



Hydrodynamics and flow: theory perspective

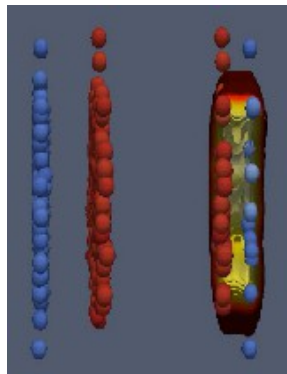
Gabriel S. Denicol

McGill University

Main Motivation

- Relativistic **fluid dynamics** has played a key role in our current understanding of the novel “**near perfect**” fluid behavior displayed by the Quark-Gluon Plasma
 - Created matter behaves as a fluid
 - “thermalization” at very early times $\tau \sim 0.5$ fm
 - “Small”, but important, shear viscosity

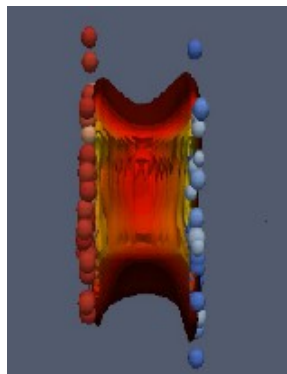
Hydrodynamic modeling of heavy ion collisions



Initial state and pre-equilibrium dynamics
description of early time-dynamics and thermalization
“initial condition” for hydrodynamic evolution



(approach) thermalization



Fluid-dynamical expansion of QGP and Hadron Gas

$$\partial_\mu T^{\mu\nu} = 0 \quad \partial_\mu N^\mu = 0$$

+ EoM for dissipative currents

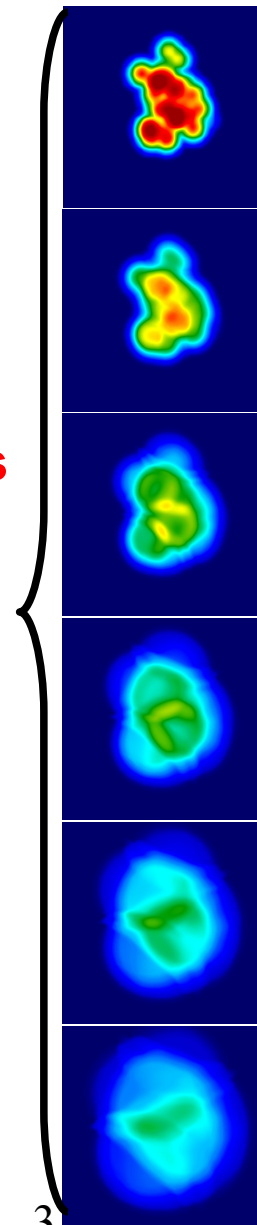
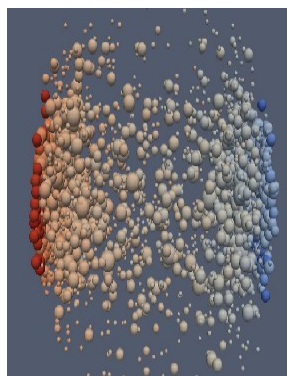
EoS, viscosities, diffusion coefficients...



fluid elements converted
to particles

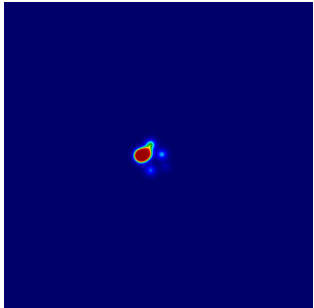
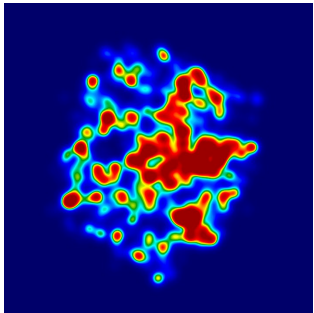
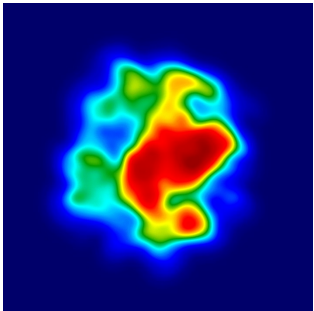
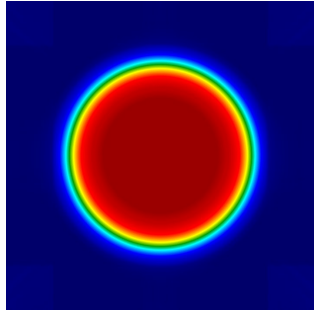
Transport description of Hadron Gas

Matter described by cross sections and decay probabilities
UrQMD, JAM, ...



Evolution of hydro model

$\varepsilon(x,y)$



**Smooth Initial conditions
($v_2=0$ in central collisions)**



**Fluctuations in nucleon positions
(odd harmonics)**



**sub-fermionic fluctuations
(v_n distributions & correlations)**



proton-Nucleus collisions

**Coarse-graining
size**

$\lambda \sim 5$ fm

$\lambda \sim 1$ fm

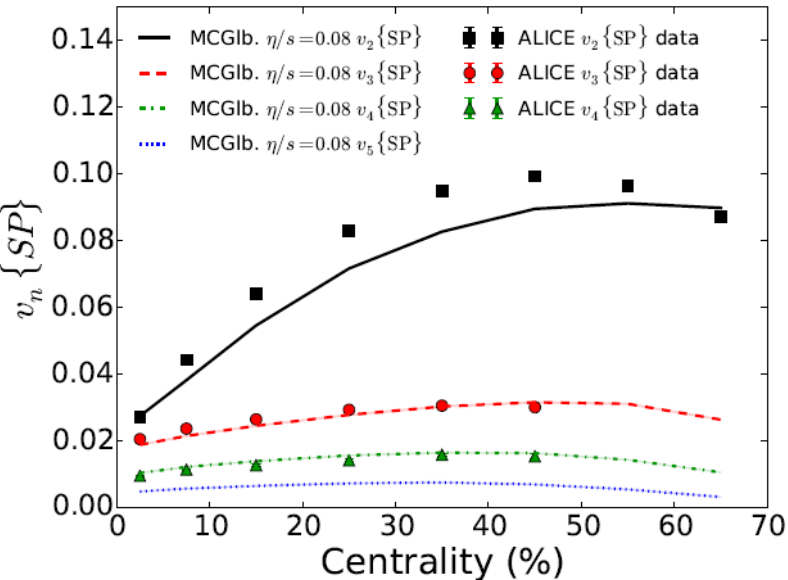
$\lambda \sim 0.3$ fm

$\lambda \sim 0.3$ fm
or smaller

Event-by-event fluctuations changed the game

Hydrodynamic models should describe, not only event-averaged observables, but also distributions/correlations of observables

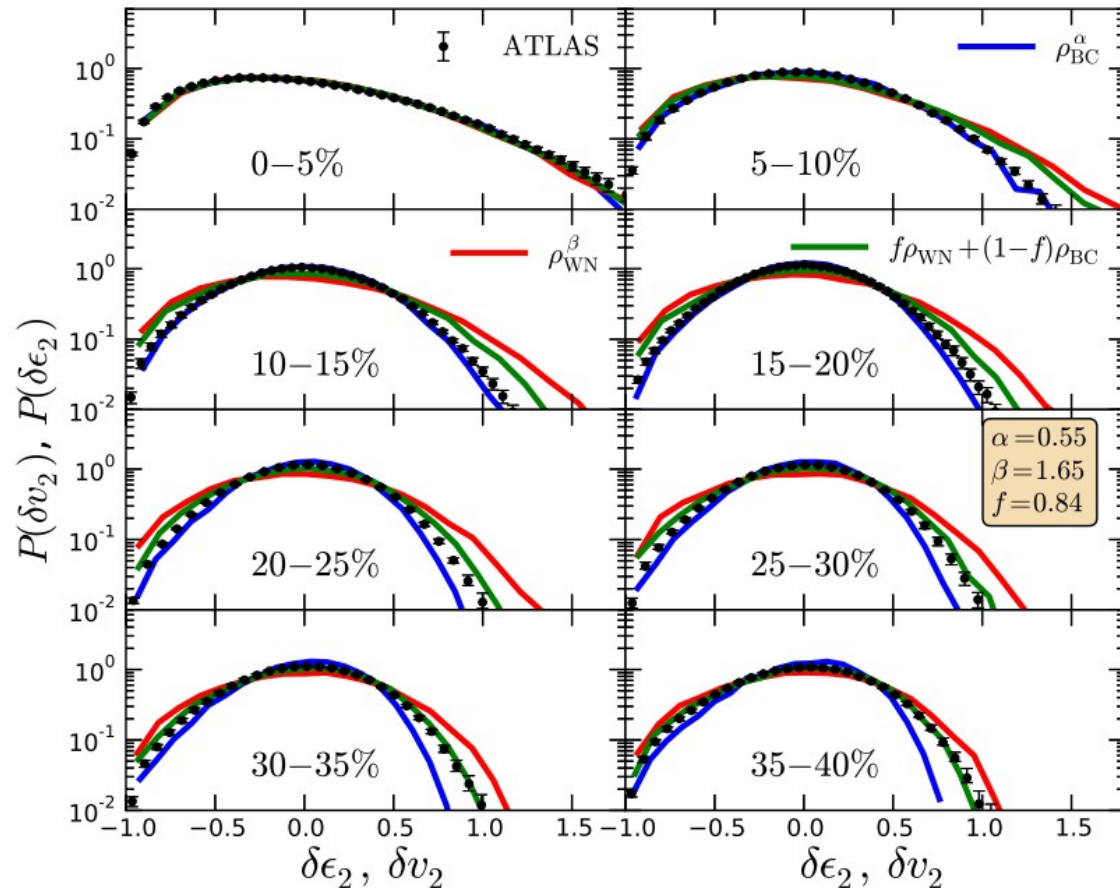
Centrality dependence of v_n



Difficult to describe v_2 and v_3 with the same shear viscosity

v_2 distributions (measured by ATLAS)

