



(Multi)-strange hadrons in Pb+Pb collisions and correlations in p+Pb collisions at the LHC

Xiangrong Zhu
(xrongzhu@pku.edu.cn)

Department of Physics and State Key Laboratory of Nuclear Physics and Technology
Peking University, Beijing 100871, P.R. China

Strangeness in Quark Matter 2015
July 06–11, 2015, Dubna, Russia

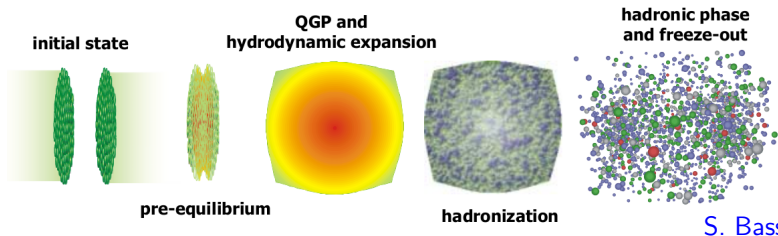
Main references:

- X. Zhu, F. Meng, H. Song, and Y. X. Liu, Phys. Rev. C **91**, no. 3, 034904 (2015).
- Y. Zhou, X. Zhu, P. Li and H. Song, Phys. Rev. C **91**, 064908 (2015).



- Introduction
 - Viscous hydrodynamics
 - Hybrid approaches for heavy-ion collisions
- (Multi-)strange hadrons in Pb+Pb at $\sqrt{s_{NN}}=2.76$ TeV
 - Multiplicities, p_T -spectra and elliptic flow of (multi-)strange hadrons
 - Chemical and thermal freeze-out of various hadrons species
- Correlations in p+Pb collisions at $\sqrt{s_{NN}}=5.02$ TeV
 - Experimental measurements and hydrodynamic calculations
 - Correlations from hadronic cascade model, UrQMD
- Summary

Stages of ultra-relativistic heavy ion collisions



S. Bass

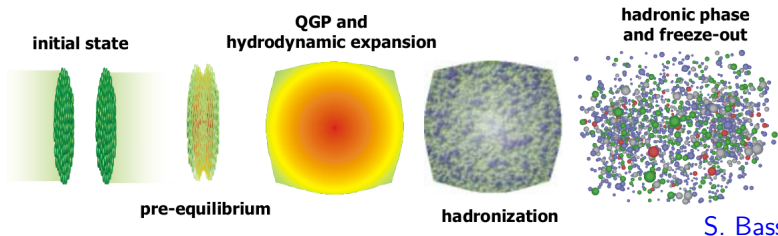
Basics of viscous hydrodynamics

- **Energy momentum tensor** $T^{\mu\nu}(x)$: $\partial_\mu T^{\mu\nu}(x) = 0$
 where $T^{\mu\nu} = [e + p + \Pi]u^\mu u^\nu - (p + \Pi)g^{\mu\nu} + \pi^{\mu\nu}$ with
 - Viscous bulk pressure Π

$$\dot{\Pi} = -\frac{1}{\tau_\Pi}(\Pi + \zeta \partial \cdot u) - \frac{1}{2}\Pi \frac{\zeta T}{\tau_\Pi} \partial_\lambda \left(\frac{\tau_\Pi}{\zeta T} u^\lambda \right)$$
 - Traceless viscous shear pressure tensor $\pi^{\mu\nu}$

$$\Delta^{\alpha\mu} \Delta^{\beta\nu} \dot{\pi}_{\alpha\beta} = -\frac{1}{\tau_\pi}(\pi^{\mu\nu} - 2\eta\sigma^{\mu\nu}) - \frac{1}{2}\pi^{\mu\nu} \frac{\eta T}{\tau_\pi} \partial_\lambda \left(\frac{\tau_\pi}{\eta T} u^\lambda \right)$$
- **Conserved charge current** $N_i^\mu(x)$: $\partial_\mu N_i^\mu(x) = 0$, $i = 1, \dots, k$
 For simplicity, only consider the conserved net baryon number current.

Stages of ultra-relativistic heavy ion collisions



S. Bass

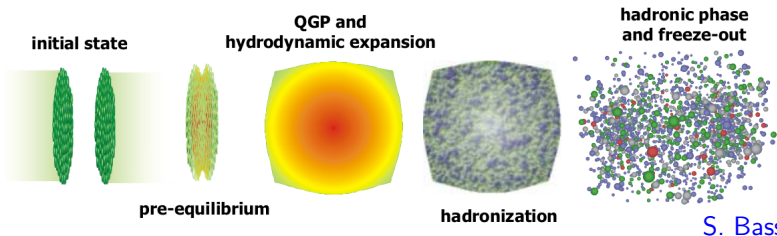
Basics of viscous hydrodynamics

- **Energy momentum tensor $T^{\mu\nu}(x)$:** $\partial_\mu T^{\mu\nu}(x) = 0$
 where $T^{\mu\nu} = [e + p + \Pi]u^\mu u^\nu - (p + \Pi)g^{\mu\nu} + \pi^{\mu\nu}$ with
 - Viscous bulk pressure Π

$$\dot{\Pi} = -\frac{1}{\tau_\Pi}(\Pi + \zeta\partial \cdot u) - \frac{1}{2}\Pi\frac{\zeta T}{\tau_\Pi}\partial_\lambda\left(\frac{\tau_\Pi}{\zeta T}u^\lambda\right)$$
 - Traceless viscous shear pressure tensor $\pi^{\mu\nu}$

$$\Delta^{\alpha\mu}\Delta^{\beta\nu}\dot{\pi}_{\alpha\beta} = -\frac{1}{\tau_\pi}(\pi^{\mu\nu} - 2\eta\sigma^{\mu\nu}) - \frac{1}{2}\pi^{\mu\nu}\frac{\eta T}{\tau_\pi}\partial_\lambda\left(\frac{\tau_\pi}{\eta T}u^\lambda\right)$$
- ~~Conserved charge current $N_i^\mu(x)$: $\partial_\mu N_i^\mu(x) = 0$, $i = 1, \dots, k$~~
 For simplicity, only consider the conserved net baryon number current.
 Assume **zero net baryon density** at the LHC.

