## **B-** anomalies

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## Introduction

The Standard Model (SM) has been tested and confirmed by many experiments.

Nowadays, the focus has shifted beyond the SM by seeking new particles and new interactions.

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So far no new particles were observed directly at the Large Hadron Collider (LHC) at CERN.

Fortunately, there are indirect hints for new physics (NP)

## Introduction

Semileptonic *B*-meson decays via charged current  $(b \rightarrow c \ell \nu_{\ell})$ 

Rare **B**-meson decays via flavor changing neutral current  $(b \rightarrow s\ell^+\ell^-)$ 

The difference of the forward-backward asymmetry in the decays  $B \rightarrow D^* \mu \nu$  vs  $B \rightarrow D^* e \nu \ (\Delta A_{\rm FB})$ 

The anomalous magnetic moment of the muon  $(a_{\mu})$ 

All these observables admit an interpretation in terms of Lepton Flovor Universality Violation (LFUV), i.e. NP that distinguishes between muon, electrons and tau leptons.

Three generations of leptons in the Standard Model (SM):

$$\left(egin{array}{c} 
u_e \ e^- \end{array}
ight), \quad \left(egin{array}{c} 
u_\mu \ \mu^- \end{array}
ight), \quad \left(egin{array}{c} 
u_ au \ au^- \end{array}
ight).$$

The SM assumes that the interactions of leptons are universal, i.e. the same for the three generations, and differ only because of their different masses.

Therefore, if we refer to LFUV we mean interactions with different couplings to electrons, muons and tau leptons (disregarding phase space effects) that directly distinguish among the leptons at the Lagrangian level.

#### $b \rightarrow c \tau \nu$

This charged current transition is already mediated at tree-level in the SM and the corresponding decays have significant branching ratios ( $\mathcal{O}(10^{-3})$ ).

**•** The differential decay rate,  $d\Gamma$ , for semileptonic decays involving  $D^{(*)}$  mesons depends on both  $m_{\ell}^2$  and  $q^2$ , the invariant mass squared of the lepton pair

$$\frac{\mathrm{d}\Gamma^{\mathrm{SM}}(\bar{B} \to D^{(*)}\ell^{-}\bar{\nu}_{\ell})}{\mathrm{d}q^{2}} = \underbrace{\frac{G_{F}^{2} |V_{cb}|^{2} |p_{D^{(*)}}^{*}| q^{2}}{96\pi^{3}m_{B}^{2}} \left(1 - \frac{m_{\ell}^{2}}{q^{2}}\right)^{2}}_{\text{universal and phase space factors}} \times \underbrace{\left[\left(|H_{+}|^{2} + |H_{-}|^{2} + |H_{0}|^{2}\right) \left(1 + \frac{m_{\ell}^{2}}{2q^{2}}\right) + \frac{3m_{\ell}^{2}}{2q^{2}}|H_{s}|^{2}\right]}_{\text{hadronic effects}} .$$
(1)

▶  $p_{D(*)}^*$  is the 3-momentum of the hadron in the *B* rest frame. The four helicity amplitudes  $H_{\pm}$ ,  $H_0$ ,  $H_s$  capture the impact of hadronic effects. They depend on the spin of the charm meson and on  $q^2$ :  $m_{\ell}^2 \leq q^2 \leq (m_B - m_{D^*})^2$ .

#### $b \rightarrow c \tau \nu$

Measurements of the ratios of semileptonic branching fractions remove the dependence on  $|V_{cb}|$ , lead to a partial cancellation of theoretical uncertainties related to hadronic effects, and reduce of the impact of experimental uncertainties.

