

Anisotropic collective flow and development of the corresponding measurement techniques for the MPD experiment

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With big help from Andrey Moshkin (VBLHEP JINR) and Dmitry Podgainy (LIT, JINR)

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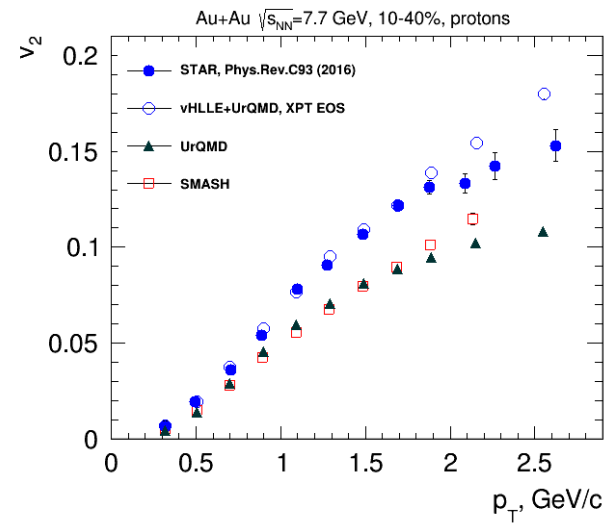
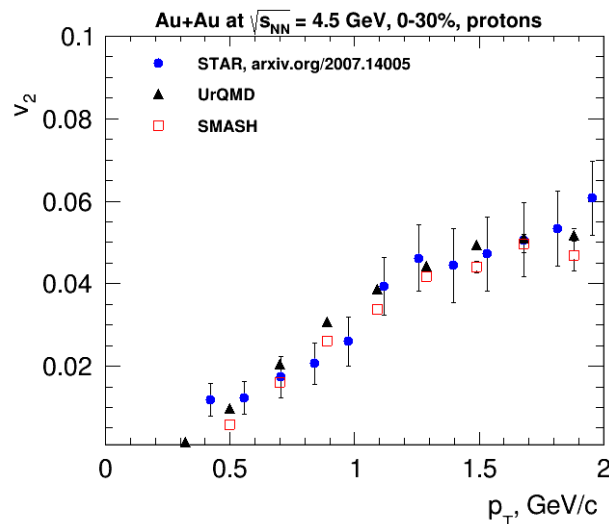
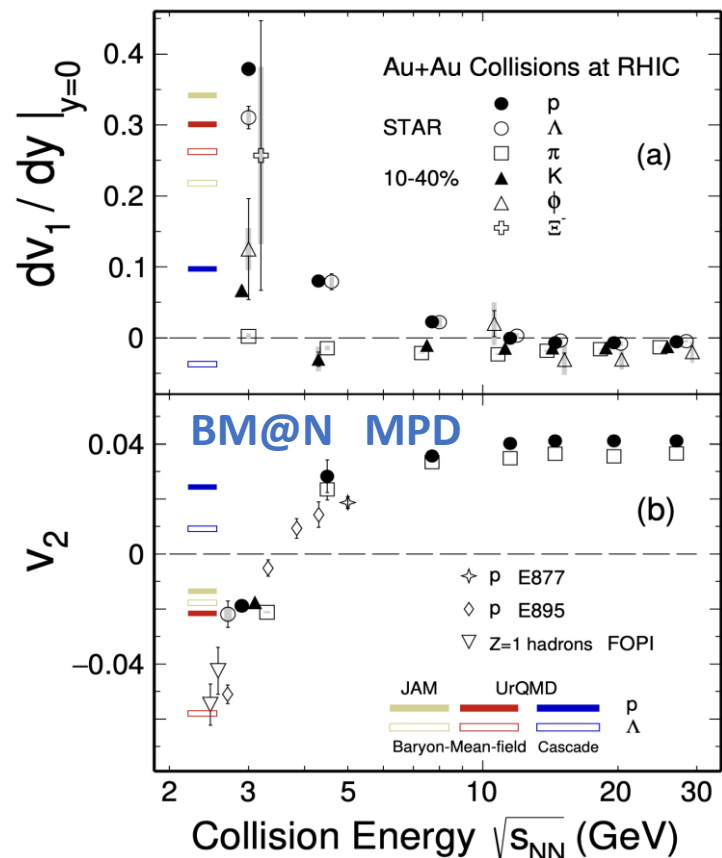
For the MPD Collaboration

10th MPD Collaboration Meeting, JINR , Dubna, 8-10 November 2022

This work is supported by: the NRNU program Priority 2030 and Special Purpose Funding Programme within the NICA Megascience Project in 2022

Anisotropic flow at NICA energies

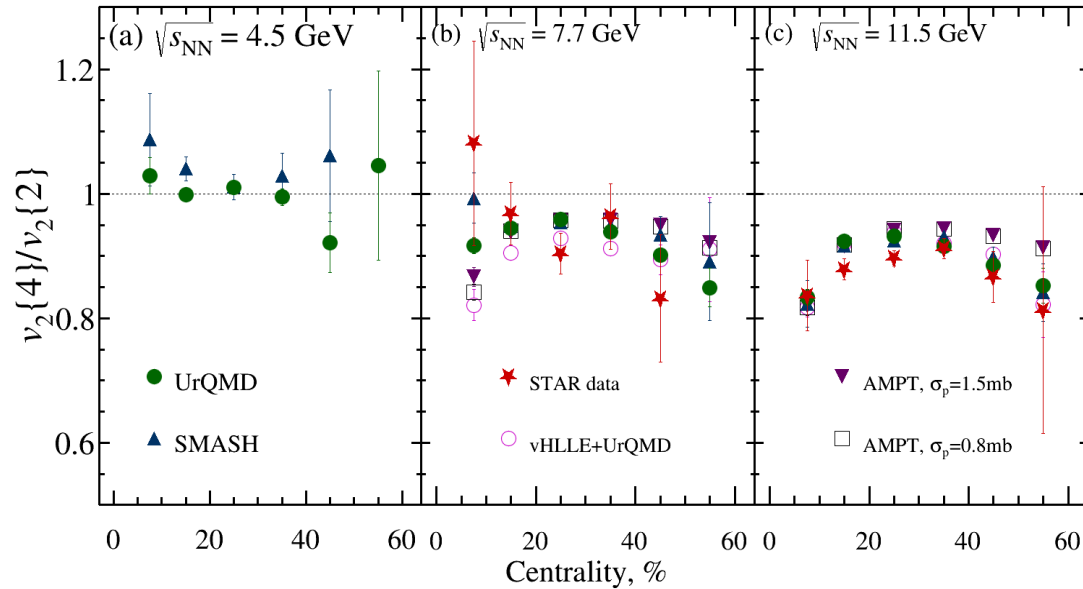
STAR Collaboration, Phys.Lett.B 827 (2022) 137003



- **Strong energy dependence of v_1 and v_2 at $\sqrt{s_{NN}} = 3-11$ GeV**
 - ▶ $v_2 \approx 0$ at $\sqrt{s_{NN}} = 3.3$ GeV and negative below
- **Lack of differential measurements of v_2 at NICA energies (p_T , centrality, PID,...)**
- **v_2 is sensitive to the properties of strongly interacting matter:**
 - ▶ at $\sqrt{s_{NN}} = 4.5$ GeV pure string/hadronic cascade models (UrQMD, SMASH,...) give similar v_2 signal compared to STAR data
 - ▶ at $\sqrt{s_{NN}} \geq 7.7$ GeV pure string/hadronic cascade models underestimate v_2 – need hybrid models with QGP phase (vHLE+UrQMD, AMPT with string melting,...)
- **Make predictions for the anisotropic flow measurements $v_n(p_T, y)$ at BM@N ($\sqrt{s_{NN}}=2.3-3.3$ GeV) and MPD ($\sqrt{s_{NN}}=4-11$ GeV) energies**

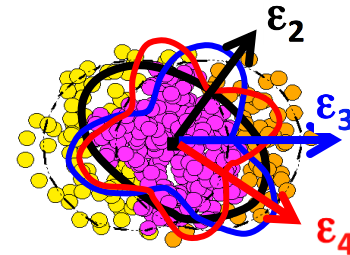
Relative flow fluctuations of charged hadrons

Au+Au, Charged hadrons, $0.2 < p_T < 3.0$ GeV/c



STAR data: Phys.Rev.C **86**, 054908 (2012)

- Relative v_2 fluctuations ($v_2\{4\}/v_2\{2\}$) observed by STAR experiment can be reproduced both in the string/cascade models (UrQMD, SMASH) and model with QGP phase (AMPT SM, vHLL+UrQMD)
- Dominant source of v_2 fluctuations: **participant eccentricity fluctuations** in the initial geometry
- Are there non-zero v_2 fluctuations at $\sqrt{s_{NN}} = 4.5$ GeV?

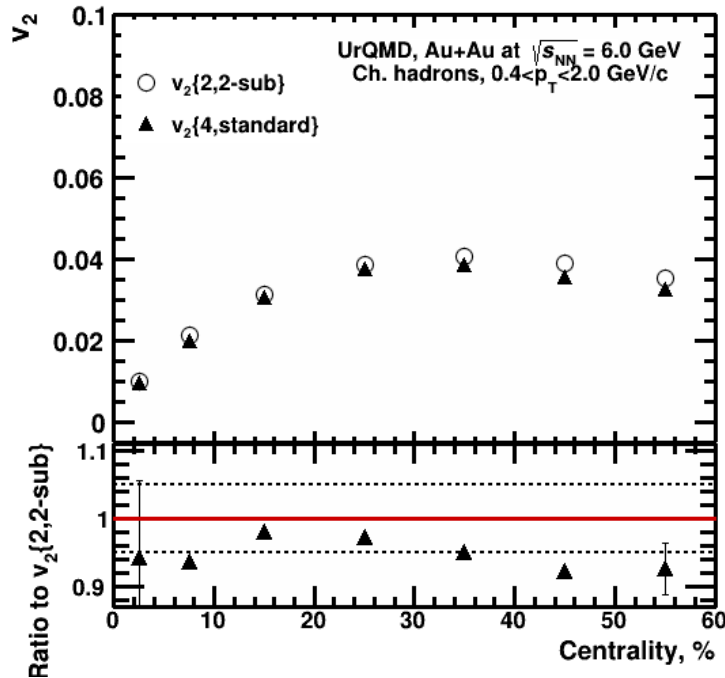
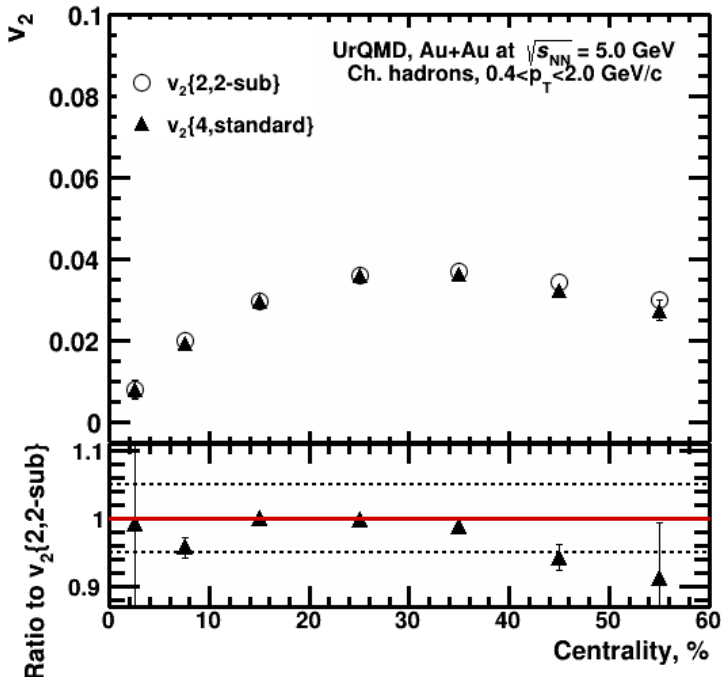


Relative v_2 fluctuations of charged hadrons

UrQMD v3.4, cascade mode

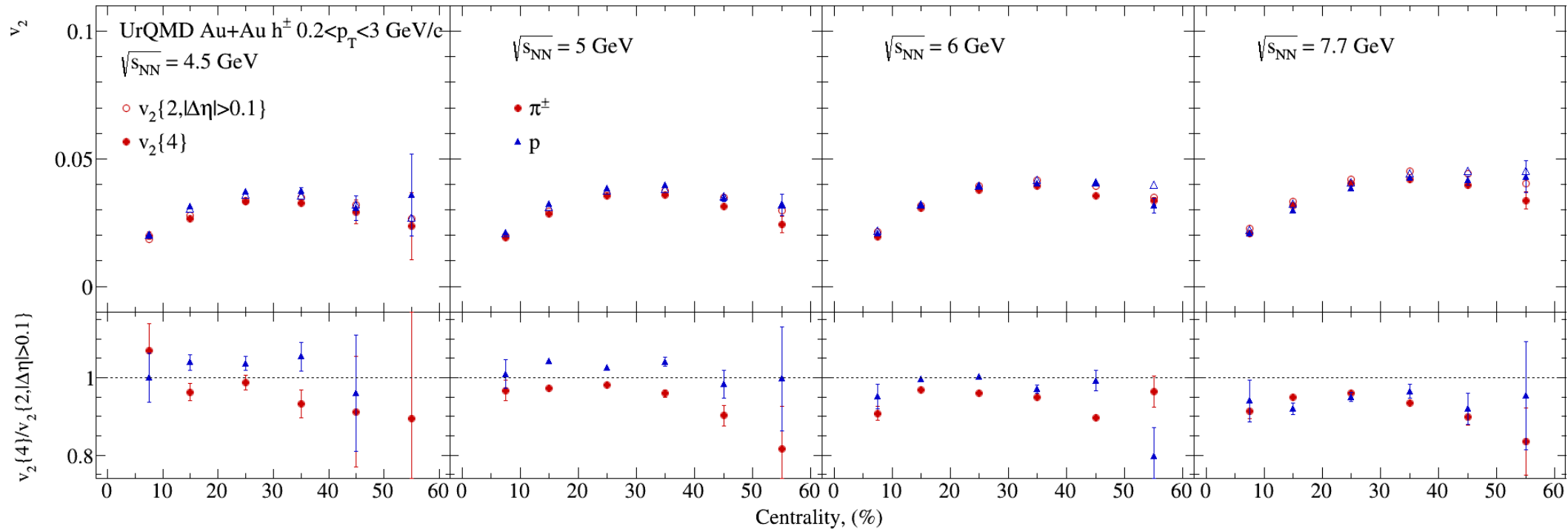
- $\sqrt{s_{NN}}=5$ GeV: 230M
- $\sqrt{s_{NN}}=6$ GeV: 270M

