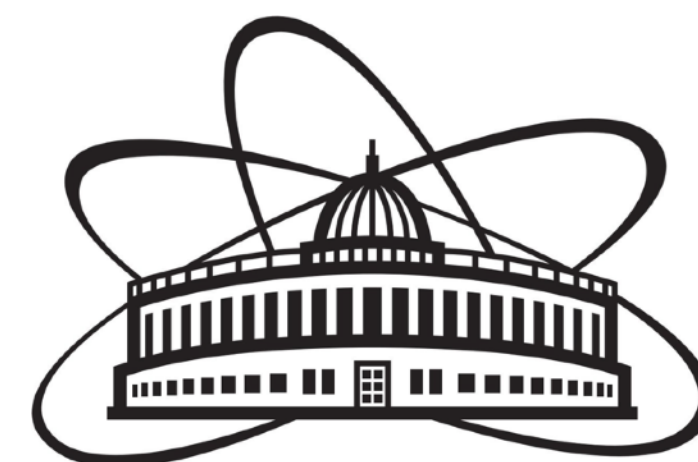


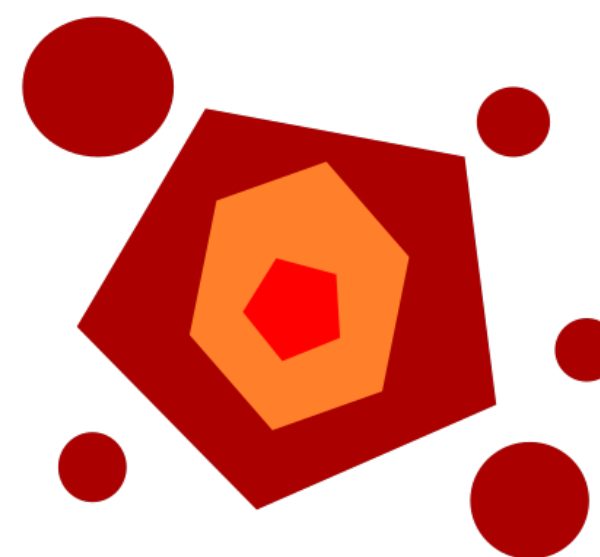
# Cluster and hypernucleus production in heavy-ion collisions

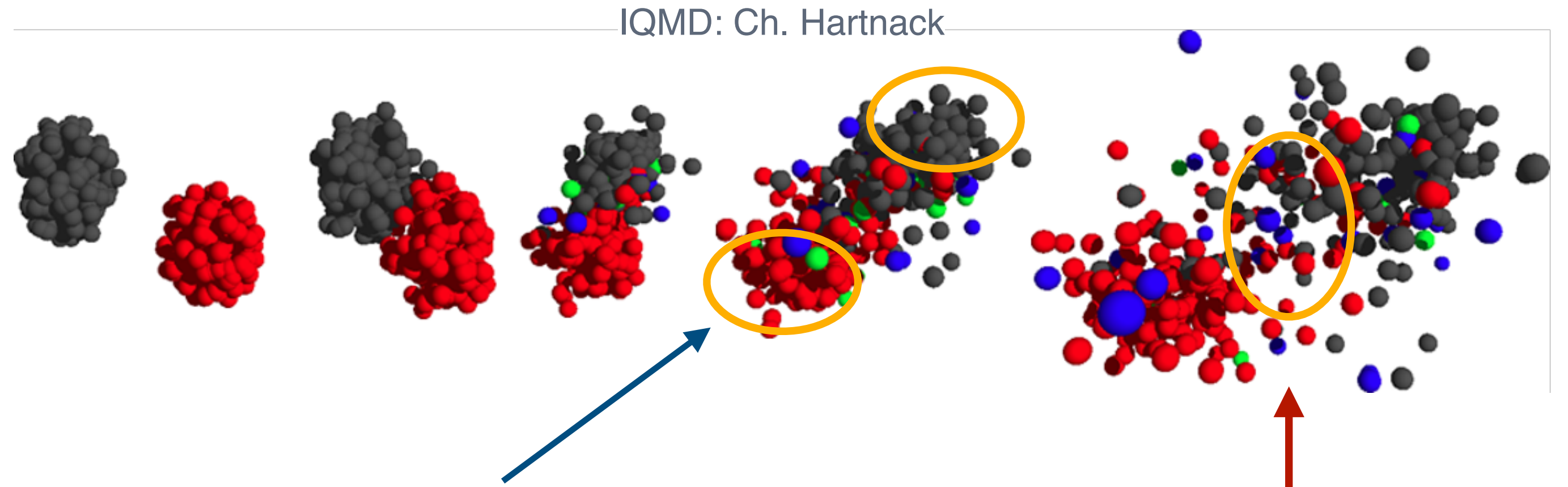
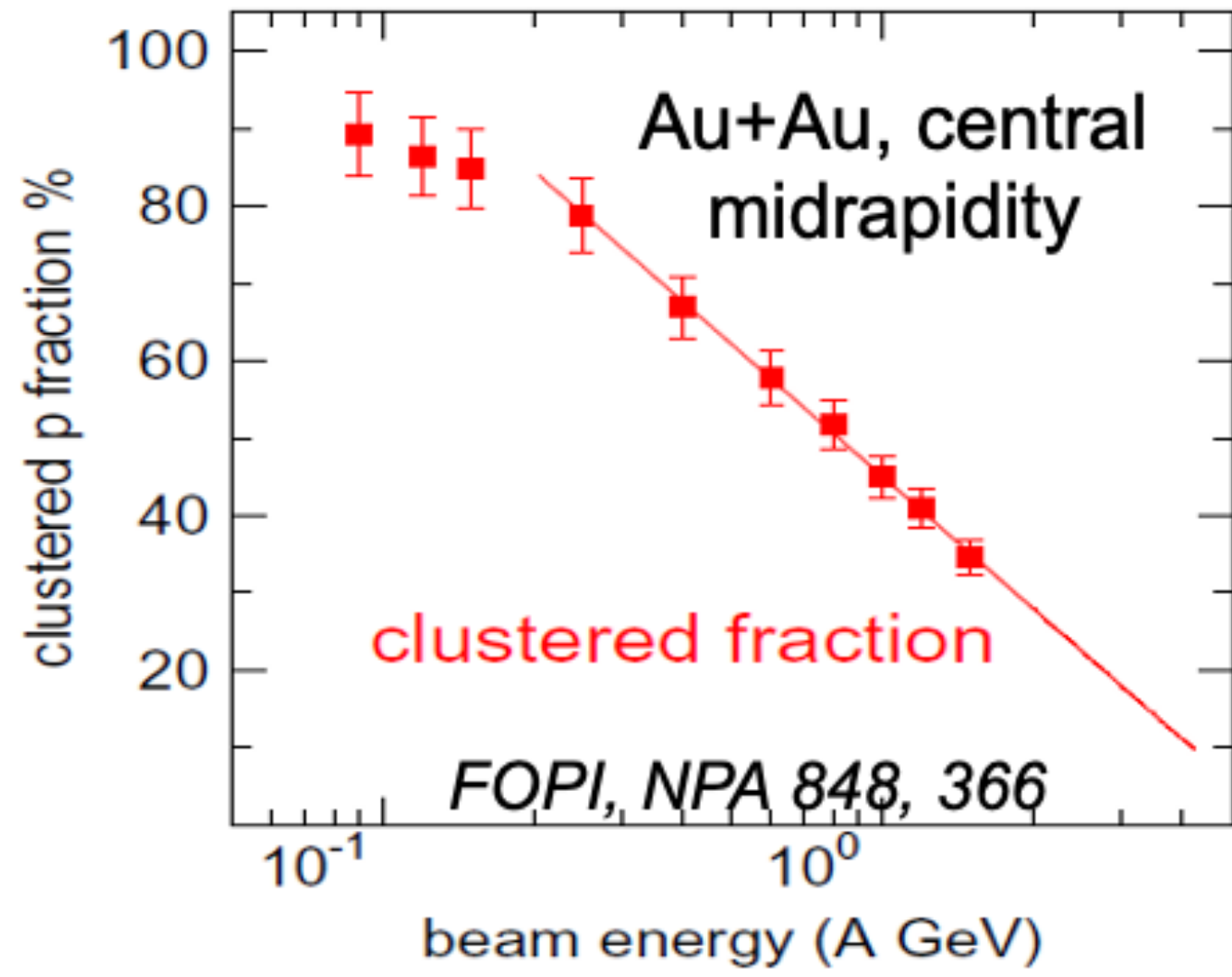
Infinite and Finite Nuclear Matter – 2023

V. Kireyeu for the PHQMD team



**HFHF**  
Helmholtz Forschungsakademie Hessen für FAIR





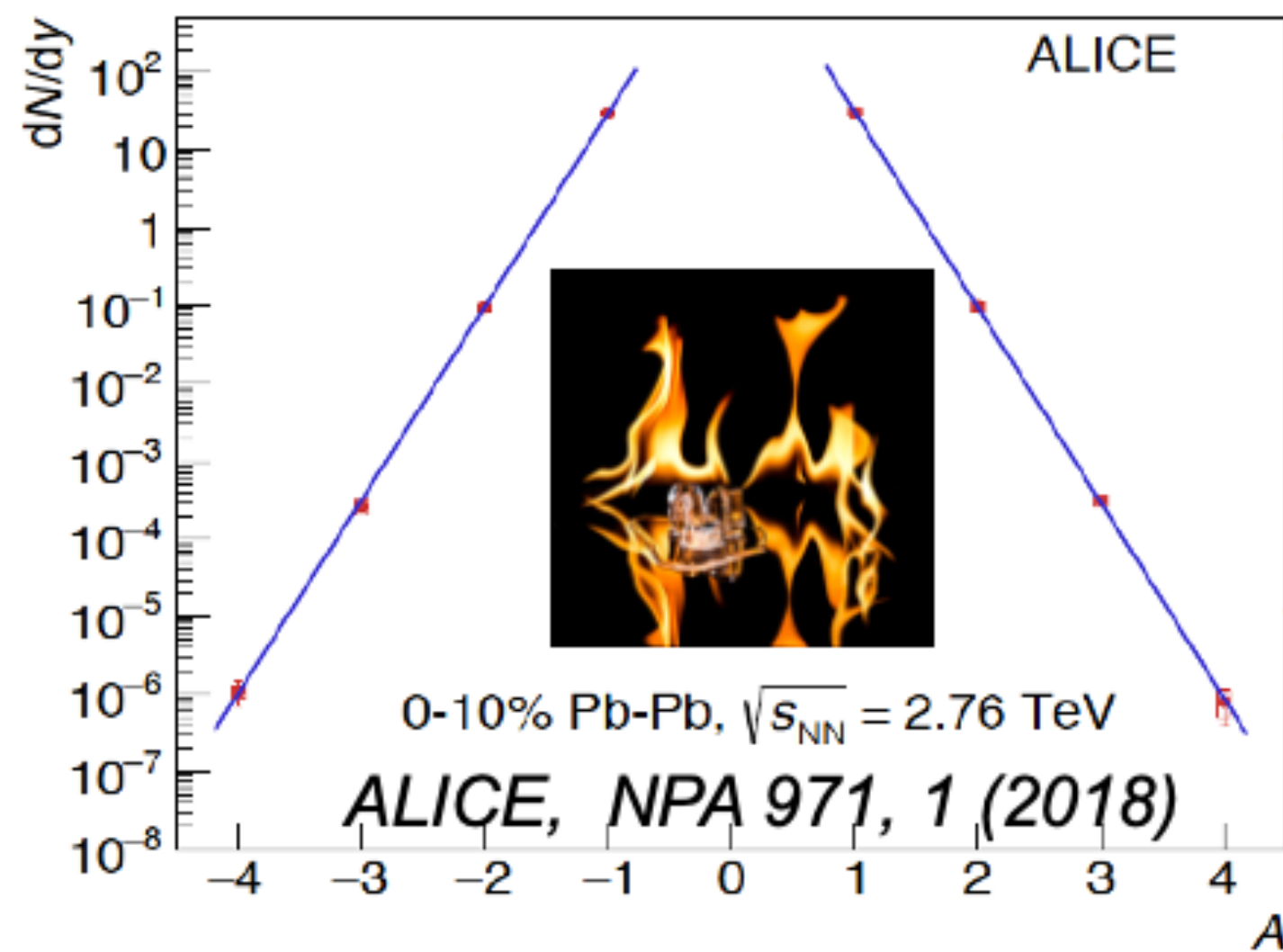
**Projectile/target spectators:** heavy cluster formation

**Midrapidity:** light clusters

**(Anti)hypernuclei** production:

at mid-rapidity by  $\Lambda$  coalescence during expansion

at projectile/target rapidity by re-scattering/absorption of  $\Lambda$  by spectators



← **«Ice in a fire» puzzle:** how the weakly bound objects can be formed and survive in a hot environment?

# Modelling of cluster formation in HIC

## Statistical models

- Production of nuclei depending on  $T$  and  $\mu_B$  at chemical freeze-out & particle mass

## Coalescence models

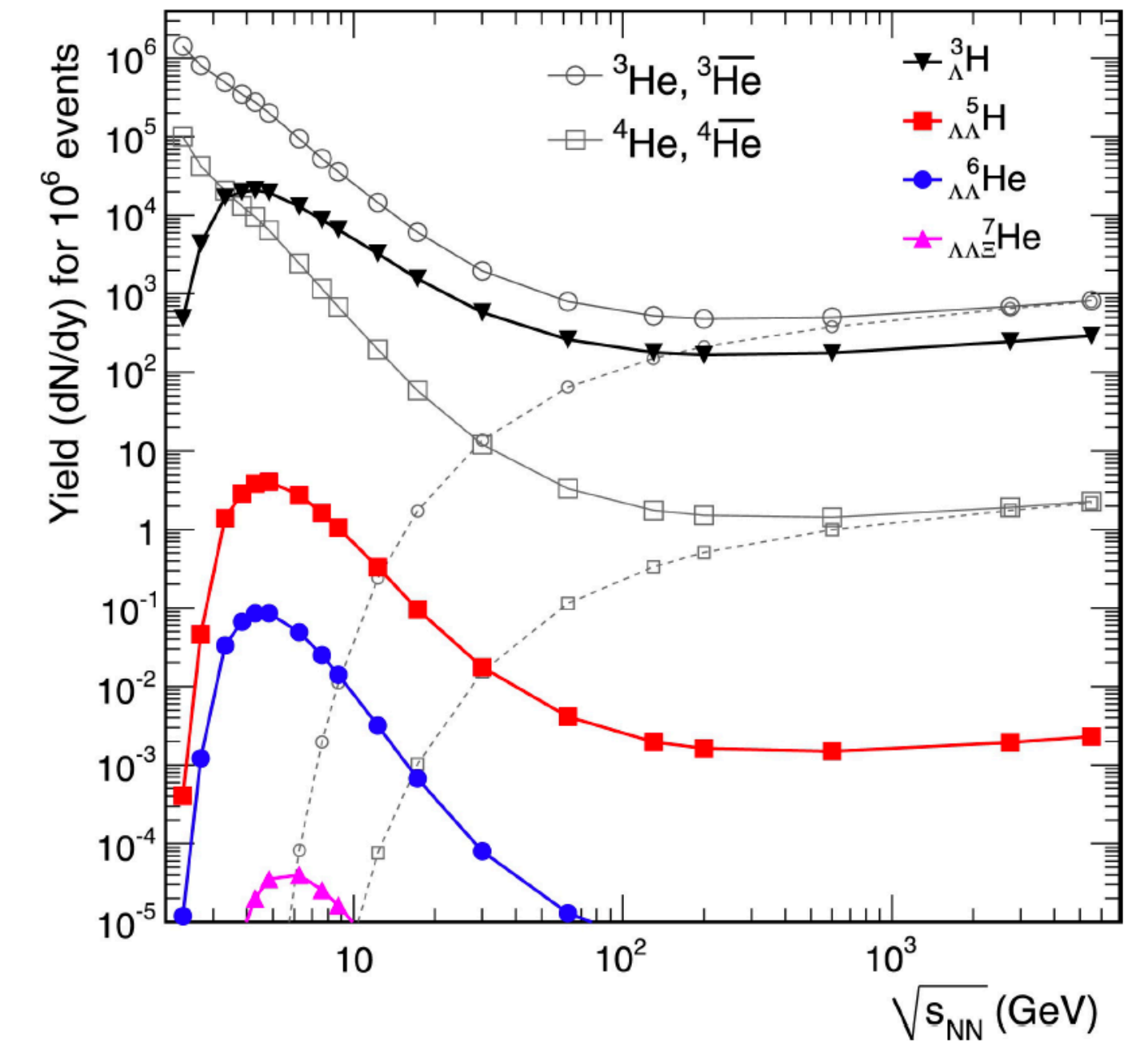
- Formation of nuclei by nucleons & hyperons that are close in coordinate and momentum spaces at freeze-out time

=> no dynamical cluster formation during time evolution

=> no information on the dynamics of clusters formation & microscopic origin

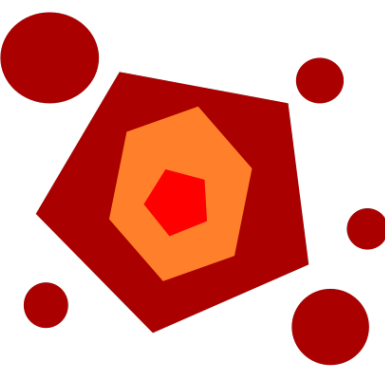
In order to understand the microscopic **origin of cluster formation** one needs a realistic model for the **dynamical time evolution** of the HIC

**Transport models** — dynamical modelling of cluster formation based on interactions:  
via potential interaction – **‘potential’ mechanism**  
by scattering – **‘kinetic’ mechanism**



A. Andronic et al., Phys. Lett. B697 (2011) 203-207.

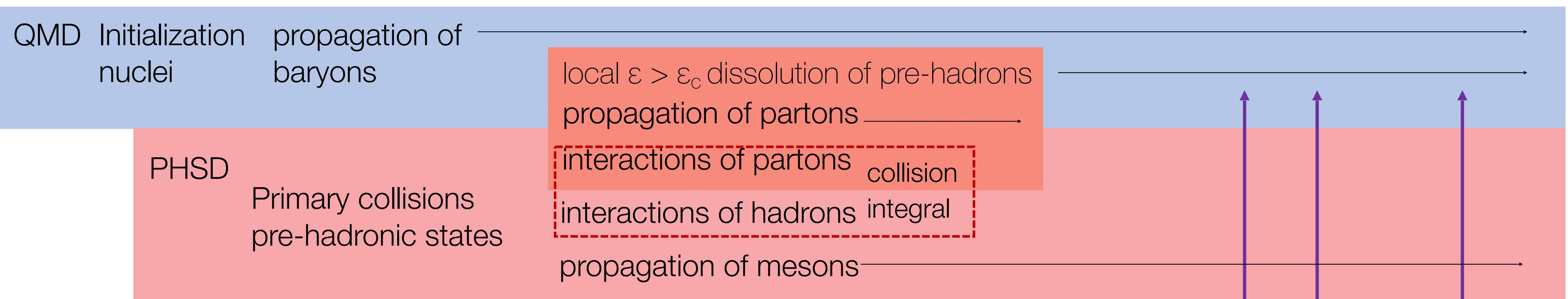
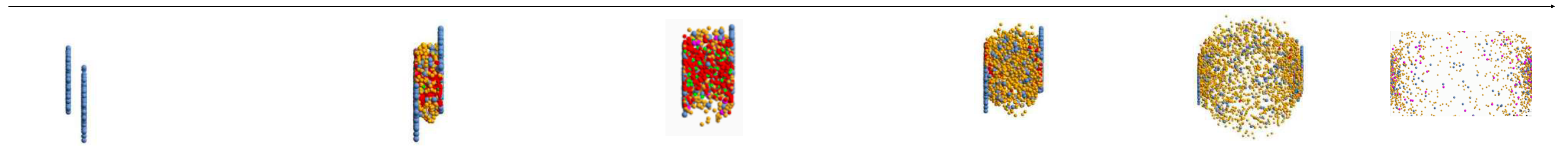
# Parton-Hadron-Quantum-Molecular Dynamics



= n-body microscopic transport approach for the description of heavy-ion dynamics with dynamical cluster formation from low to ultra-relativistic energies

Relativistic considerations + Correlations between nucleons + Cluster recognition

Initial A+A collisions    Formation of QGP    Partonic phase    Hadronization    Hadronic phase



MST or SACA



J. Aichelin et al., PRC 101 (2020) 044905

PHSD: W. Cassing, E. Bratkovskaya, PRC 78 (2008) 034919; NPA831 (2009) 215; W. Cassing, EPJ ST 168(2009)

Potential mechanism for cluster production

# Minimum Spanning Tree (MST)

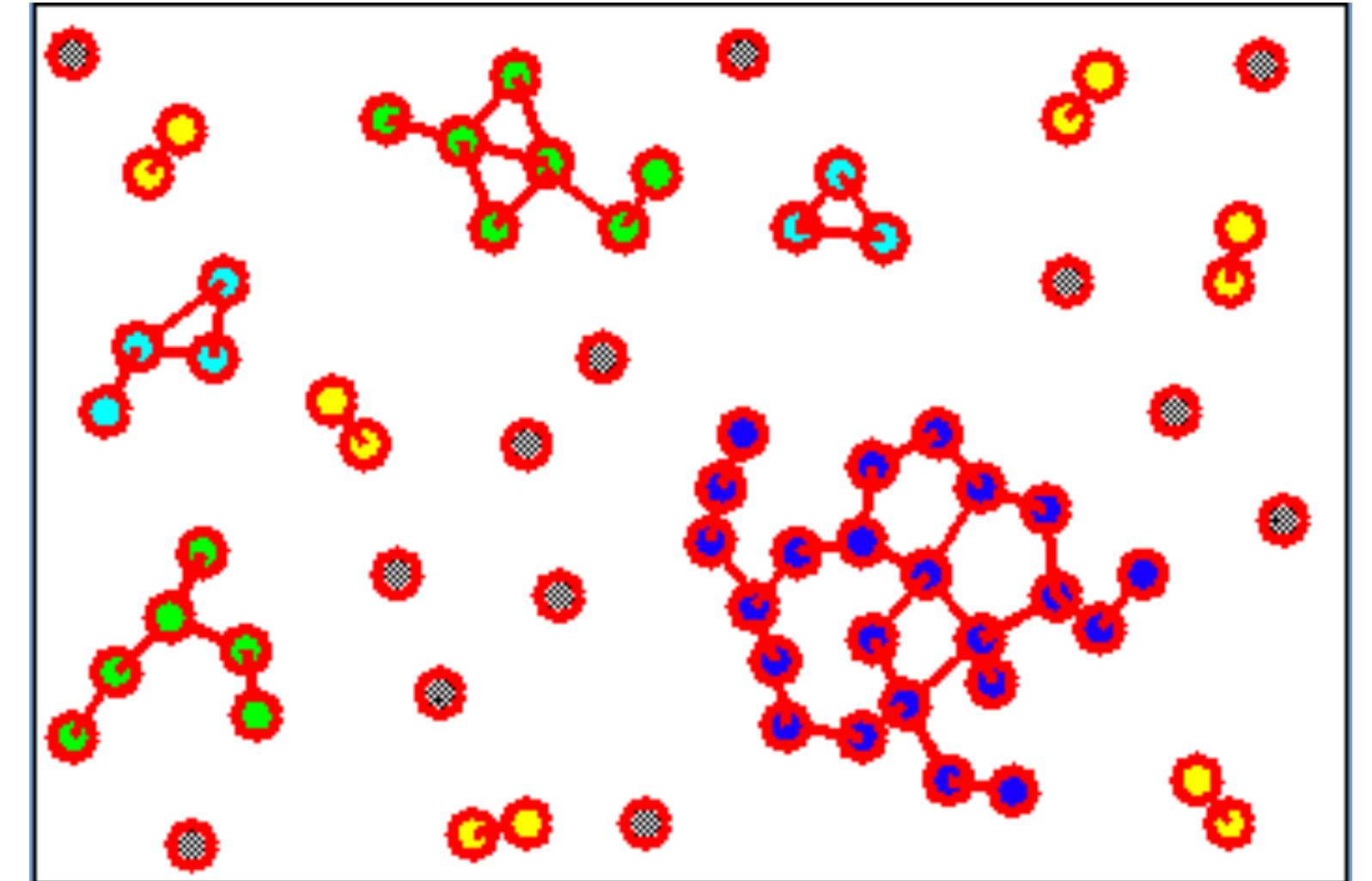
Cluster criterion: distance of nuclei

Algorithm: search for accumulations of particles in coordinate space

1. Two particles  $i$  &  $j$  are bound if:

$$|r_i - r_j| < 4.0 \text{ fm}$$

2. Particle is bound to cluster if bound with at least one particle of cluster



Remark: additional momentum cuts lead to a small changes: particles with large relative momentum are mostly not at the same position (V. Kireyeu, Phys.Rev.C 103 (2021) 5)

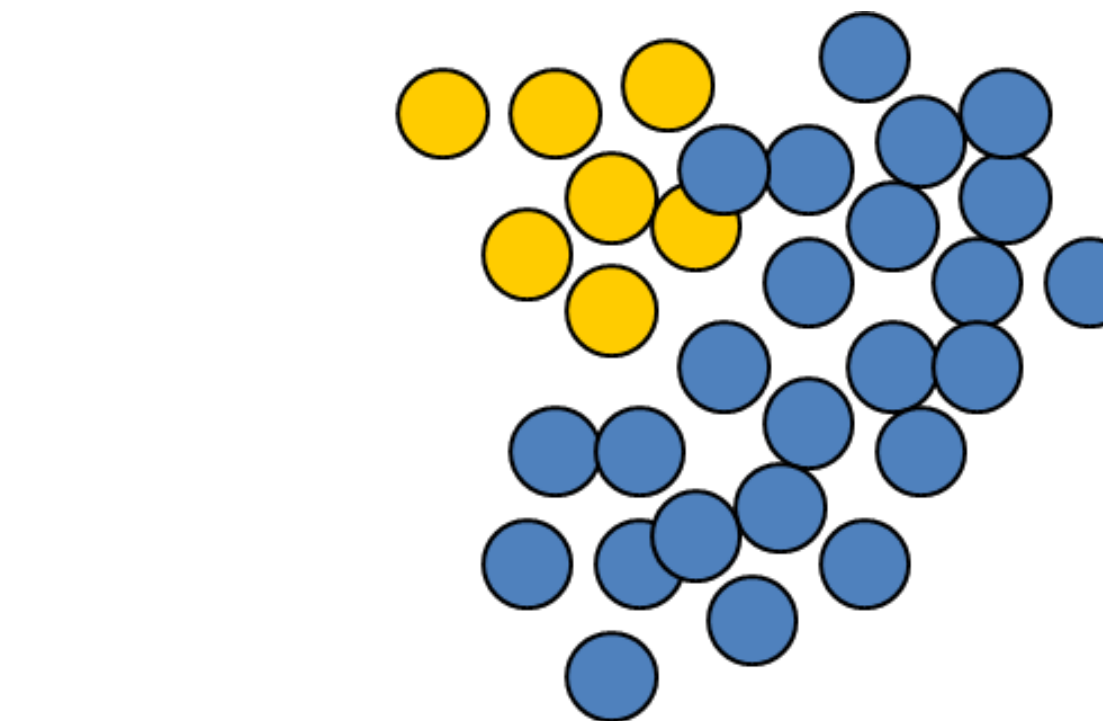
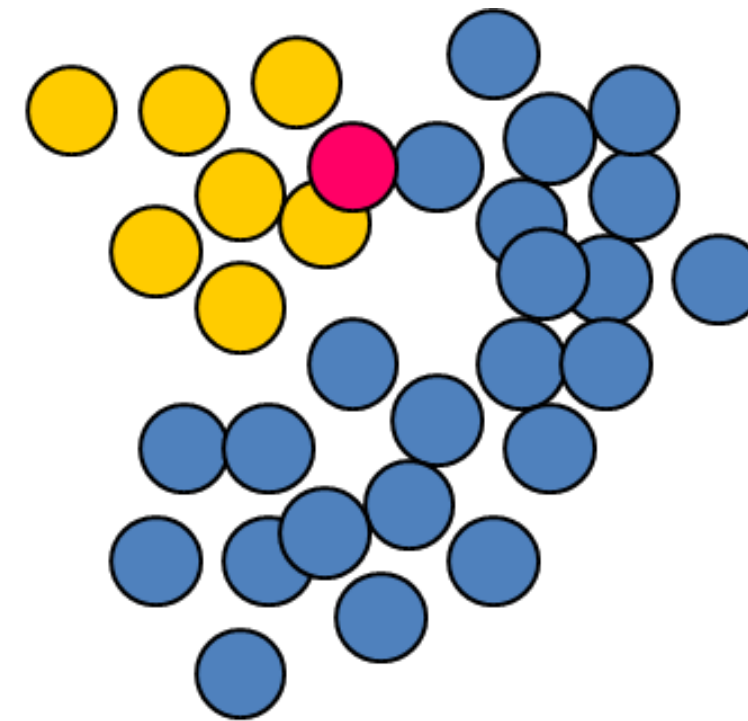
# Simulated Annealing Clusterization Algorithm (SACA)

Based on ideas by Dorso and Randrup  
(Phys.Lett. B301 (1993) 328)

- Take the positions and momenta of all nucleons at time  $t$
- Combine them in all possible ways into all kinds of clusters or leave them as single nucleons
- Neglect the interaction among clusters
- Choose that configuration which has the highest binding energy:



$$E = E_{kin}^1 + E_{kin}^2 + V^1 + V^2$$



$$E' = E_{kin}^{1'} + E_{kin}^{2'} + V^{1'} + V^{2'}$$

If  $E' < E$  take a new configuration

If  $E' > E$  take the old configuration with a probability depending on  $E' - E$

Repeat this procedure many times  $\rightarrow$  **Leads automatically to finding of the most bound configurations**  
(realized via a Metropolis algorithm)

