

# BSM physics at future lepton colliders

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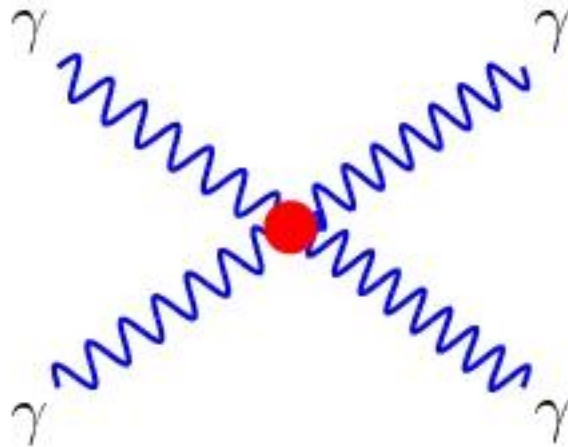
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# Summary

1. Light-by-light (LBL) scattering  $\gamma\gamma \rightarrow \gamma\gamma$  of Compton backscattered (CB) photons at high energy collider CLIC. Probing anomalous quartic  $\gamma\gamma\gamma\gamma$  couplings
2. Search for anomalous gauge couplings of  $\gamma\gamma Z$  vertex in  $\gamma\gamma \rightarrow \gamma Z$  collision of CB photons at the CLIC
3. Study of invisible massive dark photon in  $\gamma e$  scattering at future lepton colliders ILC, CLIC, and CEPC.
4. Conclusions

# Light-by-light scattering of CB photons at the CLIC



Anomalous diagram for process  $\gamma\gamma \rightarrow \gamma\gamma$

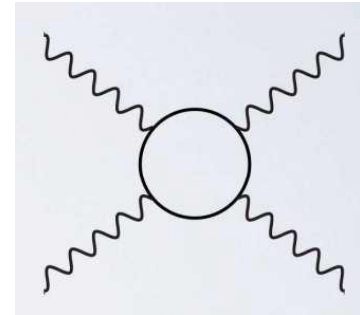
The goal is to examine anomalous quartic gauge couplings (QGCs) via reaction  $\gamma\gamma \rightarrow \gamma\gamma$  at the CLIC

# New physics contributions to $4\gamma$ couplings

## New charged particles via loops

$$\zeta_i \sim Q^4 m^{-4}$$

Example: top partner

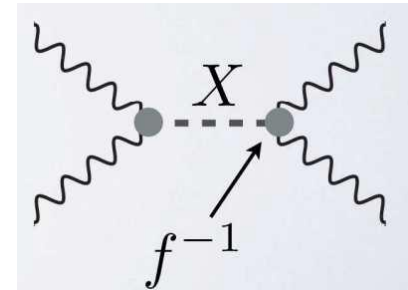


## New neutral particles at tree level

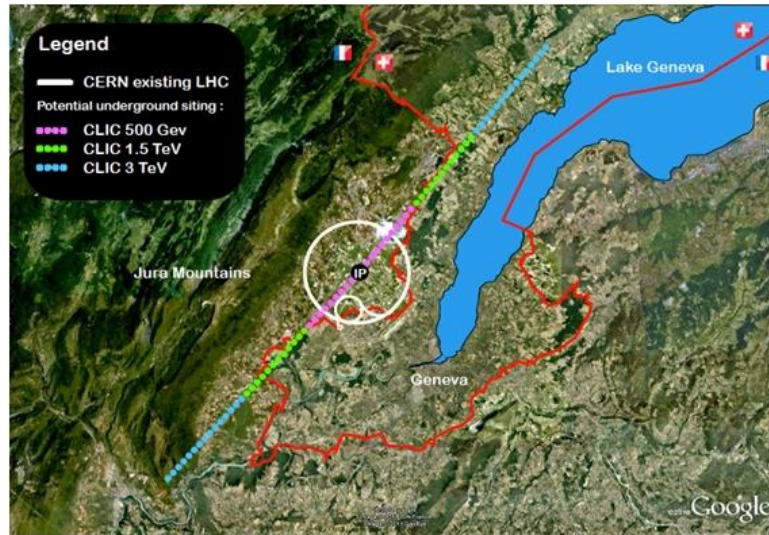
$$\zeta_i \sim f^{-2} m^{-2}$$

Example: KK gravitons, radion  
(warped extra dimension)

If  $f_{\text{KK}} \sim \text{TeV}$  and  $m_{\text{KK}} \sim \text{few TeV}$ ,  
then  $\zeta_i \sim 10^{-2} - 10^{-1} \text{ TeV}^{-4}$



# Compact Linear Collider (CLIC)



	Collision energy	Integrated luminosity (unpolarized beams)
1st stage	380 GeV	1.0 ab <sup>-1</sup>
2nd stage	1500 GeV	2.5 ab <sup>-1</sup>
3rd stage	3000 GeV	5.0 ab <sup>-1</sup>

$\lambda_0$  is helicity of laser photon beam, and  
 $\lambda_e$  is helicity of electron beam before  
**Compton backscattering**

$$(\lambda_e^{(1)}, \lambda_0^{(1)}; \lambda_e^{(2)}, \lambda_0^{(2)}) = (0.8, 1; 0.8, 1) ,$$

$$(\lambda_e^{(1)}, \lambda_0^{(1)}; \lambda_e^{(2)}, \lambda_0^{(2)}) = (-0.8, 1; -0.8, 1)$$

**CLIC energy stages and integrated luminosities  
for unpolarized and polarized electron beams**

		$L, \text{fb}^{-1}$		
Stage	$\sqrt{s}, \text{GeV}$	$\lambda_e = 0$	$\lambda_e = -0.8$	$\lambda_e = 0.8$
2	1500	2500	2000	500
3	3000	5000	4000	1000

## Differential cross section for LBL scattering

$$\begin{aligned}
 \frac{d\sigma}{d\cos\theta} = & \frac{1}{128\pi s} \int_{x_{1\min}}^{x_{1\max}} \frac{dx_1}{x_1} f_{\gamma/e}(x_1) \int_{x_{2\min}}^{x_{2\max}} \frac{dx_2}{x_2} f_{\gamma/e}(x_2) \\
 & \times \left\{ \left[ 1 + \xi \left( E_\gamma^{(1)}, \lambda_0^{(1)} \right) \xi \left( E_\gamma^{(2)}, \lambda_0^{(2)} \right) \right] \right. \\
 & \quad \times (|M_{++++}|^2 + |M_{++--}|^2) \\
 & \quad + \left[ 1 - \xi \left( E_\gamma^{(1)}, \lambda_0^{(1)} \right) \xi \left( E_\gamma^{(2)}, \lambda_0^{(2)} \right) \right] \\
 & \quad \left. \times (|M_{+--+}|^2 + |M_{+---}|^2) \right\}
 \end{aligned}$$

$f_{\gamma/e}(x)$  = CB photon distribution  
in energy fraction  $x = E_\gamma/E_e$

$\xi(E_\gamma, \lambda_0)$  = CB photon helicity

$$x_{1,\min} = (p_t/E_e)^2, \quad x_{2,\min} = (p_t/x_1 E_e)^2, \quad x_{\max} = 0.83$$

# Effective Lagrangian

Effective Lagrangian of dimension-8 operators which contribute to anomalous quartic neutral gauge couplings

$$\begin{aligned} \mathcal{L}_{\text{QNGC}} = & \frac{c_8}{\Lambda^4} B_{\rho\sigma} B^{\rho\sigma} B_{\mu\nu} B^{\mu\nu} + \frac{c_9}{\Lambda^4} W_{\rho\sigma}^a W^{a\rho\sigma} W_{\mu\nu}^b W^{b\mu\nu} + \frac{c_{10}}{\Lambda^4} W_{\rho\sigma}^a W^{b\rho\sigma} W_{\mu\nu}^a W^{b\mu\nu} \\ & + \frac{c_{11}}{\Lambda^4} B_{\rho\sigma} B^{\rho\sigma} W_{\mu\nu}^a W^{a\mu\nu} + \frac{c_{13}}{\Lambda^4} B_{\rho\sigma} B^{\sigma\nu} B_{\nu\mu} B^{\mu\rho} + \frac{c_{14}}{\Lambda^4} W_{\rho\sigma}^a W^{a\sigma\nu} W_{\nu\mu}^b W^{b\mu\rho} \\ & + \frac{c_{15}}{\Lambda^4} W_{\rho\sigma}^a W^{b\sigma\nu} W_{\nu\mu}^a W^{b\mu\rho} + \frac{c_{16}}{\Lambda^4} B_{\rho\sigma} B^{\sigma\nu} W_{\nu\mu}^a W^{a\mu\rho} \end{aligned}$$

➔ Effective Lagrangian for anomalous  $\gamma\gamma\gamma\gamma$  couplings  
(in terms of physical fields)

$$L_{\text{QNGC}}^{\gamma\gamma\gamma\gamma} = \zeta_1 (F_{\mu\nu} F^{\mu\nu})(F_{\rho\sigma} F^{\rho\sigma}) + \zeta_2 (F_{\mu\nu} F^{\nu\rho} F_{\rho\sigma} F^{\sigma\mu})$$

Anomalous couplings  $\zeta_1, \zeta_2$  have dimension -4



# Numerical analysis



Electron beam helicities:

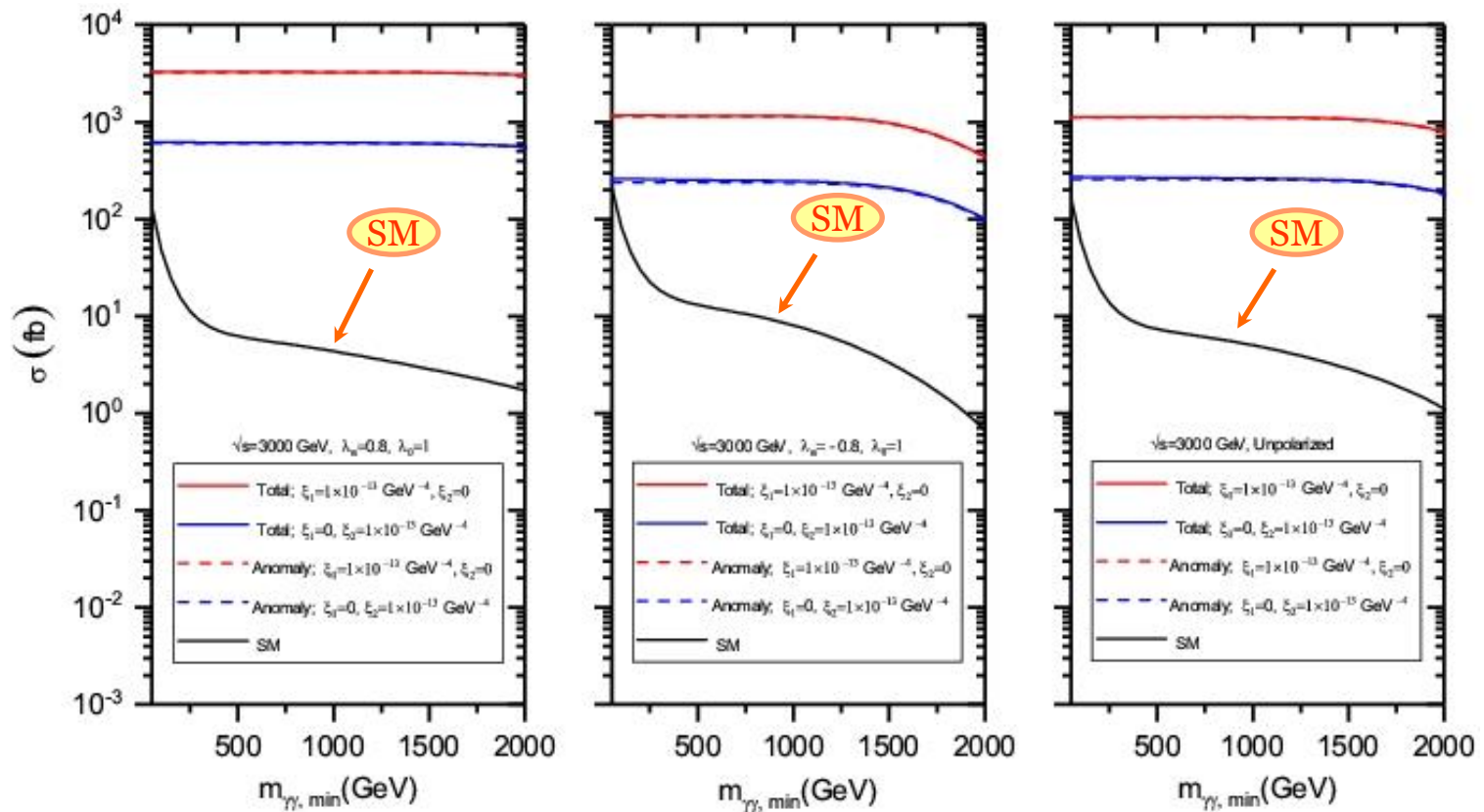
$$\lambda_e = 0.8, -0.8, \text{ and } 0 \text{ (unpolarized case)}$$

Cuts on the invariant mass and rapidities of final photons:

$$m_{\gamma\gamma} > 200 \text{ GeV}, \quad |\eta| < 2.5$$

SM amplitude: *(G.Gounaris et al., EPJC, 9, 673, 1999)*

$M_W$  (W-loop, dominates at  $\sqrt{s} > 200 \text{ GeV}$ )  
+  $M_f$  (fermion-loop) contributions



Total cross sections for  $\gamma\gamma \rightarrow \gamma\gamma$  scattering versus minimal invariant mass of outgoing photons for  $\sqrt{s} = 3$  TeV. The left, middle and right panels correspond to  $\lambda_e = 0.8, -0.8, 0$ .

The solid curves (from top downwards):  
 $(\zeta_1 = 10^{-13} \text{ GeV}^{-4}, \zeta_2 = 0)$ ,  $(\zeta_1 = 0, \zeta_2 = 10^{-13} \text{ GeV}^{-4})$ , SM.