$|\eta| < 1.5$, η -gap: $|\Delta\eta| > 0.1$



- $v_2\{4\} \approx v_2\{2\}$ in mid-central collisions at $\sqrt{s_{NN}}=5$ GeV
- $v_2\{4\}/v_2\{2\}$ shows 2-4% difference in mid-central collisions at $\sqrt{s_{NN}}=6$ GeV

Relative v_2 fluctuations of pions and protons



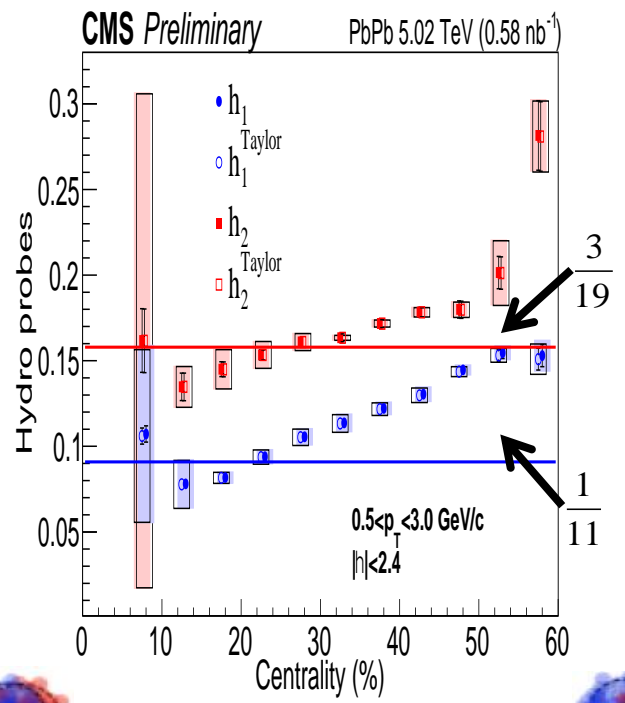
- $v_2\{4\} / v_2\{2\}$ differs for pions and protons at $\sqrt{s_{NN}} < 6$ GeV
- $v_2\{4\} / v_2\{2\} < 1$ at $\sqrt{s_{NN}} > 5$ GeV for pions and at $\sqrt{s_{NN}} > 6$ GeV for protons

High-Order Cumulants: Hydro probes & central moments

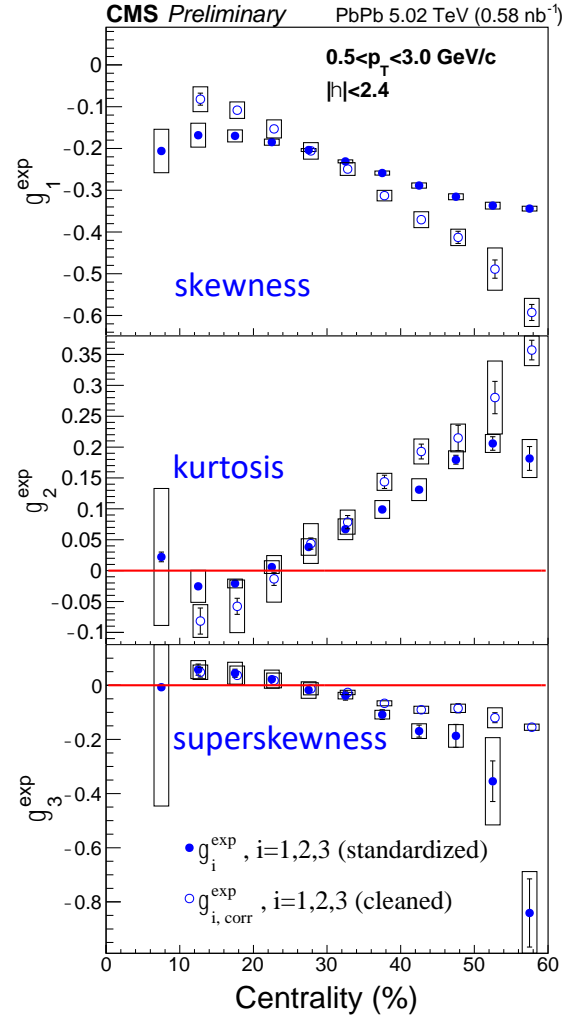
$$h_1 = \frac{v_2\{6\} - v_2\{8\}}{v_2\{4\} - v_2\{6\}} \gg h_1^{Taylor} = \frac{1}{11} - \frac{1}{11} \frac{v_2^2\{4\} - 12v_2^2\{6\} + 11v_2^2\{8\}}{v_2\{4\}^2 - v_2\{6\}^2}$$

$$h_2 = \frac{v_2\{8\} - v_2\{10\}}{v_2\{6\} - v_2\{8\}} \gg h_2^{Taylor} = \frac{3}{19} - \frac{1}{19} \frac{3v_2^2\{6\} - 22v_2^2\{8\} + 19v_2^2\{10\}}{v_2\{6\}^2 - v_2\{8\}^2}$$

$$\gamma_1^{exp} = -2^{3/2} \frac{v_2\{4\}^3 - v_2\{6\}^3}{[v_2\{2\}^2 - v_2\{4\}^2]^{3/2}} \approx -2^{3/2} \frac{-s_{30} - O_N}{[2\sigma_x^2 + O_D]^{3/2}} \approx \frac{s_{30}}{\sigma_x^3} \equiv \gamma_1$$



Higher-order moments necessary to describe data

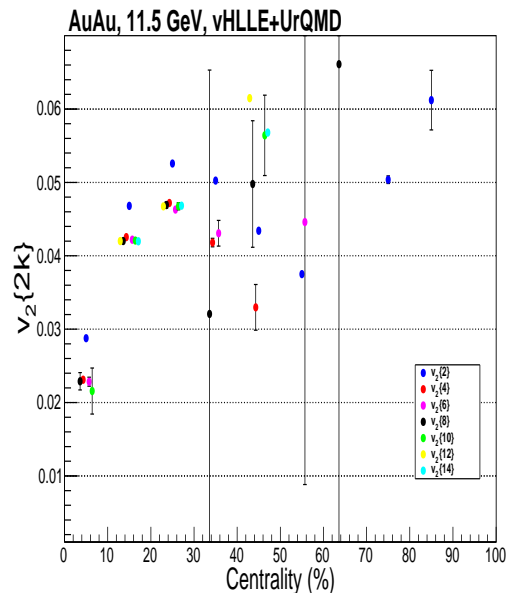
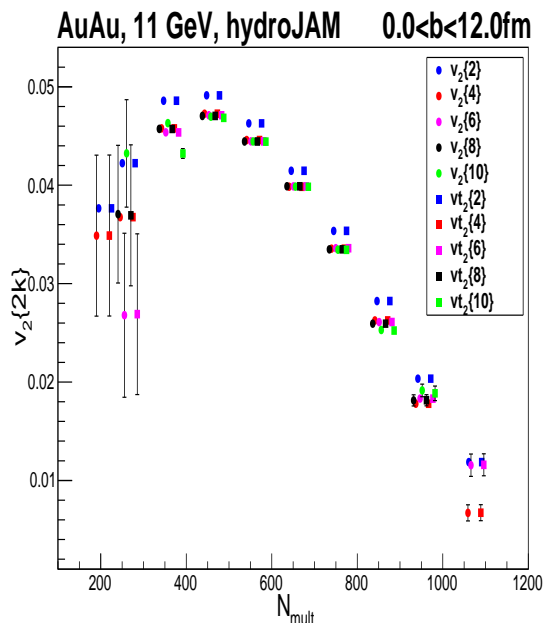


NICA energy case

✧ AuAu collisions at $\sqrt{s_{NN}} = 11.0$ GeV

- In 10 multiplicity/centrality classes

- $0.0 < b < 12.0$ fm
- JAM stat.: 1.068 B events
- vHLE stat. 34 M events



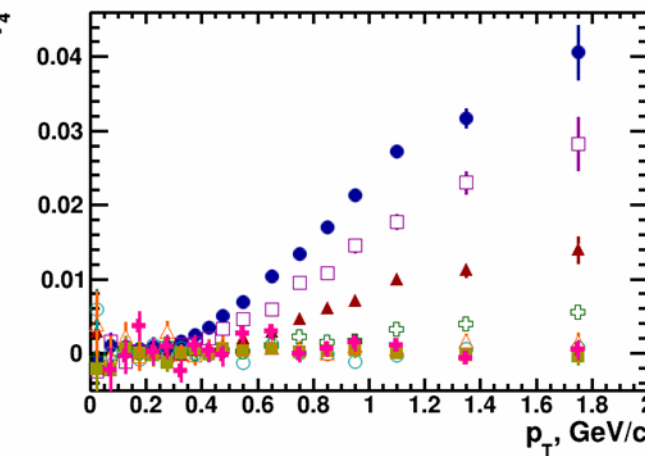
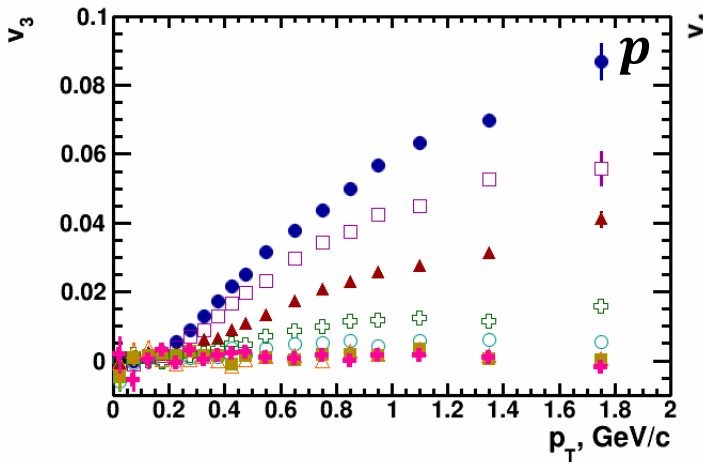
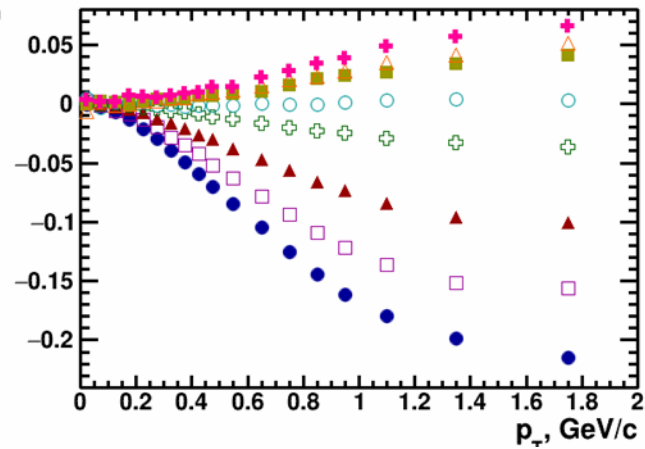
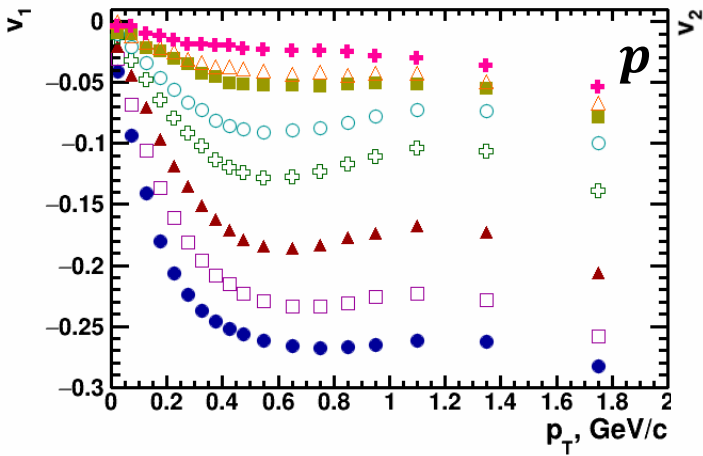
Necessary condition $v_2\{4\} > v_2\{6\} > v_2\{8\} > v_2\{10\}$ to perform hydro probes and to measure central moments

It seems JAM does not have splitting

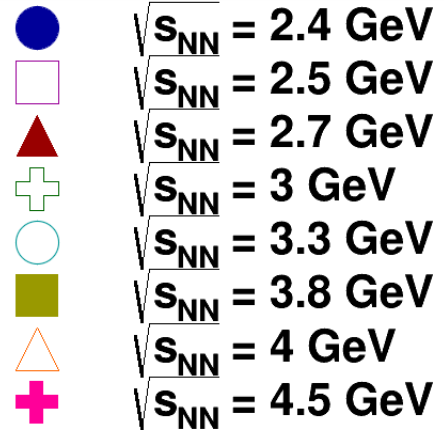
vHLE should have splitting, but current statistics is too small

Statistics of the real MPD should be about 1B (10^9) events per year that enables performing hydro probes and central moments measurements

$v_{1,2,3,4}(p_T)$ Au+Au $\sqrt{s_{NN}}=2.4-4.5$ GeV: BM@N+MPD



JAM MD3, Au+Au, 20-30%



Protons:

$V_{1,3}: -0.5 < y < -0.15$

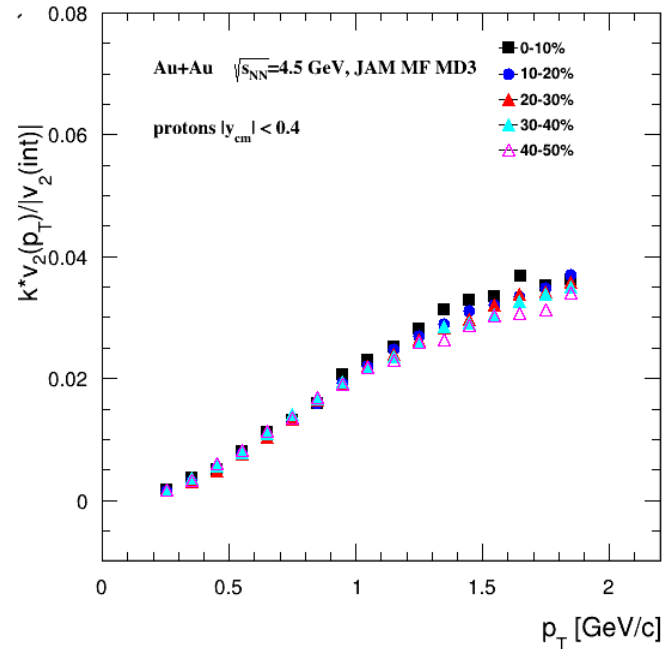
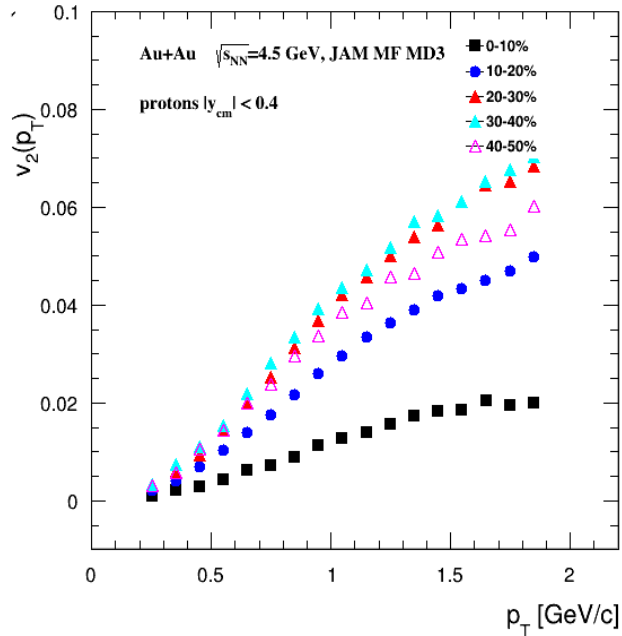
$V_{1,3}: 1.0 < p_T < 1.5$ GeV/c

$|v_{1,3}\{\Psi_1\}|$ decreases with increasing collision energy

$v_3 \approx 0$ at $\sqrt{s_{NN}} \geq 4$ GeV

Scaling with integral flow of charged hadrons. Will it work at $\sqrt{s_{NN}}=4.5$ GeV? (JAM mean field MD3)

See Peter Parfenov talk

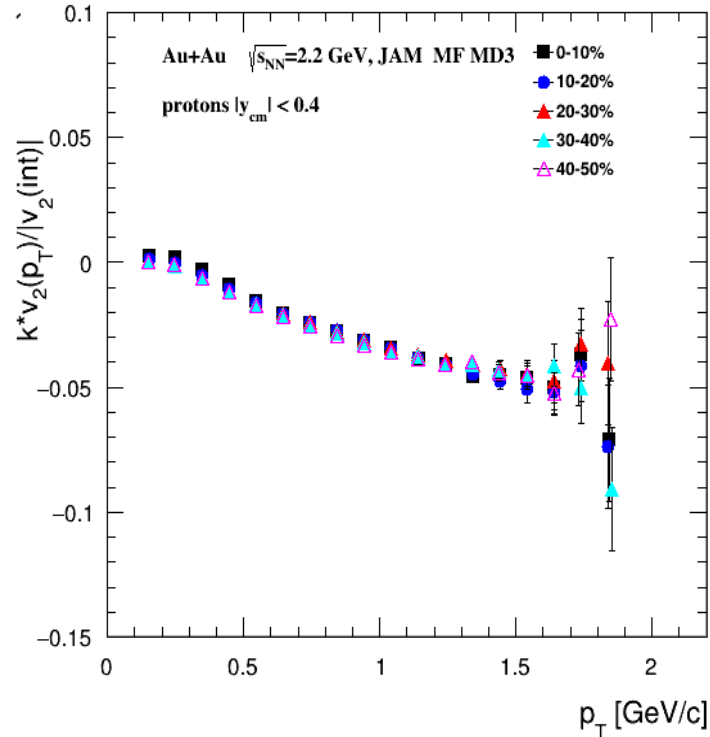
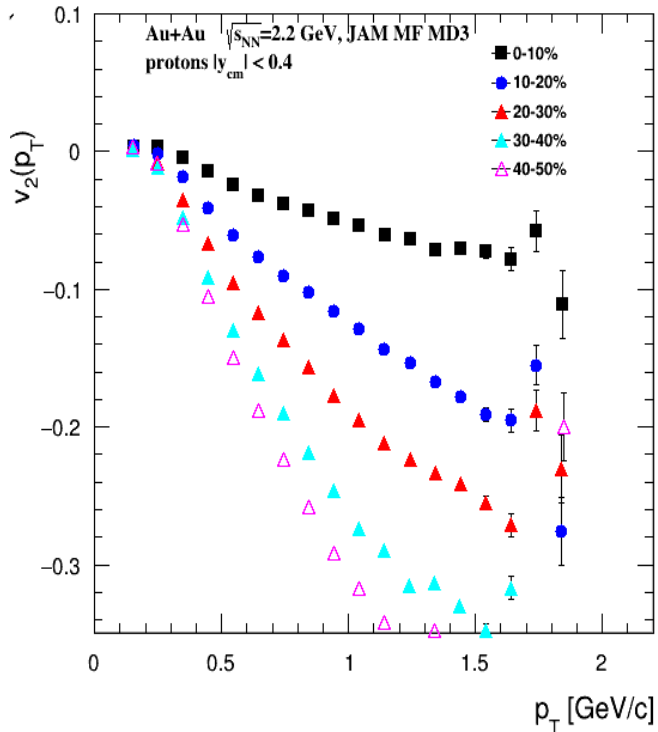


Scaling starts to work again – after the transition from out-of-plane to in-plane

$$9 \quad V_2(PID, p_T, centrality, \sqrt{s_{NN}}) = V_2(h, centrality, \sqrt{s_{NN}}) * V_2(PID, p_T) ???$$

Scaling with integral flow of charged hadrons. Will it work at $\sqrt{s_{NN}}=2.2$ GeV? (JAM mean field MD3)

See Peter Parfenov talk

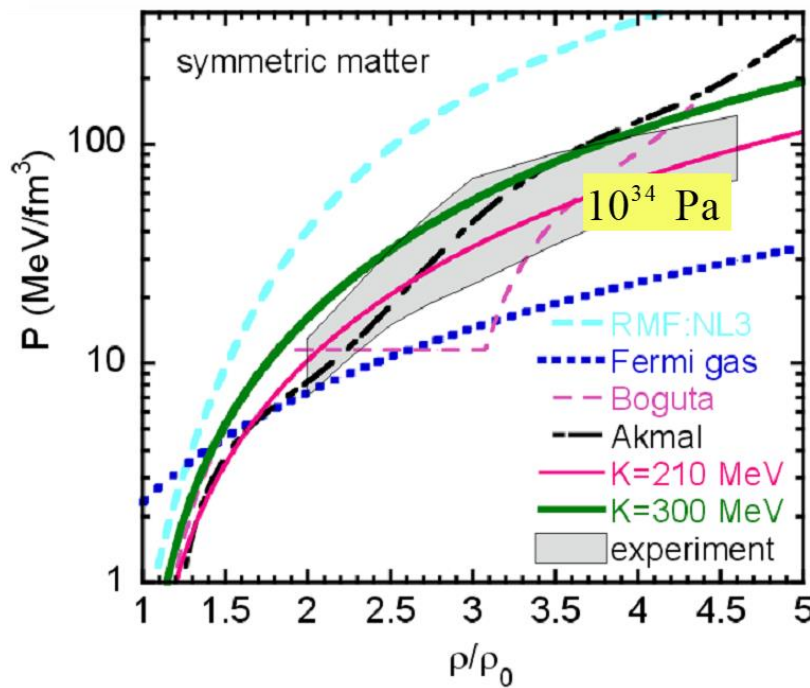
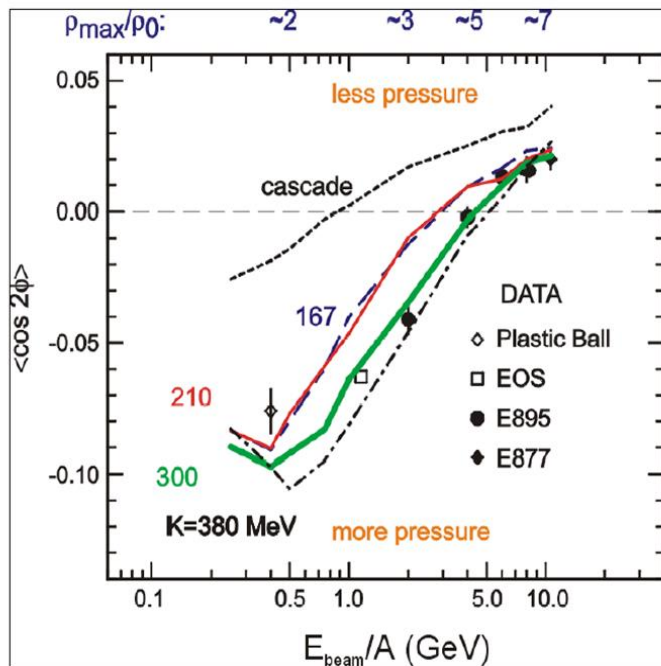


In all plots $k=0.025$ and $v_2(int)$ for $0.4 < p_T < 2.0$ GeV/c

10 $V_2(PID, p_T, centrality, \sqrt{s_{NN}}) = V_2(h, centrality, \sqrt{s_{NN}}) * V_2(PID, p_T) ???$

Flow at AGS: Constraints for the Hadronic EOS

Danielewicz, Lacey, Lynch, Science 298 (2002) 1592-1596



Passage time: $2R/(\beta_{\text{cm}}\gamma_{\text{cm}})$

Expansion time: R/c_s

$c_s = c \sqrt{dp/d\varepsilon}$ - speed of sound

$$c_s = \sqrt{K/9m_N} \approx 0.15c, 0.21c$$

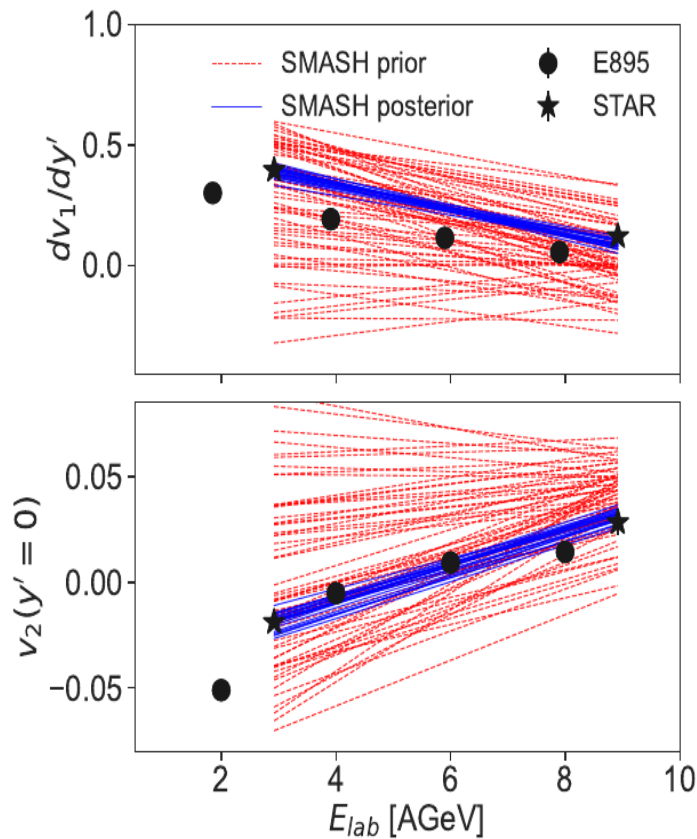
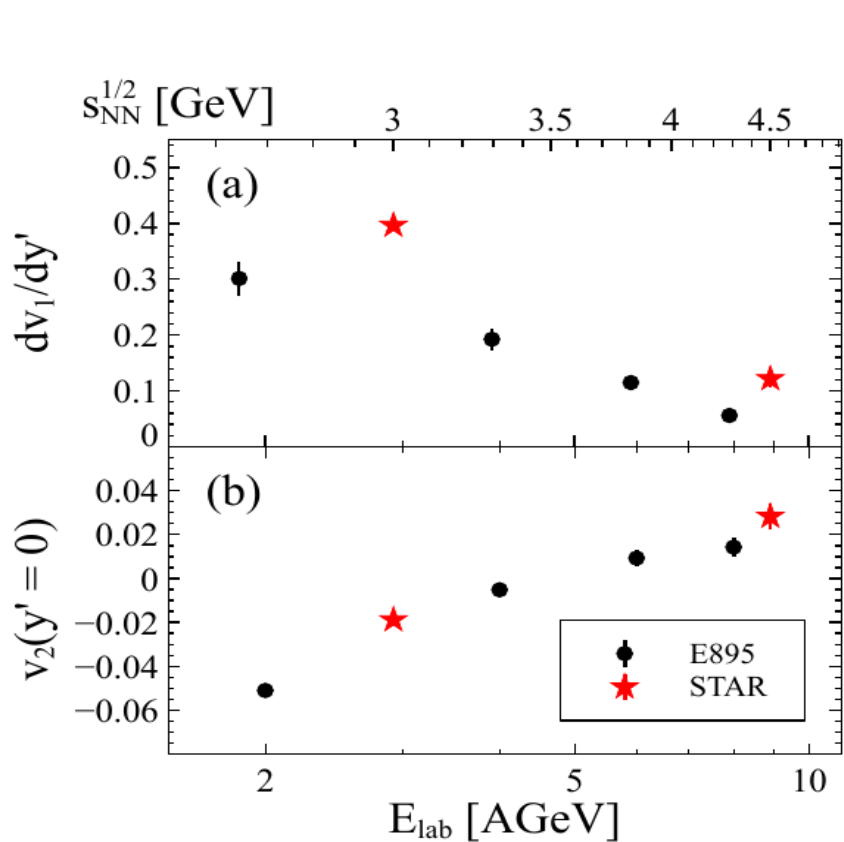
Flow at AGS/Nuclotron = Interplay of passage/expansion times

