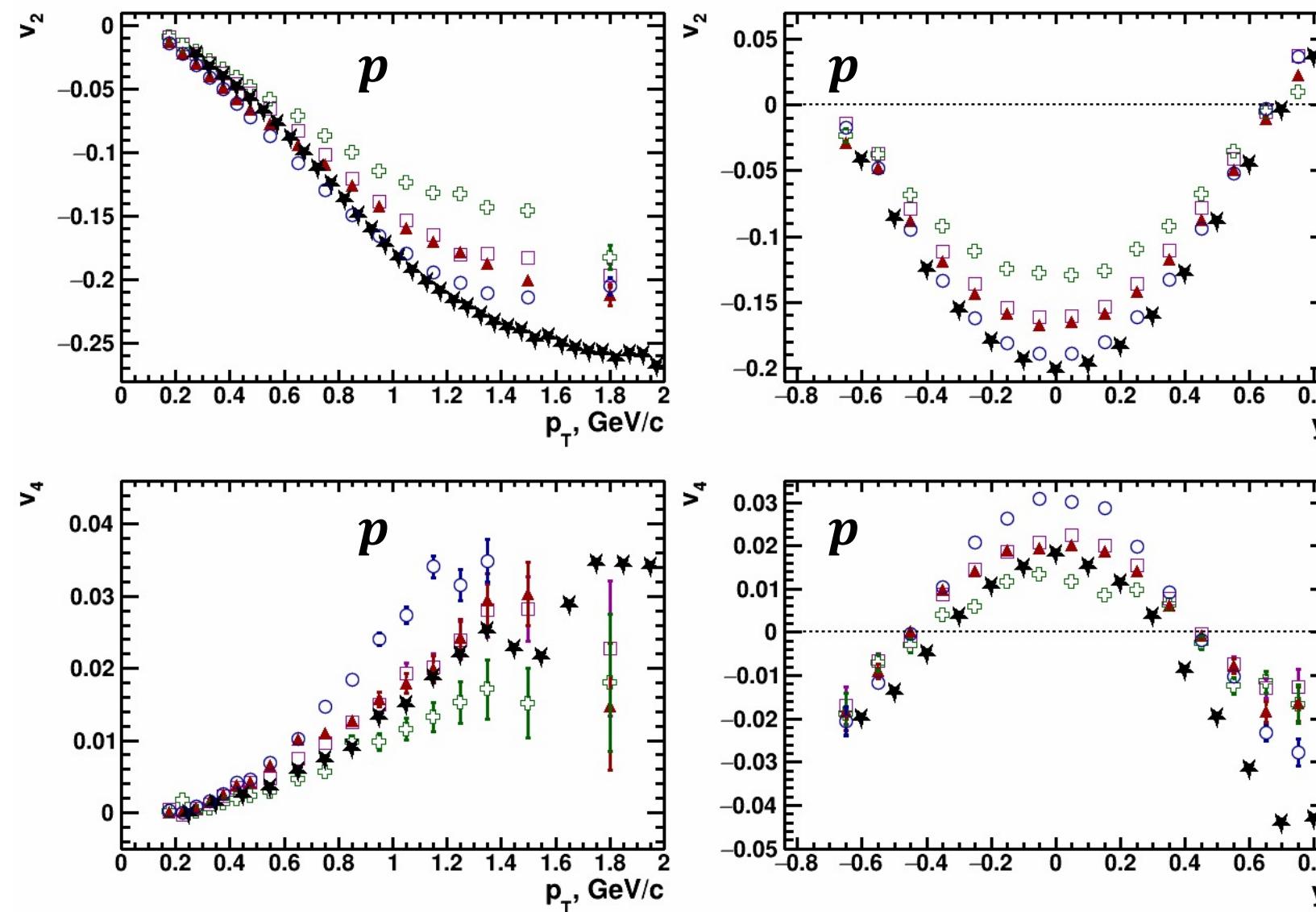
- MD3
- MD2
- ▲ NS1
- + NS2
- ★ HADES data

Experimental data points:  
Phys. Rev. Lett. **125** (2020) 262301

Kinematic cuts:  
 $V_{1,3}(p_T)$ :  $-0.25 < y < -0.15$   
 $V_{1,3}(y)$ :  $1.0 < pT < 1.5$  GeV/c

Good agreement for  $v_{1,3}(y)$   
 $v_3(y)$  is more sensitive to different  
EOS than  $v_1(y)$

# $v_{2,4}(p_T, y)$ in Au+Au $\sqrt{S_{NN}}=2.4$ GeV: model vs. HADES data



JAM, Au+Au, 20-30% (6< $b$ <9 fm)

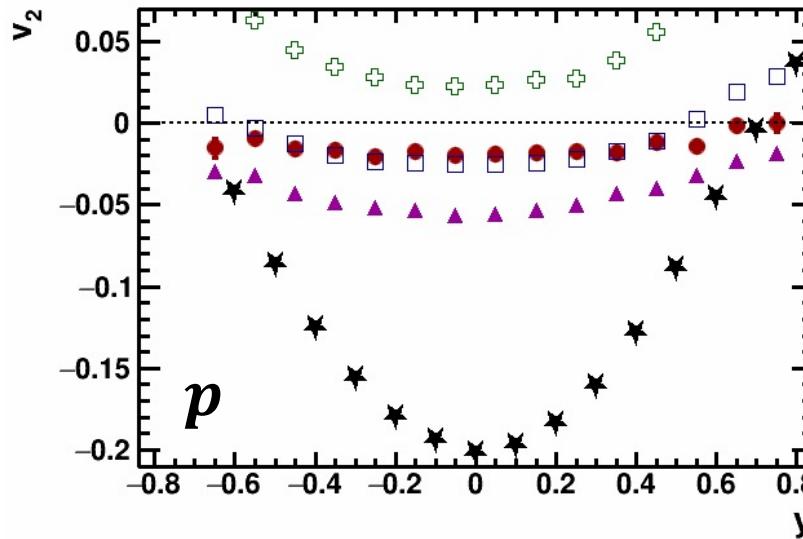
- MD3
- MD2
- ▲ NS1
- ✚ NS2
- ★ HADES data

Experimental data points:  
Phys. Rev. Lett. **125** (2020) 262301

Kinematic cuts:  
 $V_{2,4}(p_T)$ :  $-0.05 < y < 0.05$   
 $V_{2,4}(y)$ :  $1.0 < pT < 1.5$  GeV/c

Good agreement for  $v_{2,4}(y)$   
 $v_{2,4}$  more sensitive to different EOS than  $v_1$   
More JAM results with different EOS are needed

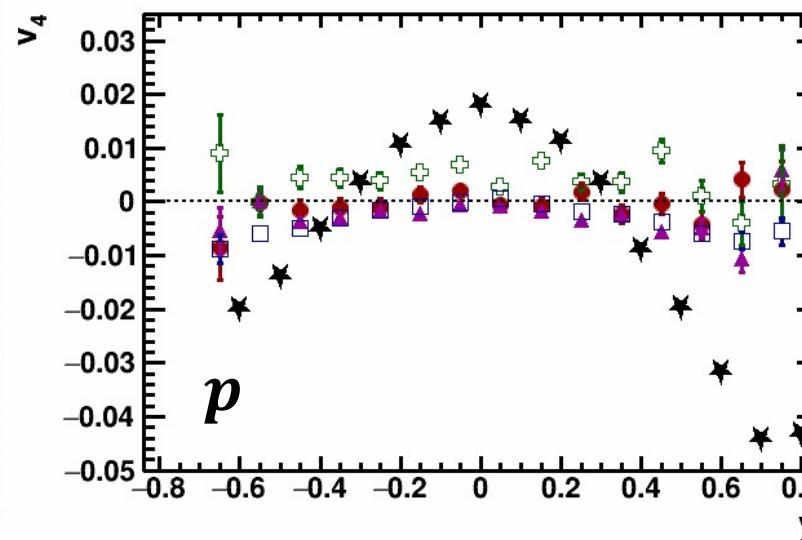
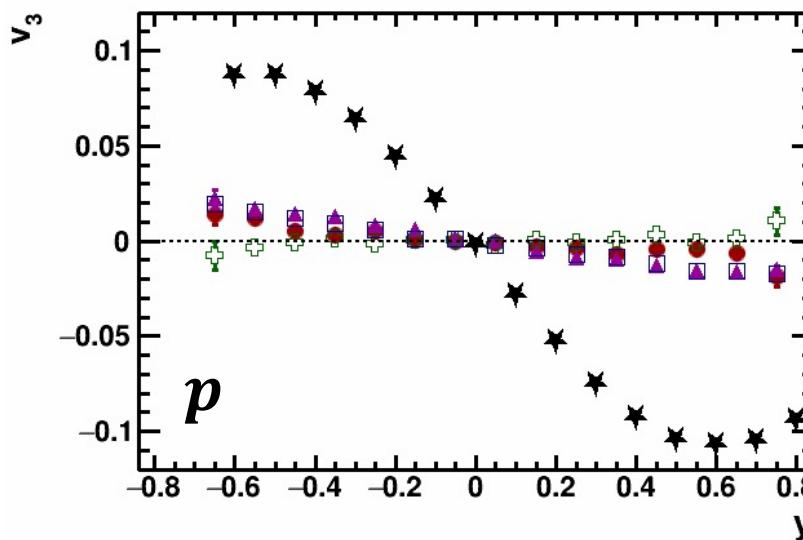
# $v_2(p_T, y)$ in Au+Au $\sqrt{s_{NN}}=2.4$ GeV: cascade models