# Exclusion significance ( $\delta$ = percentage systematic error)

(Y. Zhang & J. Shen, EPJC, 80, 811, 2020)

$$S_{\text{excl}} = \sqrt{2} \left[ s - b \ln \left( \frac{b+s+x}{2b} \right) - \frac{1}{\delta^2} \ln \left( \frac{b-s+x}{2b} \right) - (b+s-x) \left( 1 + \frac{1}{\delta^2 b} \right) \right]^{1/2}$$

$s$  ( $b$ ) = number of signal (background) events

In the limit  $\delta = 0$

$$x = \sqrt{(s+b)^2 - 4\delta^2 s b^2 / (1 + \delta^2 b)}$$

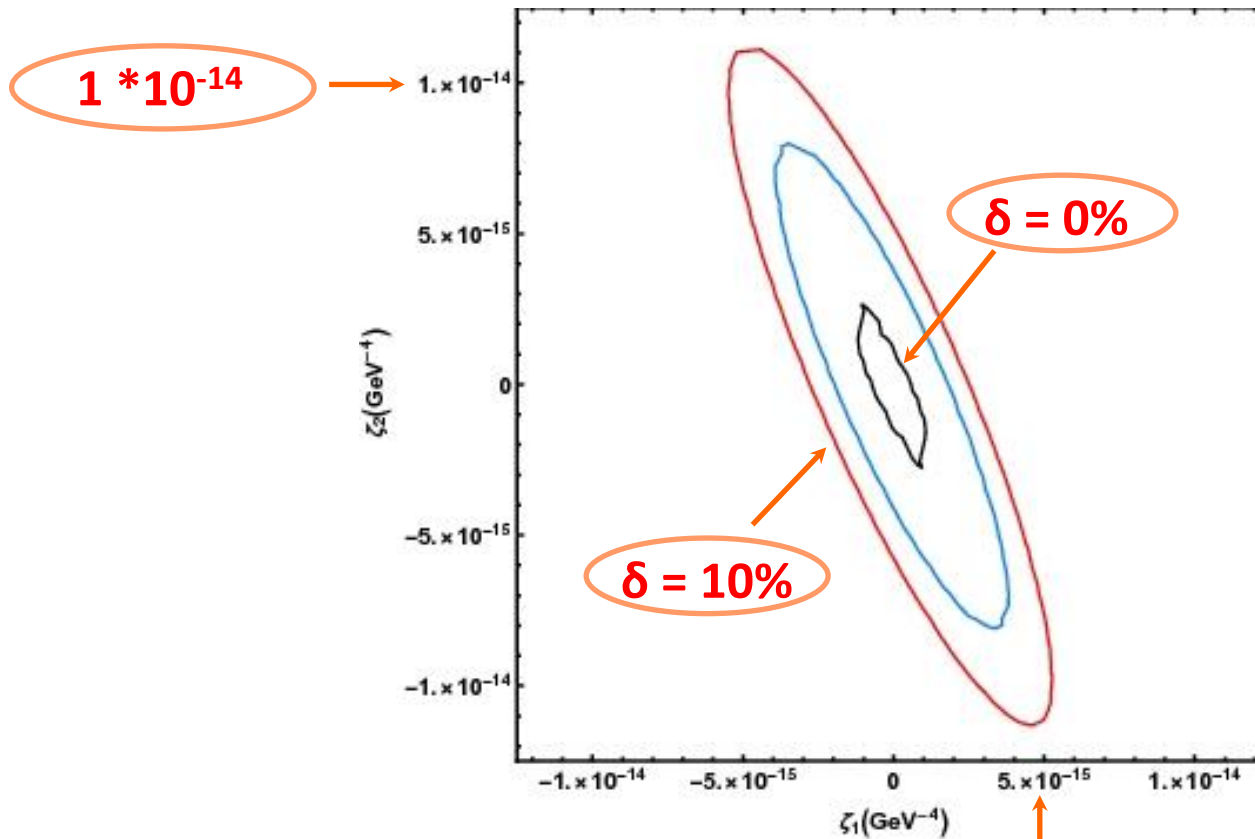
$$S_{\text{excl}} = \sqrt{2 \left[ s - b \ln \left( 1 + \frac{s}{b} \right) \right]}$$

$s \ll b$



$$S_{\text{excl}} = \frac{s}{\sqrt{b}}$$

$S_{\text{excl}} \leq 1.645$  is the region that  
can be excluded at 95% C.L.



$$|\eta| < 2.5$$

$$m_{\gamma\gamma} > 1 \text{ TeV}$$

*(S.Inan & A.K., EPJC, 81, 664, 2021)*

95% C.L. exclusion region for anomalous couplings  $\zeta_1$ ,  $\zeta_2$  for **unpolarized** LBL scattering at the CLIC. Systematic errors are 0%, 5%, and 10%. The collision energy is 3 TeV, the integrated luminosity is 5  $\text{ab}^{-1}$ . Couplings  $\zeta_1$ ,  $\zeta_2$  are **in  $\text{GeV}^{-4}$** .

## Exclusion limits on anomalous couplings for the LBL scattering at the CLIC with energy 3.0 TeV

Helicity		0	-0.8	0.8
Luminosity, fb <sup>-1</sup>		5000	4000	1000
$\zeta_1$  , GeV <sup>-4</sup> ( $\zeta_2 = 0$ )	$\delta = 0\%$	$6.85 \times 10^{-16}$	$8.82 \times 10^{-16}$	$8.73 \times 10^{-16}$
	$\delta = 5\%$	$1.90 \times 10^{-15}$	$2.48 \times 10^{-15}$	$1.56 \times 10^{-15}$
	$\delta = 10\%$	$2.63 \times 10^{-15}$	$3.37 \times 10^{-15}$	$2.12 \times 10^{-15}$
$\zeta_2$  , GeV <sup>-4</sup> ( $\zeta_1 = 0$ )	$\delta = 0\%$	$1.43 \times 10^{-15}$	$1.85 \times 10^{-15}$	$1.82 \times 10^{-15}$
	$\delta = 5\%$	$3.99 \times 10^{-15}$	$5.12 \times 10^{-15}$	$3.28 \times 10^{-15}$
	$\delta = 10\%$	$5.53 \times 10^{-15}$	$7.10 \times 10^{-15}$	$4.46 \times 10^{-15}$

*(S.Inan & A.K., EPJC, 81, 664, 2021)*

# Bounds on anomalous couplings for LHC and HL-LHC

LHC,  $L=300 \text{ fb}^{-1}$  :

$$|\zeta_1| < 1.5 \cdot 10^{-14} \text{ GeV}^{-4}, \quad |\zeta_2| < 3.0 \cdot 10^{-14} \text{ GeV}^{-4}$$

*(S.Fichet et al., JHEP 02, 165, 2015)*

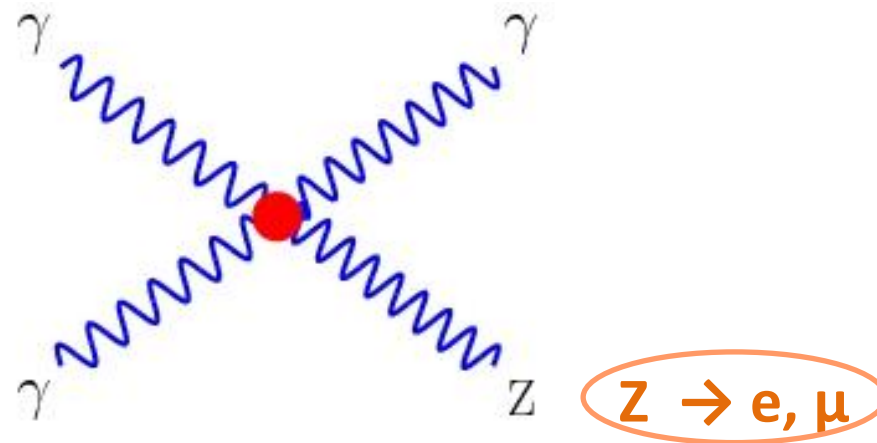
HL-LHC,  $L=3000 \text{ fb}^{-1}$  :

$$|\zeta_1| < 7.0 \cdot 10^{-15} \text{ GeV}^{-4}, \quad |\zeta_2| < 1.5 \cdot 10^{-14} \text{ GeV}^{-4}$$

*(S.Fichet et al., Phys. Rev. D 89, 114004, 2014)*

# $\gamma Z$ production in photon-photon scattering

Anomalous diagram for process  $\gamma\gamma \rightarrow \gamma Z$



Effective Lagrangian for anomalous  $\gamma\gamma Z$  couplings

$$L_{\text{QNGC}}^{\gamma\gamma Z} = g_1 (F^{\rho\mu} F^{\alpha\nu}) (\partial_\rho F_{\mu\nu} Z_\alpha) + g_2 (F^{\rho\mu} F_\mu^\nu) (\partial_\rho F_{\alpha\nu} Z^\alpha)$$

Anomalous couplings  $g_1, g_2$  have dimension -4

## Feynman rule for anomaly vertex $\gamma\gamma\gamma Z$

$$\begin{aligned}
 P^{\mu\nu\rho\alpha} = \mathcal{P} \{ & g_1 [(p_1 \cdot p_2)(p_2 \cdot p_3)g^{\mu\nu}g^{\rho\alpha} - (p_1 \cdot p_3)p_2^\mu p_1^\nu g^{\rho\alpha} \\
 & - (p_1 \cdot p_3)p_1^\nu p_2^\alpha g^{\mu\rho} + p_2^\mu p_1^\nu p_1^\rho p_3^\alpha] \\
 & + g_2 [-(p_1 \cdot p_2)(p_1 \cdot p_3)g^{\mu\alpha}g^{\nu\rho} + (p_2 \cdot p_3)p_1^\nu p_1^\alpha g^{\mu\rho} \\
 & - (p_2 \cdot p_3)p_1^\nu p_1^\rho g^{\mu\alpha} + (p_2 \cdot p_3)p_1^\nu p_2^\alpha g^{\mu\rho} + 2(p_2 \cdot p_3)p_2^\mu p_1^\rho g^{\nu\alpha} \\
 & - (p_1 \cdot p_3)p_2^\rho p_1^\alpha g^{\mu\nu} + p_3^\mu p_1^\nu p_2^\rho p_1^\alpha] \}
 \end{aligned}$$

$\mathcal{P}$  – permutations (symmetrization with respect to photon's momenta and indices)

$$M_{\lambda_1\lambda_2\lambda_3\lambda_4}(p_1, p_2, p_3) = P_{\mu\nu\rho\alpha}(p_1, p_2, p_3) \varepsilon_\mu^{\lambda_1}(p_1) \varepsilon_\nu^{\lambda_2}(p_2) \varepsilon_\rho^{*\lambda_3}(p_3) \varepsilon_\alpha^{*\lambda_4}(p_4)$$



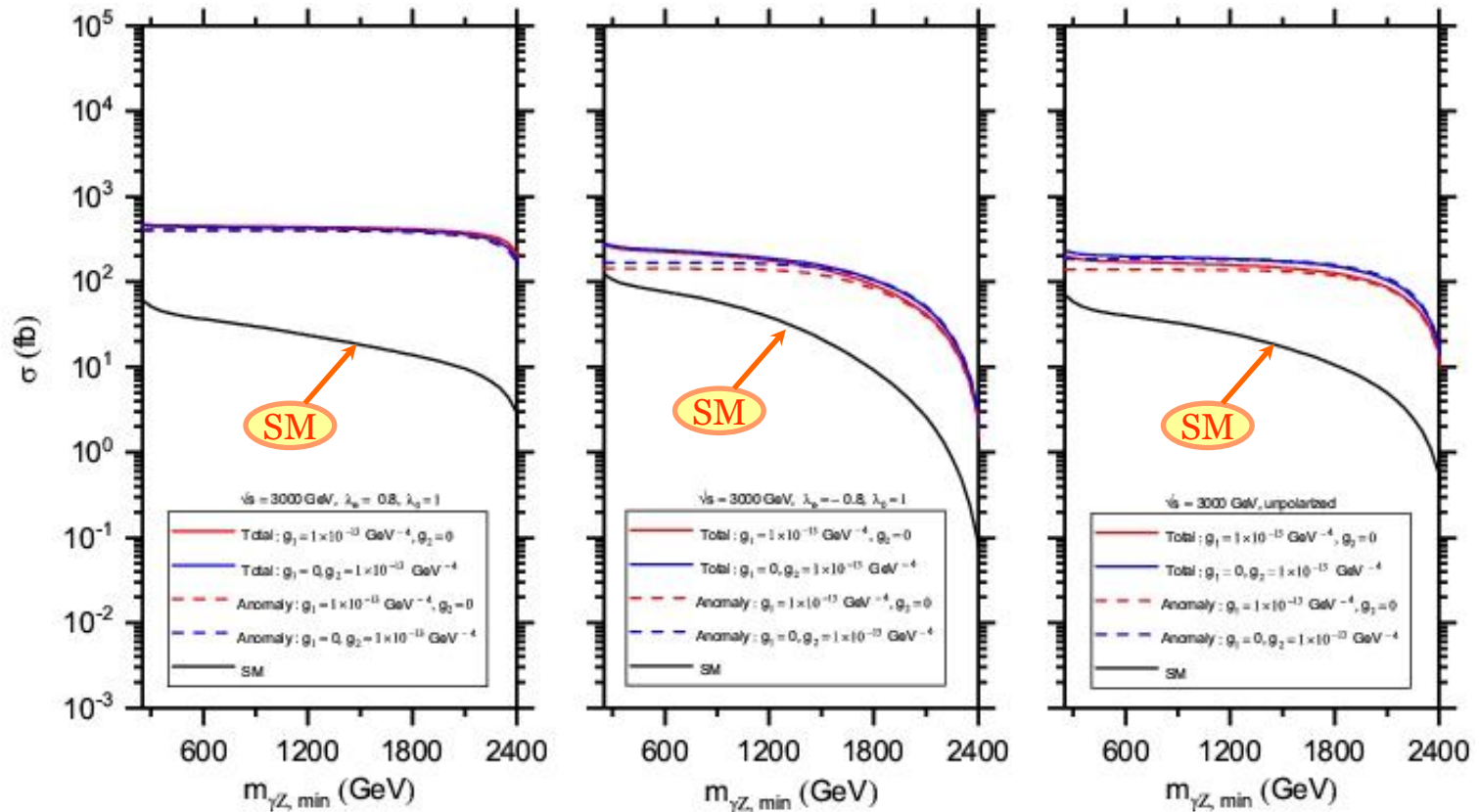
24 helicity amplitudes proportional to  $g_1$

