

Isospin symmetry breaking in double-pion production  
in the region of  $d^*(2380)$  and the scalar  $\sigma$  meson

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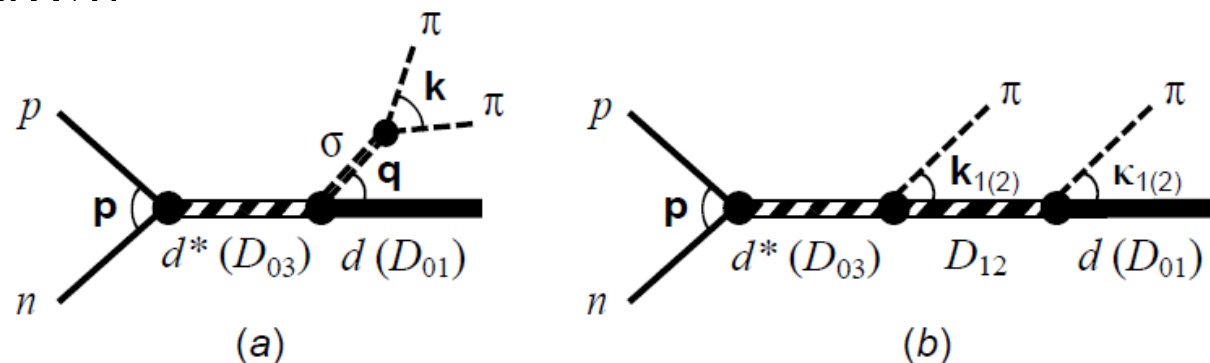
# Introduction

The first attempt is made to provide a quantitative theoretical interpretation of the WASA at-COSY experimental data on the basic double-pion production reactions  $pn \rightarrow d\pi^0\pi^0$  and  $pn \rightarrow d\pi^+\pi^-$  in the energy region  $T_p = 1-1.3\text{GeV}$  [P. Adlarson et al., *Phys. Lett. B* 721, 229 (2013)].

These measurements have revealed the significant isospin symmetry violation in the invariant-mass spectra in the near-threshold region, i.e., a suppression of the ABC enhancement by about 25% for charged dipion production as compared to neutral dipion production.

N.E. Booth, A. Abashian, and K.M. Crowe, *Phys. Rev. Lett.* 7, 35 (1961); A. Abashian, N.E. Booth, and K.M. Crowe, *ibid.* 5, 258 (1960).

M.N. Platonova and V.I. Kukuin, *Phys. Rev. C* 87, 025202 (2013)



Mass

$\pi^\pm: 139.57039(18) \text{ MeV}/c^2[1]$

$\pi^0: 134.9768(5) \text{ MeV}/c^2[1]$

# Formalism for the double-pion production reactions $pn \rightarrow d(\pi\pi)0$ in the region of $d^*(2380)$

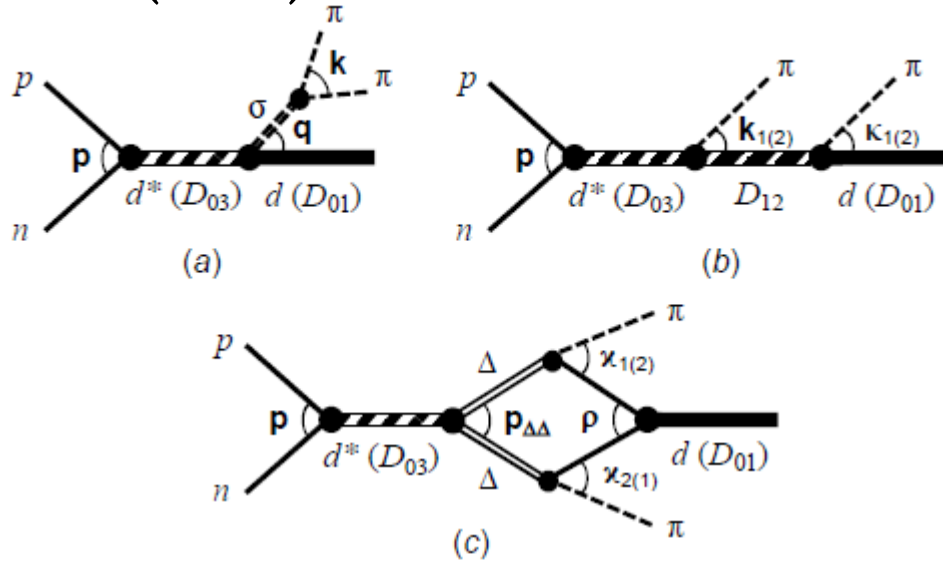


FIG. 1: Diagrams of different mechanisms for double-pion production in the region of the  $D_{03}$  (or  $d^*(2380)$ ) resonance formation. The 3-momenta in the pair center-of-mass frames are indicated between the respective lines.