Au+Au, 20-30% (6< $b$ <9 fm)

- DCM-QGSM-SMM
- UrQMD cascade
- ▲ JAM cascade
- + HSD cascade
- ★ HADES data

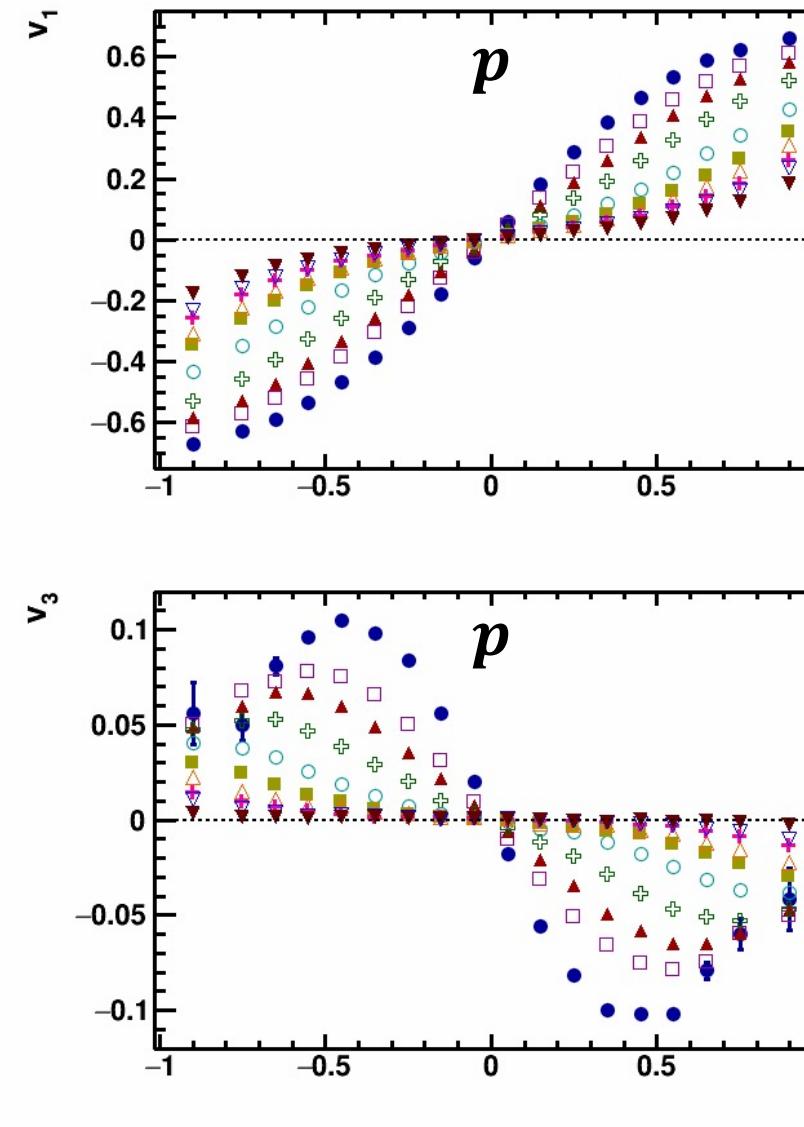
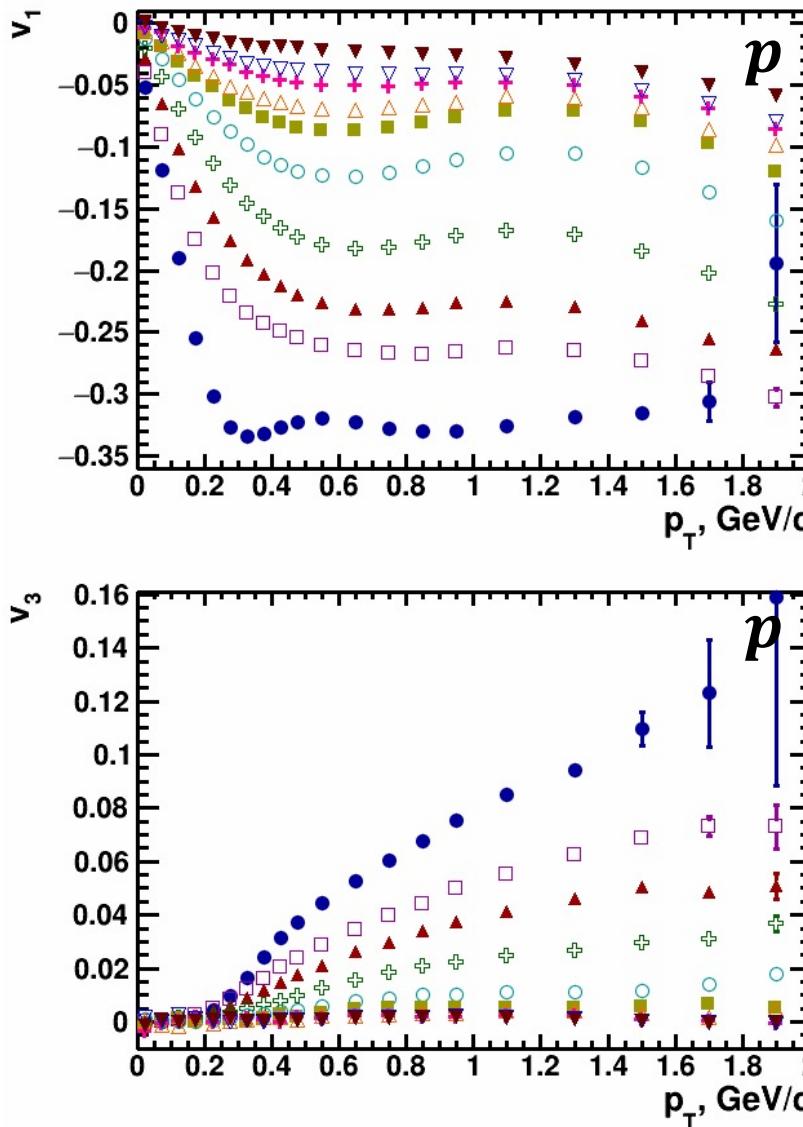
Experimental data points:  
Phys. Rev. Lett. **125** (2020) 262301



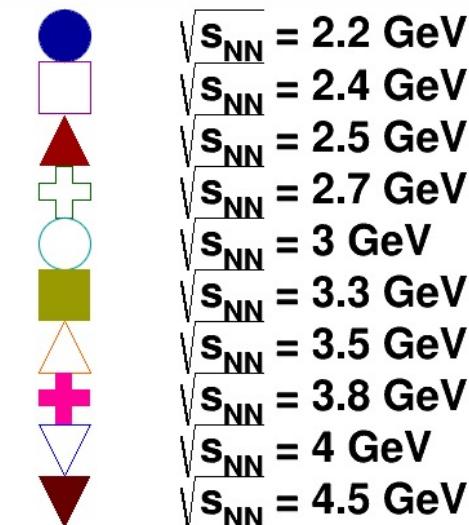
Kinematic cuts:  
 $V_{2,4}(p_T): -0.05 < y < 0.05$   
 $V_{2,4}(y): 1.0 < pT < 1.5 \text{ GeV}/c$

Models with cascade mode  
cannot reproduce the  
experimental data

# $v_{1,3}(p_T, y)$ Au+Au $\sqrt{s_{NN}}=2.2\text{-}4.5$ GeV: JAM



JAM MD3, Au+Au, 10-40%



Protons:

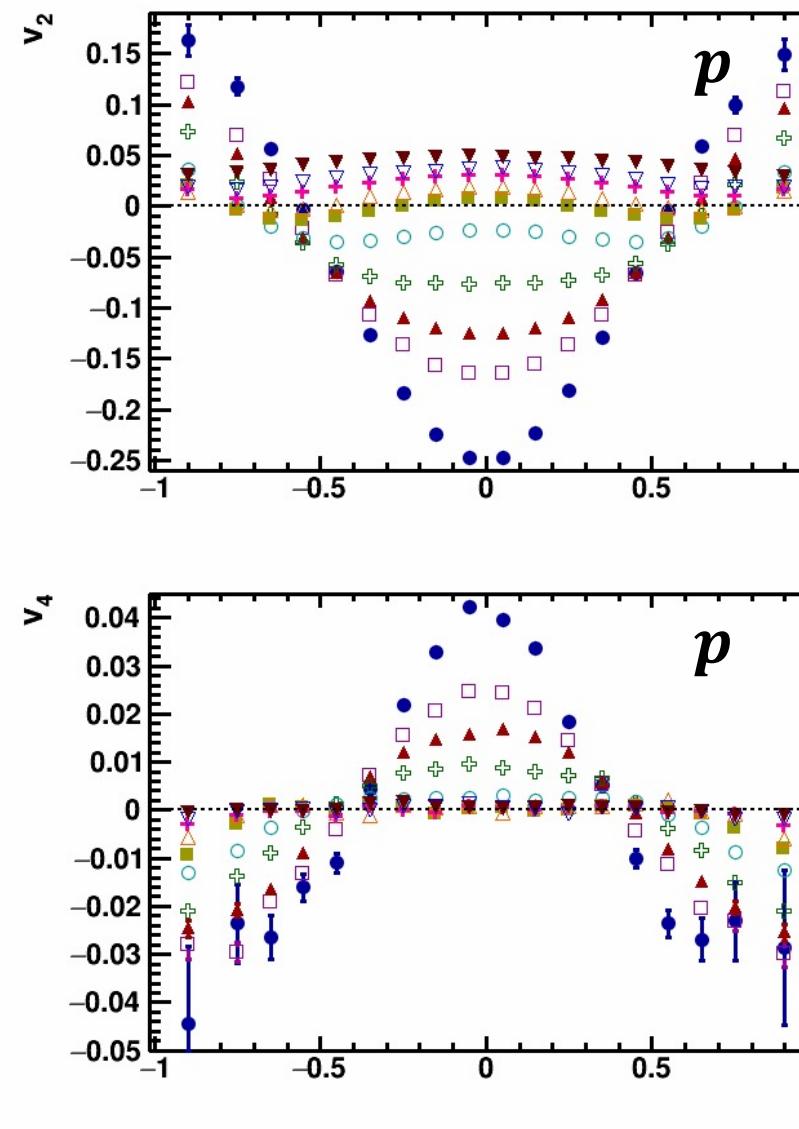
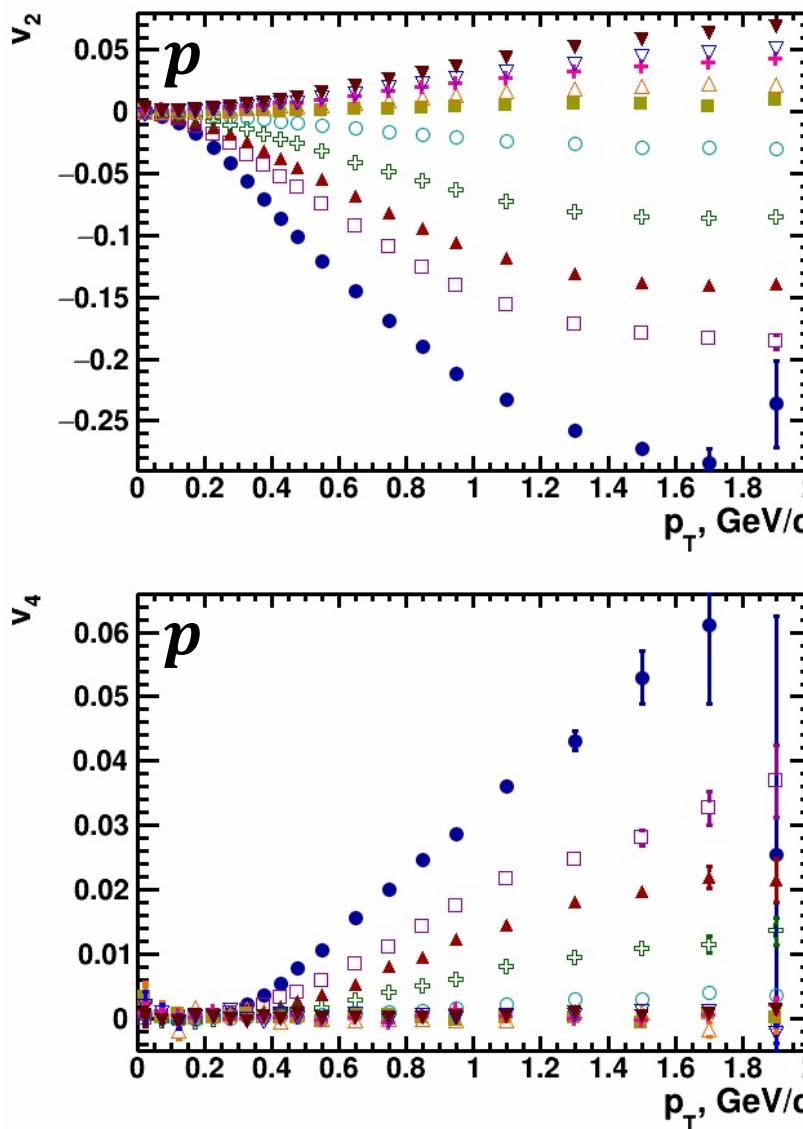
$V_{1,3}(p_T)$ :  $-0.5 < y < -0.15$

$V_{1,3}(y)$ :  $1.0 < p_T < 1.5$  GeV/c

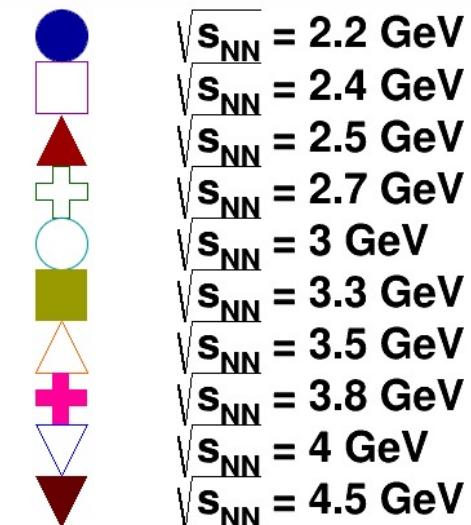
$|v_{1,3}\{\Psi_1\}|$  decreases with increasing collision energy

$v_3 \approx 0$  at  $\sqrt{s_{NN}} \geq 3.5$  GeV

# $v_{2,4}(p_T, y)$ Au+Au $\sqrt{s_{NN}}=2.2\text{-}4.5$ GeV: JAM



JAM MD3, Au+Au, 10-40%



Protons:

$V_{2,4}(p_T)$ :  $-0.2 < y < 0.2$

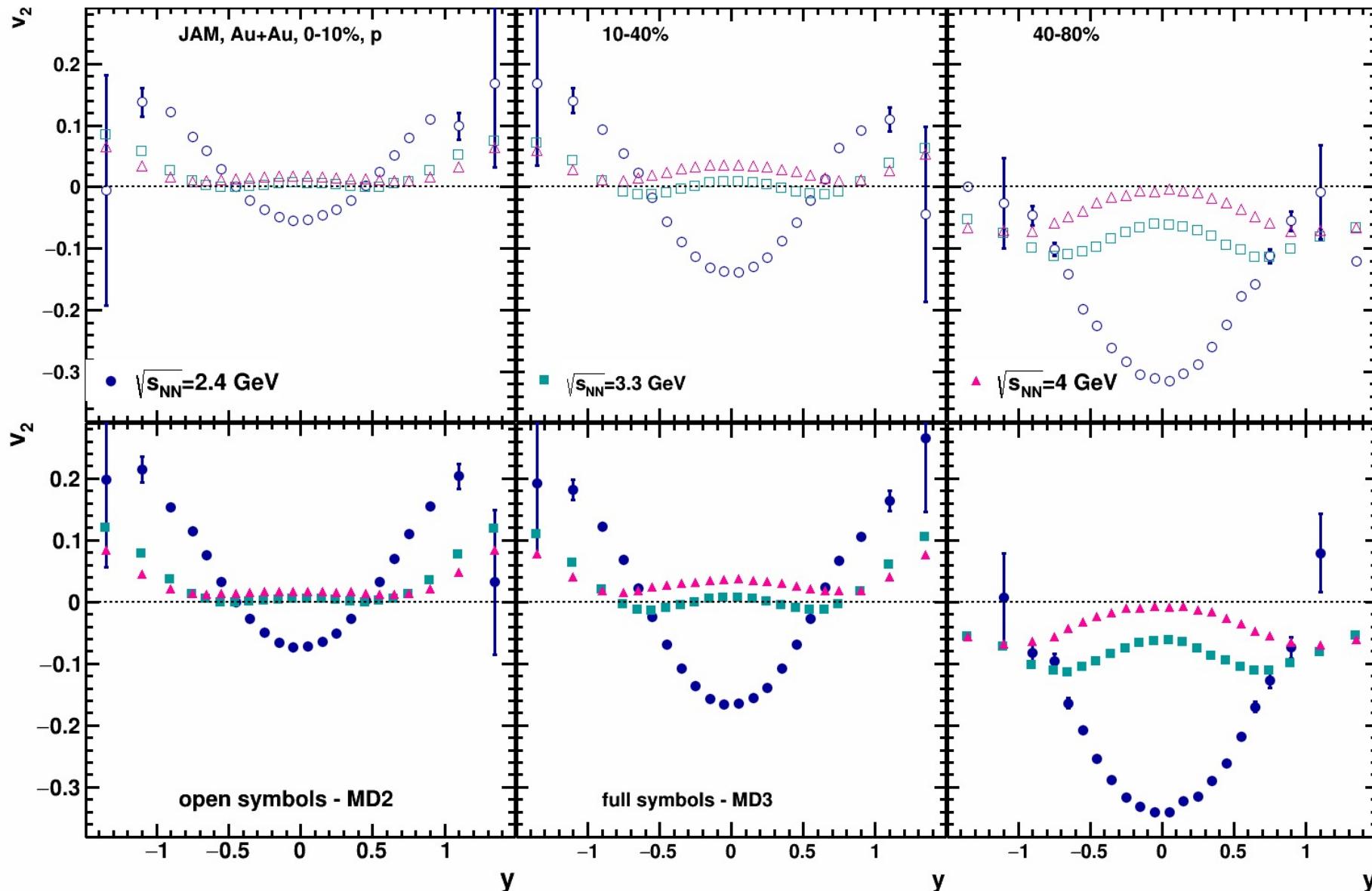
$V_{2,4}(y)$ :  $1.0 < pT < 1.5$  GeV/c

$v_2 \approx 0$  in midrapidity at  $\sqrt{s_{NN}}=3.3$  GeV

$v_4\{\Psi_1\} \approx 0$  at  $\sqrt{s_{NN}} \geq 3.5$  GeV

For more precise  $v_n(p_T, y)$  study,  
different models and EOS are needed

# $v_2(y)$ transition from out-of-plane to in-plane



- Weak dependence on EoS
- $v_2(p_T)$  strongly depends on centrality:
  - Transition from out-of-plane to in-plane depends on centrality
  - $v_2 < 0$  event at  $\sqrt{s_{NN}} = 4$  GeV in peripheral collisions