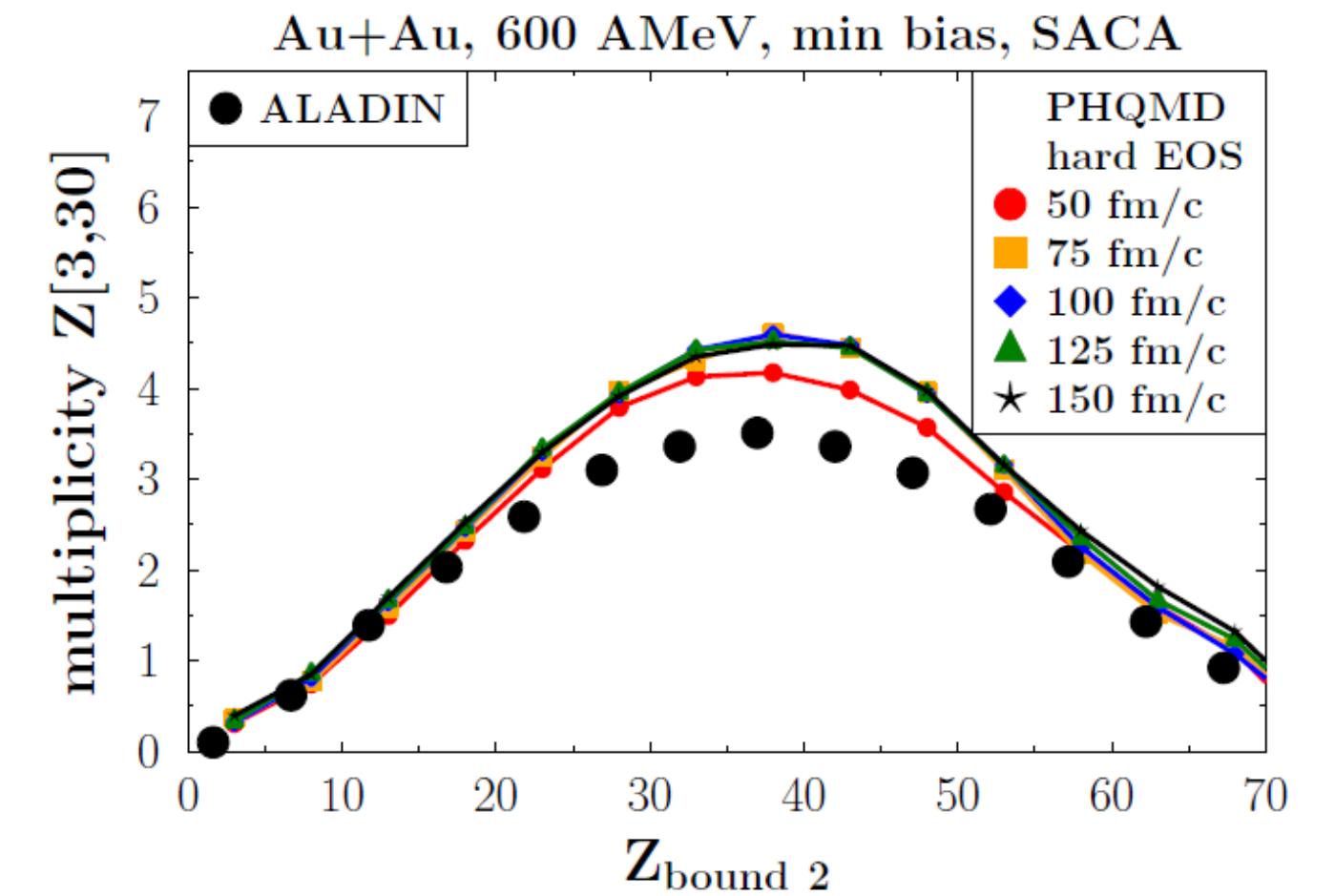
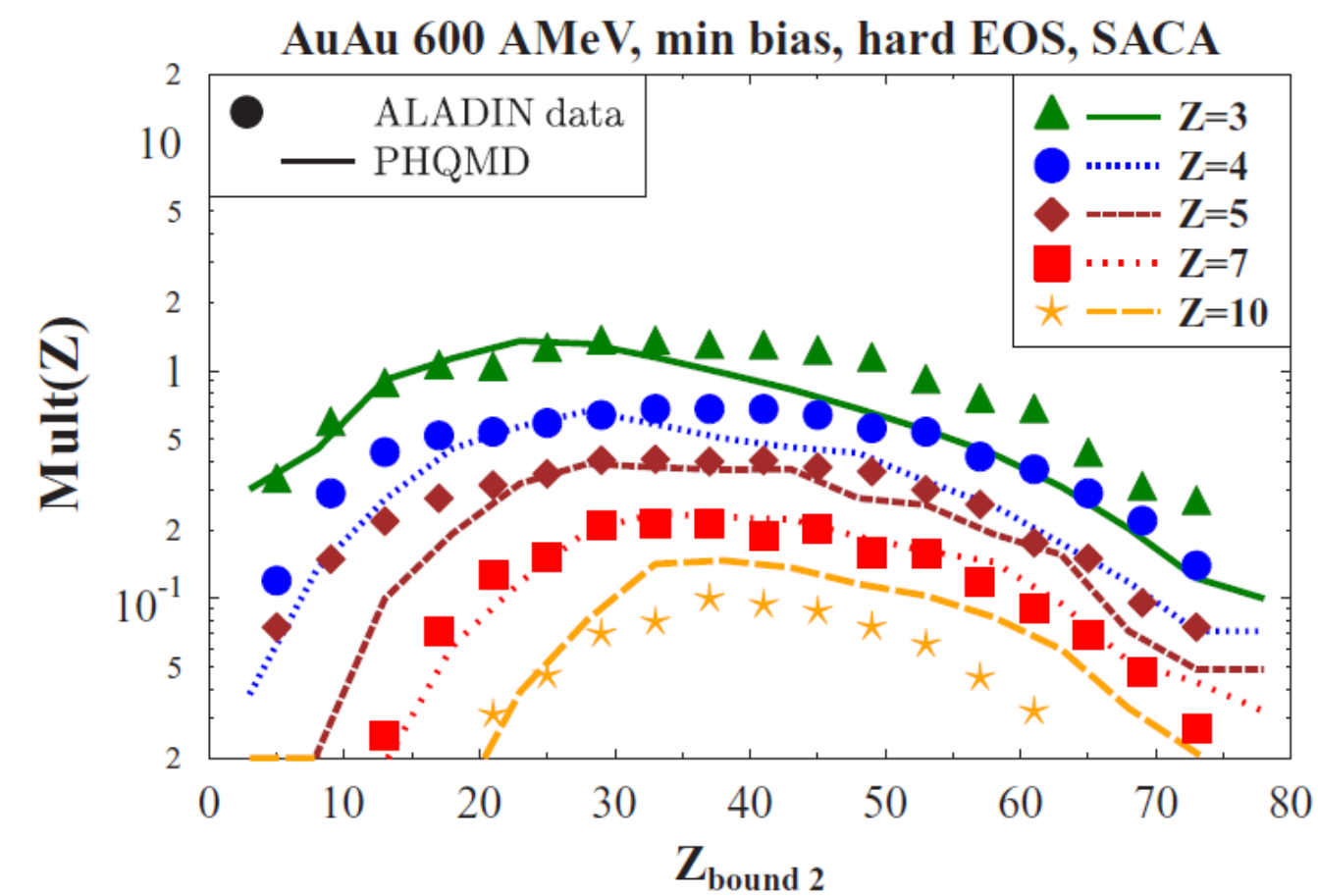
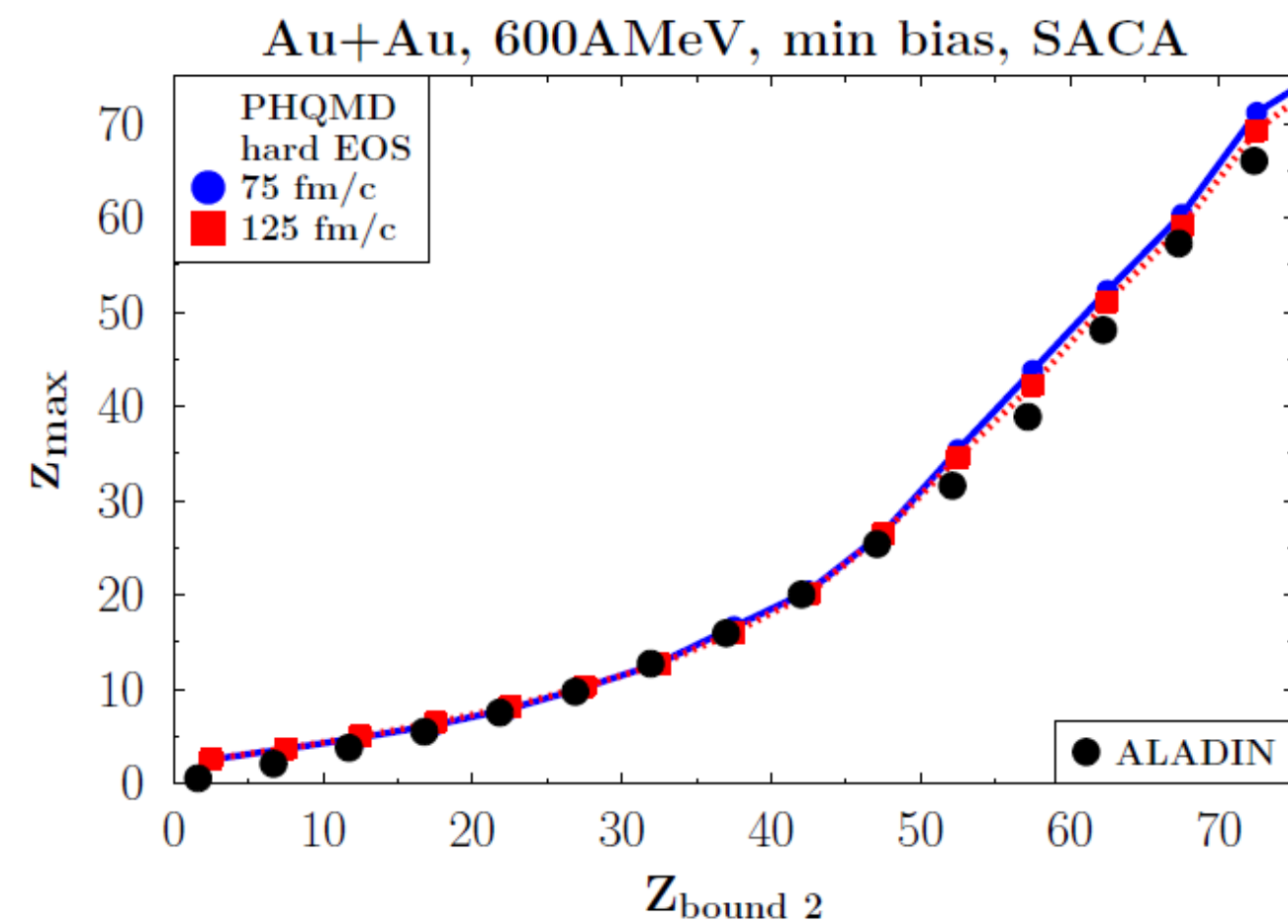
R. K. Puri, J. Aichelin, PLB301 (1993) 328, J.Comput.Phys. 162 (2000) 245-266;

P.B. Gossiaux, R. Puri, Ch. Hartnack, J. Aichelin, Nuclear Physics A 619 (1997) 379-390

# Heavy clusters in PHQMD

PHQMD with SACA shows an agreement with ALADIN data for very complex cluster observables as

- Largest clusters ( $Z_{\text{bound}}$ )
- Multiplicity ( $Z_{\text{bound}}$ )
- Energy independent ‘rise and fall’



J. Aichelin et al., PRC 101 (2020) 044905



# Cluster stability over time

QMD can not describe clusters as ‘quantum objects’

the cluster **quantum ground state** has to respect a minimal average kinetic energy of the nucleons while **the semi-classical** (QMD) ground state - not!

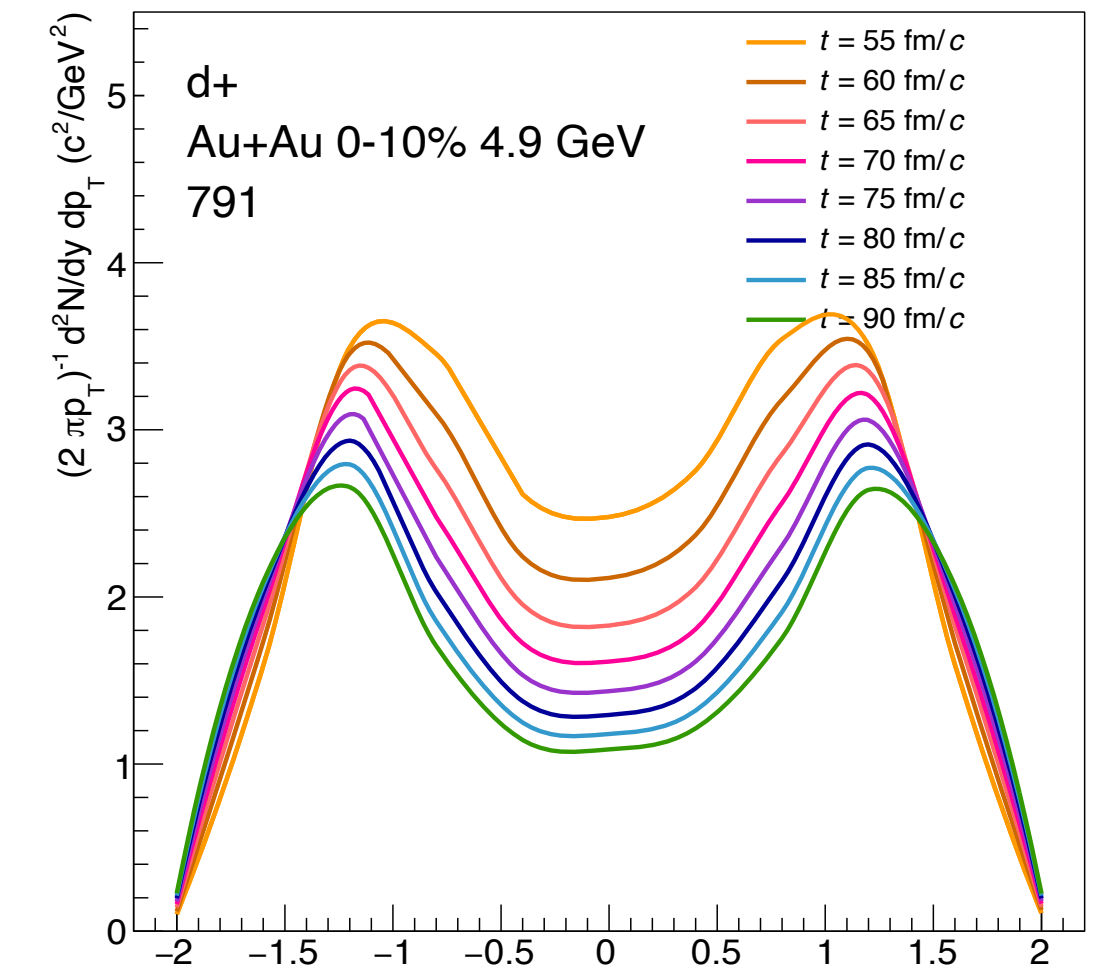
nucleons may still be emitted from the QMD clusters while in the corresponding quantum system this is not possible

thus, a cluster which is “bound” at time  $t$  can **spontaneously** dissolve at  $t + \Delta t$

= **QMD clusters are not fully stable over time:**

the multiplicity of clusters is time dependent

the form of the final rapidity,  $p_T$  distribution and ratio of particles do not change with time



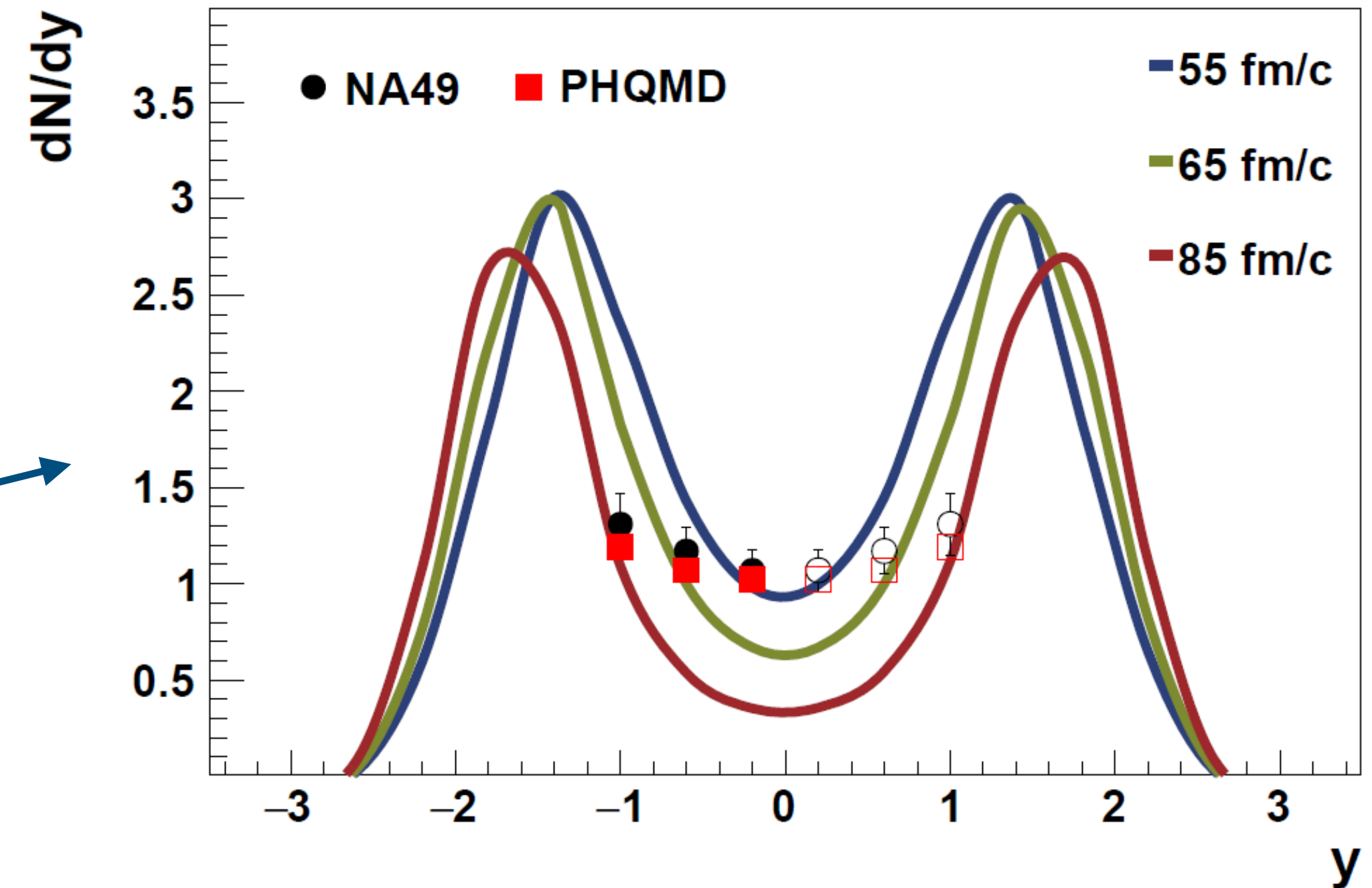
## How to stabilize QMD clusters?

**Scenario 1:** S. Gläsel et al., PRC 105 (2022) 1

PHQMD results are taken at ‘**physical time**’ :

$$t = t_0 \cosh(y)$$

where  $t_0$  is the time selected as a best description of the cluster multiplicity at  $y=0$



# Cluster stability over time

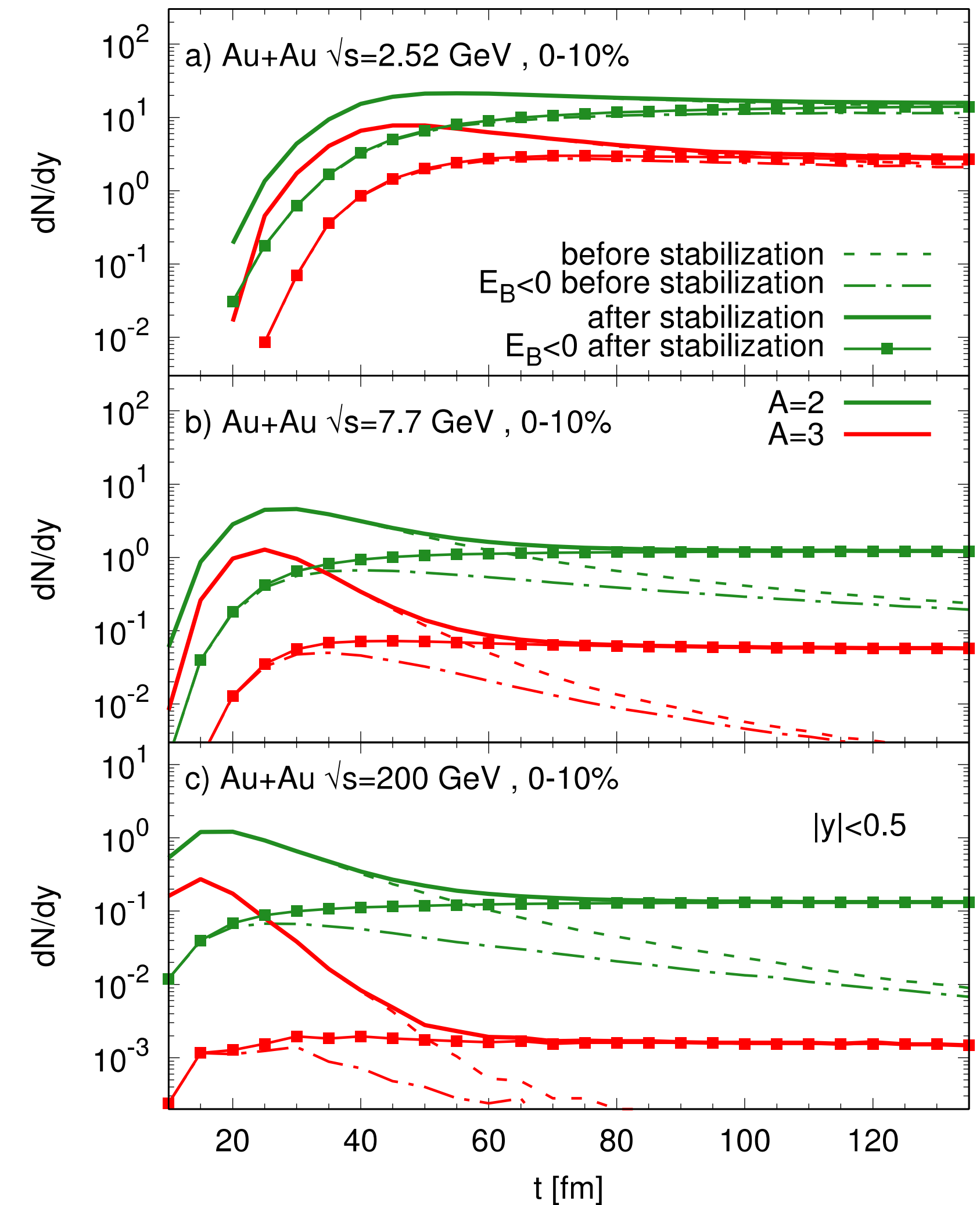
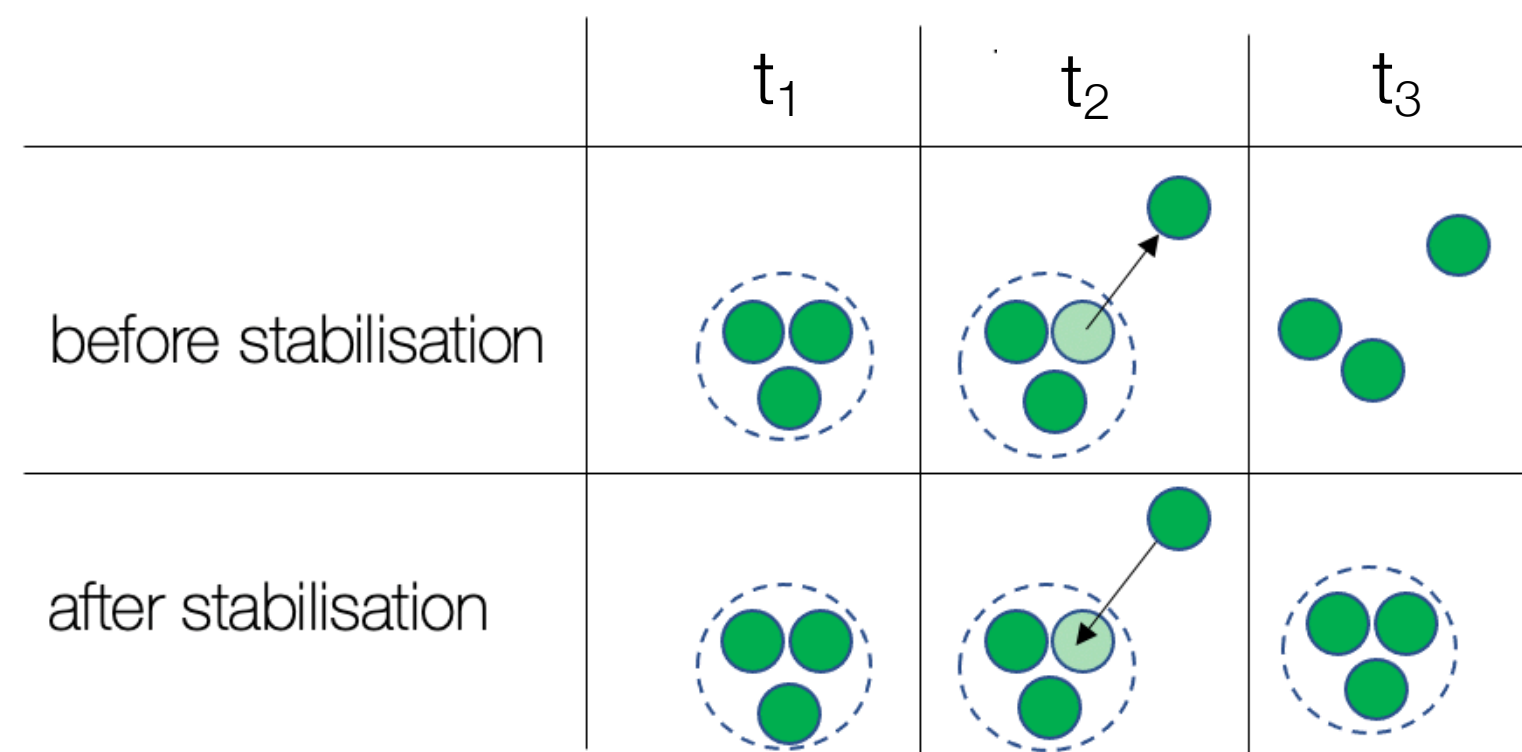
## Scenario 2:

G. Coci et al., in preparation

### Stabilisation Procedure:

- consider asymptotic state: clusters and free nucleons
- For each nucleon in MST track the **freezeout-time** = time at which the last collision occurred
- Recombine nucleons into clusters with  $E_B < 0$  if time of cluster disintegration is larger than nucleon freeze-out time

Allows to recover most of “lost” clusters



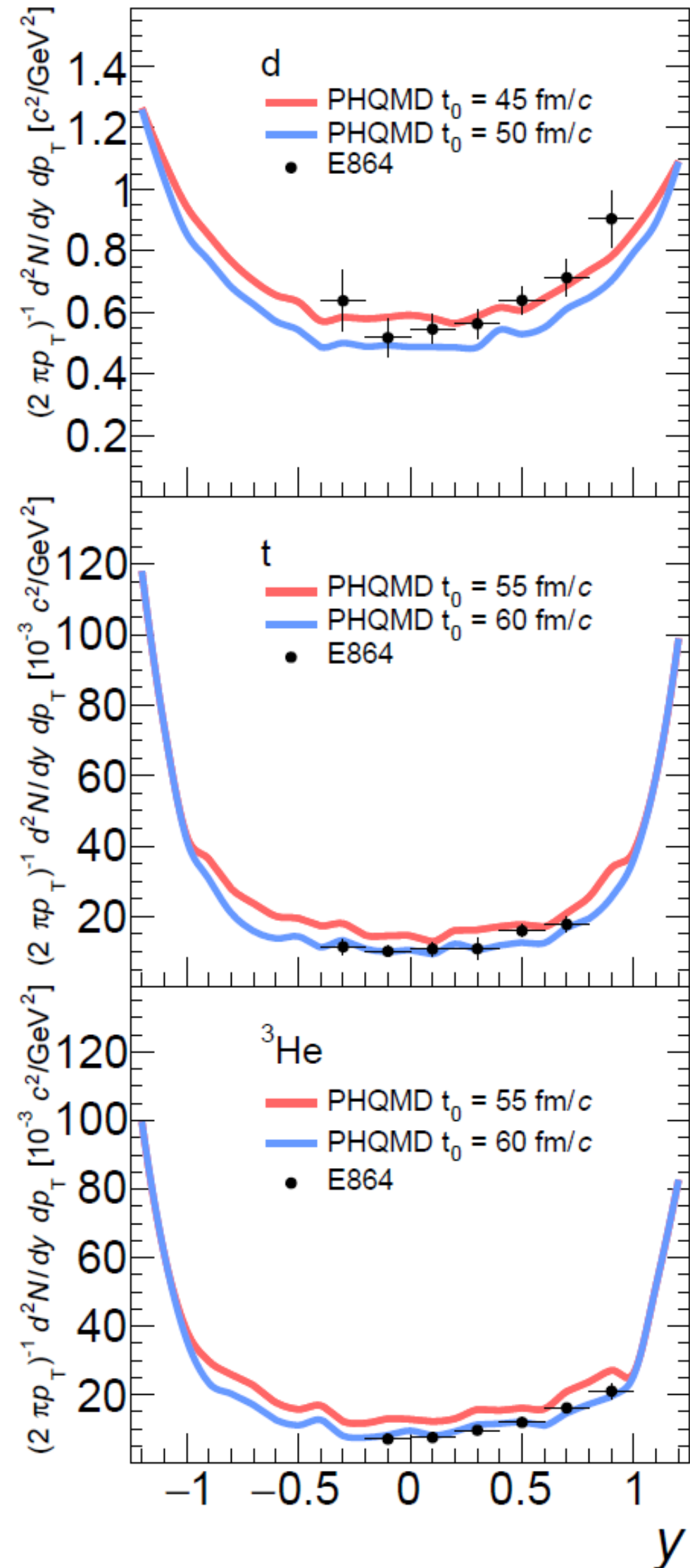
# Cluster production in HICs at AGS energies

