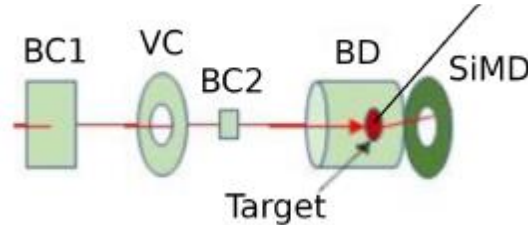


1 **Measurement of the integrated ion flux and calculation of the luminosity.**

2 To count the number of beam ions that passed through the target (beam flux N_b), a logical beam trigger
 3 $BT = BC1 \otimes VC \otimes BC2$ was used. The beam flux for active (not busy) time of DAQ was integrated spill by
 4 spill. The probability of two and more ions giving BT signal within 20 ns of BT coincidence time window is
 5 within 2% taken as the systematic uncertainty of the beam flux measurement.



6

7 Luminosity L was calculated according to the formula:

8
$$L = N_b \cdot N_A \cdot \rho \cdot l / A \cdot \text{Corr} ;$$

9 where N_b – integrated ion flux through the target, measured by BT trigger, N_A – Avogadro
 10 number, $\rho \cdot l$ – target thickness (g/cm^2), A – target atomic weight, Corr – correction factor for the
 11 fraction of the beam flux missed the target (see the last paragraph of Lumi.pdf document for
 12 Argon beam – Run7: “... Based on this assumption our evaluation of the difference in events
 13 population with Y coordinate above Y_C and below accounts 27%. The X - Y distribution of the
 14 primary vertices do not exceed the 3σ limits around the target. The systematic uncertainty for
 15 this measurement do not exceed 2%.), i.e. $\text{Corr} = 1 - 0.27/2 = 0.865 \pm 0.02$.

16 This value is valid for ToF-400 and ToF-700 data. Transformation coefficients from the beam
 17 flux to the luminosity coeff = $N_A \cdot \rho \cdot l / A$ are given in Table 1a for different targets. They are
 18 valid for ToF-400 and ToF-700 data.

19 Table 1a. Number of triggered events, transformation coefficients, beam fluxes and integrated
 20 luminosities collected in interactions of the argon beam with different targets (ToF-400 data
 21 sample).

Interactions, target thickness	coeff	Integrated beam flux / 10^7	Integrated luminosity / 10^{30} cm^{-2}
$Ar+C$ (2 mm)	0.2256	9.1	2.06
$Ar+Al$ (3.33 mm)	0.2006	11.5	2.30
$Ar+Cu$ (1.67 mm)	0.1411	12.7	1.79
$Ar+Sn$ (2.57 mm)	0.0954	11.6	1.11
$Ar+Pb$ (2.5 mm)	0.0824	6.1	0.50

22 Table 1b. Number of triggered events, beam fluxes and integrated luminosities collected in
 23 interactions of the argon beam with different targets (ToF-700 data sample).

Interactions, target thickness	Integrated beam flux / 10^7	Integrated luminosity / 10^{30} cm^{-2}
<i>Ar+C</i> (2 mm)	8.7	1.97
<i>Ar+Al</i> (3.33 mm)	10.2	2.05
<i>Ar+Cu</i> (1.67 mm)	11.3	1.60
<i>Ar+Sn</i> (2.57 mm)	9.5	0.91
<i>Ar+Pb</i> (2.5 mm)	4.9	0.40

24 Estimation of the trigger efficiency

25 For online selection of events with interactions signals from the BD and SiMD trigger detectors were
 26 used. Therefore, the efficiency of BD and SiMD triggers was calculated. BD efficiency was calculated in
 27 the runs when SiMD was included in the online trigger and BD was not enabled. Conversely, the
 28 efficiency of SiMD was calculated in the runs when BD was included in the online trigger and SiMD was
 29 not enabled. In various runs, the conditions for the minimum the number of signals in BD and SiMD
 30 changed from 2 to 4. The minimum number of signals in BD and SiMD was set by hardware. The trigger
 31 condition for which the efficiency was considered, was applied offline in program, so how the number of
 32 signals in BD and SiMD was recorded for each event in experimental data. For example, $e_{\text{tr}}(\text{BD} \geq 2)$ was
 33 estimated as

$$34 \quad e_{\text{tr}}(\text{BD} \geq 2) = N(\text{BD} \geq 2 \&\& \text{SiMD} \geq 3) / N(\text{SiMD} \geq 3), \quad (1)$$

35 where $N(\text{SiMD} \geq 3)$ is the number of events collected with the hardware-set condition $\text{SiMD} \geq 3$,
 36 $N(\text{BD} \geq 2 \&\& \text{SiMD} \geq 3)$ - the number of events collected with the hardware-set condition $\text{SiMD} \geq 3$, in
 37 which the number of registered signals $\text{BD} \geq 2$. The BD and FD detectors cover different parts of the
 38 acceptance of the BM@N setup, that is, they detect different (independent) reaction products. To
 39 evaluate the possible distortion of $e_{\text{tr}}(\text{BD} \geq 2)$ due to the selection of events with the initial condition
 40 $N(\text{SiMD} \geq 3)$, $e_{\text{tr}}(\text{BD} \geq 2)$ was evaluated in events without conditions $N(\text{SiMD} \geq 3)$, which in a limited
 41 number were registered with a beam trigger BT. The difference between the result and the result
 42 according to formula (1) was treated as the systematic uncertainty of the trigger efficiency. A similar
 43 procedure was applied to determine $e_{\text{tr}}(\text{BD} \geq 4)$, $e_{\text{tr}}(\text{FD} \geq 3)$, $e_{\text{tr}}(\text{FD} \geq 4)$, which were used in the
 44 analysis. To determine the efficiency of $e_{\text{tr}}(\text{BD} \geq 2, \text{FD} \geq 3)$, the value was used

$$45 \quad e_{\text{tr}}(\text{BD} \geq 2, \text{FD} \geq 3) = e_{\text{tr}}(\text{BD} \geq 2) * e_{\text{tr}}(\text{FD} \geq 3) \quad (2)$$

46 To evaluate the possible correlation effect of triggers $\text{BD} \geq 2$ and $\text{FD} \geq 3$, efficiency $e_{\text{tr}}(\text{BD} \geq 2, \text{FD} \geq 3)$
 47 was determined directly on a limited statistics in events registered with BT beam trigger. The difference
 48 between the result and the result according to formula (2) was treated as the systematic uncertainty of
 49 trigger efficiency. The trigger efficiency e_{tr} was evaluated as a function of the number of tracks in the
 50 primary vertex (n_{TrPV}) and the coordinates of the primary vertex in the event, X (X_{pv}) and Y (Y_{pv}). The
 51 trigger efficiency was applied to data when filling histograms of raw spectra π^+ (K^+) in rapidity and
 52 transverse momentum. For each π^+ (K^+), identified in an event with a primary vertex characterized by
 53 n_{TrPV} , X_{pv} , Y_{pv} , value added to histogram with weight $1/e_{\text{tr}}(n_{\text{TrPV}}, X_{\text{pv}}, Y_{\text{pv}})$.

54