

Nonequilibrium meson production in strong fields.

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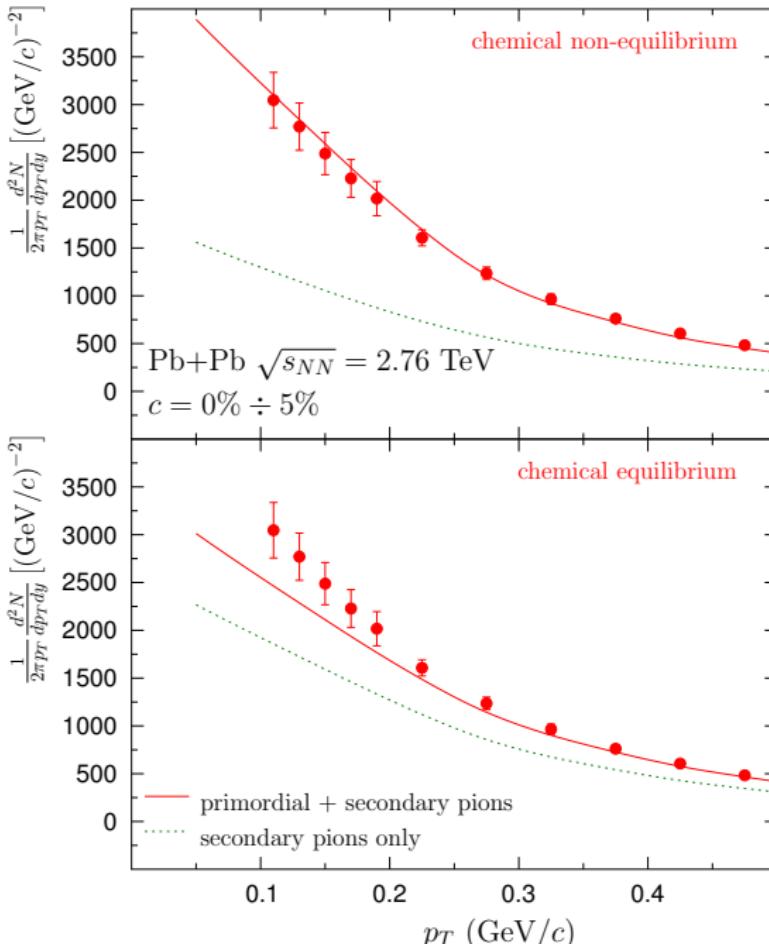
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Compact stars in the QCD Phase Diagram VI,
Dubna, September 27, 2017



Time dependent mass and dispersion relation

- Dispersion relation for σ and π

$$\omega_\sigma(t, \vec{p}) = \sqrt{m_\sigma(T(t))^2 + \vec{p}^2}, \quad \omega_\pi(\vec{p}) = \sqrt{m_\pi^2 + \vec{p}^2},$$

- The mass evolution of σ is governed by

$$m_\sigma(T(t)) = [m_\sigma(0) - m_\pi] \sqrt{1 - \frac{T(t)}{T_c}} + m_\pi, \quad T(t) = \frac{T_0 - t_0}{t}, \quad t \geq t_0,$$

- Temperature is given by

$$T(t) = \frac{T_0 - t_0}{t}, \quad t \geq t_0,$$

$$T(t) \leq T_c$$

Kinetic equation - assumptions

- Spatial homogeneity of distribution function $f_i(t, \vec{p})$

$$\frac{\partial f_i}{\partial \vec{x}} = 0$$

- Spatial isotropy
- The 3-dim expansion is governed by

$$\frac{df_i}{dt} = \frac{\partial f_i}{\partial t} - \frac{\dot{R}}{R} \mathbf{p} \cdot \frac{\partial f_i}{\partial \mathbf{p}}$$

- $R(t) = V \cdot t$ is radius of expanding fireball

J. Bernstein *Kinetic theory in the expanding universe* Cambridge Press 1988

Kinetic equation for π

$$\frac{\partial f_\pi}{\partial t}(t, \vec{p}_1) - \frac{\dot{R}(t)}{R(t)} \cdot \vec{p}_1 \frac{\partial f_\pi}{\partial \vec{p}_1} =$$

$$(1 + f_\pi(t, \vec{p}_1)) \left(\int d^3 p_\sigma \frac{d^3 p_2}{(2\pi)^3 4w_\sigma w_2} \Gamma_{\sigma \rightarrow \pi\pi}(\vec{p}_\sigma, \vec{p}_1, \vec{p}_2) (1 + f_\pi(t, \vec{p}_2)) f_\sigma(t, \vec{p}_\sigma) \right)$$

$$-f_\pi(t, \vec{p}_1) \left(\int d^3 p_\sigma \frac{d^3 p_2}{(2\pi)^3 4w_\sigma w_2} \Gamma_{\pi\pi \rightarrow \sigma}(\vec{p}_\sigma, \vec{p}_1, \vec{p}_2) f_\pi(t, \vec{p}_2) (1 + f_\sigma(t, \vec{p}_\sigma)) \right)$$