Au+Pb@10.6 AGeV

Scenario 1

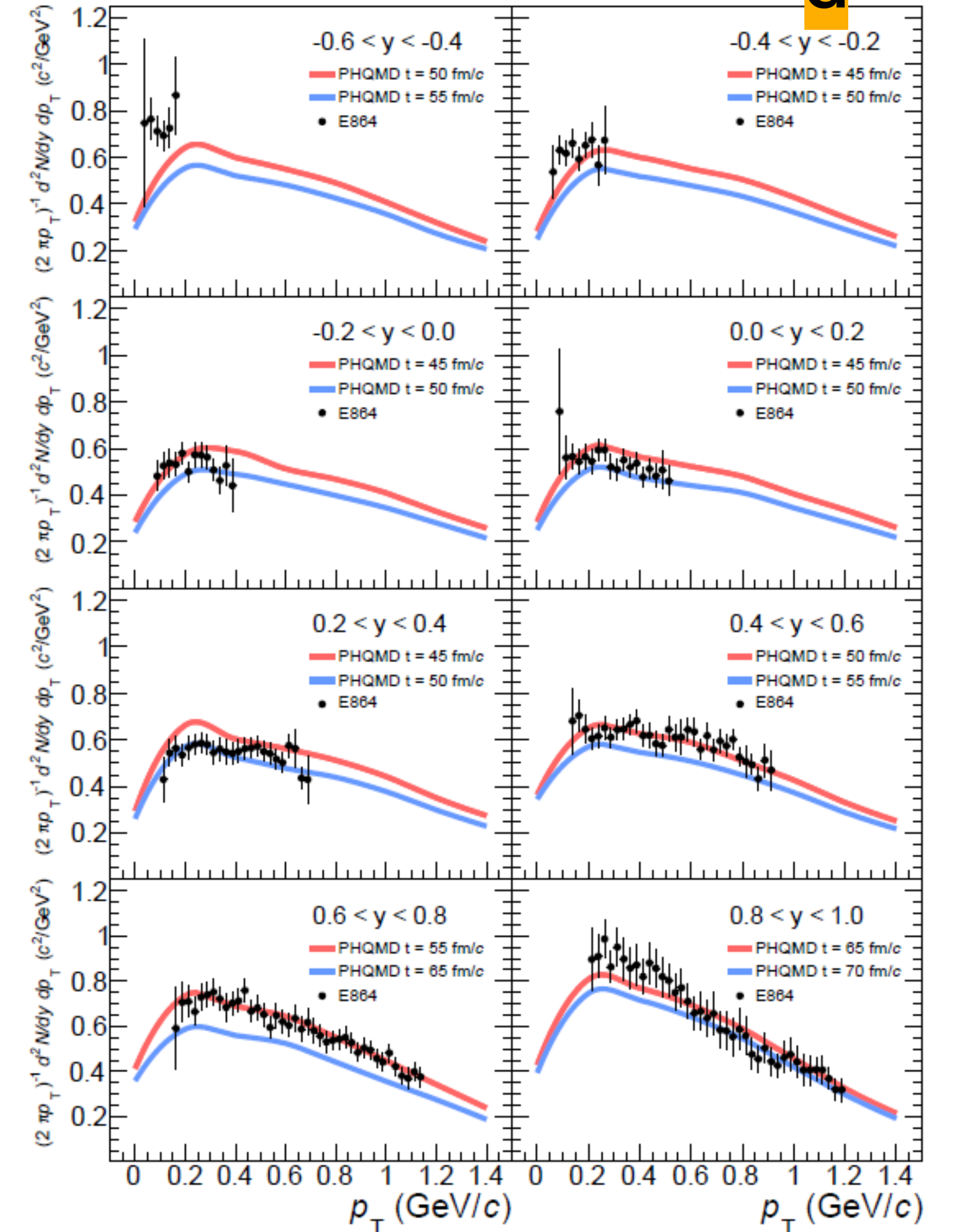
The PHQMD results for the  $y$ -distribution are taken at 'equal physical time'  
 $t = t_0 \cosh(y)$ ,  
 where  $t_0$  is the time at  $y=0$

Consider  $t_0 = 45$  and  $50$  fm/c



Au+Pb@10.6 AGeV

d

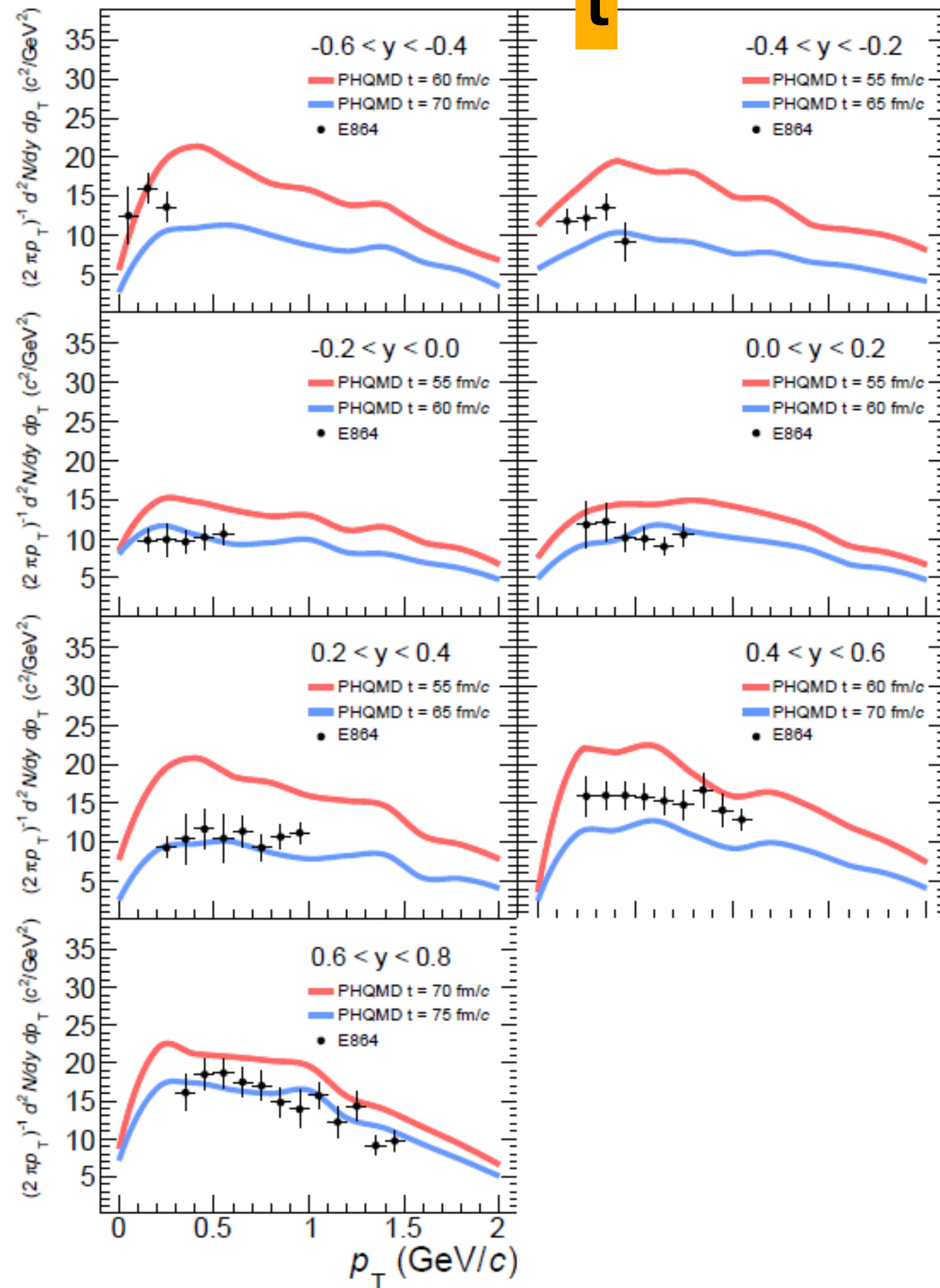


S. Gläsel et al., PRC 105 (2022) 1

# Cluster production in HICs at AGS energies

Au+Pb@10.6 AGeV

**t**



Scenario 1

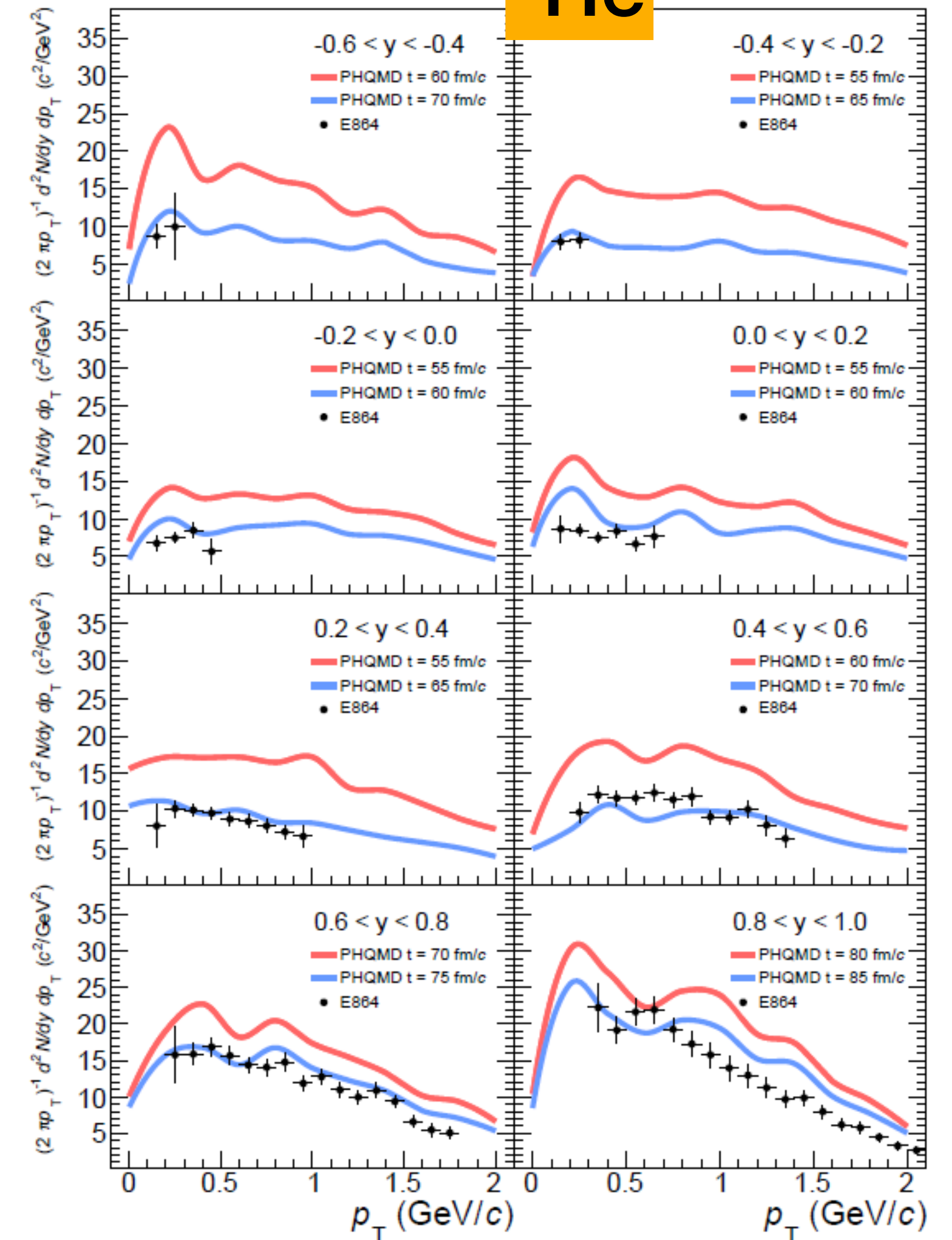
The PHQMD results for the  $y$ -distribution are taken at ‘equal physical time’  
 $t = t_0 \cosh(y)$ ,  
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Consider  $t_0 = 45$  and  $50$  fm/c

S. Gläsel et al., PRC 105 (2022) 1

Au+Pb@10.6 AGeV

**<sup>3</sup>He**

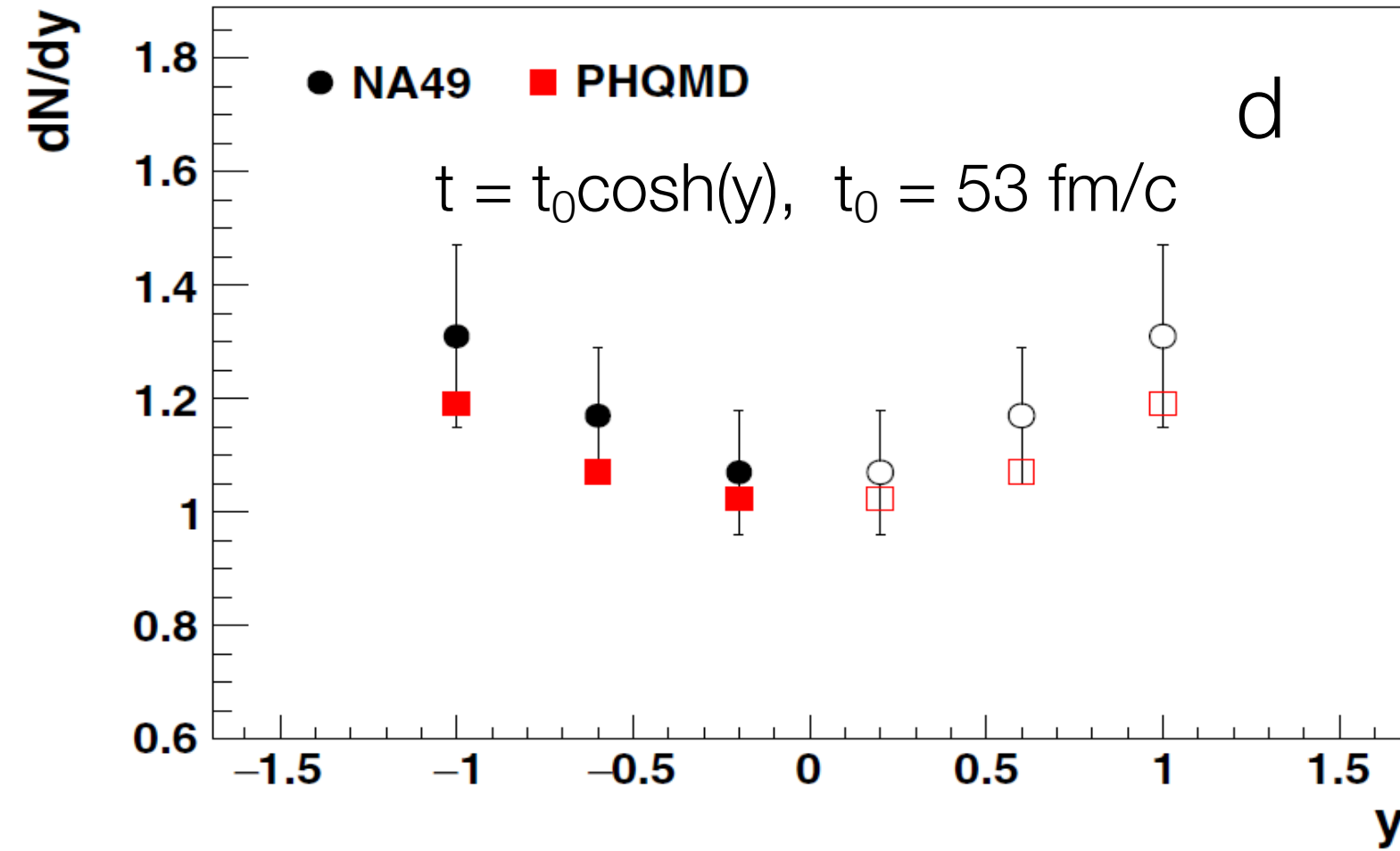


# Cluster production in HICs at SPS and RHIC energies

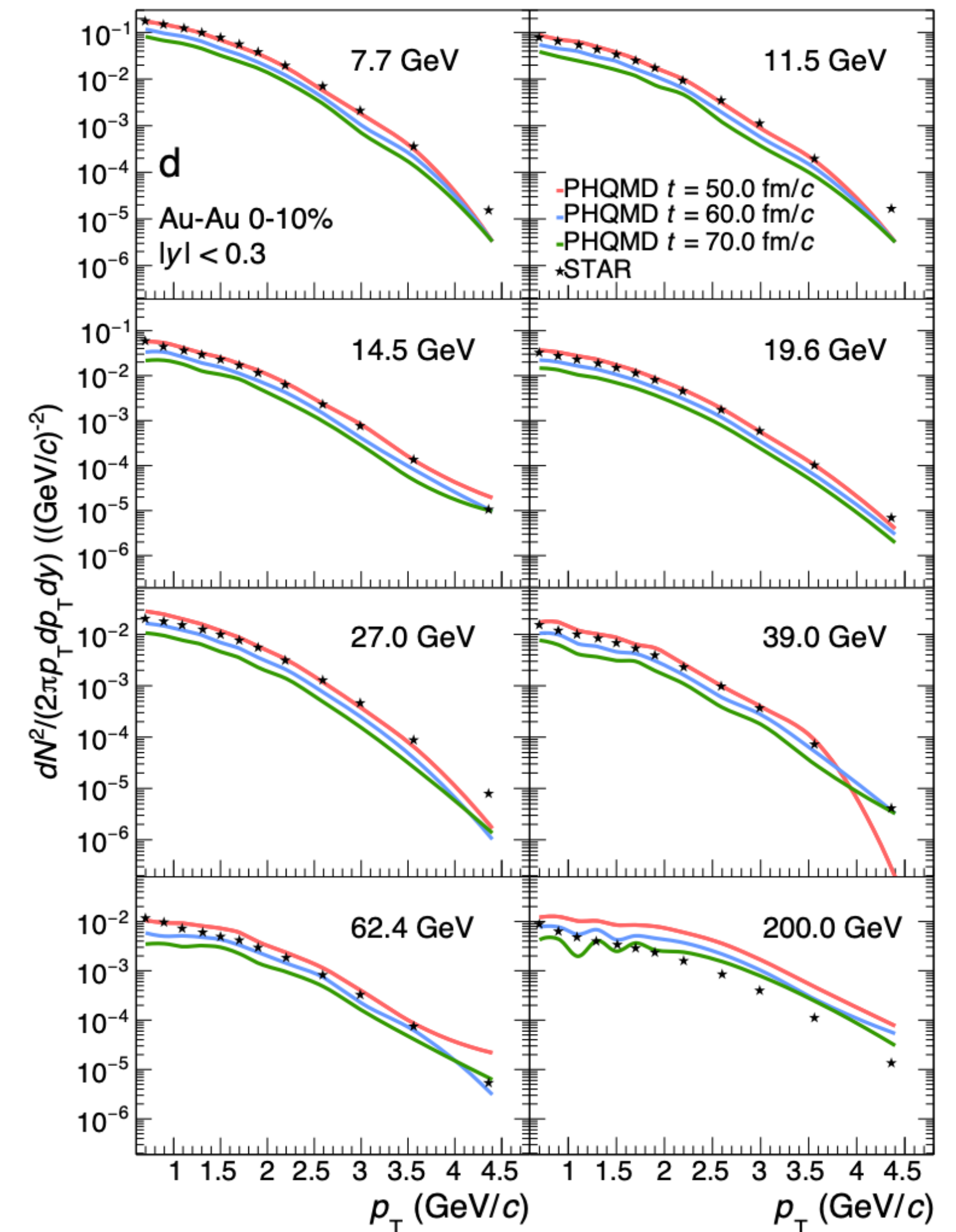
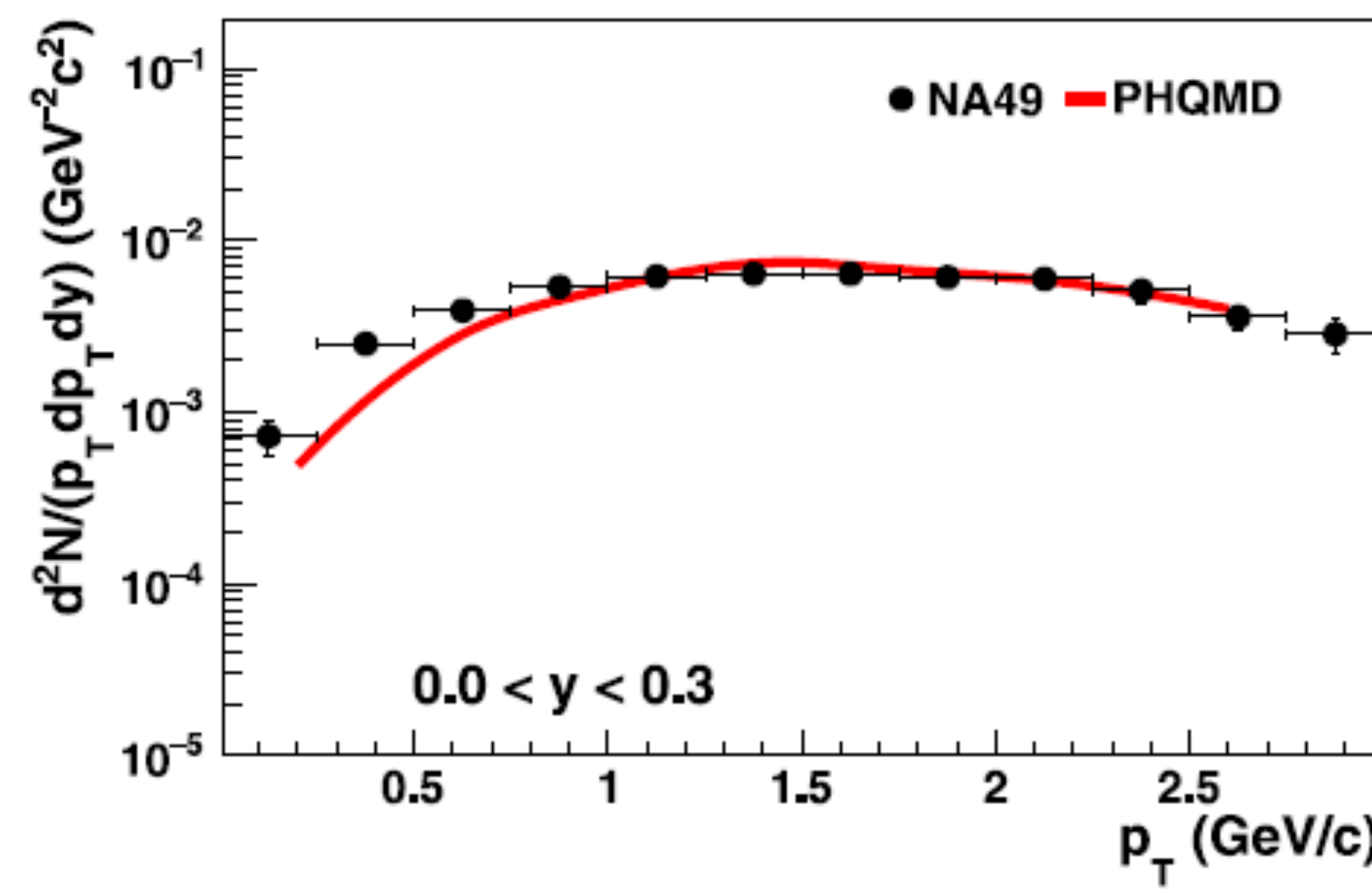
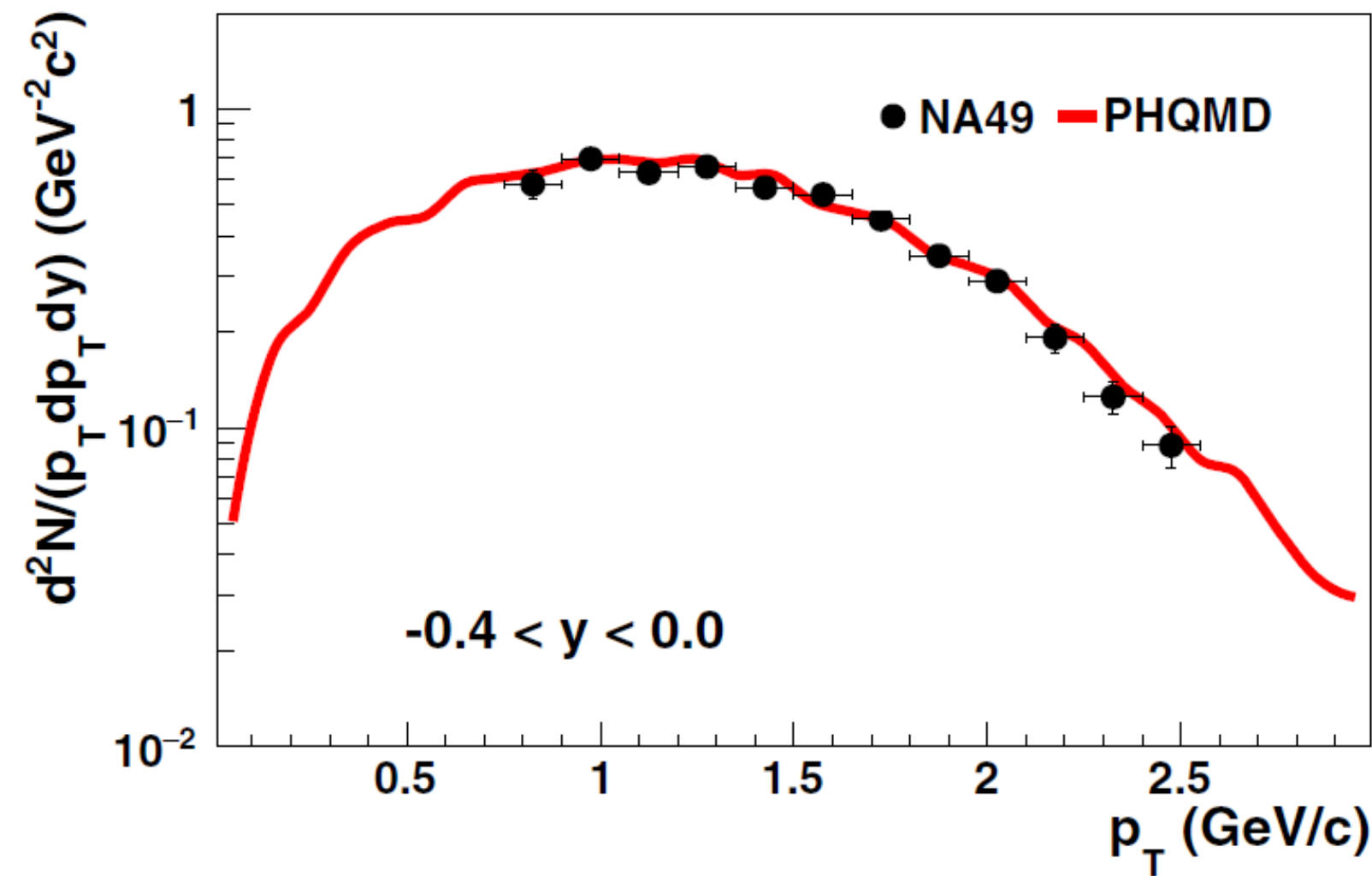
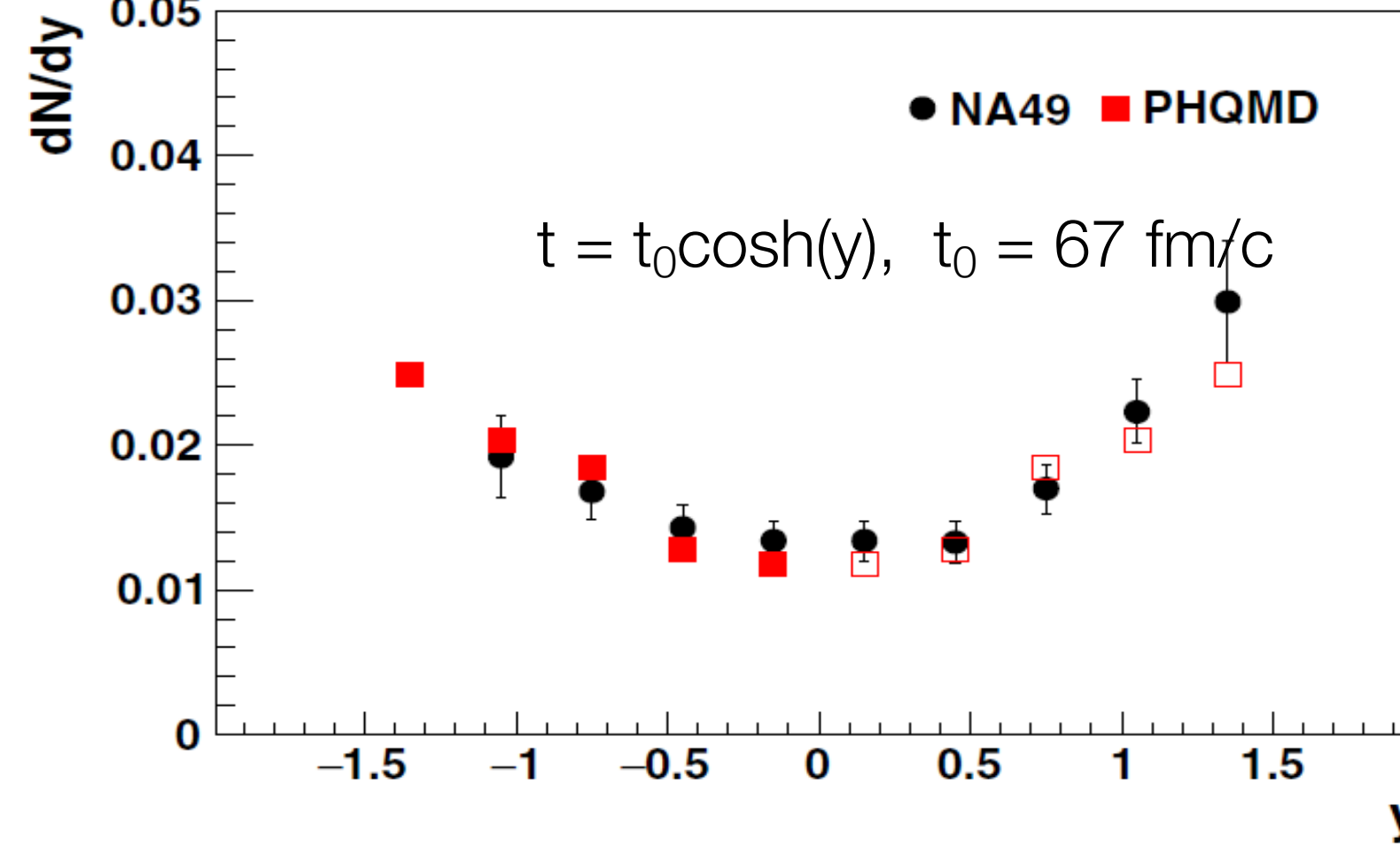
NA49  $\sqrt{s_{NN}} = 8.8$  GeV