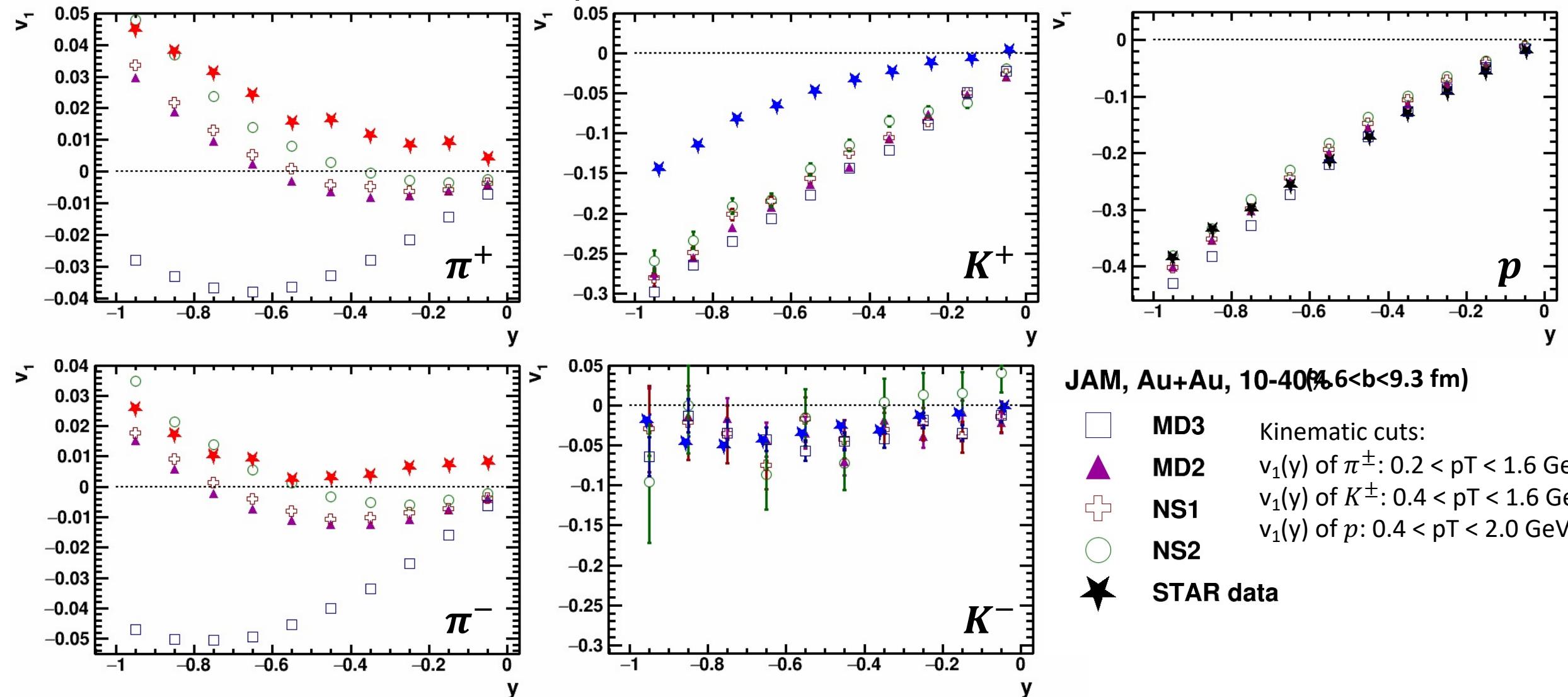
# Summary and outlook

- **Anisotropic flow at  $\sqrt{s_{NN}}=4\text{-}11.5 \text{ GeV}$ :**
  - Pure String/Hadronic Cascade models (no QGP phase) give smaller  $v_2$  signal compared to STAR data for Au+Au  $\sqrt{s_{NN}}=7.7\text{-}11.5 \text{ GeV}$
  - Models give similar  $v_2$  signal compared to STAR data for Au+Au  $\sqrt{s_{NN}}=4.5 \text{ GeV}$
- **Comparison with STAR BES at  $\sqrt{s_{NN}}=4.5, 3 \text{ GeV}$  and HADES at  $\sqrt{s_{NN}}=2.4 \text{ GeV}$ :**
  - Good overall agreement with experimental data for protons for  $v_n$
  - Models in cascade mode do not describe experimental data for  $v_n$
  - Higher harmonics more sensitive to the different EOS
- **Study of collision energy dependence of  $v_n$ :**
  - $|v_{1,3}|$  decreases with increasing collision energy
  - $v_2 \approx 0$  in midrapidity at  $\sqrt{s_{NN}}=3.3 \text{ GeV}$
  - $v_{3,4}\{\Psi_1\} \approx 0$  at  $\sqrt{s_{NN}} \geq 4 \text{ GeV}$
  - $v_2(p_T, y, \sqrt{s_{NN}})$  of protons depends on centrality
- New data from the future BM@N ( $\sqrt{s_{NN}}=2.3\text{-}3.3 \text{ GeV}$ ) and MPD ( $\sqrt{s_{NN}}=4\text{-}11 \text{ GeV}$ ) experiments will provide more detailed and robust  $v_n$  measurements
- To perform more detailed study, detailed differential measurements with different colliding systems are needed

Thank you for your attention!

# Backup slides

# $v_1(y)$ in Au+Au $\sqrt{s_{NN}}=3$ GeV: model vs. STAR data



JAM does not describe all particle species equally well  
 $v_1$  of pions is most sensitive to different EOS

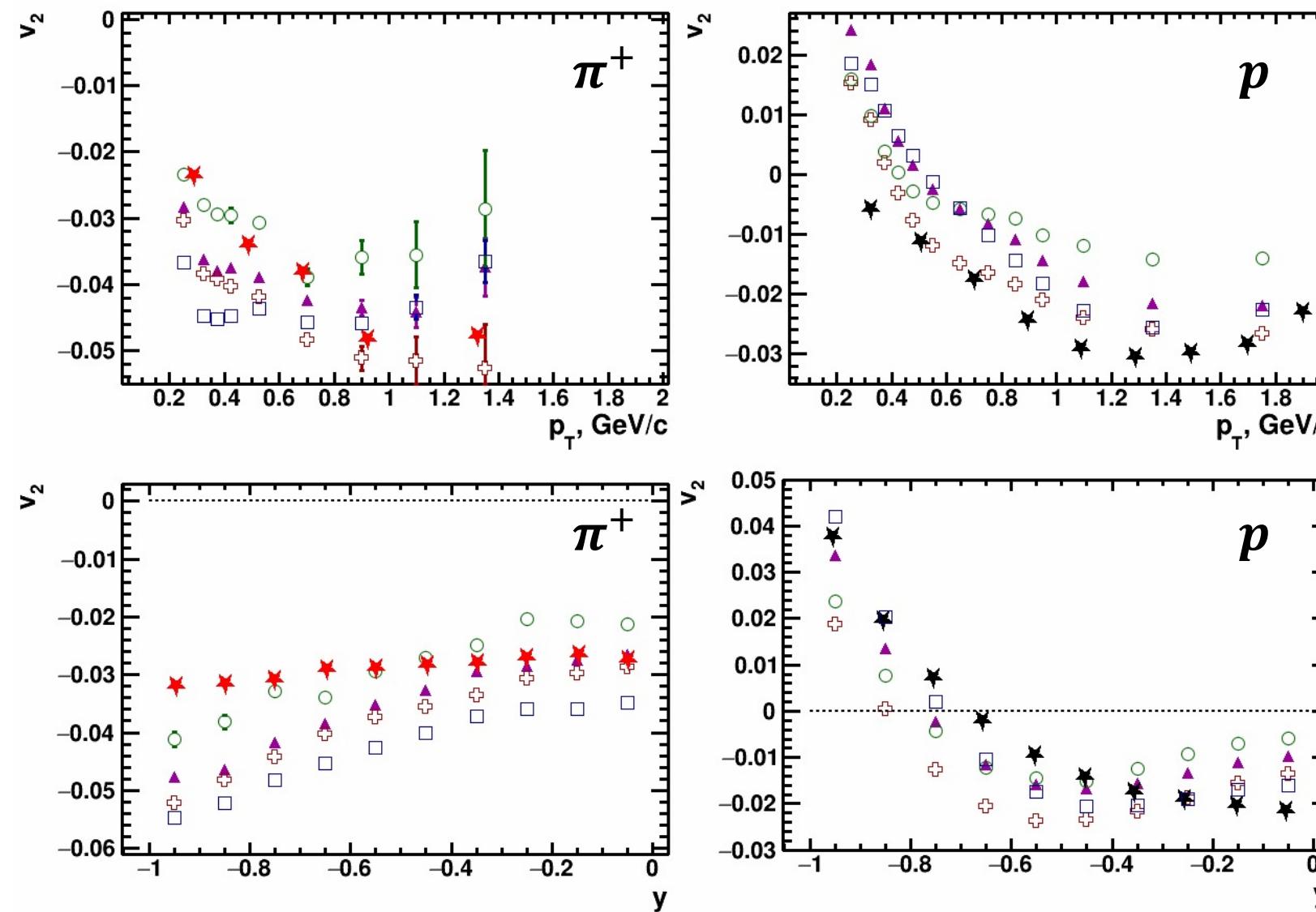
01.12.2021

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Experimental data points were taken from:  
M. Abdallah et al. [STAR Collaboration] 2108.00908 [nucl-ex]