#### Here the ratios

$$R(D^{(*)}) = \frac{\mathcal{B}(B \to D^{(*)} \tau \nu_{\tau})}{\mathcal{B}(B \to D^{(*)} \ell \nu_{\ell})}, \quad D^{(*)} = D \text{ or } D^*, \quad \ell = e \text{ or } \mu$$

**Current SM predictions** 

 $R^{\rm SM}(D) = 0.299 \pm 0.003, \qquad R^{\rm SM}(D^*) = 0.258 \pm 0.005$ 

to be compared with the averages of the experimantal measurements

 $R(D) = 0.340 \pm 0.030, \qquad R(D^*) = 0.295 \pm 0.014.$ 

There is deviation around  $3\sigma$ .

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#### $b \rightarrow c \tau \nu$

The LHCb collaboration reported about measurement of the ratio of semileptonic branching fractions  $R(J/\psi)$ :

$$R(J/\psi)=rac{\mathcal{B}(B_c^+
ightarrow J/\psi au^+
u_ au)}{\mathcal{B}(B_c^+
ightarrow J/\psi\mu^+
u_\mu)}=0.71\pm0.25.$$

R. Aaij et al. [LHCb], Phys. Rev. Lett. 120, no.12, 121801 (2018) [arXiv:1711.05623 [hep-ex]]

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This result lies within  $2\sigma$  deviations of the range of central values predicted from the Standard Model, 0.24 to 0.29. Thereby, the above results are supported by this measurement.

## $b ightarrow s \ell^+ \ell^-$

The flavor changing neutral current processes  $b \to s \ell^+ \ell^-$  transitions are loop and CKM suppressed in the SM, resulting in branching ratios which are of  $10^{-6}$ 

The ratios

$$R(K^{(*)}) = \frac{\mathcal{B}(B \to K^{(*)}\mu^+\mu^-)}{\mathcal{B}(B \to K^{(*)}e^+e^-)}$$

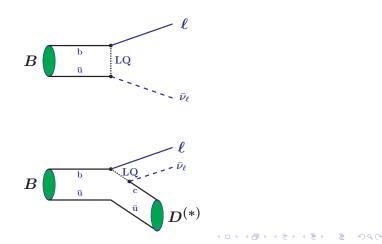
are particularly prominent. They are measured by LHCb and Belle and their theory predictions are very clean (within the SM) since the dependence on the form factors drops out to an excellent approximation. The experimental results obtained for several bins are compatible with the SM expectations at the level of  $2.1 - 2.5 \sigma$ .

There are some  $b \rightarrow s\ell^+\ell^-$  transitions that deviate from the SM predictions:

- the optimized angular decay observable  $P_5^{\prime \mu}$
- ▶ the total branching ratios  $\mathcal{B}(B \to K^* \mu^+ \mu^-)$ ,  $\mathcal{B}(B \to K \mu^+ \mu^-)$  and  $\mathcal{B}(B_s \to \phi \mu^+ \mu^-)$
- ▶ the purely leptonic decay  $B_s \rightarrow \mu^+ \mu^-$  displays a tension.

#### Theoretical attempts to explain

- A charged Higgs boson H<sup>-</sup> in two-Higgs doublet models. The H<sup>-</sup> would mediate weak decays, similar to the W<sup>-</sup>, but couple differently to leptons of different mass.
- LeptoQuarks = LQ, hypothetical particles with both electric and color charges that allow transitions from quarks to leptons and vice versa.



Weak decays of hadrons are mediated by weak interactions of their quark constituents.

The goal is to derive an effective theory of quarks at energy scale of the order 1 GeV.

The theoretical framework is provided by the operator product expansion (OPE).

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It allows to separate short- and long- distance dynamics.

## **Effective theories**

The short-distance effects can be treated **perturbatively** in terms of four-fermion operators.

The long-distance effects are encoded in hadronic matrix elements of these operators. Their calculation requires information about the structure of hadrons and therefore cannot be done in perturbation theory.

A variety of theoretical approaches have been applied to this problem.