Sensitivity of Au+Au collisions to the symmetric nuclear matter equation of state at 2–5 nuclear saturation densities

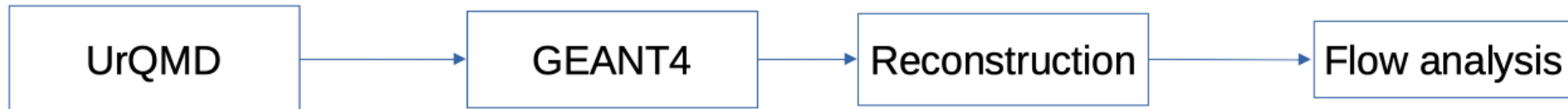
Dmytro Oliinychenko,^{1,*} Agnieszka Sorensen,^{1,†} Volker Koch,² and Larry McLerran¹

¹*Institute for Nuclear Theory, University of Washington, Box 351550, Seattle, Washington 98195, USA*

²*Lawrence Berkeley National Laboratory, 1 Cyclotron Road, Berkeley, California 94720, USA*



MPD Experiment at NICA



- Au+Au: 20M at $\sqrt{s_{NN}} = 7.7$ GeV, 10M at $\sqrt{s_{NN}} = 11.5$ GeV, Bi+Bi: 5M at $\sqrt{s_{NN}} = 9.2, 7.7, 4.5$ GeV, Ag+Ag 5M at $\sqrt{s_{NN}} = 9.2, 4.5$ GeV
- Centrality determination: Bayesian inversion method and MC-Glauber
- Event plane determination: TPC, FHCaI
- Track selection:
 - ▶ Primary tracks
 - ▶ $N_{\text{TPC hits}} \geq 16$
 - ▶ $0.2 < p_T < 3.0$ GeV/c
 - ▶ $|\eta| < 1.5$
 - ▶ PID – ToF + dE/dx

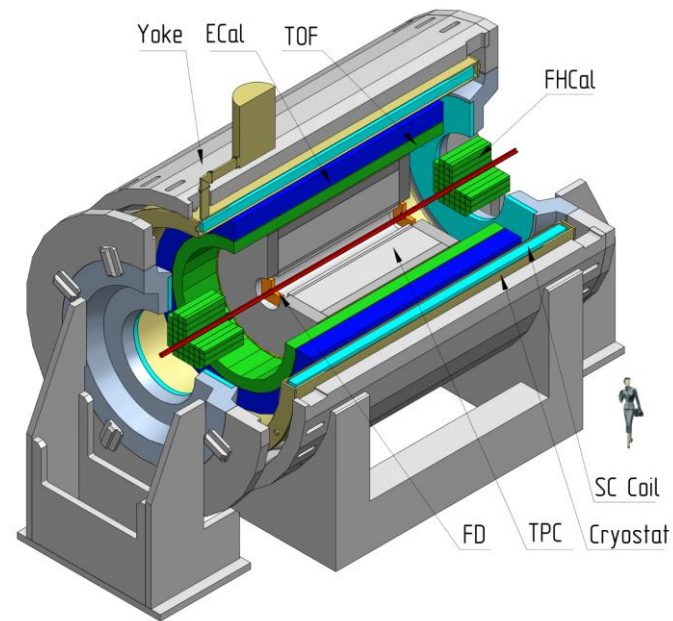
$-5 < \eta < -2$

FHCaI

$-1.5 < \eta < 1.5$
 TPC
 $0.2 < p_T < 3$ GeV/c

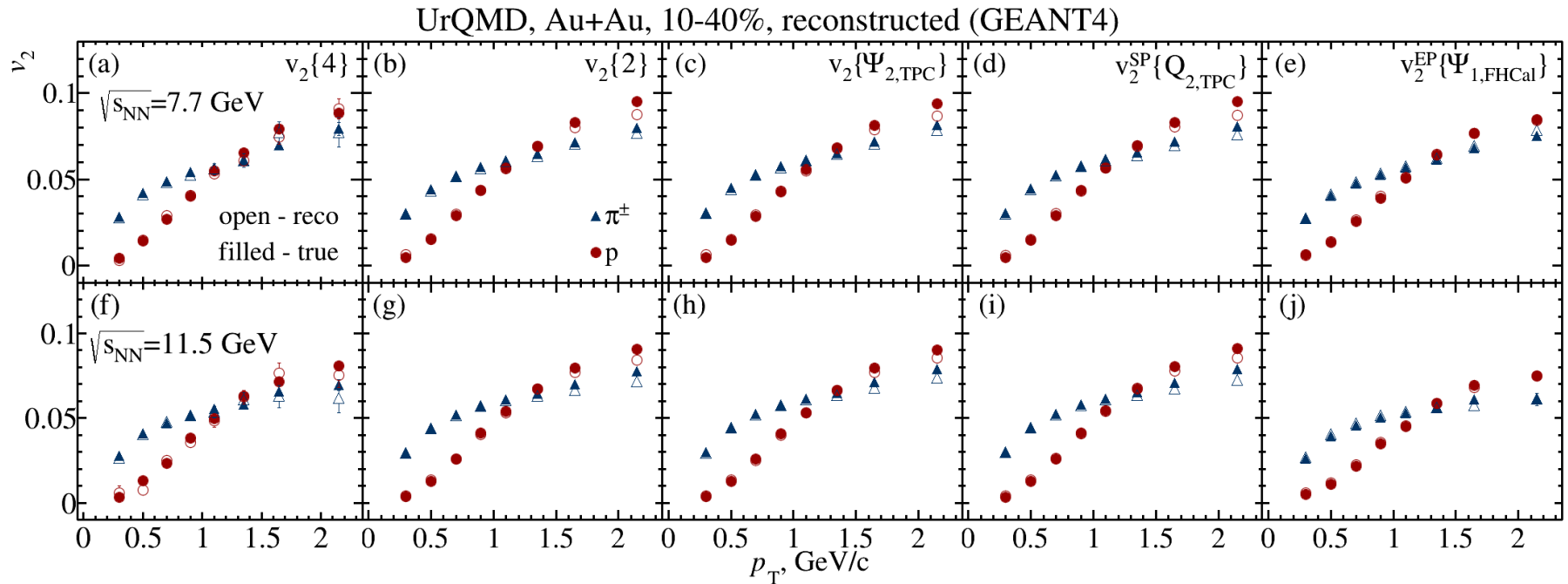
$2 < \eta < 5$

FHCaI



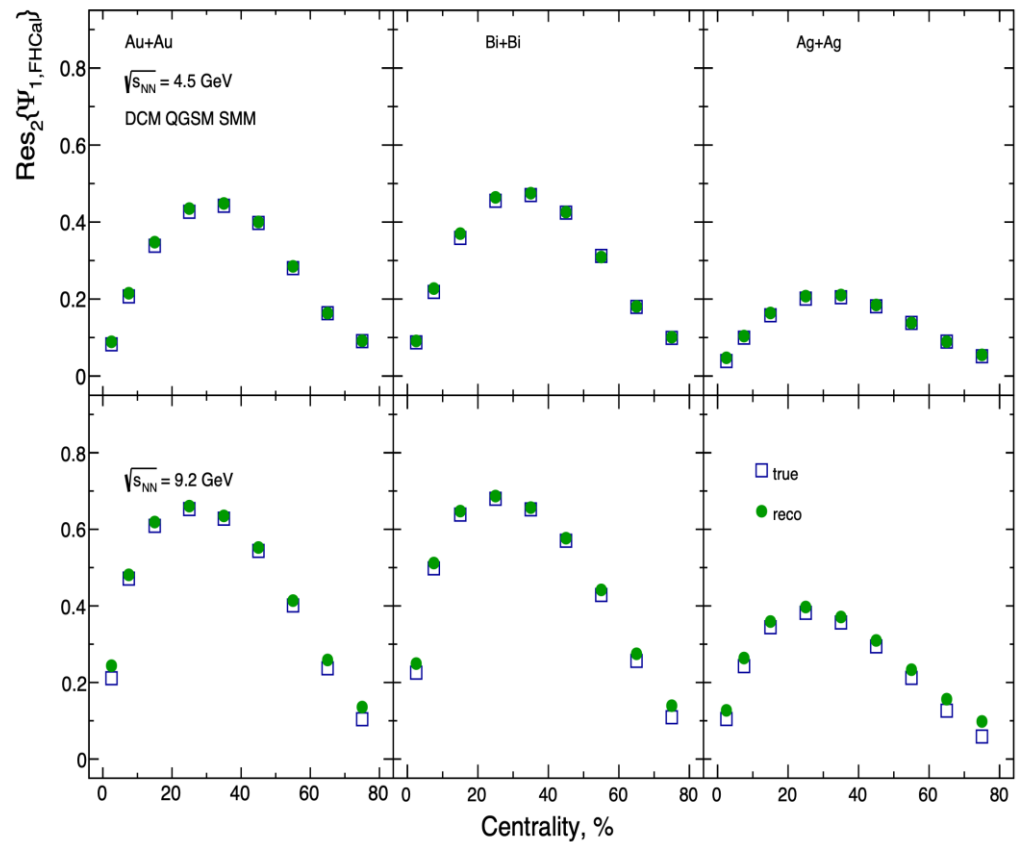
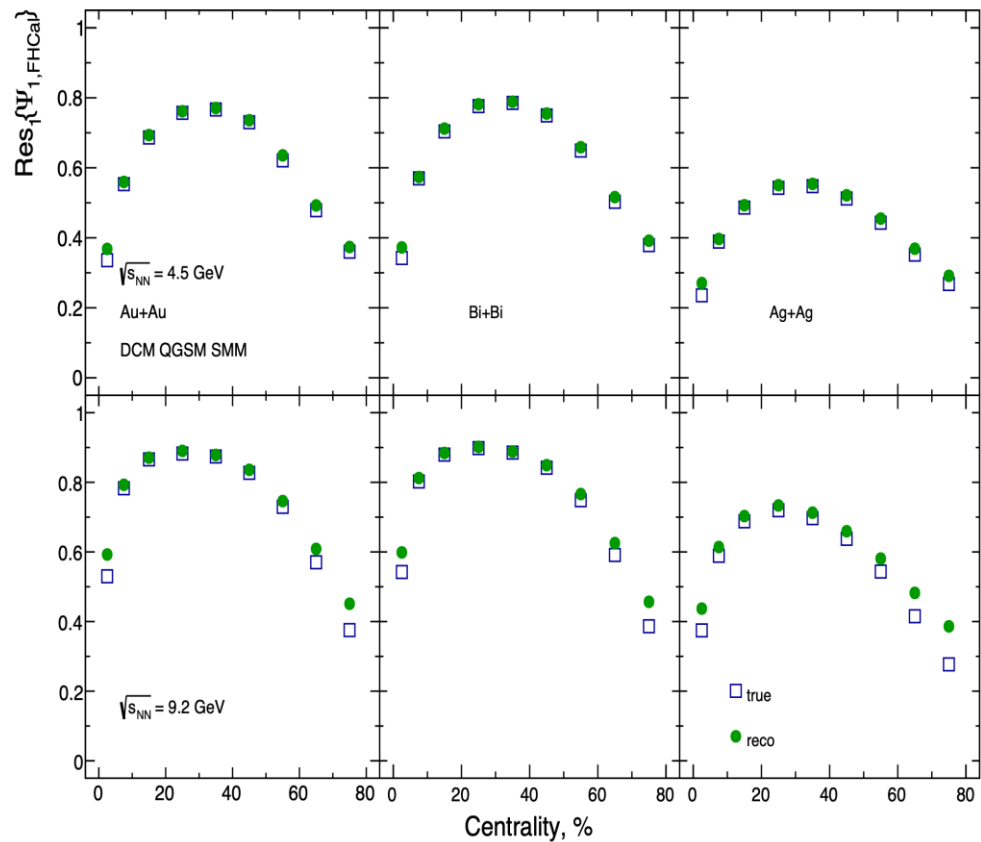
Multi-Purpose Detector (MPD) Stage 1

