

Associated production of $J/\psi + \gamma$ at the energy of SPD NICA

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- 3 Hadronization mechanisms: CSM, NRQCD and CEM
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Introduction

$$J/\psi = c\bar{c}[^3S_1], M(J/\psi) = 3.097 \text{ GeV}, \Gamma = 92.9 \text{ keV}$$

$$\Gamma(J/\psi \rightarrow \mu^+\mu^-) = 5.55 \text{ keV}$$

$$Br(J/\psi \rightarrow \mu^+\mu^-) = 5.9 \times 10^{-2}$$

Introduction

- Up to now we deal with charmonium puzzles: J/ψ polarization, double J/ψ , ...
- Test of perturbative QCD, $M_\psi \gg \Lambda_{QCD}$
- Test of heavy quark hadronization mechanism: NRQCD, CSM and CEM
- Tools for study gluon structure of proton, including helicity structure functions.
- Study of J/ψ production motivates a lot of new theoretical works about factorization, resummation and evolution ...

Factorization approaches: CPM, TMD, and GPM

Hard (factorization) scale $\mu_F \sim M_\psi$

Intrinsic parton transverse momentum $\langle q_T^2 \rangle \sim 1 \text{ GeV}^2$

- **Collinear parton model:** $q_{1,2T} \ll p_T$ and $\mu_F = M_T \geq M$

$$\sigma(pp \rightarrow \eta_c X) = \int dx_1 \int dx_2 f_g(x_1, \mu_F) f_g(x_2, \mu_F) \hat{\sigma}(g + g \rightarrow \eta_c + g)$$

- **TMD PM** by Collins, Soper, Stermann: $q_{1,2T} \sim p_T$ and $p_T \ll \mu_F$

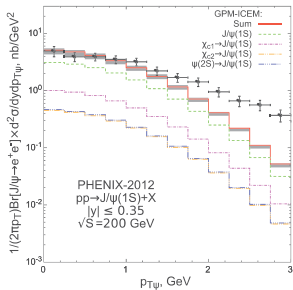
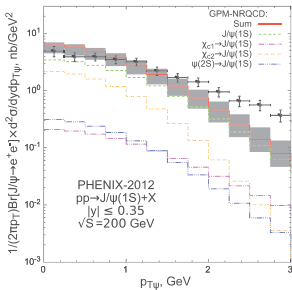
$$\begin{aligned} \sigma(pp \rightarrow \eta_c X) = & \int dx_1 d^2 q_{1T} \int dx_2 d^2 q_{2T} F_g(x_1, q_{1T}, \mu_F, \mu_Y) \times \\ & \times F_g(x_2, q_{2T}, \mu_F, \mu_Y) \hat{\sigma}(g + g \rightarrow \eta_c) \end{aligned}$$

- **Generalized parton model:** $q_{1,2T} \sim p_T$ and $p_T \sim \mu_F$

$$\begin{aligned} \sigma(pp \rightarrow \eta_c X) = & \int dx_1 d^2 q_{1T} \int dx_2 d^2 q_{2T} F_g(x_1, q_{1T}, \mu_F) \times \\ & \times F_g(x_2, q_{2T}, \mu_F) \hat{\sigma}(g + g \rightarrow \eta_c) \\ F_g(x, q_T, \mu_F) = & f_g(x, \mu_F) \times \exp(-q_T^2 / \langle q_T^2 \rangle) / (\pi \langle q_T^2 \rangle) \end{aligned}$$

