

QUASI-DEUTERON CLUSTERS IN THE ^{12}C AND SHORT-RANGE NN CORRELATIONS IN THE REACTION $^{12}\text{C}+p\rightarrow^{10}\text{A}+pp+N$

Yu.N. UZIKOV (DLNP, JINR)

- Cold dense baryonic matter in nuclei
- $^{12}\text{C}(p, pd)^{10}\text{B}$ and $p\langle pn\rangle\rightarrow dp$, $pd\rightarrow\{pp\}_s n$
- Elements of formalism for $p+^{12}\text{C}\rightarrow p+p+N+^{10}\text{B}$ (BM@N)
- SRC **c.m. momentum** distribution and **pp/pn** ratio
- ISI@ FSI
- Conclusion

- ◆ Dubna, 1957, L.S. Azhgirey, ..., **M.G. Mesheryakov** et al. ZHETF, **33**
 $p+^{12}\text{C} \rightarrow d+X$ at 670 MeV:

quasi-elastic knock-out of fast deuteron clusters:

D.I. Blokhintsev (1957) - [fluctuations of nuclear density](#);

[fluctons](#) (6q) in nuclei - **A.V. Efremov** (1976);

SRC –Short Range Correlations **M. Strikman, L. Frankfurt (1978)**

NN-pair with almost zero c.m. momentum but large (equal) internal momenta $q_1 = -q_2$; at short distances $r_{\text{NN}} < 0.5$ fm

with high relative momentum $q > 1/r_{\text{NN}} = 0.4$ GeV/c;

Repulsive NN-core \rightarrow high-momentum part of the w.f. of NN pair

- ◆ **A.M. Baldin**, Cumulative effect (1971).

- ◆ Search for high-momentum components of the nuclear wave functions

- ◆ Intensive study of SRC in nuclei during last one-two decades using mainly electron beams (e,ep), (e,epp).

The Main Results:

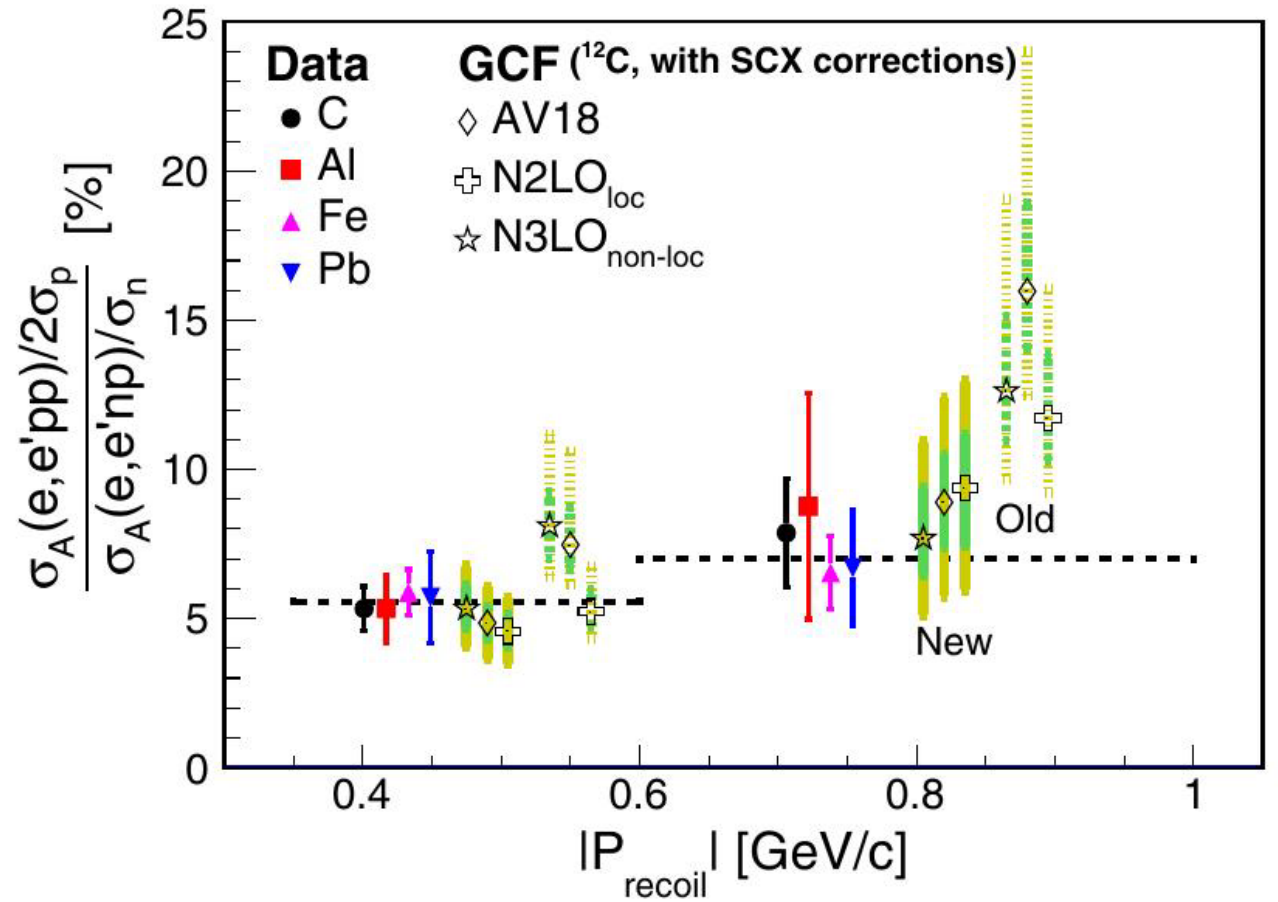
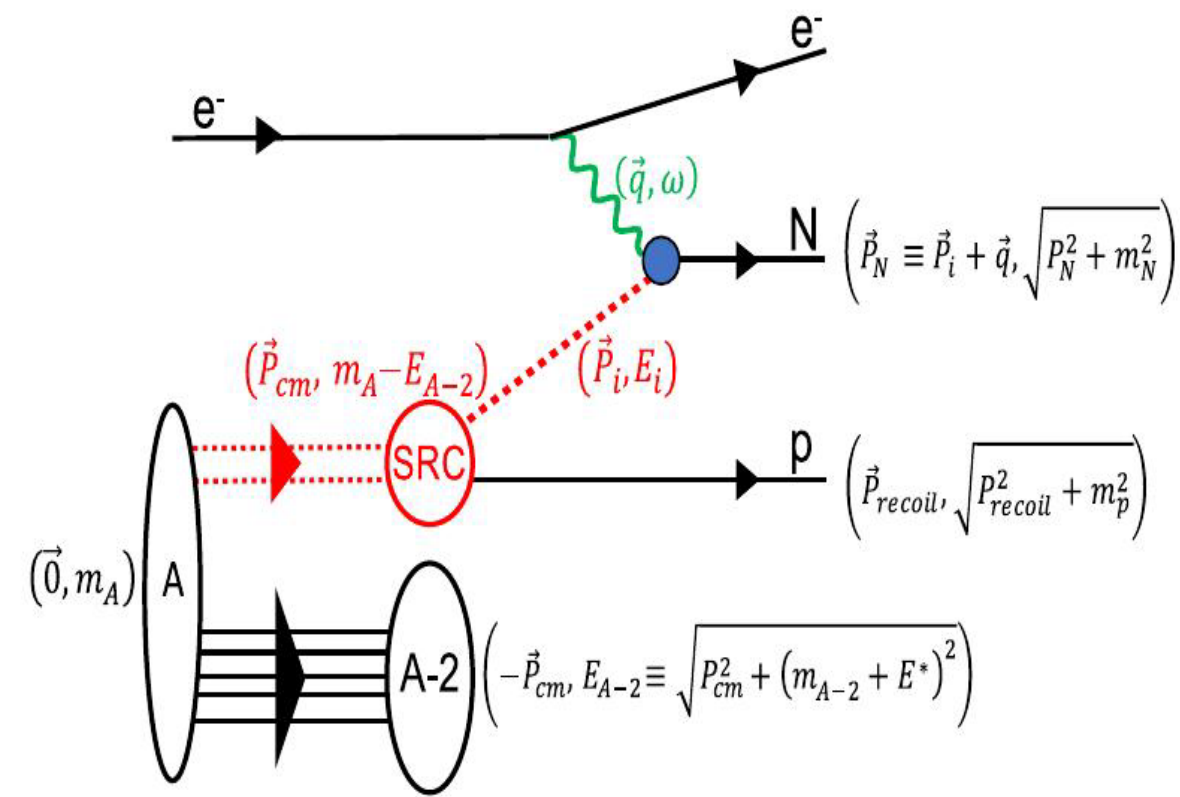
- * High-momentum part of the nucleon momentum distribution ($q > p_F \sim 250-300 \text{ MeV}/c$) accounts for 20% nucleons.
- * pn- SRC pairs dominate by factor of ~ 20 as compared to pp and nn due to the tensor forces.
- * Factorization at high q : $n(p_1, p_2) = n_{c.m.}^A(k_{cm})n_{rel}(q)$
- * SRC are connected with neutrino-nucleus interaction, neutron stars structure, modification of the bound nucleon structure (**EMC effect**).

Cioffi degli Atti, Phys. Rep. 590 (2015) 1

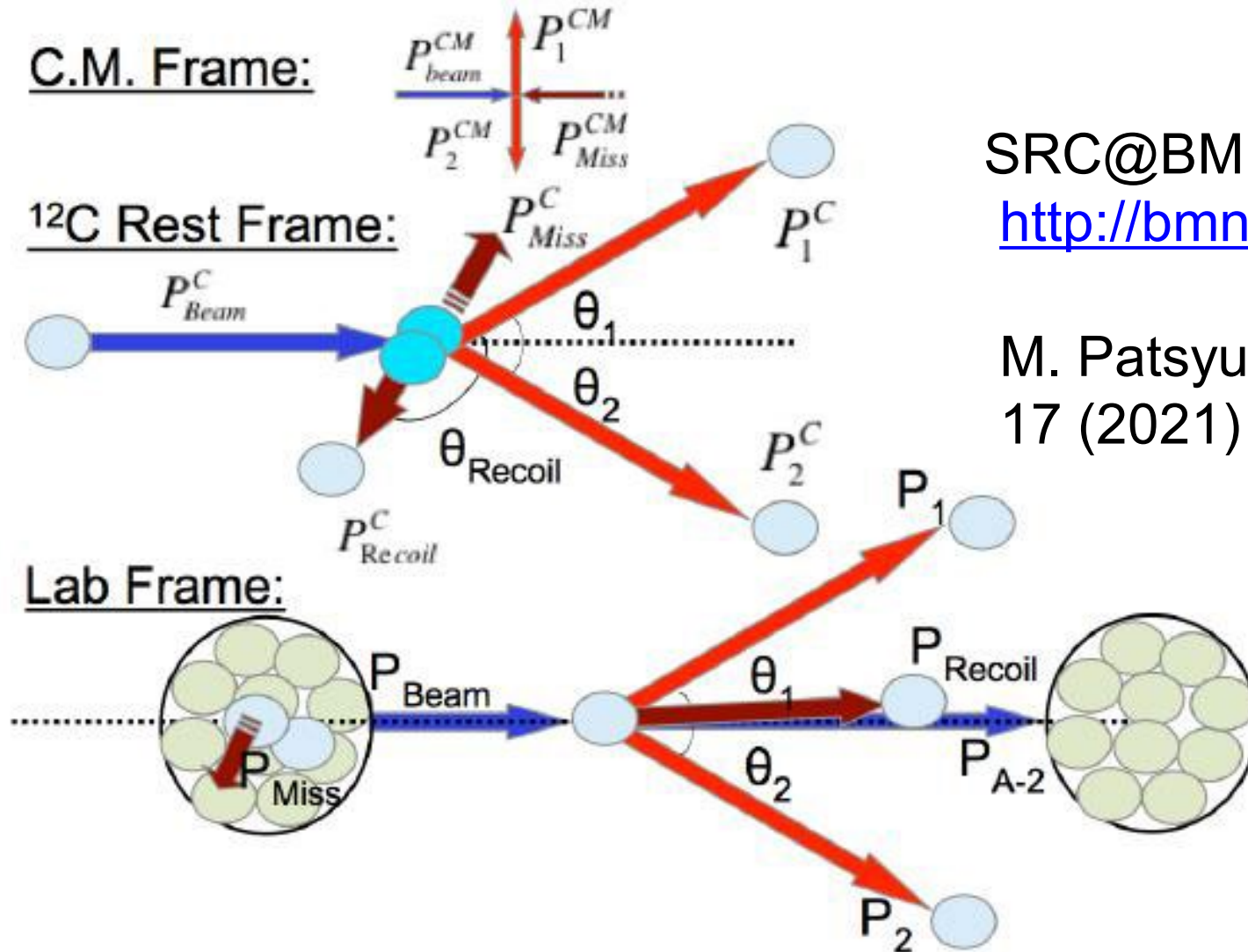
O. Hen et al. Rev. Mod. Phys. 89 (2017) 045002.

M.Duer et al. PRL 122 (2019) 172502 (CLAS Collaboration)

$E_e = 5$ GeV,
 $A(e, e'np), A(e, e'pp)$



Project of **BM@N** to study SRC in JINR with 4=GeV/c /nucleon beam of ^{12}C and proton target in Inverse kinematics . **Talk by Maria Patsyuk today**



SRC@BMN proposal

<http://bmnshift.jinr.ru/wiki/doku.pho>

M. Patsyuk et al., Nature Phys.

17 (2021) 693; arXiv:2102.02626 [nucl-ex]

$^{12}\text{C}(p,2p)^{11}\text{B}$ (g.s.), shell model is OK!

$^{12}\text{C}(p,2pN)^{10}\text{A}$, SCR:

10B 23events (pn);

10Be – 2 event (pp)

CONCLUSION: unperturbed by
ISI@FSI distributions are measured

Quasi-elastic knockout of fast deuteron clusters $^{12}\text{C}(p, pd)^{10}\text{B}$ and hard $pd \rightarrow dp$

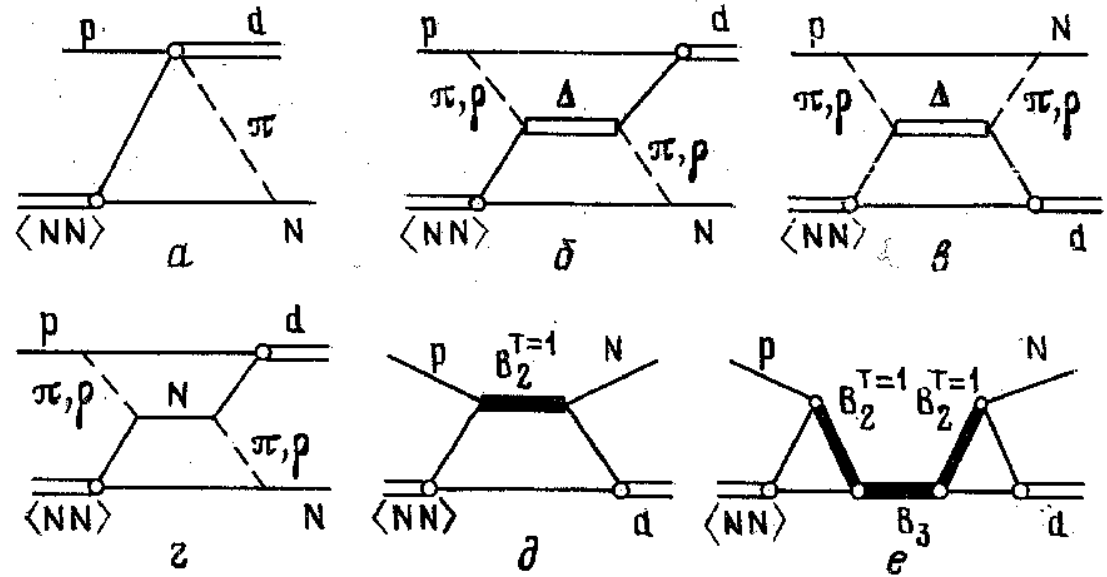
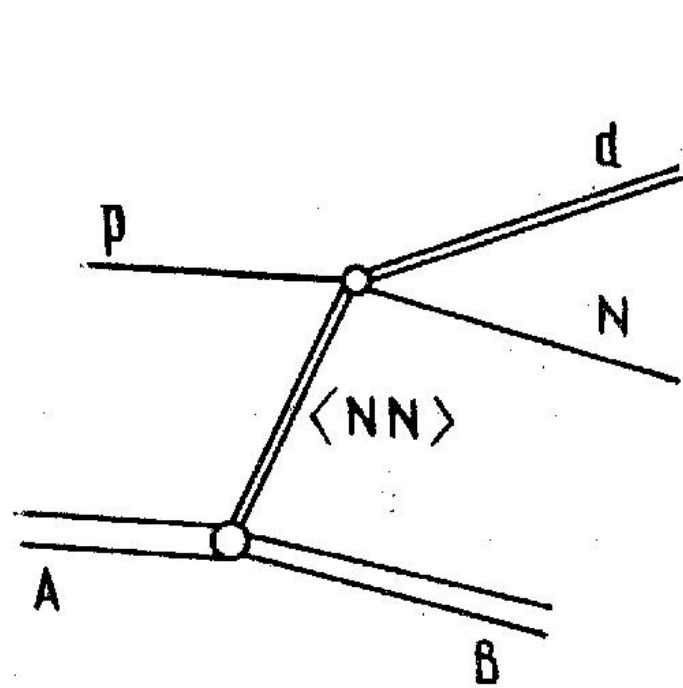