Stages of ultra-relativistic heavy ion collisions



S. Bass

Basics of viscous hydrodynamics

- **Energy momentum tensor** $T^{\mu\nu}(x)$: $\partial_\mu T^{\mu\nu}(x) = 0$
 where $T^{\mu\nu} = [e + p + \Pi]u^\mu u^\nu - (p + \Pi)g^{\mu\nu} + \pi^{\mu\nu}$ with

- Viscous bulk pressure Π

$$\dot{\Pi} = -\frac{1}{\tau\Pi}(\Pi + \zeta\partial\cdot u) - \frac{1}{2}\Pi\frac{\zeta T}{\tau\Pi}\partial_\lambda\left(\frac{\tau\Pi}{\zeta T}u^\lambda\right)$$

- Traceless viscous shear pressure tensor $\pi^{\mu\nu}$

$$\Delta^{\alpha\mu}\Delta^{\beta\nu}\dot{\pi}_{\alpha\beta} = -\frac{1}{\tau\pi}(\pi^{\mu\nu} - 2\eta\sigma^{\mu\nu}) - \frac{1}{2}\pi^{\mu\nu}\frac{\eta T}{\tau\pi}\partial_\lambda\left(\frac{\tau\pi}{\eta T}u^\lambda\right)$$

- ~~Conserved charge current $N_i^\mu(x)$: $\partial_\mu N_i^\mu(x) = 0$, $i = 1, \dots, k$~~

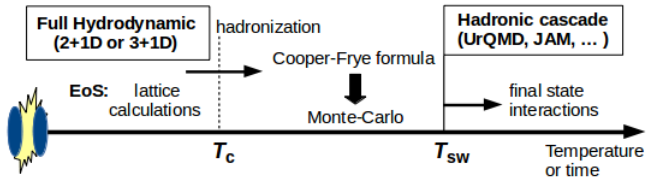
For simplicity, only consider the conserved net baryon number current.

Assume **zero net baryon density** at the LHC.

Input EoS $p(e, n)$
for closure

Hybrid approaches

Hydrodynamic+hadronic cascade hybrid approach



- **VISHNU hybrid approach:**

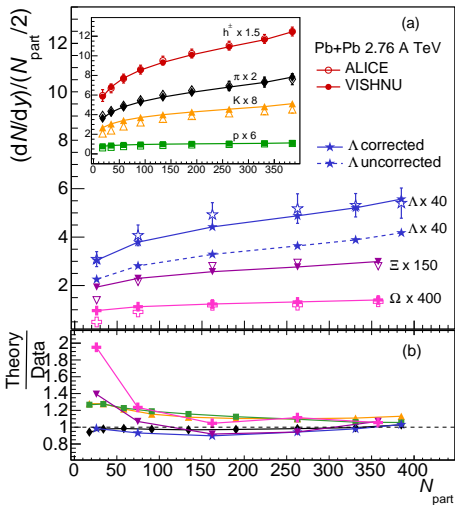
- **Initial conditions:** MC-Glauber, MC-KLN (this work)
- **Hydrodynamic:** VISH2+1, $\eta/s = 0.16$, and **EoS:** s95p-PCE
- **Switching temperature:** $T_{sw} = 165\text{MeV}$
- **Hadronic cascade:** UrQMD, hadronic rescattering and resonance decays

- **Other hybrid approaches:**

- D. Teaney, J. Lauret and E. V. Shuryak, nucl-th/0110037.
- C. Nonaka and S. A. Bass, Phys. Rev. C **75**, 014902 (2007).
- T. Hirano *et al.*, Phys. Lett. B **636**, 299 (2006).
- H. Petersen *et al.*, Phys. Rev. C **78**, 044901 (2008).
- K. Werner *et al.*, Phys. Rev. C **82**, 044904 (2010).
- ...

Multiplicities, spectra and elliptic flow for (multi-)strange hadrons

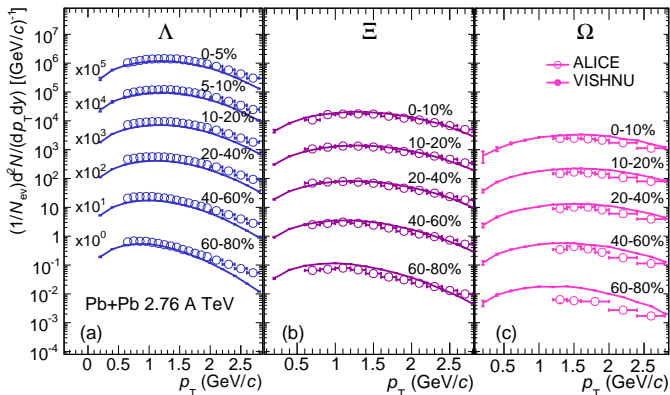
Multiplicities for identified hadrons in Pb-Pb collisions



- With baryon-antibaryon ($B\bar{B}$) annihilations
 - Reduce dN_p/dy and $dN_{\bar{p}}/dy$ by $\mathcal{O}(30\%)$.
H. Song *et al.*, PRC (2014).
- Λ results
 - ALICE results: contaminated by the feed-down decays of Σ^0 and $\Sigma(1385)$.
 - Λ corrected (solid line): summed weak decays from $\Sigma^0 \rightarrow \Lambda + \gamma$.
 - Λ uncorrected (dashed line): no weak decays of Σ^0 .
- VISHNU nicely describes the multiplicities for various hadrons species at most centrality bins.

X. Zhu, F. Meng, H. Song, and Y. X. Liu, PRC 2015.

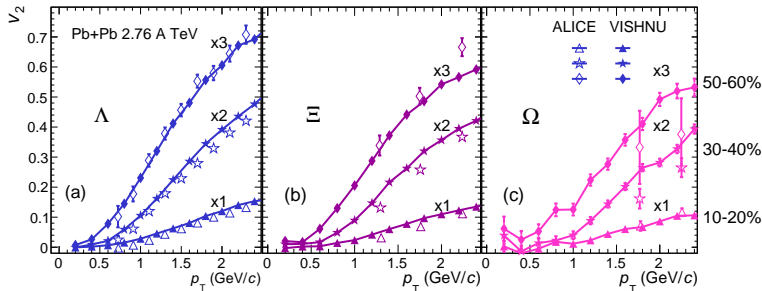
p_T -spectra for Λ , Ξ , and Ω in Pb-Pb collisions



X. Zhu, F. Meng, H. Song, and Y. X. Liu, PRC 2015.

- Λ results from VISHNU are without weak decays, $\sim 30\%$ lower than the experimental measurements with weak decay contaminations.
- VISHNU nicely fits the slope of the spectra for Λ , Ξ , and Ω and at various centralities.