24 helicity amplitudes proportional to  $g_2$

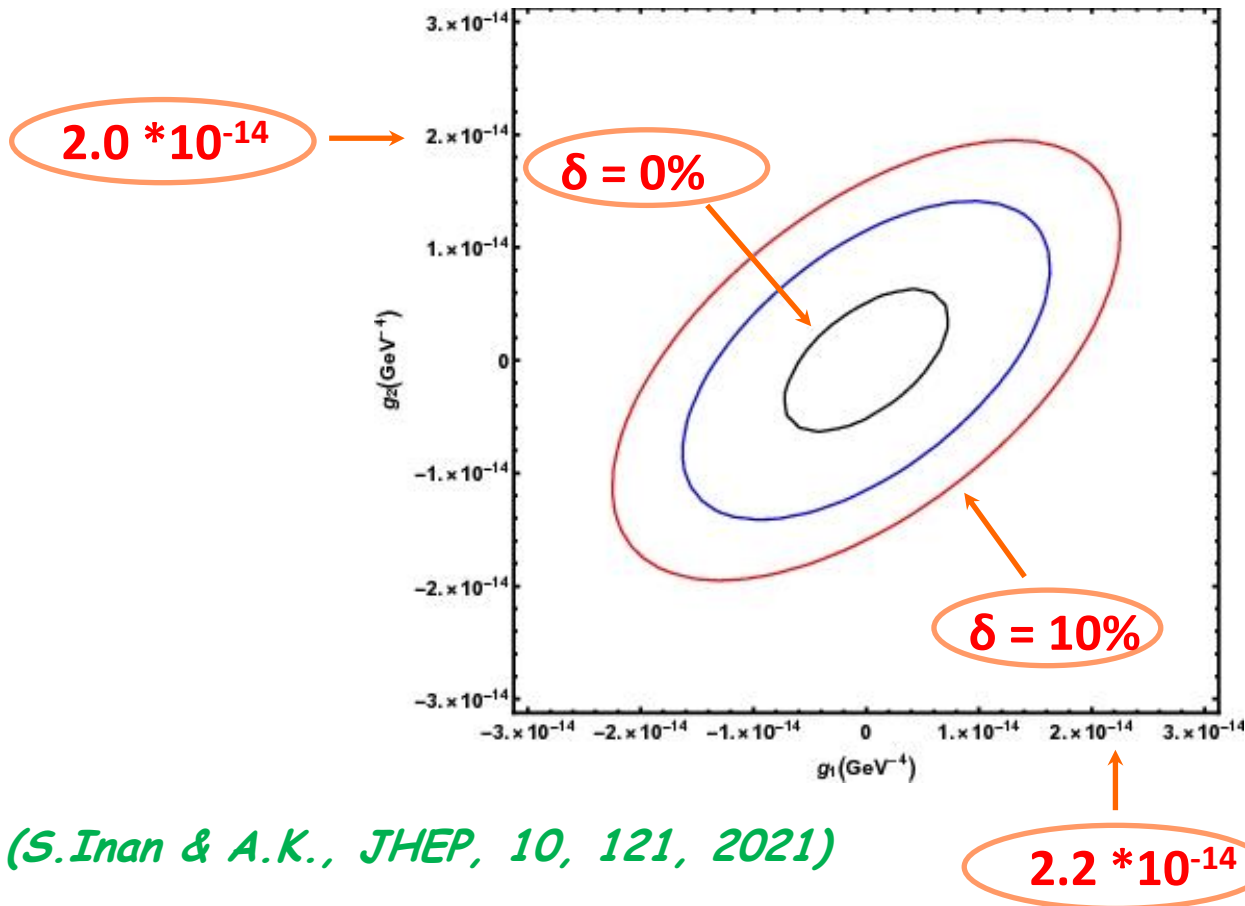
*(S.Inan & A.K., JHEP, 10, 121, 2021)*

SM amplitudes are taken from *G.Gounaris et al., EPJC, 10, 499, 1999*





Total cross sections for  $\gamma\gamma \rightarrow \gamma Z$  scattering versus minimal invariant mass of outgoing photons for  $\sqrt{s} = 3$  TeV. The left, middle and right panels correspond to  $\lambda_e = 0.8, -0.8, 0$ . Solid curves correspond to  $(g_1 = 10^{-13} \text{ GeV}^{-4}, g_2 = 0)$ , SM.



$|\eta| < 2.5$   
 $m_{\gamma Z} > 1 \text{ TeV}$

*(S.Inan & A.K., JHEP, 10, 121, 2021)*

95% C.L. exclusion region for anomalous couplings  $g_1, g_2$  for **unpolarized**  $\gamma\gamma \rightarrow \gamma Z$  scattering at the CLIC. Systematic errors are 0%, 5%, and 10%. The collision energy is 3 TeV, the integrated luminosity is  $5 \text{ ab}^{-1}$ . Couplings  $g_1, g_2$  are in  **$\text{GeV}^{-4}$** .

**Exclusion limits on anomalous couplings at the CLIC  
for energy 3.0 TeV. Polarized case**

$\lambda_e$		0	-0.8	0.8
$L, \text{fb}^{-1}$		5000	4000	1000
$ g_1 , \text{GeV}^{-4}$ ( $g_2 = 0$ )	$\delta = 0\%$	$5.98 \times 10^{-15}$	$7.14 \times 10^{-15}$	$5.13 \times 10^{-15}$
	$\delta = 5\%$	$1.33 \times 10^{-14}$	$1.73 \times 10^{-14}$	$7.79 \times 10^{-15}$
	$\delta = 10\%$	$1.85 \times 10^{-14}$	$2.39 \times 10^{-14}$	$1.04 \times 10^{-14}$
$ g_2 , \text{GeV}^{-4}$ ( $g_1 = 0$ )	$\delta = 0\%$	$5.18 \times 10^{-15}$	$6.62 \times 10^{-15}$	$5.19 \times 10^{-15}$
	$\delta = 5\%$	$1.16 \times 10^{-14}$	$1.60 \times 10^{-14}$	$7.87 \times 10^{-15}$
	$\delta = 10\%$	$1.62 \times 10^{-14}$	$2.21 \times 10^{-14}$	$1.05 \times 10^{-14}$

*(S.Inan & A.K., JHEP, 10, 121, 2021)*

# Bounds on anomalous couplings for the LHC and HL-LHC

SM expectation:  $\mathcal{B}(Z \rightarrow \gamma\gamma\gamma) = 5.41 \cdot 10^{-10}$

$$\mathcal{B}(Z \rightarrow \gamma\gamma\gamma) < 0.8 \cdot 10^{-5} \text{ (LEP)}$$

$$\mathcal{B}(Z \rightarrow \gamma\gamma\gamma) < 2.2 \cdot 10^{-6} \text{ (ATLAS)}$$

→  $|f_i| < 1.3 \cdot 10^{-9} \text{ GeV}^{-4}$  where  $f_i = g_i/8$

From  $\gamma\gamma \rightarrow \gamma Z$  at LHC:

LHC,  $L=300 \text{ fb}^{-1}$  :

$$|f_i| < 1.0 \cdot 10^{-13} \text{ GeV}^{-4}$$

HL-LHC,  $L=3000 \text{ fb}^{-1}$  :

$$|f_i| < 7.8 \cdot 10^{-14} \text{ GeV}^{-4}$$

*(C. Baldenegro et al., JHEP 06, 142, 2017)*

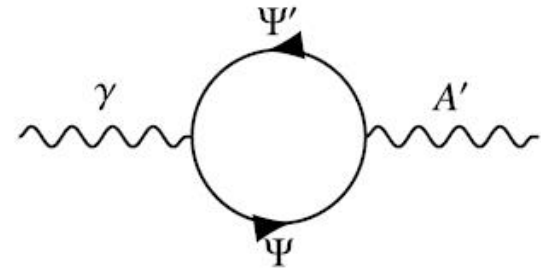
# Invisible dark photons in $\gamma e$ scattering at future lepton colliders ILC, CLIC, CEPC

We consider dark matter (DM) scenario in which **no** DM are charged under SM gauge group

Lightest stable DM particles can only interact with SM through exchange of massive vector mediator, **dark photon (DP)  $A'$**

DP **kinematically** mixes with SM  $U(1)_Y$  hypercharge gauge field (kinematic mixing portal)

Such mixing can be generated by loops of massive particles charged under both  $U(1)_Y$  and secluded  $U(1)'$  groups



## Gauge Lagrangian

$$\mathcal{L}_{\text{gauge}} = -\frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{4}\bar{F}'_{\mu\nu}\bar{F}'^{\mu\nu} - \frac{\varepsilon}{2c_W}\bar{F}'_{\mu\nu}B^{\mu\nu}$$

$B_{\mu\nu}, \bar{F}'_{\mu\nu}$  are field strength tensors of  $U(1)_Y, U(1)'$

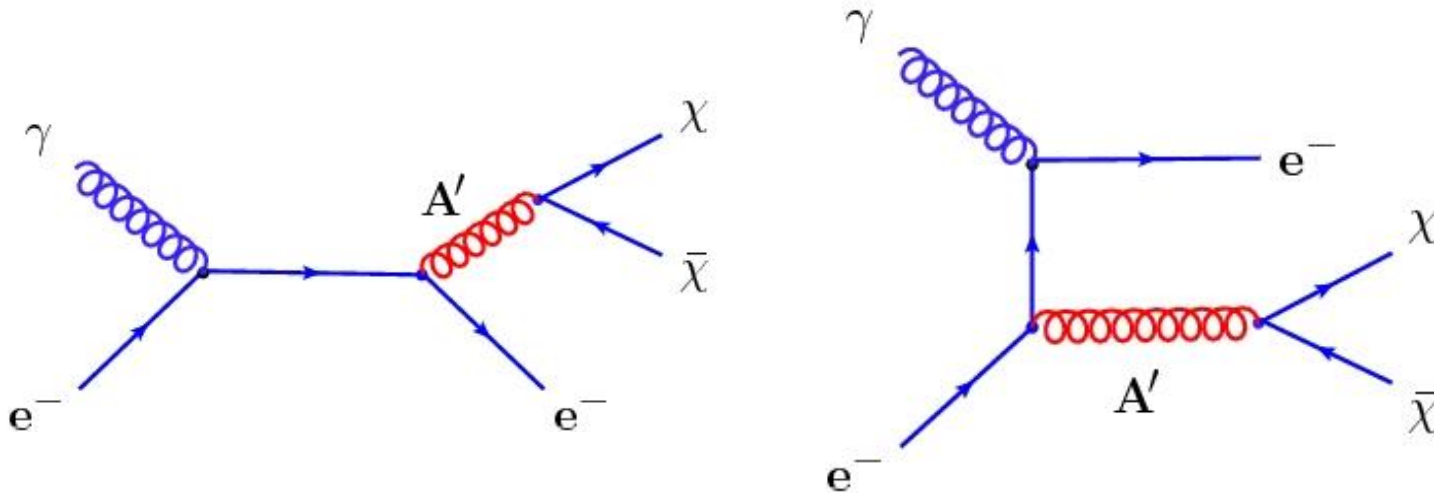
$\varepsilon$  – kinetic mixing parameter

## Interaction Lagrangian

(after diagonalizaion of gauge and DP fields)

$$\mathcal{L}_{\text{int}} = eJ_\mu A^\mu - \varepsilon e J_\mu A'^\mu + \varepsilon e' t_W J'_\mu Z_\mu + e' J'_\mu A'^\mu + \mathcal{L}_{A'\chi}$$

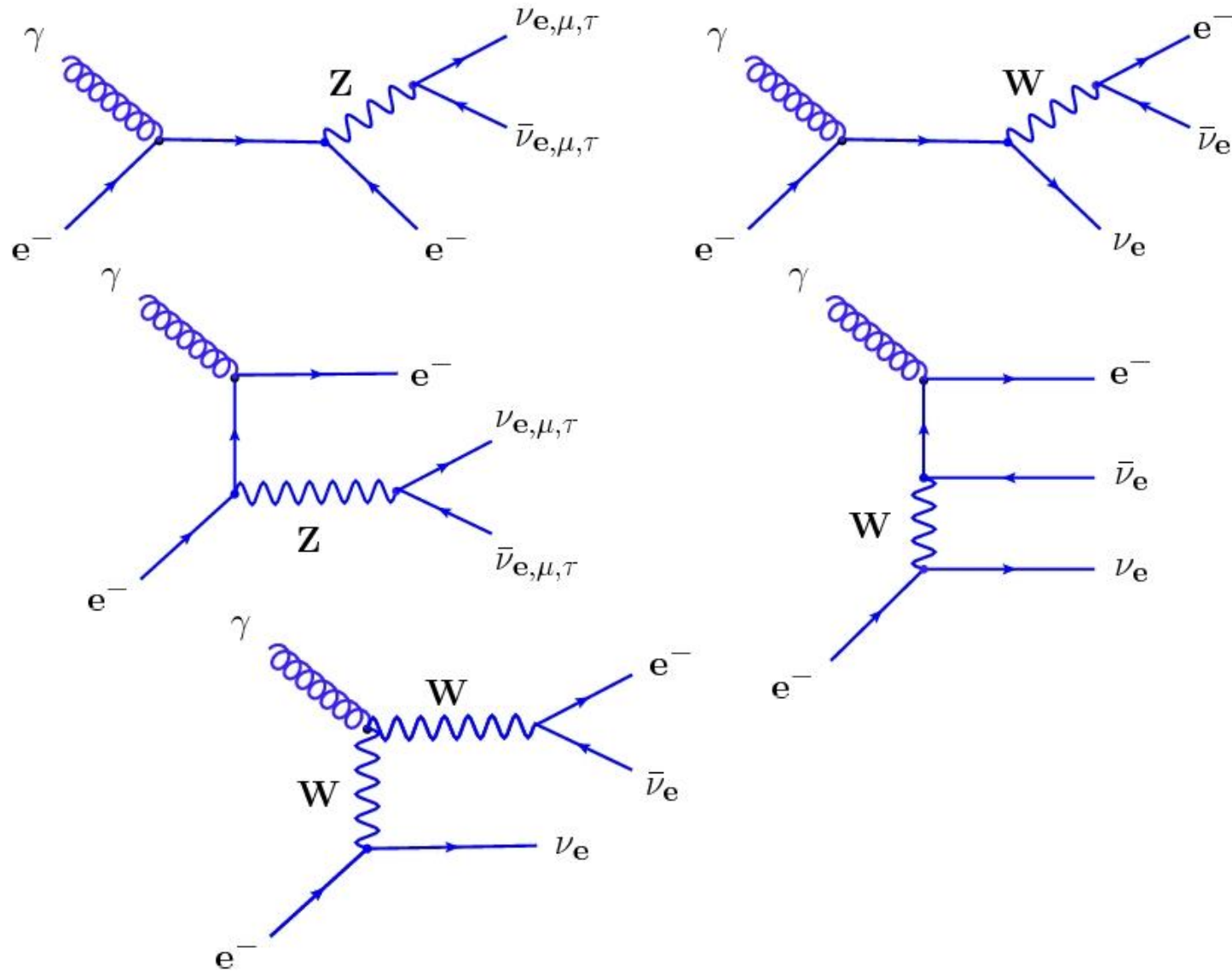
# Production of DP in $\gamma e^-$ collision with subsequent **invisible** decay