Рис. 5.6: Рис.3 . Механизмы процесса $p \langle NN \rangle \rightarrow Nd$, для которых выполняется соотношение $d\sigma(p \langle np \rangle_{T=0} \rightarrow pd) = 9d\sigma(p \langle np \rangle_{T=1} \rightarrow pd)$.

$$p + \langle np \rangle_{T=0} \rightarrow p + d,$$

$$p + \langle np \rangle_{T=1} \rightarrow p + d,$$

$$p + \langle nn \rangle_{T=1} \rightarrow n + d.$$

$$R = d\sigma(p, nd)/d\sigma(p, pd)$$

Таблица 5.3.2. Отношение дифференциальных сечений
 $[d\sigma(p, nd)/d\sigma(p, pd)]10^2$

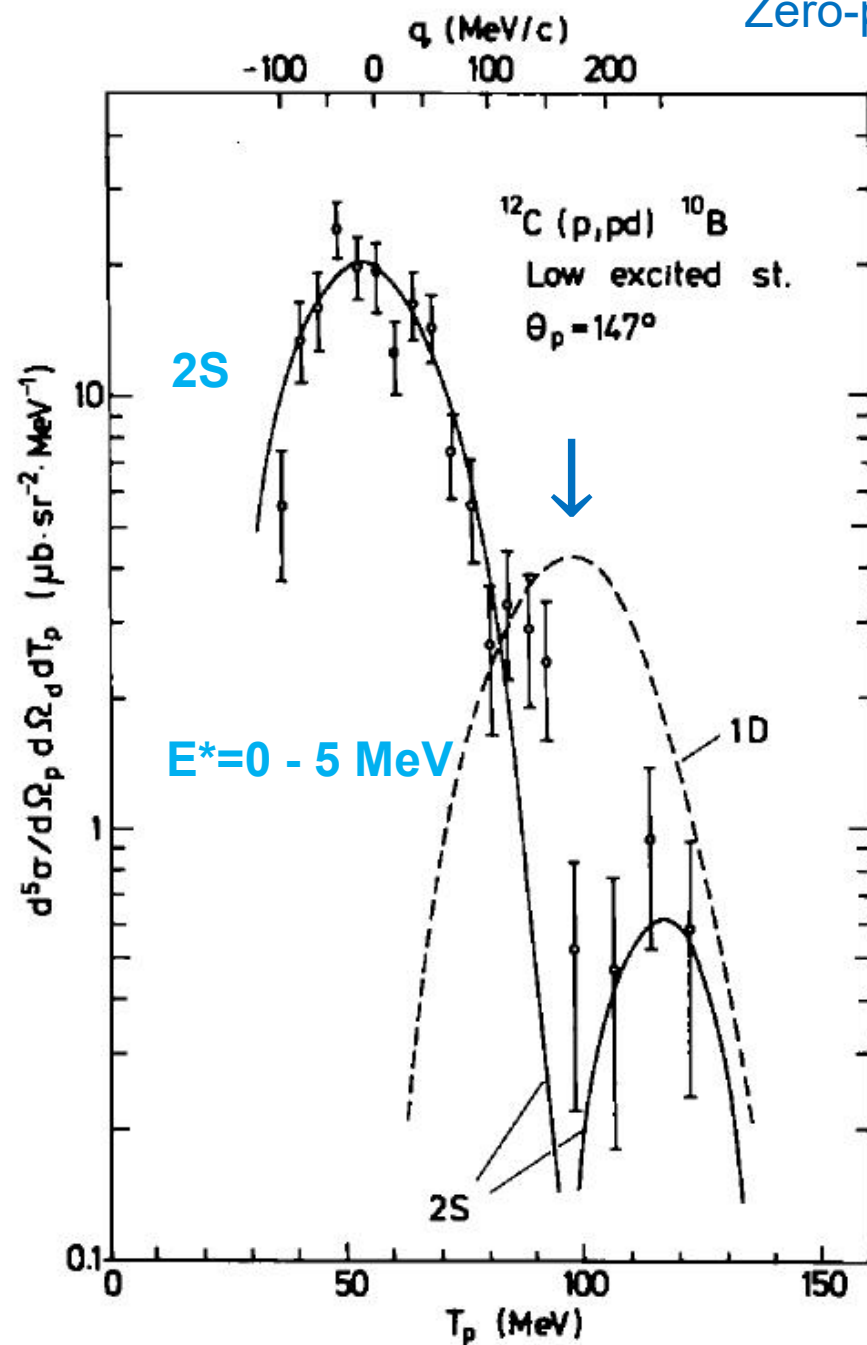
Ядро- мишень	События					
	”низкоэнергетические”			”высокоэнергетические”		
	эксп.	Теория		эксп.	Теория	
		$R_0 = 9$	$R_0 = 1$		$R_0 = 9$	$R_0 = 1$
7Li	$6,1 \pm 0,9$	13,7	80,0	$9,1 \pm 1,5$	6,1	42,8
6Li	$0,30 \pm 0,16$	0	0	$8,1 \pm 1,5$	6,9	48,6

D. Albrecht et al. Nucl. Phys. A 322 (1979) 525; exp. ${}^{6,7}Li(p,nd)$ **670 MeV**

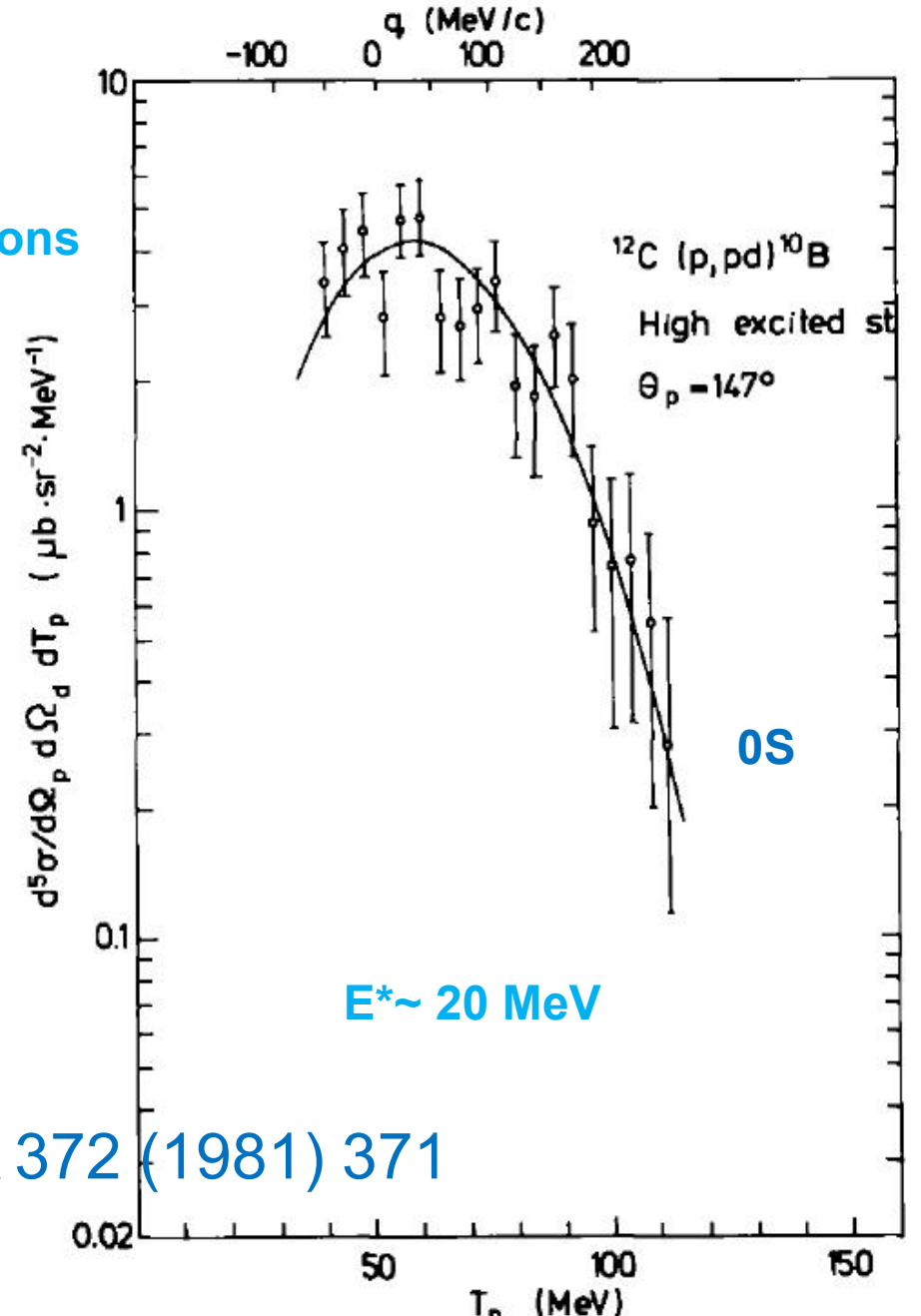
O. Imambekov, Yu.N. U., Izv. Akad. Nauk SSSR, Ser. Fiz., **51** (1987) 947- (theor. model)

Zero-point at $q \approx 180$ MeV/c

J. Erő et al. / Quasi-free scattering

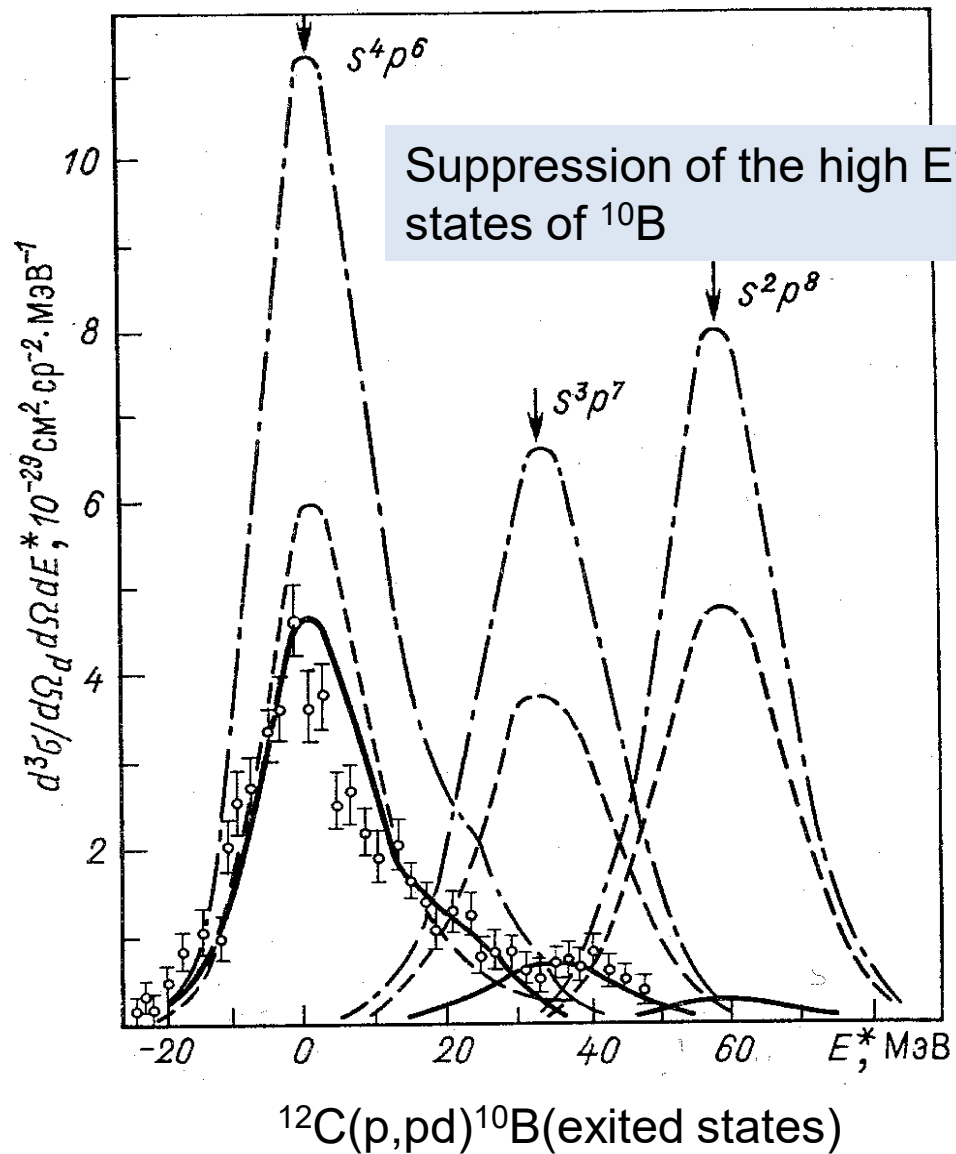
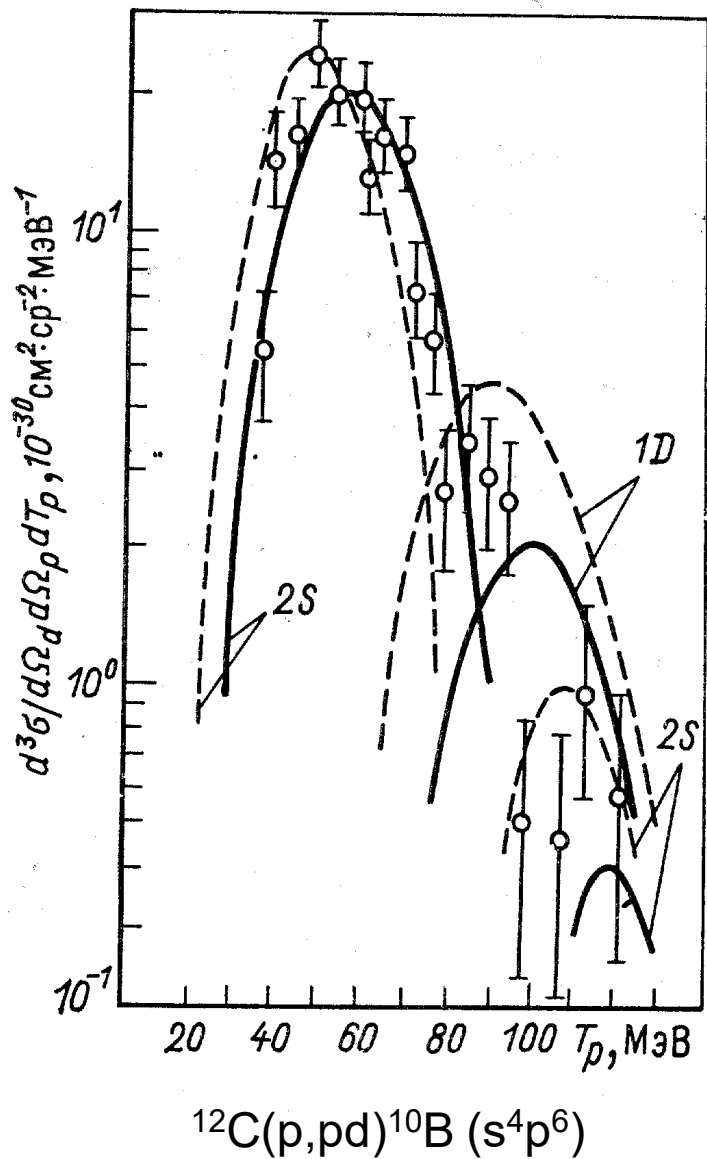