Elliptic flow for Λ , Ξ , and Ω in Pb-Pb collisions

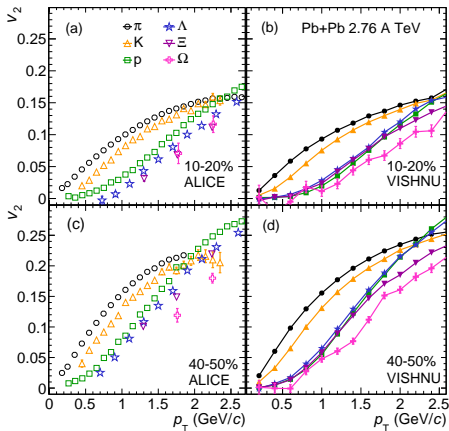


X. Zhu *et al.*, *Phys. Rev. C* **91**, no. 3, 034904 (2015).

- Below 2 GeV, v_2 for Λ , Ξ , and Ω are fairly well described by VISHNU within the statistical error bars.
- Above 2 GeV, the descriptions of v_2 for Ξ at 50-60% and Ω for at 30-40% and 50-60% become worse.

Mass ordering of elliptic flow for identified hadrons

X. Zhu, F. Meng, H. Song, and Y. X. Liu, PRC 2015.



- VISHNU nicely describes the mass ordering among π , K , p , and Ω .
- VISHNU fails to describe the mass ordering among p , Λ and Ξ .
- VISHNU slightly under-predicts the proton v_2 below 2 GeV, leading to inverse mass ordering between p and Λ .

Initial flow could enhance the radial flow

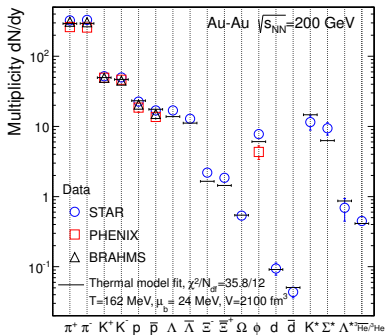
Improvement?

- An initial flow is expected to improve the description of mass ordering.
- UrQMD hadronic cross sections also need to be reevaluated and improved.

Chemical and thermal freeze-out for identified hadrons

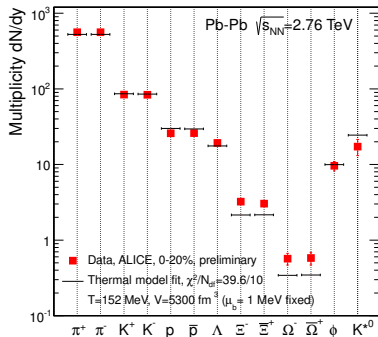
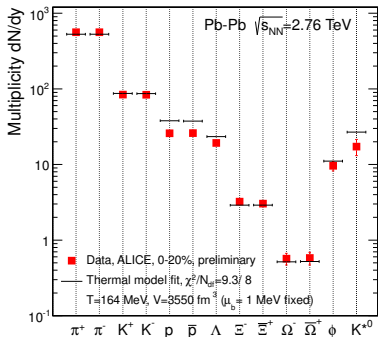
- **Chemical freeze-out:** hadron multiplicity no longer changes—termination of inelastic collisions.
- **Thermal freeze-out:** hadron momentum is fixed—end of elastic collisions.

Proton "puzzle" from statistical hadronization model



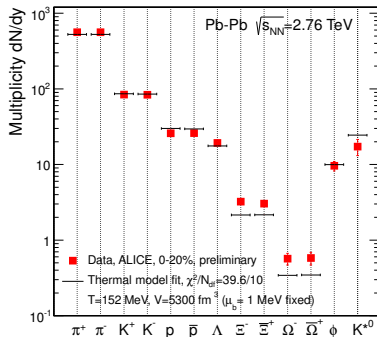
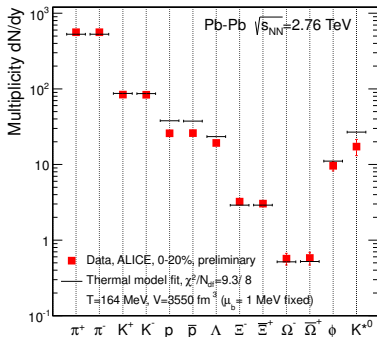
- **Statistical model:**
 - three parameters
 - Chemical freeze-out temperature T
 - Baryo-chemical potential μ_b
 - Fireball volume V
- Temperature is about 162 MeV at 200 GeV.

Proton “puzzle” from statistical hadronization model



- Excluding p/\bar{p} , other data can be described by a temperature of 164 MeV.
- A good description of the p/\bar{p} data with T around 150 MeV.
- This temperature results into the yield of Λ and Ω is under-predicted.

Proton “puzzle” from statistical hadronization model



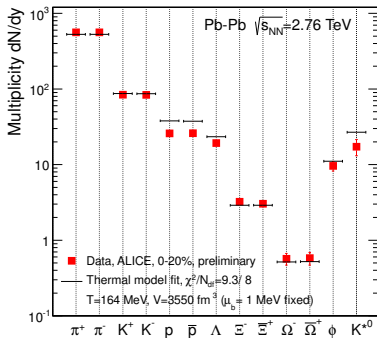
- Excluding p/\bar{p} , other data can be described by a temperature of 164 MeV.
- A good description of the p/\bar{p} data with T around 150 MeV.
- This temperature results into the yield of Λ and Ω is under-predicted.

How about the result from VISHNU?