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# $v_2(p_T, y)$ in Au+Au $\sqrt{S_{NN}}=3$ GeV: model vs. STAR data



JAM, Au+Au, 10-40% ( $4.6 < b < 9.3$  fm)

- MD3
- ▲ MD2
- + NS1
- NS2
- ★ STAR data

Experimental data points:

M. Abdallah et al. [STAR Collaboration] 2108.00908 [nucl-ex]  
сократить

Kinematic cuts:

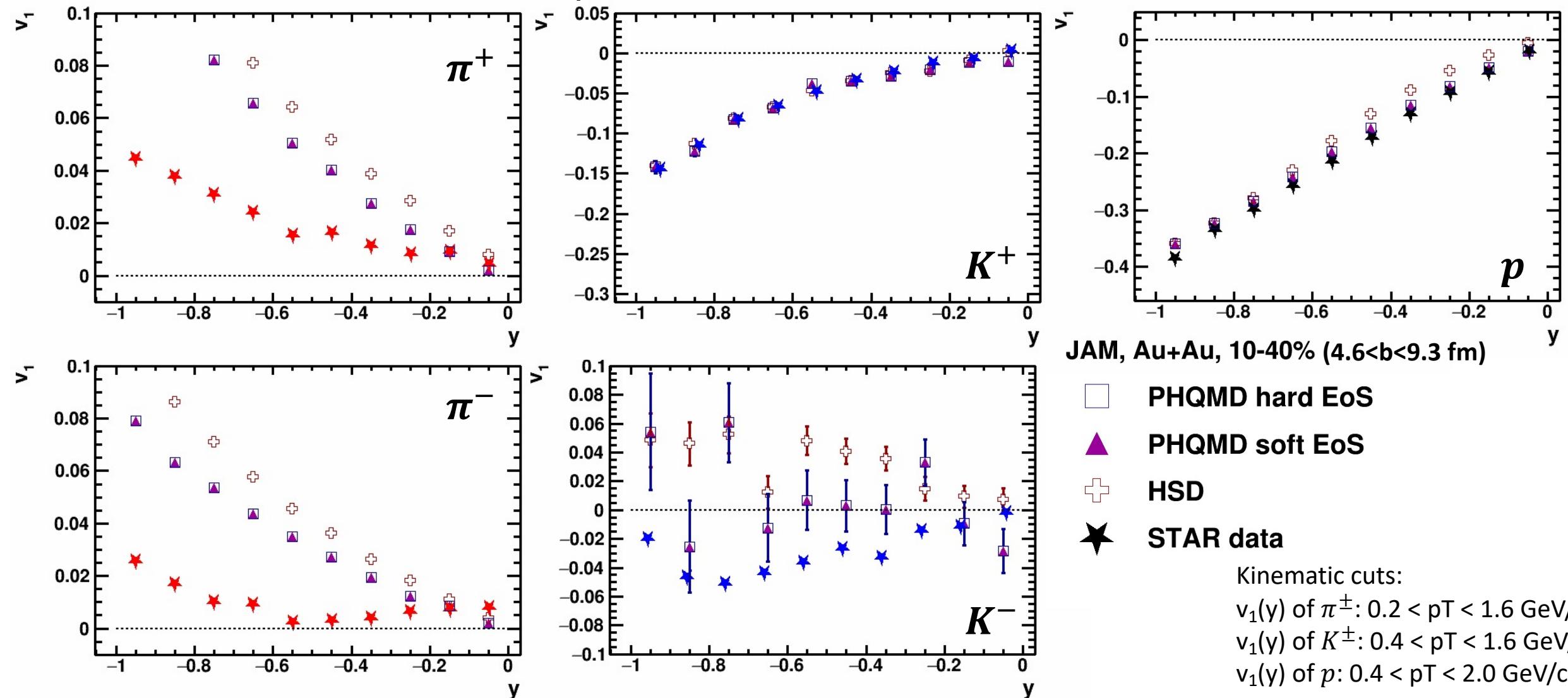
$v_2(p_T)$ :  $-1 < y < 0$

$v_2(y)$  of  $\pi^\pm$ :  $0.2 < p_T < 1.6$  GeV/c

$v_2(y)$  of  $p$ :  $0.4 < p_T < 2.0$  GeV/c

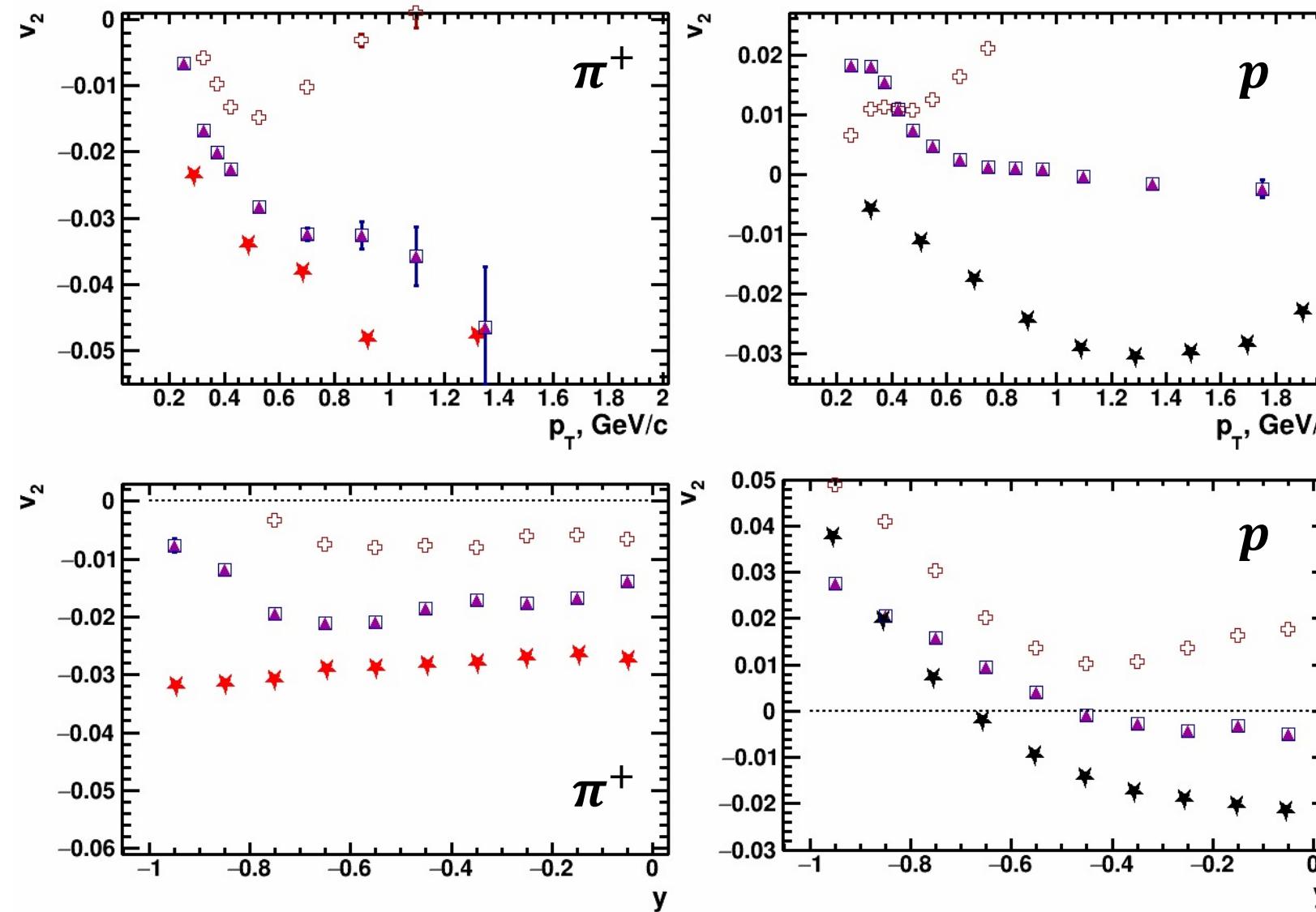
$v_2$  of pions and protons is more sensitive to different EOS than  $v_1$

# $v_1(y)$ in Au+Au $\sqrt{s_{NN}}=3$ GeV: model vs. STAR data



JAM does not describe all particle species equally well  
 $v_1$  of pions is most sensitive to different EOS

# $v_2(p_T, y)$ in Au+Au $\sqrt{S_{NN}}=3$ GeV: model vs. STAR data



JAM, Au+Au, 10-40% ( $4.6 < b < 9.3$  fm)

- PHQMD hard EoS
- ▲ PHQMD soft EoS
- + HSD
- ★ STAR data

Experimental data points:

M. Abdallah et al. [STAR Collaboration] 2108.00908 [nucl-ex]  
сократить

Kinematic cuts:

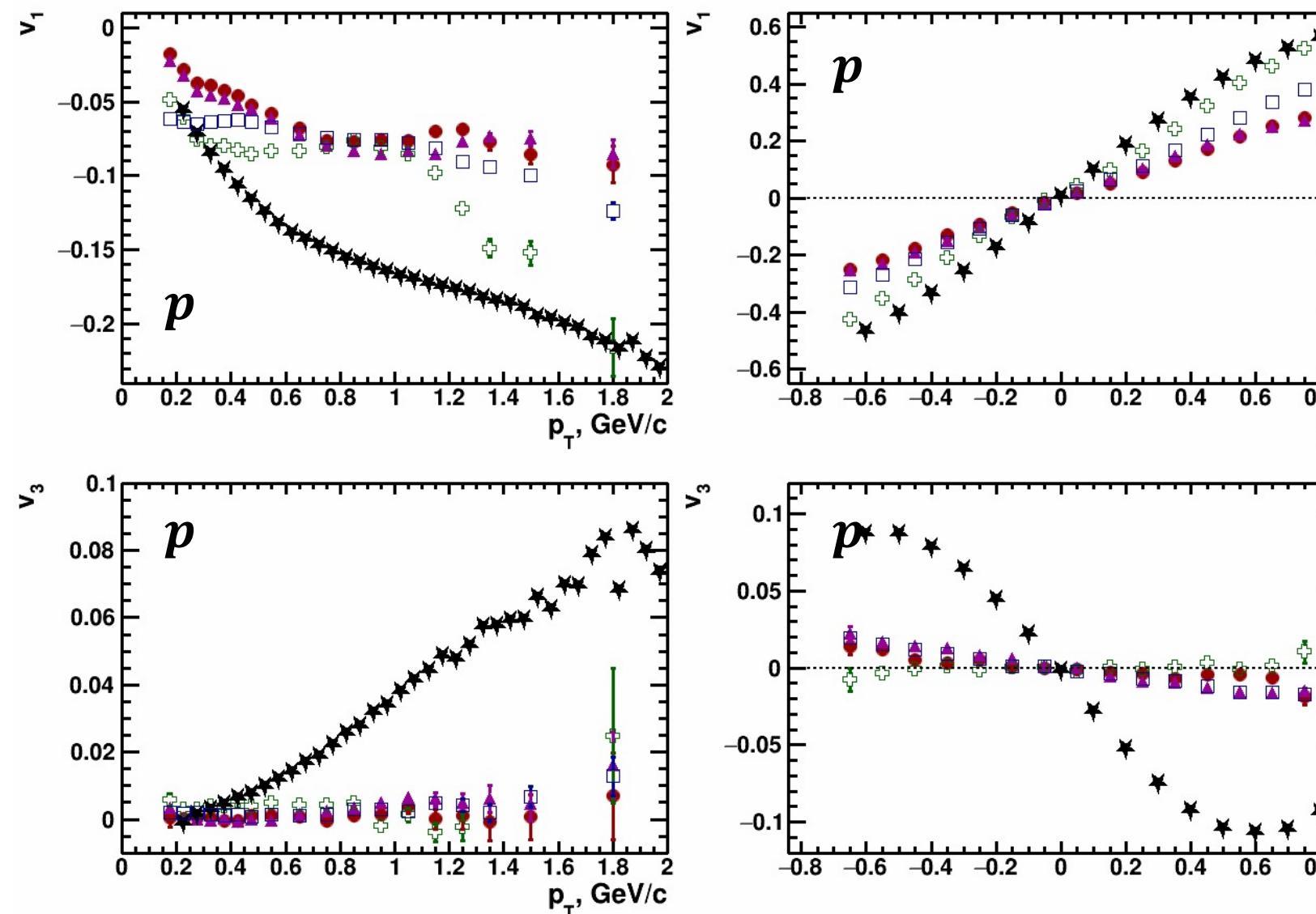
$v_2(p_T)$ :  $-1 < y < 0$

$v_2(y)$  of  $\pi^{\pm}$ :  $0.2 < p_T < 1.6$  GeV/c

$v_2(y)$  of  $p$ :  $0.4 < p_T < 2.0$  GeV/c

$v_2$  of pions and protons is more sensitive to different EOS than  $v_1$

# $v_{1,3}(p_T, y)$ in Au+Au $\sqrt{S_{NN}}=2.4$ GeV: cascade models



Au+Au, 20-30% (6< $b$ <9 fm)

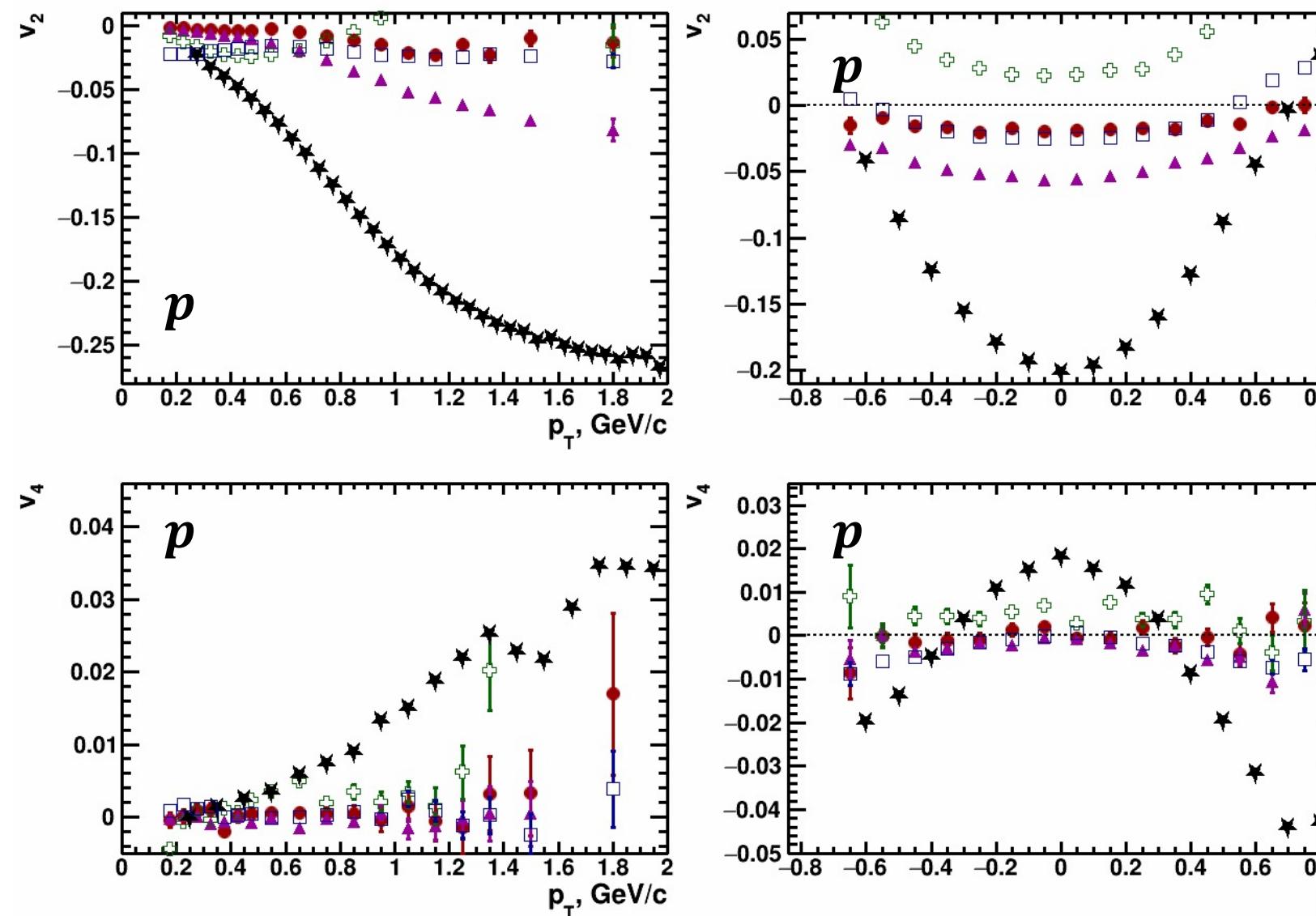
- DCM-QGSM-SMM
- UrQMD cascade
- ▲ JAM cascade
- + HSD cascade
- ★ HADES data

Experimental data points:  
Phys. Rev. Lett. **125** (2020) 262301

Kinematic cuts:  
 $V_{1,3}(p_T)$ :  $-0.25 < y < -0.15$   
 $V_{1,3}(y)$ :  $1.0 < pT < 1.5$  GeV/c

Models with cascade mode cannot reproduce the experimental data

# $v_{2,4}(p_T, y)$ in Au+Au $\sqrt{S_{NN}}=2.4$ GeV: cascade models



Au+Au, 20-30% (6< $b$ <9 fm)