Hadronization mechanisms: CSM, NRQCD and CEM

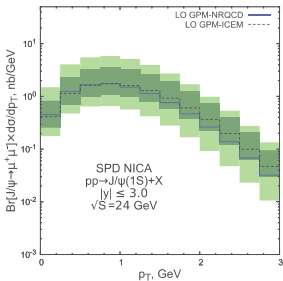
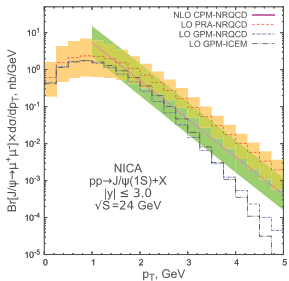
- Color Singlet Model (CSM): only $c\bar{c}$ -pairs with matched quantum number of the charmonium, $^3S_1^{(1)}$ for J/ψ -meson.
- Non-relativistic QCD (NRQCD): all $c\bar{c}$ -pairs of different color and spin states fragmenting with different probabilities long distance matrix elements (LDME)
- Color Evaporation Model (CEM): all $c\bar{c}$ -pairs with mass less than $D\bar{D}$ threshold. One hadronization parameter for each charmonium is used.

J/ψ production in CPM and GPM within framework of CSM J/ψ production at the PHENIX

J/ψ production in CPM and GPM within framework of CSM

J/ψ production at the PHENIX leads to following conclusions:

- Color octet LDMEs are not needed at low energy and small p_T . Color singlet LDME $\langle \mathcal{O}[^3S_1^{(1)}] \rangle$ can be calculated in potential model, $(|\Psi(0)|^2)$, or extracted decay width $\Gamma(J/\psi \rightarrow \mu^+ \mu^-)$.
- In process $g + g \rightarrow J/\psi + \gamma$, final state is colorless and we can neglect final-state interactions with soft (Glauber) gluons, which destroy hard-soft factorization.

J/ψ production in CPM and GPM within framework of CSM J/ψ production at the SPD NICA

$J/\psi + \gamma$ production in CPM and GPM within framework of CSMCPM for $p_T \geq M$

$$g + g \rightarrow c\bar{c}[{}^3S_1^{(1)}] + \gamma$$

GPM for $p_T < M$. There is no reduction to $2 \rightarrow 1$ subprocess in CSM

$$g + g \rightarrow c\bar{c}[{}^3S_1^{(1)}] + \gamma$$

For prompt J/ψ production we include following contributions:

$$g + g \rightarrow \psi(2S) + \gamma, \quad \psi(2S) \rightarrow J/\psi X$$

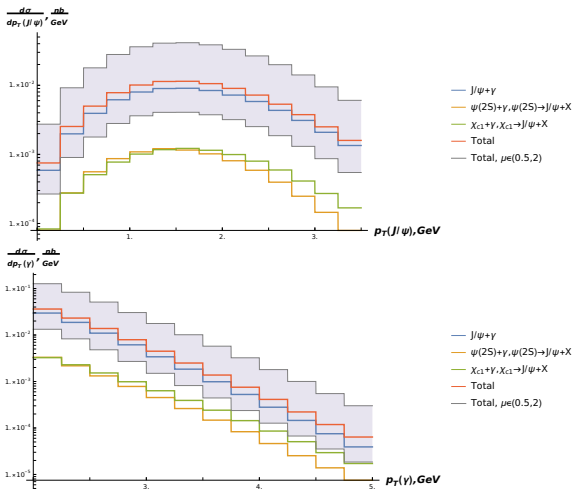
$$g + g \rightarrow \chi_{c1} + \gamma, \quad \chi_{c1} \rightarrow J/\psi X$$

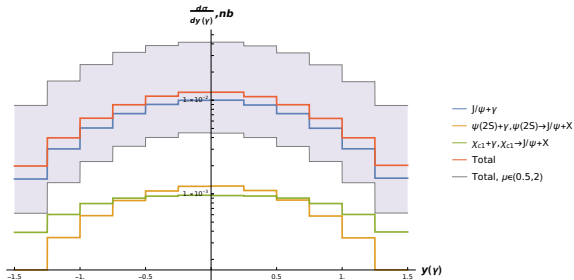
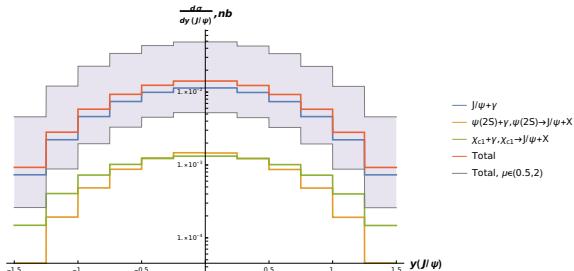
Processes of the following order