STAR  $\sqrt{s_{NN}} = 7.7$  GeV – 200 GeV

deuterons

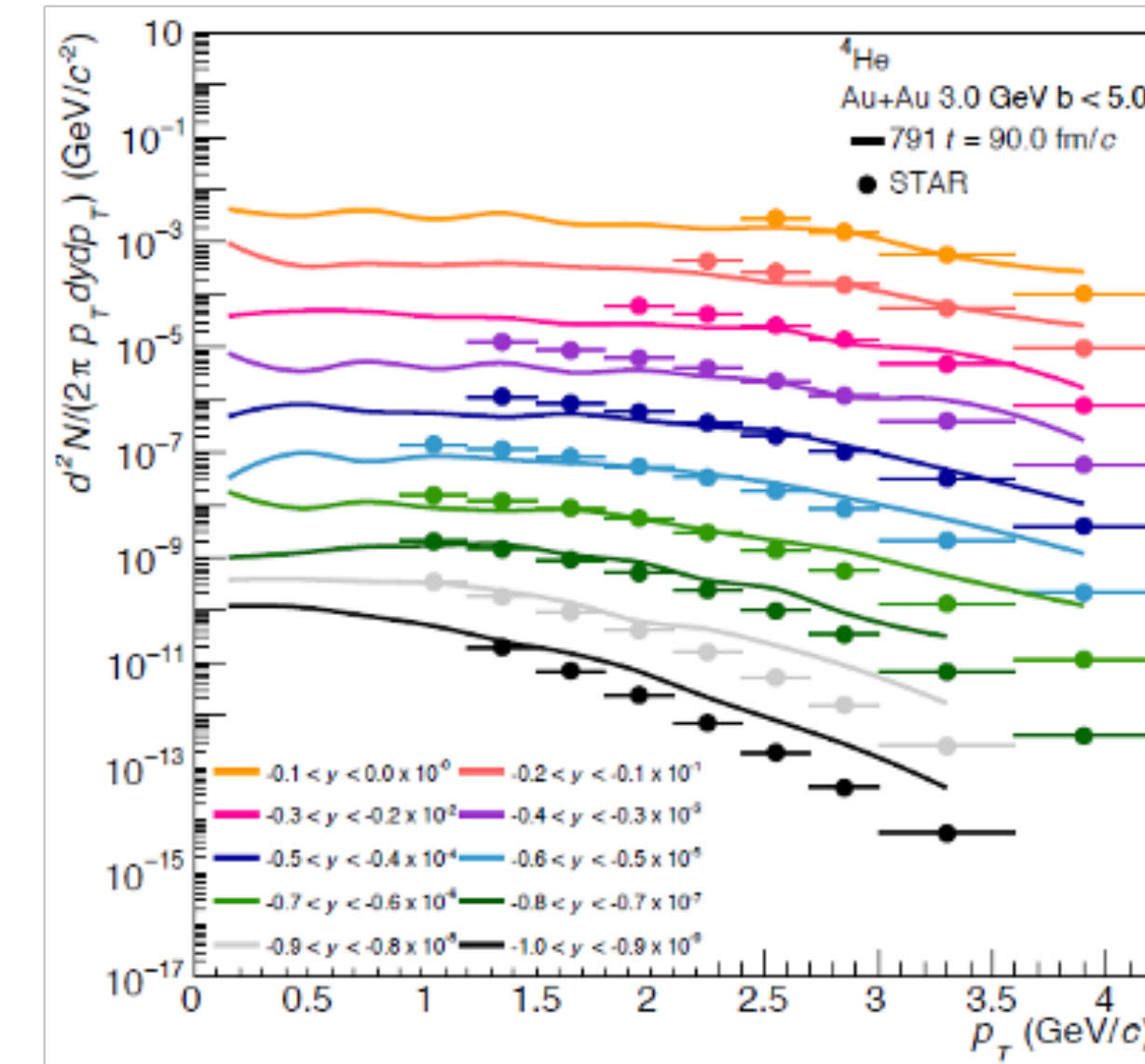
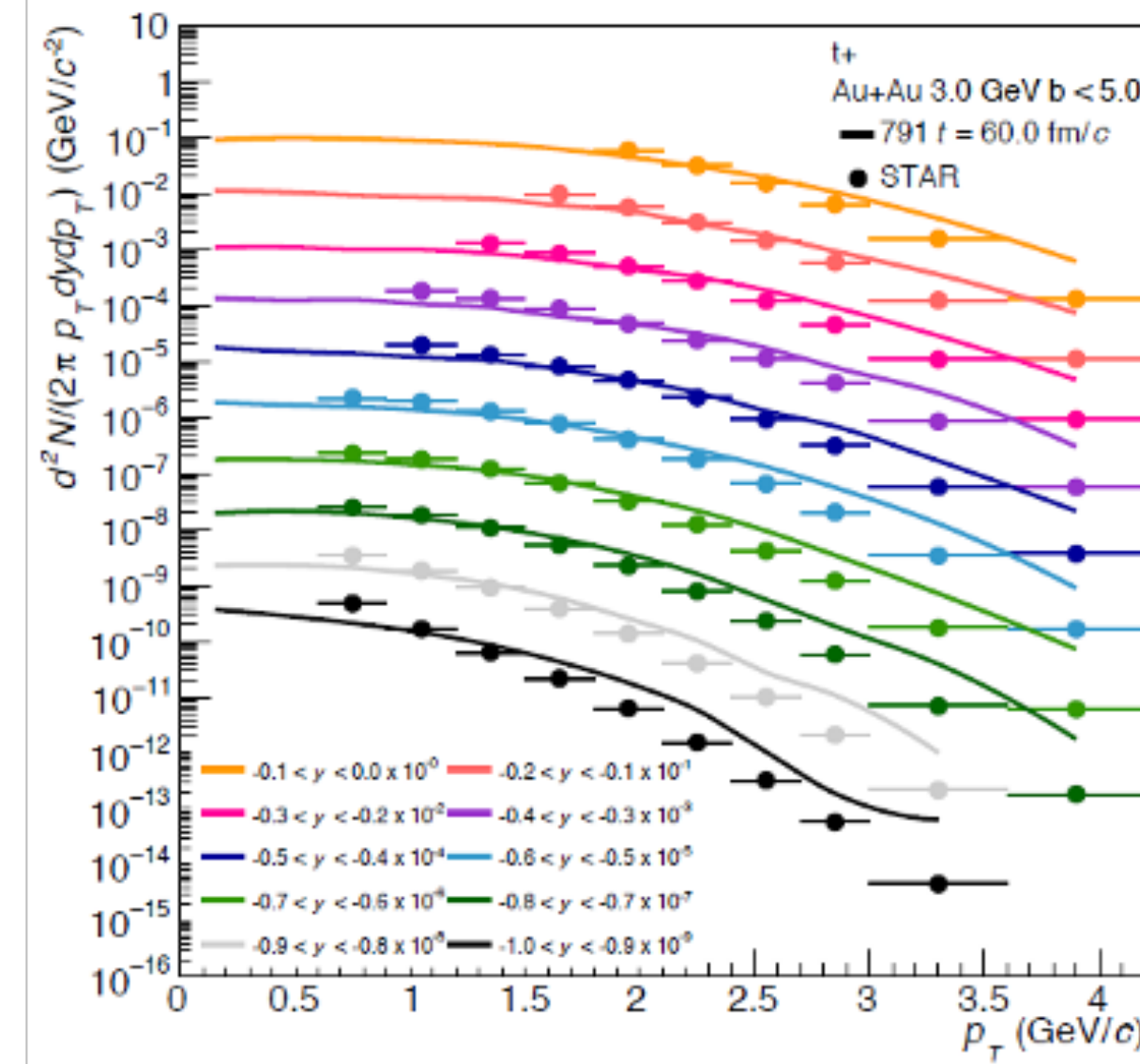
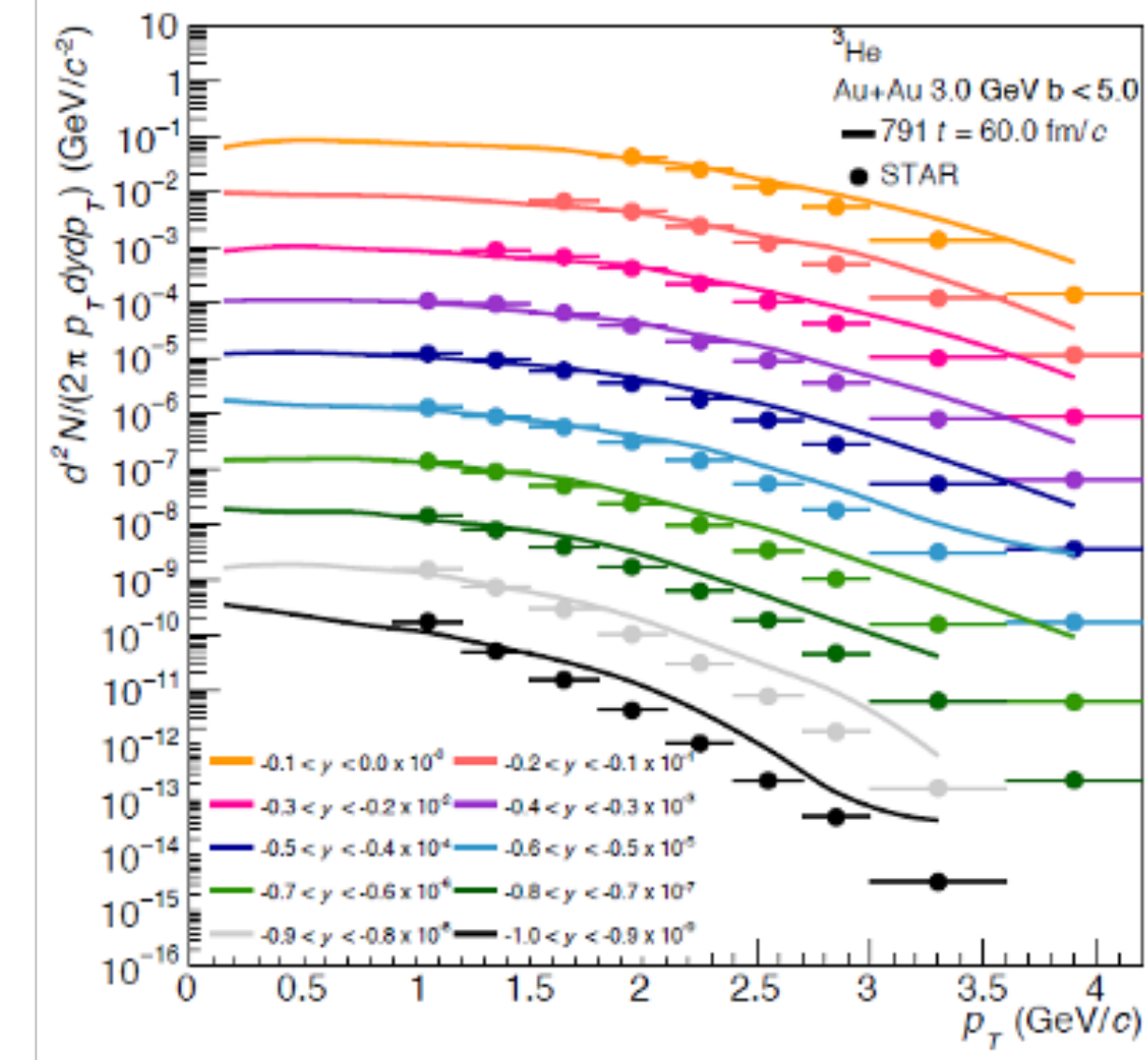
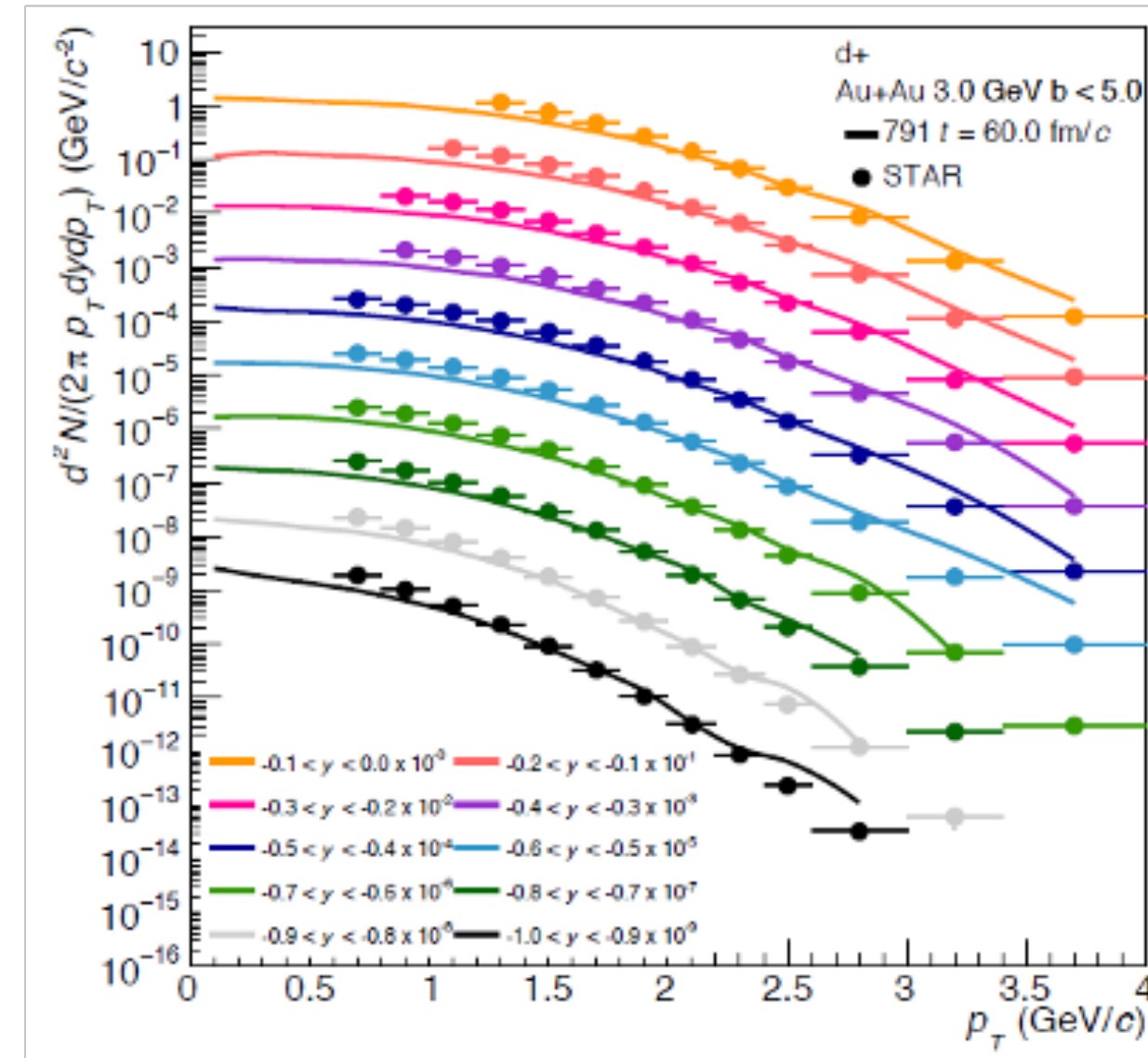
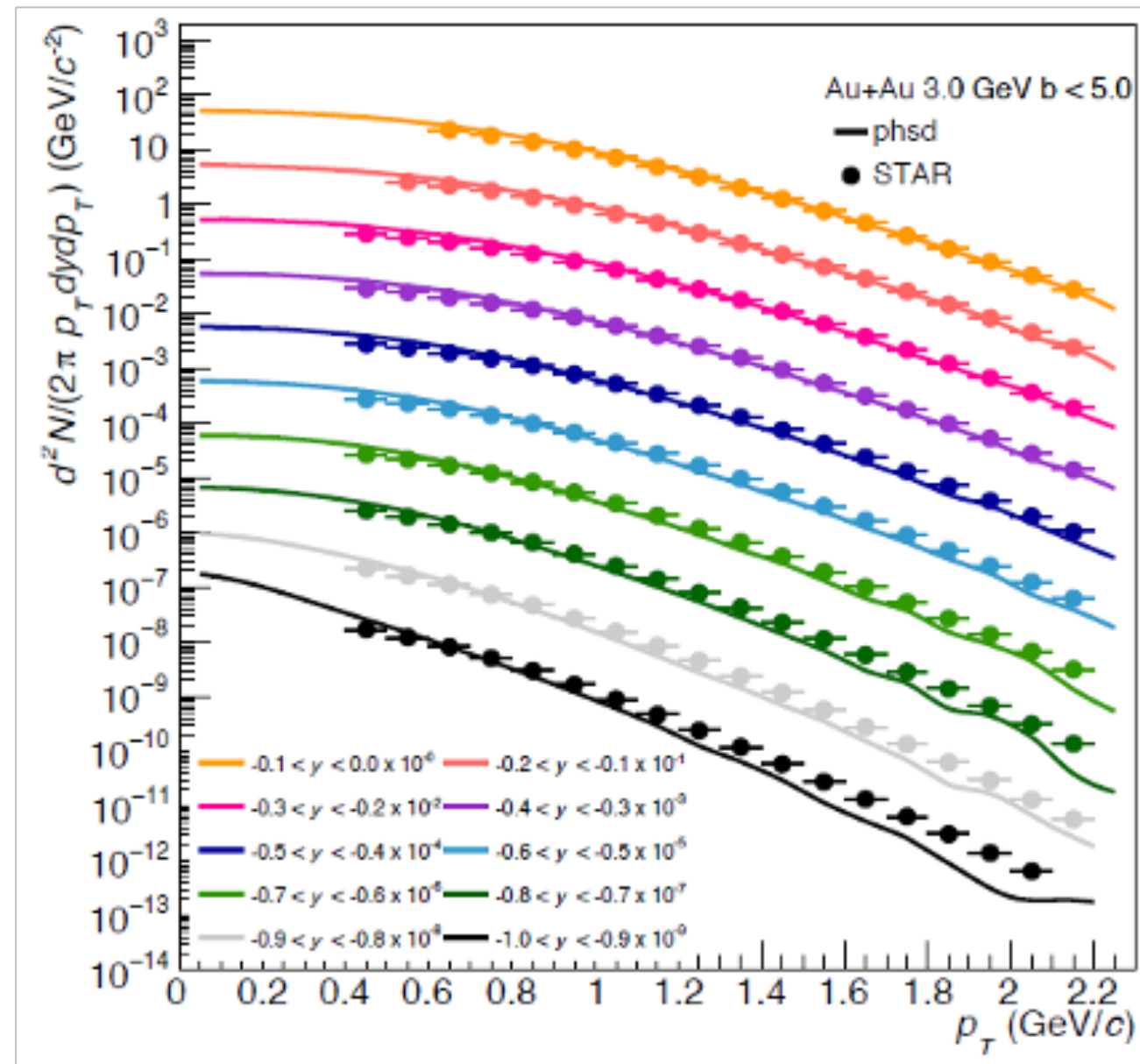


$^3\text{He}$



=> The PHQMD results for d and  $^3\text{He}$  agree with NA49 and STAR data.

# Cluster production in HICs at SPS and RHIC energies

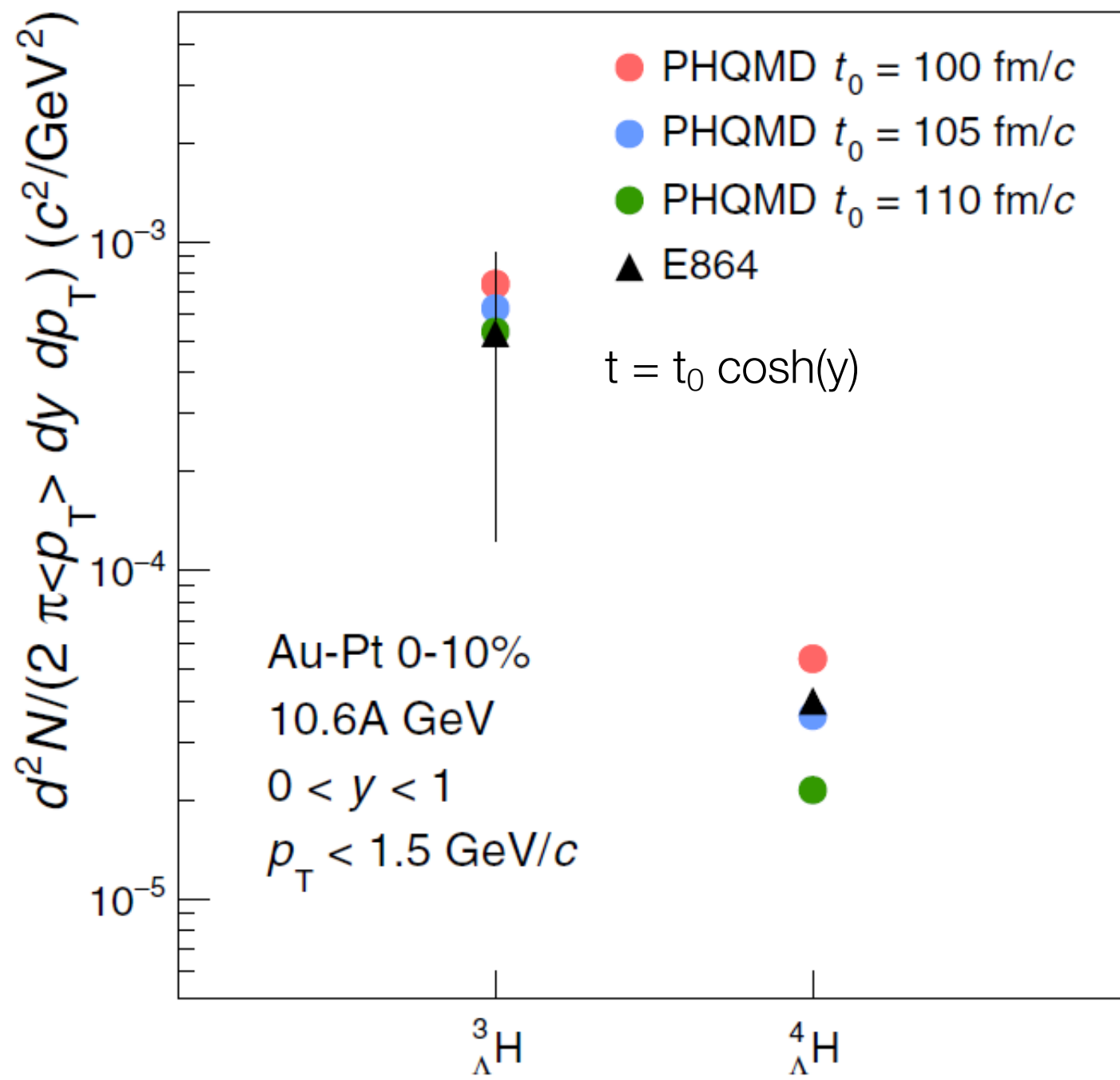


Good description of cluster production

# Hypernuclei production at $\sqrt{s_{NN}} = 3.0$ and 4.9 GeV

S. Gläsel et al., PRC 105 (2022) 1

E864  $\sqrt{s_{NN}} = 4.9$  GeV



Assumption for nucleon-hyperon potential:  $V_{NL} = 2/3 V_{NN}$

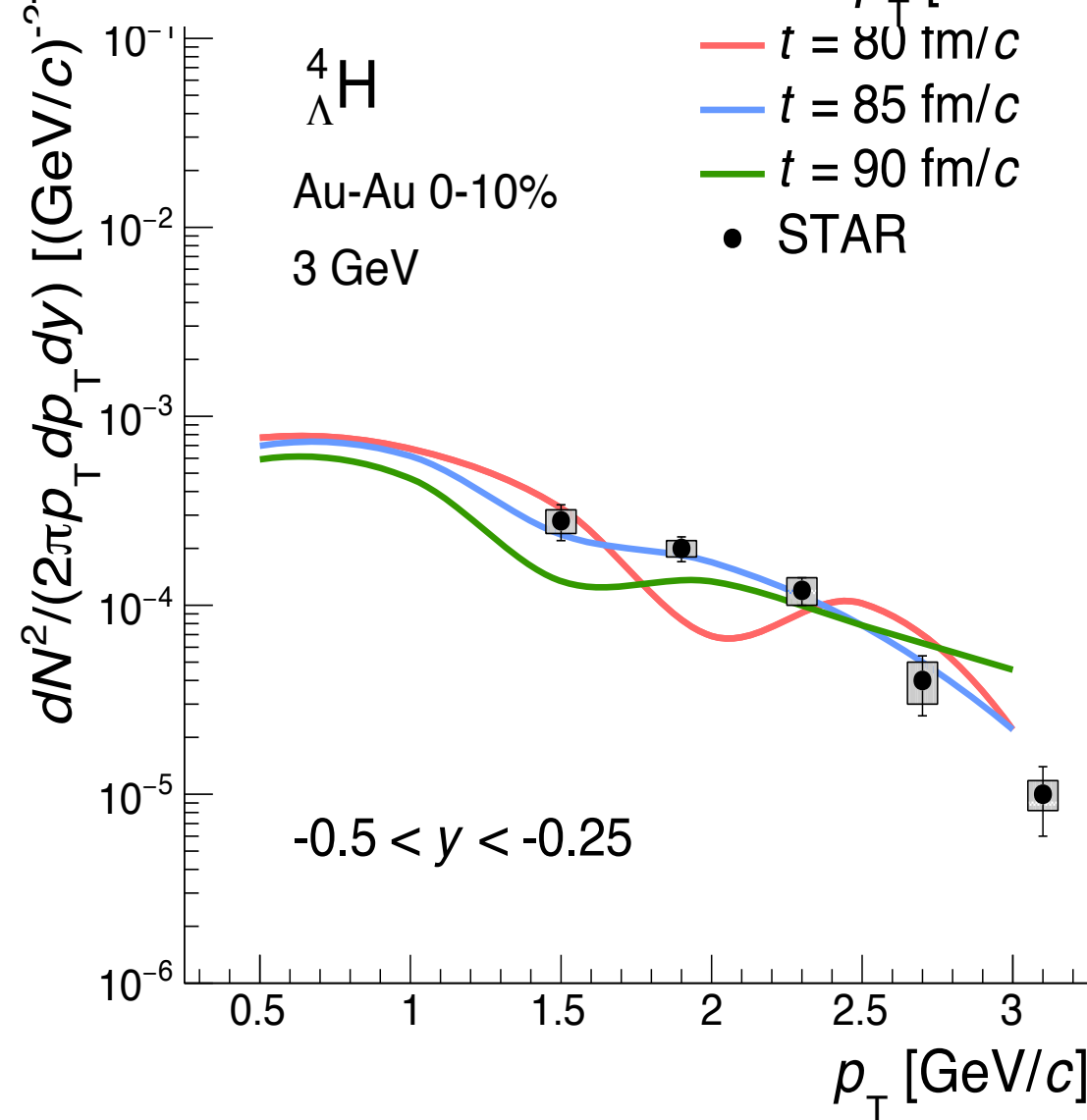
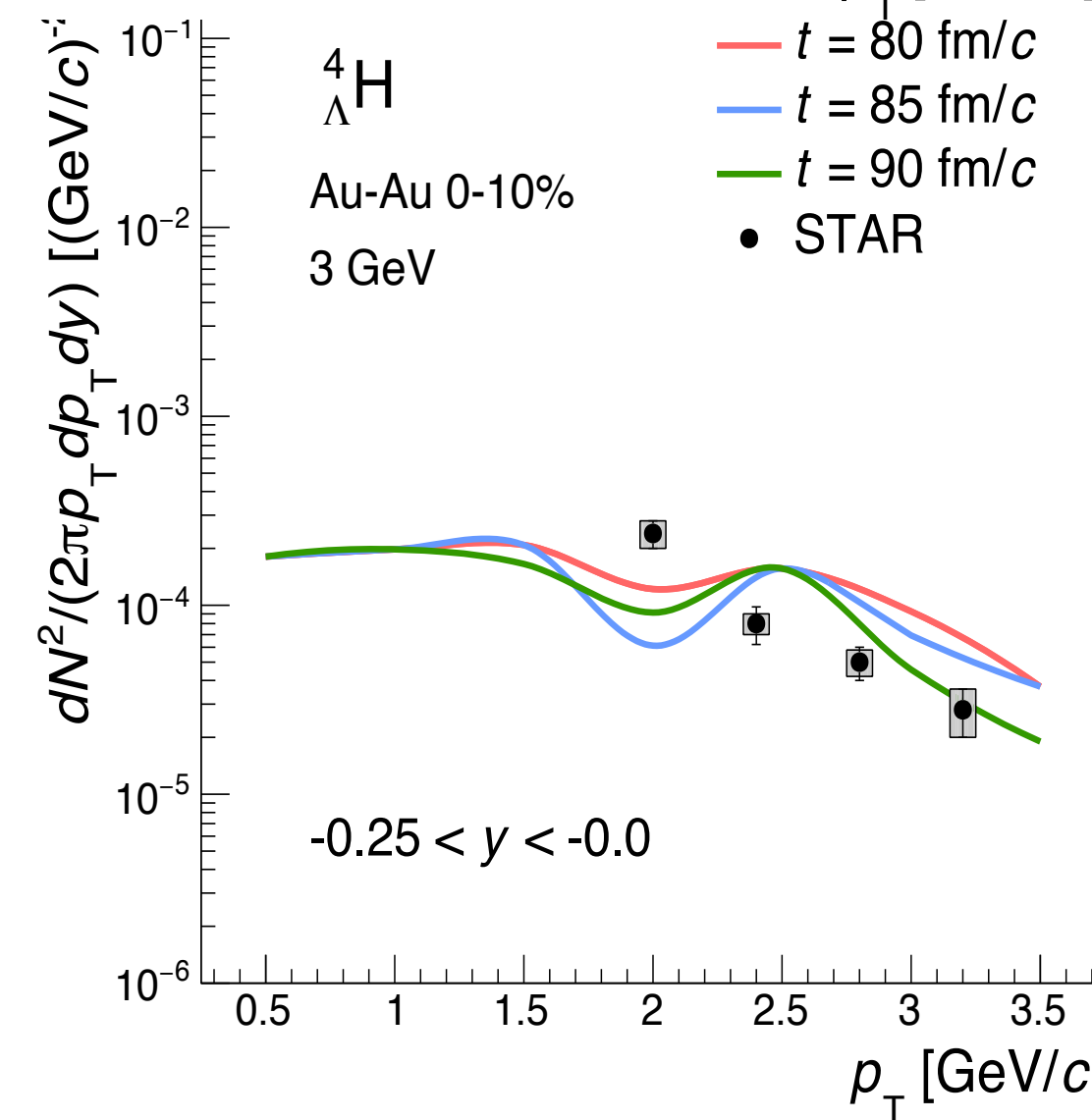
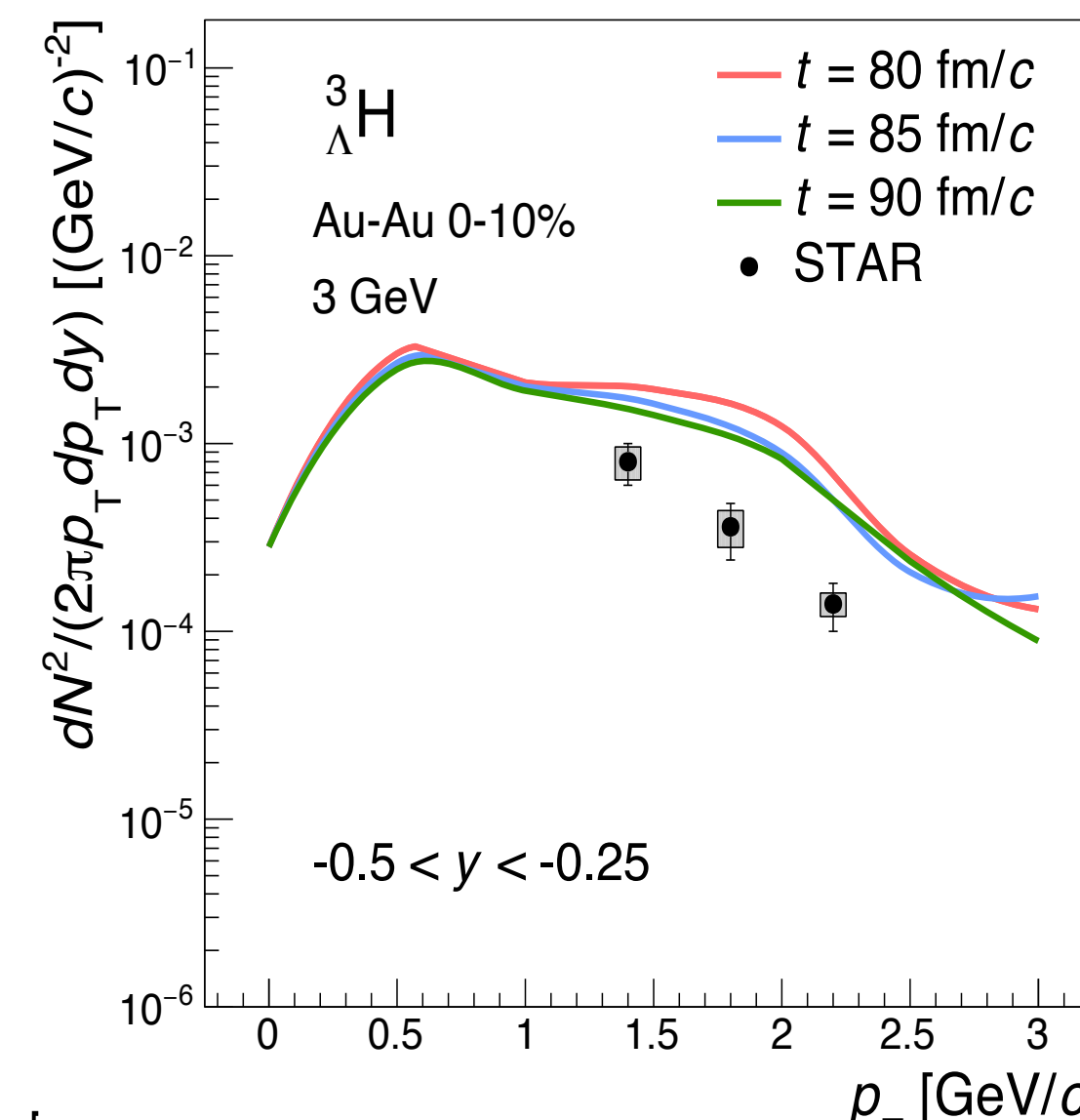
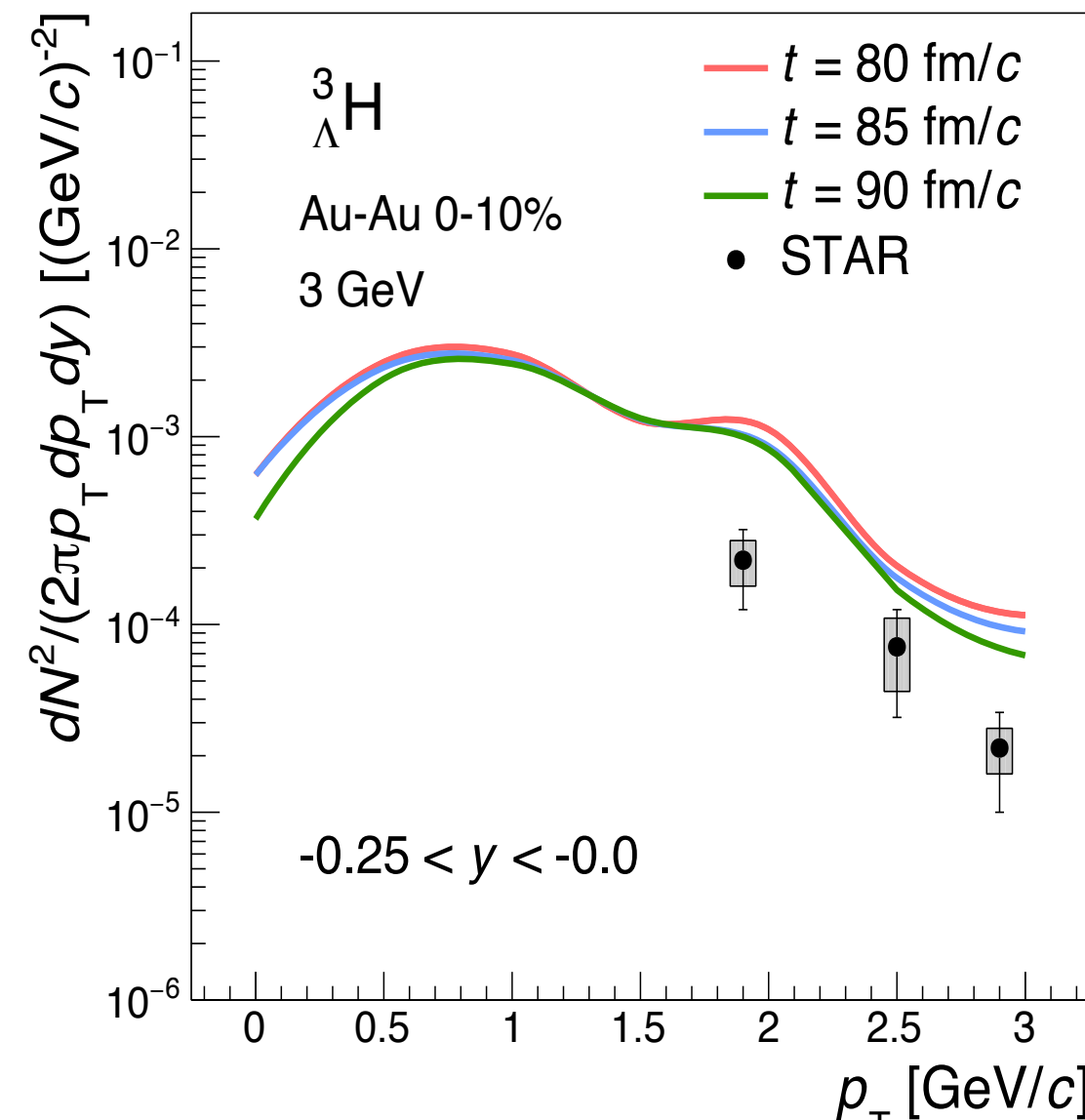
=> trend of the experimental STAR\* &