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#### Example: $b \rightarrow c \bar{u} s$ -quark transitions

The *W*-exchange tree-level amplitude:

$$-\frac{g_{2}^{2}}{8}V_{us}^{\dagger}V_{cb} \ (\bar{s}O^{\mu}u)\left[\frac{-g_{\mu\nu}}{M_{W}^{2}-k^{2}}\right](\bar{c}O^{\nu}b)$$

The momentum transfer  $|k| \ll M_W$ :

$$\frac{-g_{\mu\nu}}{M_W^2 - k^2} \longrightarrow \frac{-g_{\mu\nu}}{M_W^2} \equiv -\left(\frac{8}{g_2^2}\right) \left(\frac{G_F}{\sqrt{2}}\right) g_{\mu\nu}$$

Thus we arrive at effective Hamiltonian

$$\mathcal{H}_{\mathrm{eff}}^{\mathrm{tree}} = rac{G_F}{\sqrt{2}} V_{us}^{\dagger} V_{cb} Q_2, \qquad Q_2 \equiv (\bar{s}_{\alpha} O^{\mu} u_{\alpha}) (\bar{c}_{\beta} O_{\mu} b_{\beta})$$

By taking into account QCD corrections:

$$\begin{aligned} \mathcal{H}_{\text{eff}} &= \frac{G_F}{\sqrt{2}} V_{us}^{\dagger} V_{cb} \left[ C_1(\mu) Q_1 + C_2(\mu) Q_2 \right], \\ Q_1 &\equiv (\bar{s}_{\alpha} O^{\mu} u_{\beta}) (\bar{c}_{\beta} O_{\mu} b_{\alpha}) \end{aligned}$$

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## **Effective Hamiltonian**

Using the operator product expansion (OPE) formalism and renormalization group techniques, the effective Hamiltonian of the weak decays is derived.

$$\mathcal{A}(f \to i) = \langle f | \mathcal{H}_{\text{eff}} | i \rangle = \frac{G_F}{\sqrt{2}} \lambda_{\text{CKM}} \sum_{k} \underbrace{C_k(\mu)}_{\text{SD}} \underbrace{\langle f | Q_k(\mu) | i \rangle}_{\text{LD}}$$

- SD = Short-Distance contributions
- LD = Long-Distance contributions
- The Wilson coefficients  $C_i(\mu)$  are calculated by using "matching" the full and effective theories, and the renormalization group.
- $Q_k(\mu)$  are the local operators generated by electroweak interactions and QCD
- The problem is to evaluate the matrix elements  $\langle f | Q_k(\mu) | i \rangle$

#### Covariant confined quark model

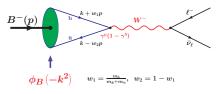
# $\begin{aligned} & \mathsf{Quark \ currents} \\ J_M(x) &= \int dx_1 \int dx_2 \ F_M(x; x_1, x_2) \cdot \bar{q}_{f_1}^a(x_1) \ \Gamma_M \ q_{f_2}^a(x_2) & \mathsf{Meson} \\ J_B(x) &= \int dx_1 \int dx_2 \int dx_3 \ F_B(x; x_1, x_2, x_3) & \mathsf{Baryon} \\ & \times \ \Gamma_1 \ q_{f_1}^{a_1}(x_1) \left[ \varepsilon^{a_1 a_2 a_3} q_{f_2}^{T \ a_2}(x_2) C \ \Gamma_2 \ q_{f_3}^{a_3}(x_3) \right] \end{aligned}$

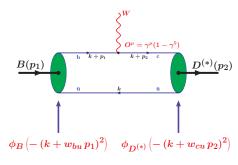
$$J_{T}(x) = \int dx_{1} \dots \int dx_{4} F_{T}(x; x_{1}, \dots, x_{4})$$
 Tetraquark  
  $\times \left[ e^{a_{1}a_{2}c} q_{f_{1}}^{T a_{1}}(x_{1}) C\Gamma_{1} q_{f_{2}}^{a_{2}}(x_{2}) \right] \cdot \left[ e^{a_{3}a_{4}c} \bar{q}_{f_{3}}^{T a_{3}}(x_{3}) \Gamma_{2}C \bar{q}_{f_{4}}^{a_{4}}(x_{4}) \right]$ 