$R(t) = v_R \cdot t$ is radius of expanding fireball

J. Bernstein *Kinetic theory in the expanding universe* Cambridge Press 1988

Ł.Juchnowski, D.B.Blaschke, T.Fischer, S. A. Smolyansky, J.Phys.Conf.Ser. 673 (2016)
1, 012009

Kinetic equation for σ

$$\begin{aligned} \frac{\partial f_\sigma}{\partial t}(t, \vec{p}_\sigma) - \frac{\dot{R}(t)}{R(t)} \cdot \vec{p}_\sigma \frac{\partial f_\sigma}{\partial \vec{p}_\sigma} = \\ = \frac{\Delta_\sigma(t, \vec{p}_\sigma)}{2} \int_{t_0}^t dt' \Delta_\sigma(t', \vec{p}_\sigma) (1 + f_\sigma(t', \vec{x}, \vec{p}_\sigma)) \cos(2\theta_\sigma(t, t', \vec{p}_\sigma)) \\ + (1 + f_\sigma(t, \vec{p}_\sigma)) \left(\int d^3 p_1 \frac{d^3 p_2}{(2\pi)^6 4w_1 w_2} \Gamma_{\pi\pi \rightarrow \sigma}(\vec{p}_\sigma, \vec{p}_1, \vec{p}_2) f_\pi(t, \vec{p}_1) f_\pi(t, \vec{p}_2) \right) \\ - f_\sigma(t, \vec{p}_\sigma) \left(\int d^3 p_1 \frac{d^3 p_2}{(2\pi)^6 4w_1 w_2} \Gamma_{\sigma \rightarrow \pi\pi}(\vec{p}_\sigma, \vec{p}_1, \vec{p}_2) (1 + f_\pi(t, \vec{p}_1)) (1 + f_\pi(t, \vec{p}_2)) \right) \end{aligned}$$

The vacuum transition amplitude and dynamical phase

$$\Delta_\sigma(t, \vec{p}_\sigma) = \frac{m_\sigma}{w_\sigma^2} \frac{\partial m_\sigma}{\partial t}, \quad \theta_\sigma(t, t', \vec{p}_\sigma) = \int_{t'}^t dt'' w_\sigma(t'', \vec{p}_\sigma)$$

A.V Filatov, *et al.*, Phys. Part. Nucl. **39** 1116 (2008)

Schmidt, Blaschke *et al.* Int.J.Mod.Phys. E7 (1998) 709-722

Reaction rate

For the σ decay and regeneration we assume a constant matrix element $|M|^2 = \text{const}$ so that the momentum dependence of $\Gamma_{\sigma \rightarrow \pi\pi}$ is simply given by the momentum conserving delta-function

$$\begin{aligned}\Gamma_{\sigma \rightarrow \pi\pi}(\vec{p}_\sigma, \vec{p}_1, \vec{p}_2) &= (2\pi)^4 \delta^4(p_\sigma - p_1 - p_2) |M|^2 \\ &\rightarrow (2\pi)^4 \delta(w_\sigma - w_1 - w_2) \delta^3(\vec{p}_\sigma - \vec{p}_1 - \vec{p}_2).\end{aligned}$$

Elastic scattering

$$\frac{df_\pi(\varepsilon_1)}{dt} = \frac{|M_{fi}|^2}{64\pi^3\varepsilon_1} \int \int F(f) \frac{D}{p_1} d\varepsilon'_1 d\varepsilon'_2,$$

$$F(f) = [1 + f_1] [1 + f_2] f'_1 f'_2 - [1 + f'_1] [1 + f'_2] f_1 f_2 ,$$

$$D \equiv \min[p_1, p_2, p'_1, p'_2]$$

Semikoz, Tkachev, Phys. Rev. D 55, 489

Thermal initial conditions (LHC)