Proton "puzzle" from statistical hadronization model

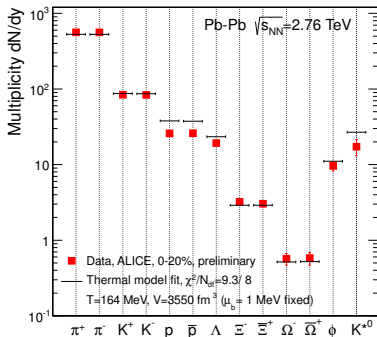


Statistical Model

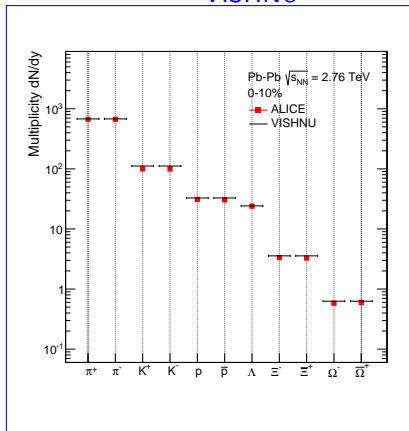


Proton “puzzle” from statistical hadronization model

Statistical Model



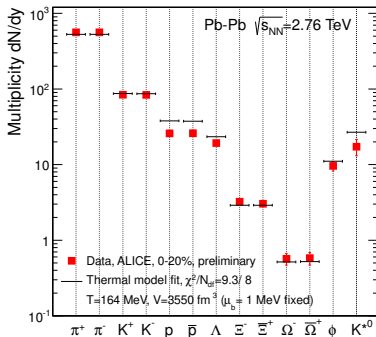
VISHNU



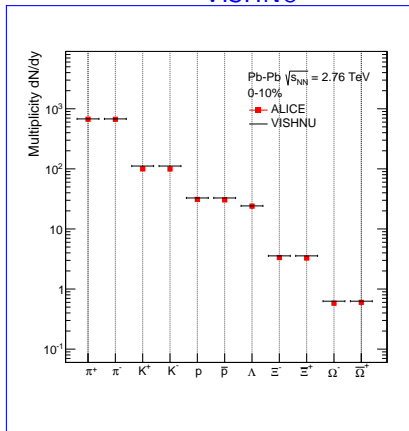
- Excluding p/\bar{p} , other data can be described by a temperature of 164 MeV.
- A good description of the p/\bar{p} data with T around 150 MeV.
- **VISHNU** gives a nice description of all hadrons.

Proton “puzzle” from statistical hadronization model

Statistical Model



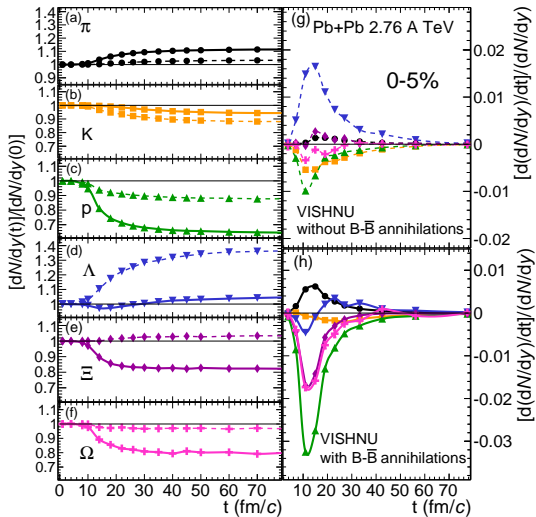
VISHNU



- Excluding p/\bar{p} , other data can be described by a temperature of 164 MeV.
- A good description of the p/\bar{p} data with T around 150 MeV.
- **VISHNU** gives a nice description of all hadrons.

It is significant to further investigate the freeze-out with the hybrid model.

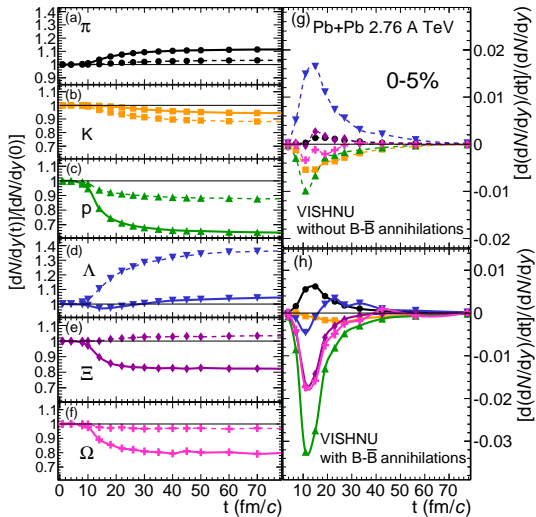
Chemical freeze-out for identified hadrons (I)



- With and without $B\bar{B}$ annihilations.
- **Method:** define different times of the calculation and output in UrQMD.
 - ▶ Left panels: the ratio of multiplicity density at t to at $t = 0$ fm/c.
 - ▶ Right panels: the change rate of multiplicity density scaled by the multiplicity density at t .

X. Zhu, F. Meng, H. Song, and Y. X. Liu, PRC 2015.

Chemical freeze-out for identified hadrons (II)

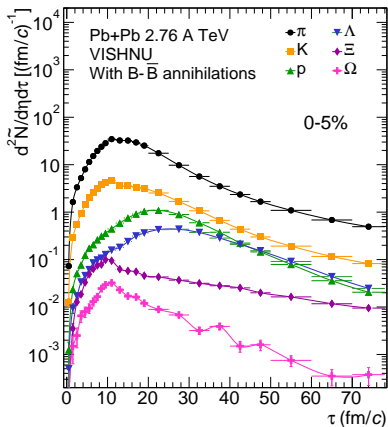


- With $B\bar{B}$ annihilations
 - ◆ influence baryons
 - $\Rightarrow \sim 30\%$ reductions for p ,
 - $\sim 20\%$ reductions for Λ , and Ω .
- With and without $B\bar{B}$
 - ◆ Ξ and Ω experience earlier chemical freeze-out.
- Different hadrons may have different effective chemical freeze-out temperature.

X. Zhu, F. Meng, H. Song, and Y. X. Liu, PRC 2015.

Further analysis of **effective chemical freeze-out** T , is needed to do when the UrQMD is updated to record more intermediate evolution information.