## Vertex functions

$$F_H(x; x_1, \ldots, x_n) = \delta\left(x - \sum_{i=1}^n w_i x_i\right) \Phi_H\left(\sum_{i < j} (x_i - x_j)^2\right), \quad w_i = \frac{m_i}{\sum_{i=1}^n m_j}$$

## **Matrix elements**





$$w_{bu} = rac{m_u}{m_b + m_u}$$
  $w_{cu} = rac{m_u}{m_c + m_u}$ 

# Leptonic decay constants

#### **Pseudoscalar mesons**

$$N_c g_P \int \frac{d^4 k}{(2\pi)^4 i} \widetilde{\Phi}_P(-k^2) \operatorname{tr} \left[ O^{\mu} S_1(k+w_1 p) \gamma^5 S_2(k-w_2 p) \right] = f_P p^{\mu}$$

#### **Vector mesons**

$$N_c g_V \int \frac{d^4k}{(2\pi)^4 i} \widetilde{\Phi}_V(-k^2) \operatorname{tr} \left[ O^{\mu} S_1(k+w_1p) \not\in_V S_2(k-w_2p) \right] = m_V f_V \epsilon_V^{\mu}$$

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# Analyzing New Physics in the decays $B \rightarrow D^{(*)} \tau \nu_{\tau}$

M.A. Ivanov, J.G. Körner and C.T. Tran, Phys. Rev. D 94, no.9, 094028 (2016)

Effective Hamiltonian for the quark-level transition  $b \rightarrow c \tau^- \bar{\nu}_{\tau}$ :

$$\mathcal{H}_{eff} \propto G_F \, V_{cb} \left[ (1 + V_L) \mathcal{O}_{V_L} + V_R \mathcal{O}_{V_R} + S_L \mathcal{O}_{S_L} + S_R \mathcal{O}_{S_R} + T_L \mathcal{O}_{T_L} \right]$$

where the four-fermion operators are written as

- $\mathcal{O}_{V_L} = (\bar{c}\gamma^{\mu}P_Lb)(\bar{\tau}\gamma_{\mu}P_L\nu_{\tau}) \qquad \mathcal{O}_{V_R} = (\bar{c}\gamma^{\mu}P_Rb)(\bar{\tau}\gamma_{\mu}P_L\nu_{\tau})$
- $\mathcal{O}_{S_L} = (\bar{c}P_L b) (\bar{\tau}P_L \nu_{\tau}) \qquad \mathcal{O}_{S_R} = (\bar{c}P_R b) (\bar{\tau}P_L \nu_{\tau})$

$$\mathcal{O}_{T_L} = (\bar{c}\sigma^{\mu\nu}P_Lb)(\bar{\tau}\sigma_{\mu\nu}P_L\nu_{\tau})$$

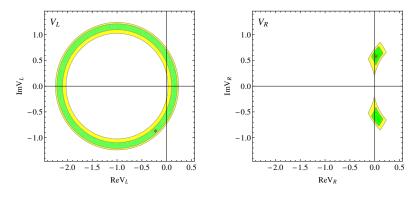
- Here,  $\sigma_{\mu\nu} = i [\gamma_{\mu}, \gamma_{\nu}]/2$ ,  $P_{L,R} = (1 \mp \gamma_5)/2$ .
- $\blacktriangleright$  V<sub>L,R</sub>, S<sub>L,R</sub>, and T<sub>L</sub> complex Wilson coefficients governing NP.

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- ▶ In the SM:  $V_{L,R} = S_{L,R} = T_L = 0$ .
- Neutrino is always left handed.
- NP only affects leptons of the third generation.

# Allowed regions for NP couplings

Assuming that besides the SM contribution, only one of the NP operators is switched on at a time, and NP only affects the tau modes.