Performance of v_2 of pions and protons in MPD

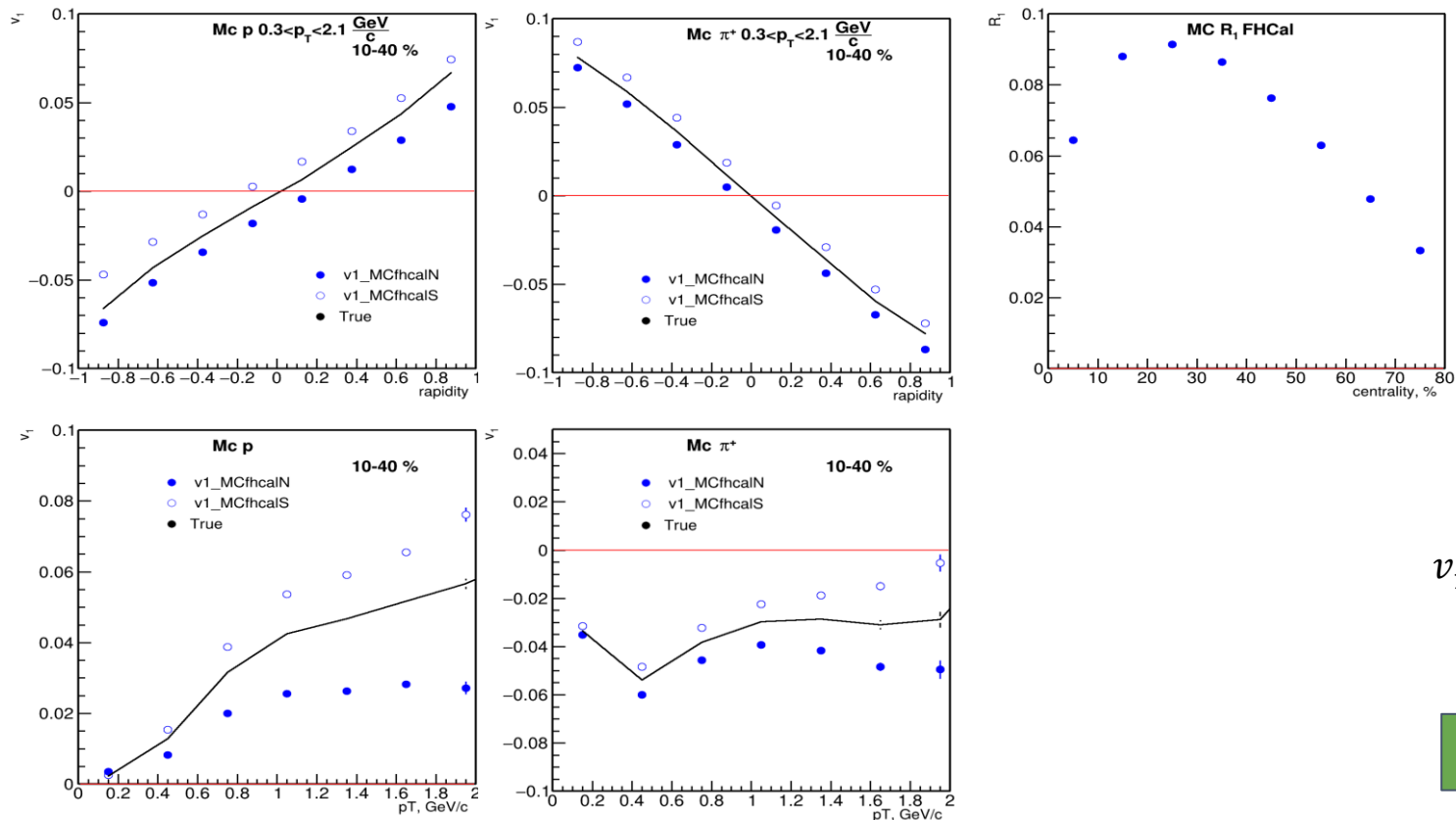


**Reconstructed and generated v_2 of pions and protons
have a good agreement for all methods**

Event Plane Resolution of $\Psi_{1,FHCal}$ for V_1 and V_2 measurements ($Bi + Bi, Au + Au, Ag + Ag$)



Difference between directed flow w.r.t. FHCaL EP



UrQMD, Bi+Bi, $\sqrt{s_{NN}}=9.2$ GeV
Production request 25

R_1 formed by all hadrons in the
FHCaL acceptance $|\eta| \in [2;5]$

$$u_1 = e^{i\phi}, Q_1 = \frac{1}{\sum w_k} \sum w_k u_{1,k}$$

$$v_1^{N,S} = 2 \frac{\langle u_1 Q_1^{N,S*} \rangle}{\sqrt{2 \langle Q_1^S Q_1^{N*} \rangle}} \equiv 2 \frac{\langle u_1 Q_1^{N,S*} \rangle}{R_1}$$

FHCaLS

TPC

FHCaLN

Difference between v_1^N and v_1^S might be due to non-flow (momentum conservation)
Methods based on mixed harmonics must be employed to suppress this effect

The QnAnalysis package

Motivation:

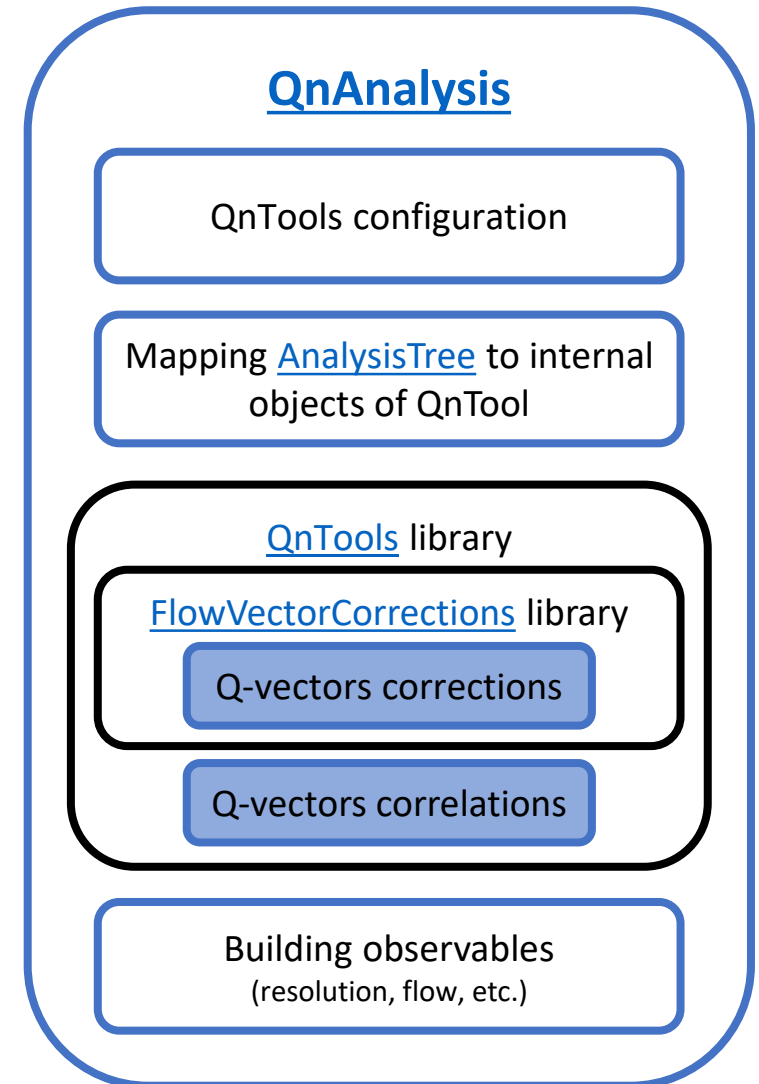
- Decoupling configuration from implementation
- Persistency of analysis setup
- Co-existence of different setups (easy systematics study)
- Unification of analysis methods
- Self-descriptiveness of the analysis results

QnAnalysis requirements:

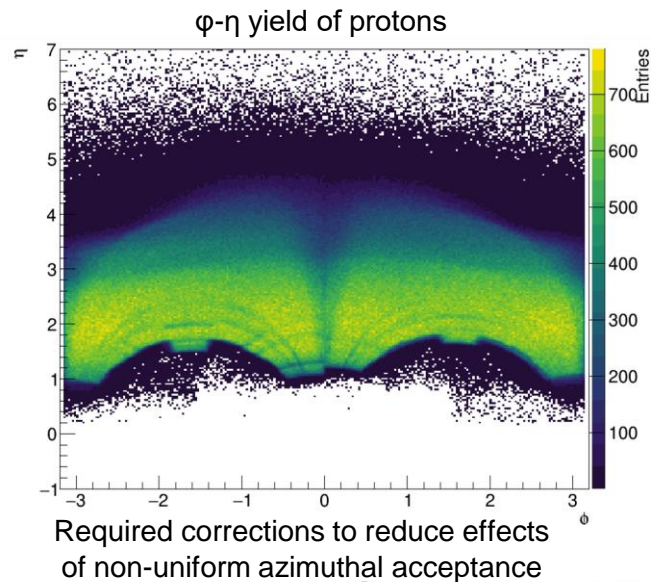
- ROOT ver. ≥ 6.20 (with MathMore library)
- C++17 compatible compiler
- CMake ver. ≥ 3.13

Can be easily installed on NICA cluster using ROOT and CMake modules

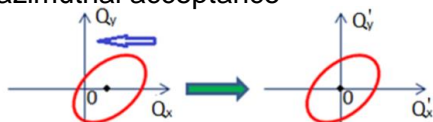
Git repository: <https://github.com/HeavyIonAnalysis/QnAnalysis>



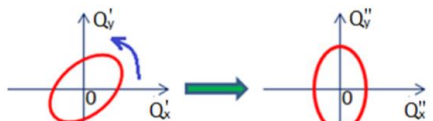
Azimuthal asymmetry of the BM@N acceptance



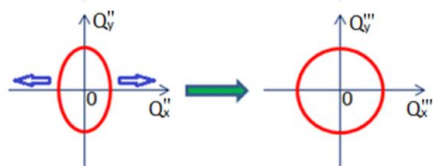
1. Recentering



2. Twist

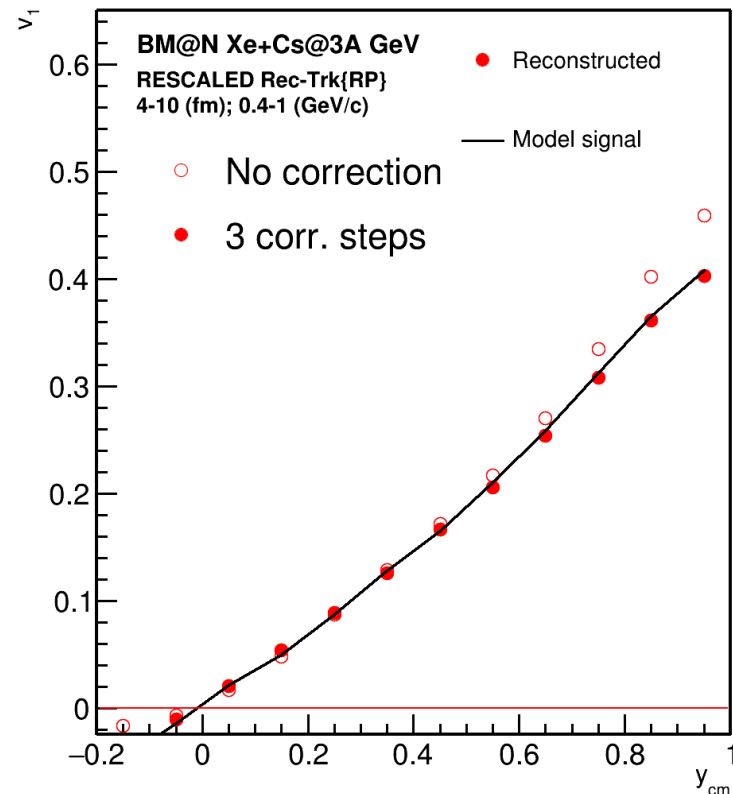


3. Rescaling



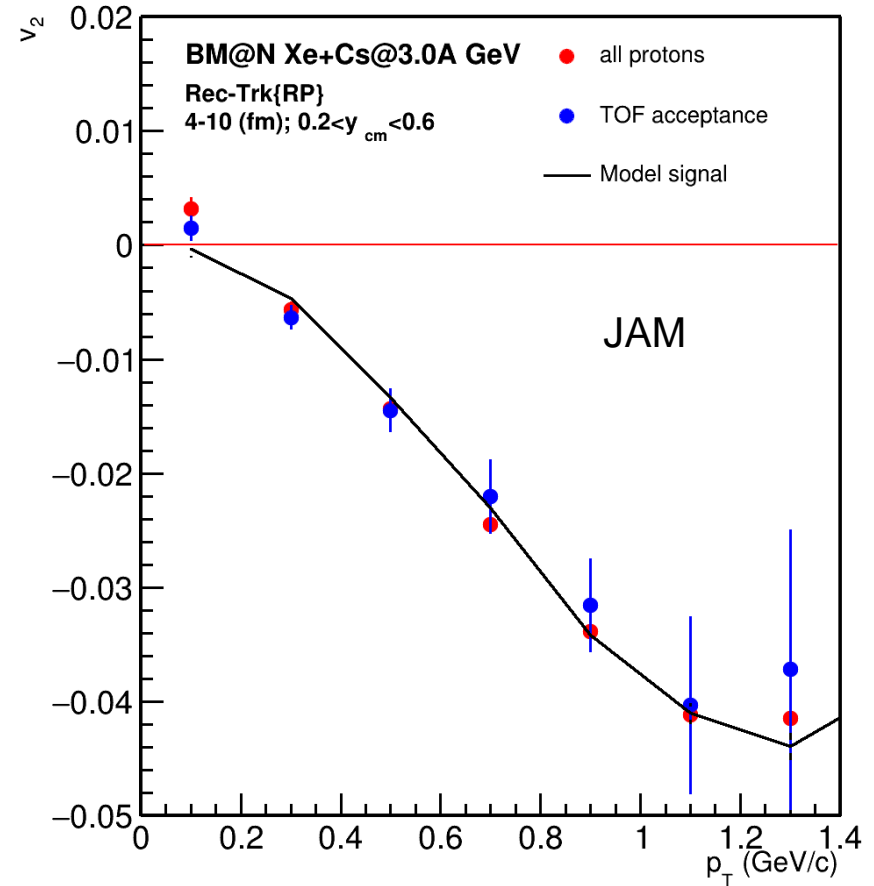
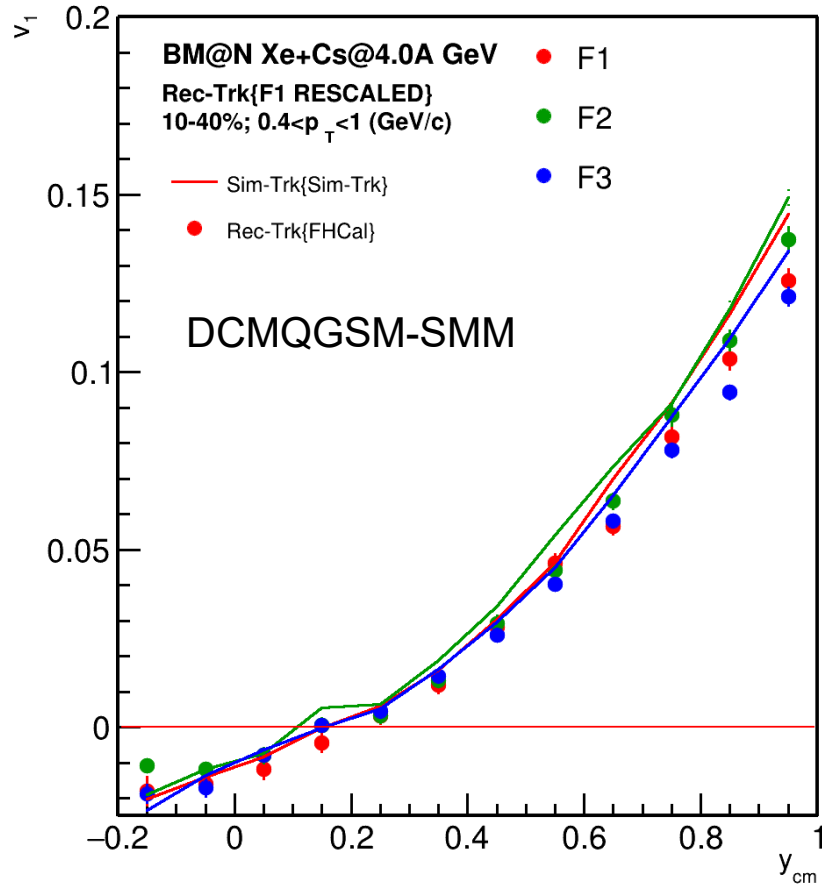
Corrections are based on method in:

I. Selyuzhenkov and S. Voloshin PRC77, 034904 (2008)



Better agreement after rescaling

BM@N performance study for the upcoming run

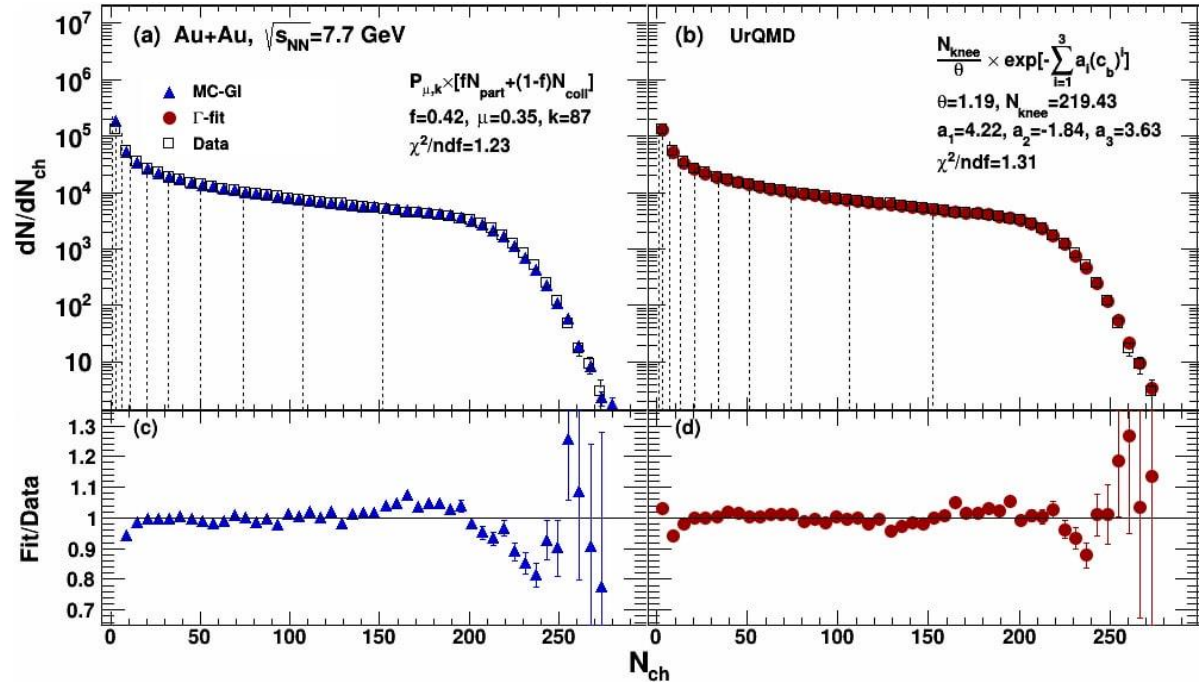


- The performance study was performed using QnAnalysis framework
- QnAnalysis framework will be verified one more time on BM@N data

Centrality determination based on charged particle multiplicity: MC-Glauber and Bayesian inversion method

1). Centrality Determination in Heavy-ion Collisions with MPD Detector at NICA, *Acta Physica Polonica B Proceedings Supplement 14* (2021) 3, 503-506

2) Relating Charged Particle Multiplicity to Impact Parameter in Heavy-Ion Collisions at NICA Energies, *Particles 4* (2021) 2, 275-287



Implementation in MPD:

<https://github.com/FlowNICA/CentralityFramework>

<https://github.com/Dim23/GammaFit>

Summary and outlook

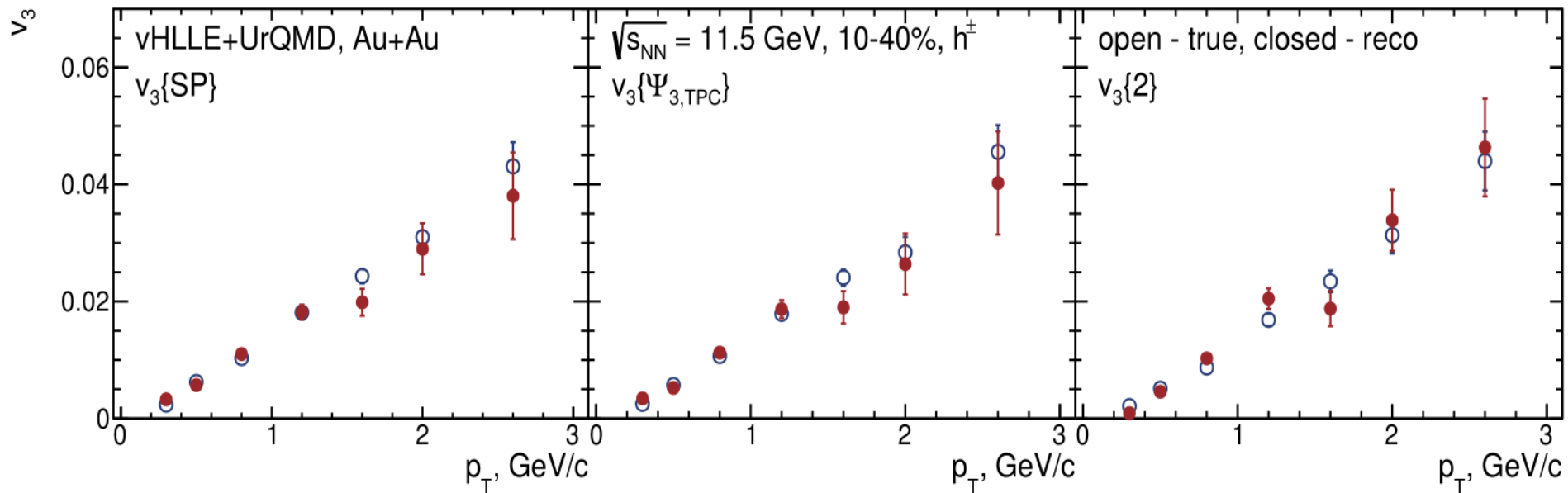
- v_n at NICA energies shows strong energy dependence:
 - At $\sqrt{s_{NN}}=4.5$ GeV v_2 from UrQMD, SMASH are in a good agreement with the experimental data
 - At $\sqrt{s_{NN}}\geq 7.7$ GeV UrQMD, SMASH underestimate v_2 – need hybrid models with QGP phase
 - Detailed JAM model calculations for differential measurements of v_n at $\sqrt{s_{NN}} = 2.4-4.5$ GeV
 - v_2 from cumulants of different orders
- **Comparison of methods for elliptic flow measurements using UrQMD and AMPT models:**
 - The differences between methods are well understood and could be attributed to non-flow and fluctuations
- **Feasibility study for anisotropic flow in MPD:**
 - v_n of identified charged hadrons: results from reconstructed and generated data are in a good agreement for all methods
- Small differences in v_n for 2 colliding systems (Au+Au, Bi+Bi) were observed as expected
- Programs for flow analysis are available for MPD collaboration:
 - Github repository: <https://github.com/FlowNICA/CumulantFlow>
 - QnAnalysis git link: <https://github.com/HeavyIonAnalysis/QnAnalysis>
 - AnalysisTree git link: <https://github.com/HeavyIonAnalysis/AnalysisTree>

Results for 2019-2022

3 Workshops on physics performance studies at FAIR and NICA, <http://indico.oris.mephi.ru/event/221>

28 presentations at conferences and workshops, 22 publications and 3 master diploma works

Triangular flow with MPD at NICA



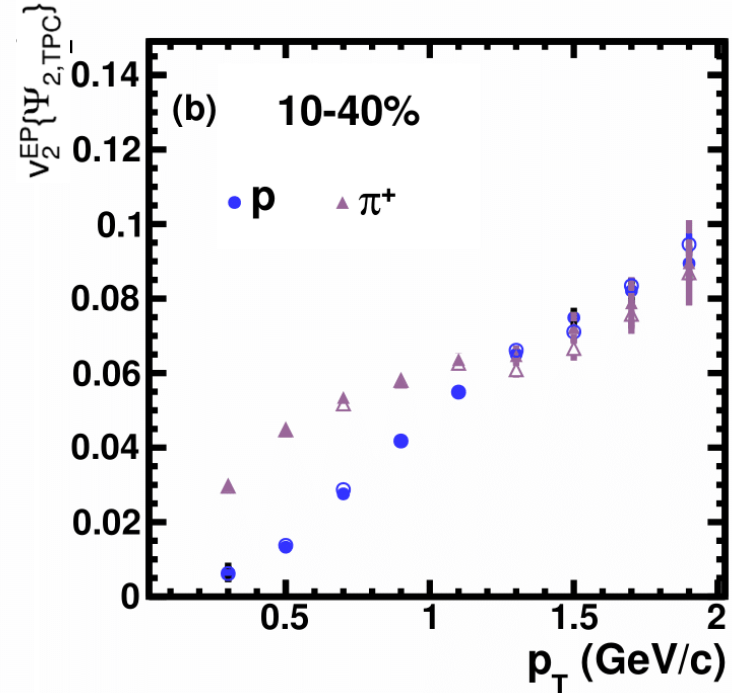
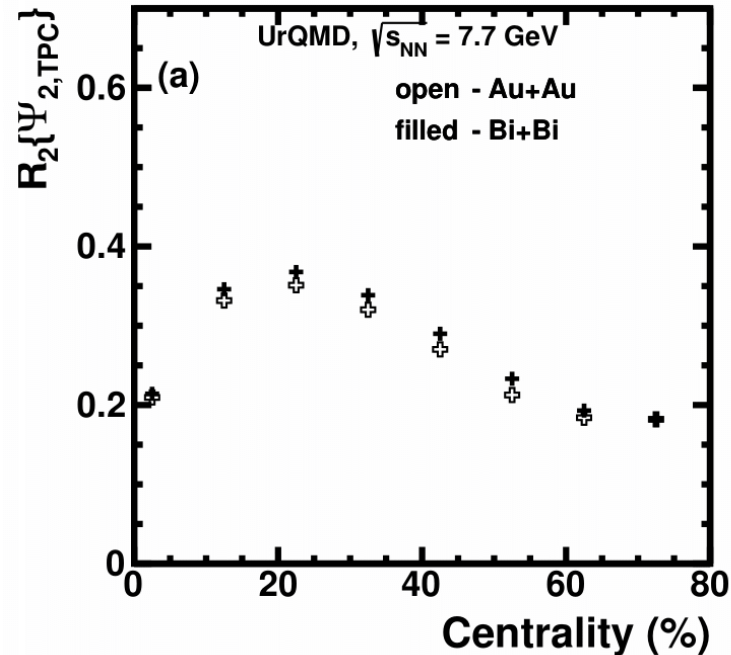
Models show that higher harmonic ripples are more sensitive to the existence of a QGP phase

In models, v_3 goes away when the QGP phase disappears????