Different $\langle NN \rangle$ c.m.s. momentum distributions



J. Ero et al. NPA 372 (1981) 371

FSI- strong absorption



SRC in $A(p, 3N)B$

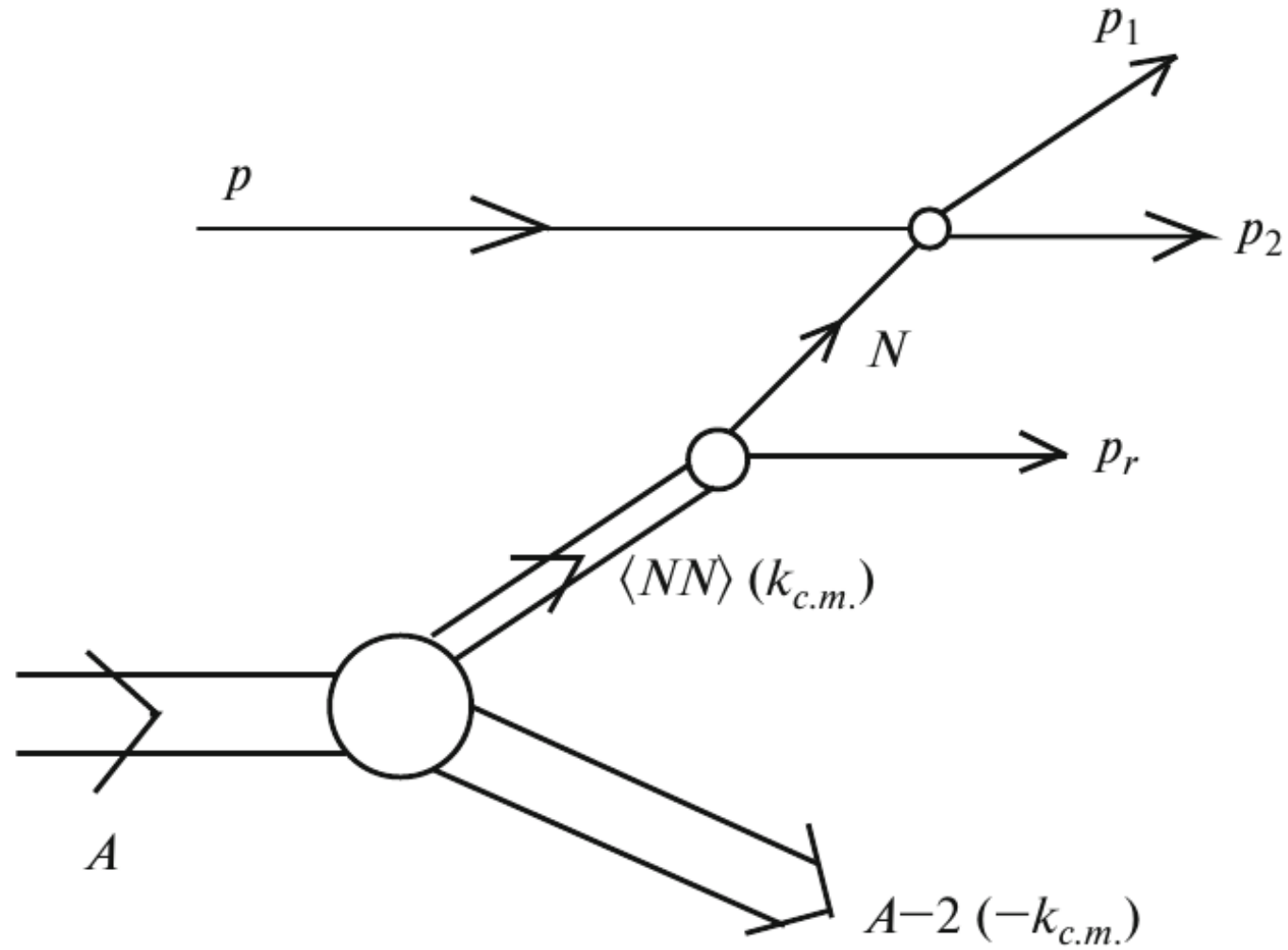


Fig. 1. The pole mechanisms of the reaction $A(p, 2pN)A-2$.

SRC from ab initio quantum Monte Carlo calculations

R.Cruz-Torres et al. *Nature Phys.* **17** (2021) 306 (and references therein)

NN: =AV18+UX, AV4'+UIX, N²LO, NV2+3+Ia ; Generalized Contact Formalizm

Factorization at small r or high q :

$$\rho_{\alpha,NN}^A(R, r) = C_{\alpha,NN}^A(R) \times |\varphi_{NN}^\alpha(r)|^2,$$

$$n_{\alpha,NN}^A(Q, q) = \tilde{C}_{\alpha,NN}^A(Q) \times |\tilde{\varphi}_{NN}^\alpha(q)|^2,$$

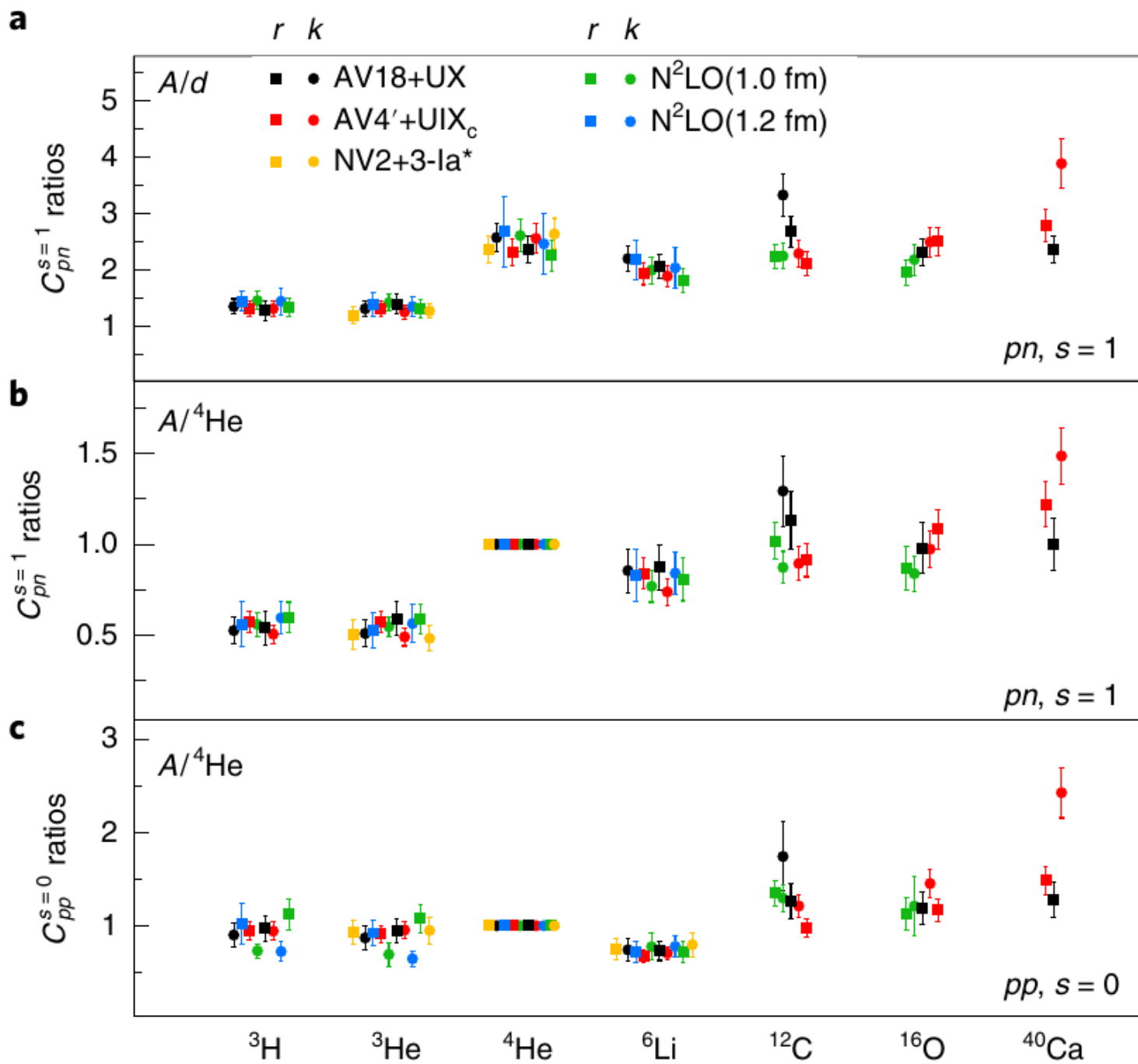
Nuclear contact coefficients:

$$C_{\alpha,NN}^A \equiv \int d\mathbf{R} C_{\alpha,NN}^A(\mathbf{R}),$$

$$\tilde{C}_{\alpha,NN}^A \equiv \frac{1}{(2\pi)^3} \int d\mathbf{Q} e_{\alpha,NN}^A(\mathbf{Q}),$$

“NN models with very different short-range physics all lead to the same contact term ratios A/d ... Relative abundance of SRC pairs in nuclei is a long-range (that is mean-field) quantity that is insensitive the short-distance nature of the nuclear force”

Thus, at the first step, one may apply a shell model (h.o.TISM=TIMMO) with NN-correlators for the SRC analysis like it was done for the $^{12}\text{C}(p,pd)\text{B}$,



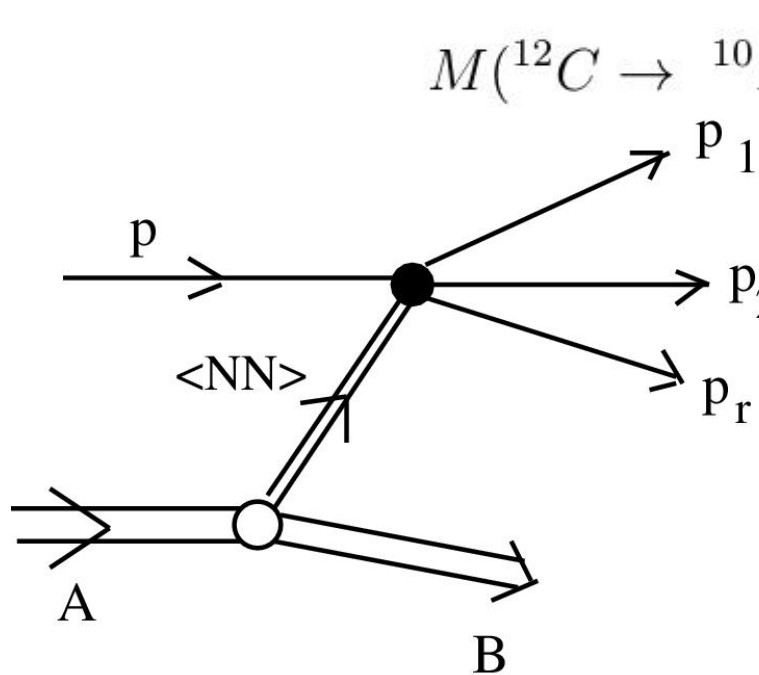
R.Cruz-Torres et al.,
Nature Phys. 17 (2021) 306

Matrix element

$$M_{fi} = M(A \rightarrow B + \langle NN \rangle) \frac{1}{p_{NN}^2 - M_{NN}^2 + i\epsilon} M(p \langle NN \rangle \rightarrow ppN),$$

$$d\sigma = (2\pi)^4 \delta^4(P_i - P_f) \frac{1}{4I} |M_{fi}|^2 \prod_{j=1}^n \frac{d^3 p_j}{2E_j (2\pi)^3}$$

In the rest frame of A:



$$M(^{12}\text{C} \rightarrow ^{10}\text{B} + \langle NN \rangle) = - \left(\frac{A}{2} \right)^{1/2} \langle \Psi_A | \Psi_B, \Psi_{NN}, \Psi_{\nu\Lambda} \rangle$$

$$\times \left(\varepsilon_A^{B+\langle NN \rangle} + \frac{q^2}{2\mu} \right) \Psi_{\nu\Lambda M_\Lambda}(\mathbf{q}) \sqrt{2m_A 2m_B 2m_{\langle NN \rangle}},$$

$$\varepsilon_A^{B+\langle NN \rangle} = m_B + m_{\langle NN \rangle} - m_A,$$

$$\mu = m_B m_{\langle NN \rangle} / (m_B + m_{\langle NN \rangle}),$$

$$\mathbf{q} = \frac{m_B \mathbf{p}_{\langle NN \rangle} - m_{\langle NN \rangle} \mathbf{p}_B}{m_B + m_{\langle NN \rangle}}$$

Spectroscopic factors within the translationally-invariant shell model (TISM)

/For future: ab initio microscopic calculations of A=12 system/

$$S^x_A = \binom{A}{x}^{1/2} \langle \psi_A | \psi_B \psi_{\nu\Lambda}(\mathbf{R}_{A-x} - \mathbf{R}_x) \psi_x \rangle.$$

Oscillator rule:

$$\psi_A^{TISM} = |AN[f](\lambda\mu)\alpha LSTJMM_T \rangle$$

$$N_A - N_B = N_x + \nu$$

Mixing shell-model configurations:

$$\psi_{J,T}^A = \sum_{[f]LS} \alpha_{[f]LS}^{A,JT} |AN[f](\lambda\mu)\alpha LSTJMM_T \rangle$$

$$|AN_A\alpha \rangle = \sum_{\beta\gamma\Lambda M_\Lambda N_B N_x \nu} \langle AN_A\alpha | A - x N_B \beta, \nu \Lambda M_\Lambda, x N_x \gamma \rangle$$

$$|BN_B\beta \rangle |xN_x\gamma \rangle |\nu\Lambda M_\Lambda \rangle .$$

– Matrix element for $p + {}^{12}C \rightarrow p + p + N + {}^{10}B$ —————

$$\begin{aligned}
 M_{fi}(pA \rightarrow ppNB) &= \binom{A}{2}^{1/2} \sum_{M_{J_d}, \bar{J}, \bar{M}, M_\Lambda} \sum_{\alpha_i, \alpha_f, N, \Lambda, \mathcal{L}} \alpha_i^{AJ_i T_i} \alpha_f^{A-2J_f T_f} \\
 &\langle A\alpha_i | A - 2\alpha_f, N\Lambda; d' \rangle (\Lambda M_\Lambda J_{d'} M_{J_{d'}} | \bar{J} \bar{M}) (J_f M_{J_f} \bar{J} \bar{M} | J_i M_i) \\
 &\quad (T_f M_{T_f} T_{d'} M_{T_{d'}} | T_i M_{T_i}) U(\Lambda L_{d'} \bar{J} S_{d'}; \mathcal{L} J_{d'}) \left\{ \begin{array}{ccc} L_f & S_f & J_f \\ \mathcal{L} & S_{d'} & \bar{J} \\ L_i & S_i & J_i \end{array} \right\} \\
 &\quad [(2L_i + 1)(2S_i + 1)(2J_f + 1)(2\bar{J} + 1)]^{1/2} \Psi_{N\Lambda M_\Lambda}^{dist}(\mathbf{k}_B) \\
 &\quad \times \langle \mathbf{p}_1 \sigma_1, \mathbf{p}_2 \sigma_2, \mathbf{p}_r \sigma_r | \hat{M}(p < NN > \rightarrow p_1 p_2 p_r) | \mathbf{p} \sigma_p, -\mathbf{k}_B \Psi_{NN} \rangle
 \end{aligned}$$

$${}^{12}C: L_i = S_i = J_i = 0, T_i = 0; |10B \rangle = |s^4 p^6 \rangle$$

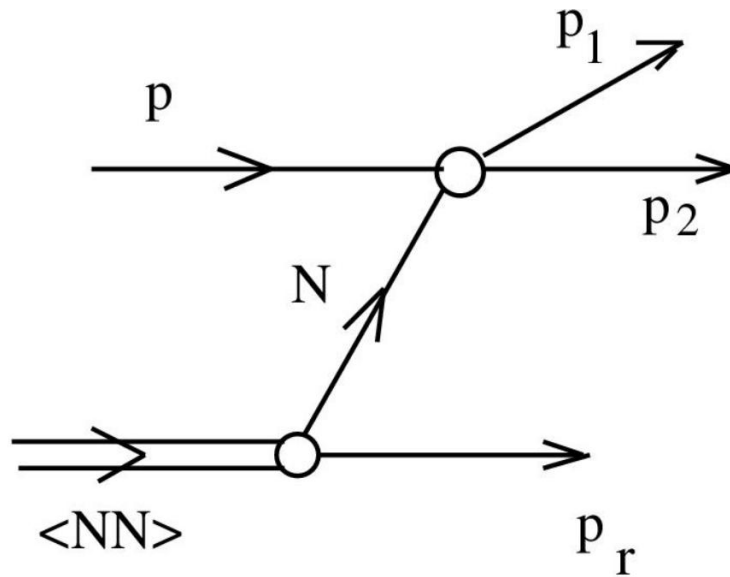
– Matrix element of the $p+ \langle NN \rangle \rightarrow p + p + N$ —————

In the Light front dynamics

$$M_{fi}^{LFD}(p \langle NN \rangle \rightarrow p_1 p_2) = \frac{\Psi_d^{LFD}(\mathbf{k}_\perp, \xi)}{1 - \xi} M_{fi}(pN \rightarrow p_1 p_2),$$

$$\xi = \frac{p_r^+}{p_r^+ + p_N^+}, \quad \mathbf{q}_\perp = (1 - \xi)\mathbf{p}_{r\perp} - \xi\mathbf{p}_{N\perp},$$

$$M_{pN}^2 = \frac{m_p^2 + \mathbf{p}_{N\perp}^2}{\xi(1 - \xi)}.$$



$$\Psi_d^{LFD}(\mathbf{q}) = \sqrt{\varepsilon(\mathbf{q})} \varphi_d^{\text{nonrel}}(\mathbf{q})$$