Cannot be described by Glauber and KLN



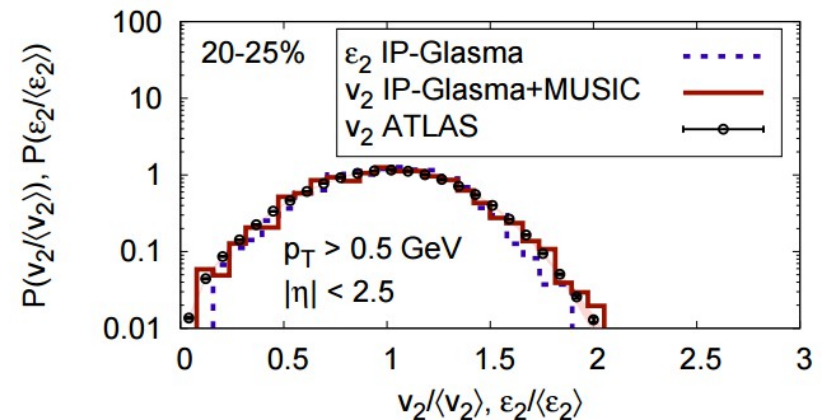
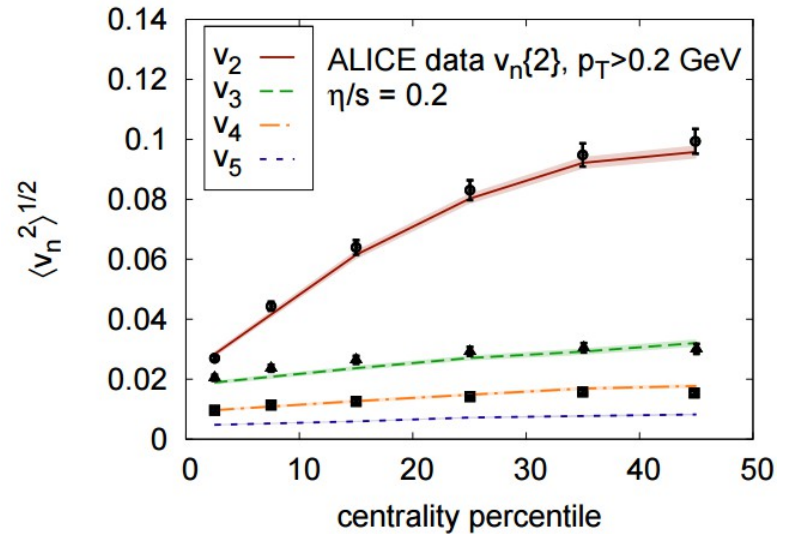
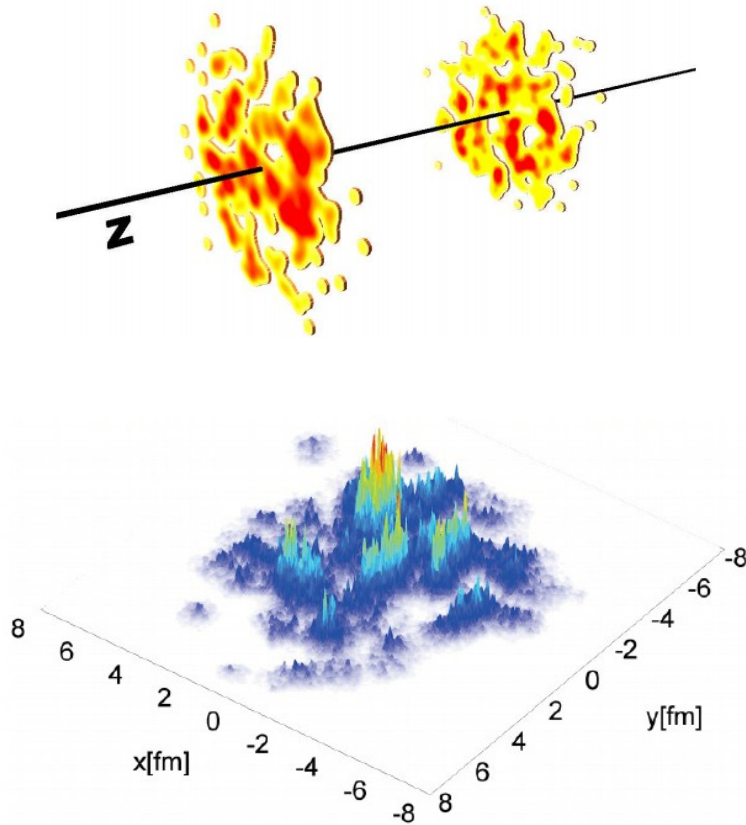
IP-Glasma: IPsat model + Yang-Mills evolution

$\eta/s=0.2$

Very good description of flow harmonic coefficients

Prediction of v_n distribution

Gale *et al*, PRL 110 (2013) 1, 012302

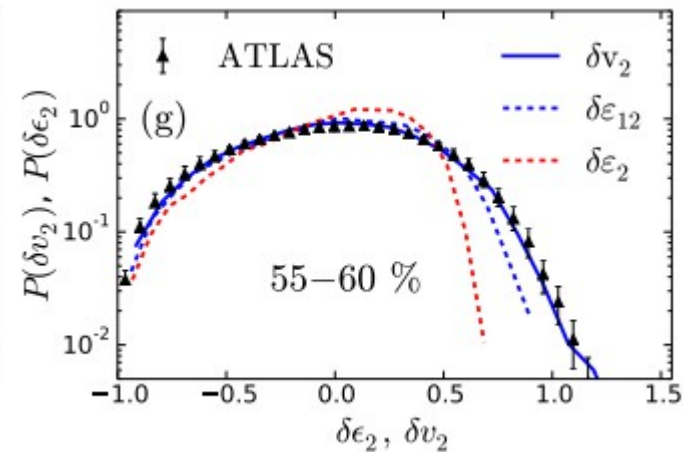
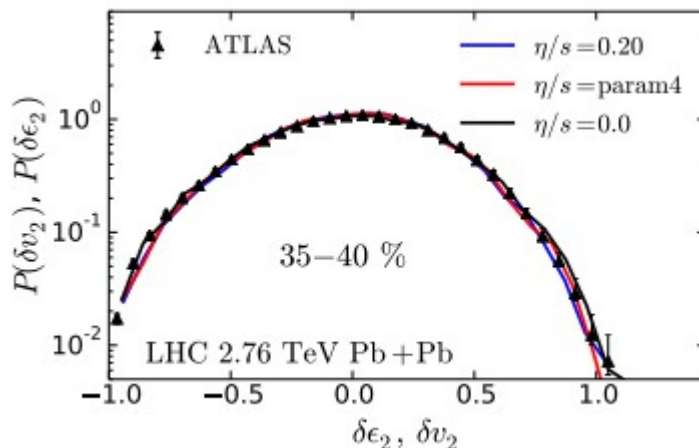
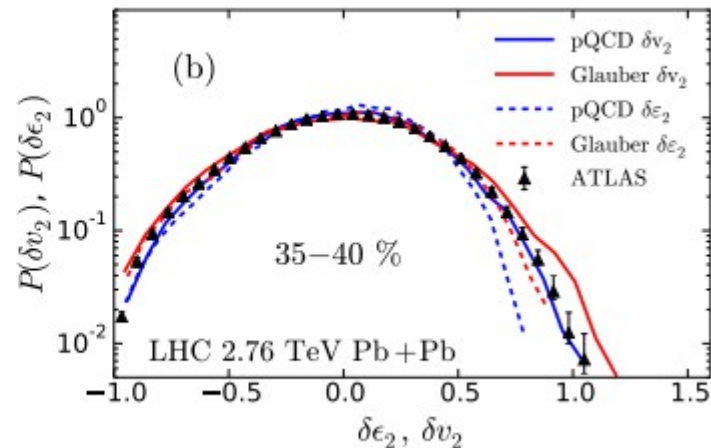
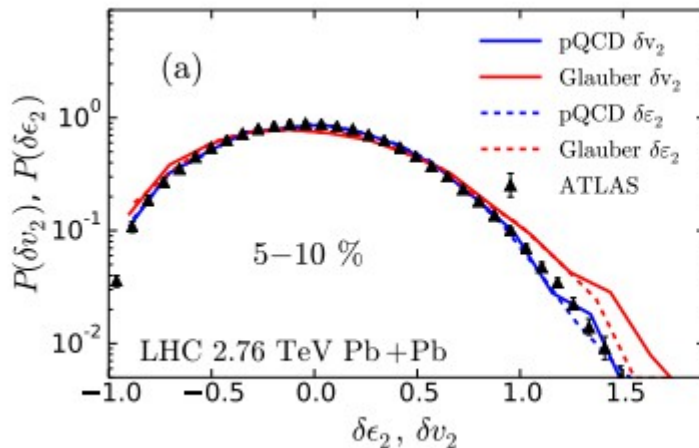