$$f_i(t_0, \vec{p}) = g_i \left[\exp(\sqrt{p^2 + m_i^2(T_0)/T_0}) - 1 \right]^{-1}, \quad i = \pi, \sigma.$$

$$T_0 = Tc = 170 \text{ MeV}$$

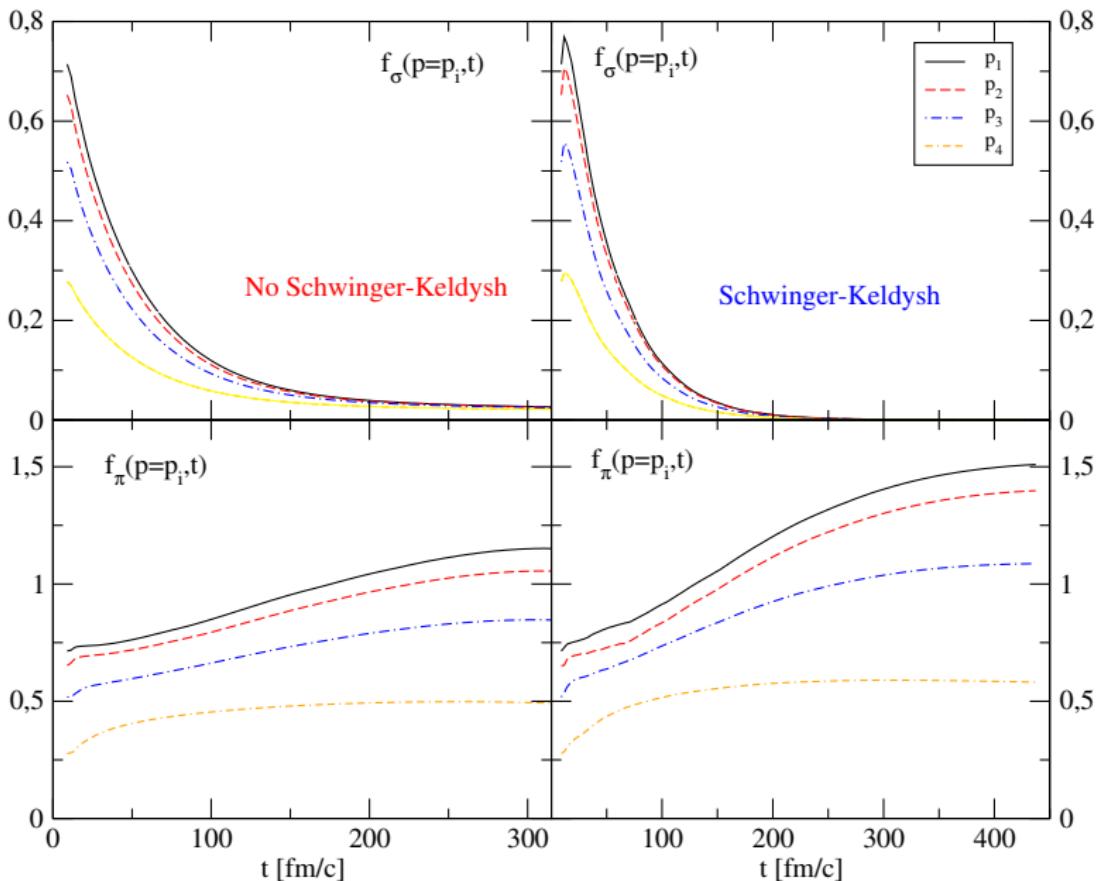
$$\mu = 0$$

$$t_0 = 9 \text{ fm/c}$$

$$m_\pi = 140 \text{ MeV}$$

$$m_\sigma(0) = 550 \text{ MeV}$$

Value of t_0 corresponding to a Hubble flow velocity of $v_R = 0.72 c$ for gold nuclei with radius $R_0 = 6.5 \text{ fm}$



$$p_1 = 5 \text{ MeV}, \quad p_2 = 50 \text{ MeV}, \quad p_3 = 100 \text{ MeV}, \quad p_4 = 200 \text{ MeV}$$

Enhancement factor

$$r = \frac{n_{\text{final}}}{n_{\text{initial}}} = \int_0^{\infty} dp p^2 f_{\pi}(t_f, \vec{p}) \Big/ \int_0^{\infty} dp p^2 f_{\pi}(t_0, \vec{p}) \quad (1)$$