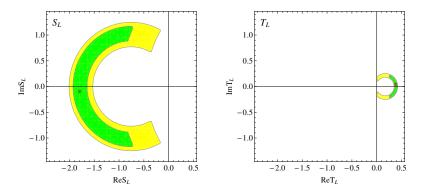


The allowed regions of the Wilson coefficients  $V_{L,R}$  within  $2\sigma$  (green, dark) and  $3\sigma$  (yellow, light).

The best fit value in each case is denoted with the symbol \*.

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## Allowed regions for NP couplings



The allowed regions of the Wilson coefficients  $S_L$ , and  $T_L$  within  $2\sigma$  (green, dark) and  $3\sigma$  (yellow, light).

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## Allowed regions for NP couplings

- It is important to note that while determining these regions, we also take into account a theoretical error of 10% for the ratios  $R(D^{(*)})$ .
- **•** The operator  $\mathcal{O}_{S_R}$  is excluded at  $2\sigma$  and is not presented here.
- In each allowed region at  $2\sigma$  we find the best-fit value for each NP coupling.

 $V_L = -1.33 + i \, 1.11,$   $V_R = 0.03 - i \, 0.60,$  $S_L = -1.79 - i \, 0.22,$   $T_L = 0.38 - i \, 0.06.$ 

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#### Form-factor-independent test of lepton universality

S. Groote, M. A. Ivanov, J. G. Körner, V. E. Lyubovitskij, P. Santorelli and C. T. Tran, Phys. Rev. D 103, no.9, 093001 (2021)

Generic differential  $(q^2, \cos \theta)$  distribution for the semileptonic decays

$$ar{B}^0 o D^{(*)+} \ell^- ar{
u}_\ell, \qquad B_c^- o J/\psi(\eta_c) \ell^- ar{
u}_\ell, \qquad \Lambda_b o \Lambda_c \ell^- ar{
u}_\ell$$

is written as

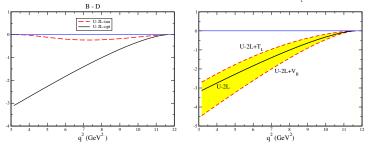
$$\frac{d^2\Gamma(q^2,\ell)}{dq^2\,d\,\cos\theta} \propto \,\boldsymbol{v}^2\Big(A_0(q^2,\ell) + A_1(q^2,\ell)\cos\theta + \boldsymbol{v}\,A_2(q^2)\cos^2\theta\Big)$$

The velocity type factor  $v = 1 - m_{\ell}^2/q^2$  factors out in the quadratic  $\cos^2 \theta$  coefficient. Therefore one can define an optimized partial rates:  $d\Gamma^{\text{opt}}(q^2)/dq^2 \propto A_2(q^2)$  which are the same in the SM for all three  $(e, \mu, \tau)$  modes in the common phase space  $m_{\tau}^2 < q^2 \leq (m_1 - m_2)^2$ :

$$|d\Gamma^{\mathrm{opt}}(q^2)|_e = d\Gamma^{\mathrm{opt}}(q^2)|_{\mu} = d\Gamma^{\mathrm{opt}}(q^2)|_{\tau}$$

This equality is form-factor independent. In this way one can test  $\mu/e$ ,  $\tau/\mu$  and  $\tau/e$  lepton universality regardless of form-factor effects. New Physics (NP) contributions designed to strengthen the  $\tau$  rate will clearly lead to a violation of these equalities.

## Form-factor-independent test of lepton universality



 $B \rightarrow D + \tau + \overline{\nu}$ 

Left panel:  $q^2$  dependence of the optimized partial rate  $d\Gamma_{U-2L}^{optd}/dq^2$  (solid curve) and  $d\Gamma_{U-2L}/dq^2 = v^3 d\Gamma_{U-2L}^{optd}/dq^2$  ( $\tau$ -mode, dashed curve) in units of  $10^{-15}$  GeV<sup>-1</sup> Right panel:  $P \rightarrow P'$  (V) semileptonic transitions taking into account NP effects for the  $\tau$  mode.