EKRT model: NLO-improved pQCD + saturation

Niemi *et al*, arXiv:1505.02677

Also able to describe event-by-event distributions of flow

Central



Peripheral

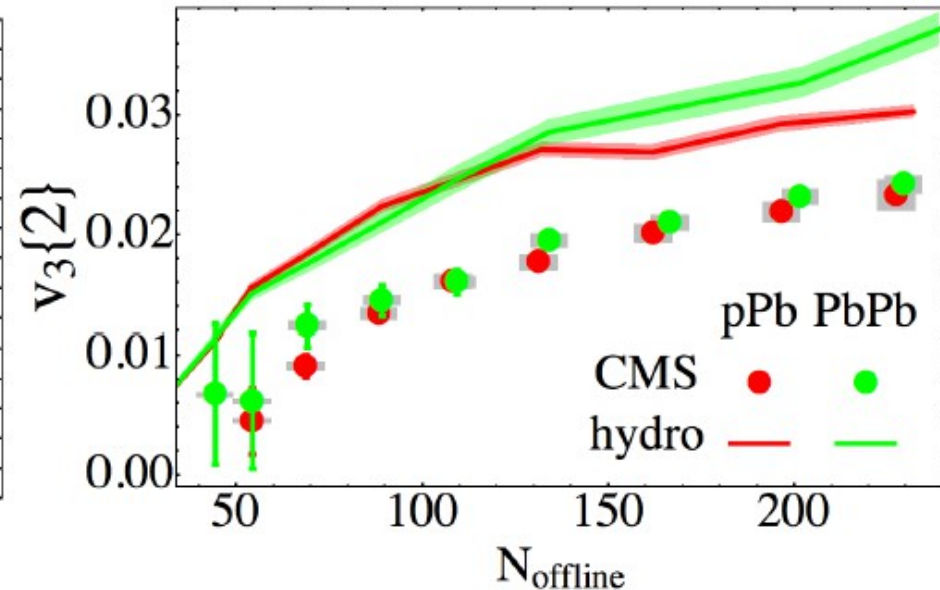
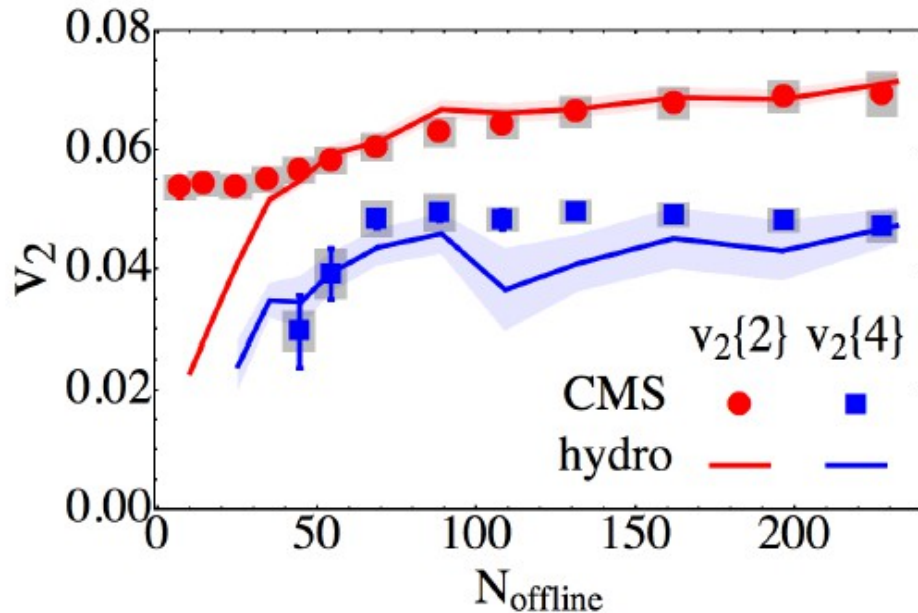
Why can only EKRT and IP-Glasma describe this data?

Hydrodynamics in small systems

Hydrodynamic description of small systems?

The same signals usually associated to flow in AA collisions are now also seen in pA

Nucl.Phys. A931 (2014) 1045-1050

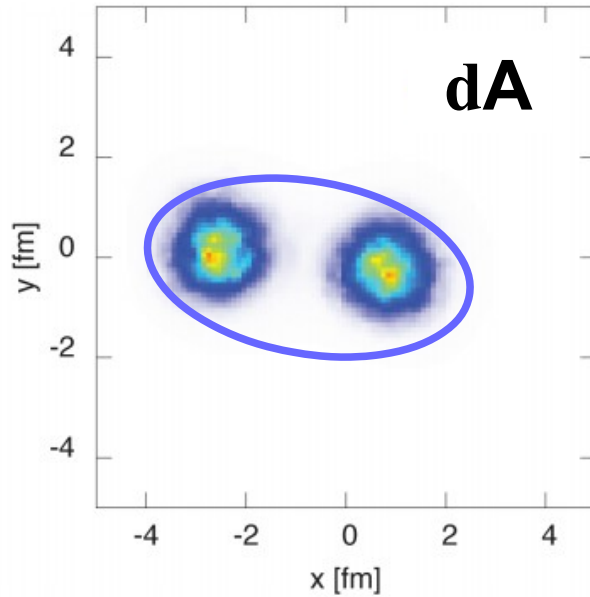


Large v_2 signal is also observed in p-N collisions

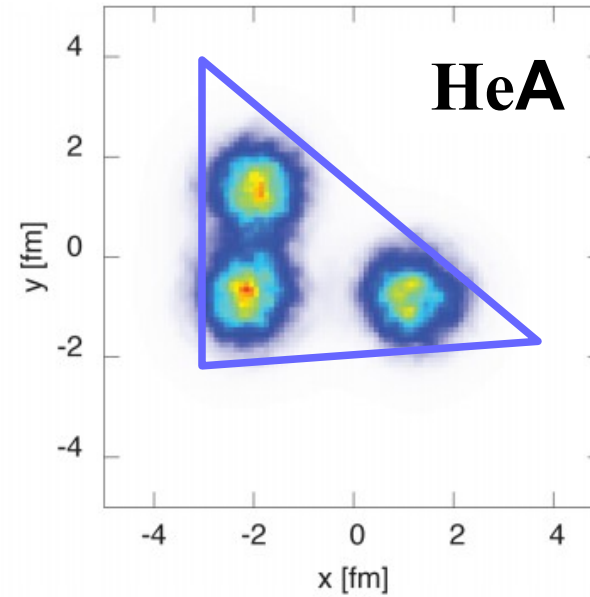
Hydrodynamic simulations seem to be able to describe it!

But how? What is a large volume for the QGP?

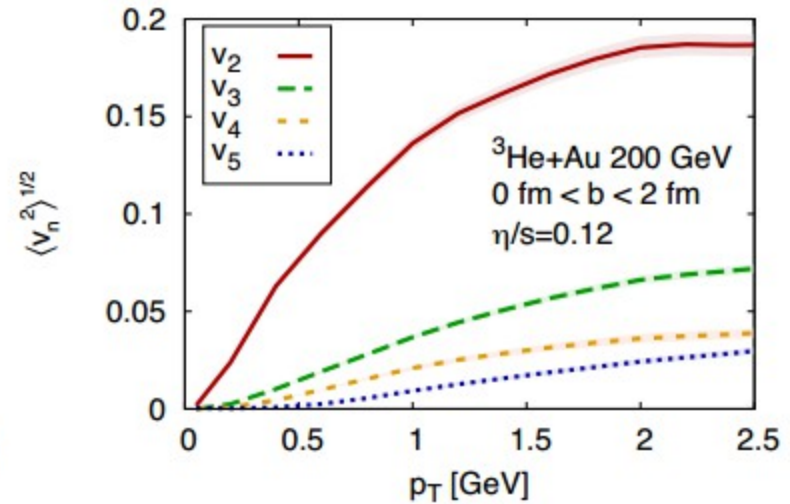
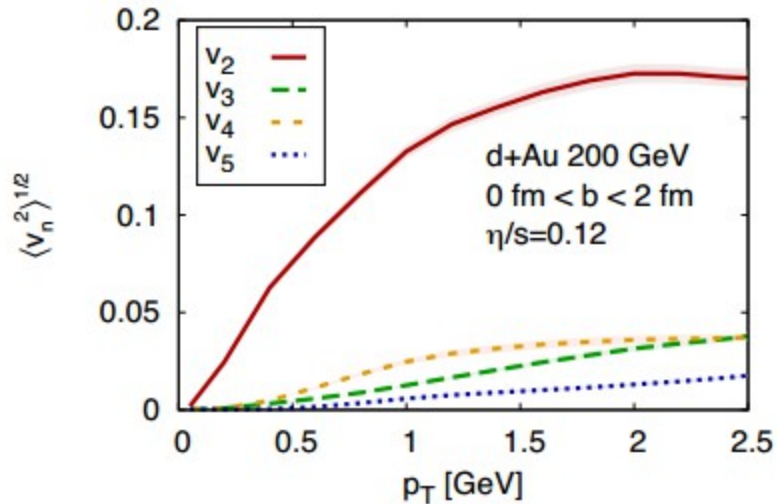
Hydrodynamic description of small systems?



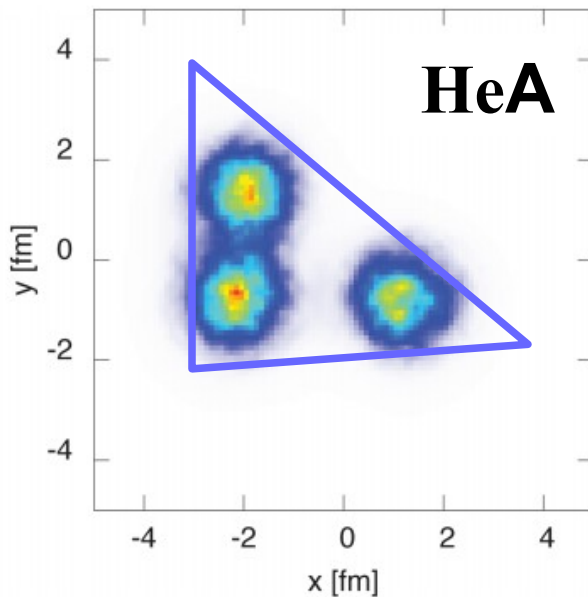
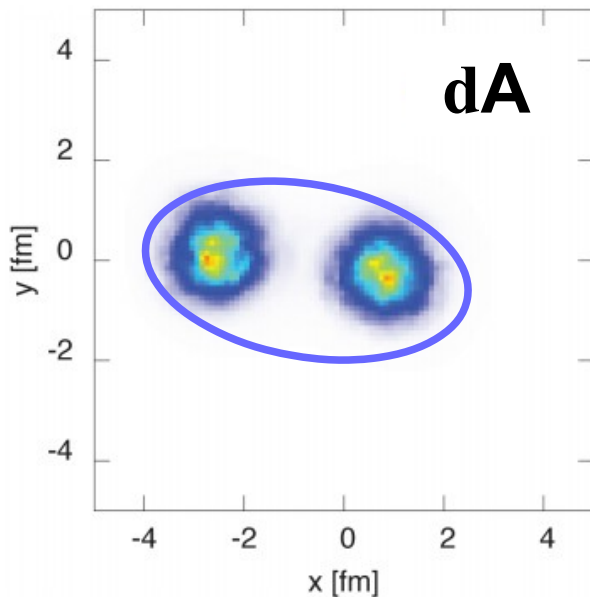
Large ellipticity