$p_T$ -spectra at  $\sqrt{s_{NN}} = 3$  is produced

well

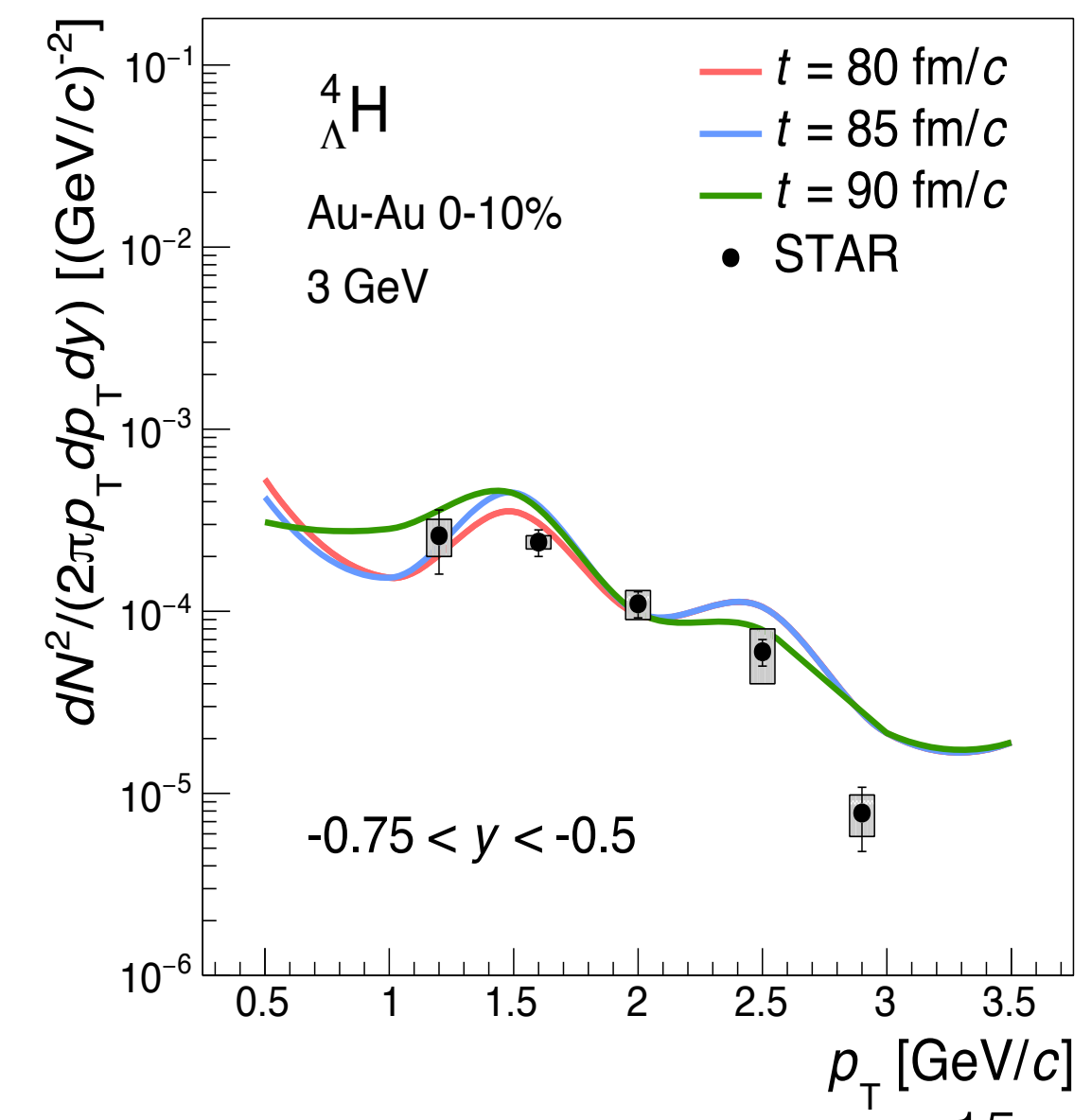
=> yields are slightly overpredicted

STAR  $\sqrt{s_{NN}} = 3.0$  GeV



=> Reasonable description of hypernuclei production at  $\sqrt{s_{NN}} = 3.0$  GeV

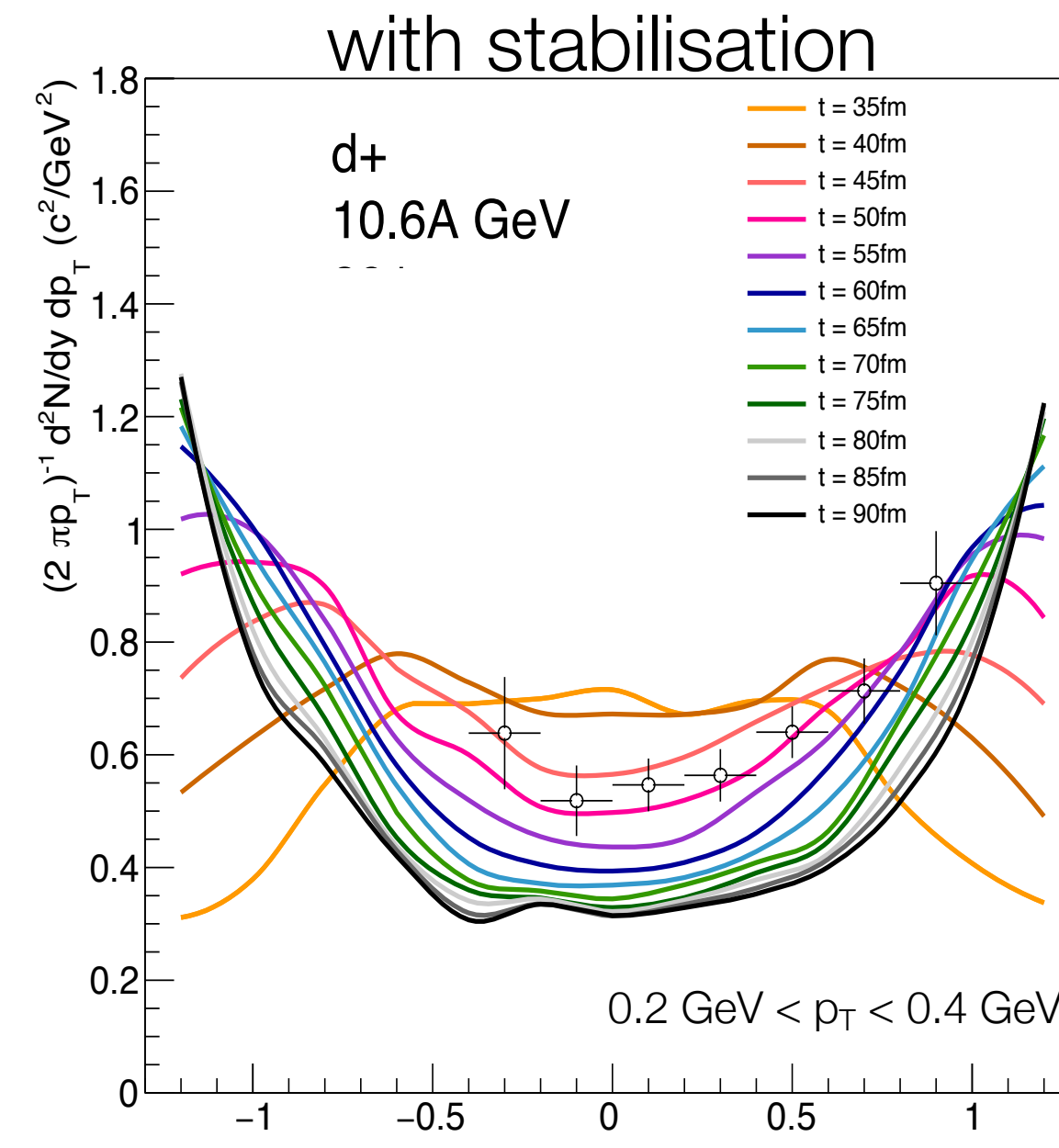
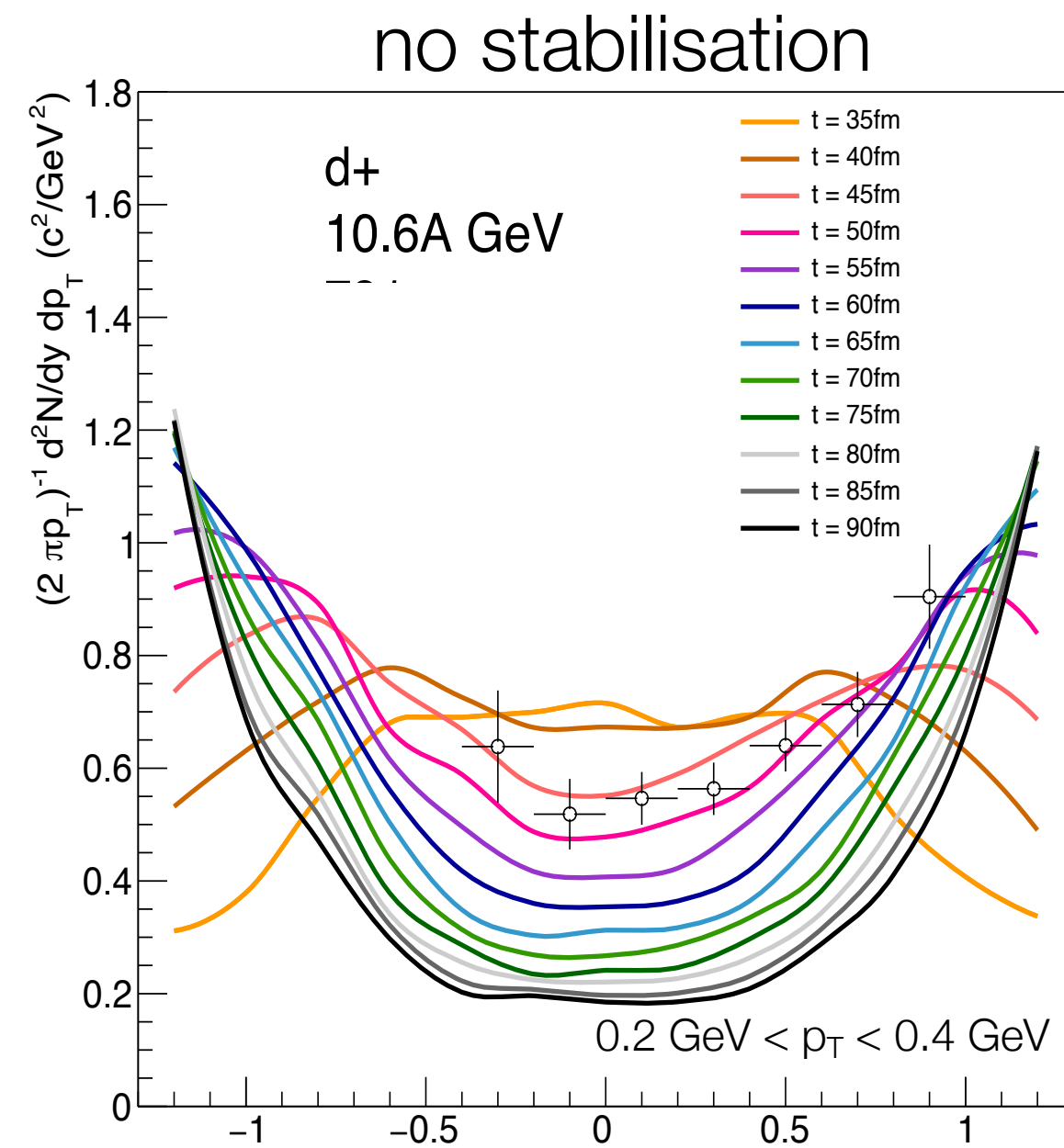
\*Yue-Hang Leung: First results of H3L & H4L ( $dN/dy$ ,  $c_T$ ,  $v_1$ ) from 3 GeV Au+Au collisions with the STAR detector (CPOD2021)



# dN/dy time evolution for deuteron at $\sqrt{s_{NN}} = 4.9$ GeV

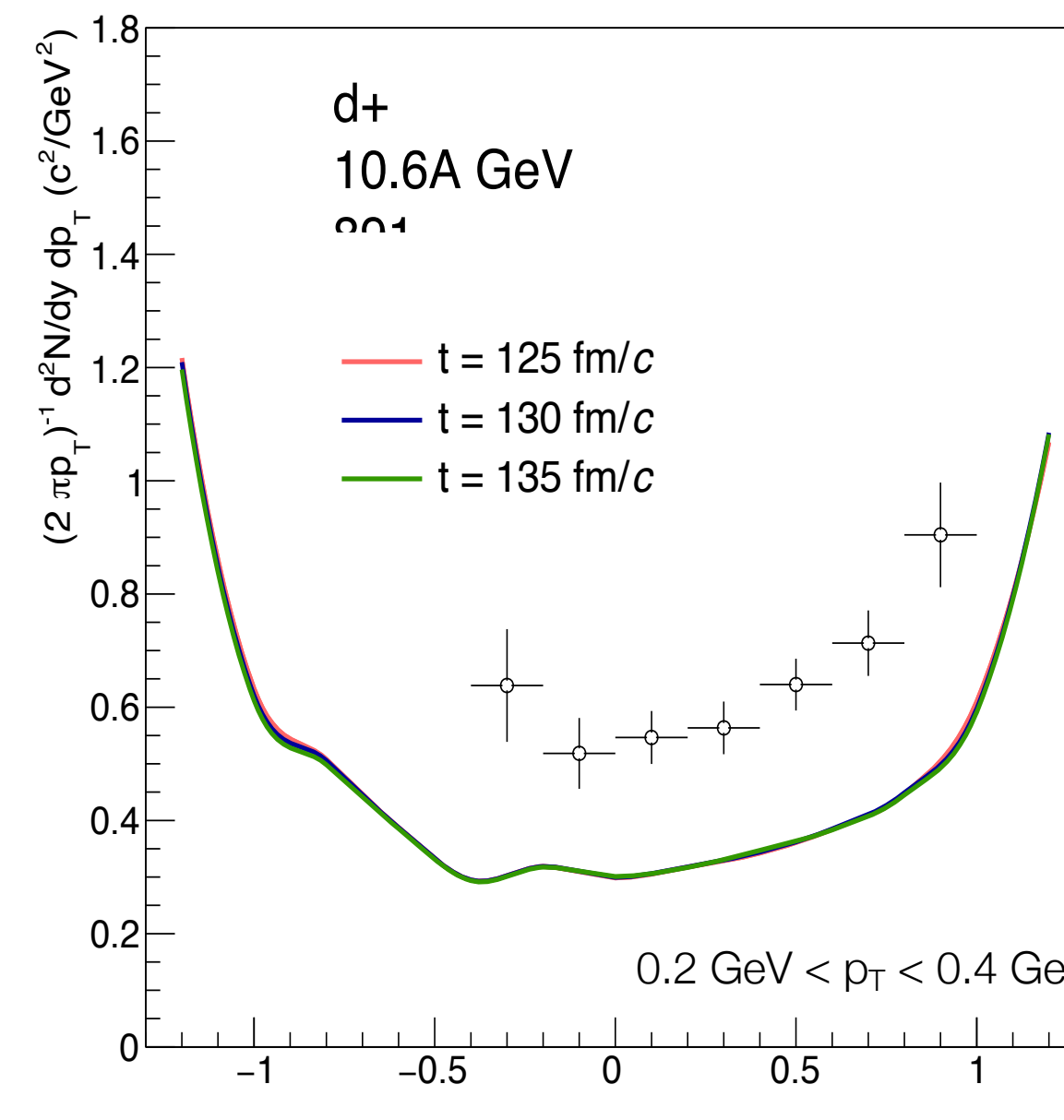
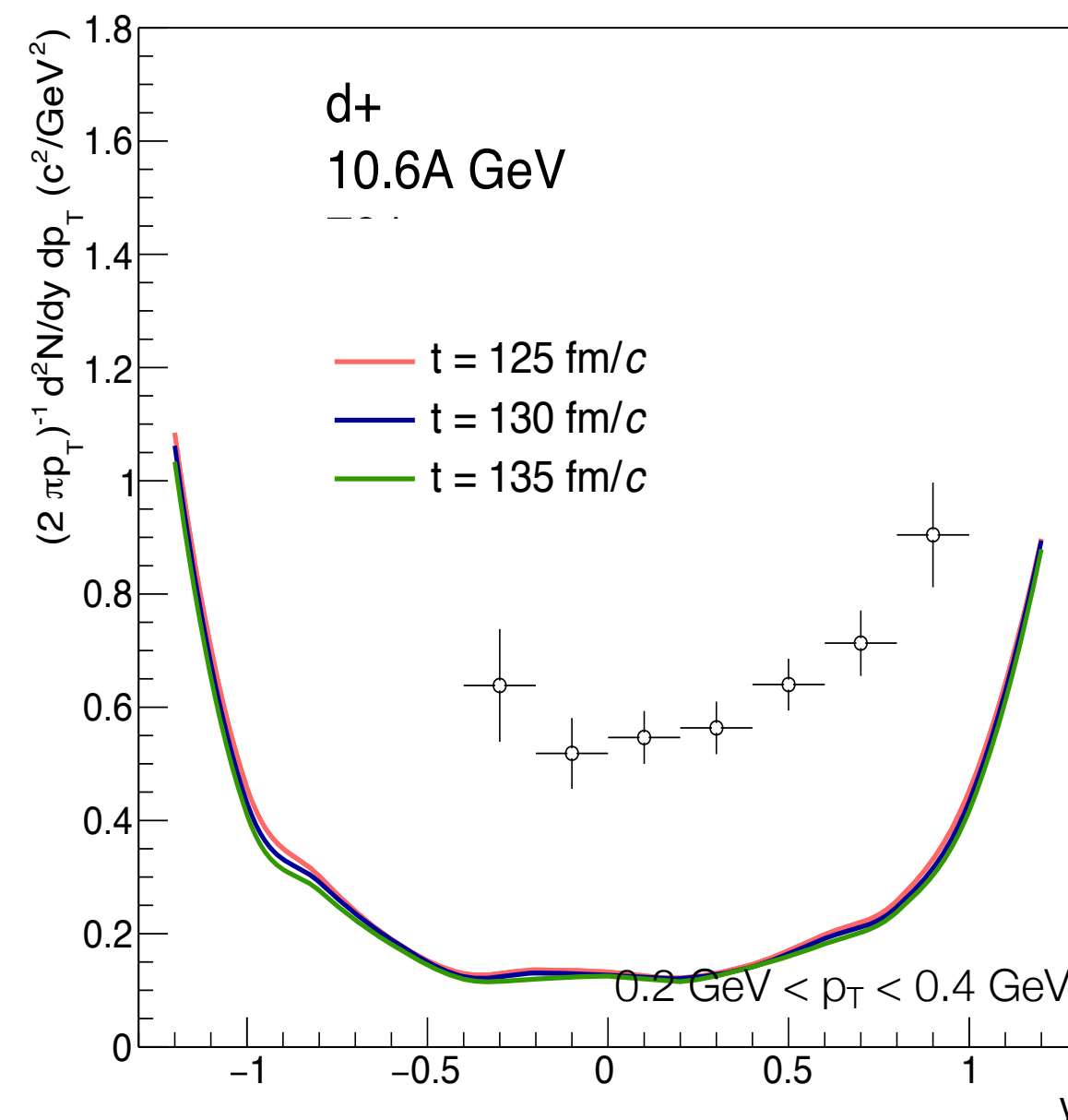
## Scenario 2: «Advanced MST»

35 fm < t < 90 fm



=> With stabilisation, multiplicity starts to drop slower at around 60 fm/c.

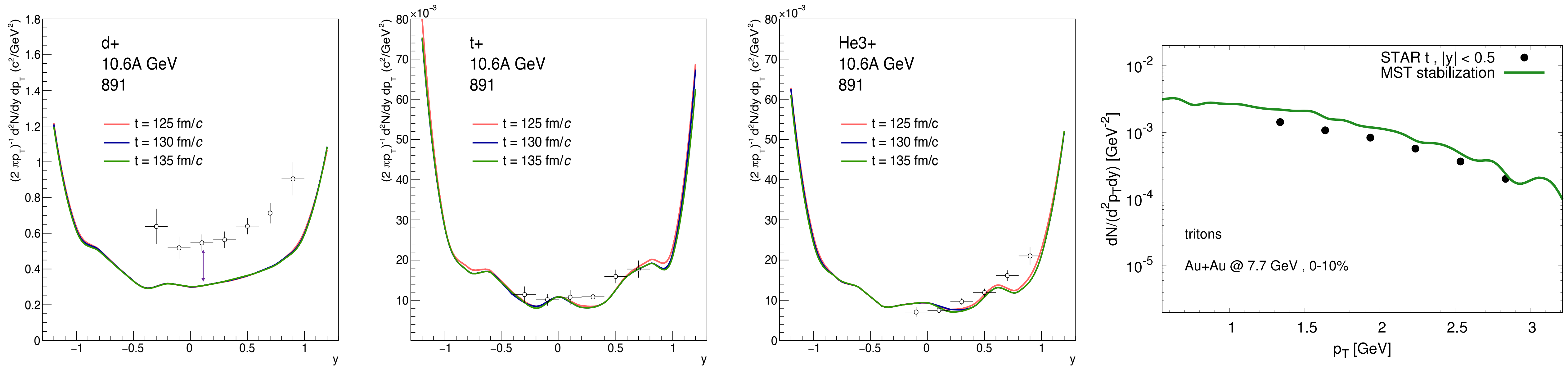
125 fm < t < 135 fm



=> At the final time, deuteron multiplicity is ~2 times higher with stabilisation.



# Stable light nuclei at $\sqrt{s_{NN}} = 4.9$ and 7.7 GeV with aMST



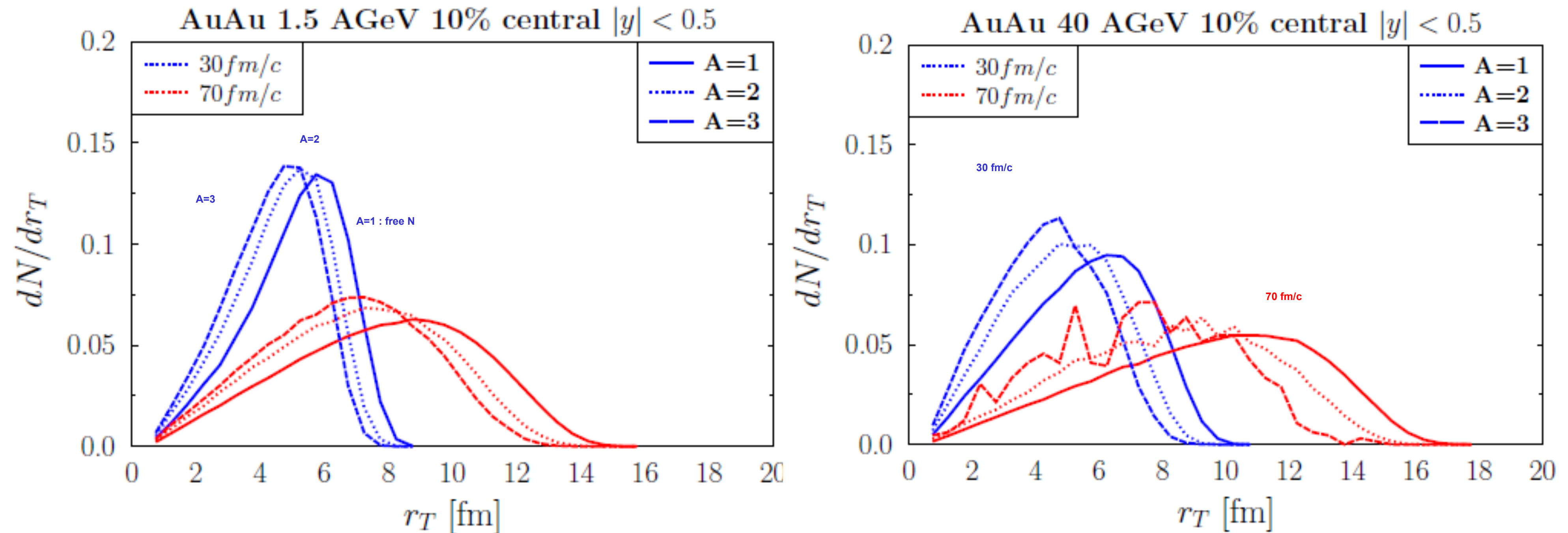
PHQMD with stabilisation procedure fits the experimental data at  $\sqrt{s_{NN}} = 4.9$  and 7.7 GeV very well for triton and  $^3\text{He}$ .

Deuterons are underestimated => contribution of deuterons formed by inelastic scattering.

# Where clusters are formed?

The MST snapshot (taken at time 30 and 70 fm/c) of the normalized distribution of the transverse distance  $r_T$  of the nucleons to the center of the fireball.