The optimized partial rate  $\Gamma_{U-2L}^{optd}$  in units of  $10^{-14}$  GeV

$q_{\min}^2$	$B \rightarrow D$	$B_c  ightarrow \eta_c$	$B  ightarrow D^*$	$B_c  ightarrow J/\psi$	$\Lambda_b - \Lambda_c$
$m_{ au}^2$	-1.14	-1.21	-0.73	-0.49	-0.90
$4 \text{ GeV}^2$	-0.89	-0.93	-0.54	-0.36	-0.71

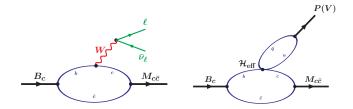
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The decays 
$${\it B_c} 
ightarrow {\it J}/\psi + ar{\ell} 
u_\ell$$
 and  ${\it B_c} 
ightarrow {\it J}/\psi + \pi({\it K})$ 

A. Issadykov and M.A. Ivanov, Phys. Lett. B 783, 178-182 (2018)

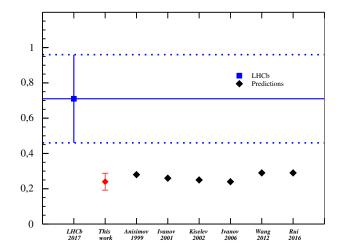
The LHCb Collaboration reported on the measurements of the ratios of the branching fractions:

$$\begin{aligned} \mathcal{R}_{\pi^{+}/\mu^{+}\nu} &= \frac{\mathcal{B}(B_{c}^{+} \to J/\psi\pi^{+})}{\mathcal{B}(B_{c}^{+} \to J/\psi\mu^{+}\nu_{\mu})} = 0.0469 \pm 0.0028(\text{stat}) \pm 0.0046(\text{syst}) \\ \mathcal{R}_{K^{+}/\pi^{+}} &= \frac{\mathcal{B}(B_{c}^{+} \to J/\psiK^{+})}{\mathcal{B}(B_{c}^{+} \to J/\psi\pi^{+})} = \begin{cases} 0.069 \pm 0.019(\text{stat}) \pm 0.005(\text{syst}) \\ 0.079 \pm 0.007(\text{stat}) \pm 0.003(\text{syst}) \end{cases} \\ \mathcal{R}_{J/\psi} &= \frac{\mathcal{B}(B_{c}^{+} \to J/\psi\tau^{+}\nu_{\tau})}{\mathcal{B}(B_{c}^{+} \to J/\psi\mu^{+}\nu_{\mu})} = 0.71 \pm 0.17(\text{stat}) \pm 0.18(\text{syst}) \end{aligned}$$



Pictorial representation of the semileptonic and nonleptonic  $B_c$  decays in the CCQM.

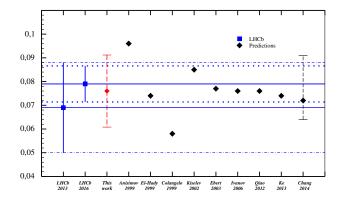
Theoretical predictions vs. LHCb data for the ratio  $\mathcal{R}_{\mathcal{J}/\psi}$ 



Solid line-central experimental value, dotted lines-experimental error bar.

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# Theoretical predictions vs. LHCb data for the ratio $\mathcal{R}_{\mathcal{K}^+/\pi^+}$



Two solid lines- central experimental values, dash-dotted and dotted lines –experimental error bar from two LHCb-experiments.