**$\chi$**  – dark matter particle

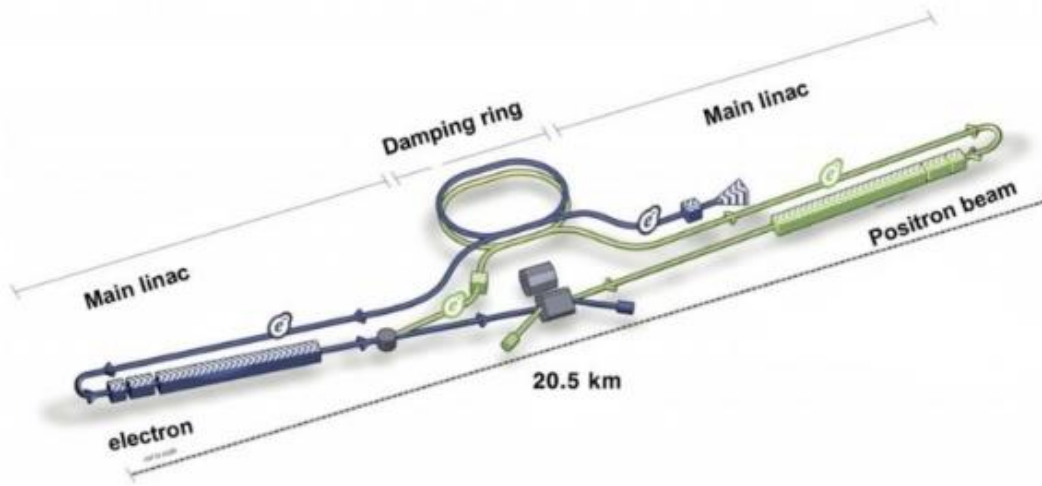
We assume that  $\mathcal{B}(A' \rightarrow \chi \bar{\chi}) = 1$

# SM background $\gamma e^- \rightarrow e^- + \nu + \bar{\nu}$





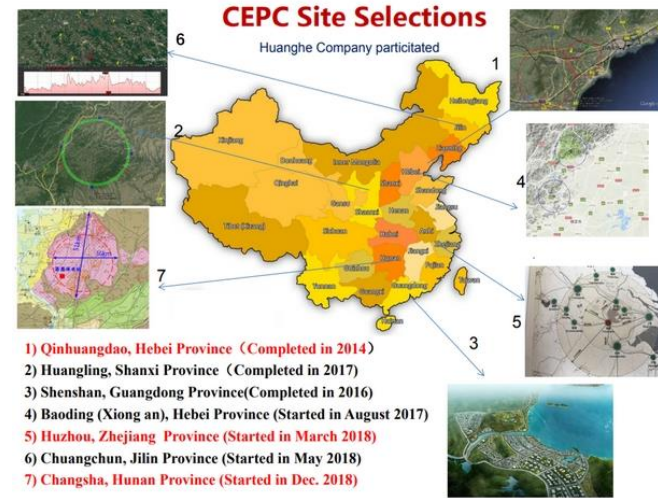
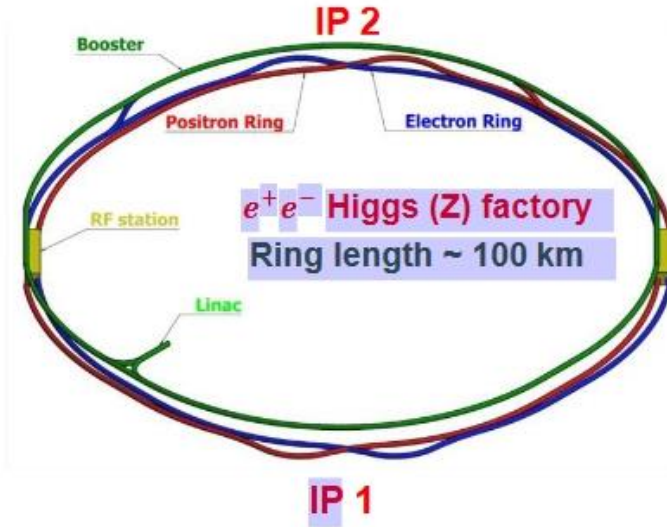
# International Linear Collider (ILC)



	Collision energy	Integrated luminosity (unpolarized beams)
1st stage	250 GeV	2.0 ab <sup>-1</sup>
2nd stage	500 GeV	4.0 ab <sup>-1</sup>
3rd stage	1000 GeV	5.4 ab <sup>-1</sup>

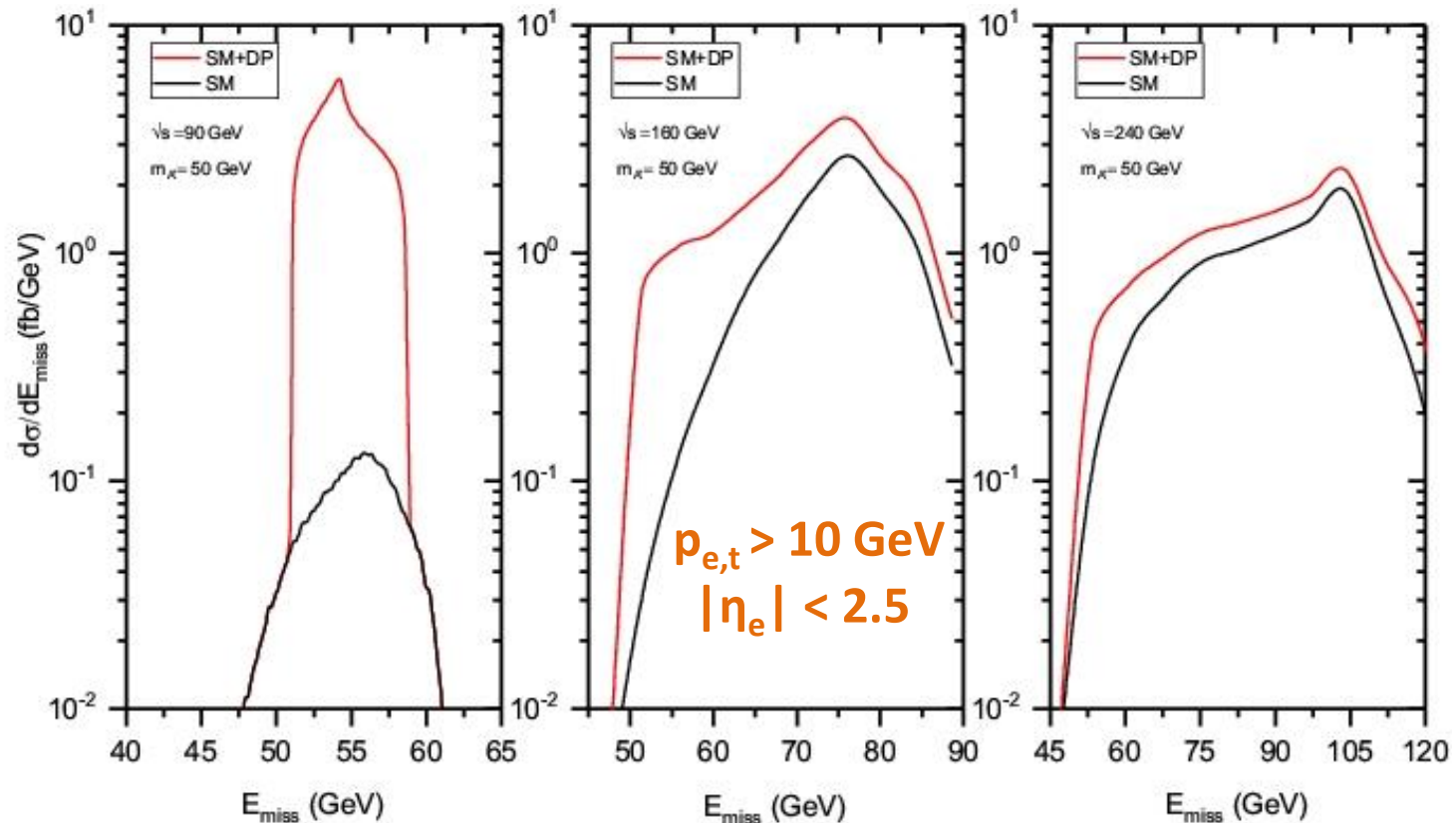
*(ILC Technical Design Report, arXiv:1306.6327, 1903.01629)*

# Circular Electron Positron Collider (CEPC)

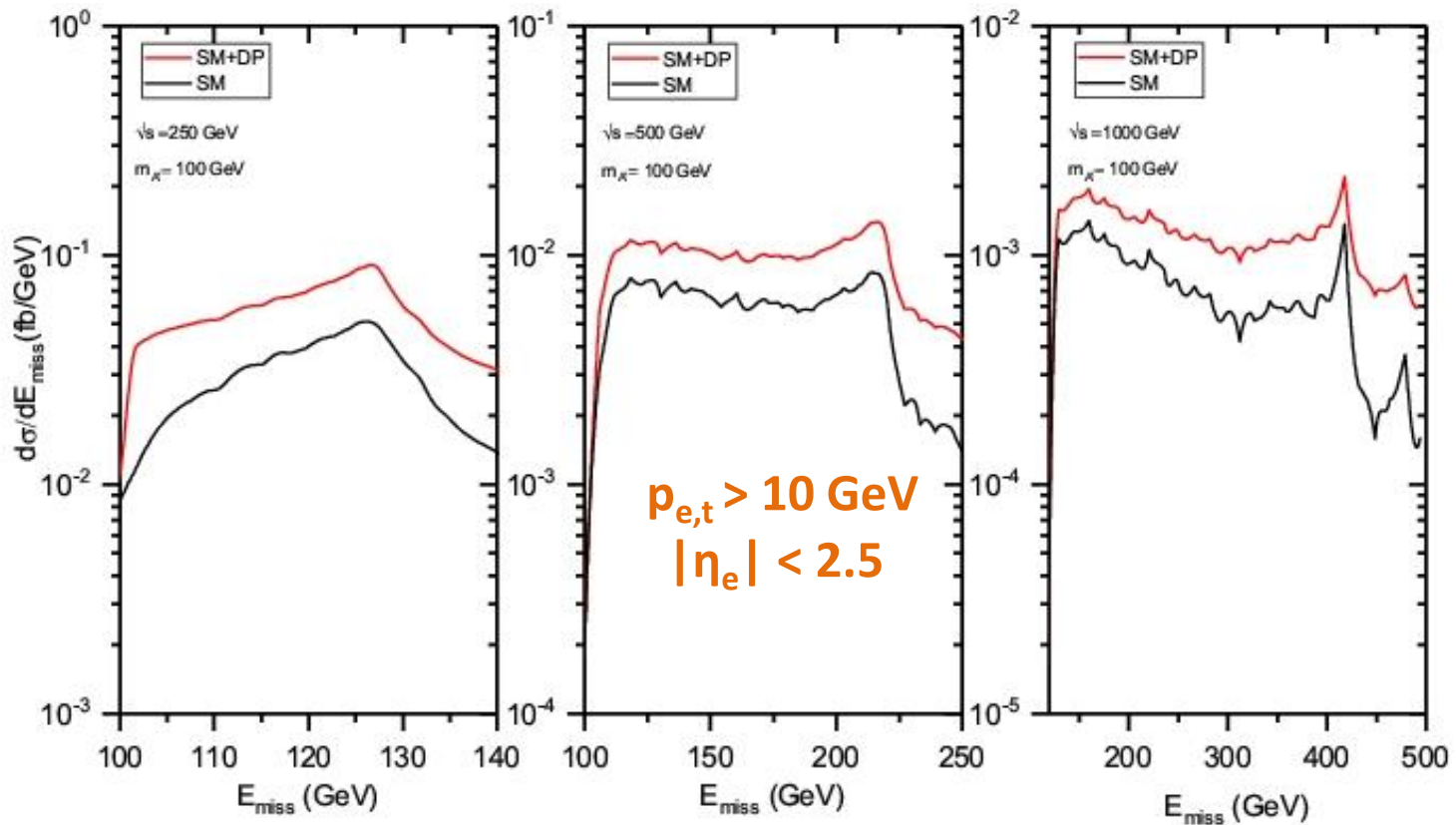


	Collision energy	Integrated luminosity (unpolarized beams)
1st stage	90 GeV	16 ab <sup>-1</sup>
2nd stage	180 GeV	2.6 ab <sup>-1</sup>
3rd stage	240 GeV	5.6 ab <sup>-1</sup>

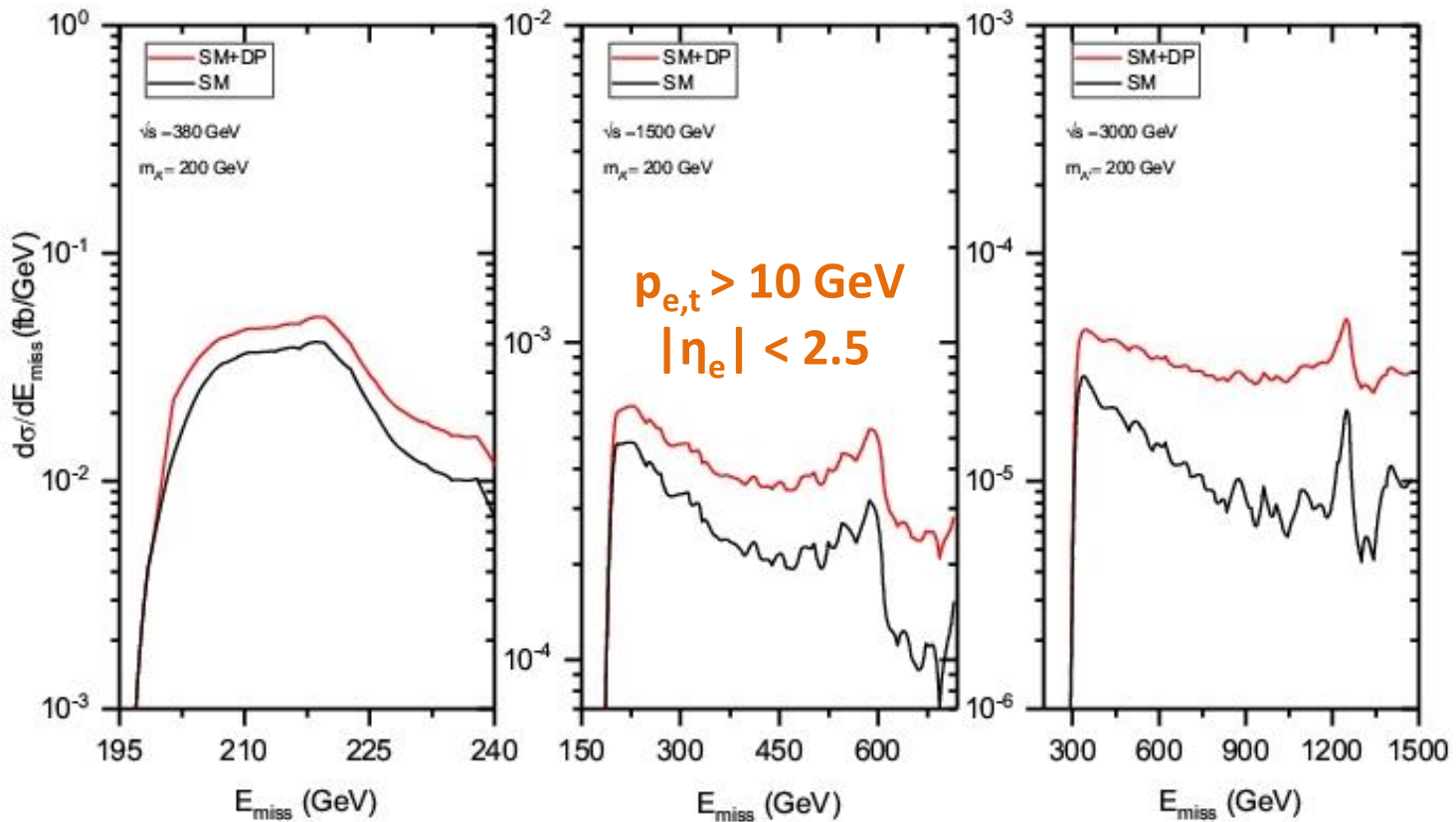
(CEPC Study Group, arXiv:1809.00285, 1811.10545)