SRC

— Momentum distribution in $\langle NN \rangle -^{10}B_5$

TISM(TIMO)

$N\Lambda = 20, 22$ for $|s^4p^6\rangle$

$$R_{20}^2 = \frac{6}{\sqrt{\pi} p_0^3} \left[1 - \frac{2}{3} \left(\frac{p}{p_0} \right)^2 \right]^2 \exp \left\{ - \left(\frac{p}{p_0} \right)^2 \right\}, \quad (1)$$

$$R_{22}^2 = \frac{16}{15\sqrt{\pi} p_0^3} \left(\frac{p}{p_0} \right)^4 \exp \left\{ - \left(\frac{p}{p_0} \right)^2 \right\} \quad (2)$$

$N\Lambda = 00$ for $|s^2p^8\rangle$

$$R_{00}^2 = \frac{4}{\sqrt{\pi} p_0^3} \exp \left\{ - \left(\frac{p}{p_0} \right)^2 \right\}$$

where $p_0 = \sqrt{\mu}/r_0 = \sqrt{\mu} p_0^{h.o.}$;

$\mu = \frac{m_1 m_2}{m_1 + m_2} = \frac{5}{3}$ – the reduced mass of the $d -^{10}B$ system in m_N ;

r_0 is the h.o. shell model parameter;

$p_0^{h.o.} = \hbar/r_0$

The $\langle NN \rangle$ c.m. distribution in mean-field model

(Cioffi degli Atti, Simula, PRC, 1996)

$$\langle (\sum_{i=1}^A \vec{k}_i)^2 \rangle = 0, \quad \langle k_{c.m.}^2 \rangle = \frac{2(A-2)}{A-1} \langle k^2 \rangle$$

$$n_{c.m.}(k_{c.m.}) = C \exp(-\alpha_{c.m.} k_{c.m.}^2) \quad \langle k_{c.m.}^2 \rangle = 3/2\alpha_{c.m.}$$

$$\alpha_{c.m.} = \frac{3(A-1)}{4(A-2)} \frac{1}{2M \langle T \rangle}$$

$$T_s = \frac{3}{2} \frac{p_0^2}{2M} \quad \text{and} \quad T_p = \frac{5}{2} \frac{p_0^2}{2M}$$

$$\langle T \rangle = \frac{4T_s + 8T_p}{12} = \frac{13}{6} \frac{p_0^2}{2M}$$

$$p_0 = ?$$

Antisymmetrization effects are not taken into account; s-shape is assumed.

Charge form factor of the ^{12}C

$$\begin{aligned} \rho(r) &= 2R_{00}^2(r) + 4R_{11}^2(r) \\ &= \frac{8}{r_0^3 \sqrt{\pi}} \left[1 + \frac{4}{3} \left(\frac{r}{r_0} \right)^2 \right] \exp\left(-\frac{r^2}{r_0^2} \right), \end{aligned}$$

where $r_0 = \hbar/p_0$. Then the charge form factor is

$$F(q) = \int d^3r \rho(r) \exp\left(i \frac{A-1}{A} \mathbf{q} \mathbf{r} \right).$$

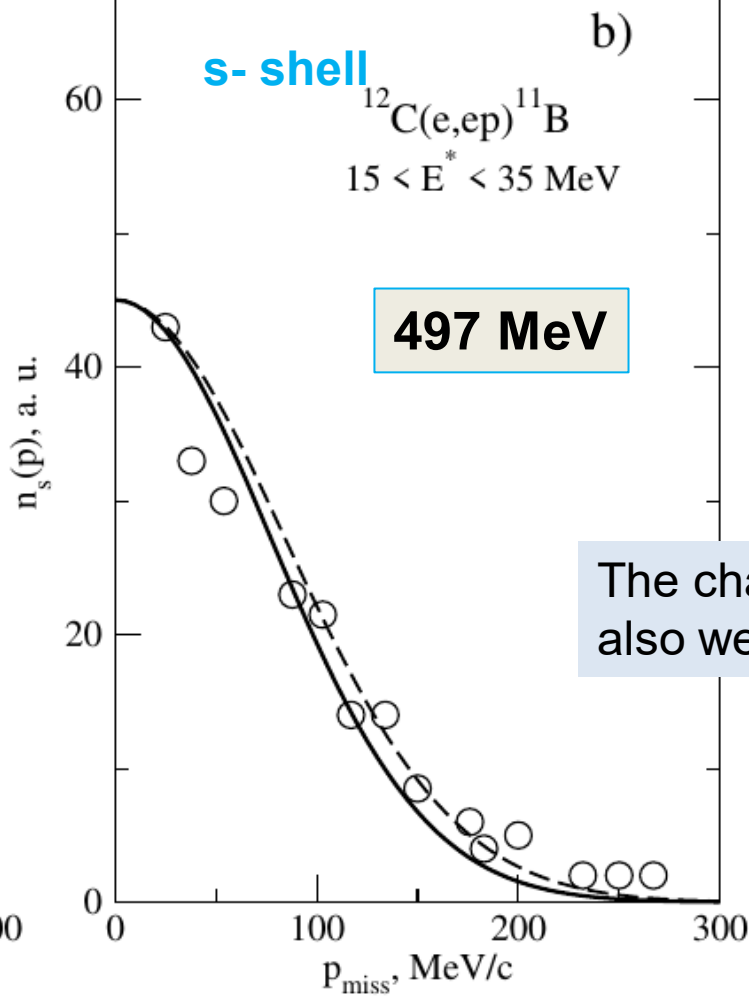
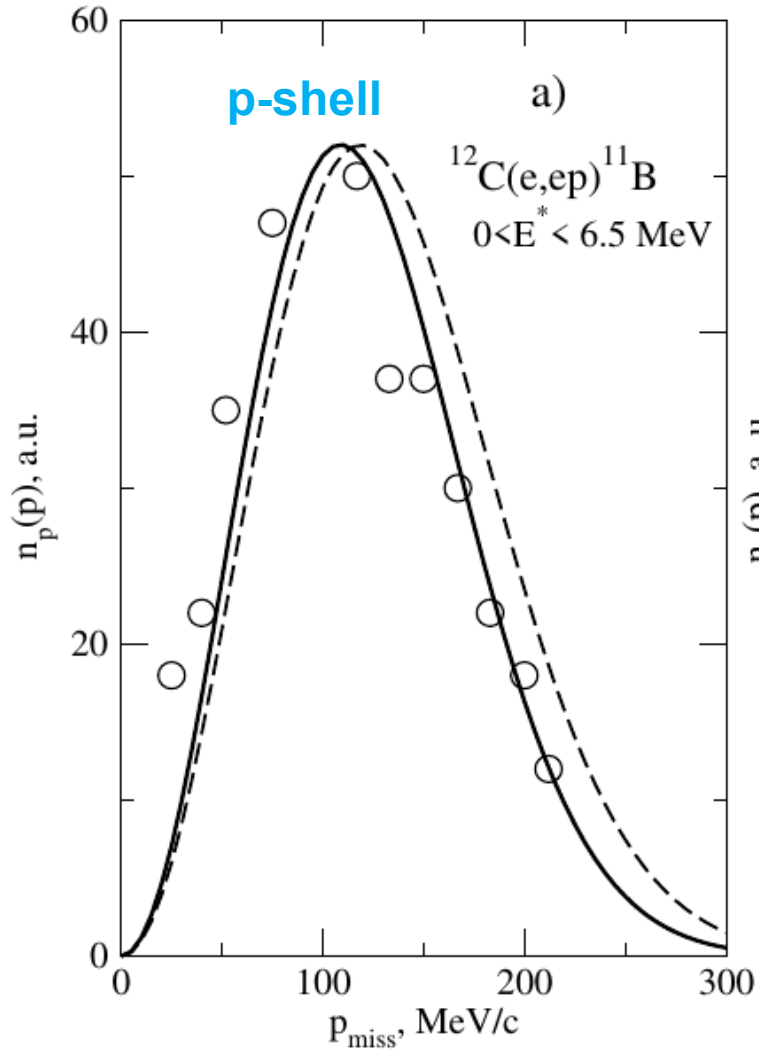
F_{ch} fit: $p_0 = 109 \text{ MeV}/c$;

$$R_{00}^2(p_{cm}) = C \exp\left\{ \frac{p_{cm}^2}{P_0^2} \right\}; \quad \tilde{p}_0 = \sqrt{\frac{12}{11}} p_0 = 113.8 \text{ MeV} / c, \langle T \rangle = 15 \text{ MeV}$$

$$TISM : P_0^2 = \frac{5}{3} \tilde{p}_0^2 \quad P_0 = 146.8 \text{ MeV} / c$$

Talmi-Moshinsky for $^{10}\text{A} - 2$ relative motion

$^{12}\text{C}(e,ep)^{11}\text{B}$: Data – A. Dieperink, T. Forest, Ann. Rev. Nucl. Part. Sci. 25 (1975) 1.



Mean-field-model, C. — deg. — Atti, Simula(1996)

$\langle T \rangle = 16.9 \text{ MeV}; \alpha_{c.m.} = 1.0 \text{ fm}^2;$

$\sigma = 142.8 \text{ MeV} / c;$

$$n(p_{cm}) = C \exp\left\{-\frac{p_{cm}^2}{2\sigma^2}\right\} = C \exp(-\alpha_{cm} p_{cm}^2);$$

fit to $^{12}\text{C}(e,ep)^{11}\text{B}$ — $^{12}\text{C} F_{ch}$: $\langle T \rangle = 14.9 \text{ MeV}$

$\sigma^{TISM} = 103 \text{ MeV} / c$

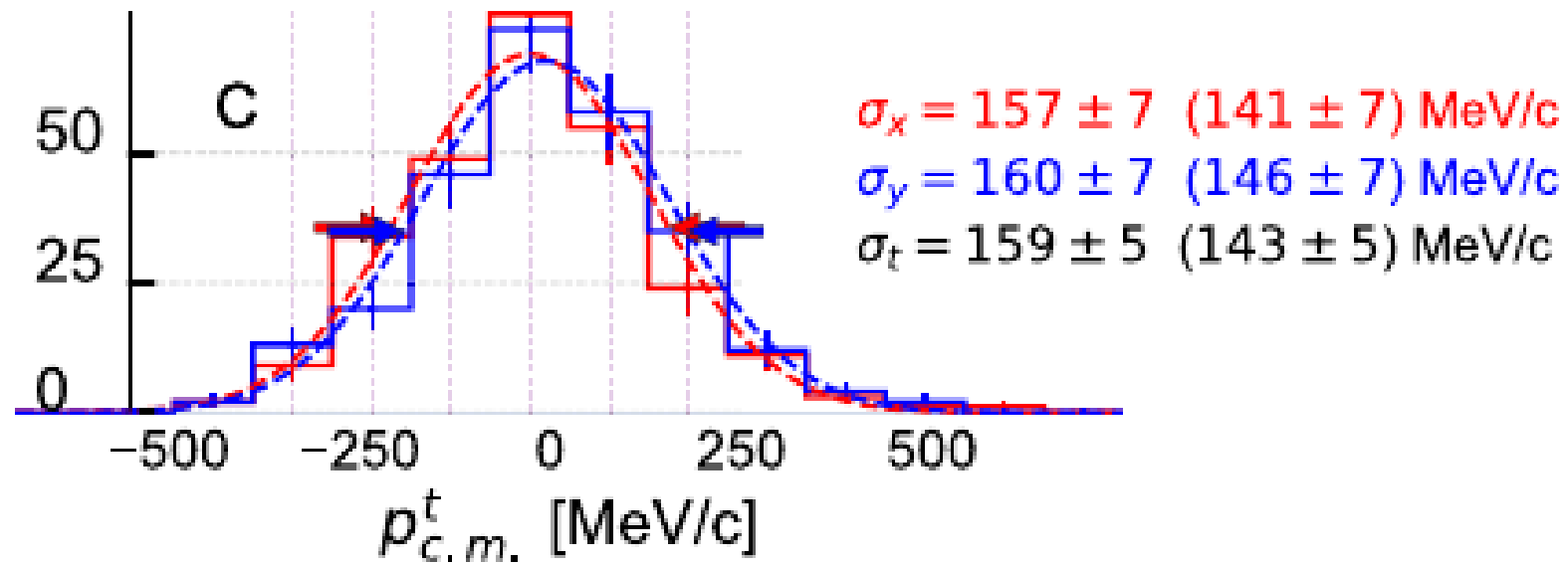
$\sigma_{exp.}(e, epp) = (143 \pm 6) \text{ MeV} / c$

The charge form factor of ^{12}C is also well described

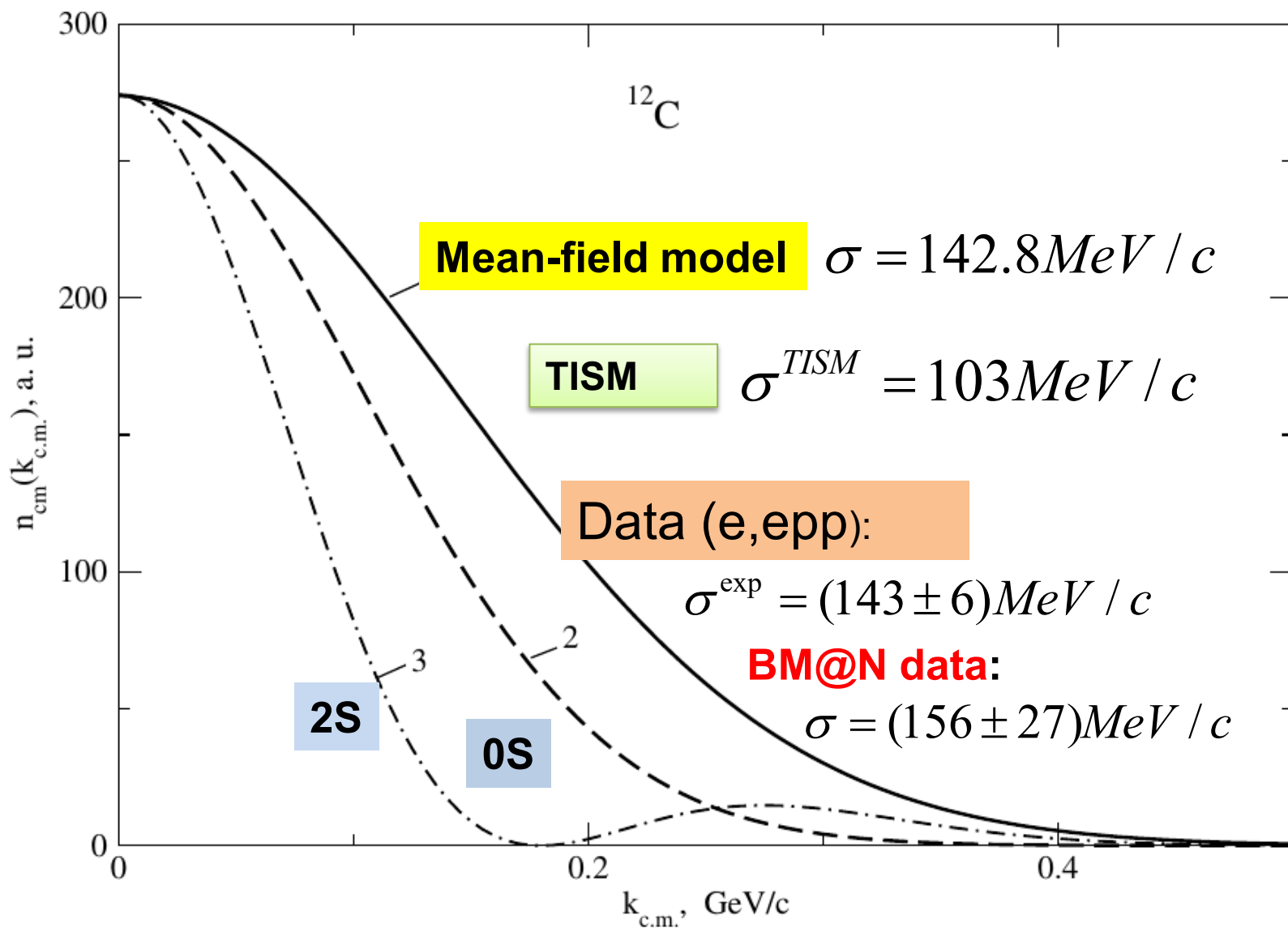
Yu.N.U. Phys. Part. Nucl. 52 (2021)652

Fig. 2. Single nucleon momentum distribution in the reaction $^{12}\text{C}(e,ep)^{11}\text{B}$ at electron beam energy 497 MeV for the p-shell (a) and s-shell nucleons (b) corresponding to transitions to the states of the residual nucleus ^{11}B with excitation energy $0 < E^* < 6.5 \text{ MeV}$ and $15 < E^* < 35 \text{ MeV}$, respectively. The curves show the results of our calculations in the plane wave impulse

E. Cohen et. al. PRL 121 (2018) 092501



Comparison with calculations appears to show that the SRC pairs are formed from mean-field nucleons in specific quantum states.



