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Self-similarity of strangeness production in pp collisions at RHIC

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Introduction

- z-Scaling (ideas, definitions,...)
- > Properties of data z-presentation
- Self-similarity of strange particle production in pp collisions at RHIC
- Momentum fraction, recoil mass and constituent energy loss vs. \sqrt{s} , p_T , strangeness content
- > Summary







Motivation & Goals

Search for new symmetries in Nature

Systematic analysis of inclusive cross sections of particle production in pp, pA and AA collisions to search for general features of structure, interaction and fragmentation over a wide scale range

z-Scaling as a new scaling in high energy physics
 Development of z-scaling approach for description of processes
 with strange particle production in inclusive reactions
 and verification of self-similarity principle

Analysis of new RHIC data on strange particle spectra in pp collisions

The suggested approach can be used to study

- Origin of strangeness
- > Symmetry of constituent interactions at small scales
- Similarity and difference of u,d,s,c,b,t quark fragmentation
- Strangeness as probe to search for new physics
- > pp is a reference frame for pA and AA physics







"Fundamental symmetry principles dictate the basic laws of physics, control the structure of matter, and define the fundamental forces in Nature."

Leon M. Lederman

Self-similarity is a property of physical phenomena and the principle to construct theories.







- A self-similar object is exactly or approximately similar to a part of itself (i.e. the whole has the same shape as one or more of the parts).
- Self-similarity is a typical property of fractals.
- Scale invariance is an exact form of self-similarity where at any magnification there is a smaller piece of the object that is similar to the whole.

Dimensionless dynamical function vs. self-similarity parameter

Drag force vs. Reynolds number Re= ρVD/η hy
 Friction force vs. Mach number Ma=v/c ae
 Structure function F (x) vs. Bjorken variable x=-q²/2(pq) dee

hydrodynamics aerodynamics deep-inelastic scattering









Self-similarity: z-scaling

Inclusive cross sections of π^- , K⁻, \bar{p} , Λ in pp collisions

FNAL: PRD 75 (1979) 764

ISR:

NPB 100 (1975) 237 PLB 64 (1976) 111 NPB 116 (1976) 77 (low p_T) NPB 56 (1973) 333 (small angles)

STAR:

PLB 616 (2005) 8 PLB 637 (2006) 161 PRC 75 (2007) 064901



- Energy & angular independence
- > Flavor independence $(\pi, K, \bar{p}, \Lambda)$
- ➤ Saturation for z < 0.1</p>
- > Power law $\Psi(z) \sim z^{-\beta}$ for high z > 4

Energy scan of spectra at U70, ISR, Sp̄pS, SPS, HERA, FNAL(fixed target), Tevatron, RHIC, LHC

MT & I.Zborovsky T.Dedovich Phys.Rev.D75,094008(2007) Int.J.Mod.Phys.A24,1417(2009) J. Phys.G: Nucl.Part.Phys. 37,085008(2010) Int.J.Mod.Phys.A27,1250115(2012) J.Mod.Phys.3,815(2012)



Scaling – "collapse" of data points onto a single curve. Universality classes – hadron species (ϵ_F , α_F).





- > Energy independence of $\Psi(z)$ (s^{1/2} > 20 GeV)
- > Angular independence of $\Psi(z)$ ($\theta_{cms}=3^0-90^0$)
- > Multiplicity independence of $\Psi(z)$ (dN_{ch}/dη=1.5-26)
- Saturation of $\Psi(z)$ at low z (z < 0.1)
- > Power law, $\Psi(z) \sim z^{-\beta}$, at high z(z > 4)
- Flavor independence of $\Psi(z)$ ($\pi, K, \varphi, \Lambda, ..., D, J/\psi, B, \Upsilon, ..., top$)

These properties reflect self-similarity, locality, and fractality of hadron interactions at a constituent level. It concerns the structure of the colliding objects, constituent interactions and fragmentation process.







 P_1

z-Scaling

Principles: locality, self-similarity, fractality

Locality: collisions of hadrons and nuclei are expressed via interactions of their constituents (partons, quarks and gluons,...). M_1, δ_1

Self-similarity: interactions of the constituents are mutually similar.

Fractality: self-similarity is valid over a wide scale range.

Hypothesis of z-scaling :

 $s^{1/2}$, p_T , θ_{cms}

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₽**,**

Inclusive particle distributions can be described in terms of constituent sub-processes and parameters characterizing bulk properties of the system.