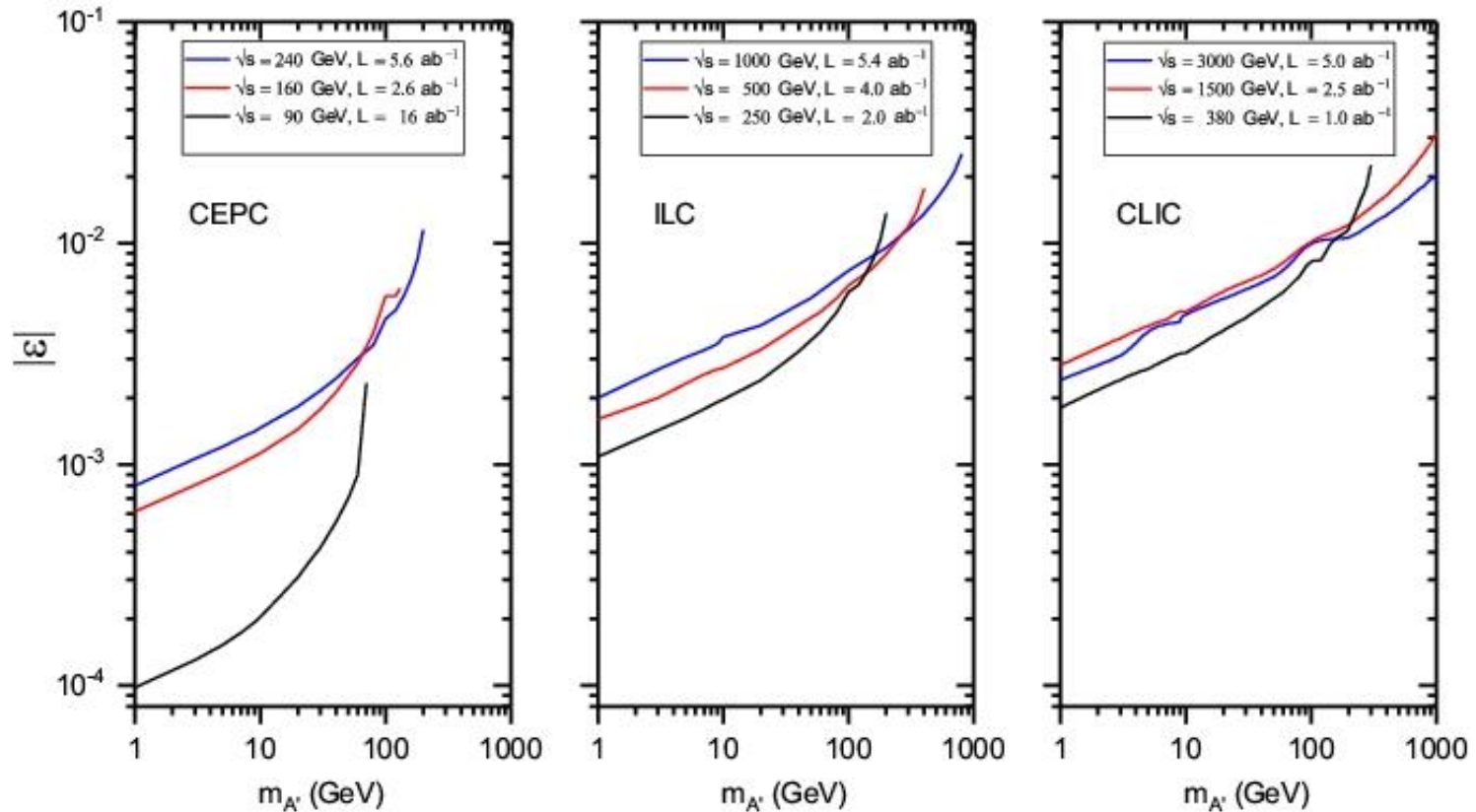
Differential cross sections for  $\gamma e^- \rightarrow e^- + E_{\text{miss}}$  scattering at the collider **CEPC**. DP mass is  $m_{A'} = 50 \text{ GeV}$ , mixing parameter is  $\varepsilon = 0.1$ . Black curves are SM predictions.



Differential cross sections for  $\gamma e^- \rightarrow e^- + E_{\text{miss}}$  scattering at the collider ILC. DP mass is  $m_{A'} = 100 \text{ GeV}$ , mixing parameter is  $\epsilon = 0.1$ . Black curves are SM predictions.

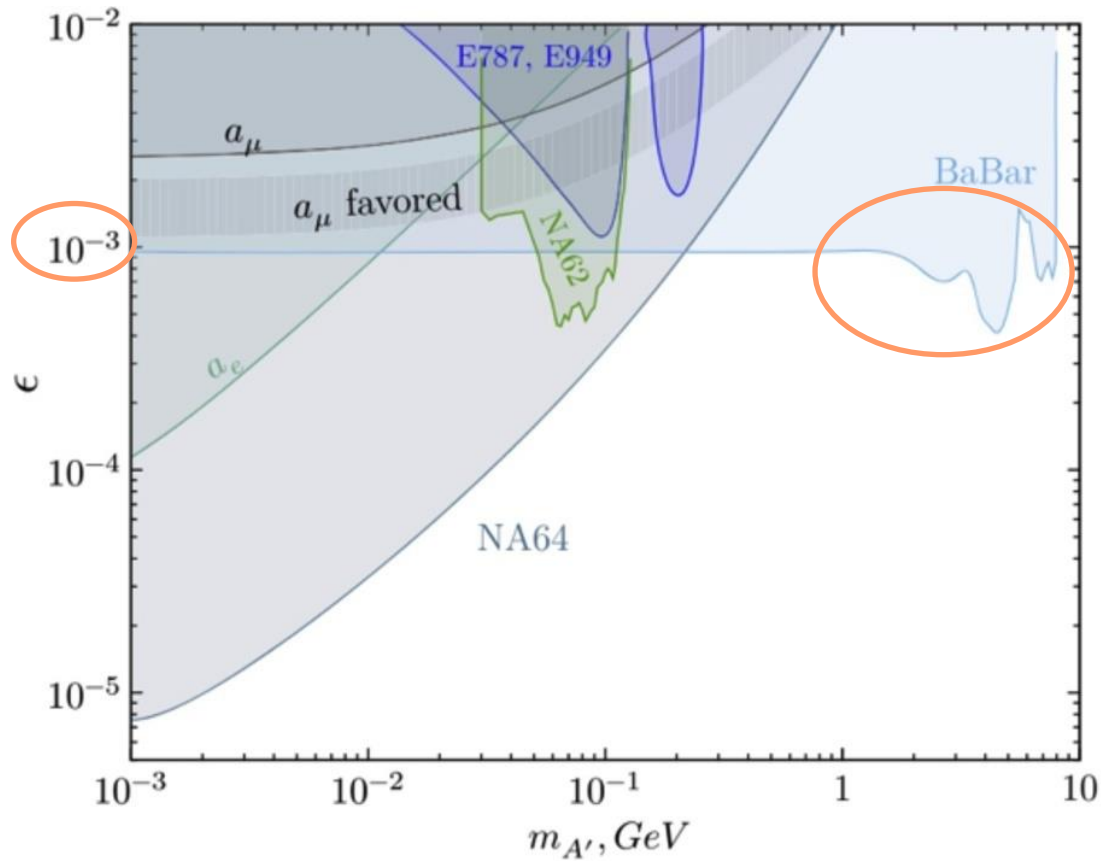


Differential cross sections for  $\gamma e^- \rightarrow e^- + E_{\text{miss}}$  scattering at the collider CLIC. DP mass is  $m_{A'} = 200 \text{ GeV}$ , mixing parameter is  $\epsilon = 0.1$ . Black curves are SM predictions.



Excluded bounds at 95% C.L. on DP mass  $m_{A'}$  and mixing parameter  $\epsilon$  for invisible DP production in  $\gamma e^- \rightarrow A' e^-$  *unpolarized* scattering at future lepton colliders

$p_{e,t} > 10$  GeV,  $|\eta_e| < 2.5$ ,  $|m_{A'} - m_{\text{miss}}| < 10$  GeV



Exclusion limits on mixing parameter  $\epsilon$   
for massive DP going into invisible states

(A. Filippi & M. De Napoli, *Rev. Phys.* 5, 100042, 2020)

# Conclusions

- We have studied anomalous quartic neutral gauge couplings in unpolarized and polarized LBL scattering of CB photons at 3 TeV CLIC
- Exclusion regions for these couplings are obtained. Our best constraints are  $\zeta_1 = 6.9 \cdot 10^{-4} \text{ TeV}^{-4}$  and  $\zeta_2 = 1.4 \cdot 10^{-3} \text{ TeV}^{-4}$ , one order of magnitude stronger than the HL-LHC bounds derived for integrated luminosity of  $3 \text{ ab}^{-1}$
- Sensitivity to anomalous couplings of the  $\gamma\gamma Z$  vertex is examined using CB photon scattering  $\gamma\gamma \rightarrow \gamma Z$  at 3 TeV CLIC. For both couplings,  $g_1$  and  $g_2$ , our best bound is  $5 \cdot 10^{-3} \text{ TeV}^{-4}$ , while the HL-LHC bounds are  $(1-0.7) \cdot 10^{-1} \text{ TeV}^{-4}$



- For the first time, production of the massive DP in  $\gamma e$  scattering at future lepton colliders ILC, CLIC and CEPC is studied
- Invisible decay mode of DP is addressed. Wide range, 1 GeV - 1 TeV, of DP mass  $m_{A'}$  is considered. We have obtained exclusion regions in the plane  $(m_{A'}, \varepsilon)$ , where  $\varepsilon$  is the kinetic mixing parameter
- In low mass region, 1-10 GeV, our bounds on  $\varepsilon$  for the 90 CEPC are several times stronger than BaBar limit ( $\sim 10^{-3}$ ). The CEPC bounds for 160 and 240 GeV, as well as bounds for the 250 ILC are close to the BaBar constraints

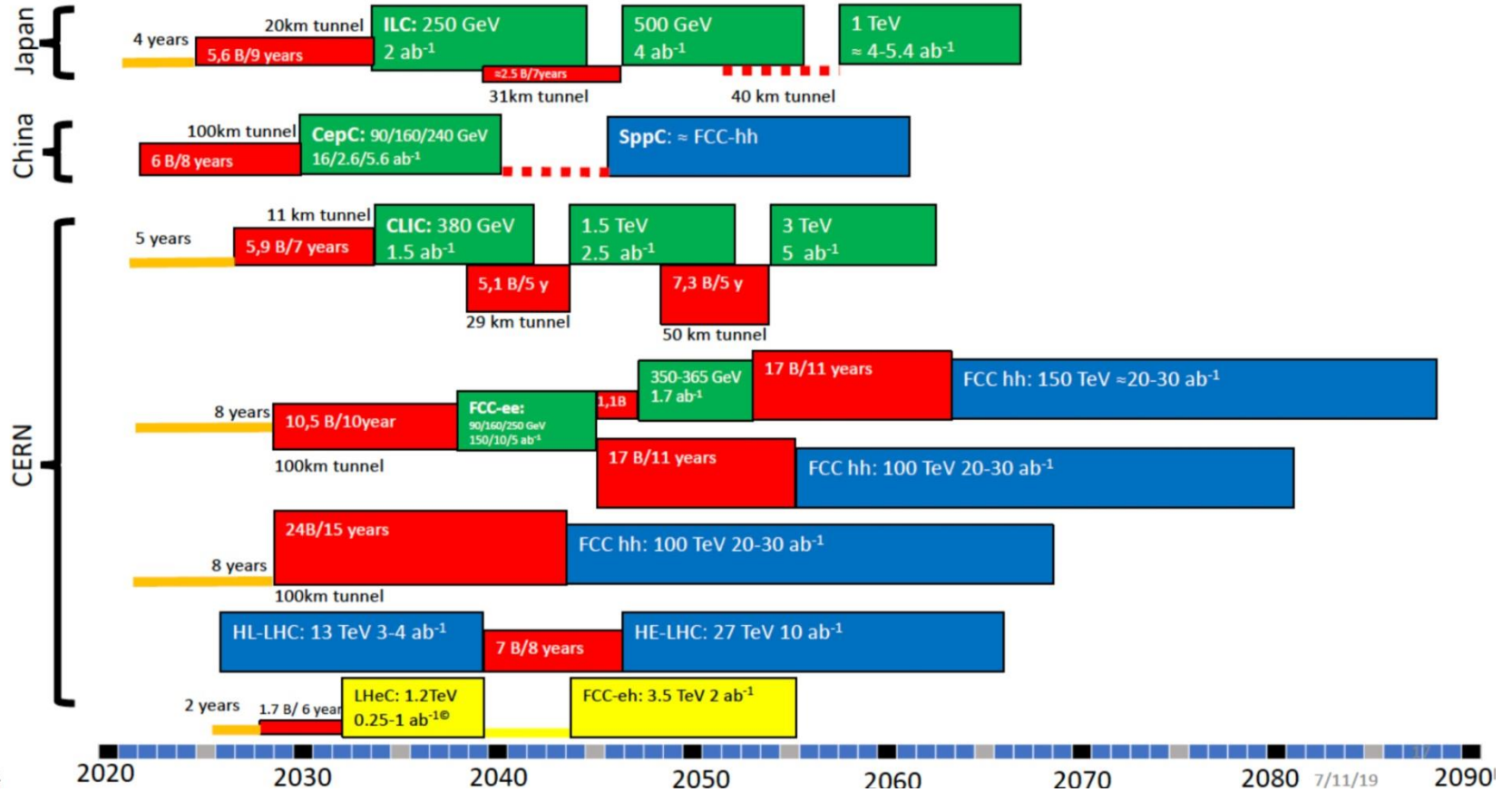
**Thank you for  
your attention**

# Back-up slides

# Possible scenario of future colliders

Possible scenarios of future colliders

- Proton collider
- Electron collider
- Electron-Proton collider
- Construction/Transformation: heights of box construction cost/ye
- Preparation