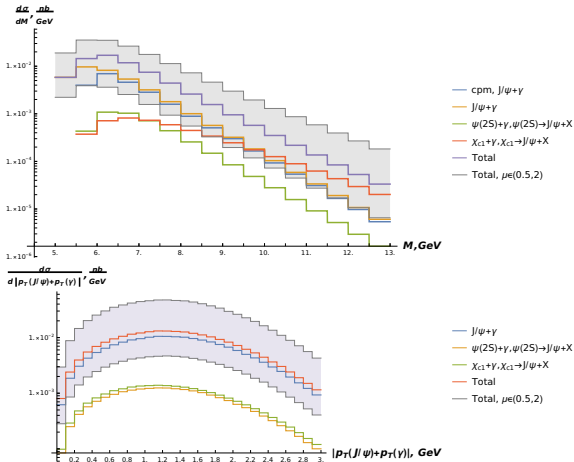
$$g + g \rightarrow J/\psi + g(\rightarrow \gamma)$$

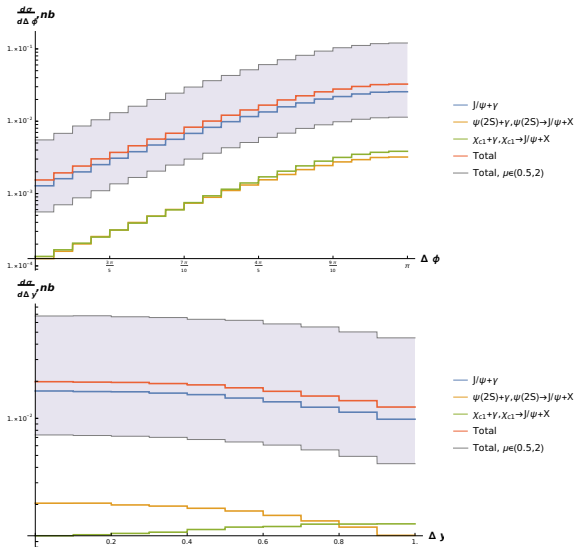
$$g + g \rightarrow \chi_{cj} + g(\rightarrow \gamma), \chi_{cj} \rightarrow J/\psi X, j = 1, 2, 3$$

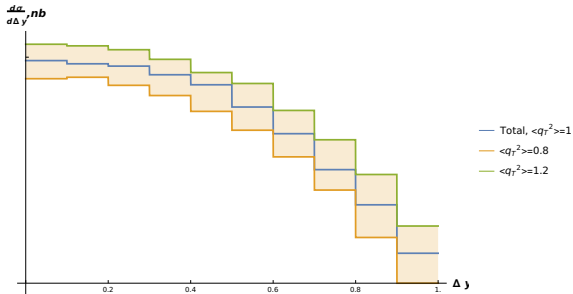
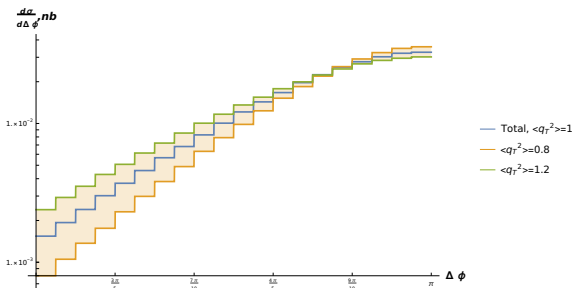
$$g + g \rightarrow \psi(2S) + g(\rightarrow \gamma), \psi(2S) \rightarrow J/\psi X$$