TISM

$$\nu = N_A - N_x - N_{A-x}$$

$$N_x = 0, N_A = 8$$

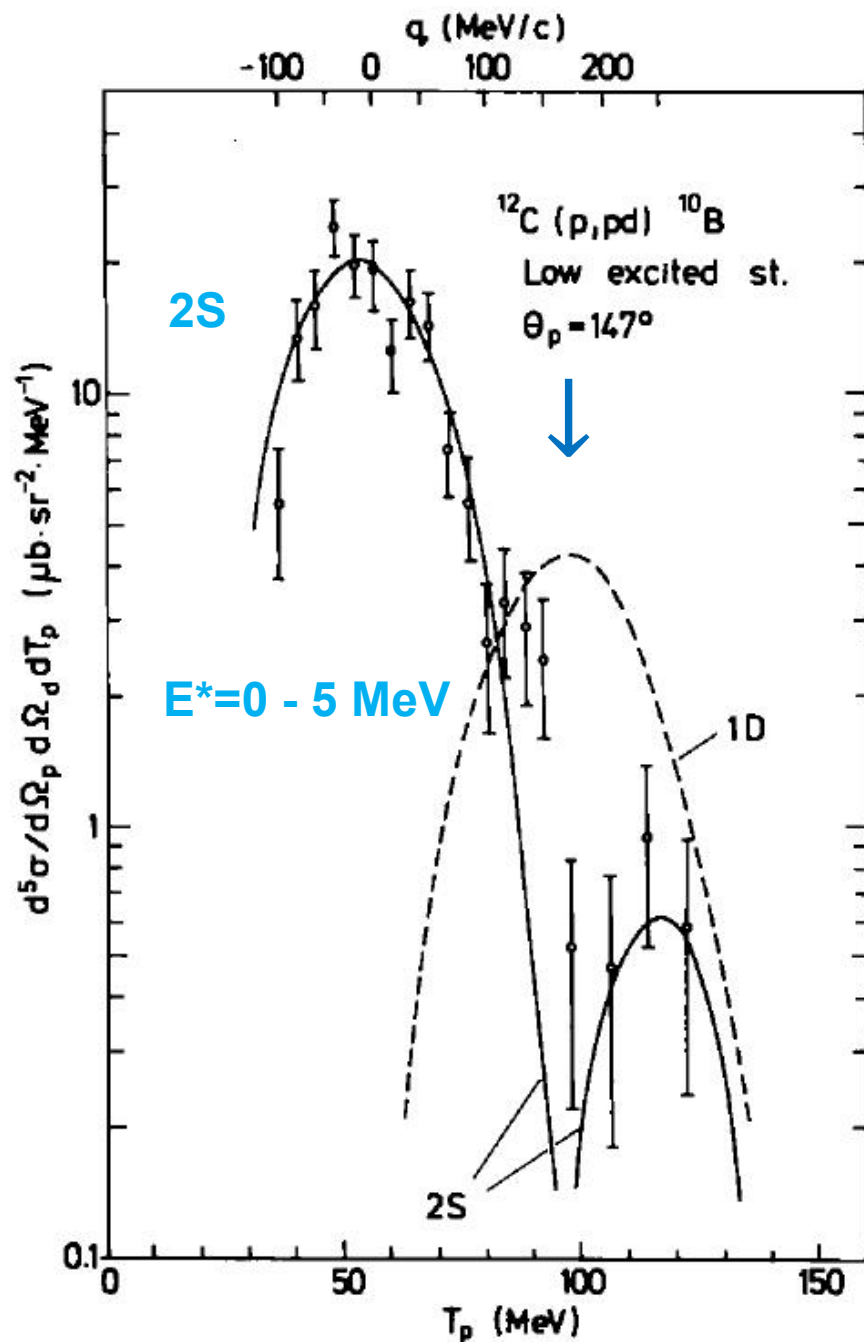
$$R_{\nu\Lambda}(k_{\text{c.m.}})$$

$$s^4 p^6, \nu = 2$$

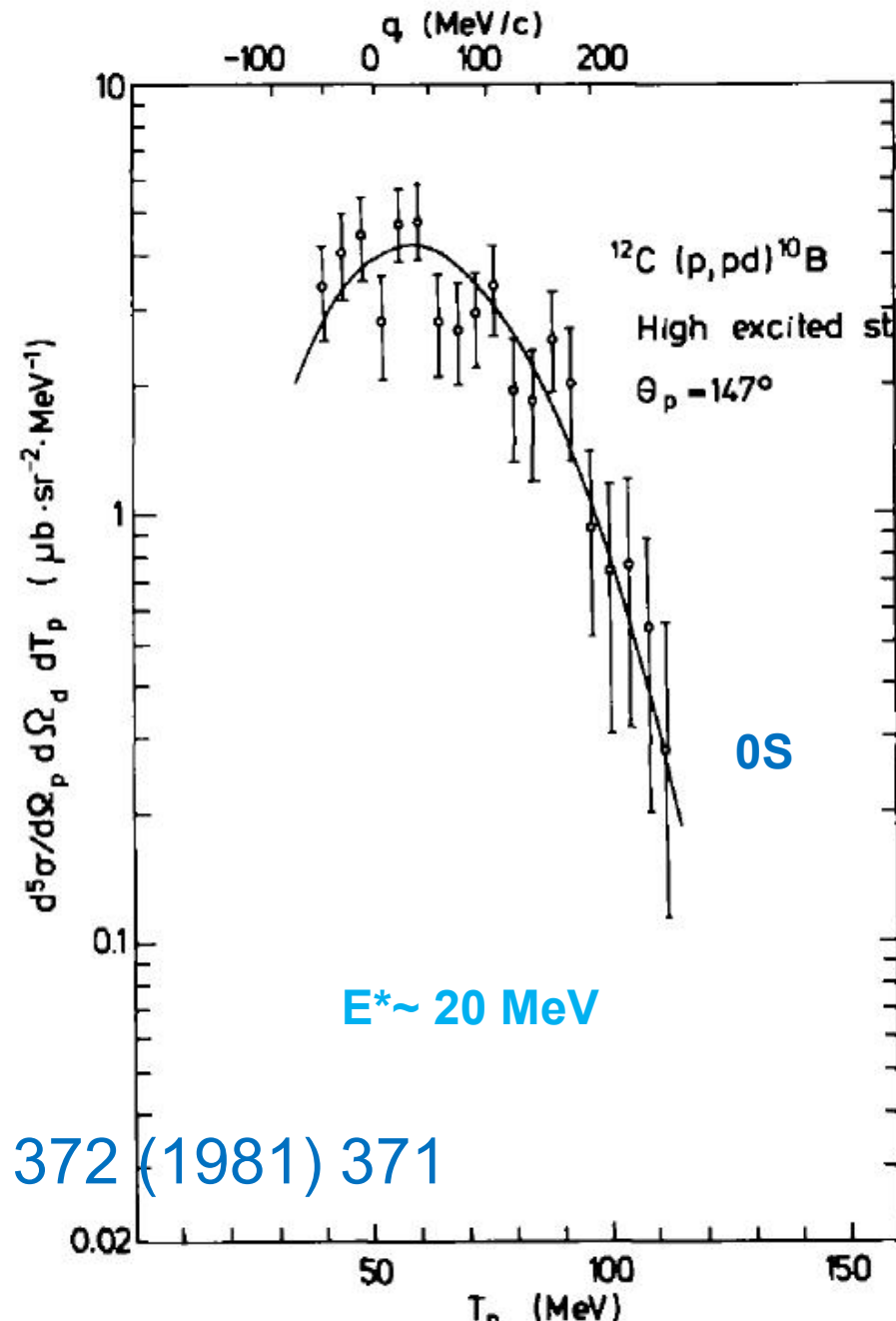
$$s^2 p^8, \nu = 0$$

$k_{\text{c.m.}}$ - PUZZLE

Fig. 3. Distribution over the c.m. momentum of the SCR pair $p_{\text{c.m.}}$ in the ^{12}C for the mean-field model with $\alpha_{\text{c.m.}} = 0.95 \text{ fm}^2$ (full line) and the TISM wave function squared with $p_0 = 146.9 \text{ MeV}/c$ for the 0S-type (dashed), and 2S-type (dashed-dotted). All distributions are arbitrary normalized at $p_{\text{c.m.}} = 0$ to the same value.



$^{12}\text{C}(p, pd)^{10}\text{B}$
 670 MeV



J. Ero et al. NPA 372 (1981) 371

pp/pn ratio

$$S_A^x = \binom{A}{2}^{1/2} \frac{1}{\sqrt{2T+1}} PC(S, T)$$

$$|M_{fi}(A(p, 2pN)B)|^2 \propto \frac{1}{2T+1} n_{cm}(k_{c.m.}) n_{NN}(q_{rel}) |M^{pN}|^2 [I_{pN} PC(s, T)]^2$$

$$R = \frac{pp}{pn} = \frac{(pp)_{S=1, T=1}}{(pn)_{S=1, T=0} + (pn)_{S=0, T=1}} = \frac{1}{2} R_{rel}$$

$$^{12}C : |[444], L_i = 0, S_i = 0, T_i = 0, J_i = 0 >$$

$$PC(S = 1, T = 0) = PC(S = 0, T = 1)$$

pp to pn pairs ratio of the spectroscopic factors: 1/2

GCF: Contact terms ratio $C_{S=0}(pp)/C_{S=1}(pn) \sim 1/14$

R. Cruz-Torres, et al. Nature Phys. 17 (2021) 306; R. Weiss et al. PLB 780 (2018) 211

pp/pn ratio

$$R_{rel} = \int_{q_{min}}^{q_{max}} dq q^2 \psi_{pp;ST=01}^2(q) / \int_{q_{min}}^{q_{max}} dq q^2 \psi_{d;ST=01}^2(q);$$

$$\psi_{10}^2(q) = u^2(q) + w^2(q); \psi_{01}(q), pp(^1S_0) - \text{scattering};$$

$$\int_0^{\infty} dq q^2 \psi_{ST}^2(q) = 1;$$

$$R = \frac{pp}{pn} = \frac{pp}{(pn)_{S=1,T=0} + (pn)_{S=0,T=1}} = \frac{1}{2} R_{rel}$$

Table 1. The $(ST = 01)/(ST = 10)$ ratio R_{rel} versus q_{min} at $q_{max} = 1.0 \div 2.0$ GeV/c

$q_{min}, \text{ GeV/c}$	R_{rel}	$q_{min}, \text{ GeV/c}$	R_{rel}
0.2	0.15	0.6	0.27-0.3
0.3	0.06-0.07	0.7	0.39-0.54
0.4	0.09-0.10	0.8	0.55-0.88
0.5	0.17-0.2	0.9	0.78-1.5

M.Duer et al. (CLAS coll.) PRL 122
(2019) 172502

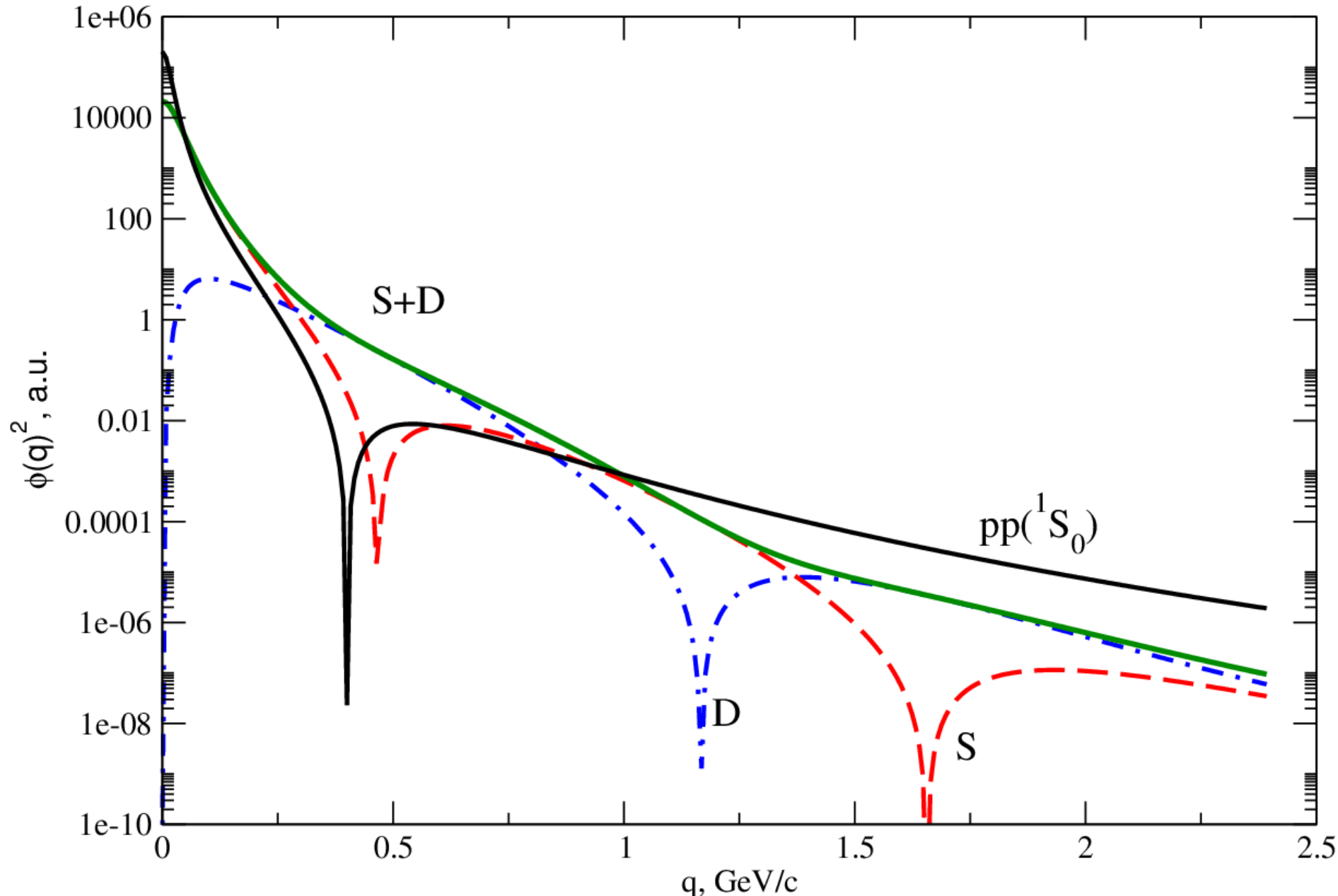
$R_{rel}=0.06-0.07$ at $q_{min}=0.3$ GeV/c, $q_{max}=1-2$ GeV/c
 $pp/pn=0.03-0.035$

$R_{exp}=5\%$ (that is 3% with account for
charge-exchange in the final state)

pp and deuteron internal momentum distribution

pp($1S_0$) scattering
Lensky V. et al.,
EPJ A 26 (2005)107
CD – Bonn NN

Yu. Uzikov, A. Uvarov, Phys.
Part. Nucl. **53**, №2, 426 (2022).



How to take into account ISI and FSI?