It is shown for  $A=1$  (free nucleons) and for the nucleons in  $A=2$  and  $A=3$  clusters

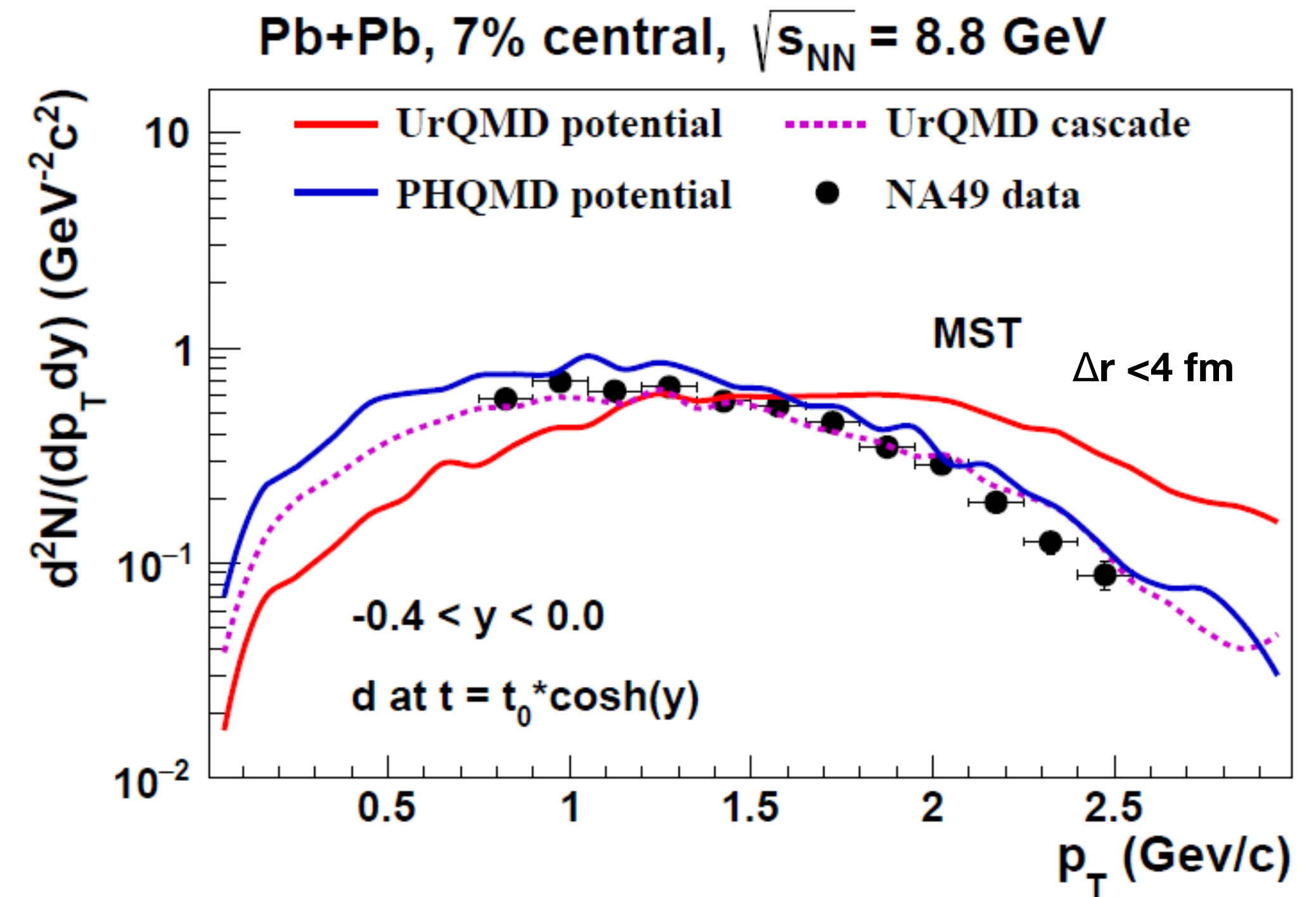
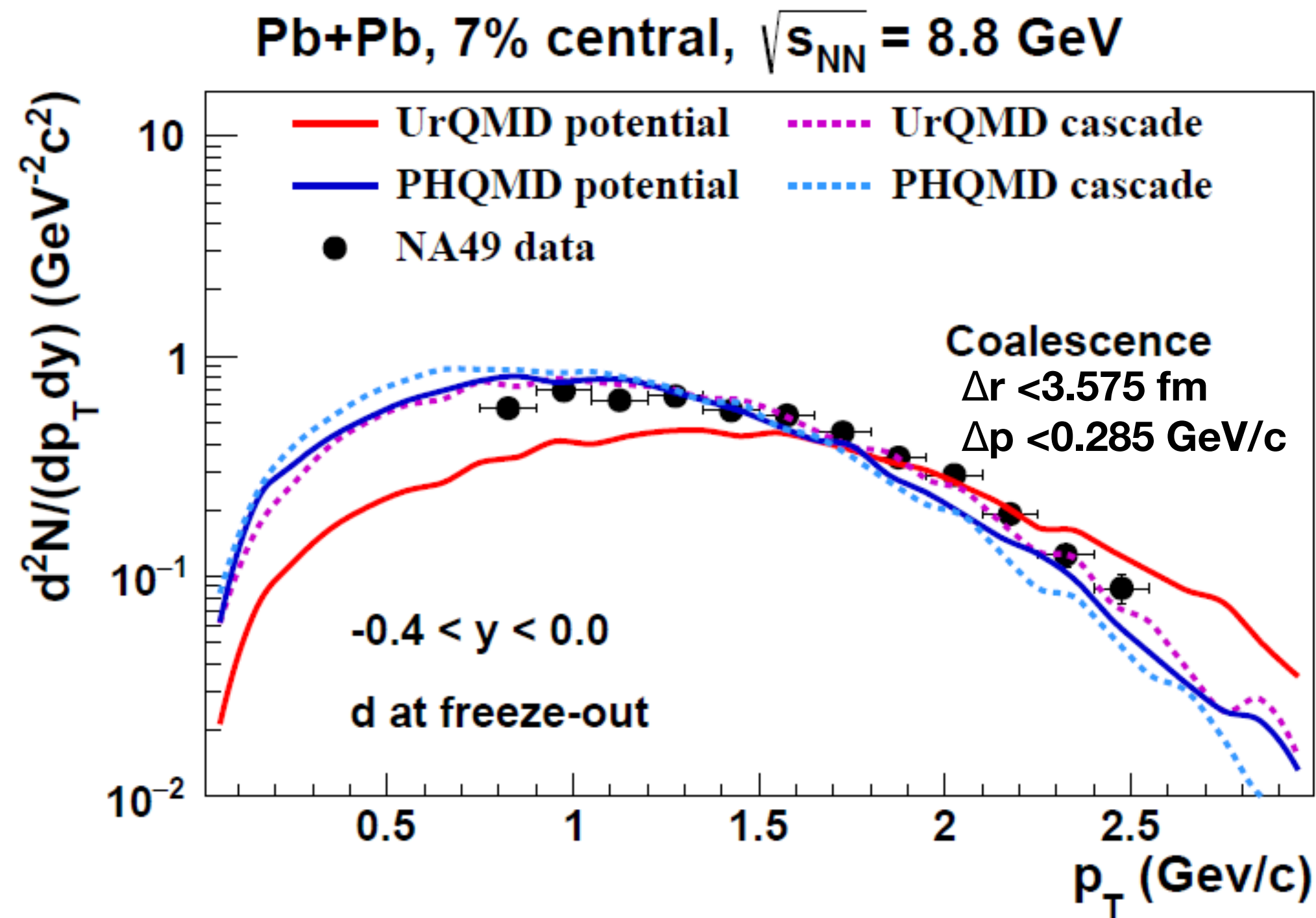


**Transverse distance profile** of free nucleons and clusters are different!

Clusters are mainly formed **behind the 'front' of free nucleons** of expanding fireball

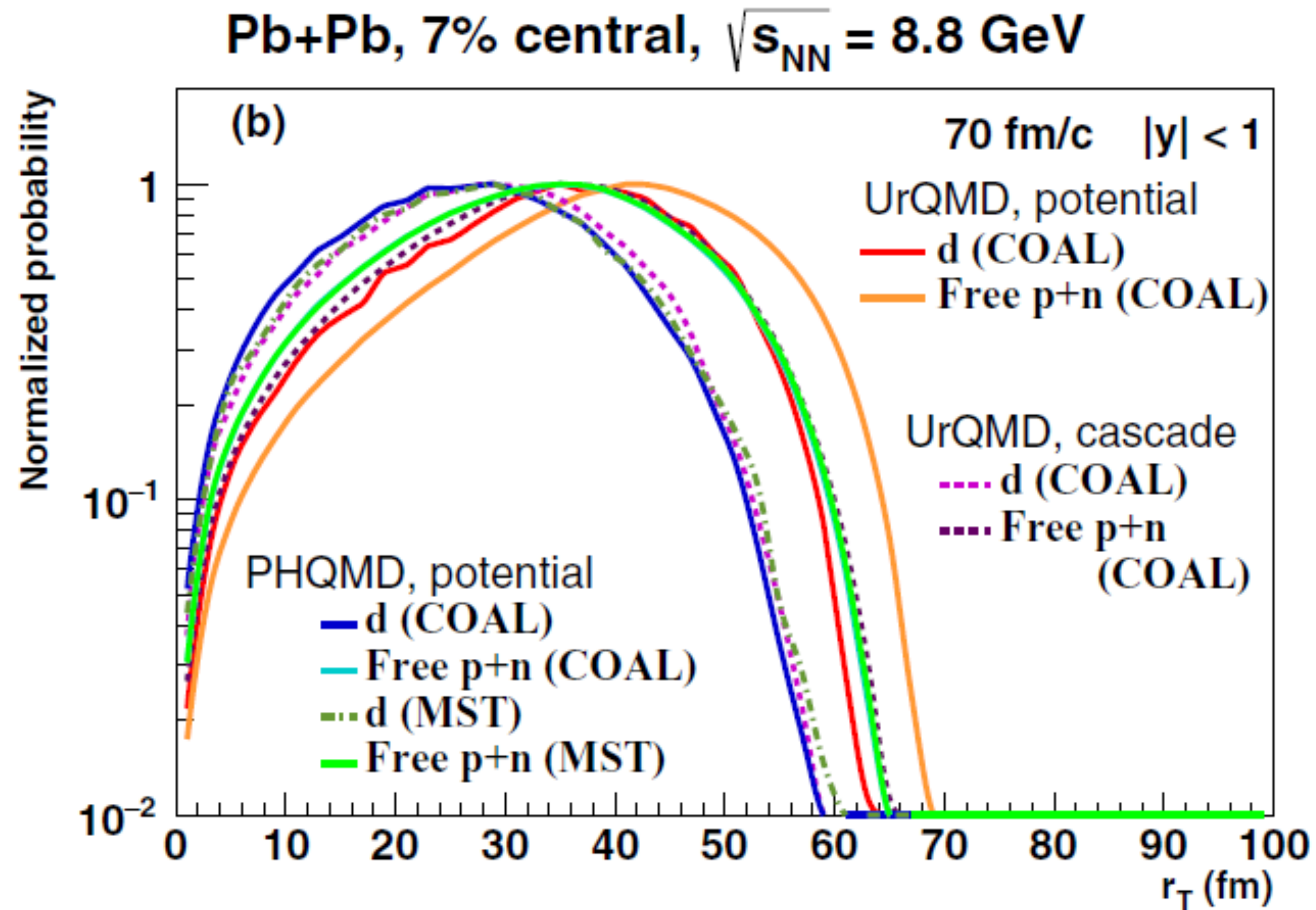
**'ice' is behind the 'fire'** —> cluster can survive

# Where clusters are formed?



- **Coalescence and MST** give very similar multiplicities and  $y$ - and  $p_T$  -distributions
- PHQMD and UrQMD results in the cascade mode are very similar
- Deuteron production is sensitive to the realization of potential in transport approaches

# Where clusters are formed?



Coalescence as well as the MST procedure show that the **deuterons remain in transverse direction closer to the center** of the heavy-ion collision than free nucleons

**deuterons are behind** the fast nucleons (and pion wind)

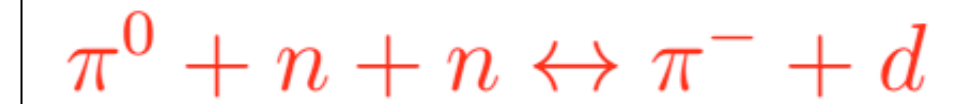
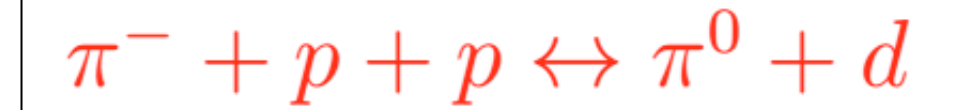
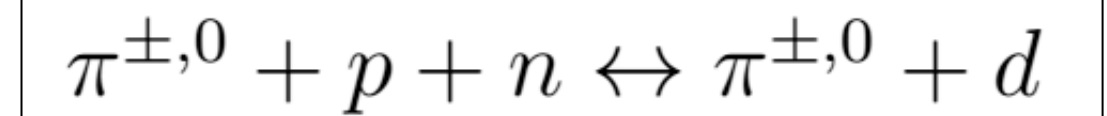
# Kinetic mechanism for cluster production

# Kinetic mechanism for deuteron formation

Gabriele Coci et al., in preparation

N+N+ $\pi$  inclusion of all possible channels allowed by total isospin T conservation:

$$P_{3,2}(\sqrt{s}) = F_{spin} F_{iso} P_{2,3}(\sqrt{s}) \frac{E_1^f E_2^f}{2E_3 E_4 E_5} \frac{R_2(\sqrt{s}, m_1, m_2)}{R_3(\sqrt{s}, m_3, m_4, m_5)} \frac{1}{\Delta V_{cell}}$$



NN $\pi$  expanded as superposition of eigenstates of total isospin T

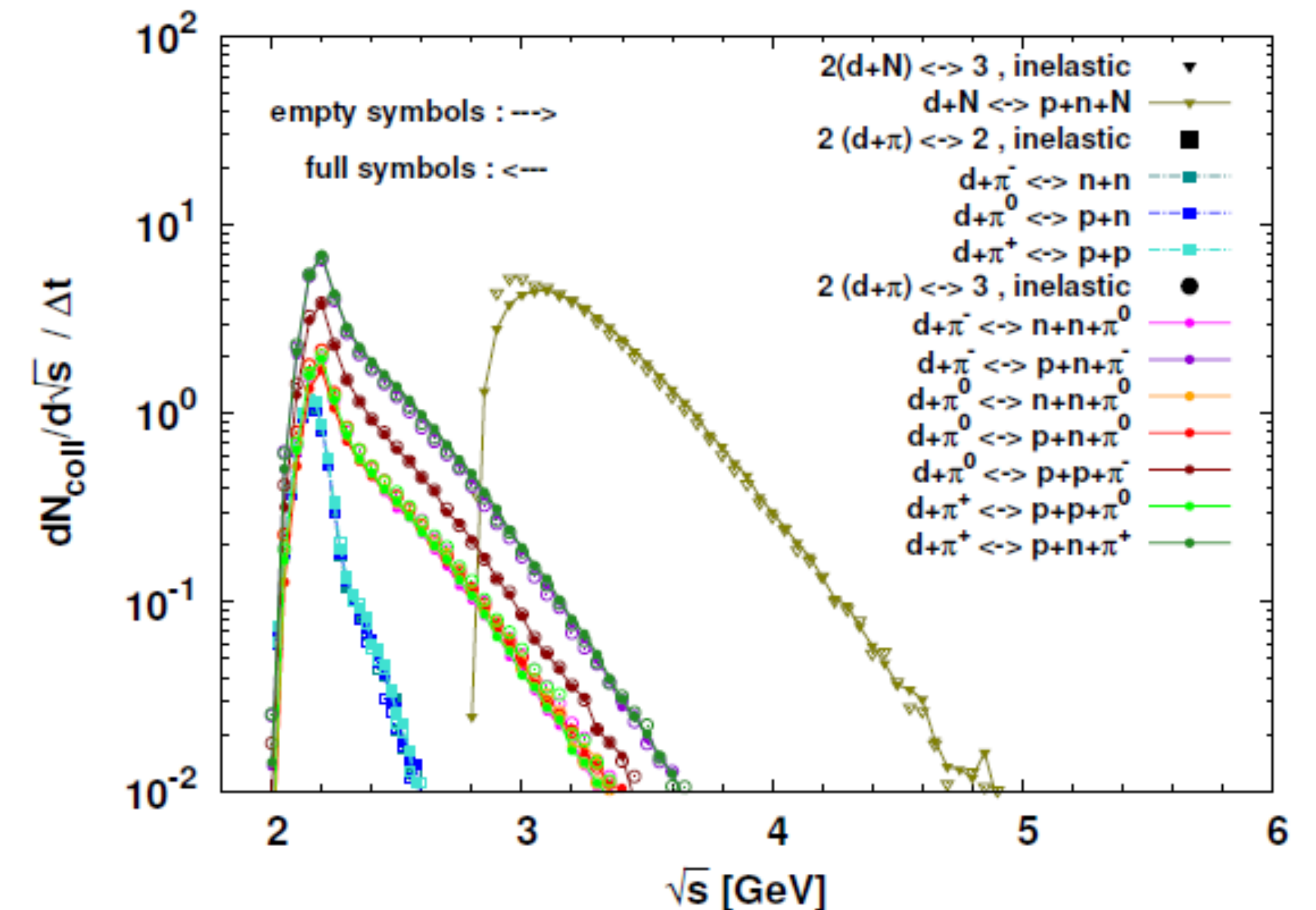
$$|N, N, \pi\rangle = \sum_T \sum_{T_3=-T}^{-T} \langle T, T_3 | N, N, \pi \rangle |T, T_3\rangle$$

Fourier coefficient of eigenstate of total isospin 1 (= T(d  $\pi$ )=T( $\pi$ ))

$$F_{iso} = |\langle N, N, \pi | T(d + \pi) = 1, T_3 \rangle|^2$$

**For the realistic description of HICs:**

**Important to account for all possible isospin channels !**

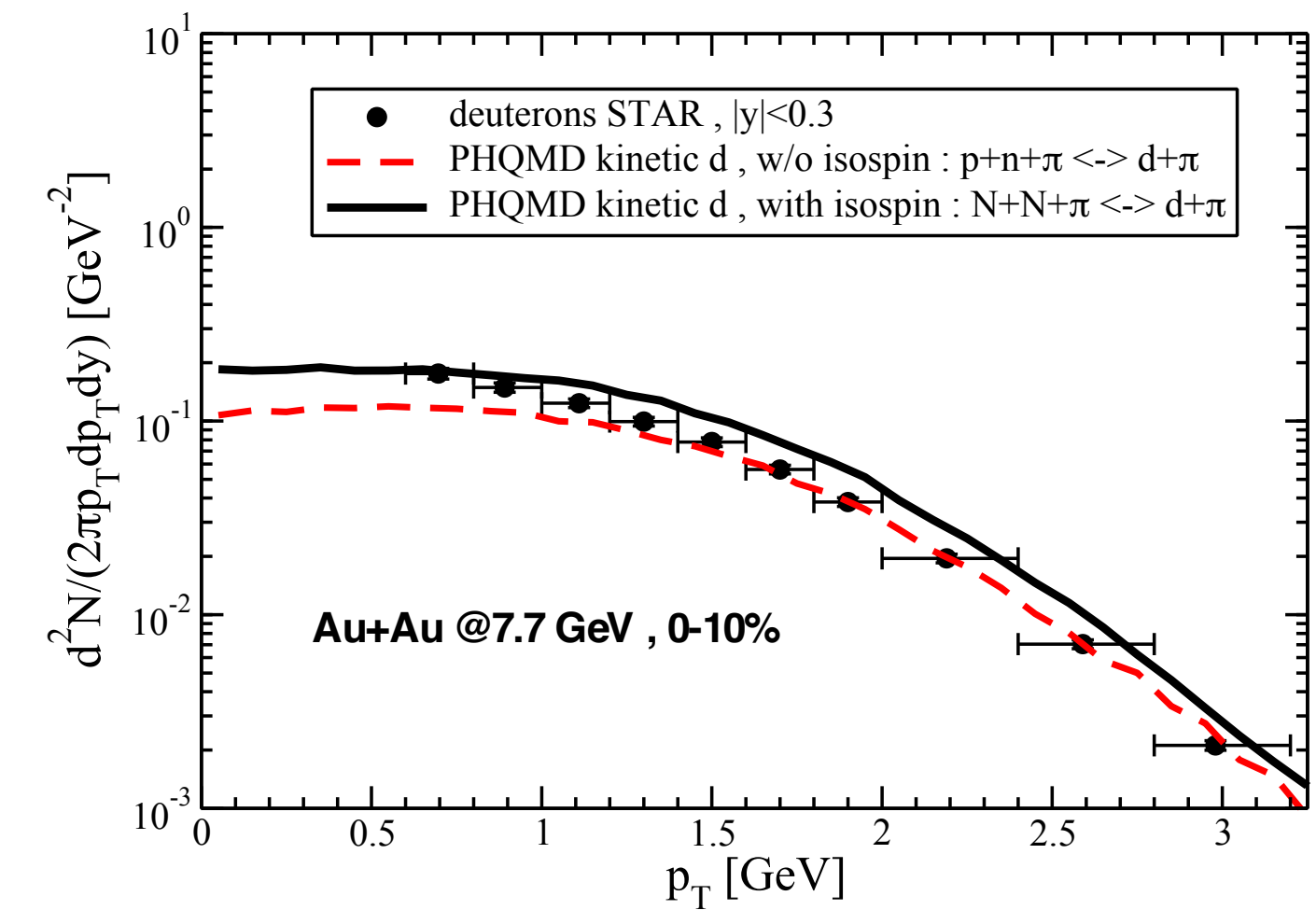
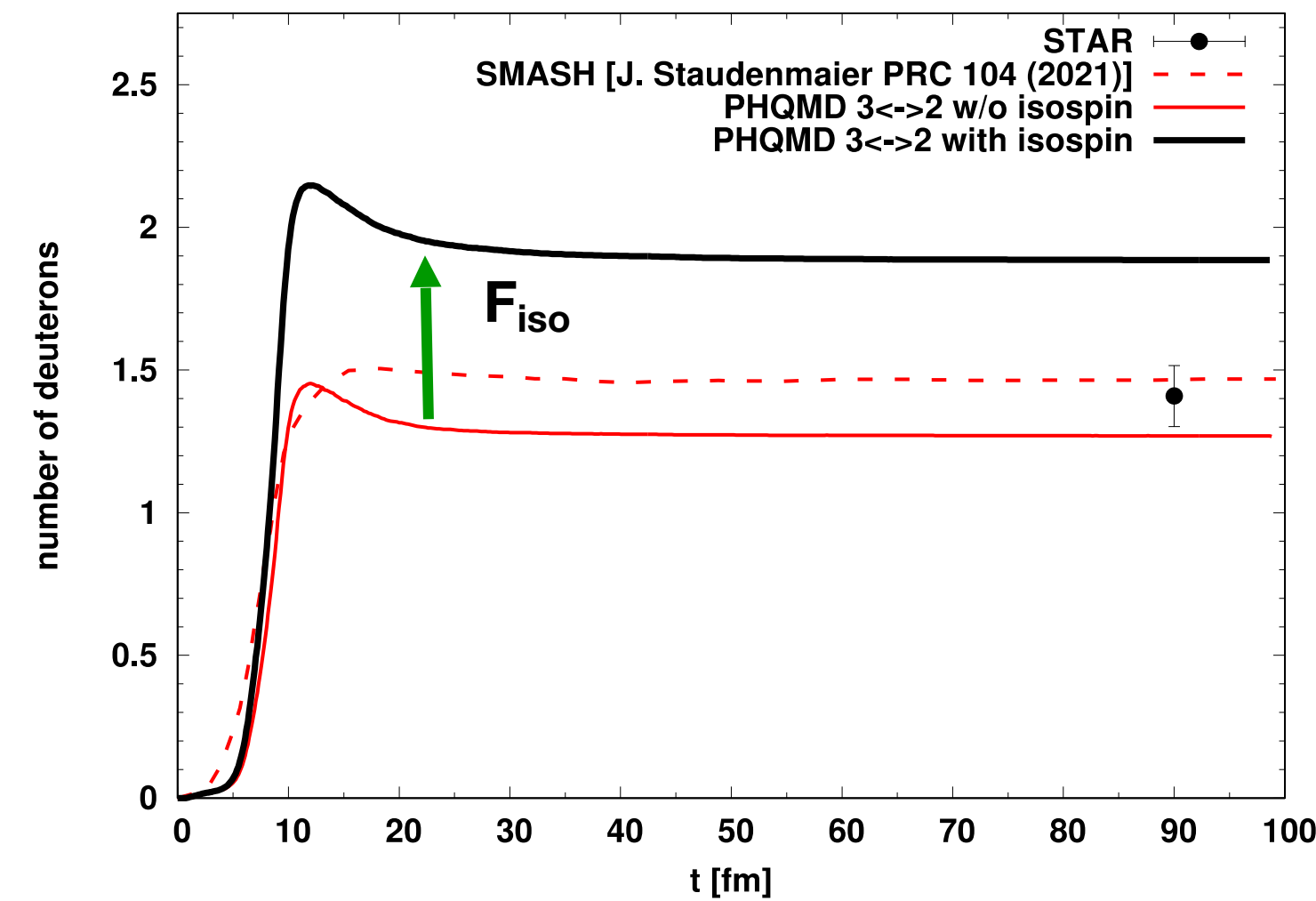


# Kinetic mechanism for deuteron formation

Gabriele Coci et al., in preparation

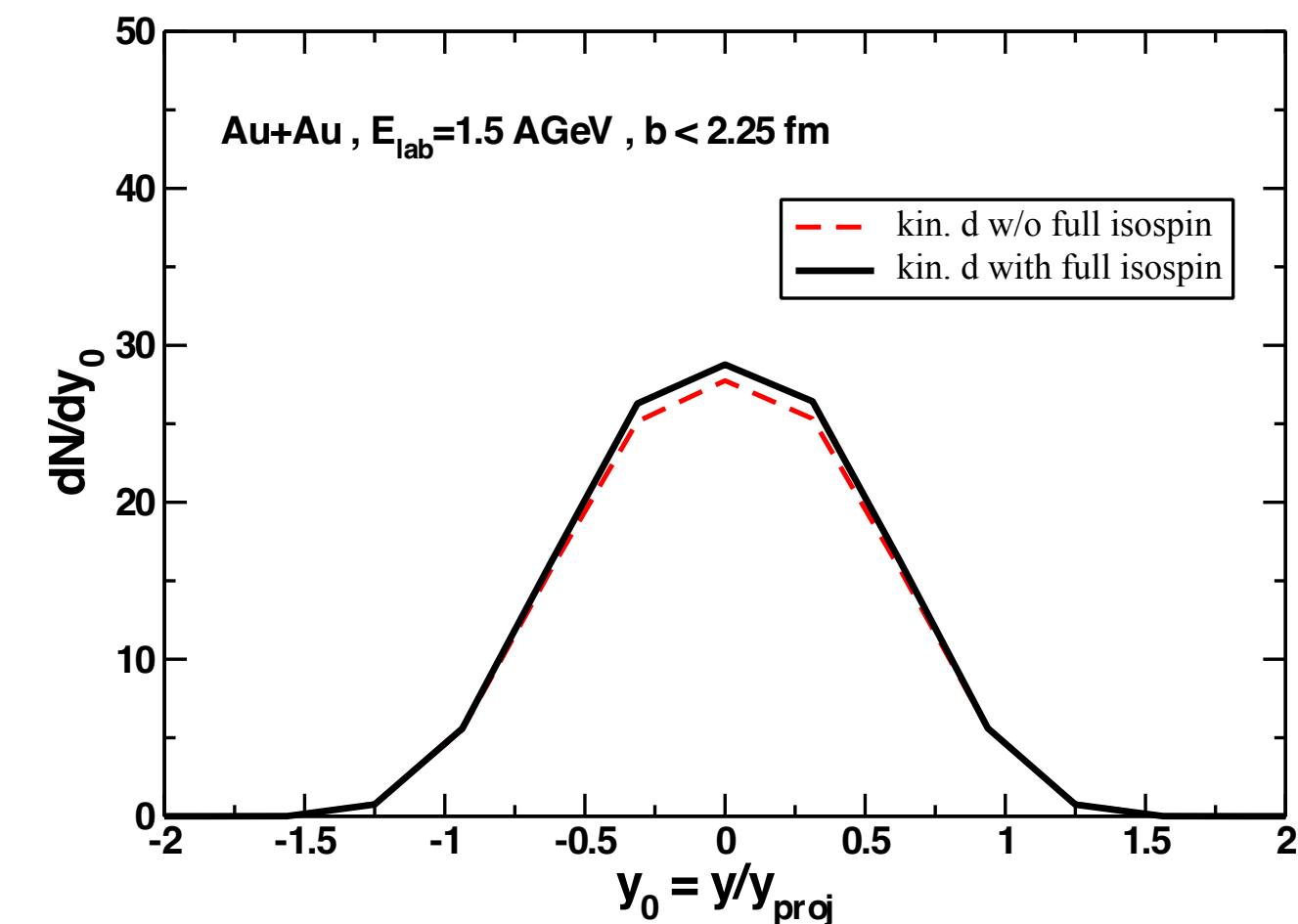
## RHIC BES energy $\sqrt{s} = 7.7$ GeV:

- Hierarchy due to large  $\pi$  abundance  
 $\pi+N+N \rightarrow \pi+d \gg N+p+n \rightarrow N+d$
- Inclusion of **all isospin channels**  
**enhances deuteron yield  $\sim 50\%$ .**
- $p_T$  slope is not affected



## GSI SIS energy $\sqrt{s} < 3$ GeV :

- **Baryon dominated matter**
- Enhancement due to inclusion of isospin  $\pi+N+N$  channels is **negligible**