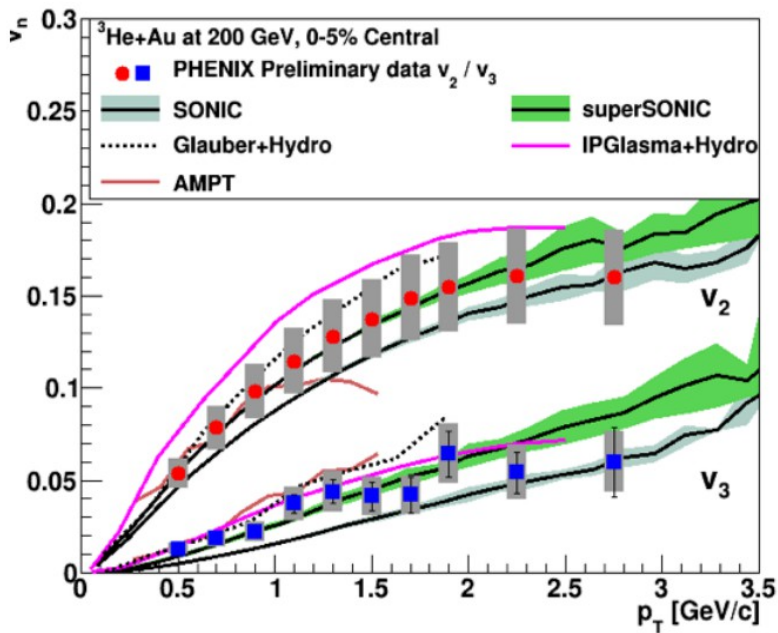
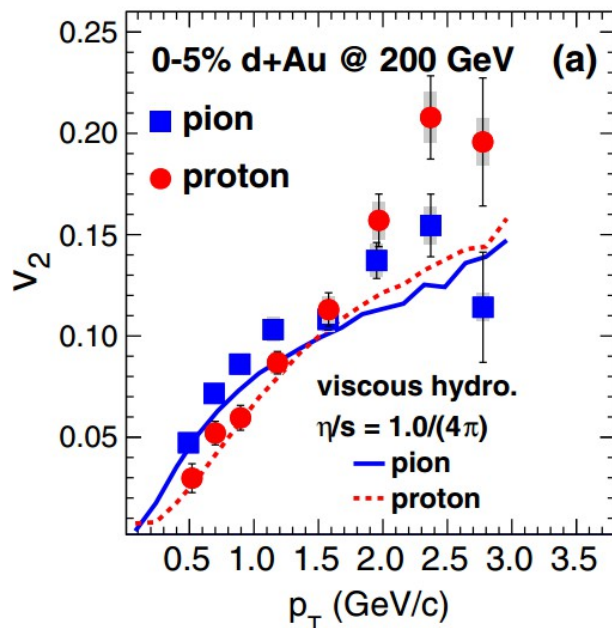
Large triangularity



Hydrodynamic description of small systems?



Good agreement of hydro calc. with PHENIX data



Hydrodynamic description of small systems?

Apparent strong response to initial shape:
typical signature of hydrodynamic behavior

What is small?

Finite viscosity defines a length scale
(mean free-path for dilute gases)

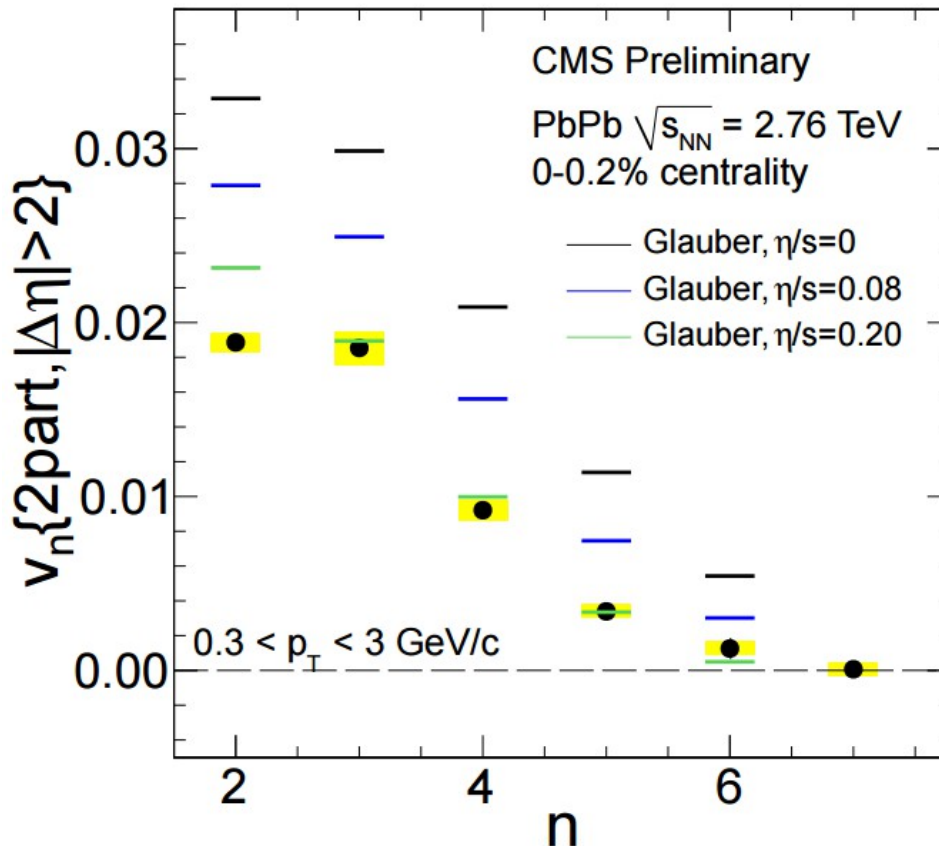
$$\text{Relaxation time: } \tau_{\pi} = 5 \frac{\eta}{\varepsilon + P}$$

Right now, very small values of shear viscosity
are being used: $\eta/s=0.08$

Unlike in AA collisions, not much room to increase
the viscosity (hydro becomes not applicable)

Ultracentral Heavy ion collisions

- **Nonhydrodynamic**(?) behaviour in ultracentral PbPb collisions



$$v_2 \sim v_3$$

where is viscous damping?

Hydrodynamic models
always over-predict
the elliptic flow

CMS coll., CMS-PAS-HIN-12-011
Calculations by Luzum, arXiv:1210.6010

So far, all hydro models cannot get this right

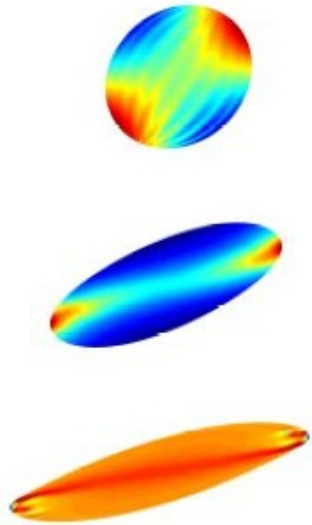
Transport coefficients

Sources of viscosity and dissipation

Shear viscosity

Resistance to deformation

$$\pi^{\mu\nu} = 2\eta \nabla^{\langle\mu} u^{\nu\rangle}$$



very studied

Bulk viscosity

Resistance to expansion

$$\Pi = -\zeta \nabla_{\mu} u^{\mu}$$



little studied

Charge/particle diffusion

$$q^{\mu} = \kappa \nabla^{\mu} \frac{\mu_B}{T}$$

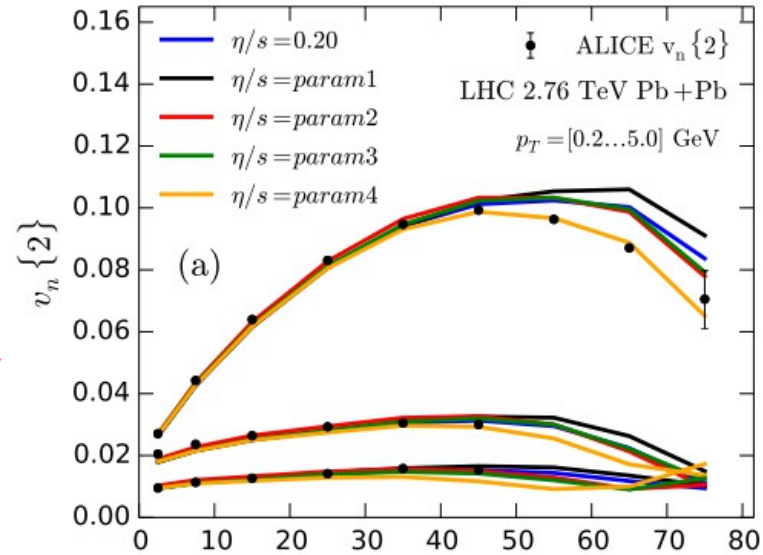
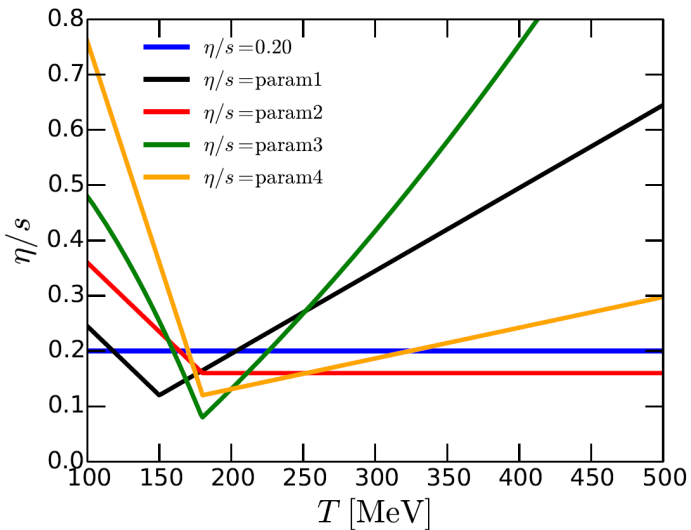