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#### Some observations

- ► The theoretical predictions for the ratio  $\mathcal{R}_{J/\psi}$  are more than 2  $\sigma$  less than the experimental data. This may indicate on the possibility of New physics effects in this decay since it is similar to the ratio  $\mathcal{R}_{D}(*)$ .
- At the same time the theoretical predictions for the ratio  $\mathcal{R}_{K/\pi}$  are well consistent with the experimental data. This might be very important since it may imply that the new physics (if there is any) has strong couplings to the leptons but not hadrons.
- Such a comparison is very difficult in the  $B \to D^{(*)} K(\pi)$  case since these processes are described not only by one tree diagram but sum of the different tree diagram (color-allowed, color-suppressed, annihilation), which induces more hadronic parameters.
- ► So the  $B_c \rightarrow J/\psi K(\pi)$  channels, coming only from color-allowed tree diagram, can be used as a better test of this observation.
- ▶ Indeed, since the  $H_t^{B_c \to J/\psi}(m_K^2) \approx H_t^{B_c \to J/\psi}(m_\pi^2)$  in our model then

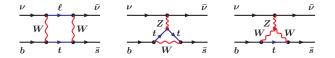
$$\mathcal{R}_{K/\pi} pprox rac{|V_{us}|^2}{|V_{ud}|^2} rac{f_K^2}{f_\pi^2} pprox 0.076$$

that fits very well the last LHCb-data.

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## The rare decay $B \rightarrow K(K^*) + \nu \bar{\nu}$

One loop diagrams giving the leading contributions to the transition  $b \rightarrow s + \nu \bar{\nu}$ 



**Effective Hamiltonian:** 

$$\mathcal{H}_{\rm eff} = \frac{G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[ \frac{\alpha_{em}}{2\pi} \frac{X_t}{\sin^2 \theta_W} \right] (\bar{s} O_\mu b) (\bar{\nu} O^\mu \nu) + {\rm h.c.}$$

The function  $X_t$  is calculated in the leading order (LO) plus subleading contributions. The results of such precision calculations are given by

 $X_t = 1.469 \pm 0.017$ .

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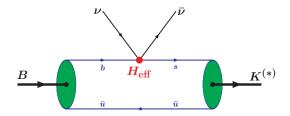
## Matrix elements and branching fractions

Matrix elements:

$$\mathcal{M}(B \to \mathcal{K}^{(*)}\nu\bar{\nu}) = \frac{G_F}{\sqrt{2}} \frac{\alpha_{em}}{2\pi} \frac{X_t}{\sin^2 \Theta_W} V_{tb} V_{ts}^* \langle \mathcal{K}^{(*)} | \bar{s} O^{\mu} b | B \rangle \langle \bar{\nu}^{s_1} O_{\mu} \nu^{s_2} \rangle.$$

where  $K^{(*)} = K$  or  $K^*$ .

The quark diagram describing the decay  $B \to K^{(*)} \nu \bar{\nu}$ 



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## Form factors

The definition of the form factors:

$$\langle K(p_2) \, | \, \bar{s} \, O^{\,\mu} \, b \, | \, B(p_1) \rangle = F_+(q^2) \, P^{\,\mu} + F_-(q^2) \, q^{\,\mu},$$

$$\langle K^*(p_2, \epsilon_2) \, | \, \bar{s} \, O^{\,\mu} \, b \, | \, B(p_1) \rangle = \frac{\epsilon_2^{\,\dagger}}{m_1 + m_2} \left( -g^{\,\mu\alpha} \, Pq \, A_0(q^2) + P^{\,\mu} \, P^{\,\alpha} \, A_+(q^2) \right)$$

$$+ q^{\,\mu} \, P^{\,\alpha} \, A_-(q^2) + i \, \varepsilon^{\,\mu\alpha Pq} \, V(q^2) \Big)$$

where  $P = p_1 + p_2$ ,  $q = p_1 - p_2$ , and  $\epsilon_2$  is  $K^*$  polarization vector  $(\epsilon_2^{\dagger} \cdot p_2 = 0)$ . Numerically calculated form factors were approximated by the dipole formula with relative accuracy less than 1%.

$$F(q^2) = \frac{F(0)}{1-as+bs^2}, \quad s = \frac{q^2}{m_1^2}$$

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#### **Branching fractions**