15 M of reconstructed vHLL+UrQMD events for Au+Au at 11.5 GeV

Au+Au vs. Bi+Bi collisions for MPD reconstructed data

- TPC event plane



- Expected small difference between two colliding systems

v_n of V0 particles: invariant mass fit method (Nikolay Geraksiev)

Data set:

- 25 million events, UrQMD 3.4 non-hydro, 11.0 GeV, minbias

Geant4 simulation, full reconstruction with:

- TPCv7, TOFv7, FHCAL

Centrality by TPC multiplicity, Event-plane method with FHCAL

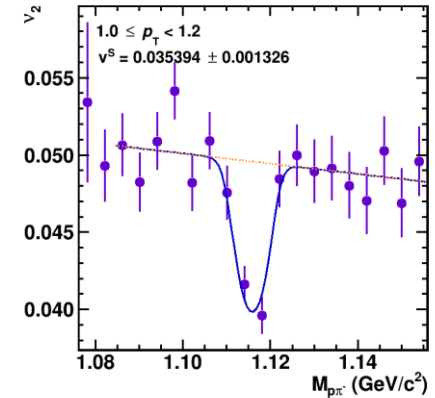
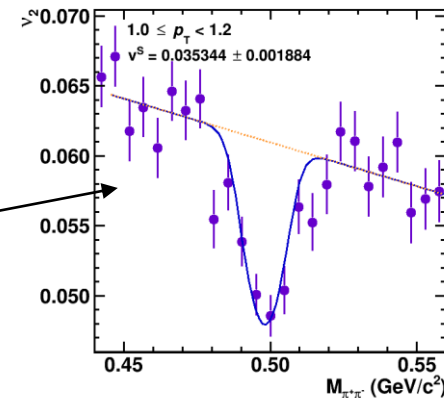
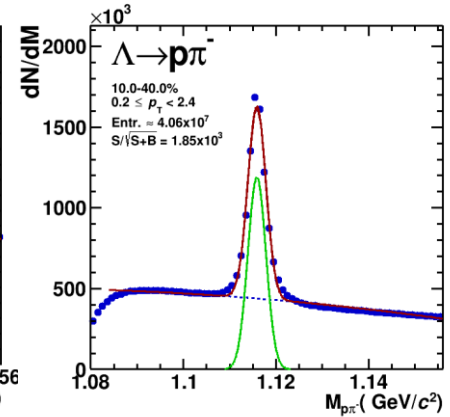
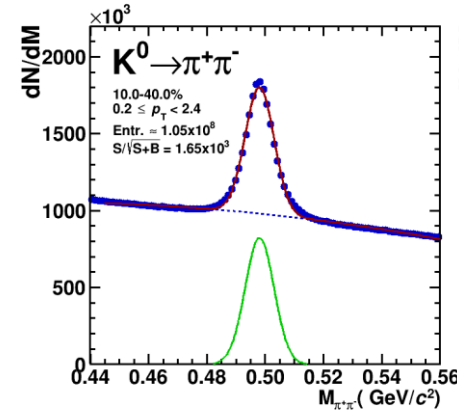
Particle decays reconstructed with MpdParticle realistic cuts

Differential flow signal extraction by bins in transverse momentum (or rapidity) with a simultaneous fit

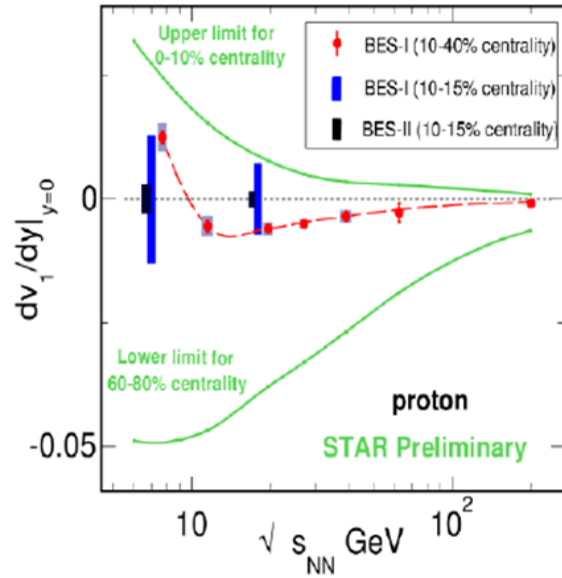
$$v_2^{SB}(m_{inv}, p_T) = v_2^S(p_T) \frac{N^S(m_{inv}, p_T)}{N^{SB}(m_{inv}, p_T)} + v_2^B(m_{inv}, p_T) \frac{N^B(m_{inv}, p_T)}{N^{SB}(m_{inv}, p_T)}$$

Outlook:

- * Larger statistics with vHLE (hydrodynamic evolution)
- * Larger signal magnitude due to hydro (realistic input)
- * Latest versions of detector geometry
- Multi-variate analysis for reconstructed particle selection (TMVA)
- KFParticle

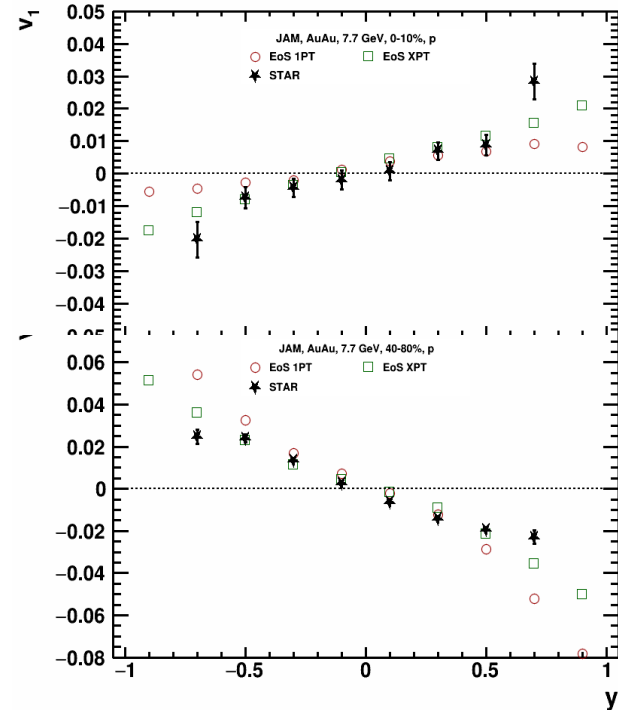


v_1 study at NICA energies



Slope dv_1/dy has non-monotonic behavior and strong centrality dependence

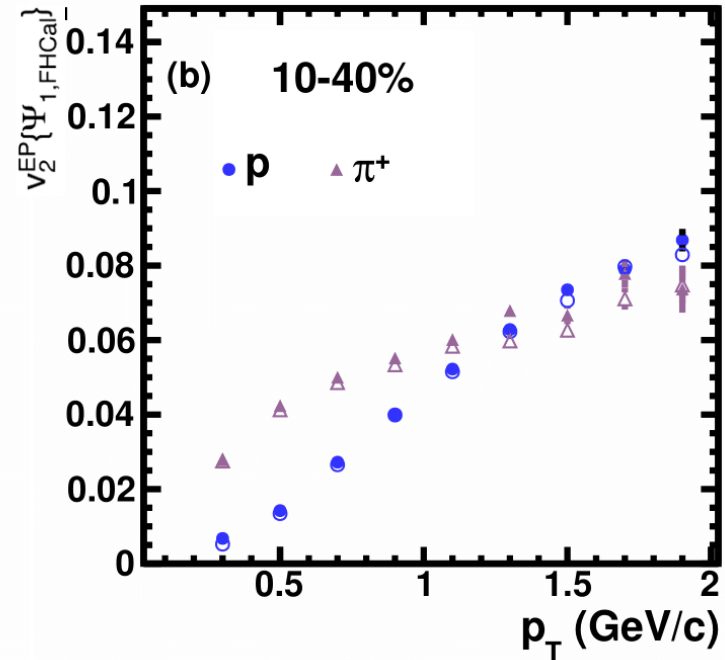
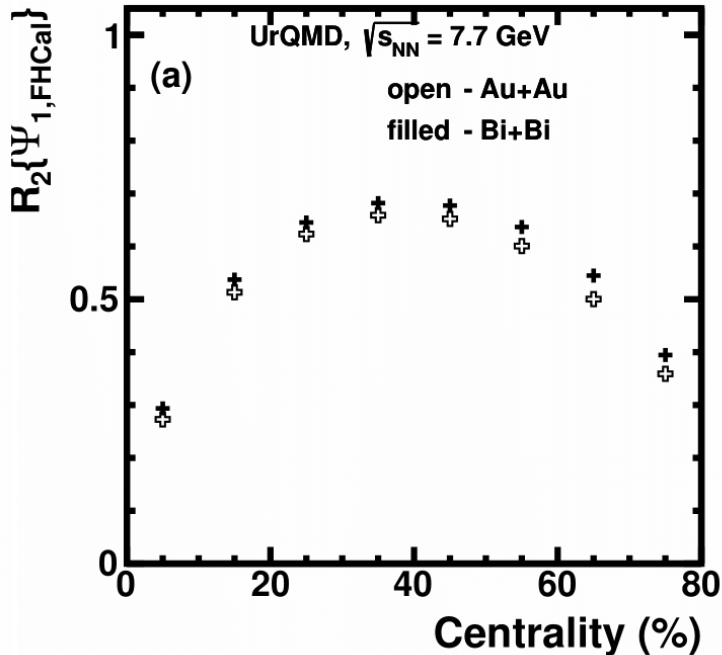
P. Parfenov, The Conference "RFBR Grants for NICA", Dubna (2020)



dv_1/dy slope changes dramatically with centrality for protons

Au+Au vs. Bi+Bi collisions for MPD reconstructed data

- FHCa1 event plane

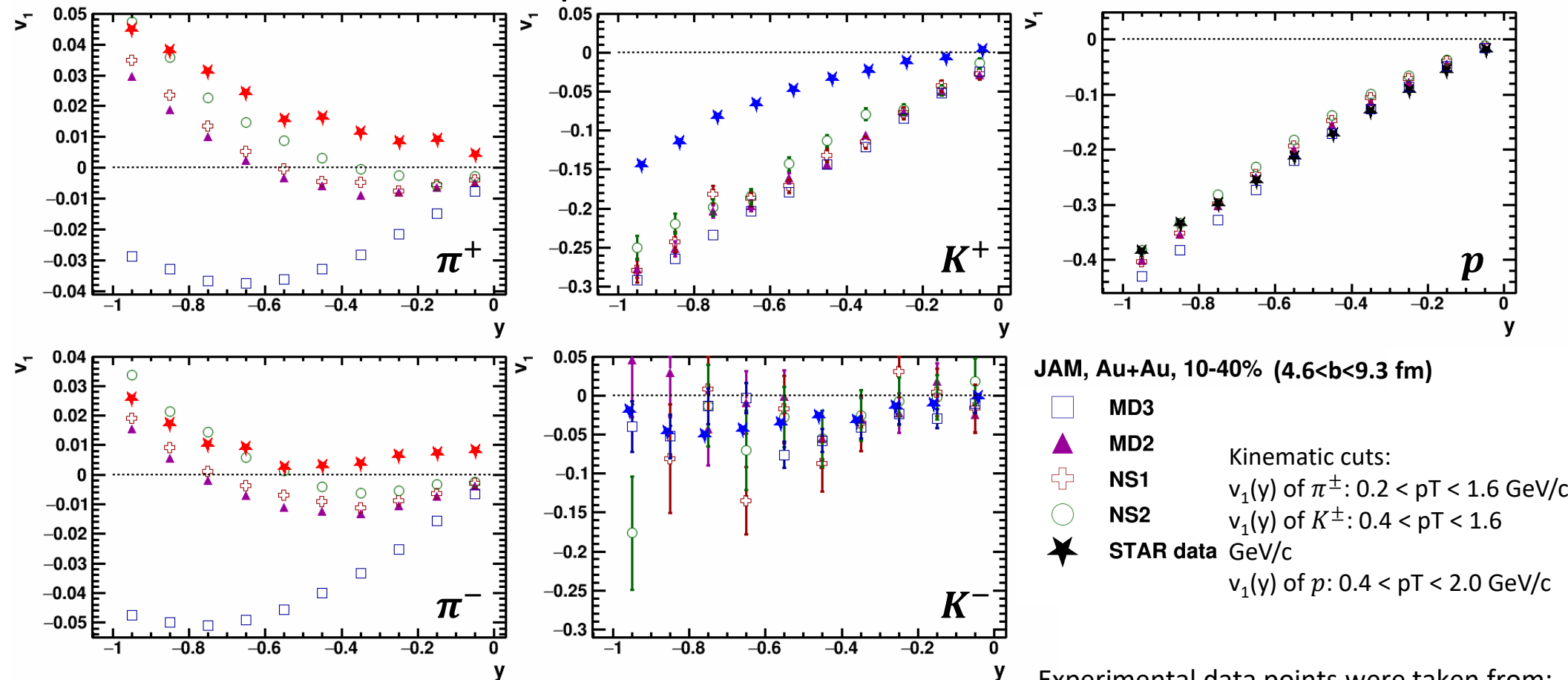


- Expected small difference between two colliding systems



Back-up slides

$v_1(y)$ in Au+Au $\sqrt{s_{NN}}=3$ GeV: model vs. STAR data



JAM does not describe all particle species equally well
 v_1 of pions is most sensitive to different EOS

JAM, Au+Au, 10-40% ($4.6 < b < 9.3$ fm)

- MD3
- ▲ MD2
- + NS1
- NS2
- ★ STAR data

Kinematic cuts:

$v_1(y)$ of π^\pm : $0.2 < p_T < 1.6$ GeV/c

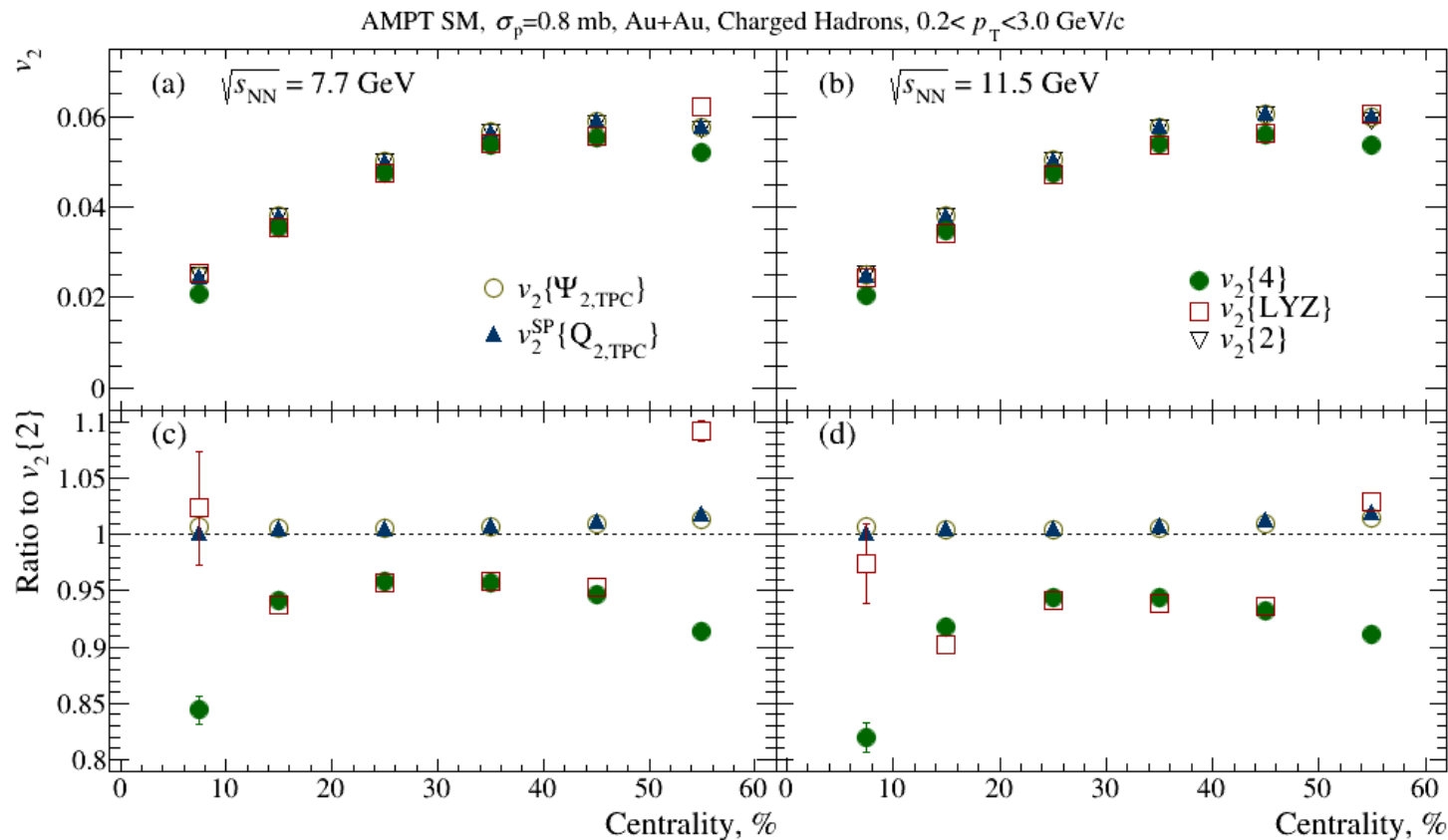
$v_1(y)$ of K^\pm : $0.4 < p_T < 1.6$

GeV/c

$v_1(y)$ of p : $0.4 < p_T < 2.0$ GeV/c

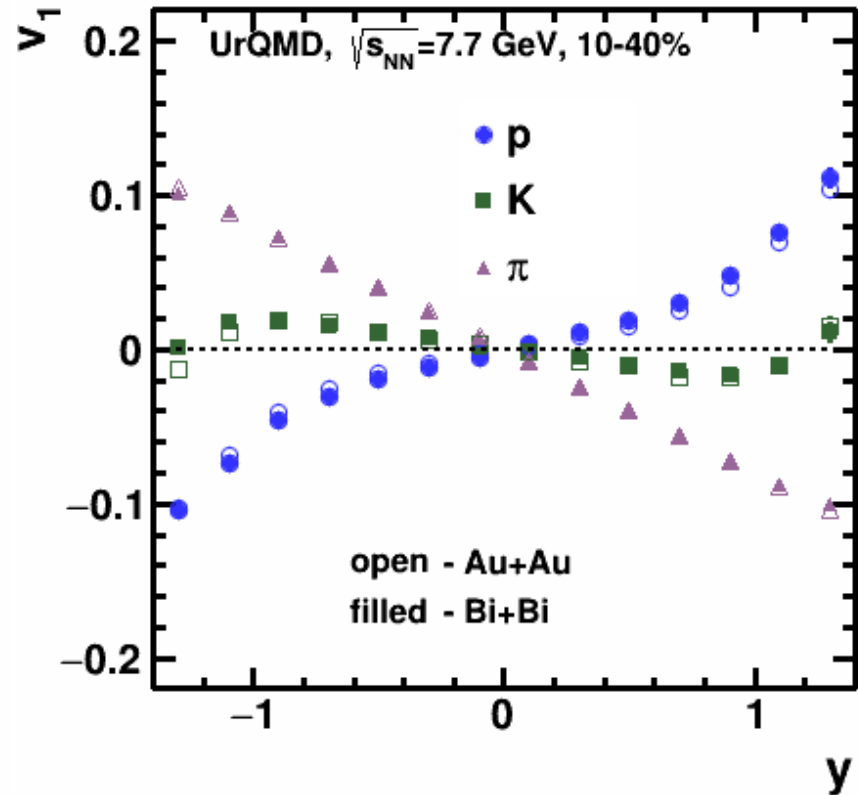
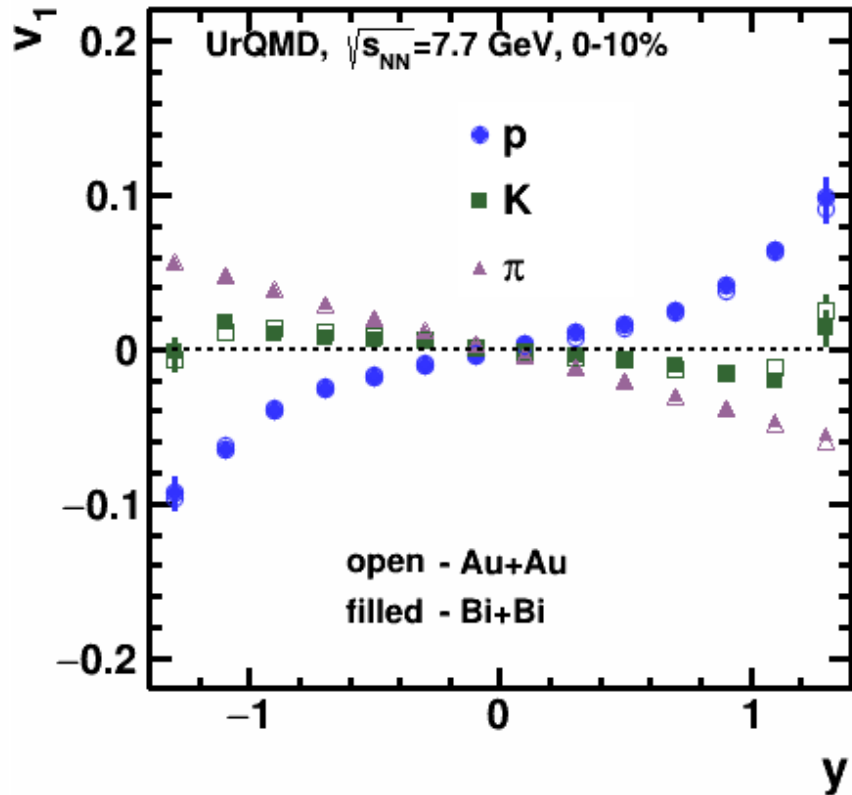
Experimental data points were taken from:
 Mohamed Abdallah et al. [STAR Collaboration]
 2108.00908 [nucl-ex]

Centrality dependence of v_2 {methods}



$$v_2\{4\} \approx v_2\{LYZ\}, v_2\{2\} \approx v_2\{SP\} \approx v_2\{\Psi_{2,TPC}\}$$

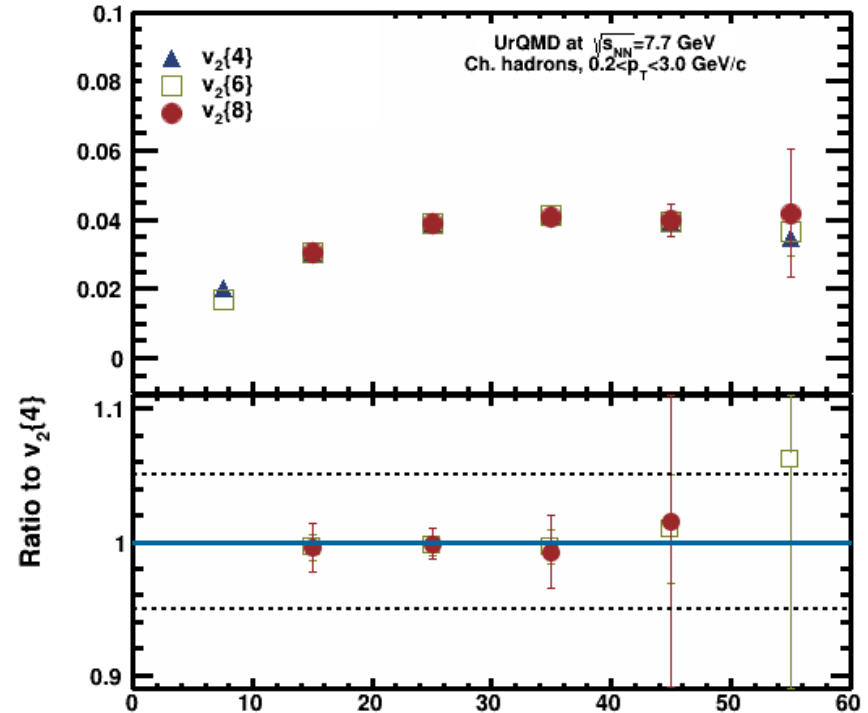
$v_1(y)$: Bi+Bi vs Au+Au



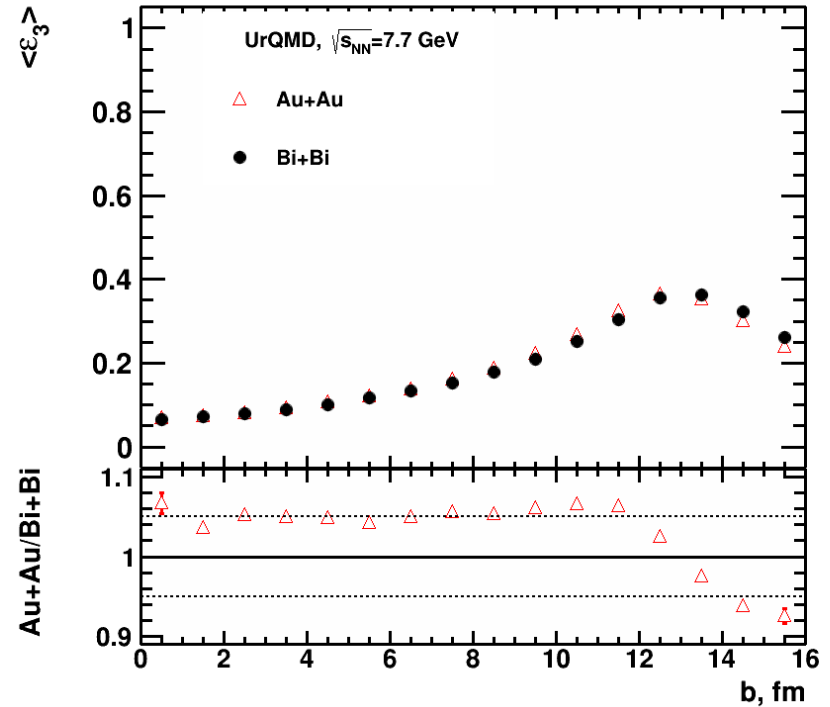
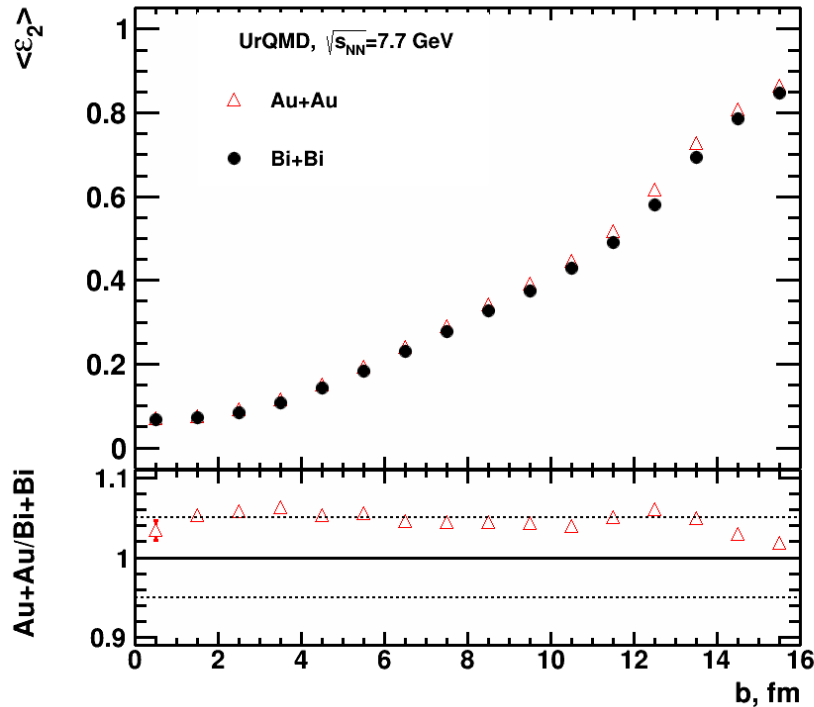
Expected small difference for $v_1(y)$ for particles produced in Au+Au and Bi+Bi collisions.

Description of high-order Q-Cumulants

- Higher order Q-Cumulants $v_2\{m\}$ ($m=6,8$):
- (A. Bilandzic et al., Phys. Rev. C **89** (2014), 064904)
 - ▶ number of terms in “standalone” analytical expressions increases quickly with order of correlators
 - ▶ using recursive algorithms: calculate analytically higher-order correlators in terms of lower ones



Eccentricity: Bi+Bi vs. Au+Au



UrQMD model predicts small difference between ε_n of Au+Au and Bi+Bi