Not yet ... but
coming¹⁵

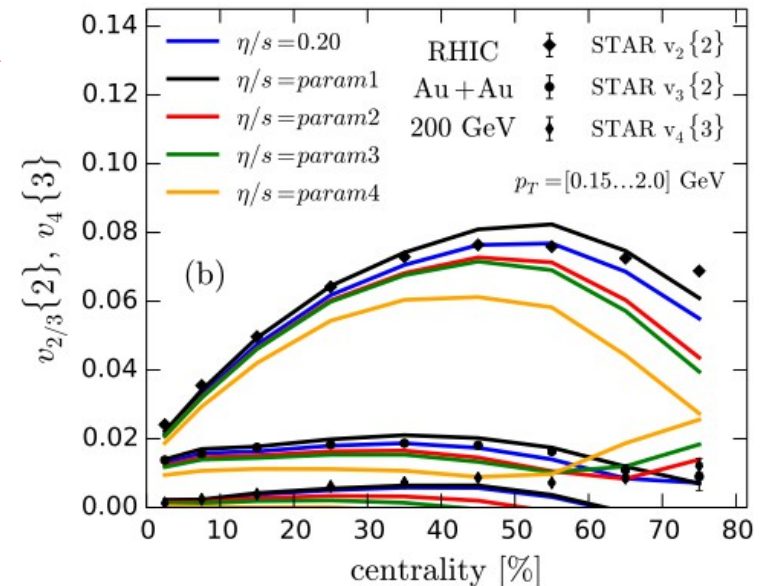
EKRT model + second order viscous hydro

Niemi *et al.*, arXiv:1505.02677

$\eta/s(T)$



LHC

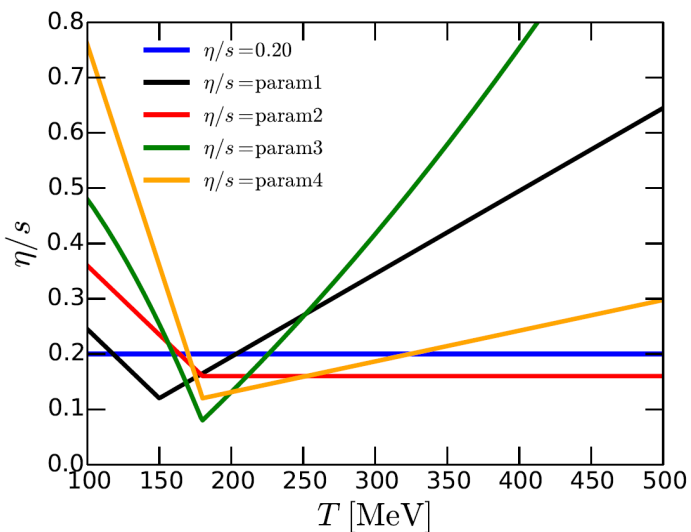


RHIC

What happens when we change $\eta/s(T)$?

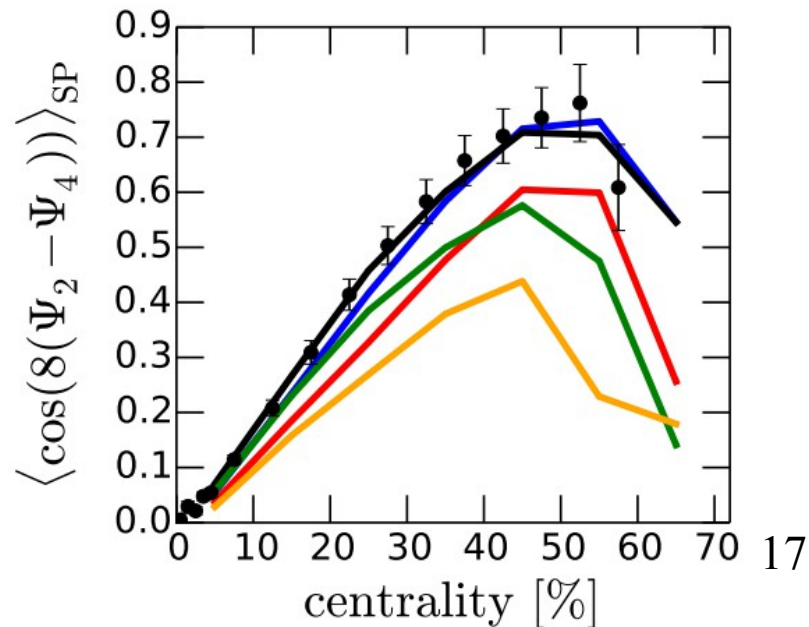
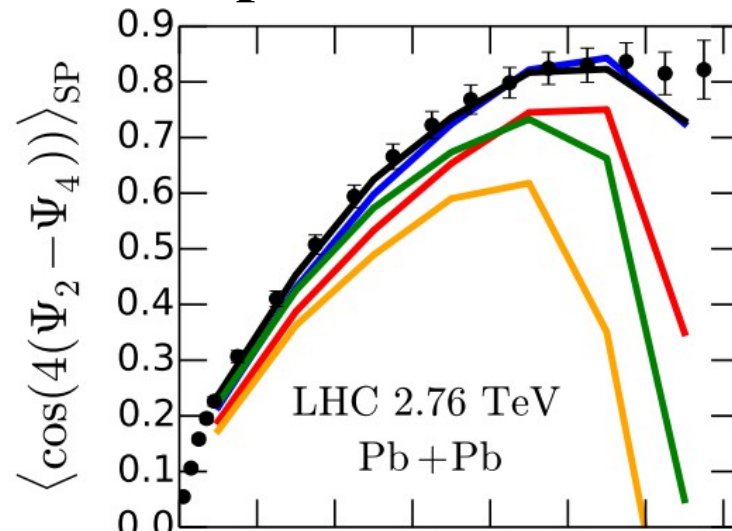
Can we extract it ?

$\eta/s(T)$



It is necessary to look at more than $v_{2,3}$ to obtain $\eta/s(T)$

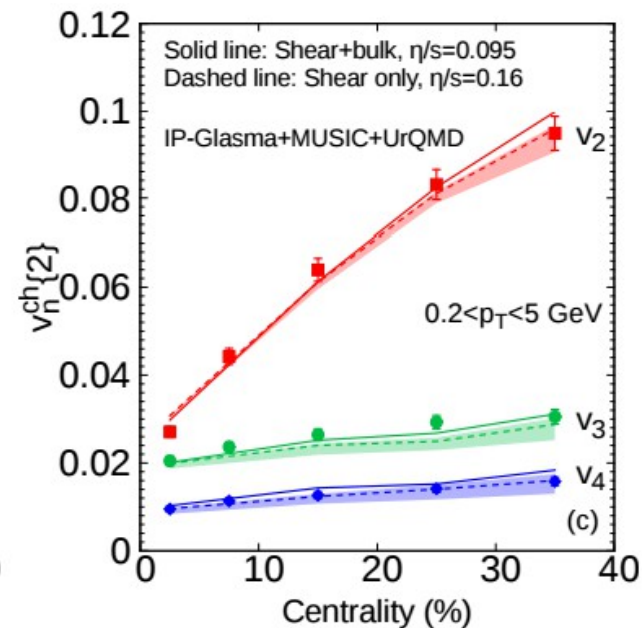
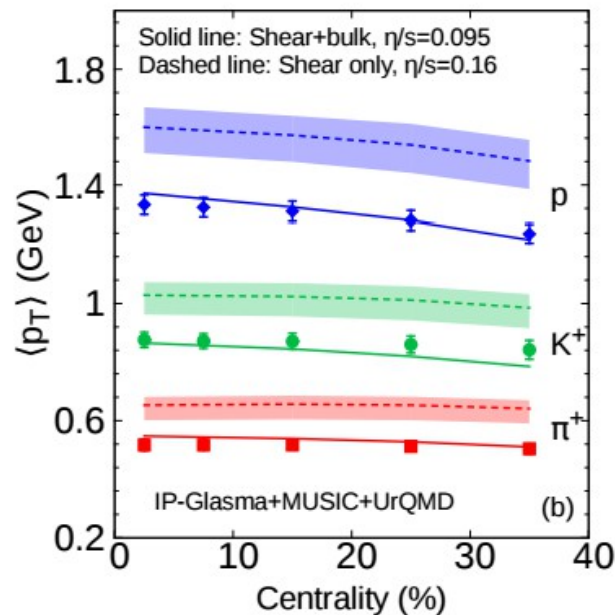
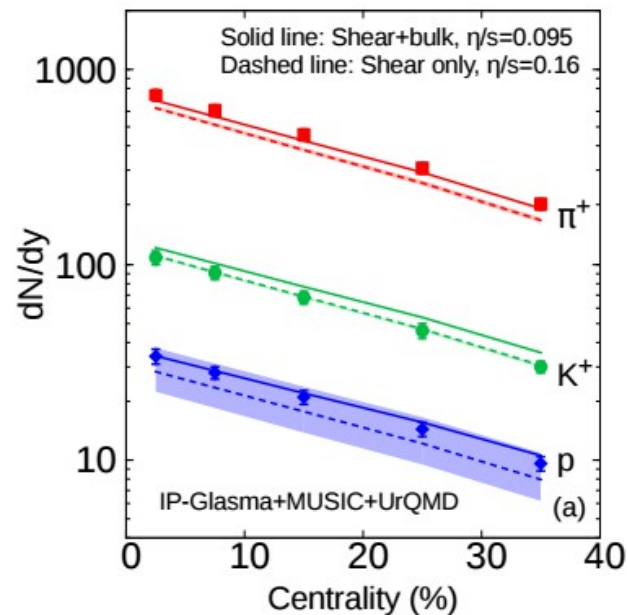
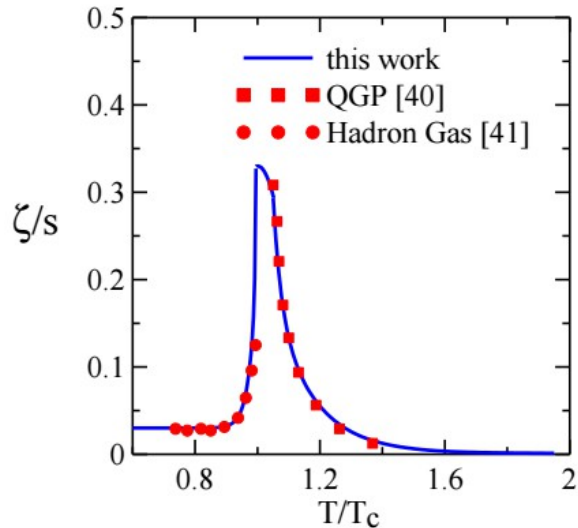
event-plane correlations