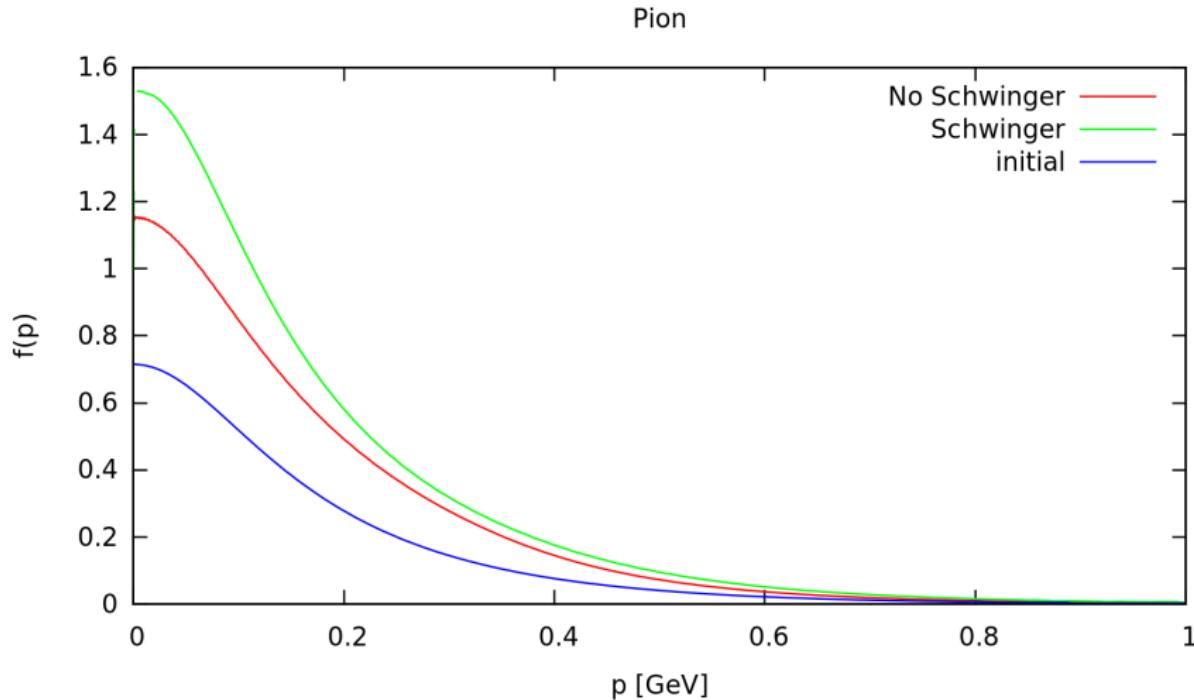
- in the presence of Keldysh-Schwinger process