 $Ed^3\sigma/dp^3$

Scaled inclusive cross section of particles depends in a self-similar way on a single scaling variable z. x_1, x_2, y_a, y_b $\delta_1, \delta_2, \varepsilon_a, \varepsilon_b, c$

 m_1

 $\Psi(z)$



 M_2, δ_2



Locality

Collisions of colliding objects are expressed via interactions of their constituents



Momentum conservation law for constituent sub-process

$$(x_1P_1+x_2P_2-p/y_a)^2 = M_X^2$$

 $\begin{array}{c} \textbf{Recoil mass} \\ \textbf{M}_{X} = \textbf{x}_{1}\textbf{M}_{1} + \textbf{x}_{2}\textbf{M}_{2} + \textbf{m}_{2}/\textbf{y}_{b} \end{array}$







Self-similarity

Interactions of constituents are mutually similar



- > Ω^{-1} is the minimal resolution at which a constituent sub-process can be singled out of the inclusive reaction
- > $s_{\perp}^{1/2}$ is the transverse kinetic energy of the sub-process consumed on production of $m_1 \& m_2$
- $> dN_{ch}/d\eta|_0$ is the multiplicity density of charged particles at $\eta = 0$
- ➤ c is a parameter interpreted as a "specific heat" of created medium
- \blacktriangleright m is an arbitrary constant (fixed at the value of nucleon mass)





Fractality

Self-similarity over a wide scale range



 $z = z_0 \cdot \Omega^{-1}$

$$\Omega = (1 - x_1)^{\delta_1} (1 - x_2)^{\delta_2} (1 - y_a)^{\epsilon_a} (1 - y_b)^{\epsilon_b}$$

 Ω is relative number of configurations containing a sub-process with fractions x_1, x_2, y_a, y_b of the corresponding 4-momenta



- $\delta_1, \delta_2, \epsilon_a, \epsilon_b$ are parameters characterizing structure of the colliding objects and fragmentation process, respectively
- $\Omega^{-1}(x_1, x_2, y_a, y_b)$ characterizes resolution at which a constituent subprocess can be singled out of the inclusive reaction

The fractal measure z diverges as the resolution Ω^{-1} increases.

$$z(\Omega)|_{\Omega^{-1}\to\infty}\to\infty$$





Principle of minimal resolution: The momentum fractions x_1, x_2 and y_a, y_b are determined in a way to minimize the resolution Ω^{-1} of the fractal measure z with respect to all constituent sub-processes taking into account 4-momentum conservation law:

$$\Omega = (1 - x_1)^{\delta_1} (1 - x_2)^{\delta_2} (1 - y_a)^{\varepsilon_a} (1 - y_b)^{\varepsilon_b}$$

$$\begin{cases} \partial \Omega / \partial x_1 |_{y_a = y_a(x_1, x_2, y_b)} = 0 \\ \partial \Omega / \partial x_2 |_{y_a = y_a(x_1, x_2, y_b)} = 0 \\ \partial \Omega / \partial y_b |_{y_a = y_a(x_1, x_2, y_b)} = 0 \end{cases}$$

$$M_1, \delta_1$$

$$M_1, \delta_1$$

$$M_2, \delta_2$$

$$M_1, \delta_1$$

$$M_2, \delta_2$$

$$M_1, \delta_1$$

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$$M_1, \delta_1$$

$$M_2, \delta_2$$

$$M_2$$







Scaling function $\Psi(z)$



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The scaling function $\Psi(z)$ is probability density to produce the inclusive particle with the corresponding z.





Self-similarity at RHIC





Self-similarity of particle production with various flavor content.



SQM'15, Dubna, 2015, M.Tokarev

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PRD 19 (1979) 764

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PRD 19 (1979) 764

NPB 100 (1975) 237

PRD 40 (1989) 2777

NPB 100 (1975) 237

NPB 100 (1975) 237

 K^*

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PRC 90 (2014) 054905

PRC 71 (2005) 064902

△ NPB 203 (1982) 27

PRC 84 (2011) 064909

PRC 75 (2007) 064901

PRL 108 (2012) 072302

Recent data from RHIC







$$z = z_0 \Omega^{-1}$$

$$z_0 = \frac{s_{\perp}^{1/2}}{(dN_{ch}/d\eta|_0)^c m_N}$$

$$\Omega = (1 - x_1)^{\delta} (1 - x_2)^{\delta} (1 - y_a)^{\epsilon_F} (1 - y_b)^{\epsilon_F}$$

- > $dN_{ch}/d\eta|_0$ multiplicity density
- c "specific heat" of bulk matter
- > δ proton fractal dimension
- \succ $\epsilon_{\rm F}$ fragmentation fractal dimension

Scaling function

$$\Psi(z) = \frac{\pi}{(dN/d\eta) \cdot \sigma_{inel}} \cdot J^{-1} \cdot E \frac{d^3\sigma}{dp^3}$$