IP-Glasma initial conditions lead to high mean p_T
(sub-fermionic fluctuators?)

Need bulk viscosity to explain the mean p_T
of identified hadrons

Value of shear viscosity extracted changes
 $\eta/s=0.16 \longrightarrow 0.095$

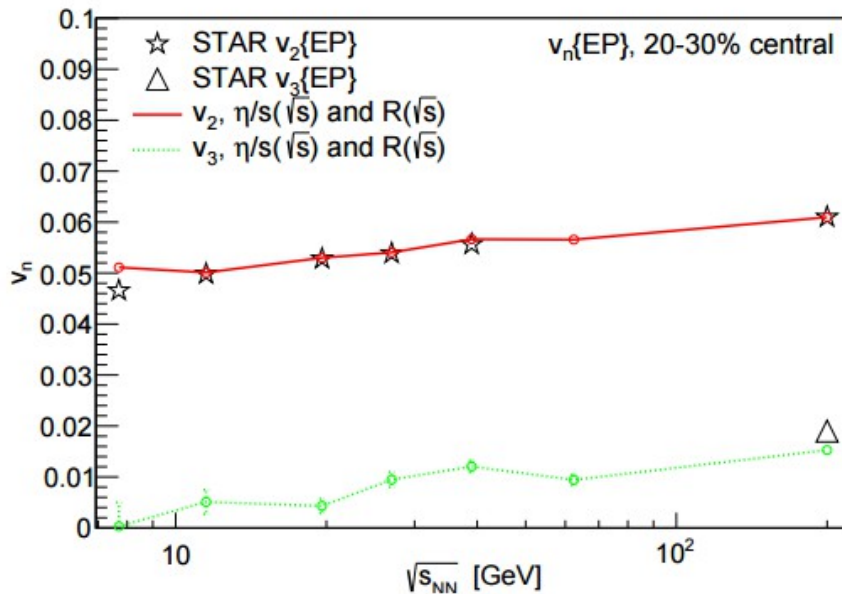


Modeling of heavy ion collisions at lower energies

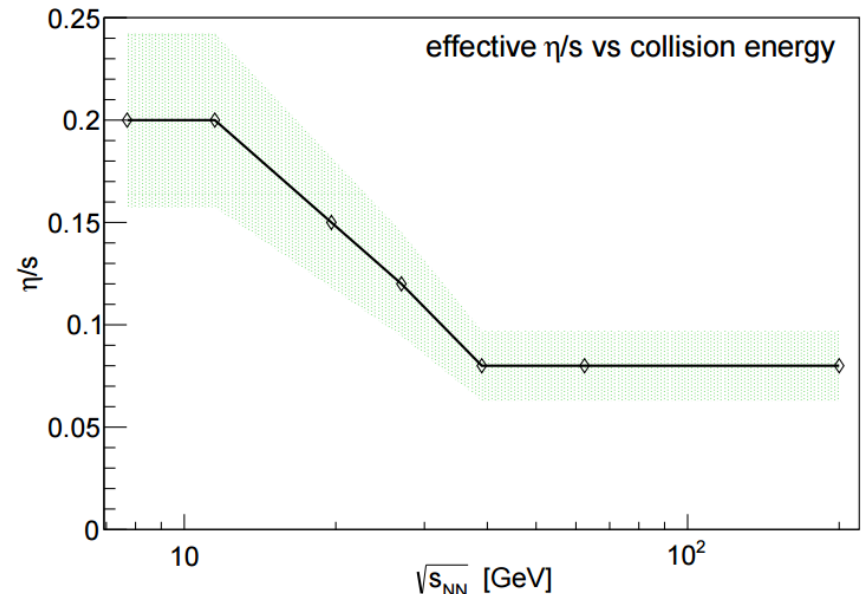
Finite baryon number, isospin, and electric charge must be included

Effective EoS is employed

Steinheimer&Schramm&Stocker, J. Phys. G 38, 035001 (2011).



Good description of v_2 as a function of energy



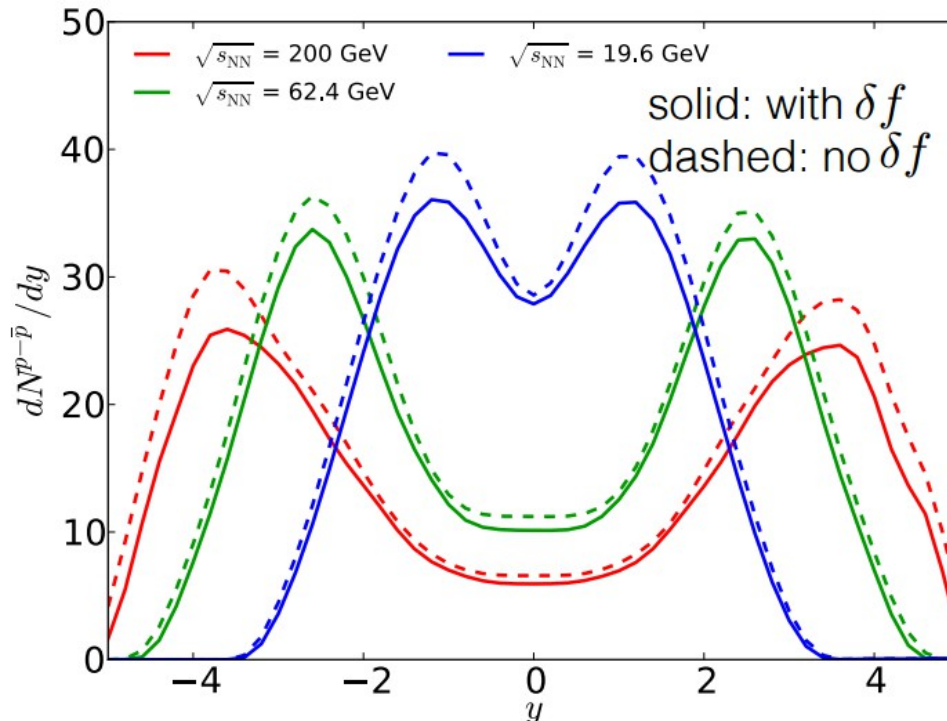
η/s estimated

Modeling of heavy ion collisions at lower energies

$$\Delta^{\mu\alpha} \Delta^{\nu\beta} D\pi_{\alpha\beta} = -\frac{1}{\tau_\pi} (\pi^{\mu\nu} - 2\eta\sigma^{\mu\nu}) - \frac{4}{3}\pi^{\mu\nu}\theta$$

$$\Delta^{\mu\nu} Dq_\nu = -\frac{1}{\tau_q} \left(q^\mu - \kappa \nabla^\mu \frac{\mu_B}{T} \right) - q^\mu \theta - \frac{3}{5} \sigma^{\mu\nu} q_\nu$$

Effect on multiplicity can be large



Can we use RHIC and SPS data to understand this transport coefficient?