The differential branching fraction is written as

$$\frac{d\mathcal{B}(B^+ \to K^{(*)\,+} + \nu\bar{\nu})}{dq^2} = 3\tau_{B^+} \frac{(G_F \lambda_t \alpha_{em})^2}{3(2\pi)^5} \Big(\frac{X_t}{\sin^2 \theta_W}\Big)^2 \\ \times \frac{|\mathbf{p}_2|}{4m_1^2} \Big(\tilde{H}_+^2 + \tilde{H}_-^2 + \tilde{H}_0^2\Big).$$

A factor of 3 at the beginning of the formula results from the summation by neutrino flavors:  $\nu_e$ ,  $\nu_\mu$ ,  $\nu_\tau$ . The scaled helicity amplitudes  $\tilde{H}$  are written down

$$\begin{split} B &\to K \quad \text{transition:} \\ \tilde{H}_{\pm} &= 0, \qquad \tilde{H}_{0} = 2 \ m_{1} \ |\mathbf{p}_{2}| \ F_{+}. \\ B &\to K^{*} \quad \text{transition:} \\ \tilde{H}_{\pm} &= \frac{\sqrt{q^{2}}}{m_{1} + m_{2}} \Big( - Pq \ A_{0} \pm 2 \ m_{1} \ |\mathbf{p}_{2}| \ V \Big), \\ \tilde{H}_{0} &= \frac{1}{m_{1} + m_{2}} \frac{1}{2 \ m_{2}} \Big( - Pq \ (Pq - q^{2}) \ A_{0} + 4 \ m_{1}^{2} \ |\mathbf{p}_{2}|^{2} \ A_{+} \Big). \end{split}$$

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## Numerical results

The branching fractions of the decays  $B \to K^{(*)} \nu \bar{\nu}$ 

	CCQM	Buras [1]	BaBar [2]	Belle [3]
$10^6\mathcal{B}(K^+)$	$\textbf{4.96} \pm \textbf{0.74}$	$\textbf{3.98} \pm \textbf{0.47}$	< 17 (90% CL)	_
$10^6  {\cal B}(K^{*+})$	$\textbf{9.57} \pm \textbf{1.43}$	$\textbf{9.19} \pm \textbf{0.99}$	_	< 40 (90% CL)

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- 1. A. J. Buras, J. Girrbach-Noe, C. Niehoff and D. M. Straub, JHEP 02, 184 (2015)
- 2. J. P. Lees et al. [BaBar], Phys. Rev. D 87, no.11, 112005 (2013)
- 3. O. Lutz et al. [Belle], Phys. Rev. D 87, no.11, 111103 (2013)

## Summary

- The observed enhancements of the tauonic mode in the (semi)leptonic *B*-meson decay may indicate a violation of lepton universality.
- At present, the measurements are limited by the available experimental uncertainties
- In addition, searches for lepton universality violation in semileptonic decays of Λ<sub>b</sub>-baryons are being planned.

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► We have proposed a form-factor-independent test of lepton universality for semileptonic *B* meson, *B<sub>c</sub>* meson, and  $\Lambda_b$  baryon decays by analyzing the two-fold  $(q^2, \cos \theta)$  decay distribution.

## Summary

- ► The calculated branching fractions  $\mathcal{R}_{\pi^+/\mu^+\nu}$  and  $\mathcal{R}_{\mathcal{K}^+/\pi^+}$  are in good agreement with the LHCb data and other theoretical approaches. At the same time the theoretical predictions for the ratio  $\mathcal{R}_{J/\psi}$  are more than 2  $\sigma$  less than the experimental data. This may indicate on the possibility of New physics effects in this decay.
- The future data will show whether the obtained results are an indication of beyond-the-SM physics or the result of larger-than-expected statistical or systematic deviations.
- A confirmation of new physics contributions in these decays would change our understanding of matter and trigger an intense program of experimental and theoretical research.

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