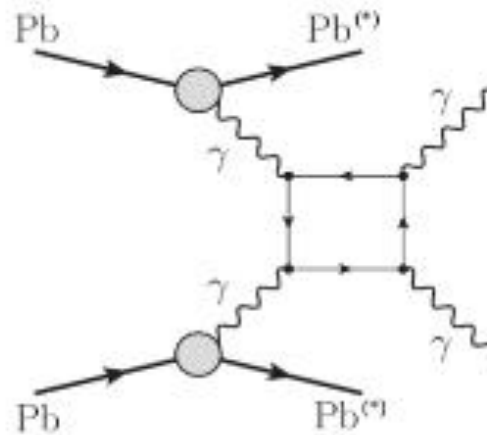


# Anomalous $\gamma\gamma\gamma\gamma$ vertex

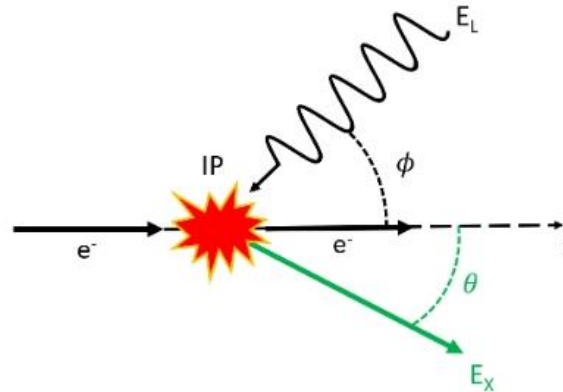
# The first evidence of $\gamma\gamma \rightarrow \gamma\gamma$ process was observed by ATLAS & CMS in Pb-Pb collisions

*(ATLAS Collab., Nat. Phys., 13, 852, 2017)*

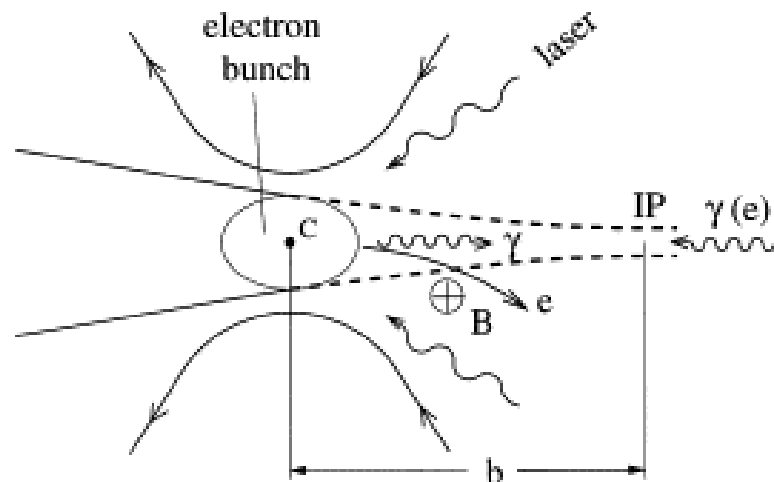
*(CMS Collab., Phys. Rev. Lett. 123, 052001, 2019)*



# Inverse laser-Compton scattering process



## Scheme of $\gamma\gamma$ ( $\gamma e$ ) collider



## Helicity of CB photon

$$\xi(E_\gamma, \lambda_0) = \frac{\lambda_0(1-2r)[1-x+1/(1-x)] + \lambda_e r \zeta [1+(1-x)(1-2r)^2]}{1-x+1/(1-x) - 4r(1-r) - \lambda_e \lambda_0 r \zeta (2r-1)(2-x)},$$

where  $x = E_\gamma/E_e$ ,  $r = x/\zeta(1-x)$ ,  $\zeta = 4E_e E_0/m_e^2$ ,  $m_e$  being the electron mass.

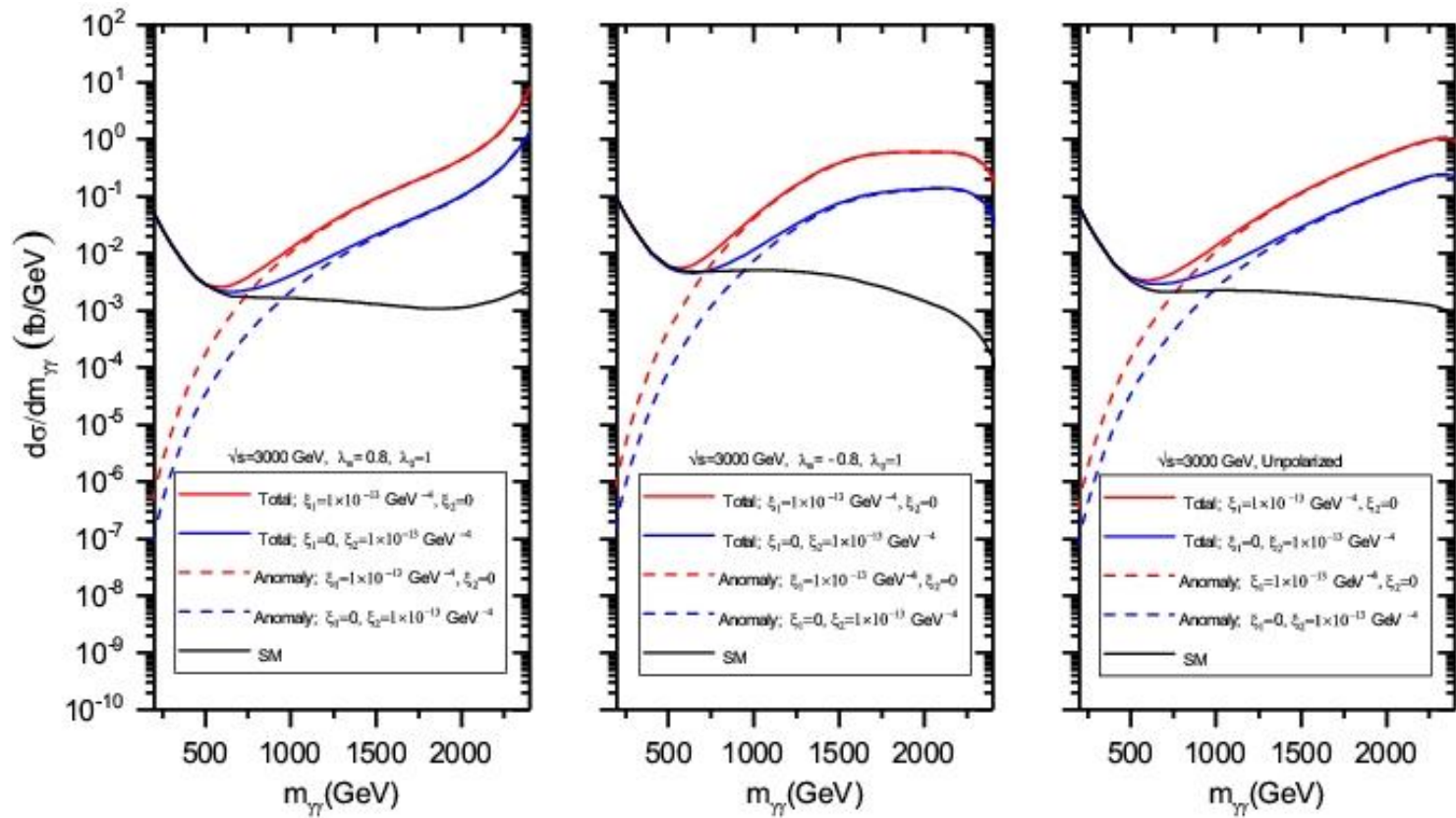


## Spectrum of CB photons

$$f_{\gamma/e}(x) = \frac{1}{g(\zeta)} \left[ 1 - x + \frac{1}{1-x} - \frac{4x}{\zeta(1-x)} + \frac{4x^2}{\zeta^2(1-x)^2} + \lambda_0 \lambda_e r \zeta (1-2r)(2-x) \right],$$

where

$$g(\zeta) = g_1(\zeta) + \lambda_0 \lambda_e g_2(\zeta),$$
$$g_1(\zeta) = \left( 1 - \frac{4}{\zeta} - \frac{8}{\zeta^2} \right) \ln(\zeta + 1) + \frac{1}{2} + \frac{8}{\zeta} - \frac{1}{2(\zeta + 1)^2},$$
$$g_2(\zeta) = \left( 1 + \frac{2}{\zeta} \right) \ln(\zeta + 1) - \frac{5}{2} + \frac{1}{\zeta + 1} - \frac{1}{2(\zeta + 1)^2}.$$



Differential cross sections for the process  $\gamma\gamma \rightarrow \gamma\gamma$  versus invariant mass of outgoing photons at  $\sqrt{s} = 3$  TeV. The left, middle and right panels correspond to  $\lambda_e = 0.8, -0.8, 0$ .

Solid curves (from top downwards):  
 $(\zeta_1 = 10^{-13} \text{ GeV}^{-4}, \zeta_2 = 0)$ ,  $(\zeta_1 = 0, \zeta_2 = 10^{-13} \text{ GeV}^{-4})$ , SM.

## Discovery significance ( $\delta$ = percentage systematic error)

$$S_{\text{dis}} = \sqrt{2} \left[ (s+b) \ln \left( \frac{(s+b)(1+\delta^2 b)}{b + \delta^2 b(s+b)} \right) - \frac{1}{\delta^2} \ln \left( 1 + \frac{\delta^2 s}{1 + \delta^2 b} \right) \right]^{1/2}$$

In the limit  $\delta = 0$

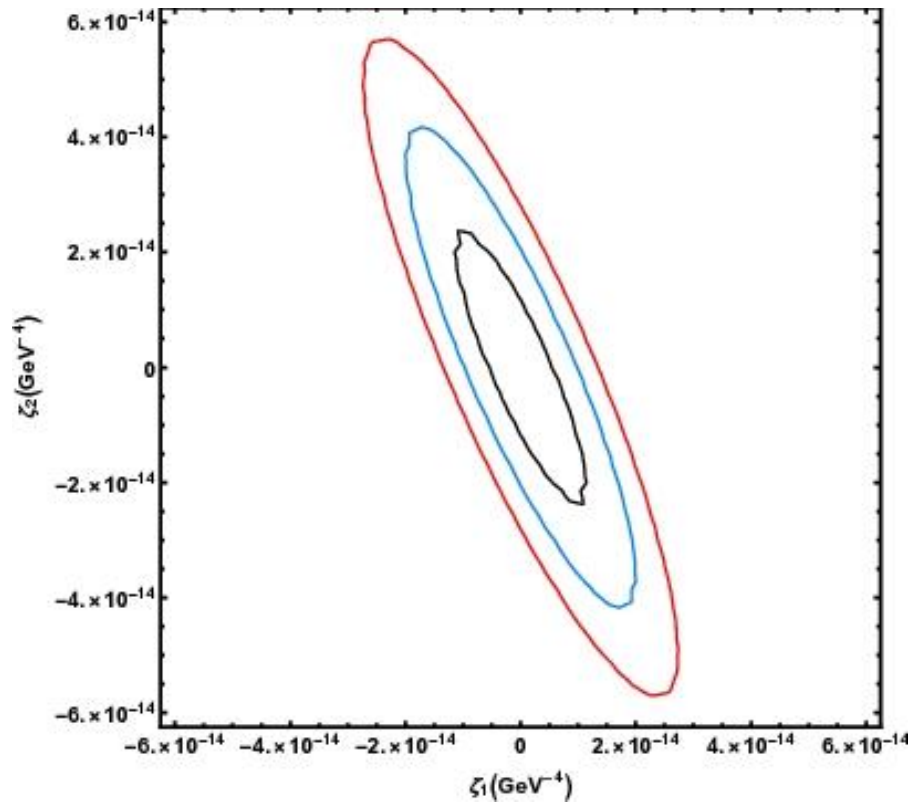
$$S_{\text{dis}} = \sqrt{2 \left[ (s+b) \ln \left( 1 + \frac{s}{b} \right) - s \right]}$$

$s \ll b$



$$S_{\text{dis}} = \frac{s}{\sqrt{b}}$$

$S_{\text{dis}} \geq 5$  as discovery region



$$|\eta_{\gamma\gamma}| < 2.5$$

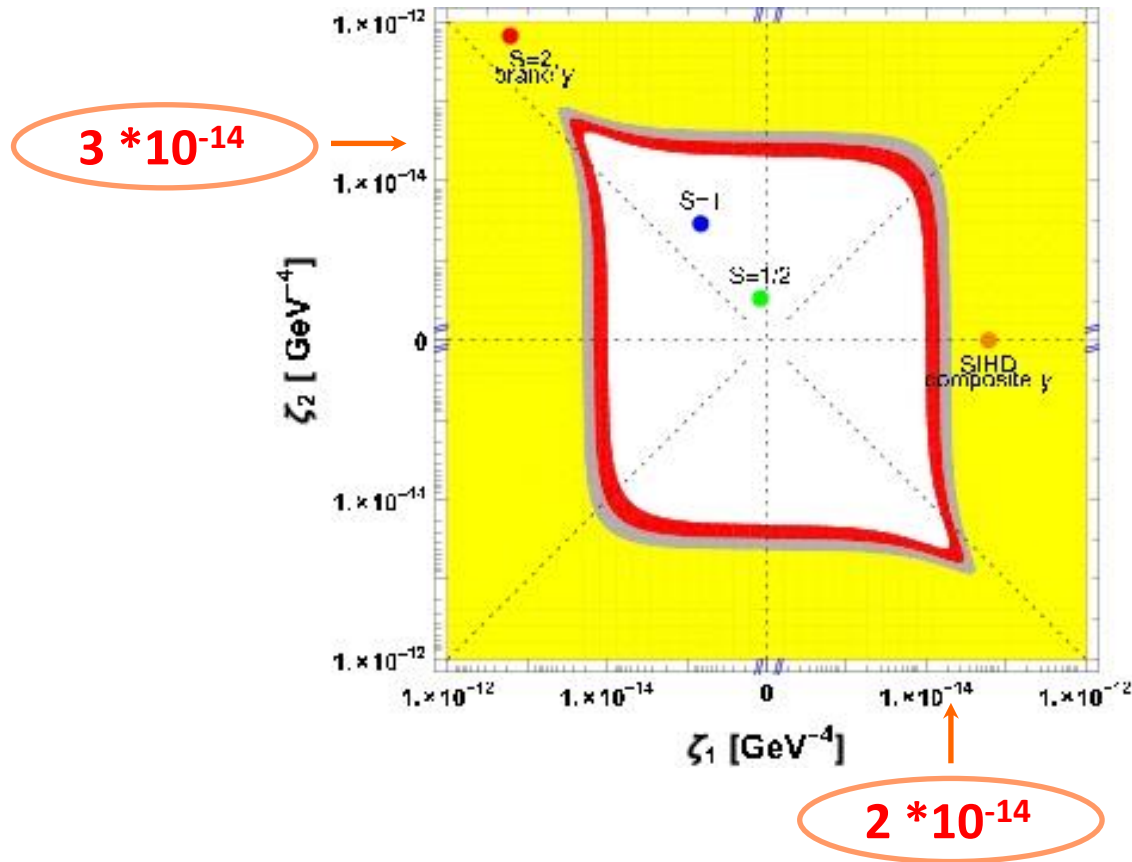
$$m_{\gamma\gamma} > 1 \text{ TeV}$$

95% C.L. exclusion region for anomalous couplings  $\zeta_1, \zeta_2$  for **unpolarized** LBL scattering at the CLIC. Systematic errors are 0%, 5%, and 10%. The collision energy is **1.5 TeV**, the integrated luminosity is **2.5 ab<sup>-1</sup>**. Couplings  $\zeta_1, \zeta_2$  are in **GeV<sup>-4</sup>**.