Maybe we will know the answer soon

Summary

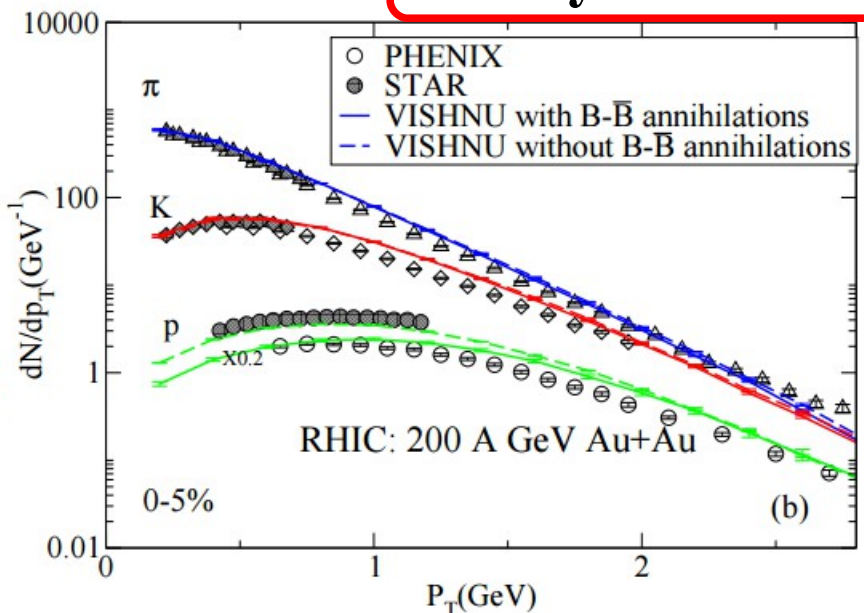
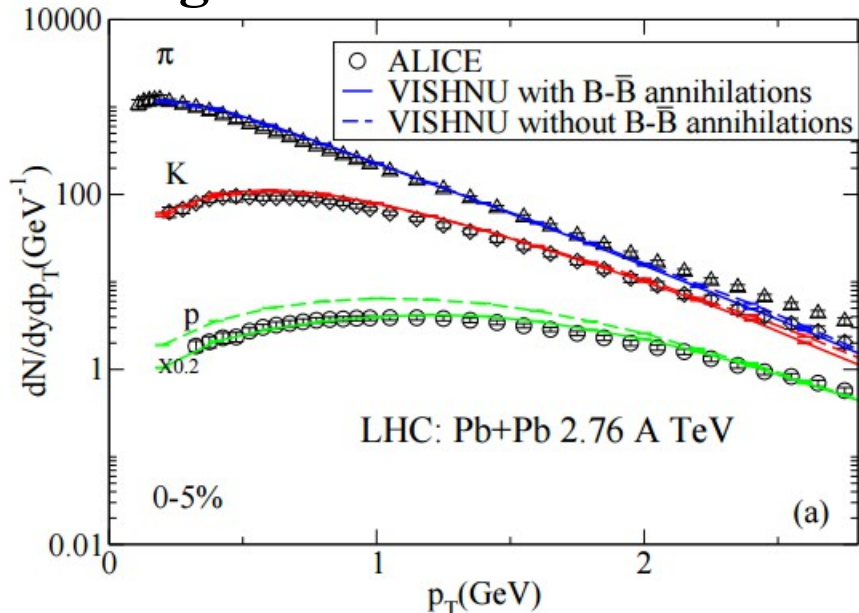
- ✓ Hydrodynamic models are being applied with success to describe small systems and subfermionic fluctuations in AA

Will this hold? Too soon to say ...

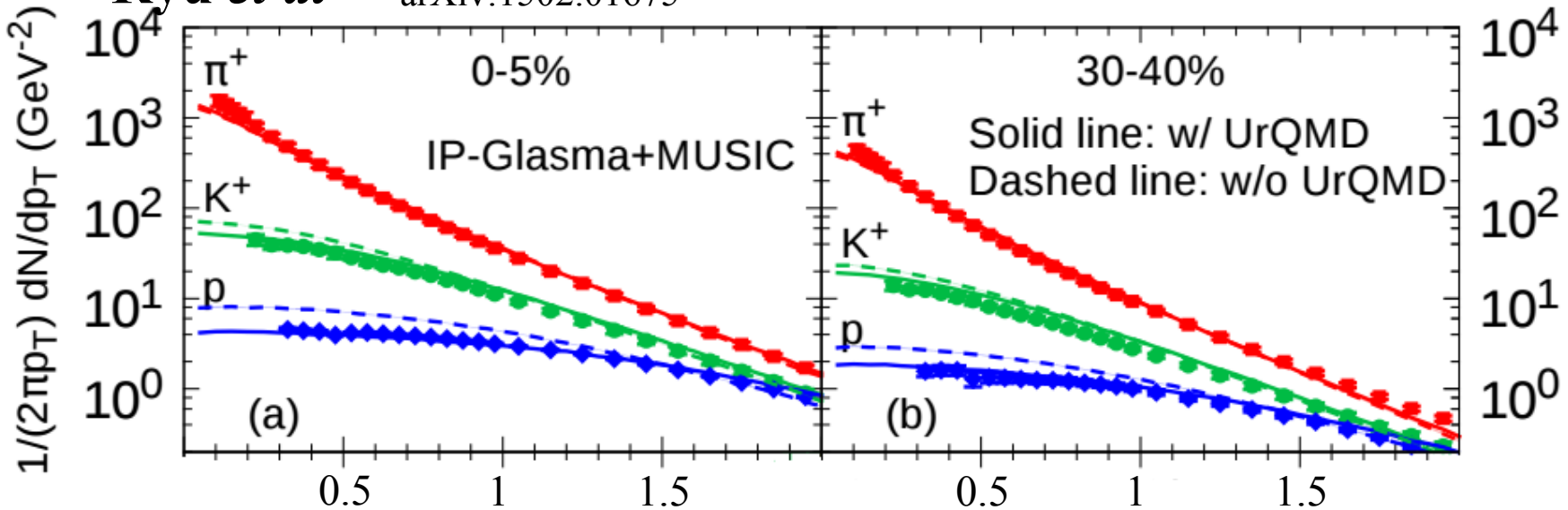
- ✓ But ultracentral AA collisions still cannot be described ...
- ✓ Some progress in understanding transport coefficients:
 - 1) possibility to extract $\eta/s(T)$ also using event-plane correlations
 - 2) IP-Glasma IC suggests a finite bulk viscosity around T_c
 - 3) First estimation of η/s at lower energies

talk by X. Zhu today

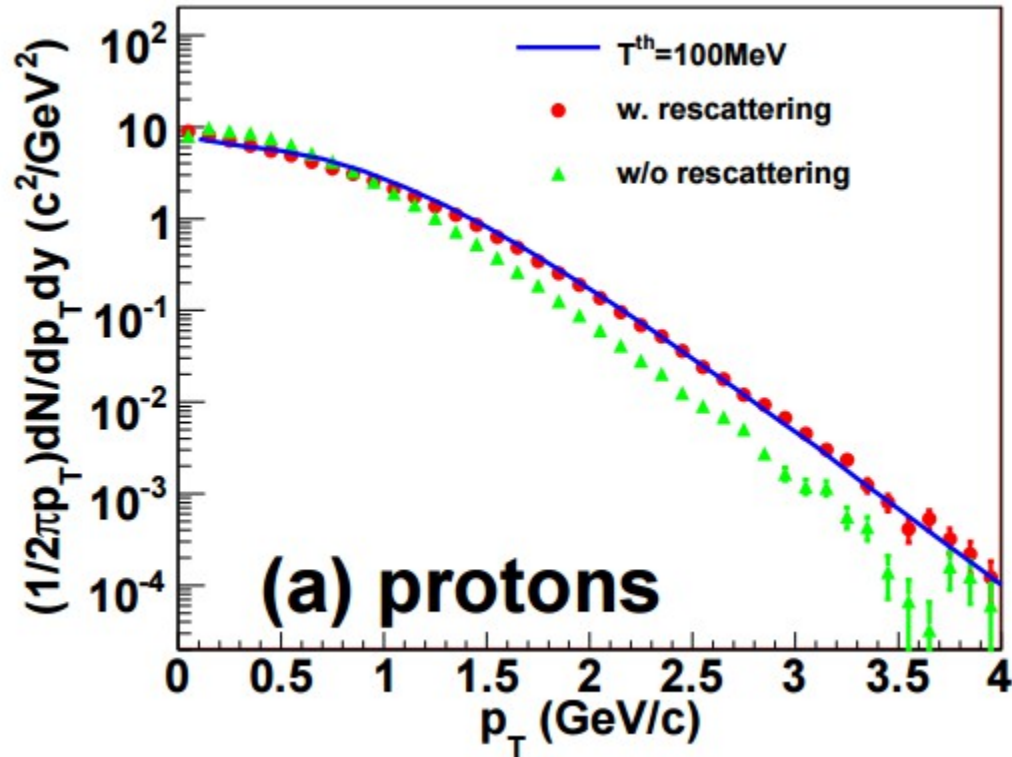
Song et al arXiv:1311.0157



Ryu et al arXiv:1502.01675



Both calculations show an important effect from annihilation as first shown by Steinheimer&Aichelin&Bleicher arXiv:1203.5302

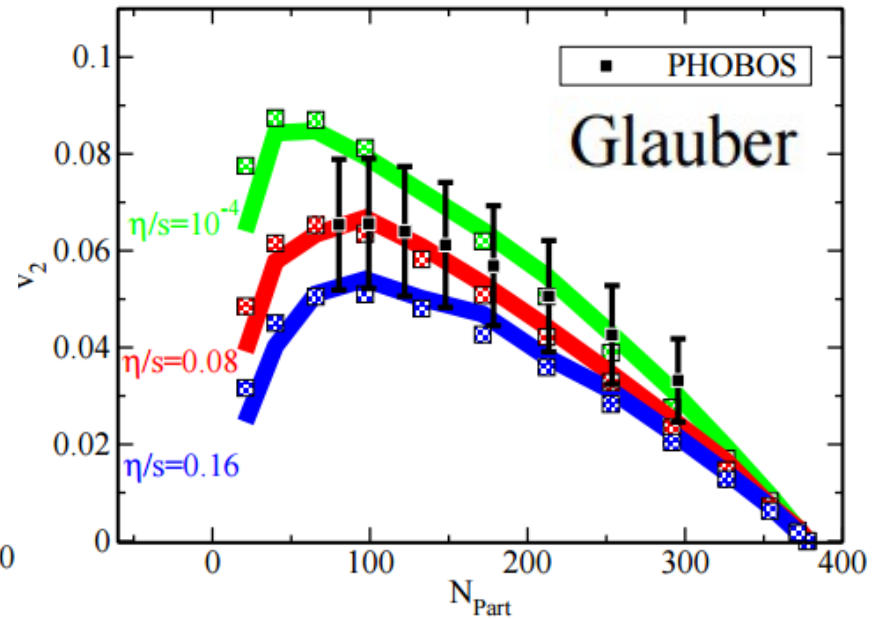
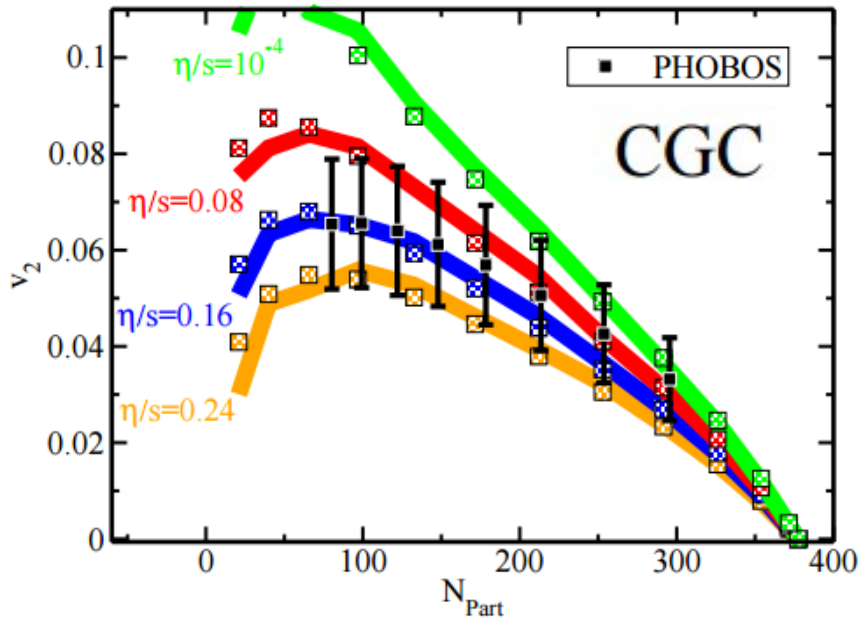