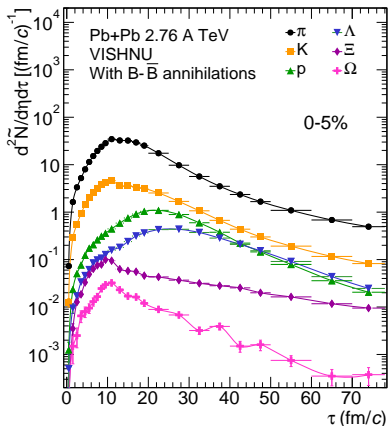
Thermal freeze-out for identified hadrons (I)



- Only with $B-\bar{B}$ annihilations
- **Thermal freeze-out time:** time of last elastic collision or decay for various hadrons species.

X. Zhu, F. Meng, H. Song, and Y. X. Liu, PRC 2015.

Thermal freeze-out for identified hadrons (II)



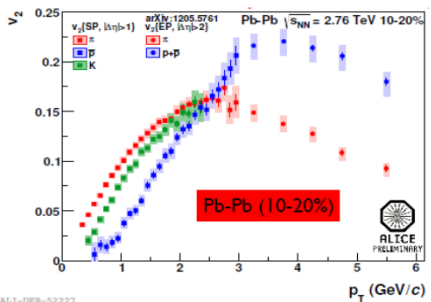
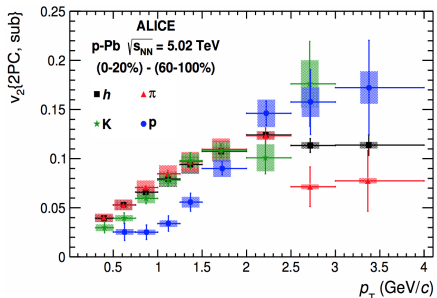
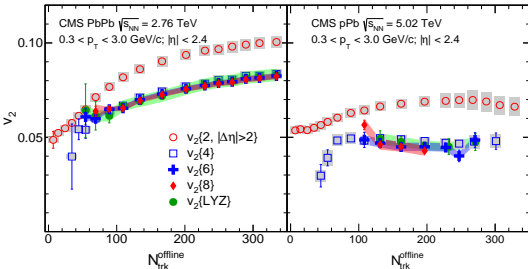
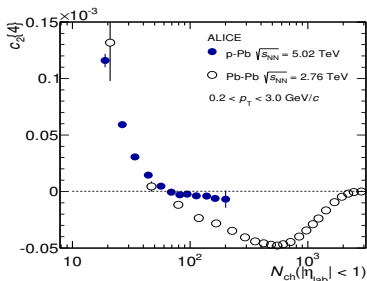
- The peaks of Ξ and Ω are located around 10 fm/c.
- The peaks of p and Λ are shifted to 20-30 fm/c.
 ⇒ Multistrange hadrons experience earlier thermal freeze-out.
- Freeze-out time distributions of π and K spread widely along the time axis.
 ⇒ Meson species still suffer hadronic scattering even during the late stage.

X. Zhu, F. Meng, H. Song, and Y. X. Liu, PRC 2015.

- Thermal freeze-out is strongly hadron species dependent.
- Multistrange hadrons Ξ and Ω experience earlier thermal freeze-out, as expected, due to their much smaller hadronic cross sections.

Correlations in p+Pb collisions at $\sqrt{s_{NN}}=5.02$ TeV

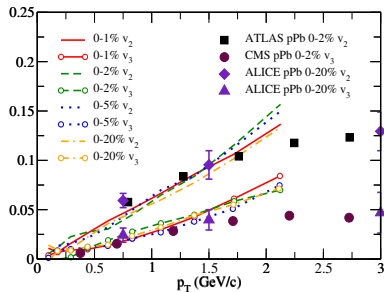
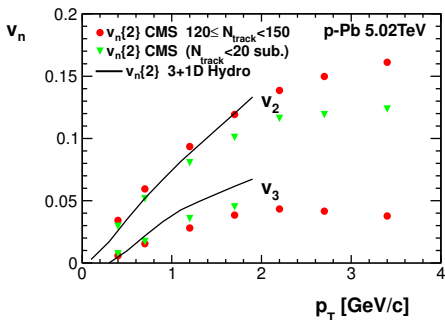
Collective flow in p+Pb? – Experimental Observations



ALICE Collaboration, PRC (2014), PLB (2013); CMS Collaboration PRL (2015)

Collective flow in p+Pb? – Hydrodynamics simulations

Elliptic and triangular flow from 3+1-dimensional hydrodynamics



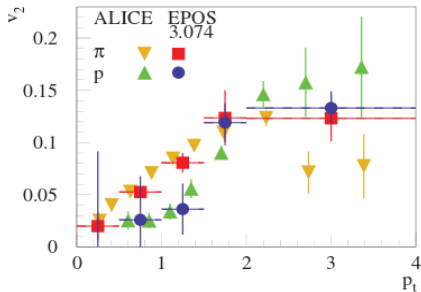
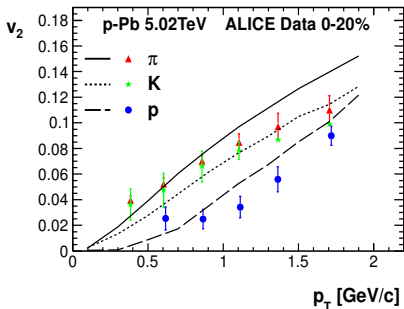
• P. Božek *et al.*, NPA **926**, 16 (2014).

• G. Y. Qin *et al.*, PRC **89**, 044902 (2014).

Collective flow in p+Pb? – Hydrodynamics simulations



Mass ordering of v_2 for π , K , and p



• P. Božek *et al.*, NPA **926**, 16 (2014).

• K. Werner, *et al.*, PRL **112**, 232301 (2014).

- Where does the correlations (collective flow) in 5.02 TeV p+Pb collisions come from?
 - Initial State or/and QGP?
- Is it possible to generate such flow-like correlations through pure hadronic interaction?