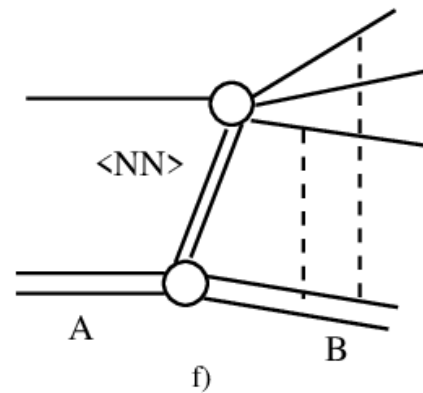
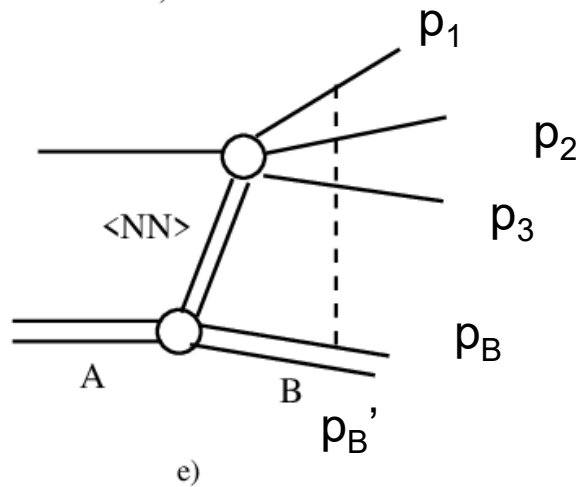
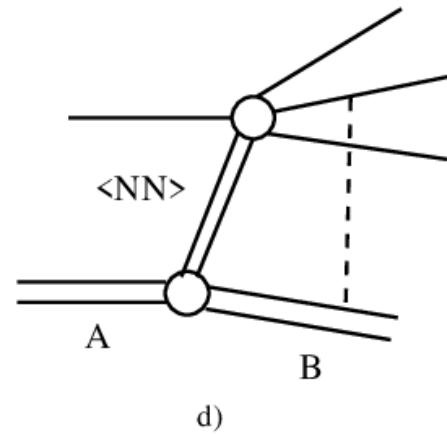
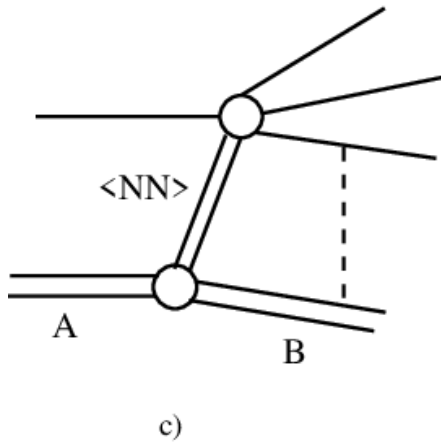
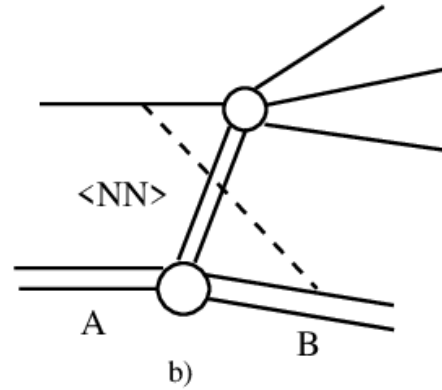
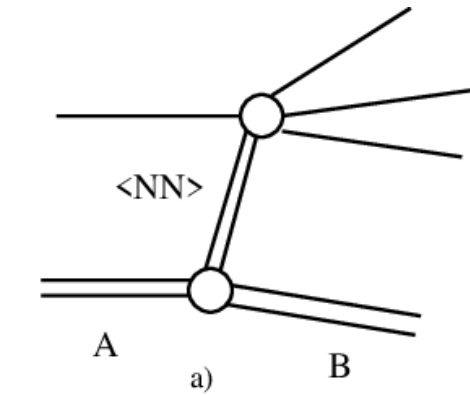
Transition matrix element

$$T_{fi} = \begin{pmatrix} A \\ x \end{pmatrix}^{1/2} \sum_{x' \nu \Lambda} \langle \psi_A | \psi_B \psi_{x'}, \psi_{\nu \Lambda} \rangle \underbrace{\Phi_{\nu \Lambda}(\mathbf{k}_B)} T^{px' \rightarrow Nx}.$$

$$T^{px' \rightarrow Nx} = \langle \mathbf{k}_N \mathbf{k}_x \chi_N \psi_x | \tau(px' \rightarrow Nx) | \mathbf{k}_p, -\mathbf{k}_B \chi_p \psi_{x'} \rangle$$

$$N_A - N_B = N_x + \nu$$

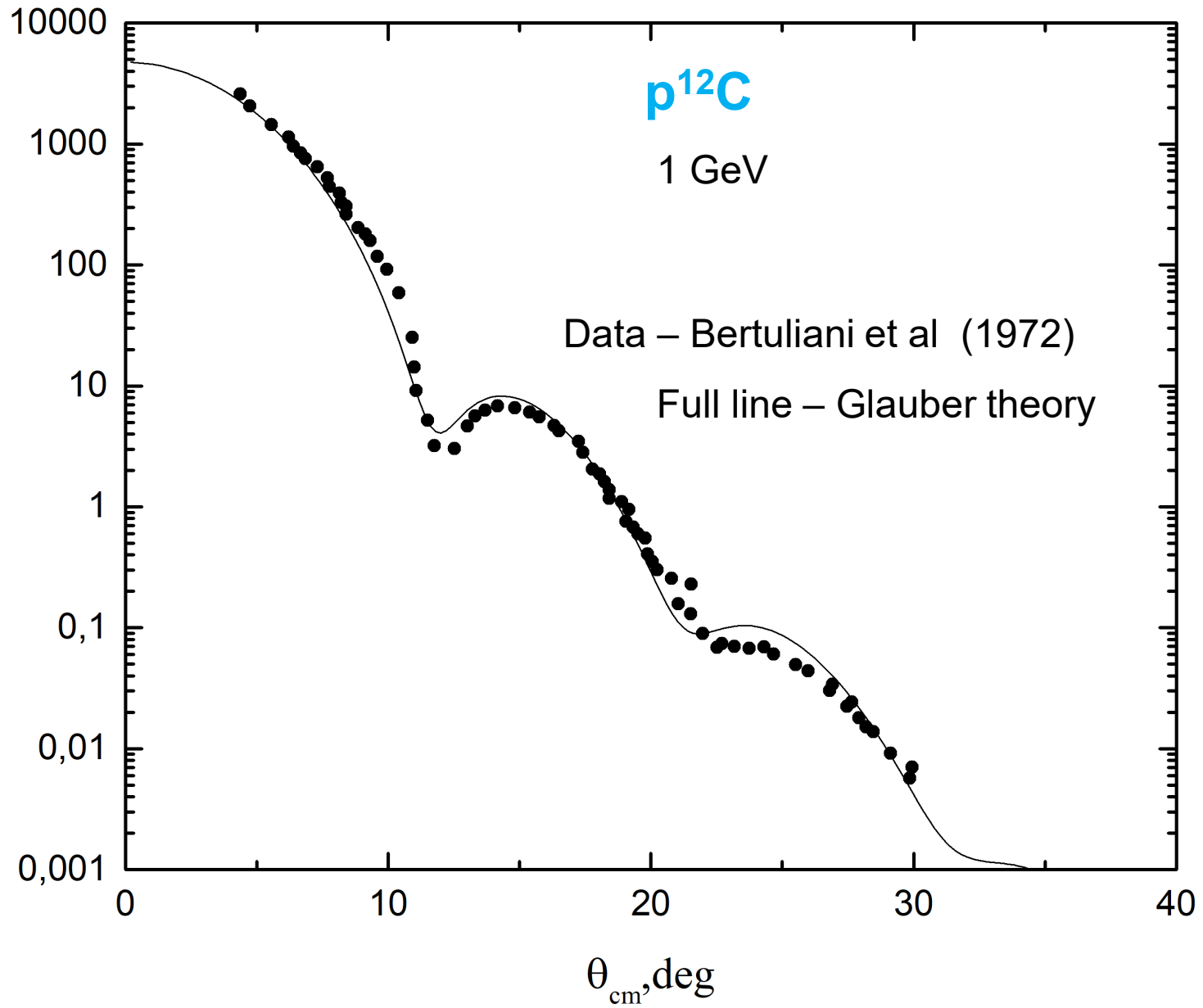
ISI@FSI ELASTIC RESCATTERINGS



Feynman graphs + generalized eikonal appr.
L.L. Frankfurt et al. PRC 56(1997) 2752

T-operator formalism with eikonal appr.
kollinear kinematics.
M.A. Zhusupov, Yu. N. Uzikov ,
Fiz. Elem. Chast. At. Yadr. 18(1987) 323

$d\sigma/d\Omega$, mb/ster



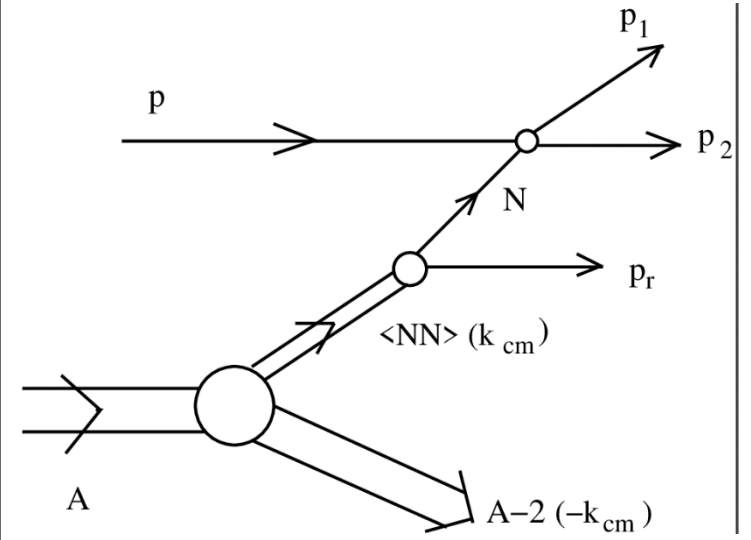
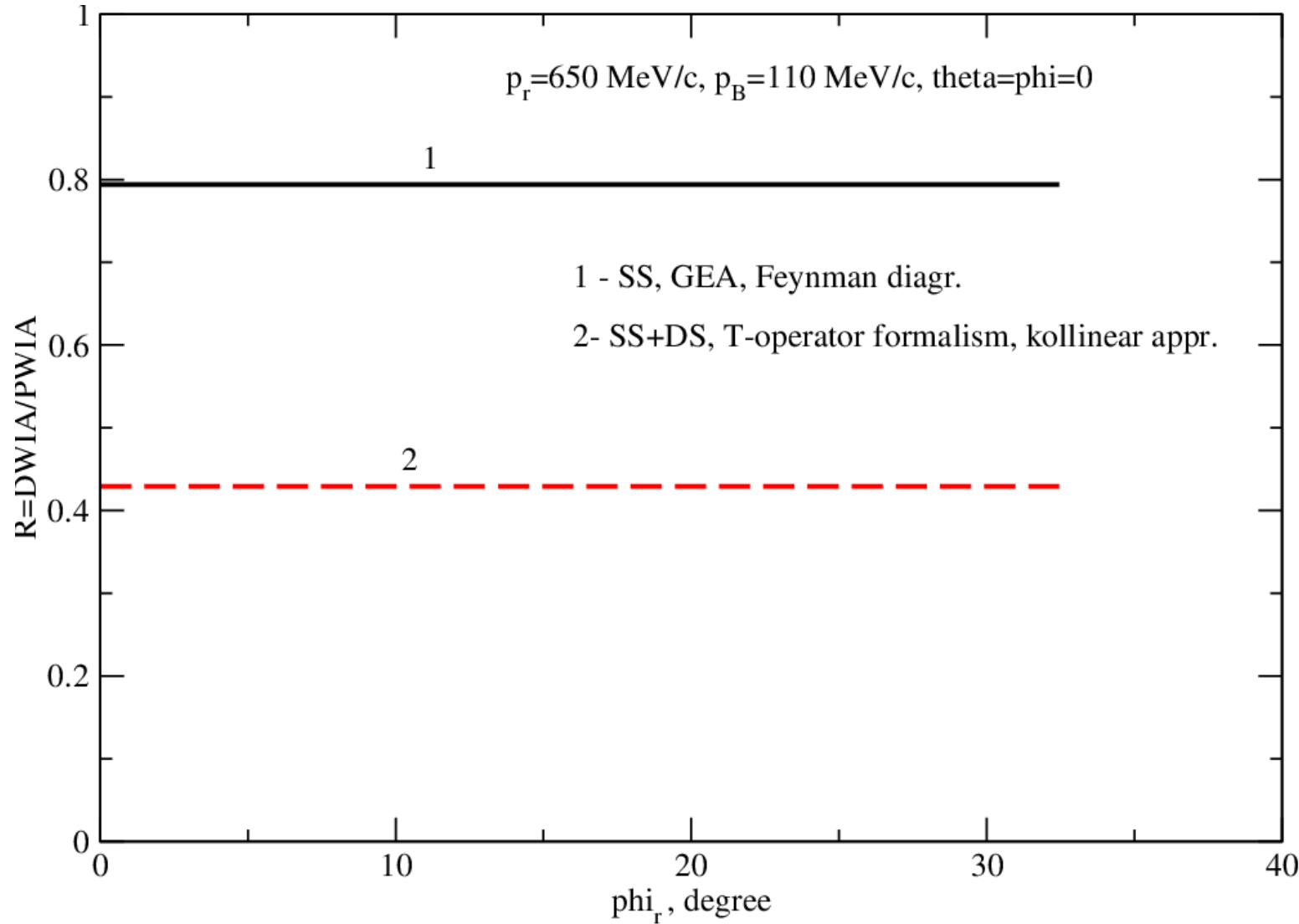
Feynman graphs + generalized eikonal approximation (GEA)
 L.L. Frankfurt et al. PRC 56(1997) 2752

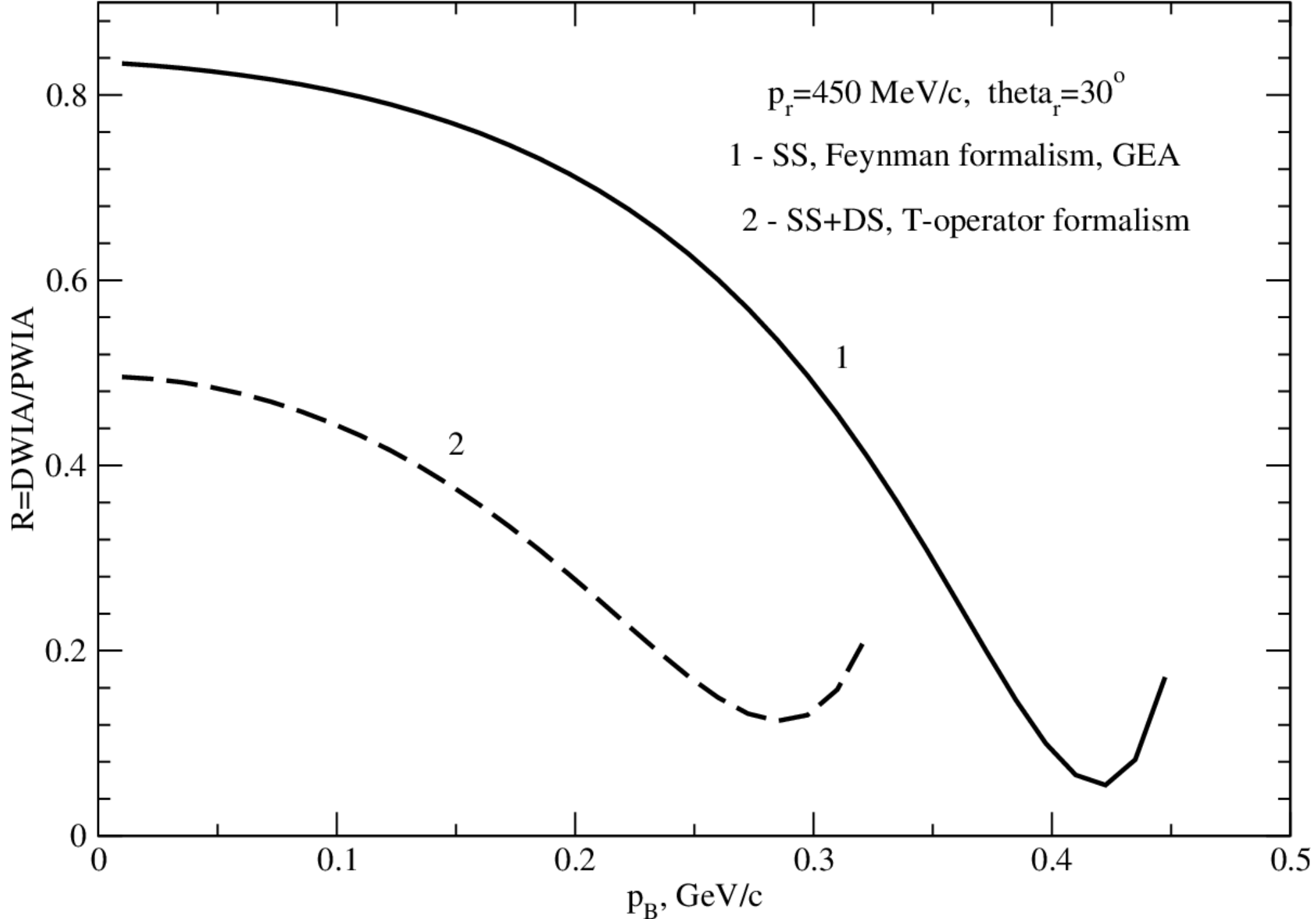
$$\frac{1}{(p_1 + p_B - p_{B'})^2 - m^2 + i\varepsilon} \approx \frac{1}{2p_{1z}} \frac{1}{p_{B'_z} - p_{B_z} + \Delta_1 + i\varepsilon};$$

$$\Delta_1 = -\frac{\vec{p}_{1t}}{p_{1z}} (\vec{p}_{B_t} - \vec{p}_{B'_t}) + \frac{E_1}{p_{1z}} (E_B - E_{B'});$$

$$\Delta_1 \neq 0 \rightarrow GEA$$

$$\begin{aligned}
 \Phi_{\nu\Lambda}(\mathbf{k}_B) = & \psi_{\nu\Lambda}(\mathbf{k}_B) + \frac{i}{4\pi k_{pA}} \int d^2\mathbf{q}_p F_{pB}(\mathbf{q}_p) \psi_{\nu\Lambda}(\mathbf{k}_B - \mathbf{q}_p) + \\
 & + \frac{i}{4\pi k_{xB}} \int d^2\mathbf{q}_x F_{xB}(\mathbf{q}_x) \psi_{\nu\Lambda}(\mathbf{k}_B - \mathbf{q}_x) + \frac{i}{4\pi k_{NB}} \int d^2\mathbf{q}_N F_{NB}(\mathbf{q}_N) \psi_{\nu\Lambda}(\mathbf{k}_B - \mathbf{q}_N) \\
 & - \frac{1}{(4\pi)^2 k_{pA} k_{NB}} \int d^2\mathbf{q}_p d^2\mathbf{q}_N F_{pB}(\mathbf{q}_p) F_{NB}(\mathbf{q}_N) \psi_{\nu\Lambda}(\mathbf{k}_B - \mathbf{q}_N - \mathbf{q}_p) - \\
 & - \frac{1}{(4\pi)^2 k_{pA} k_{xB}} \int d^2\mathbf{q}_p d^2\mathbf{q}_x F_{pB}(\mathbf{q}_p) F_{xB}(\mathbf{q}_x) \psi_{\nu\Lambda}(\mathbf{k}_B - \mathbf{q}_p - \mathbf{q}_x) - \\
 & - \frac{1}{(4\pi)^2 k_{xB} k_{NB}} \int d^2\mathbf{q}_x d^2\mathbf{q}_N F_{xB}(\mathbf{q}_p) F_{NB}(\mathbf{q}_N) \psi_{\nu\Lambda}(\mathbf{k}_B - \mathbf{q}_p - \mathbf{q}_N) - \\
 & - \frac{i}{(4\pi)^3 k_{pA} k_{NB} k_{xB}} \int d^2\mathbf{q}_p d^2\mathbf{q}_N d^2\mathbf{q}_x \times \\
 & \times F_{pB}(\mathbf{q}_p) F_{NB}(\mathbf{q}_N) F_{xN}(\mathbf{q}_x) \psi_{\nu\Lambda}(\mathbf{k}_B - \mathbf{q}_N - \mathbf{q}_p - \mathbf{q}_x).
 \end{aligned}$$