And is still able to describe protons and multi-strange hadrons ... arXiv:1505.05961

Why? Is hadronic transport under control?

Event-by-event fluctuations changed the game

BEFORE: different initial state models could fit the same data by changing the shear viscosity



Luzum&Romatschke PRC 78, 034915 (2008)

Initial state enters as an uncertainty in the extraction of shear viscosity

Hydrodynamic description of small systems?

What is small?

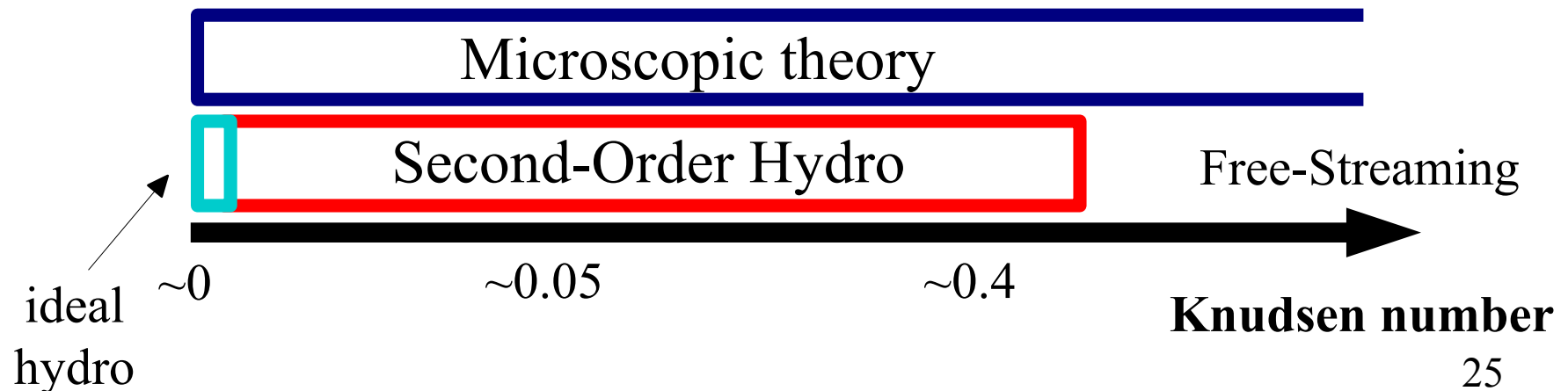
Finite viscosity defines a length scale
(mean free-path for dilute gases)

$$\text{Relaxation time: } \tau_\pi = 5 \frac{\eta}{\varepsilon + P}$$

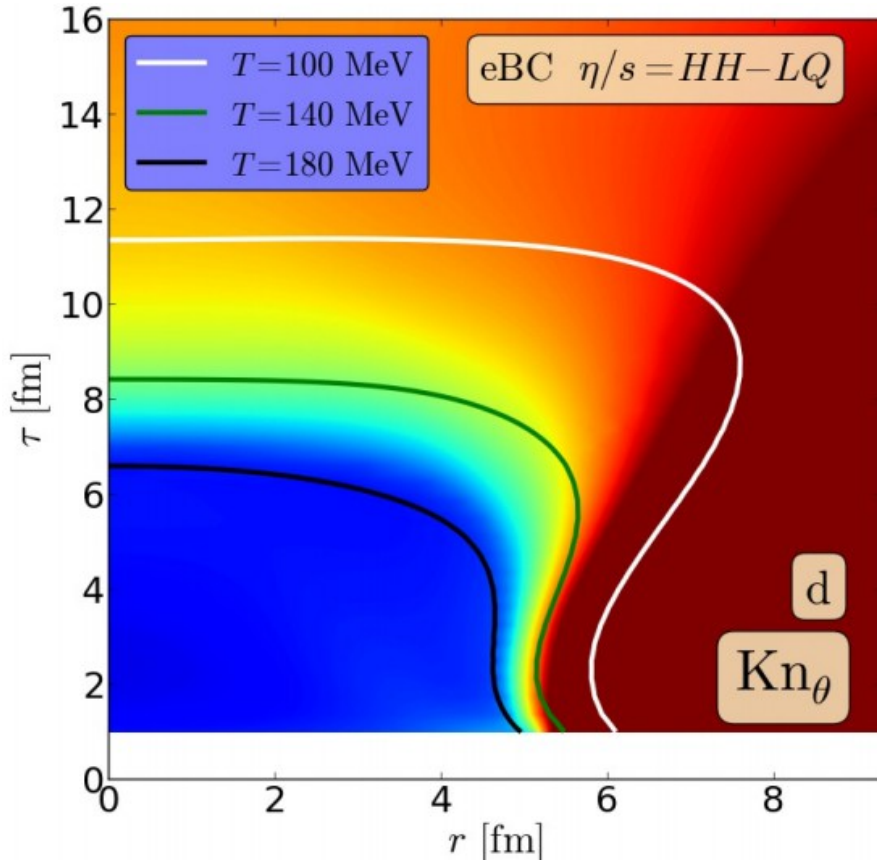
**Validity of fluid dynamics
defined by Knudsen number:**

$$\text{Kn}_i = \tau_\pi / L_{\text{macro}}^i$$

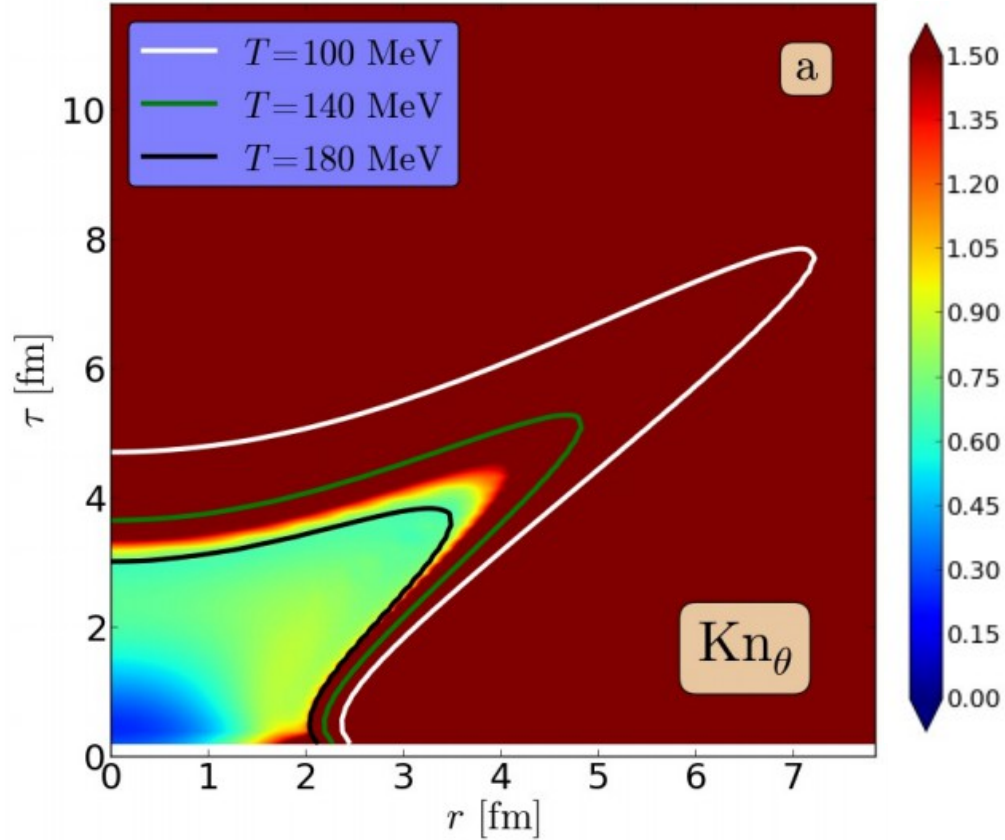
$L_{\text{macro}} \sim$ expansion rate



Snapshot of a collision: Kn in $\tau, x=y$ plane



Noncentral collision, LHC
 $\tau_0=0.6$ fm, $\eta/s=0.08$ in QGP



Ultracentral pA collision, LHC
 $\tau_0=0.2$ fm, $\eta/s=0.08$ in QGP

pA: hydro applies at early times, but breaks down quickly

Viscosity has to be small