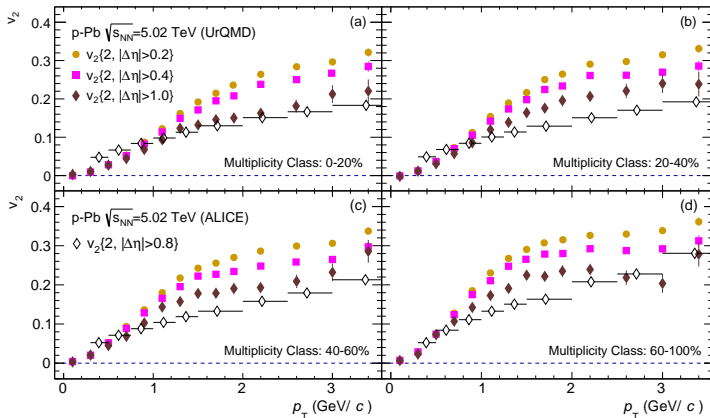
UrQMD Baseline Calculations

Y. Zhou, X. Zhu, P. Li and H. Song, Phys. Rev. C **91**, 064908 (2015).

Assumption:

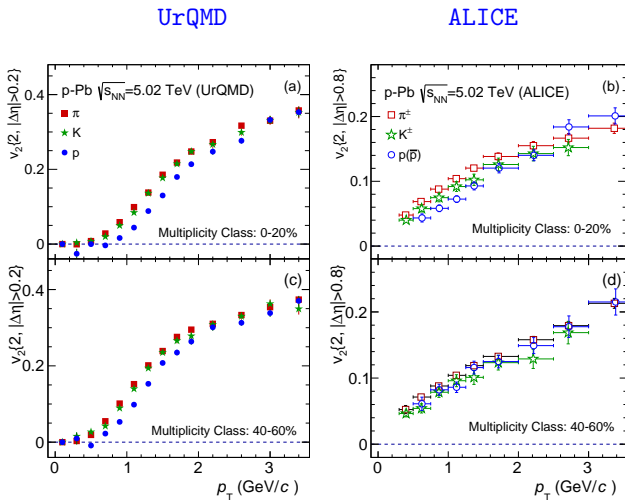
p+Pb collisions only produce hadronic systems without reach the threshold of the QGP formation

$v_2(p_T)$ in p+Pb collisions at 5.02 TeV



- Multi-particle cumulant method. [Y. Zhou et al, PRC 91, 064908 \(2015\)](#)
- Sizeable values of $v_2\{2\}$ with different pseudorapidity gap cuts.
- With large pseudo-rapidity gap cuts, $v_2\{2\}$ from UrQMD is comparable to the experimental data

$v_2(p_T)$ mass ordering in p+Pb collisions at 5.02 TeV



Y. Zhou *et al*, PRC **91**, 064908 (2015)

- Remarkable mass ordering is produced by UrQMD like ALICE data, but with larger magnitude.

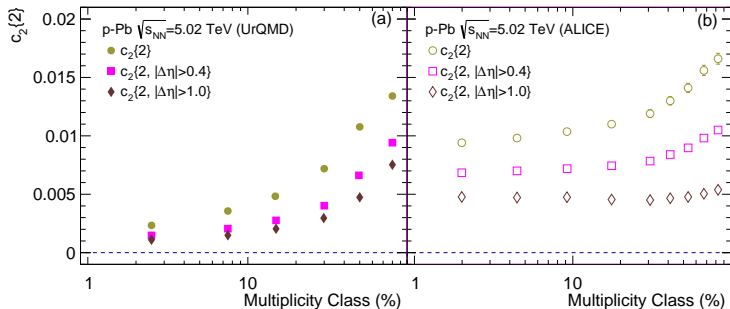
Does the Hadronic p+Pb system really flow?

Does the Hadronic p+Pb system really flow?

Check with the multi-particle method

- $v_n\{2\} = \sqrt{c_n\{2\}} \Rightarrow$ 2-particle cumulant should be **positive**.
- $v_n\{4\} = \sqrt[4]{-c_n\{4\}} \Rightarrow$ 4-particle cumulant should be **negative**.

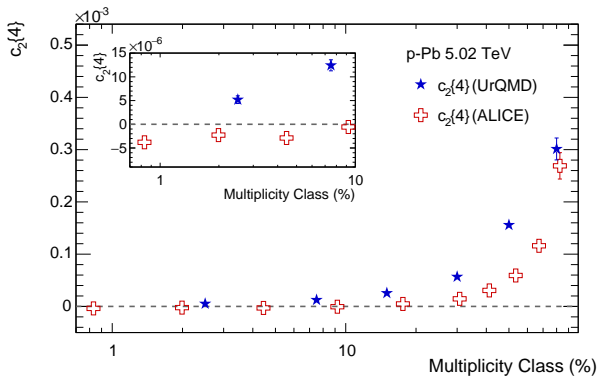
Multi-particle cumulants of v_2 from UrQMD



Y. Zhou *et al*, PRC **91**, 064908 (2015)

- 2-particle cumulant of v_2 : $c_2\{2\} = \langle\langle 2 \rangle\rangle = \langle\langle e^{i2(\phi_1 - \phi_2)} \rangle\rangle = \langle v_2^2 + \delta_2^2 \rangle$
- The UrQMD systems are largely influenced by non-flow effects
- Non-flow effects: $\delta \sim 1/M$, M multiplicity in one event
- $c_2\{2\}$ is **positive**.

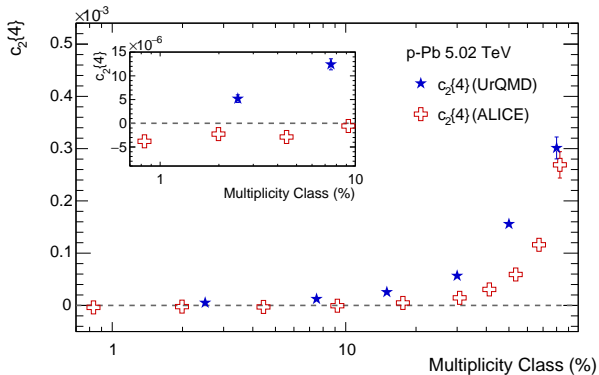
Multi-particle cumulants of v_2 from UrQMD



Y. Zhou *et al*, PRC **91**, 064908 (2015)

- ALICE results of $c_2\{4\}$ becomes negative when centrality $< 10\%$.
- But, $c_2\{4\}$ of UrQMD keeps **positive** at all centrality bins.