*(S.Inan & A.K., EPJC, 81, 664, 2021)*

# Bounds on anomalous couplings for LHC

(S.Fichet et al., JHEP 02, 165, 2015)



# Anomalous $\gamma\gamma Z$ vertex

## Another effective Lagrangian for anomalous $\gamma\gamma Z$ couplings

$$L_{\gamma\gamma Z} = \tilde{g}_1(F_{\mu\nu}F^{\mu\nu})(F_{\rho\sigma}Z^{\rho\sigma}) + \tilde{g}_2(F_{\mu\nu}\tilde{F}^{\mu\nu}F_{\rho\sigma}\tilde{Z}^{\rho\sigma})$$

*(C. Baldenegro et al., JHEP 06, 142, 2017)*



Relations between two sets  
of coupling constants

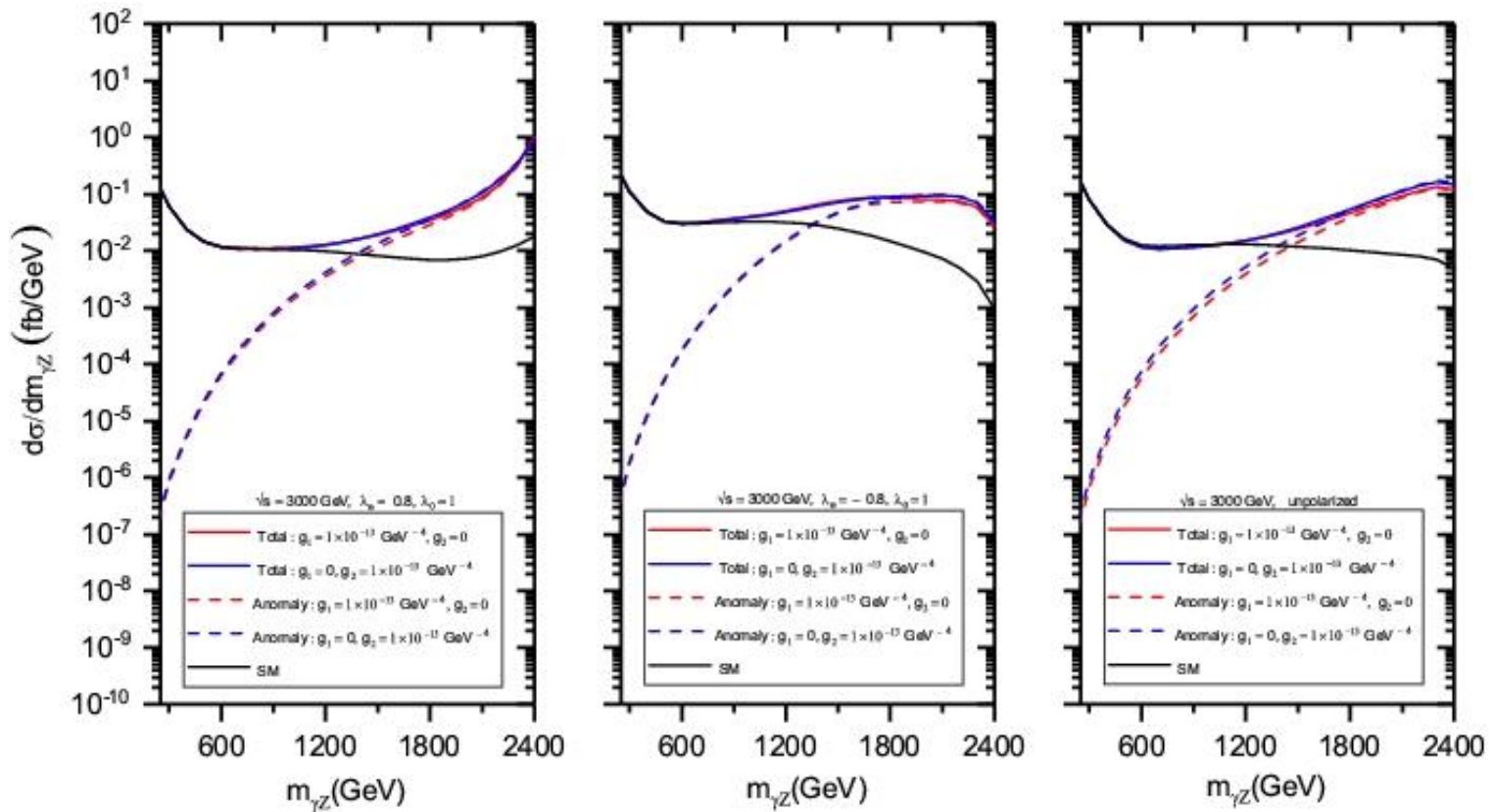
$$g_1 = 8(\tilde{g}_2 - \tilde{g}_1), \quad g_2 = 8\tilde{g}_2$$

## Unpolarized case

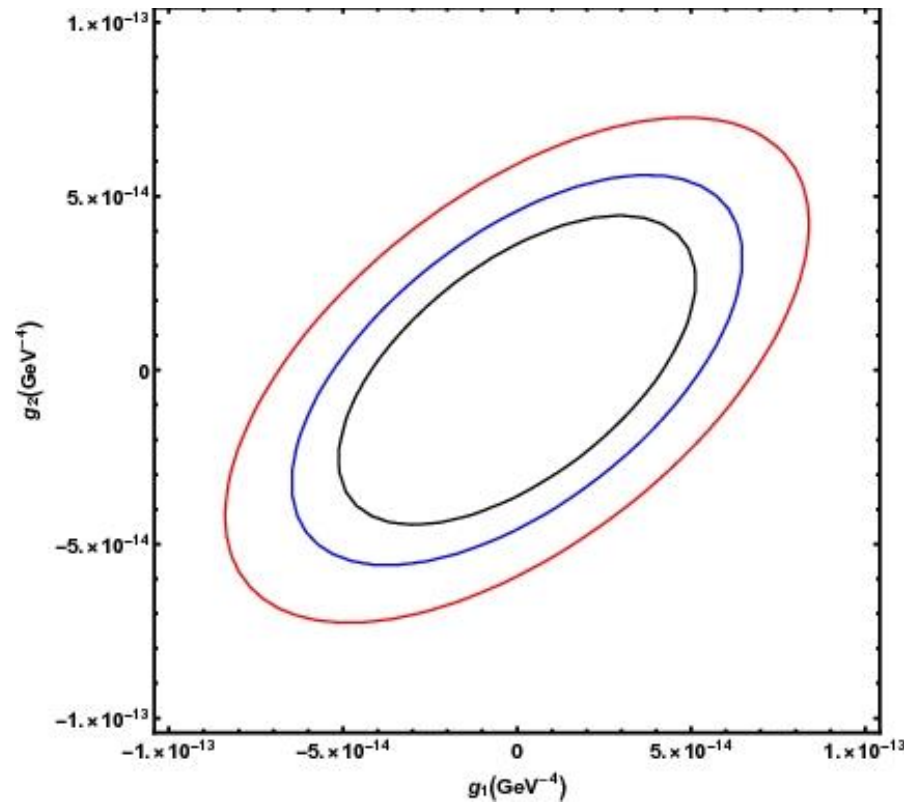
$$\sum_{\lambda_1 \dots \lambda_4} |M_{\lambda_1 \lambda_2 \lambda_3 \lambda_4}|^2 = \frac{1}{4} [g_1^2(3A + 2B) - 4g_1 g_2(A + B) + 4g_2^2(A + B)]$$

$$A = s^2 t^2 + t^2 u^2 + u^2 s^2, \quad B = stu m_Z^2$$





Differential cross sections for the process  $\gamma\gamma \rightarrow \gamma Z$  versus invariant mass of outgoing photons at  $\sqrt{s} = 3$  TeV. The left, middle and right panels correspond to  $\lambda_e = 0.8, -0.8, 0$ . Solid curves (from top downwards): ( $g_1 = 10^{-13} \text{ GeV}^{-4}, g_2 = 0$ ), SM.



$$|\eta| < 2.5$$

$$m_{\gamma Z} > 1 \text{ TeV}$$

95% C.L. exclusion region for anomalous couplings  $g_1, g_2$  for **unpolarized**  $\gamma\gamma \rightarrow \gamma Z$  scattering at the CLIC. Systematic errors are 0%, 5%, and 10%. The collision energy is **1.5 TeV**, the integrated luminosity is **2.5 ab<sup>-1</sup>**. Couplings  $g_1, g_2$  are **in GeV<sup>-4</sup>**.

*(S.Inan & A.K., JHEP, 10, 121, 2021)*

## Partial-wave expansion of helicity amplitude

*(M. Jacob & G. Wick, Ann. Phys. 7, 404, 1959; ibid 281, 774 2000)*

$$M_{\lambda_1\lambda_2\lambda_3\lambda_4}(s, \theta, \varphi) = 16\pi \sum_J (2J + 1) \sqrt{(1 + \delta_{\lambda_1\lambda_2})(1 + \delta_{\lambda_3\lambda_4})} \\ \times e^{i(\lambda - \mu)\phi} d_{\lambda\mu}^J(\theta) T_{\lambda_1\lambda_2\lambda_3\lambda_4}^J(s)$$

$d_{\lambda\mu}^J =$  Wigner's (small) d-function

$$T_{\lambda_1\lambda_2\lambda_3\lambda_4}^J(s) = \frac{1}{32\pi} \frac{1}{\sqrt{(1 + \delta_{\lambda_1\lambda_2})(1 + \delta_{\lambda_3\lambda_4})}} \int_{-1}^1 M_{\lambda_1\lambda_2\lambda_3\lambda_4}(s, z) d_{\lambda\mu}^J(z) dz$$

Partial-wave **unitarity** bound

$$\left| T_{\lambda_1\lambda_2\lambda_3\lambda_4}^J(s) \right| \leq 1$$

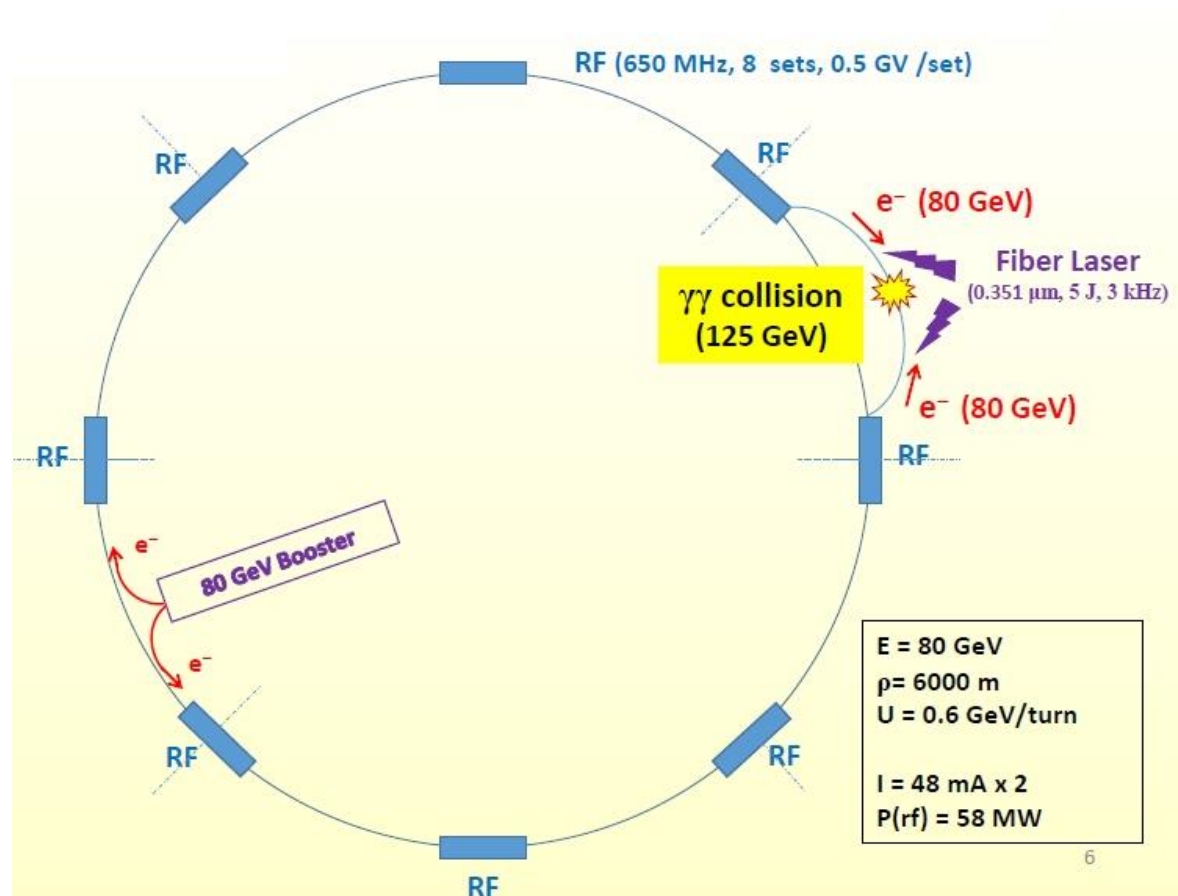
# Invisible dark photons

## Diagonalization of gauge fields $W^3$ , B and DP field $A'$

$$\begin{pmatrix} W_\mu^3 \\ B_\mu \\ \bar{A}'_\mu \end{pmatrix} = \begin{pmatrix} c_W & s_W & -s_W \varepsilon \\ -s_W & c_W & -c_W \varepsilon \\ t_W \varepsilon & 0 & 1 \end{pmatrix} \begin{pmatrix} Z_\mu \\ A_\mu \\ A'_\mu \end{pmatrix}$$