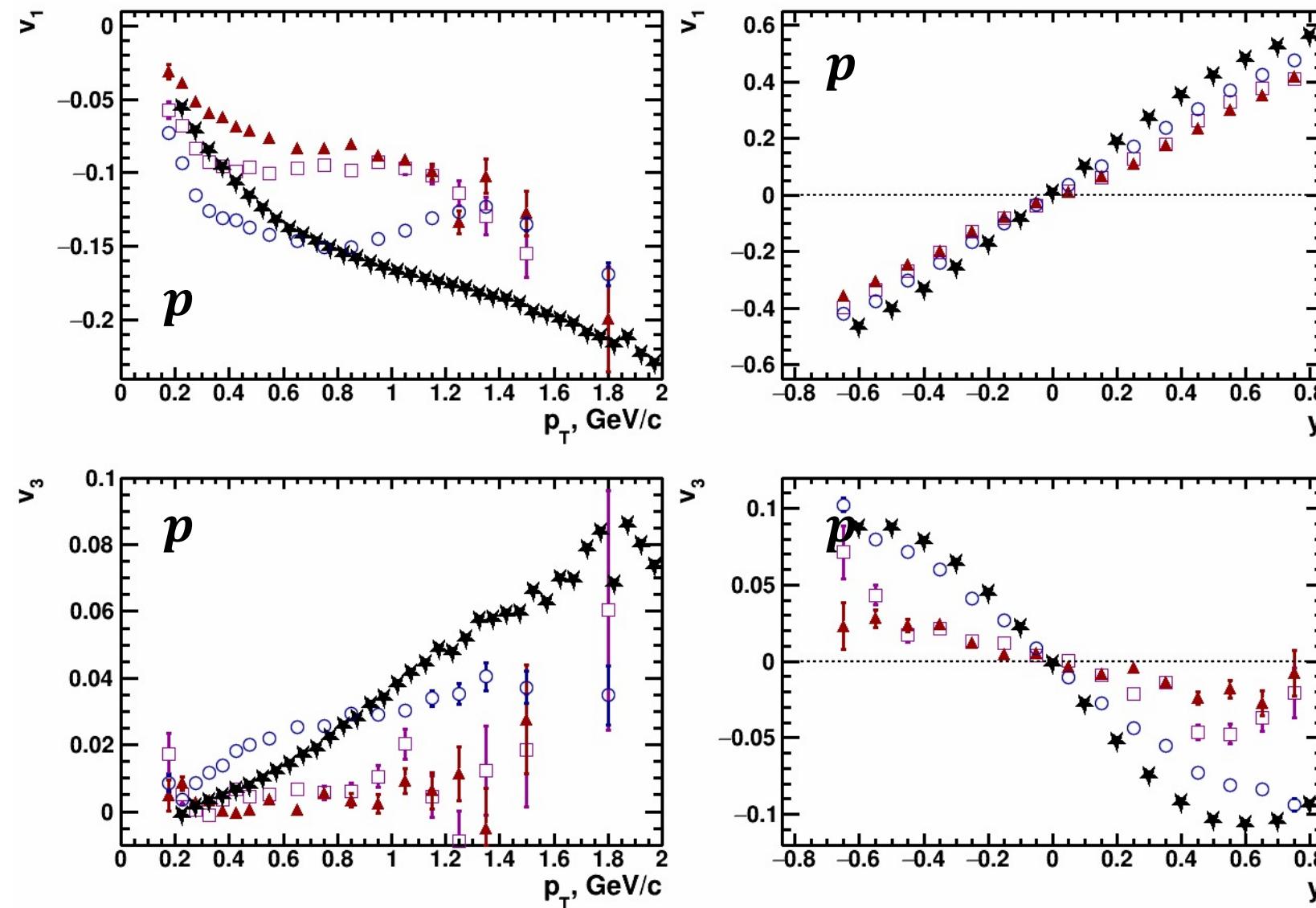
- DCM-QGSM-SMM
- UrQMD cascade
- ▲ JAM cascade
- + HSD cascade
- ★ HADES data

Experimental data points:  
Phys. Rev. Lett. **125** (2020) 262301

Kinematic cuts:  
 $V_{2,4}(p_T)$ :  $-0.05 < y < 0.05$   
 $V_{2,4}(y)$ :  $1.0 < pT < 1.5$  GeV/c

Models with cascade mode cannot reproduce the experimental data

# $v_{1,3}(p_T, y)$ in Au+Au $\sqrt{S_{NN}}=2.4$ GeV: mean-field models



Au+Au, 20-30% (6< $b$ <9 fm)

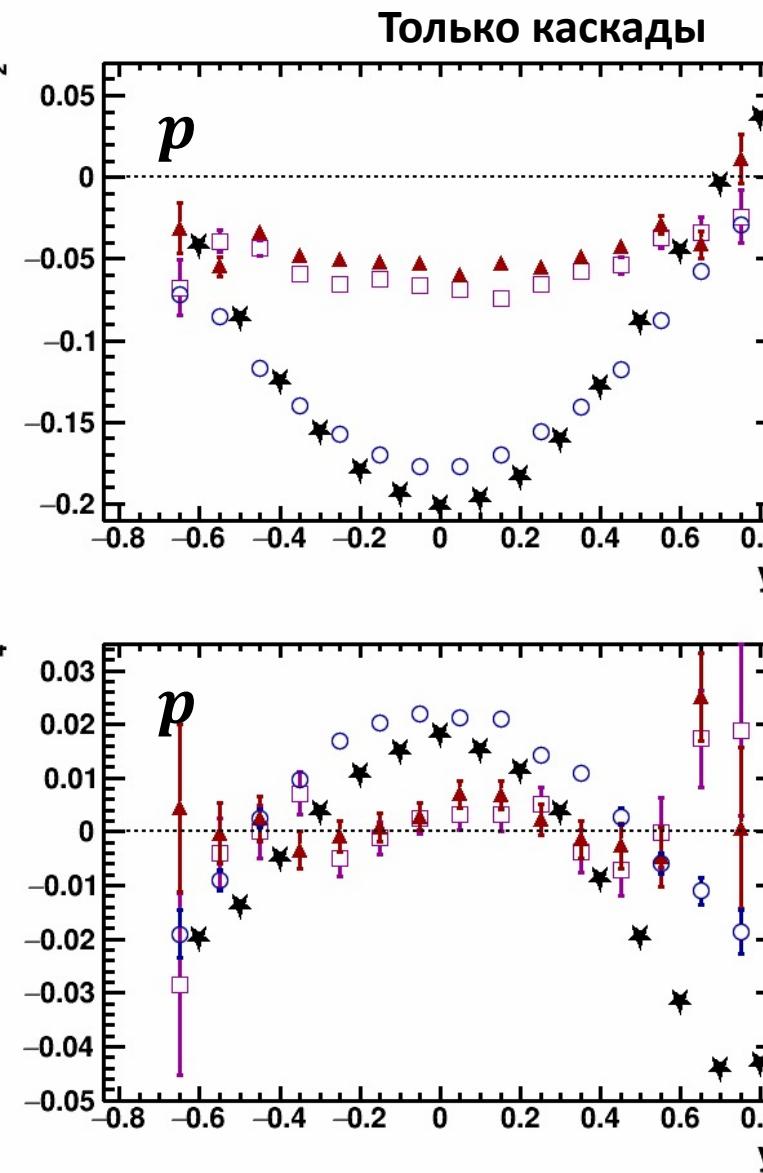
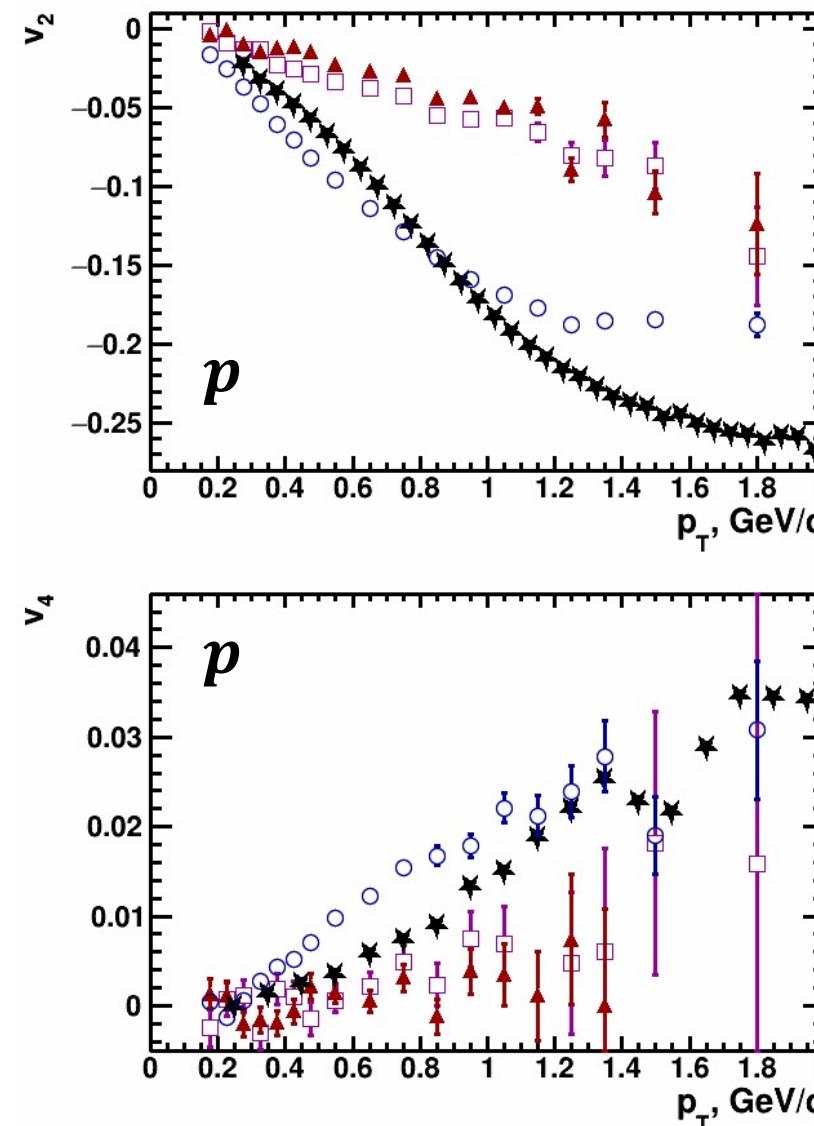
- UrQMD hardSkyrme
- PHQMD hard EoS
- ▲ PHQMD soft EoS
- ★ HADES data