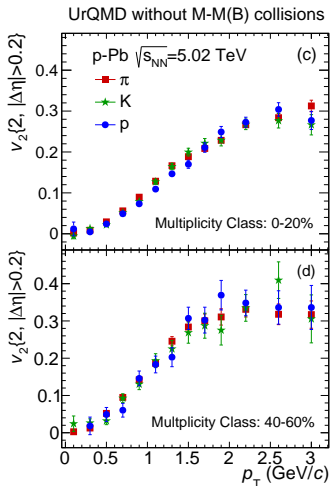
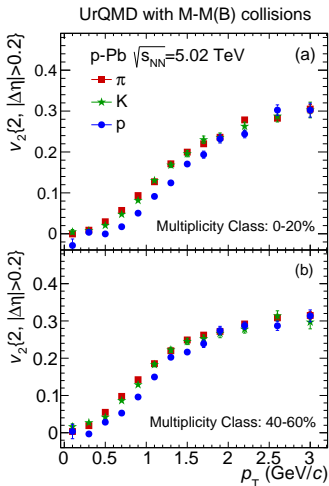
Multi-particle cumulants of v_2 from UrQMD



Y. Zhou *et al*, PRC **91**, 064908 (2015)

- ALICE results of $c_2\{4\}$ becomes negative when centrality $< 10\%$.
- But, $c_2\{4\}$ of UrQMD keeps **positive** at all centrality bins.
- **UrQMD simulations for p+Pb collisions can not generate the collective flow!**
- In p+Pb collisions, effects from initial state and/or QGP are needed to generate collective.

Where is the mass ordering from?



Y. Zhou *et al*, PRC 91, 064908 (2015)

- Hadronic interaction can generate a mass ordering for 2-particle correlations.
- Some unknown cross sections are calculated by the **additive quark model**
 \Rightarrow cross sections of meson-baryon are $\sim 50\%$ larger than meson-meson.

- **Multiplicity, spectra, and elliptic flow for (multi-)strange hadrons**
 - VISHNU gives nice description of the multiplicity, spectra and elliptic flow in most of centrality bins.
 - VISHNU nicely describes the mass ordering among π , K , p , and Ω , but fails among p , Λ and Ξ .
- **Chemical and thermal freeze-out**
 - Ξ and Ω experience earlier chemical freeze-out.
 - Thermal freeze-out is strongly hadron species dependent.
 - Ξ and Ω also experience earlier thermal freeze-out, as expected, due to their much smaller hadronic cross sections.
- **Correlations in p+Pb collisions**
 - Experimental results strongly indicate the development of collective flow.
 - Hydrodynamics semi-quantitatively reproduce these experimental data
 - UrQMD simulations shows hadronic interactions can not produce flow data measured in experiments; effects from initial state and /or QGP are needed
 - v_2 mass-ordering is observed in UrQMD, which is the consequence of hadronic interactions and not necessarily associated with strong fluid-like expansions.

- **Multiplicity, spectra, and elliptic flow for (multi-)strange hadrons**
 - VISHNU gives nice description of the multiplicity, spectra and elliptic flow in most of centrality bins.
 - VISHNU nicely describes the mass ordering among π , K , p , and Ω , but fails among p , Λ and Ξ .
- **Chemical and thermal freeze-out**
 - Ξ and Ω experience earlier chemical freeze-out.
 - Thermal freeze-out is strongly hadron species dependent.
 - Ξ and Ω also experience earlier thermal freeze-out, as expected, due to their much smaller hadronic cross sections.
- **Correlations in p+Pb collisions**
 - Experimental results strongly indicate the development of collective flow.
 - Hydrodynamics semi-quantitatively reproduce these experimental data
 - UrQMD simulations shows hadronic interactions can not produce flow data measured in experiments; effects from initial state and /or QGP are needed
 - v_2 mass-ordering is observed in UrQMD, which is the consequence of hadronic interactions and not necessarily associated with strong fluid-like expansions.

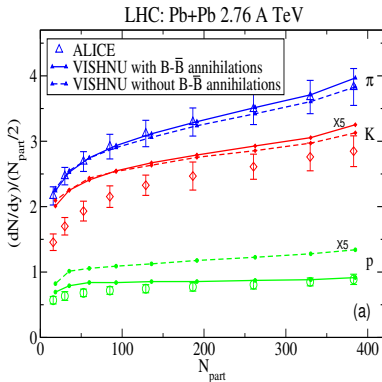
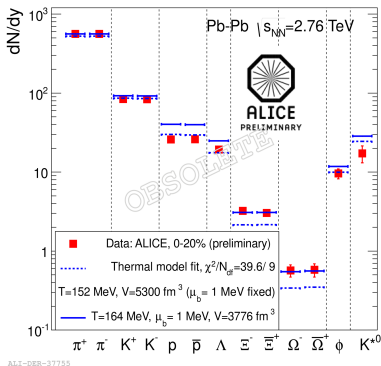
Thanks for your attention!

Backup

Baryon-antibaryon annihilations influence

A. Andronic et al., Nucl. Phys. A 904-905, 535c (2013).

H. Song et al., PRC 89, no. 3, 034919 (2014).

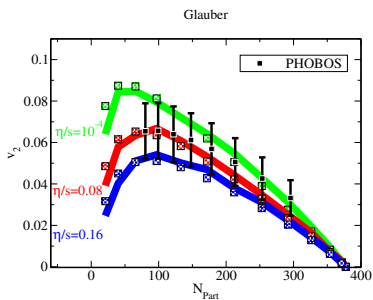
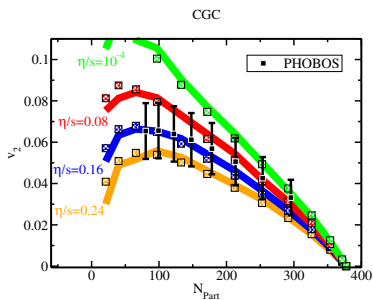


- **Statistical Model** does not include Baryon-antibaryon ($B-\bar{B}$) annihilations!
- $B-\bar{B}$ annihilations mainly reduce dN_p/dy and $dN_{\bar{p}}/dy$ by $\mathcal{O}(30\%)$.

$B-\bar{B}$ annihilations play an important role for a nice fit of the proton data.