- Energy independence of $\Psi(z)$
- > Centrality independence of $\Psi(z)$
- Power law at high z
- Saturation at low **z**



Universality: the same shape of Ψ both for K⁻ and π^- (solid line)





Constituent level of particle production in terms of

Momentum fraction

Recoil mass

Energy loss $\Delta E/E \sim (1-y_a)$







Momentum fraction
 increases with p_T
 decreases with √s_{NN}

Recoil mass
 increases with p_T
 increases with √s_{NN}

Constituent energy loss ➤ decreases with p_T

▶ increases with $\sqrt{s_{NN}}$







- > $dN_{ch}/d\eta|_0$ multiplicity density
- c "specific heat" of bulk matter
- > δ proton fractal dimension
- > $\epsilon_{\rm F}$ fragmentation fractal dimension

Scaling function

$$\Psi(z) = \frac{\pi}{(dN/d\eta) \cdot \sigma_{inel}} \cdot J^{-1} \cdot E \frac{d^3\sigma}{dp^3}$$



- Energy independence of $\Psi(z)$
- > Centrality independence of $\Psi(z)$
- Power law at high z
- Saturation at low z



Universality: the same shape of Ψ both for K_S^0 and π^- (solid line)





Constituent level of particle production in terms of









- $ightarrow dN_{ch}/d\eta|_0$ multiplicity density
- c "specific heat" of bulk matter
- > δ proton fractal dimension
- > $\epsilon_{\rm F}$ fragmentation fractal dimension

Scaling function

$$\Psi(z) = \frac{\pi}{(dN/d\eta) \cdot \sigma_{inel}} \cdot J^{-1} \cdot E \frac{d^3\sigma}{dp^3}$$

"Collapse" of data onto a single curve



- Energy independence of $\Psi(z)$
- Example to Centrality independence of $\Psi(z)$
- Power law at high z
- Saturation at low z



Universality: the same shape of Ψ both for K^* and π^- (solid line)





Constituent level of particle production in terms of



Recoil mass



Momentum fraction
 increases with p_T
 decreases with √s_{NN}

Recoil mass
 increases with p_T
 increases with √s_{NN}

Energy loss $\Delta E/E \sim (1-y_a)$ 1.2 $p+p\rightarrow K^*(892)+X$ 1.0midrapidity s^{1/2} (GeV) 0.817.3 ya 200 STAR 0.6 0.4 0.2 0.02 6 8 $p_T (GeV/c)$

Constituent energy loss decreases with p_T

▶ increases with $\sqrt{s_{NN}}$







- > $dN_{ch}/d\eta|_0$ multiplicity density
- c "specific heat" of bulk matter
- > δ proton fractal dimension
- \triangleright ϵ_F fragmentation fractal dimension

Scaling function

$$\Psi(z) = \frac{\pi}{(dN/d\eta) \cdot \sigma_{inel}} \cdot J^{-1} \cdot E \frac{d^3\sigma}{dp^3}$$



- Energy independence of $\Psi(z)$
- > Centrality independence of $\Psi(z)$
- Power law at high z
- Saturation at low z



Universality: the same shape of Ψ both for φ and π^- (solid line)





Constituent level of particle production in terms of





Self-similarity of strangeness production in pp

Universality: flavor independence of the scaling function

DUBNA 2015





$K_{S}^{0}, K^{\overline{}}, K^{\ast}, \phi, \Lambda, \Xi, \Omega, \Sigma^{\ast}, \Lambda^{\ast}$

Constituent level of particle production in terms of





Self-similarity dictates the properties of constituent sub-process.





Model parameters: δ , ϵ_F , c

Parameters δ , ϵ_F , c are found from the scaling behavior of Ψ as a function of self-similarity variable z

Proton fractal dimension

Fragmentation dimension





A discontinuity and strong correlation of the model parameters could give indication on new physics in pp collisions: Search for phase transition, critical point with strange probes.





- New data on transverse momentum spectra of strange hadrons produced in p+p collisions at RHIC in mid-rapidity region were analyzed in the z-scaling approach.
- Self-similarity of strangeness production in p+p collisions over a wide kinematical range was found.
- Constituent energy loss as a function of collision energy and transverse momentum of different strange particles was estimated.
- The energy independence of fractal dimensions and "specific heat" was confirmed.

Specific features of constituent sub-process with strange particles found in the z-scaling approach can be sensitive to critical phenomena in Strange Quark Matter created in pp, pA and AA collisions.

Discontinuity of z-scaling parameters would be manifestation of these phenomena .





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Satellite Meetings: Summer School "Dense Matter" 29 June-11 July 2015 Roundtable "Physics at NICA" 5 July 2015

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