$$r_+ = 2.57$$

- in the absence of Keldysh-Schwinger process

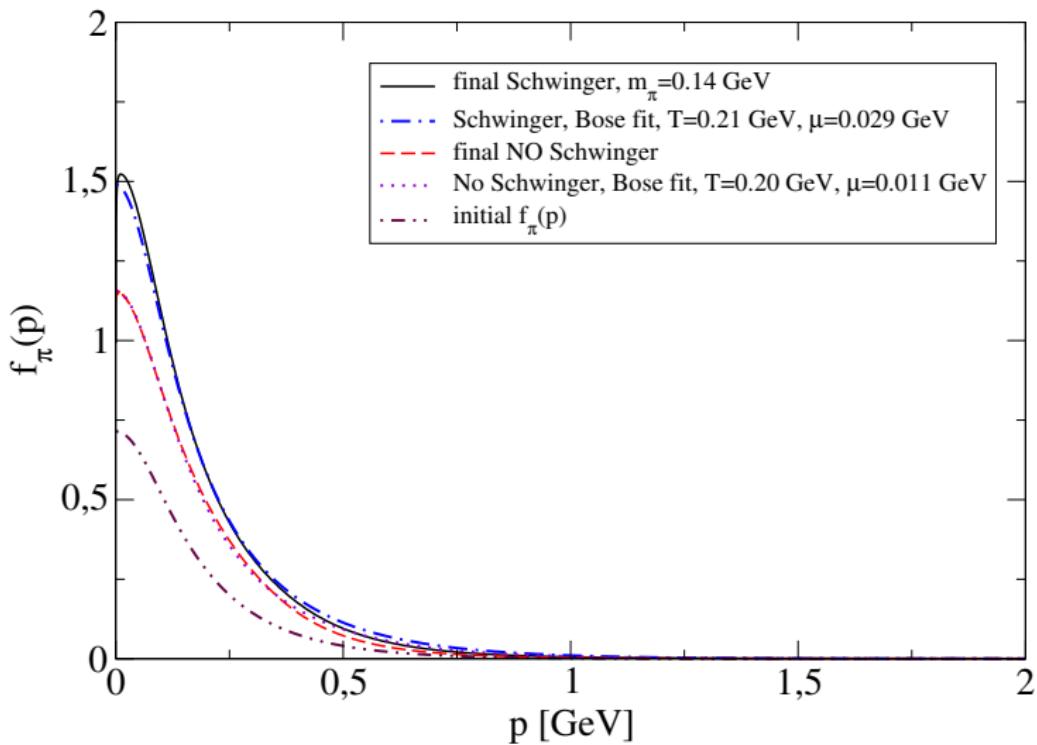
$$r_- = 2.08$$

Pion distribution function



$$r_+ = \frac{n_{\text{final}}}{n_{\text{initial}}} = 2.57 \quad r_- = 2.08$$

Pion distribution function



$$r_+ = \frac{n_{\text{final}}}{n_{\text{initial}}} = 2.57 \quad r_- = 2.08$$

Summary & Conclusion

- Expansion term

$$\frac{\dot{R}}{R} \mathbf{p} \cdot \frac{\partial f_i}{\partial \mathbf{p}}$$

and time dependent dispersion relation

$$\omega_\sigma(t, \vec{p}) = \sqrt{m_\sigma(T(t))^2 + \vec{p}^2}$$

seems to be main driving "force"

- Production ratio is not high \Rightarrow enhancement in partonic phase (?)
- More chiral physics is needed
- There is a need to study B-E condensation

$$\tilde{f} = f(\vec{p}, t) + (2\pi)^3 N_c(t) \delta^3(\vec{p})$$

To the future

- Full 3D solver instead of the expansion term
- Collision integrals evaluation with minimal number of approximations/assumptions
- Study of non-equilibrium effects in HIC/Supernovae
- Study dynamical Schwinger effect/inertial mechanism in HIC and supernovae

THE END

The resulting system of kinetic equations

$$\begin{aligned}
 \frac{\partial f_\sigma}{\partial t}(t, p_\sigma) &= \frac{\Delta_\sigma(t, p_\sigma)}{2} \int_{t_0}^t dt' \Delta_\sigma(t', p_\sigma) (1 + f_\sigma(t', p_\sigma)) \cos(2\theta_\sigma(t, t', p_\sigma)) \\
 &+ \frac{1}{8\pi} (1 + f_\sigma(t, p_\sigma)) \frac{1}{p_\sigma w_\sigma} \int_{p_1^-}^{p_1^+} p_1 dp_1 \frac{|M|^2}{w_1} f_\pi(t, p_1) f_\pi(t, p_2) \\
 &- \frac{1}{8\pi} f_\sigma(t, p_\sigma) \frac{1}{p_\sigma w_\sigma} \int_{p_1^-}^{p_1^+} p_1 dp_1 \frac{|M|^2}{w_1} (1 + f_\pi(t, p_1)) (1 + f_\pi(t, p_2)) \\
 \frac{\partial f_\pi}{\partial t}(t, p_1) &= \frac{1}{8\pi} (1 + f_\pi(t, p_1)) \frac{1}{p_1 w_1} \int_{p_\sigma^-}^{p_\sigma^+} p_\sigma dp_\sigma \frac{|M|^2}{w_\sigma} f_\sigma(t, p_\sigma) (1 + f_\pi(t, p_2)) \\
 &- \frac{1}{8\pi} f_\pi(t, p_1) \frac{1}{p_1 w_1} \int_{p_\sigma^-}^{p_\sigma^+} p_\sigma dp_\sigma \frac{|M|^2}{w_\sigma} f_\pi(t, p_2) (1 + f_\sigma(t, p_\sigma)) ,
 \end{aligned}$$

$$p_2 = p_2(\vec{p}_1; \vec{p}_\sigma)$$

$$p_1^\pm = \frac{1}{2} \left| p_\sigma \pm w_\sigma \sqrt{1 - \frac{4m_\pi^2}{m_\sigma^2}} \right|, \quad p_\sigma^\pm = \frac{m_\sigma^2}{m_\pi^2} \frac{1}{2} \left| p_1 \pm w_1 \sqrt{1 - \frac{4m_\pi^2}{m_\sigma^2}} \right|$$