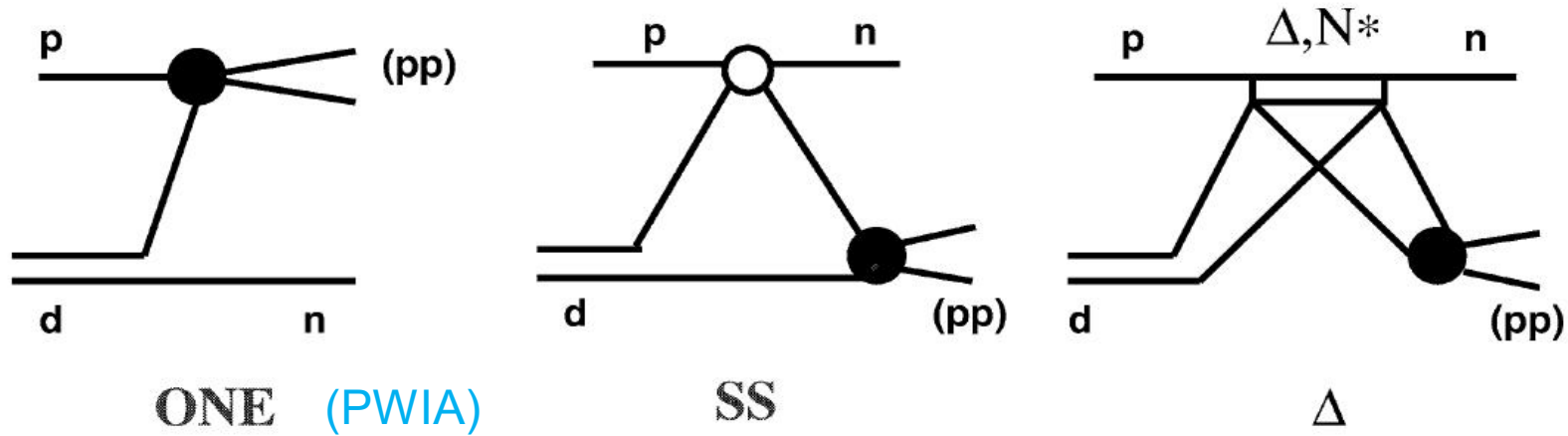


SUMMARY

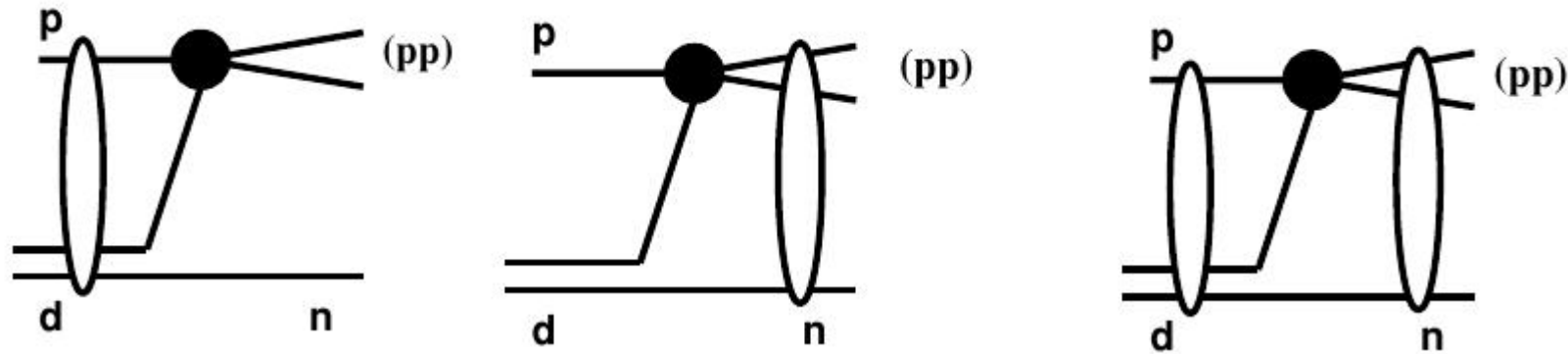
- TISM applied for the $k_{c.m}$ distribution of $\langle NN \rangle$ clusters works quite well in the case of $^{12}\text{C}(p,pd)^{10}\text{B}$ reaction at separation of s^4p^6 and s^2p^8 states of the ^{10}B .
- TISM allows oneto **explains pp/pn** ratio for SRC in ^{12}C , but **fails** to describe data on the $k_{c.m}$ – distribution (whereas a simple **mean–field** model is OK).
- **ISI@FSI** effects in differential cross sections of the reaction $^{12}\text{C}(p,2pN)^{10}\text{A}$ in kinematics of the **BM@N** SRC experiment are **not negligible**:
 - ◆ suppression factor $R=\text{DWIA}/\text{PWIA} \sim 0.4\text{-}0.8$;
 - ◆ smooth dependence on all scattering angles and momenta except of p_B –dependence
- A study of SRC pairs in $A(p,3N)B$ with separation of the final states of the residual nucleus and BM@N conditions will be very important.
- Is TISM it too simple for SRC?
Further study using the ^{12}C w.f. based on microscopic ab initio calculations /M.Piarulli et al.PRC 107 (2023)/ **is necessary**

THANK YOU FOR ATTENTION!

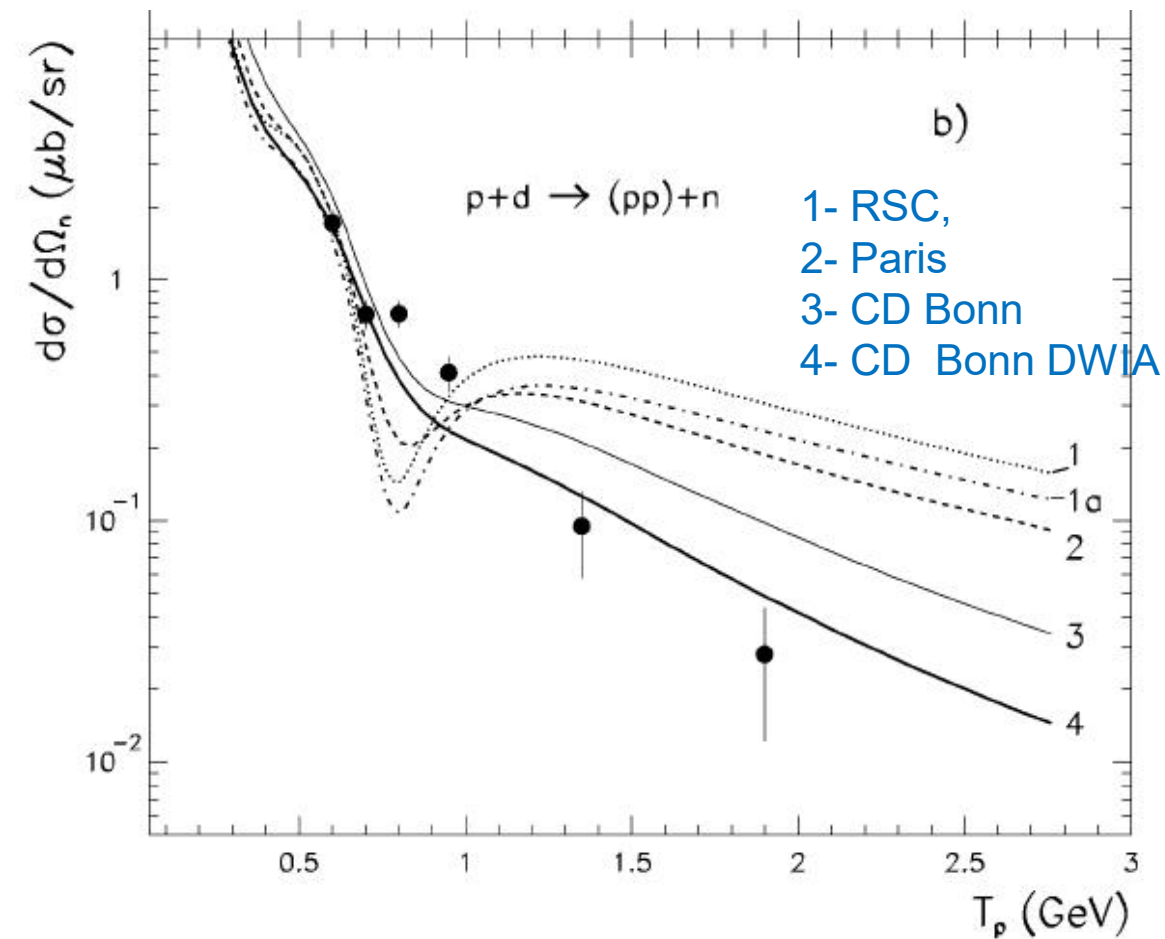
BUCKUP



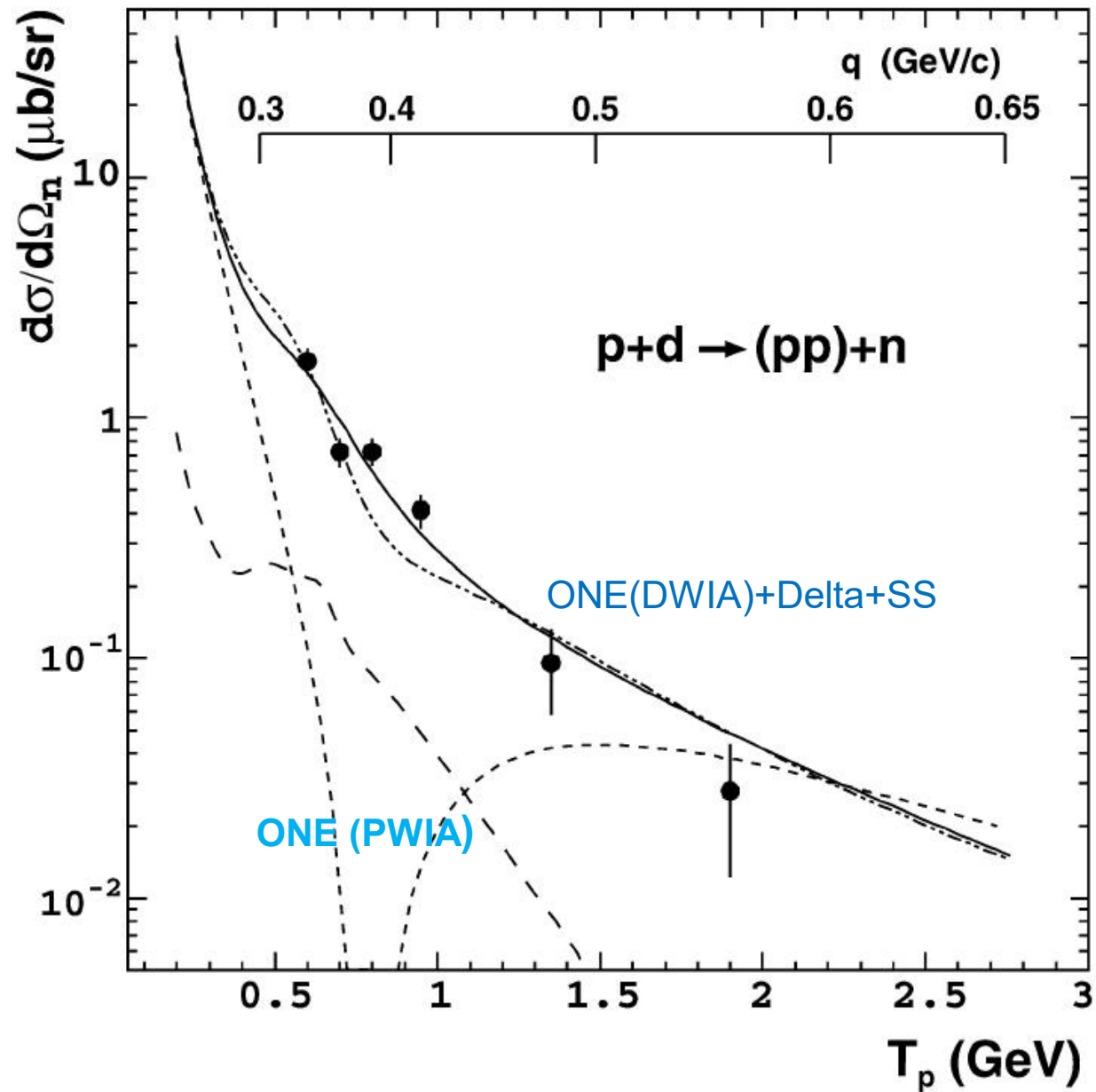
Mechanisms of the breakup reaction $pd \rightarrow (pp)n$. The same mechanisms are used for the reaction $pd \rightarrow dp$.