Experimental data points:  
Phys. Rev. Lett. **125** (2020) 262301

Kinematic cuts:  
 $V_{1,3}(p_T)$ :  $-0.25 < y < -0.15$   
 $V_{1,3}(y)$ :  $1.0 < p_T < 1.5$  GeV/c

Models with cascade mode cannot reproduce the experimental data

# $v_{2,4}(p_T, y)$ in Au+Au $\sqrt{S_{NN}}=2.4$ GeV: mean-field models



Au+Au, 20-30% (6< $b$ <9 fm)

- UrQMD hardSkyrme
- PHQMD hard EoS
- ▲ PHQMD soft EoS
- ★ HADES data

Experimental data points:  
Phys. Rev. Lett. **125** (2020) 262301

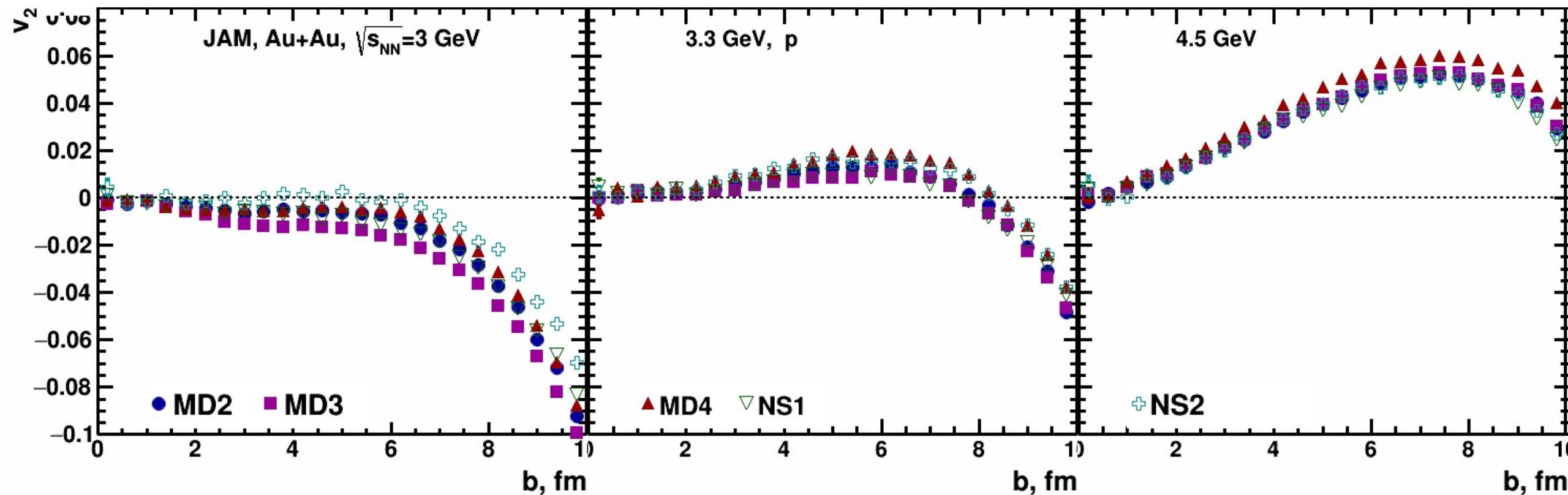
Kinematic cuts:  
 $V_{2,4}(p_T)$ :  $-0.05 < y < 0.05$   
 $V_{2,4}(y)$ :  $1.0 < p_T < 1.5$  GeV/c

Models with cascade mode cannot reproduce the experimental data

# $\nu_2(y)$ transition from out-of-plane to in-plane

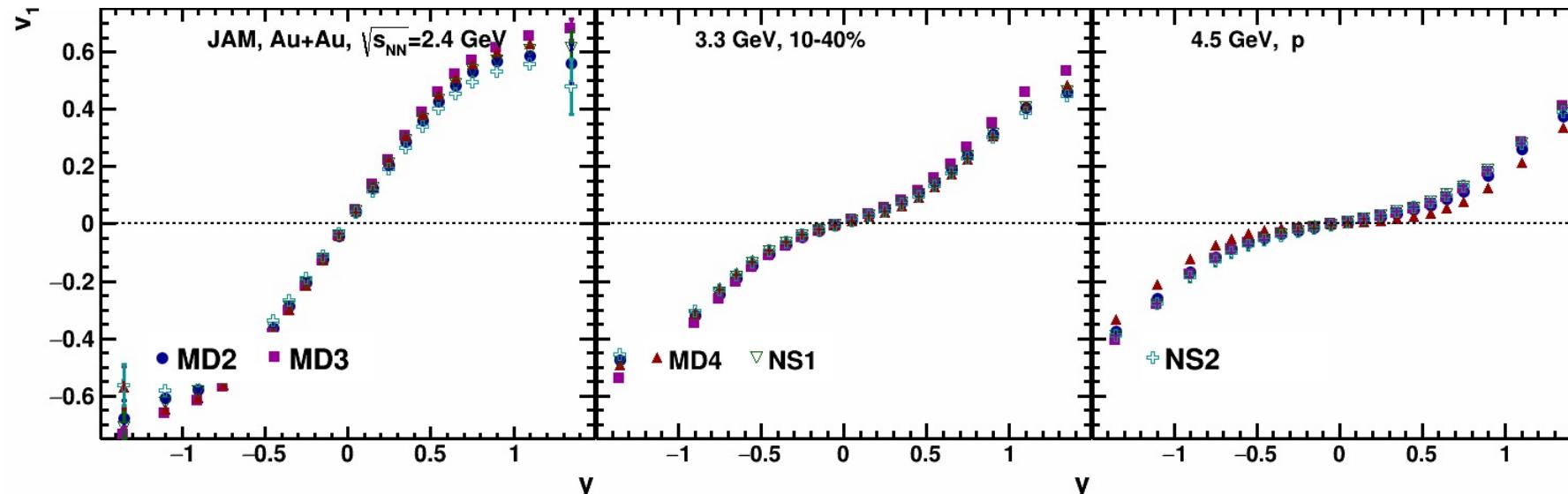
Protons:

$V_{2,4}(y)$ :  $1.0 < pT < 1.5 \text{ GeV}/c$ ;  $|y| < 0.2$



Transition of  $\nu_2$  from out-of-plane to in-plane depends on centrality and EoS

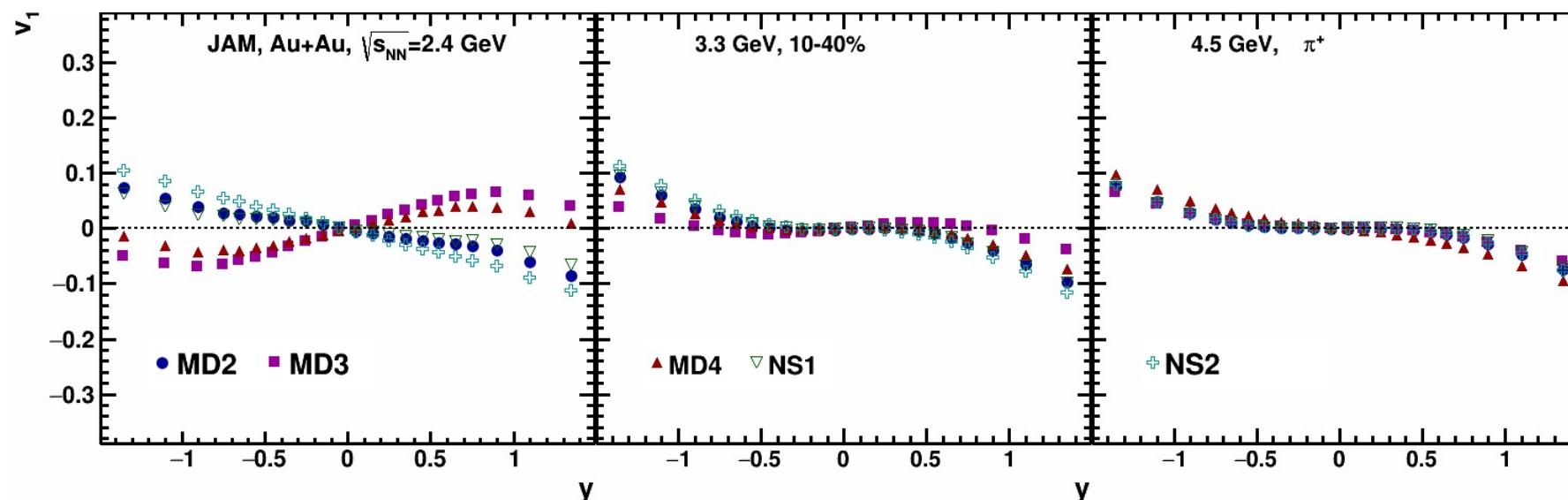
# $v_1(y)$ transition from out-of-plane to in-plane



**Protons:**  
 $v_1(y)$ :  $1.0 < pT < 1.5 \text{ GeV}/c$

**Pions:**  
 $v_1(y)$ :  $0.2 < pT < 0.5 \text{ GeV}/c$

Выбрать то, что чувствительно  
к EoS – найти такие переменные



- Weak dependence on EoS
- $v_2(p_T)$  strongly depends on centrality:
  - Transition from out-of-plane to in-plane depends on centrality
  - $v_2 < 0$  event at  $\sqrt{s_{NN}} = 4 \text{ GeV}$  in peripheral collisions