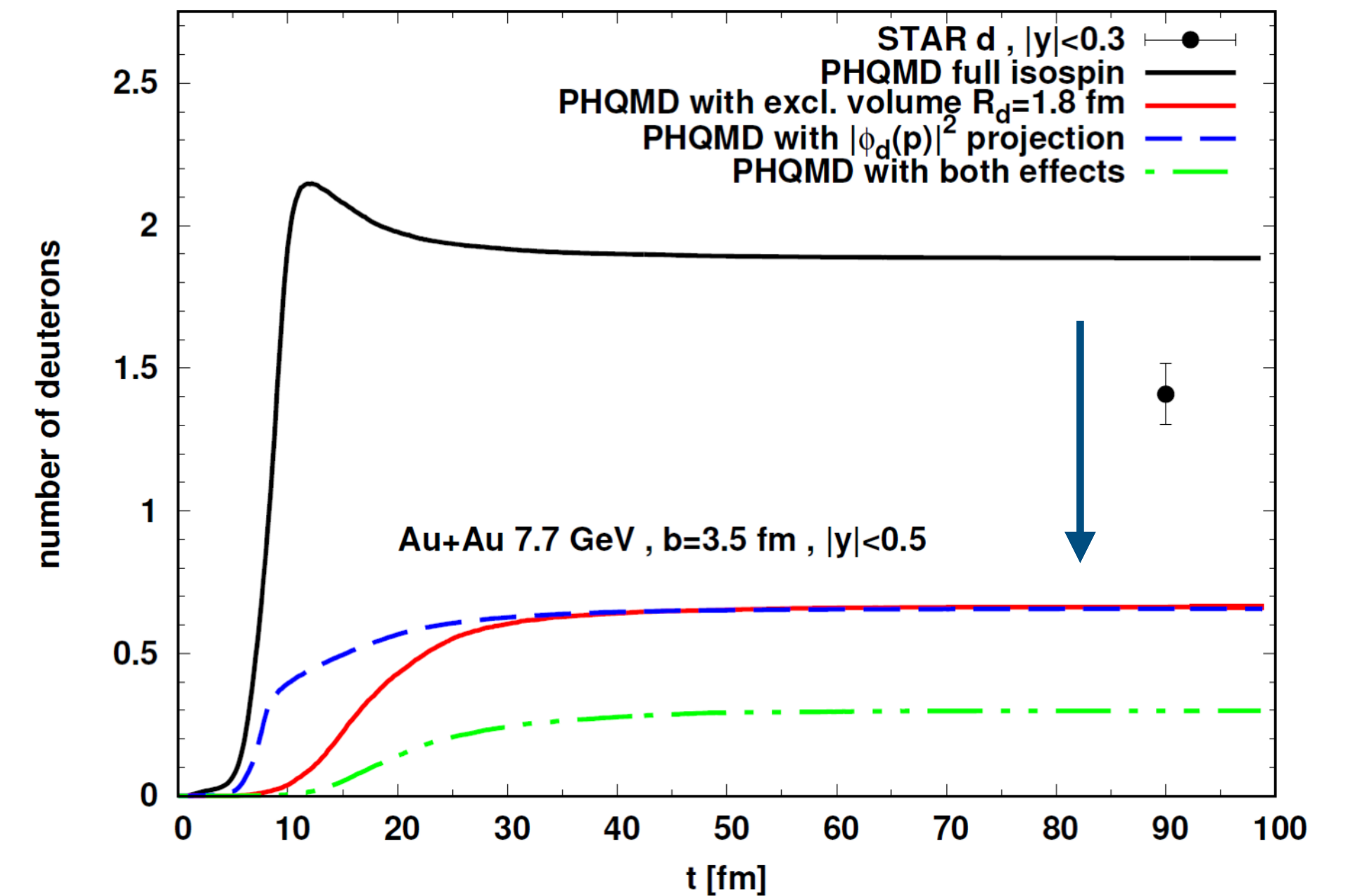
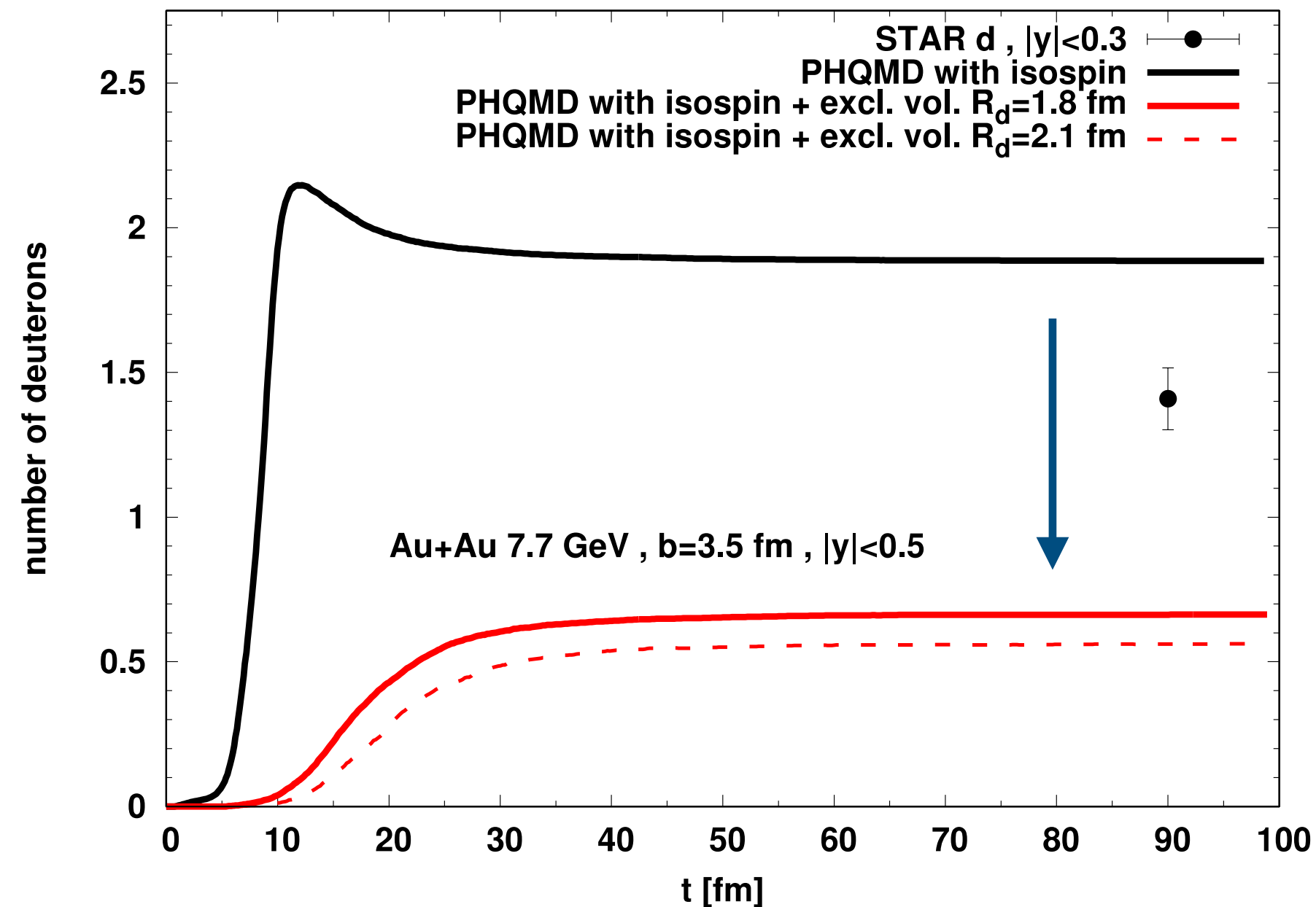
# Kinetic mechanism for deuteron formation

Gabriele Coci et al., in preparation

1) the finite-size of  $d$  in **coordinate space** ( $d$  is not a point-like particle) – for in-medium  $d$  production: assume that a deuteron can not be formed in a high density region, i.e. if there are other particles (hadrons or partons) inside the ‘excluded volume’  $R_d \sim 1.8$  fm

2) the **momentum correlations** of  $p$  and  $n$  inside  $d$ : QM properties of deuteron must be also in momentum space  
 -> **momentum correlations of pn-pair**

- For a “candidate” deuteron calculate the relative momentum  $p$  of the interacting  $pn$ -pair in the deuteron rest frame
- The probability of the  $pn$ -pair to bind into a final deuteron with momentum  $p$  is given by the projection on DWF



Strong reduction of  $d$  production!  
 $p_T$  slope is not affected by excluded volume condition

Strong reduction of  $d$  production by projection on DWF

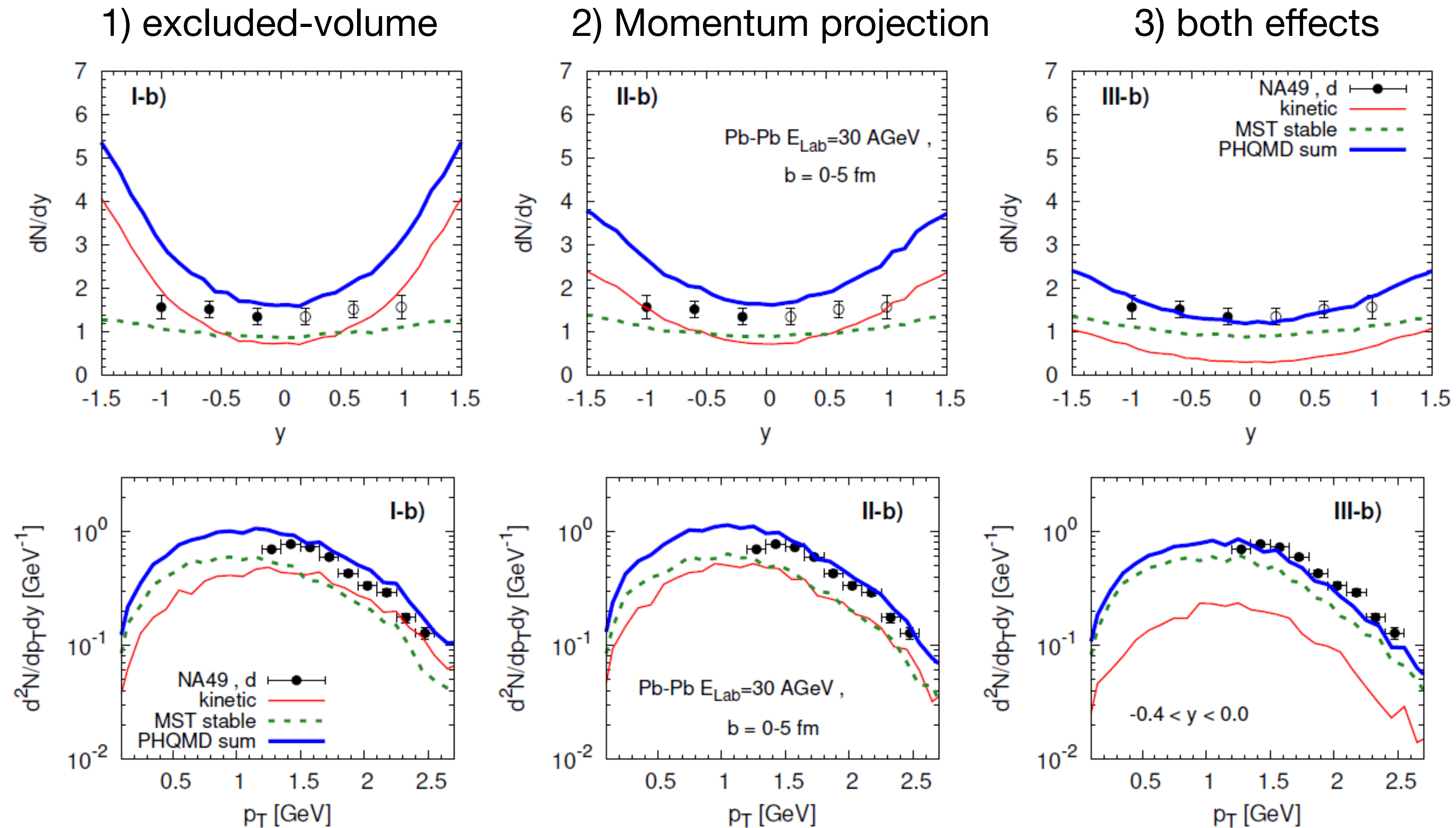


# Kinetic vs potential deuteron formation

Gabriele Coci et al., in preparation

Total deuteron production = **Kinetic mechanism with finite-size effects**  
+ **MST (with stabilization)** identification of deuterons (“stable” bound ( $E_B < 0$ )  $A=2$ ,  $Z=1$  clusters)

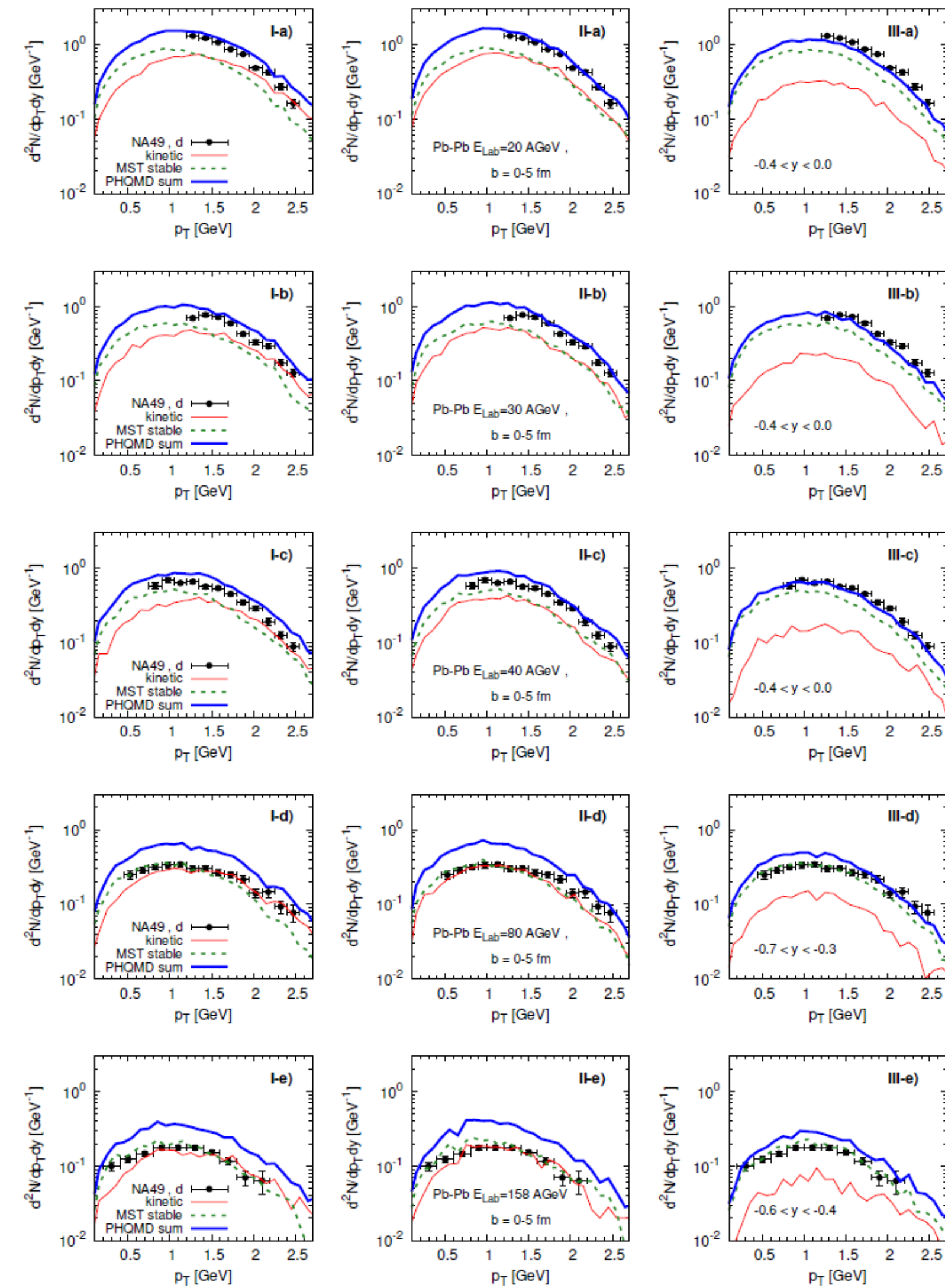
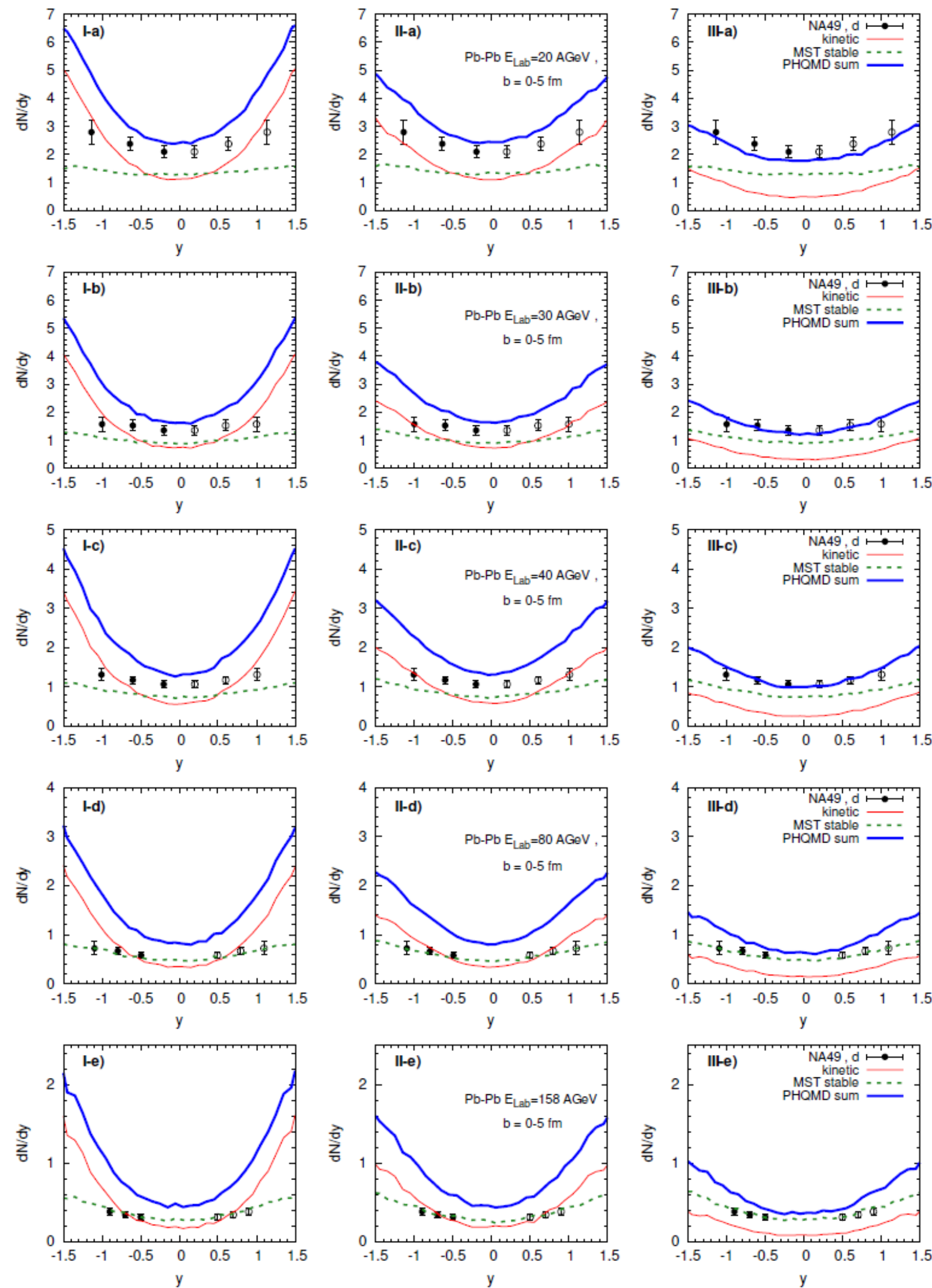
Finite-size effects for kinetic deuterons:



Good description of **mid-rapidity** NA49 data [PRC 94 (2016) 04490699]

# Kinetic vs potential deuteron formation

Gabriele Coci et al., in preparation

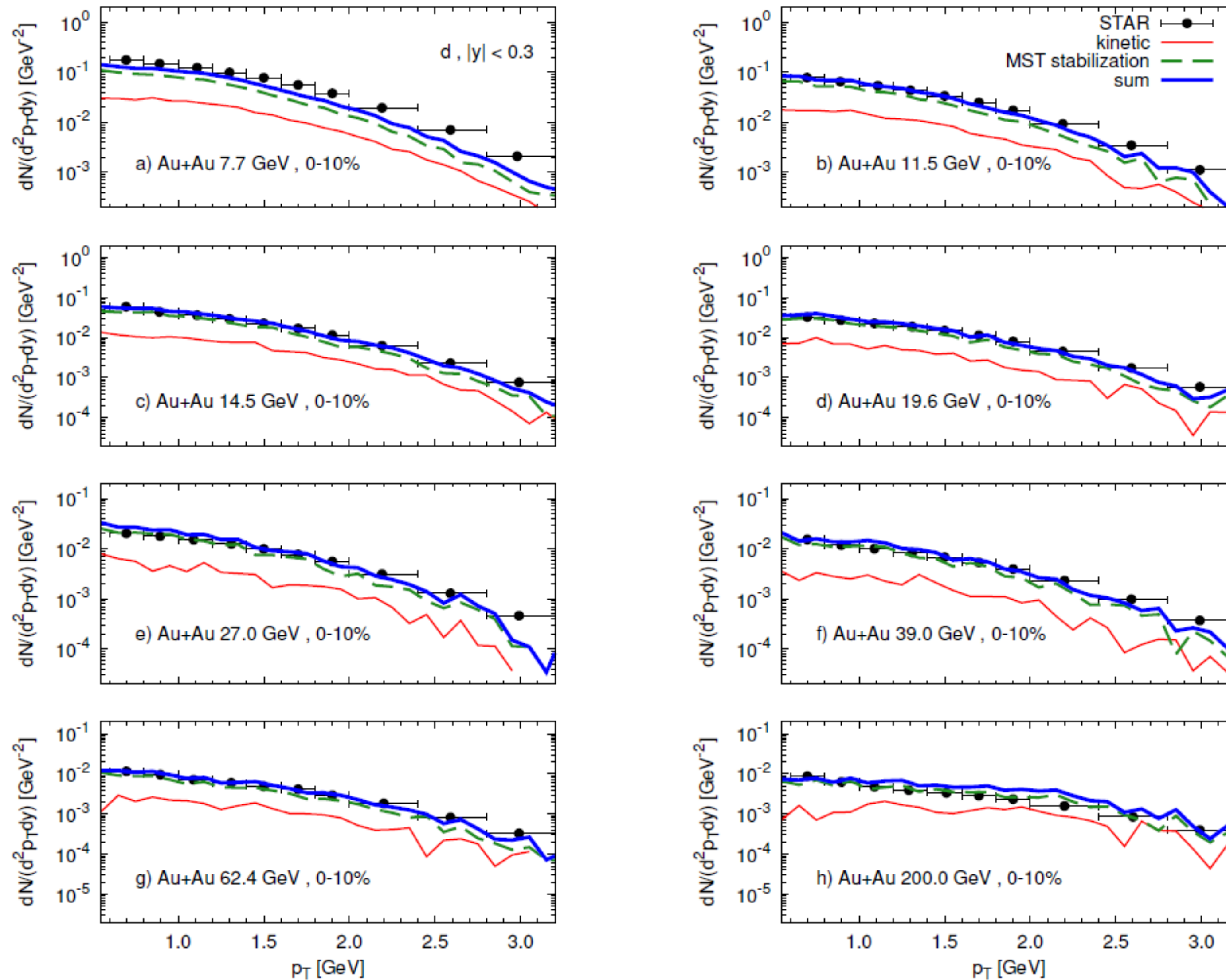


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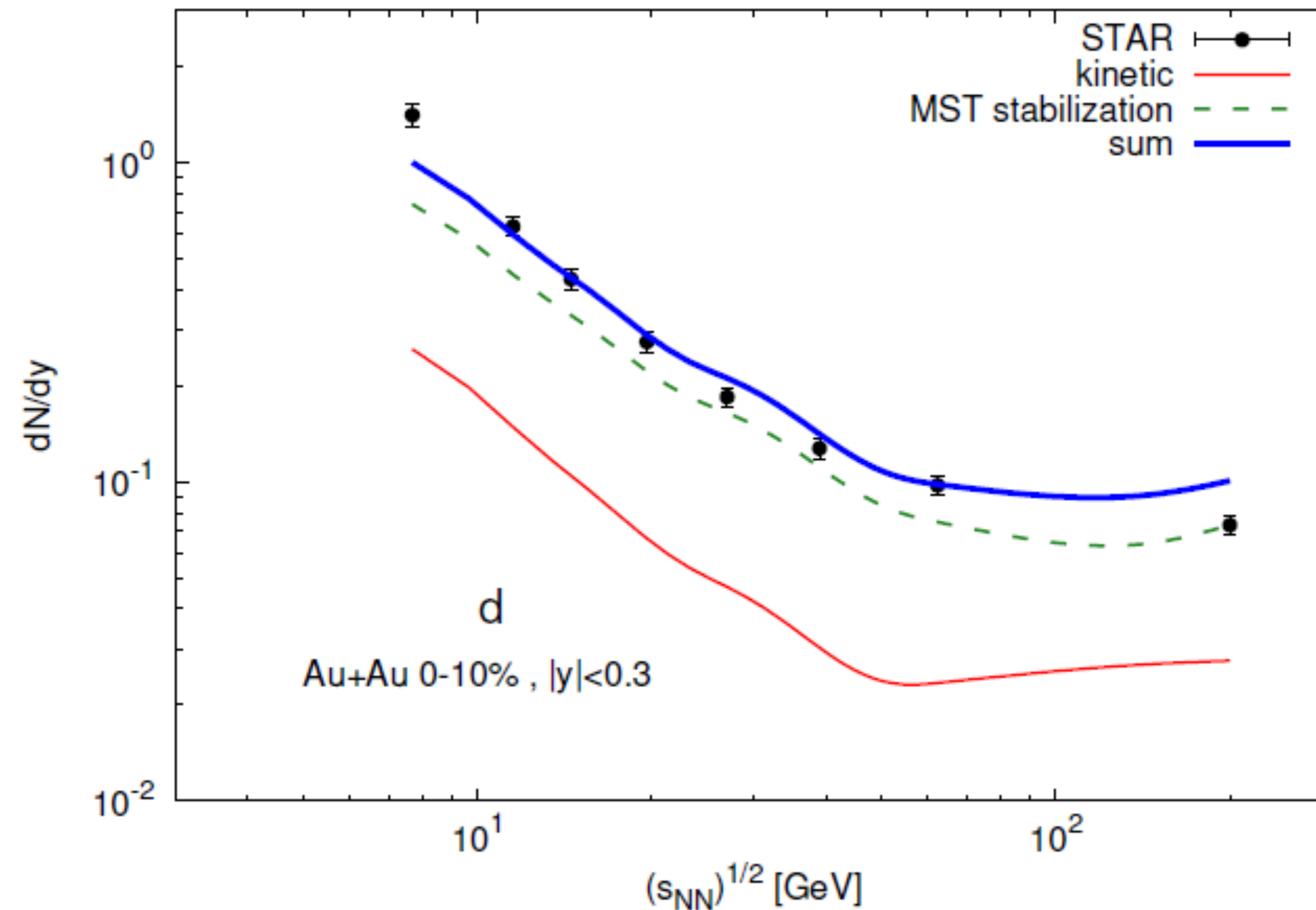


Good description of **mid-rapidity** STAR data [PRC 99, (2019)]