ONE (DWIA)



ONE+Delta+SS



PARENTAGE COEFFICIENTS of TISM

$$\langle AN_i = 8[f_i](\lambda_i \mu_i) \alpha_i L_i S_i T_i | A - 2N_f [f_f](\lambda_f \mu_f) \alpha_f L_f S_f T_f, \nu \Lambda; N_x L_x S_x T_x : L_i S_i T_i \rangle$$

N_f	6												
$[f_f]$	[442]												
$(\lambda_f \mu_f)$	(22)												
$\nu \Lambda$	00						22						
$N_x L_x$	22						00						
${}^{2T_f+1}2S_f+1L_f$	${}^{13}D_I$	${}^{31}D_I$	${}^{13}D_{II}$	${}^{31}D_{II}$	${}^{13}D_I$	${}^{31}D_I$	${}^{13}D_{II}$	${}^{31}D_{II}$	${}^{13}D_I$	${}^{31}D_I$	${}^{13}D_{II}$	${}^{31}D_{II}$	
PC	$\sqrt{\frac{1}{264}}$	$\sqrt{\frac{1}{264}}$	$-\sqrt{\frac{35}{792}}$	$\sqrt{\frac{35}{792}}$	$-\sqrt{\frac{3}{550}}$	$\sqrt{\frac{3}{550}}$	$-\sqrt{\frac{7}{110}}$	$\sqrt{\frac{7}{110}}$	$-\sqrt{\frac{2}{99}}$	$\sqrt{\frac{2}{99}}$	$-\sqrt{\frac{8}{275}}$	$\sqrt{\frac{8}{275}}$	
	6						7						8
	[442]						[433]						[442]
	(22)						(03)						(13)
	00						11						00
	20						00						11
	${}^{31}S$	${}^{13}S$	${}^{31}S$	${}^{13}S$	${}^{13}D_I$	${}^{31}D_I$	${}^{13}D_{II}$	${}^{31}D_{II}$	${}^{13}D_I$	${}^{31}D_I$	${}^{13}D_{II}$	${}^{31}D_{II}$	
	$-\sqrt{\frac{2}{99}}$	$\sqrt{\frac{2}{99}}$	$-\sqrt{\frac{8}{275}}$	$\sqrt{\frac{8}{275}}$	$\sqrt{\frac{1}{55}}$	$\sqrt{\frac{9}{55}}$	$-\sqrt{\frac{21}{275}}$	$\sqrt{\frac{21}{275}}$	$\sqrt{\frac{3}{110}}$	$\sqrt{\frac{27}{110}}$	$\sqrt{\frac{3}{110}}$	$-\sqrt{\frac{3}{110}}$	

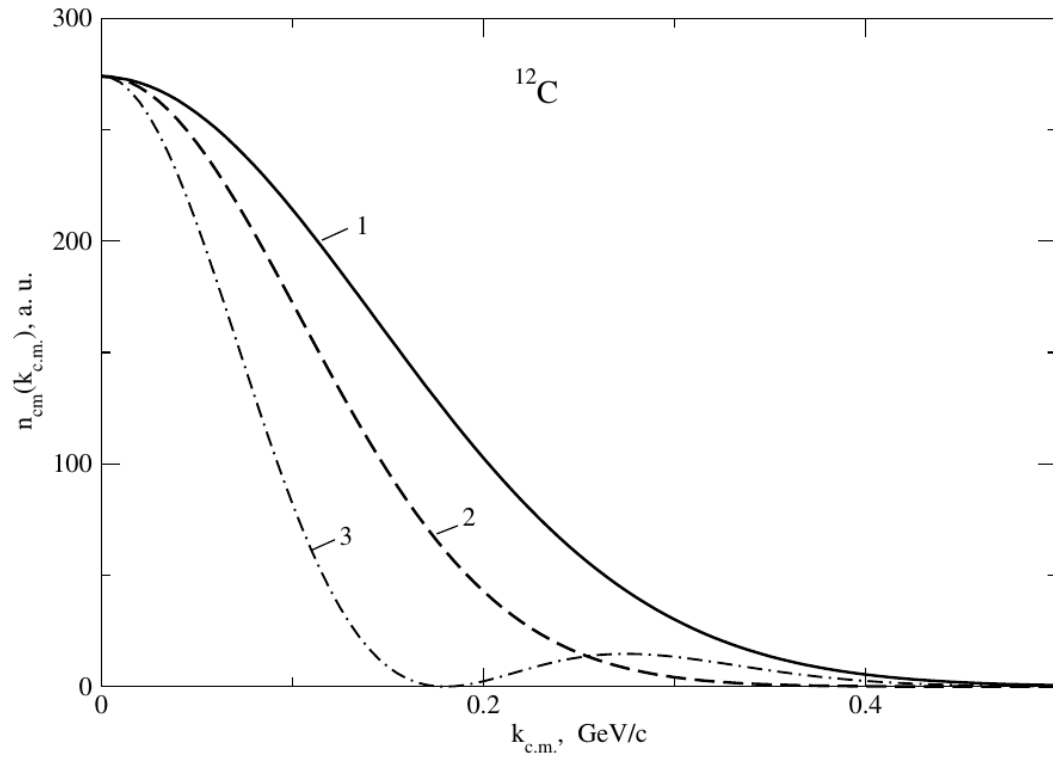
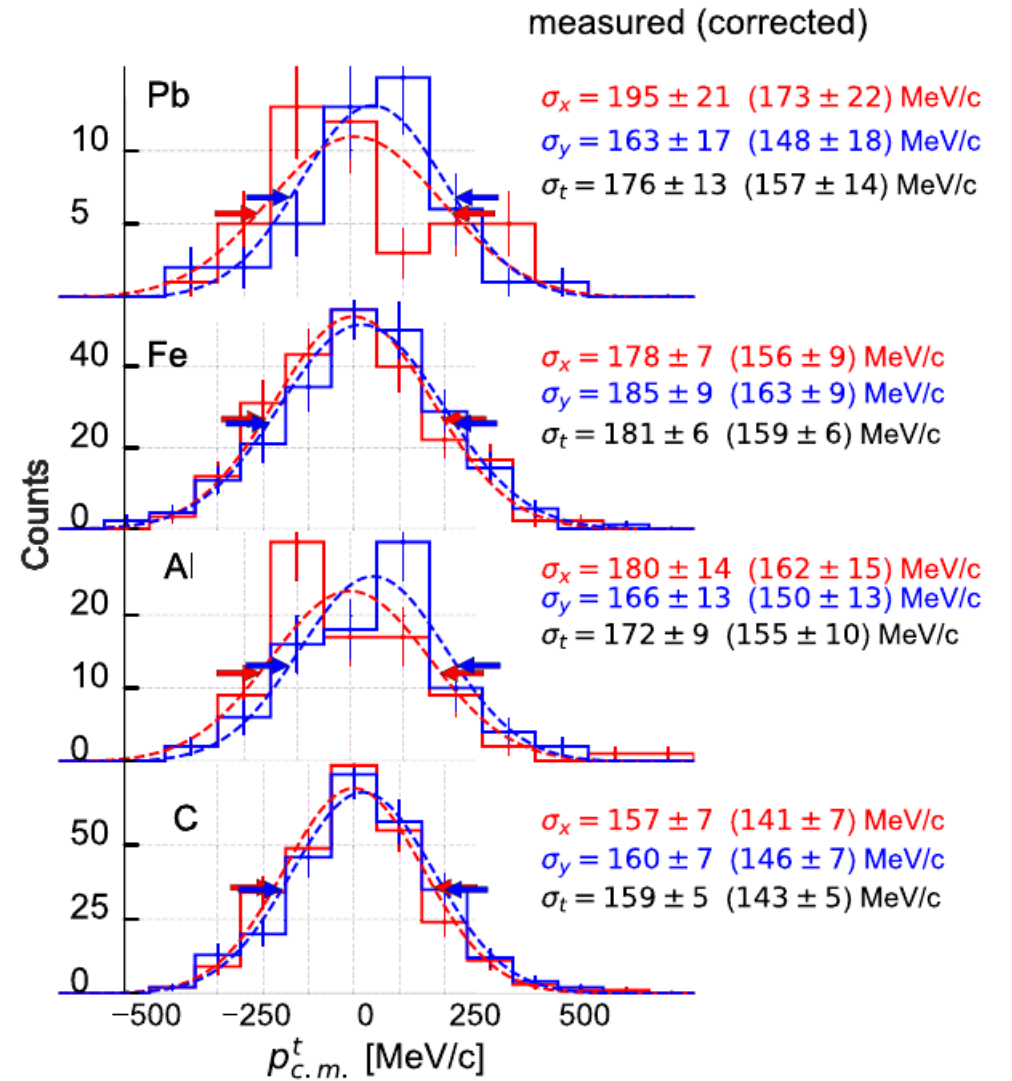


Fig. 3. Distribution over the c.m. momentum of the SCR pair $p_{c.m.}$ in the ^{12}C for the mean-field model with $\alpha_{c.m.} = 0.95 \text{ fm}^2$ (full line) and the TISM wave function squared with $p_0 = 146.9 \text{ MeV}/c$ for the $0S$ -type (dashed), and $2S$ -type (dashed-dotted). All distributions are arbitrary normalized at $p_{c.m.} = 0$ to the same value.



EMC-effect and SRC

O. Hen et al. Rev. Mod. Phys. 89 (2017) 045002

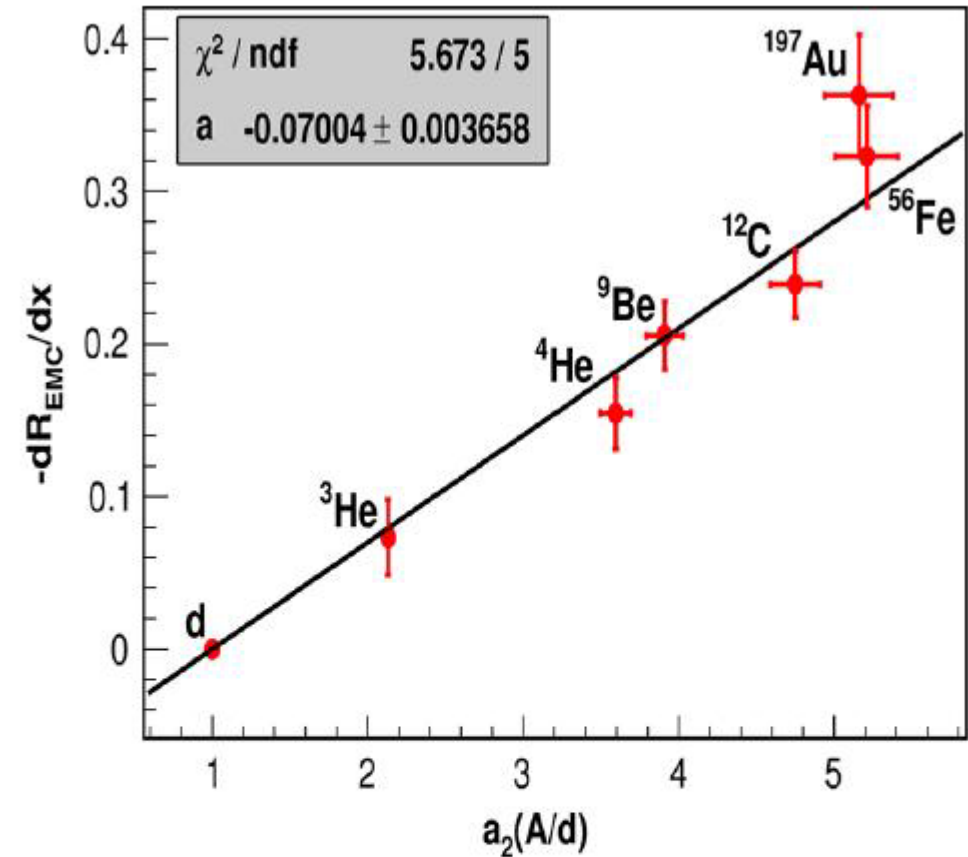
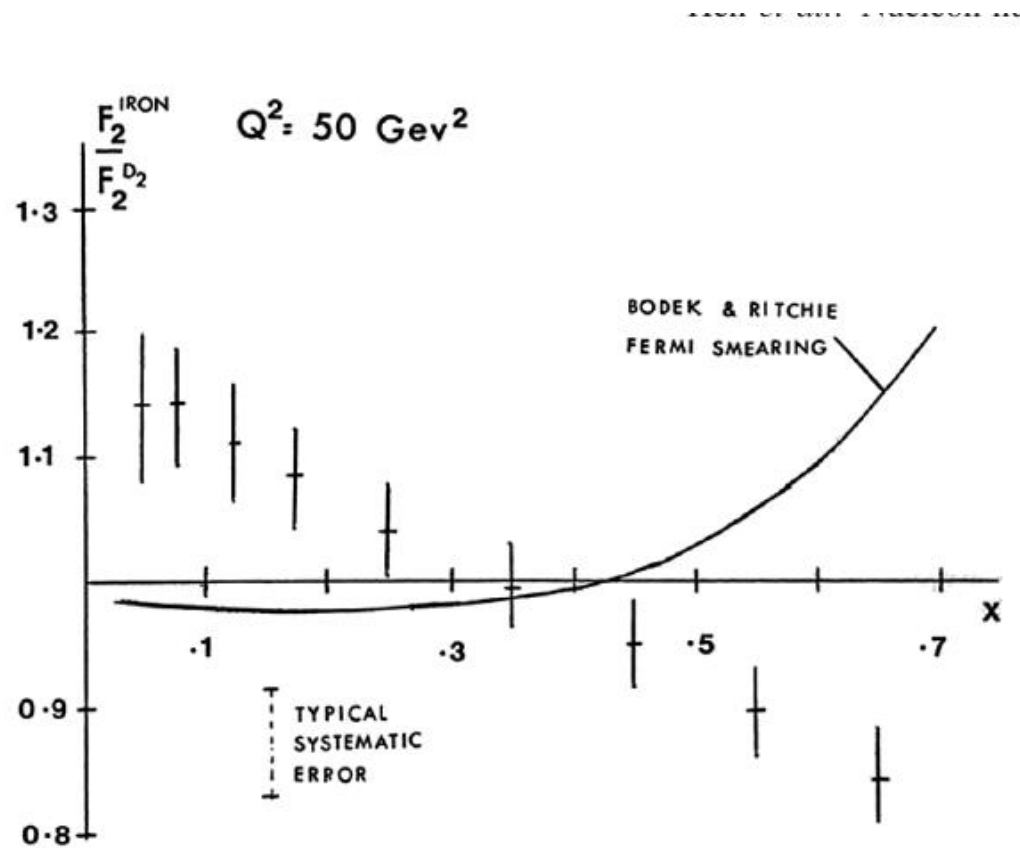


FIG. 34. The slope of the EMC effect (R_{EMC} , ratio of nuclear to deuteron cross section) for $0.35 \leq x_A \leq 0.7$ plotted vs $a_2(A)$, the SRC scale factor (the relative probability that a nucleon belongs to an SRC NN pair) for a variety of nuclei. The fit parameter $a = -0.070 \pm 0.004$ is the intercept of the line constrained to pass through the deuteron (and is therefore also the negative of the slope of that line). From Hen *et al.*, 2013.

— *Center mass motion of SRC NN pairs in nuclei* —————

E.O. Cohen et al. Phys.Rev.Lett. **121** (2018) 092501

Hard breakup of a pp-SRC pair in a hard two-nucleons knockout
 $A(e, e'pp)$ reactions at recoil proton momentum $p_{rec} \geq 350$ MeV/c
assuming factorization

$$d\sigma(e, e'pp) \sim n_{SRC}(\vec{p}_1, \vec{p}_2) \approx n_{c.m.}^A(\vec{p}_{c.m.}) n_{rel}^{NN}(\vec{p}_{rel})$$

$n_{c.m.}^A(\vec{p}_{c.m.})$ is approximated by the 3-D Gaussian $g(x)g(y)g(z)$,

$$g(x) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left[-\frac{x^2}{2\sigma^2}\right]$$

^{12}C :

$$\sigma_x \approx \sigma_y \approx \sigma_z = (145 \pm 5) \text{ MeV}/c$$

$$\text{i.e. } p_0 = \sqrt{2}(145 \pm 5) \text{ MeV}/c = (205 \pm 7) \text{ MeV}/c$$

$$S_A^x = \binom{A}{x}^{1/2} \sum_{\mathcal{L} \bar{J} \bar{M}} (J_B M_B \bar{J} \bar{M} | J_A M_A) (\Lambda M_\Lambda J_x M_x | \bar{J} \bar{M})$$

$$(T_B M_{T_B} T_x M_{T_x} | T_A M_{T_A}) U(\Lambda L_x J S_x; \mathcal{L} J_x)$$

$$[(2L_A + 1)(2S_A + 1)(2J_B + 1)(2\bar{J} + 1)]^{1/2} \left\{ \begin{array}{ccc} L_B & S_B & I_B \\ L & S_x & \bar{J} \\ L_A & S_A & I_A \end{array} \right\}$$

$$\langle A N_A [f_A] (\lambda_A \mu_A) \alpha_A L_A S_A T_A |$$

$$| A - x N_B [f_B] (\lambda_B \mu_B) \alpha_B L_B S_B T_B; \nu \Lambda, x N_x [f_x] (\lambda_x \mu_x) \alpha_x L_x S_x T_x (\mathcal{L}) : L_A S_A T_A \rangle$$

Theoretical model: C.Ciofi degli Atti, S.Simula, PRC 53 (1996) 1689

$$n_{cm}(p) = \left(\frac{\alpha}{\pi}\right) \exp[-\alpha p^2] \quad (3)$$

$$\alpha = 1 \text{ fm}^2 \text{ or } p_0 = \hbar/\sqrt{\alpha} = 197 \text{ MeV}/c$$

From the deuteron knock-out $^{12}\text{C}(p, pd)^{10}\text{B}$ from p-shell ($|^{10}\text{B}\rangle = |s^4p^6\rangle$) (J.Erö et al., 1981) one has

$$p_0 = 155 \text{ MeV}/c$$

(not for 1S-wave distribution in Eq.(3), but for 2S Eq.(1)!)

$$\underline{^4\text{He}}: \alpha = 2.4 \text{ fm}^2 \text{ or } p_0 = \hbar/\sqrt{\alpha} = 127.3 \text{ MeV}/c,$$

that is compatible with $p_0 = (144.6 \pm 18.2) \text{ MeV}/c$ from the deuteron knockout $^{12}\text{C}(p, pd)^{10}\text{B}$ from the α -core, (J.Erö et al., NPA 372, 1981), $|^{10}\text{B}\rangle = s^2p^8\rangle$