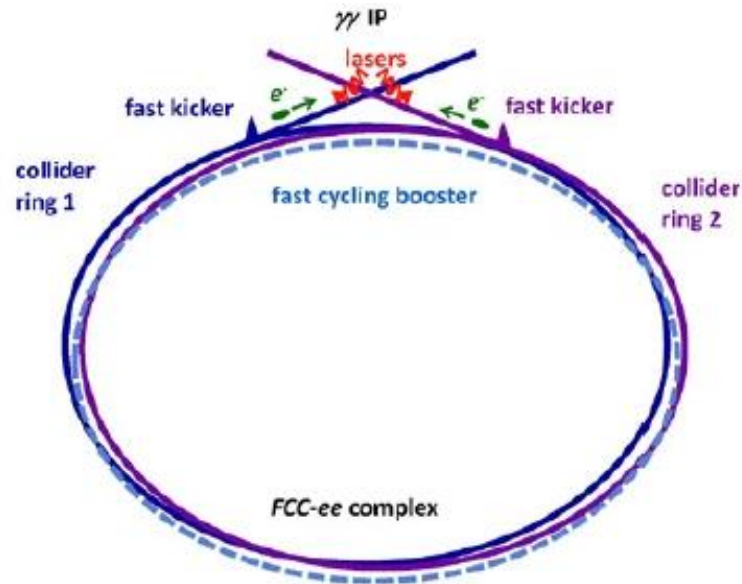
# CEPC as a $\gamma\gamma$ factory

*(Ch. Zhang & W. Chou, Photon Beam Workshop, Padova, Italy, 2017)*



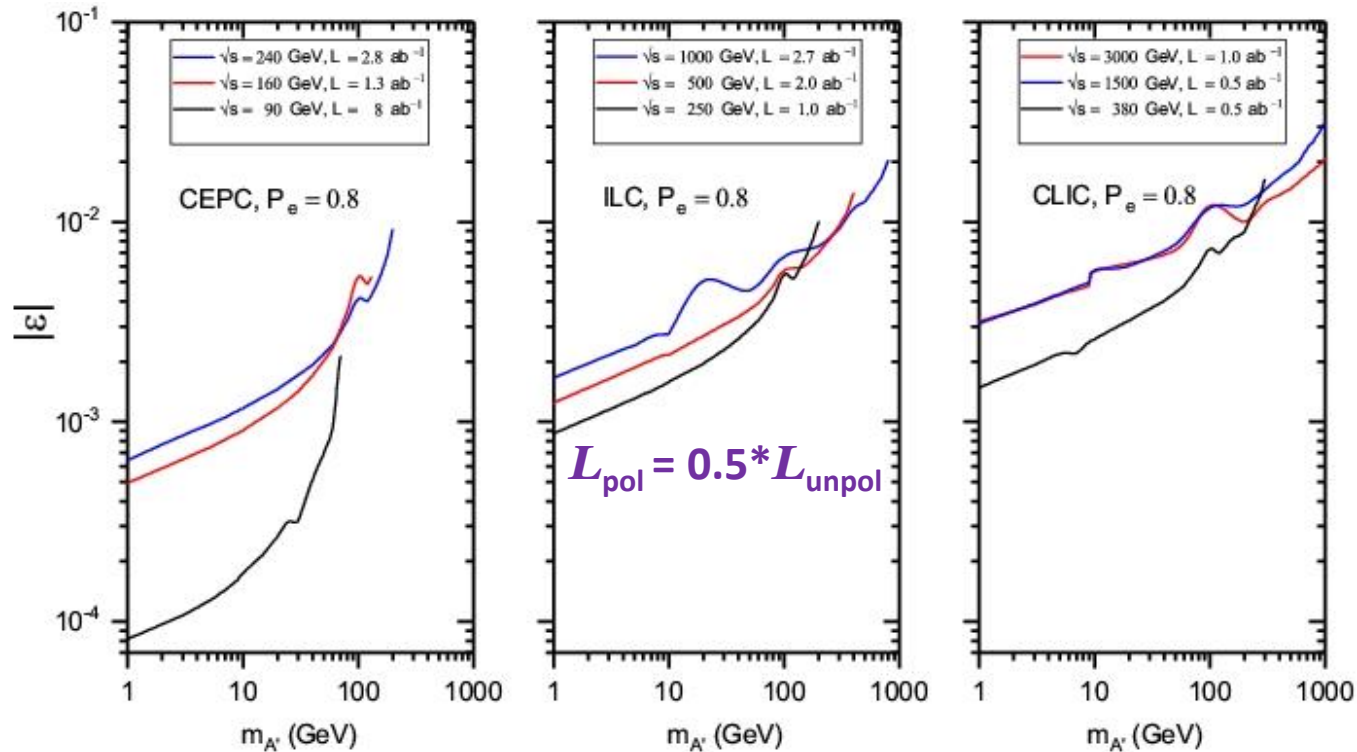
# FCC-ee as a $\gamma\gamma$ factory

*(R. Alesan et al., IPAC 2015, Richmond, VA, USA, 2015)*



$\gamma\gamma$  Higgs factory can be realized by back-scattering two counter-propagating electron bunches off laser pulses

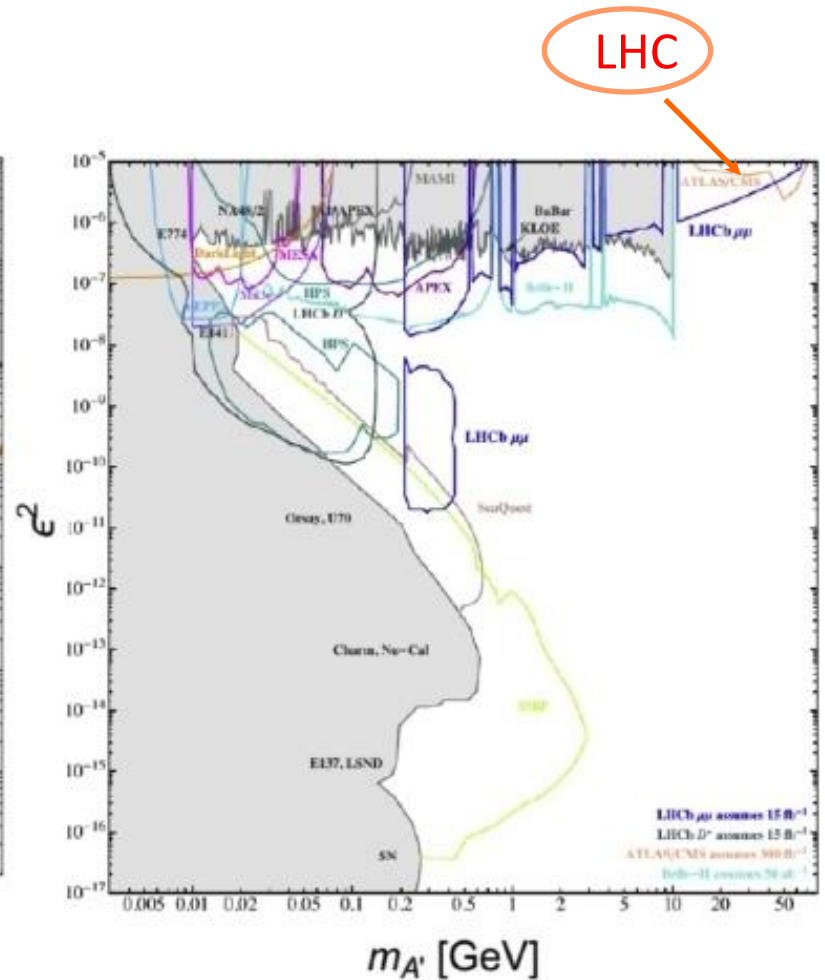
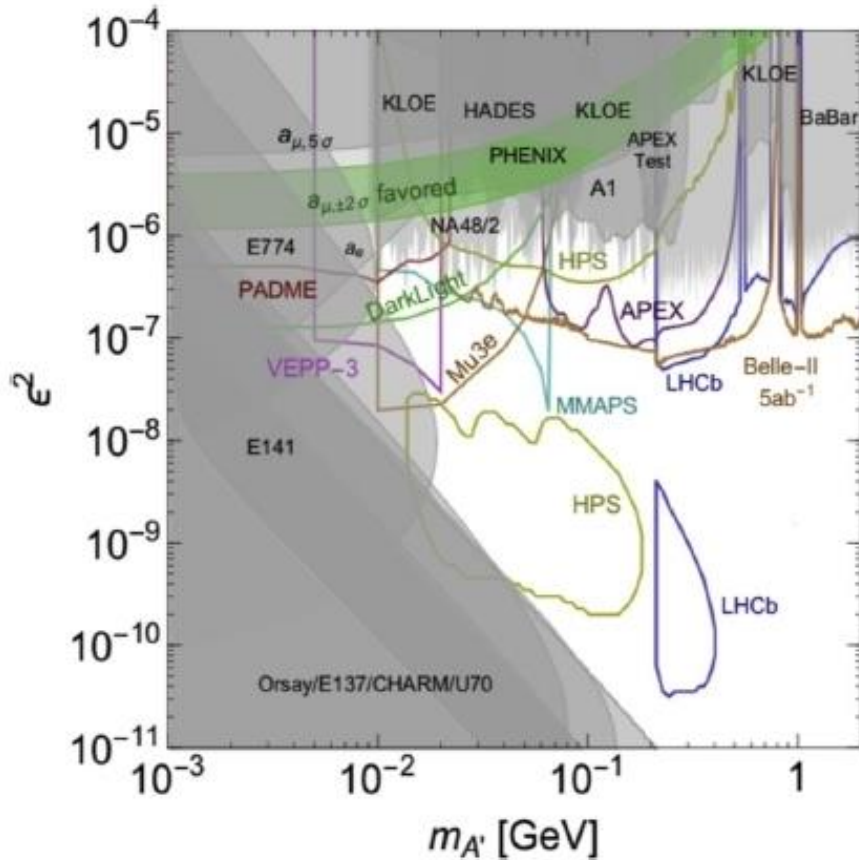
(S.Inan & A.K., EPJC, 82, 592, 2022)



Excluded bounds at 95% C.L. on DP mass  $m_{A'}$  and mixing parameter  $\epsilon$  for invisible DP production in collision of *unpolarized* photon and electron whose *polarization is 80%*

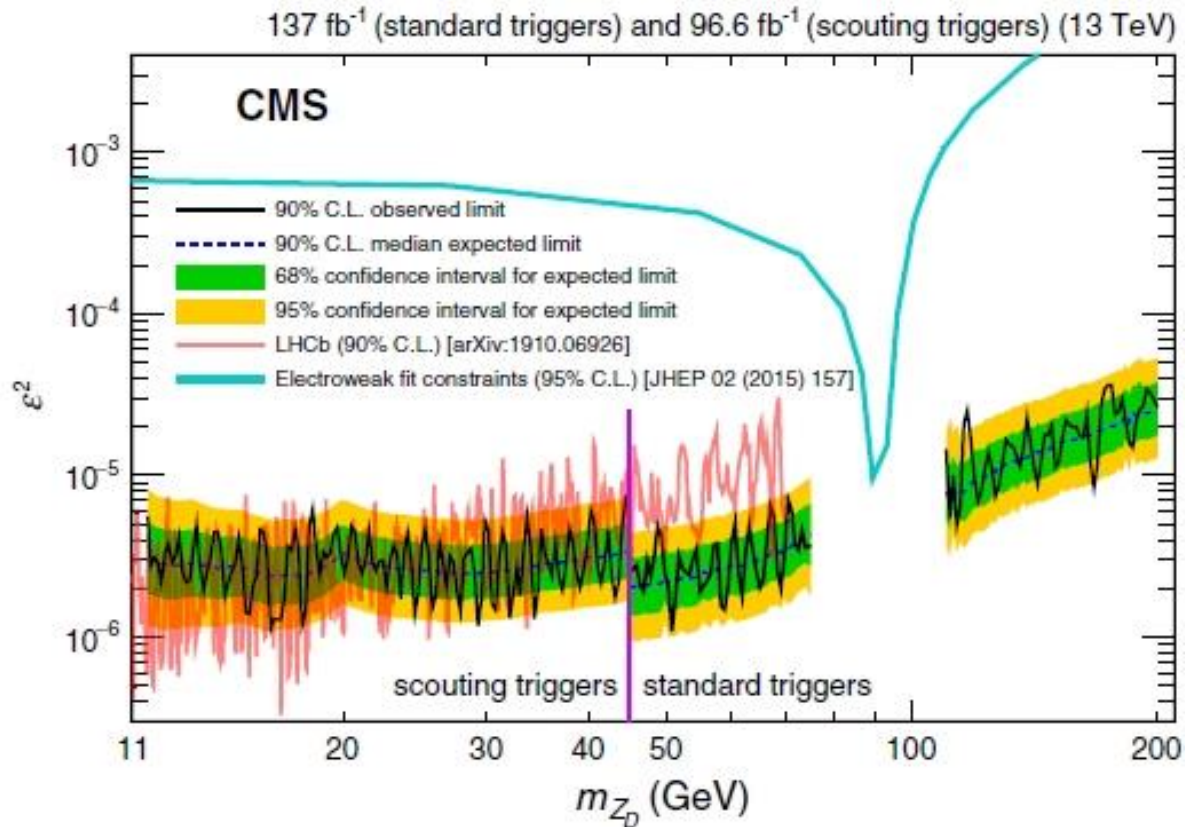
$$p_{e,t} > 10 \text{ GeV}, |\eta_e| < 2.5, |m_{A'} - m_{\text{inv}}| < 10 \text{ GeV}$$





Existing bounds (shaded regions) for DP in **visible** decays

*(A. Filippi & M. De Napoli, Rev. Phys. 5, 100042, 2020)*



**CMS limit on mixing parameter for DP decaying into muon pair**

*(CMS Collab., Phys. Rev. Lett. 124, 131802, 2020)*

# DP at future ep colliders LHeC and FCC-he

*(CMS Collab., Phys. Rev. D 101, 015020, 2020)*