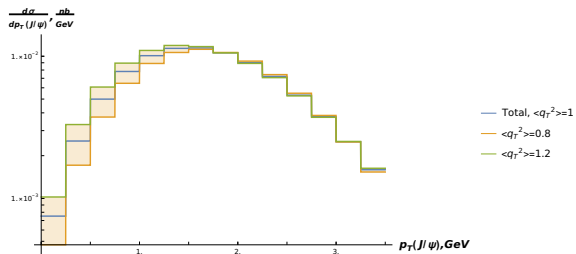
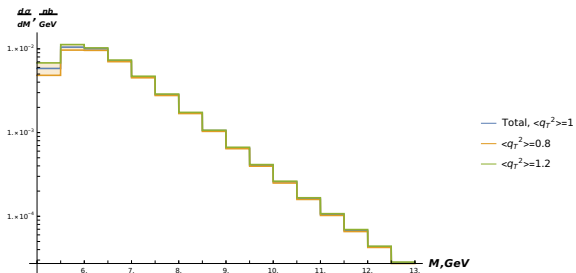
$J/\psi + \gamma$ production in CPM and GPM within framework of CSM

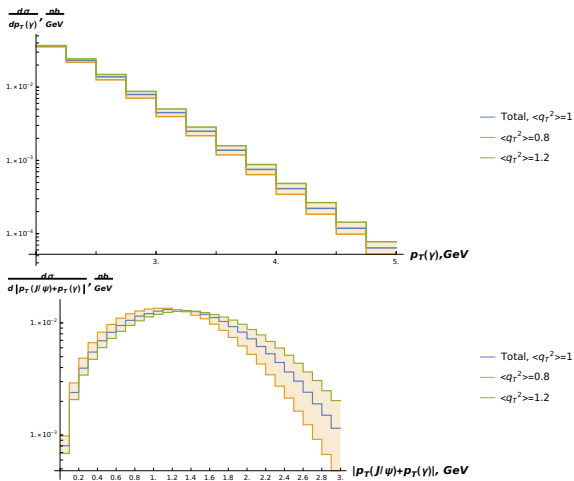
$J/\psi + \gamma$ production in CPM and GPM within framework of CSM

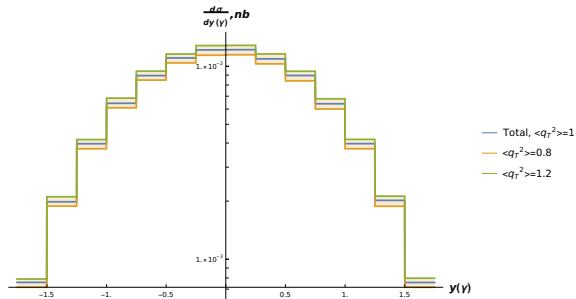
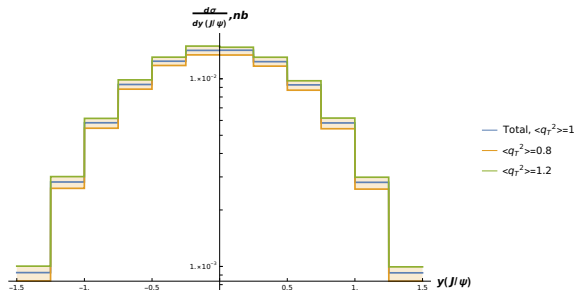
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$J/\psi + \gamma$ production in CPM and GPM within framework of CSM

Conclusions

- We estimate cross section of associated $J/\psi + \gamma$ production at the energy of SPD NICA as 5.7×10^{-3} nb, where $p_{T\psi} \in [0, 6]$ GeV, $|y_\psi, y_\gamma| \in [0, 3]$ and $p_{T\gamma} \in [2, 6]$ GeV.
- We calculate J/ψ and γ transverse momentum and rapidity spectra, as well as azimuthal angle difference and rapidity difference spectra in GPM+CSM approach.
- The factorization-scale choice uncertainty is found as large, about factor 2.
- We test dependence of obtained results as function of average intrinsic transverse momentum of gluon, $\langle q_T^2 \rangle$.

Thank you for your attention!