η/s from viscous hydrodynamics

Specific shear viscosity η/s (how “perfect” is the created matter)

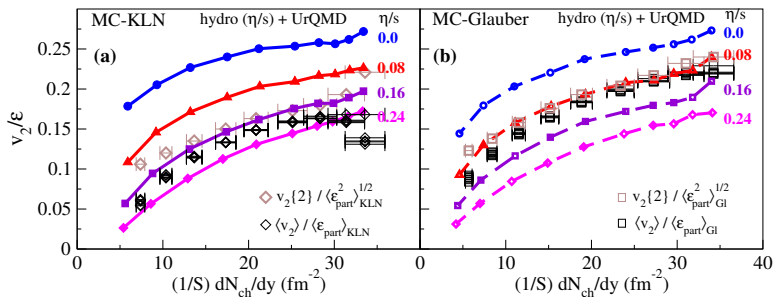


M. Luzum and P. Romatschke, Phys. Rev. C **78**, 034915 (2008).

- The mean value of η/s extracted is very small but existence.
- **No** finite chemical potential, bulk viscosity, heat flow, **hadron cascades**, three-dimensional fluid dynamic effects.

η/s from hybrid approaches

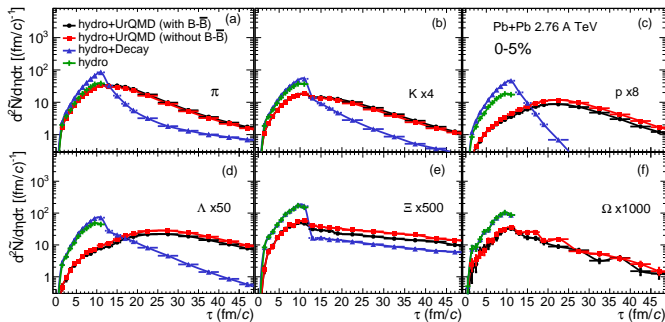
Specific shear viscosity η/s (how “perfect” is the created matter)



H. Song *et al.*, *Phys. Rev. Lett.* **106**, 192301 (2011).

- v_2/ϵ only depends on the viscosity.
- η/s is estimated at $1 < 4\pi(\eta/s) < 2.5$.

Thermal freeze-out for identified hadrons

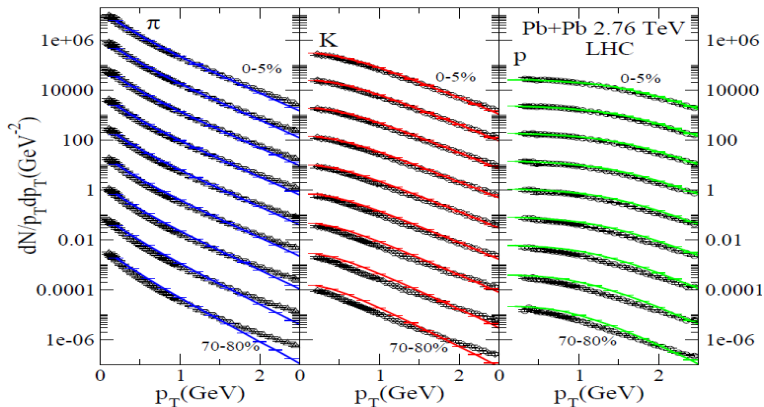


For comparisons, four simulations, **hydro**, **hydro+Decay**, **hydro+UrQMD with and without $B-\bar{B}$** , are done.

1. **hydro**: thermal freeze-out time distributions for all hadrons stop ~ 10 fm/c.
2. **hydro+Decay**: resonance decays \Rightarrow **remarkable enhancement for π and p before 10 fm/c** and **a long tail for π , K , p , Λ and Ξ after 10 fm/c**.
3. **hydro+UrQMD**: UrQMD hadronic scatterings broaden thermal freeze-out time distributions of all hadron species.

What is the difference among all particle species in **hydro+UrQMD**? **Please see next ...**

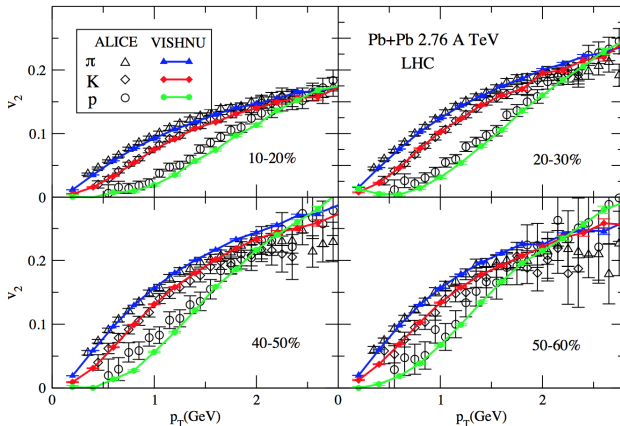
p_T -spectra for π , K , and p in Pb-Pb collisions



H. Song *et al.*, PRC **89**, no. 3, 034919 (2014).

VISHNU hybrid model gives a good description of spectra for π , K , and p at central and semi-central collisions.

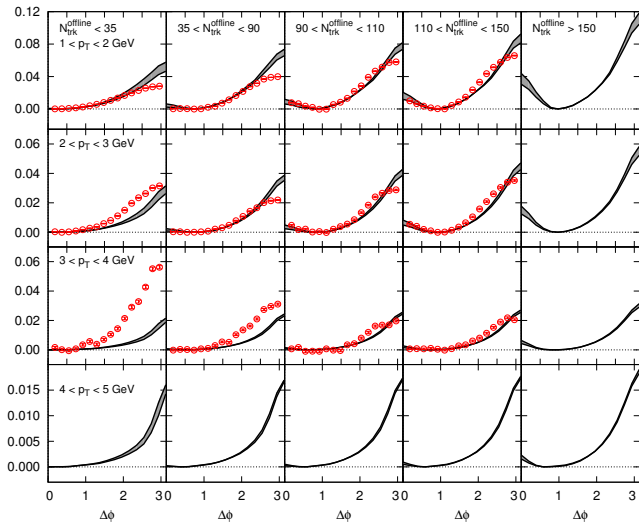
Elliptic flow for π , K , and p in Pb-Pb collisions



H. Song *et al.*, PRC **89**, no. 3, 034919 (2014).

- VISHNU gives a good description of elliptic flow data for π , K and p .

Correlations from Initial States



K. Dusling and R. Venugopalan, Phys. Rev. D **87**, no. 9, 094034 (2013)