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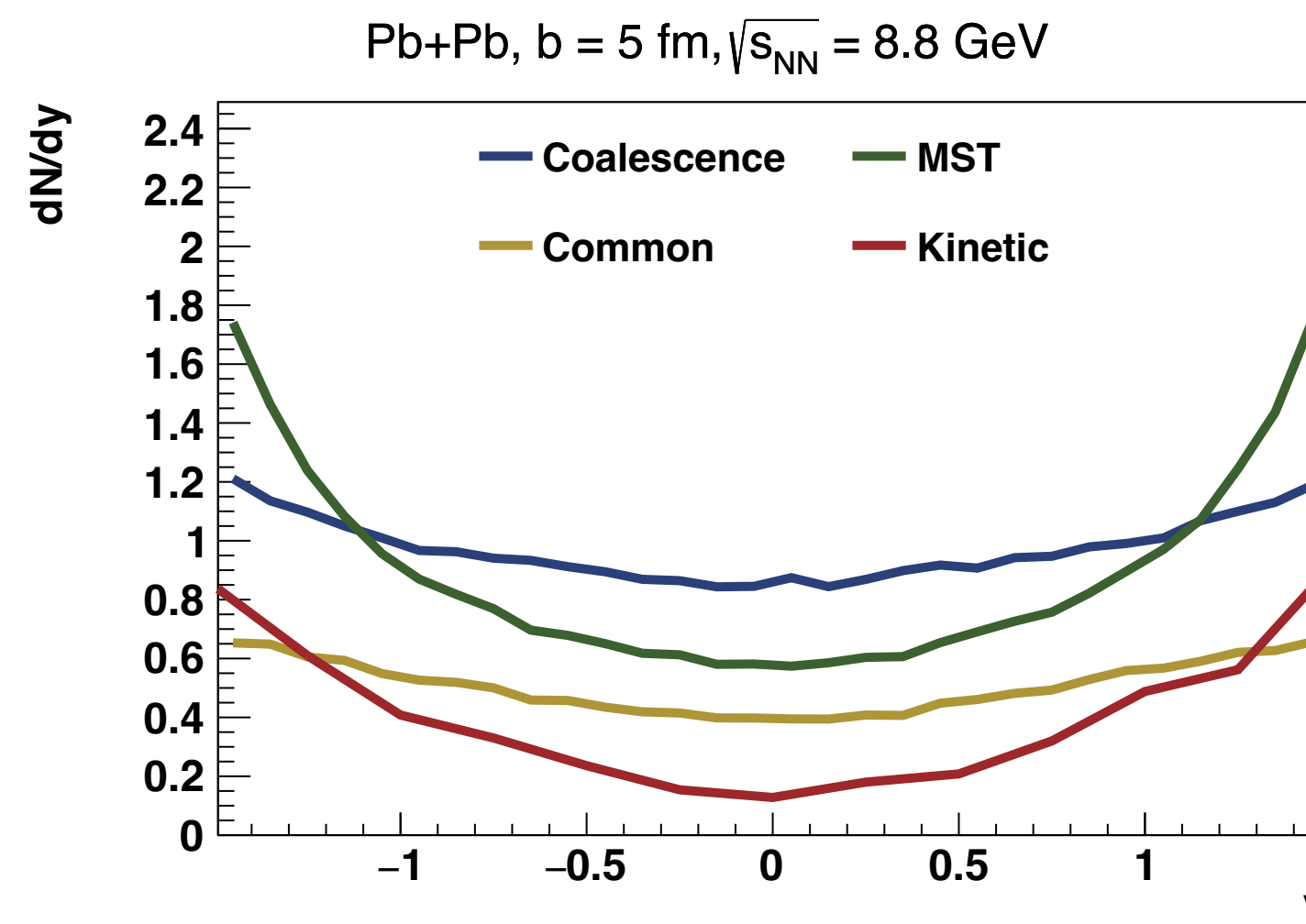
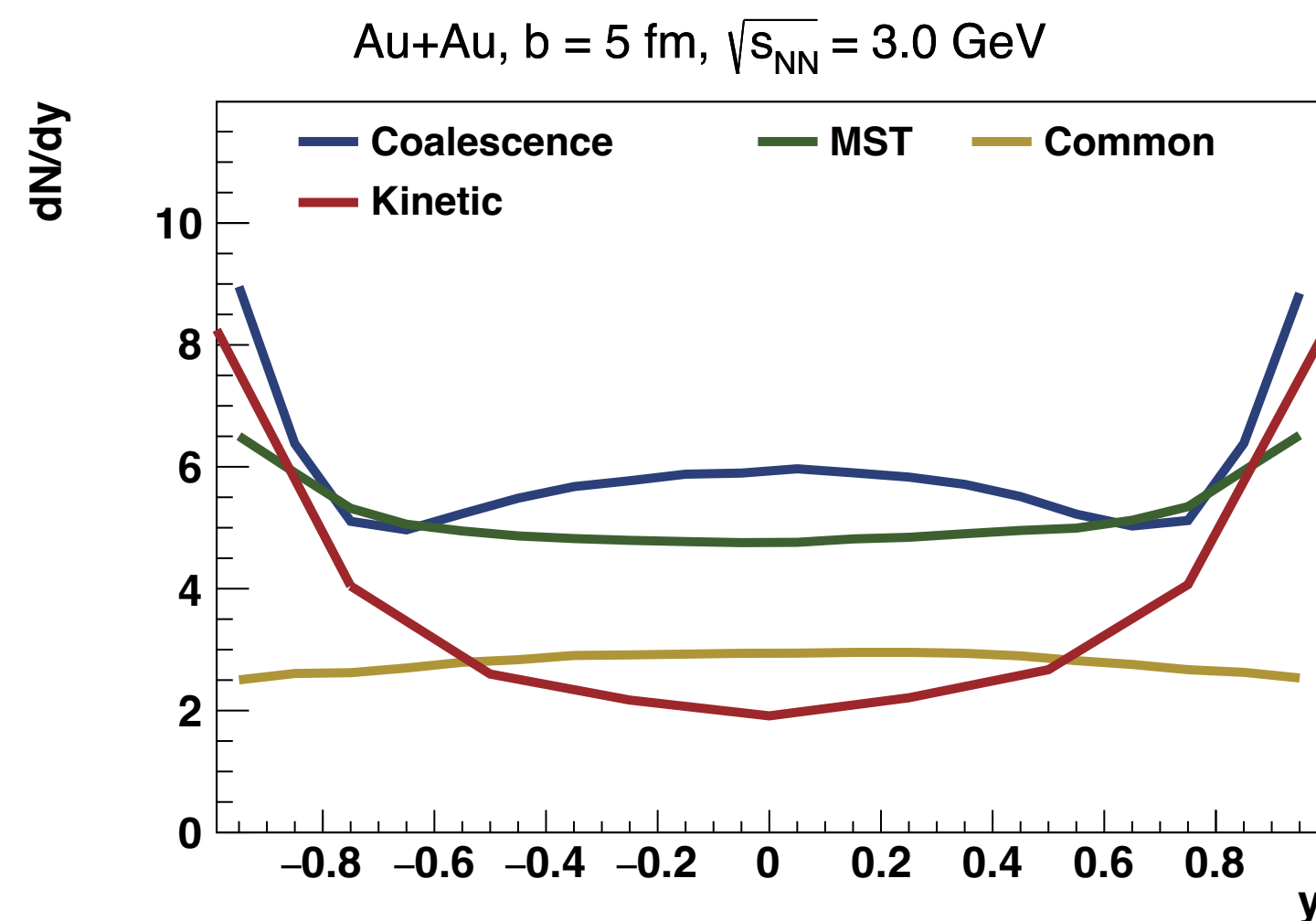
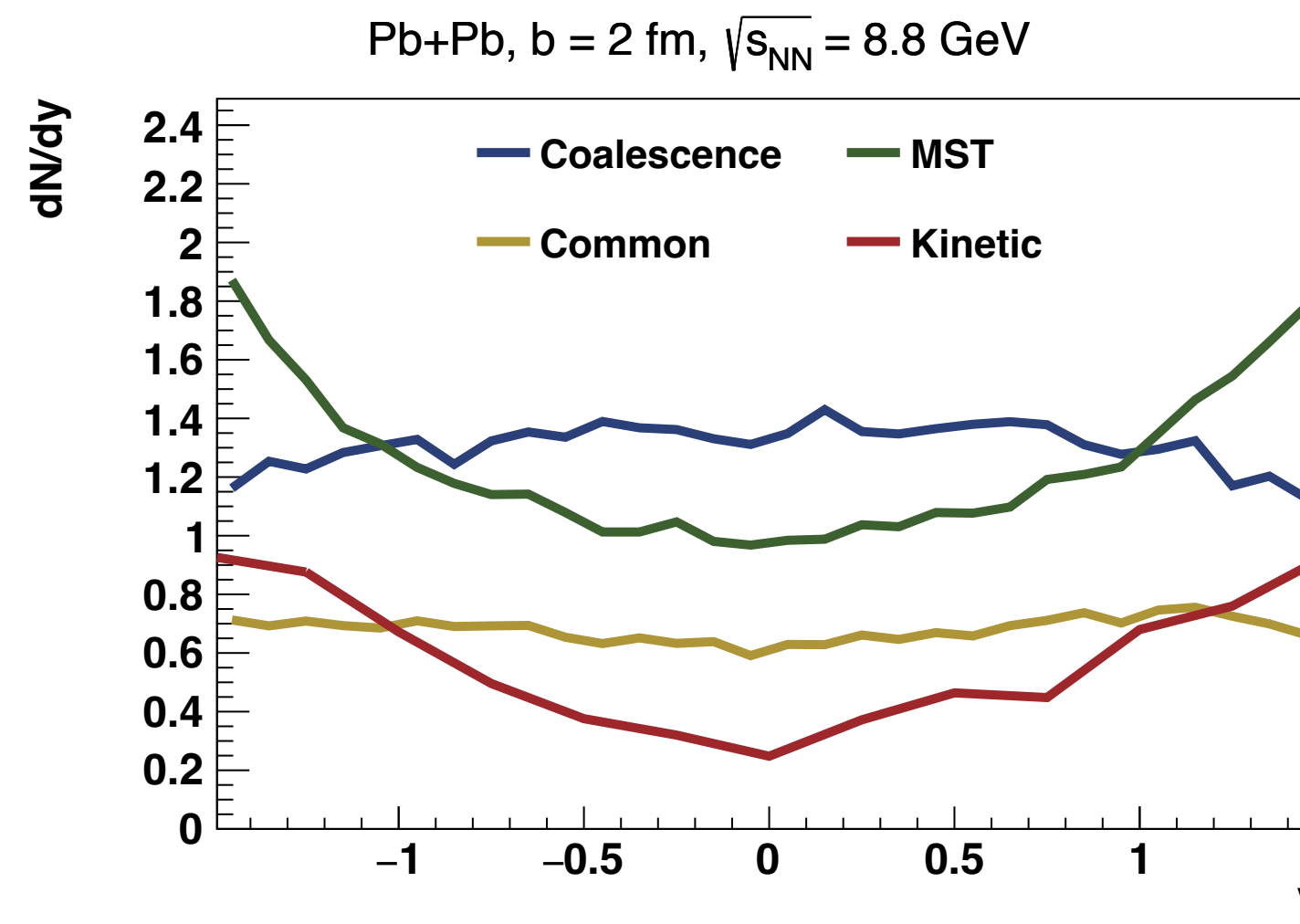
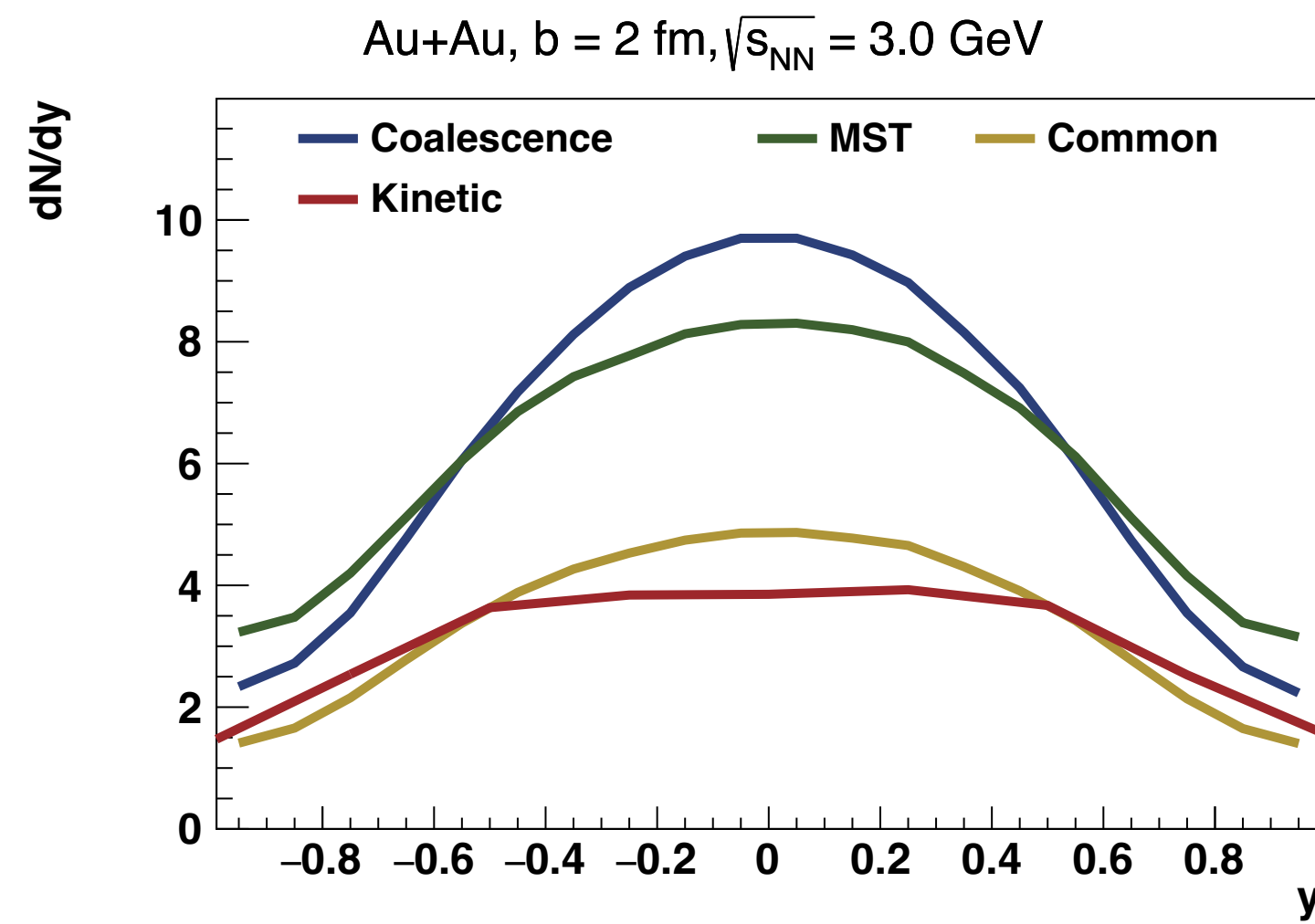


- PHQMD provides a good description of STAR data on d yield at midrapidity
- The potential mechanism is dominant for d production at all energies!

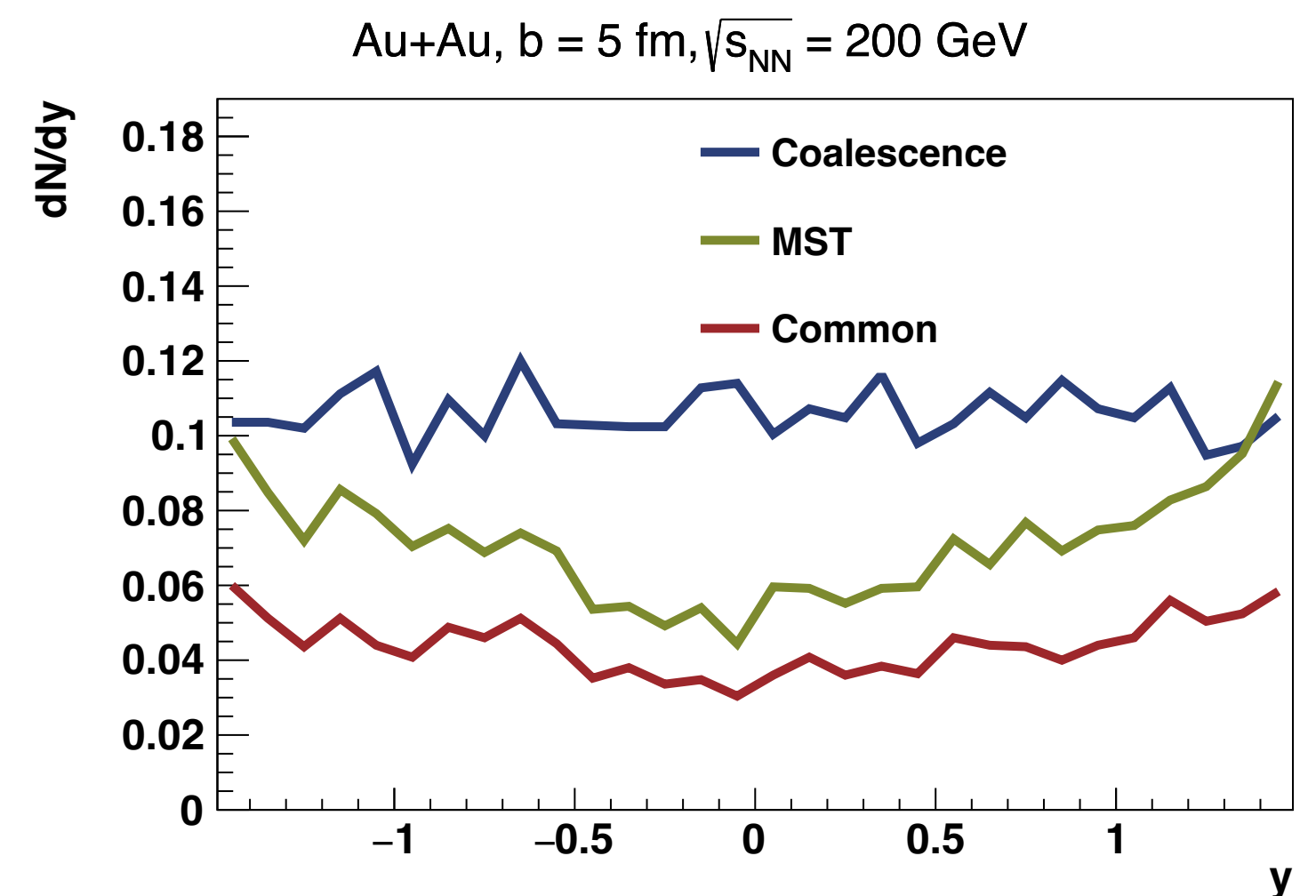
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# Can the deuteron formation mechanism be identified experimentally?

V. Kireyeu, in progress

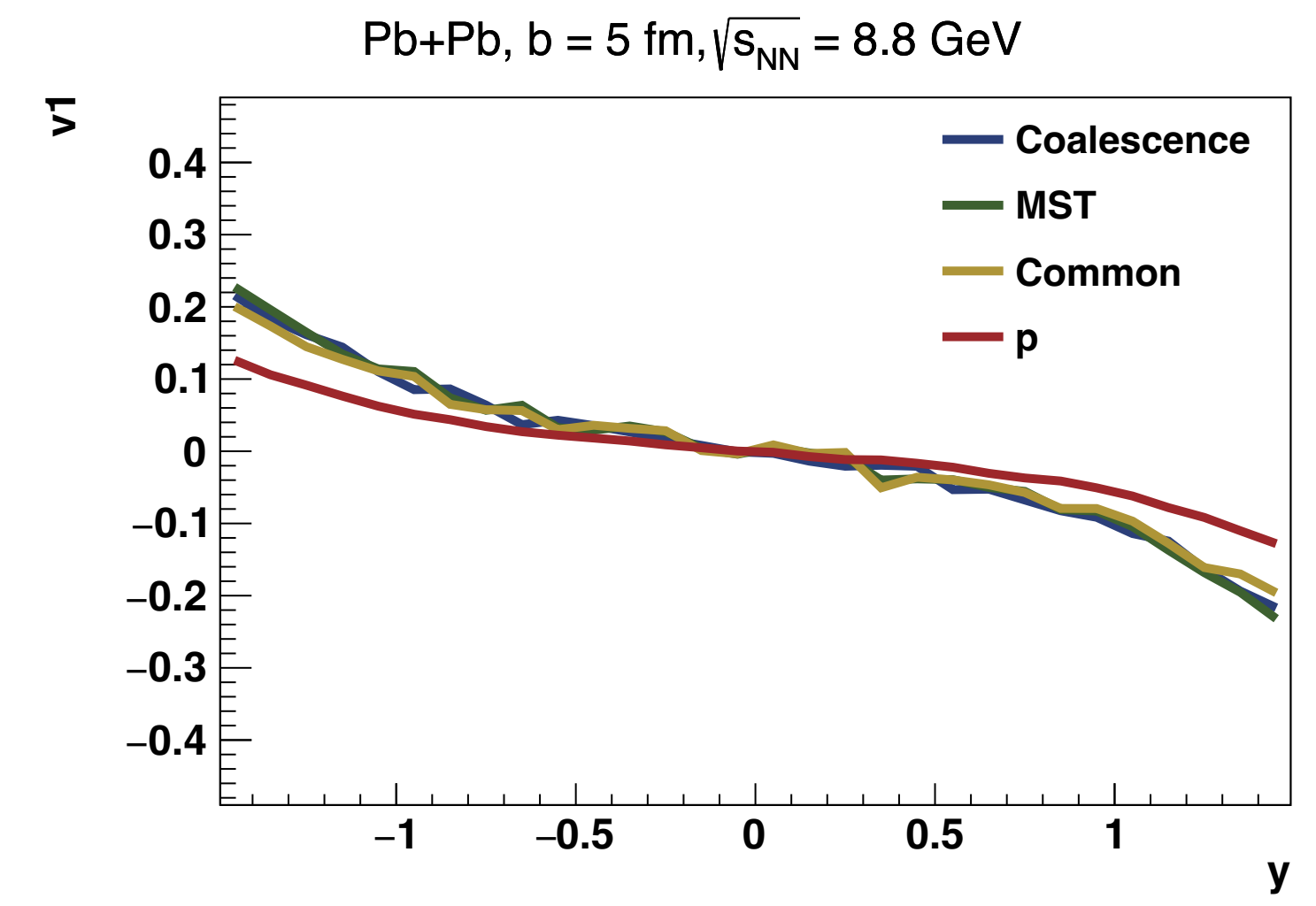
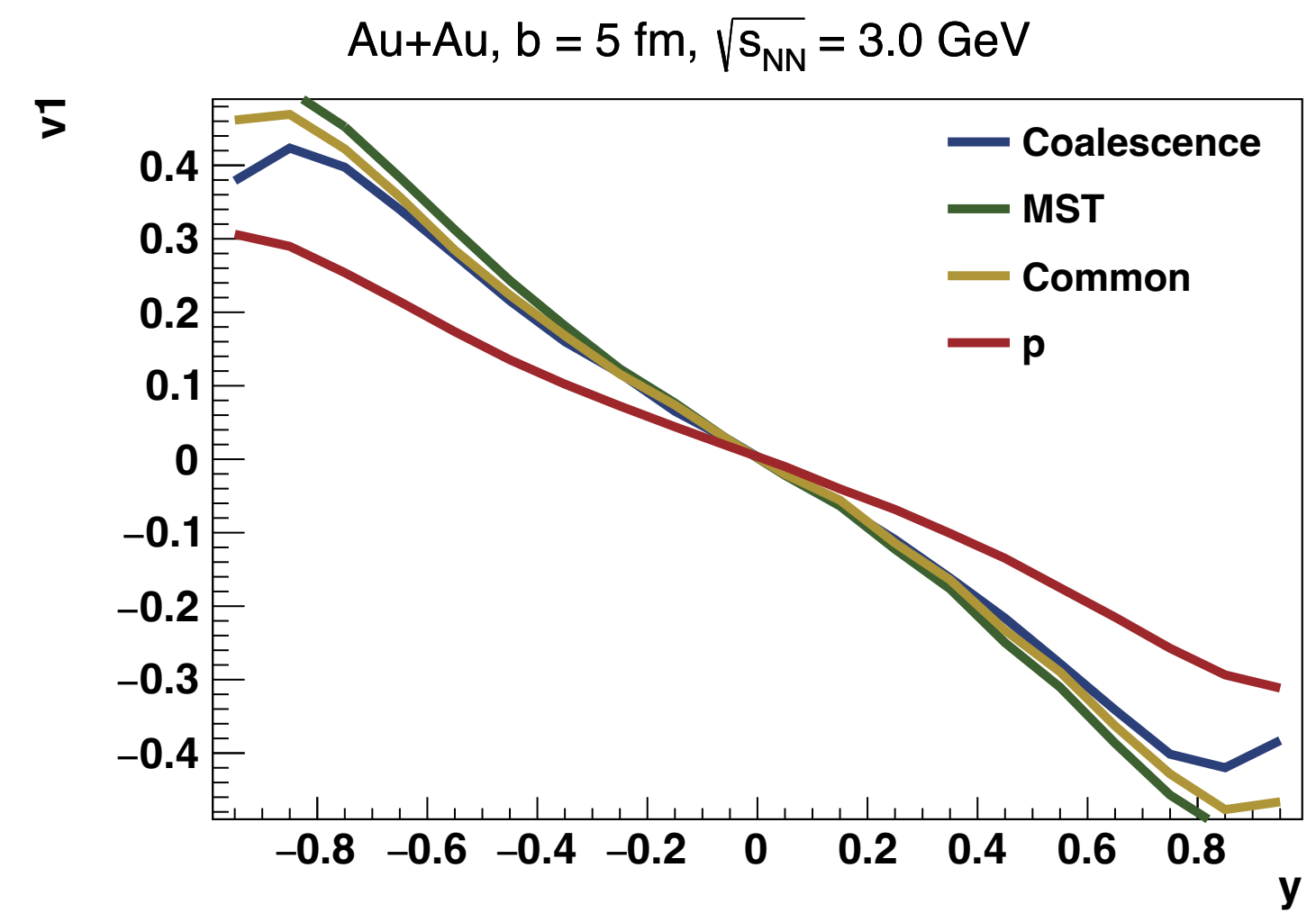
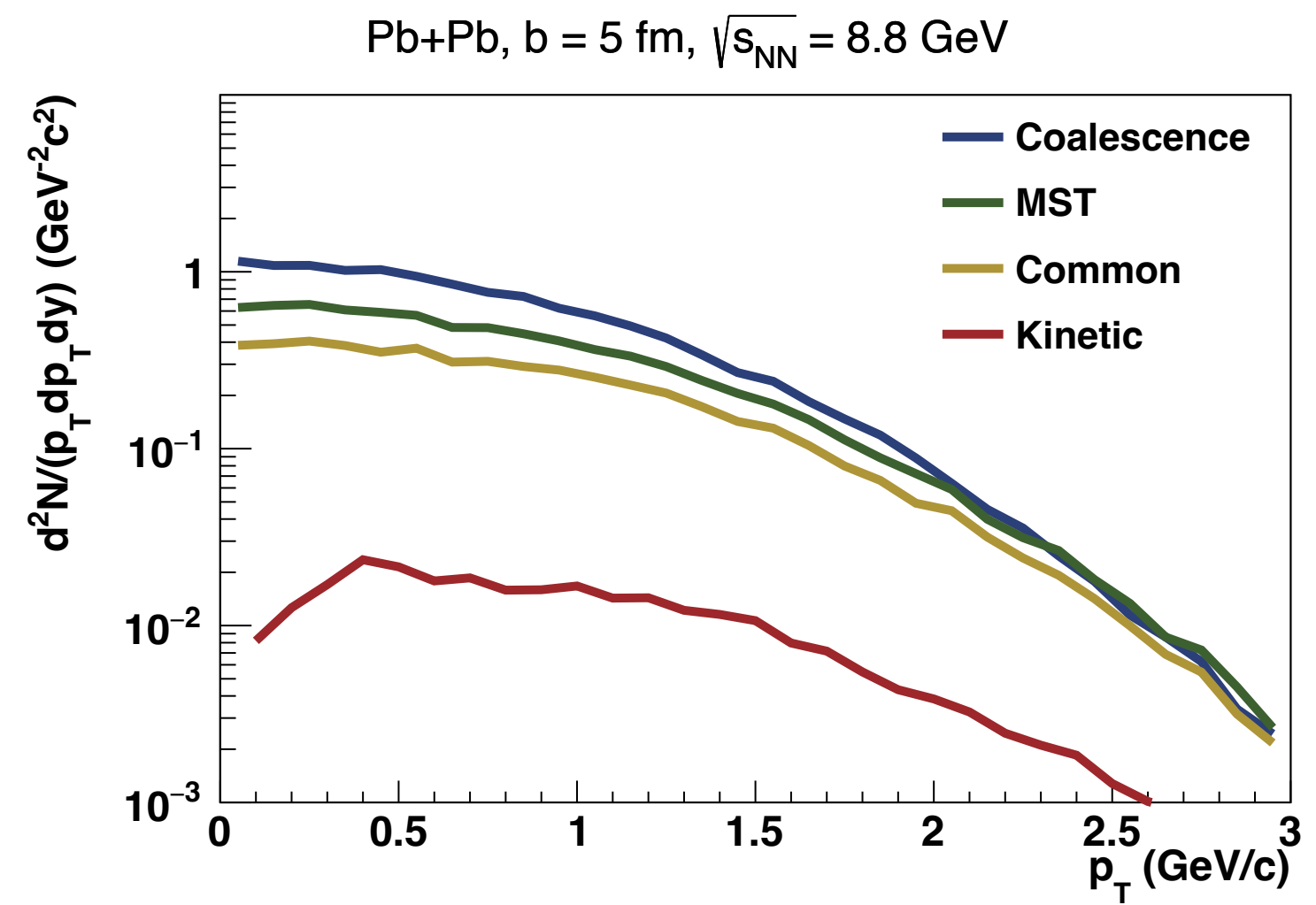
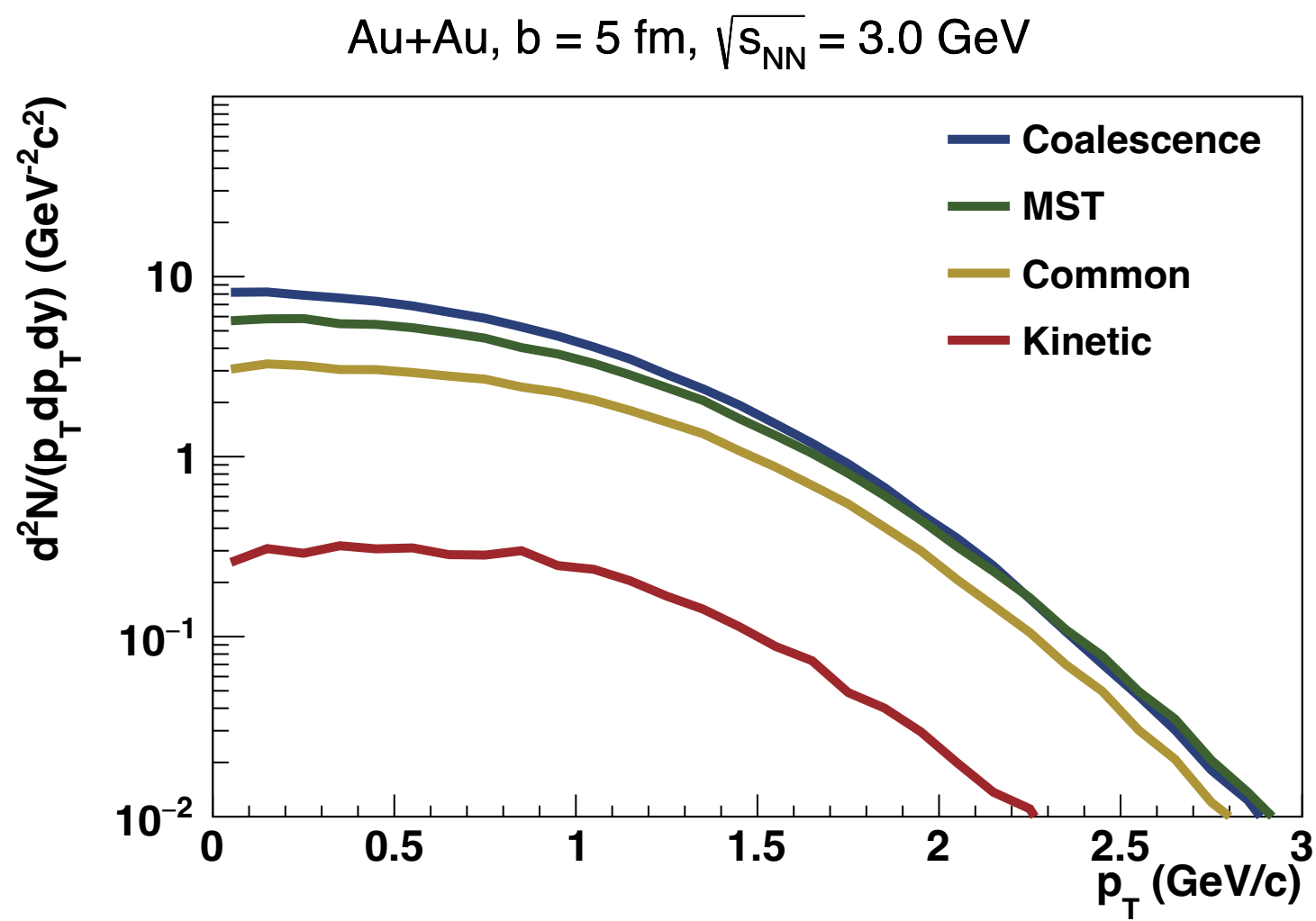


- **At mid-rapidity only ~50%** of coalescence deuterons (at freeze-out) are found by MST.
- Rapidity and  $p_T$  distributions from MST and coalescence have a **different shape  $\rightarrow$  distinguishable in experiments!**



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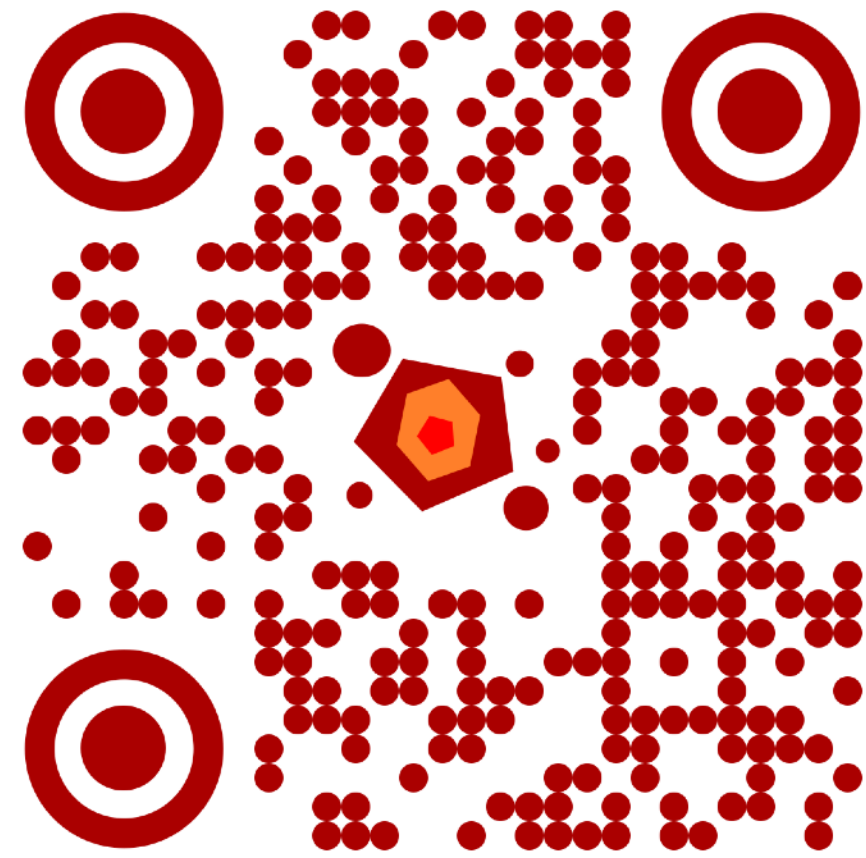
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# Summary

- **The PHQMD** is a microscopic n-body transport approach for the description of heavy-ion dynamics and cluster and hypernuclei formation
- Clusters are formed **dynamically by potential interactions** among nucleons and hyperons and identified by Minimum Spanning Tree model
- **Kinetic mechanism** for deuteron production is implemented in the PHQMD with inclusion of **full isospin** decomposition for hadronic reactions which enhances d production
- However, **accounting for the quantum properties** of the deuteron, modelled by the finite-size excluded volume effect in coordinate space and projection of relative momentum of the interacting pair of nucleons on the deuteron wave-function in momentum space, leads to a **strong reduction of d** production, especially at target/projectile rapidities
- The PHQMD reproduces cluster and hypernuclei data on  $dN/dy$  and  $dN/dp_T$  as well as ratios  $d/p$  and  $\bar{d}/\bar{p}$  for heavy-ion collisions from AGS to top RHIC energies
- A detailed analysis reveals that **stable clusters are formed**:
  - shortly after elastic and inelastic collisions have ceased
  - behind the front of the expanding energetic hadrons
  - **since the 'fire' is not at the same place as the 'ice', cluster can survive**
- PHQMD and UrQMD give very **similar coalescence and MST distributions of deuterons**
- Shape of  $y$ -and  $p_T$ - distributions depends on a **production mechanism → possibility to distinguish between production mechanisms experimentally!**

**Thank you for your attention!**

**Thanks to the Organisers!**



<https://phqmd.gitlab.io/>