$$\mathcal{M}_{\lambda_p, \lambda_n, \lambda_d} = \frac{\sum_{\lambda_3} \mathcal{M}_{\lambda_p, \lambda_n, \lambda_3}^{(D_{03})} \left[ \mathcal{M}_{\lambda_3, \lambda_d}^{(\sigma)} + \mathcal{M}_{\lambda_3, \lambda_d}^{(D_{12})} + \mathcal{M}_{\lambda_3, \lambda_d}^{(\Delta\Delta)} \right]}{s - M_{D_{03}}^2 + i\sqrt{s}\Gamma_{D_{03}}(s)}$$

$$\mathcal{M}_{\lambda_p, \lambda_n, \lambda_3}^{(D_{03})} = F_{pn \rightarrow D_{03}}(p) C_{1\lambda_3 20}^{3\lambda_3} C_{\frac{1}{2}\lambda_p \frac{1}{2}\lambda_n}^{1\lambda_3} Y_{20}(\hat{p}),$$

$$\mathcal{M}_{\lambda_3, \lambda_d}^{(\sigma)} = \frac{F_{D_{03} \rightarrow d\sigma}(q) F_{\sigma \rightarrow \pi\pi}(k)}{M_{\pi\pi}^2 - m_\sigma^2 + iM_{\pi\pi}\Gamma_\sigma(M_{\pi\pi}^2)} C_{1\lambda_d 2\mu}^{3\lambda_3} Y_{2\mu}(\hat{q}),$$

$$\mathcal{M}_{\lambda_3, \lambda_d}^{(D_{12})} = \frac{F_{D_{03} \rightarrow D_{12}\pi_1}(k_1) F_{D_{12} \rightarrow d\pi_2}(\kappa_1)}{M_{d\pi_2}^2 - M_{D_{12}}^2 + iM_{d\pi_2}\Gamma_{D_{12}}(M_{d\pi_2}^2)}$$

$$\times \sum_{\lambda_2} C_{2\lambda_2 1\mu_2}^{3\lambda_3} C_{1\lambda_d 1\mu_1}^{2\lambda_2} Y_{1\mu_2}(\hat{k}_1) Y_{1\mu_1}(\hat{\kappa}_1) + (\pi_1 \leftrightarrow \pi_2),$$

$$\mathcal{M}_{\lambda_3, \lambda_d}^{(\Delta\Delta)} = \int \frac{d^3\rho}{(2\pi)^3} \varphi_d(\rho) F_{D_{03} \rightarrow \Delta\Delta}(p_{\Delta\Delta})$$

$$\times G_\Delta(M_{N_1\pi_1}) G_\Delta(M_{N_2\pi_2}) F_{\Delta \rightarrow N_1\pi_1}(\varkappa_1) F_{\Delta \rightarrow N_2\pi_2}(\varkappa_2)$$

$$\times \sum_{\lambda_{\Delta_1} \lambda_{N_1}} C_{\frac{3}{2}\lambda_{\Delta_1} \frac{3}{2}\lambda_{\Delta_2}}^{3\lambda_3} C_{\frac{1}{2}\lambda_{N_1} 1\mu_1}^{\frac{3}{2}\lambda_{\Delta_1}} C_{\frac{1}{2}\lambda_{N_2} 1\mu_2}^{\frac{3}{2}\lambda_{\Delta_2}} C_{\frac{1}{2}\lambda_{N_1} \frac{1}{2}\lambda_{N_2}}^{1\lambda_d}$$

$$\times Y_{1\mu_1}(\hat{\varkappa}_1) Y_{1\mu_2}(\hat{\varkappa}_2) + (\pi_1 \leftrightarrow \pi_2), \quad (5)$$

# Neutral and charged dipion production via the intermediate $D_{12}$ and $\Delta$ $\Delta$ excitation

TABLE I: Parameters of resonances  $R$  and their decay channels  $R \rightarrow a + b$ . For the parameter  $p_0$ , the given interval corresponds to all possible isospin channels.

$R$	$M_R$ (MeV)	$\Gamma_R^{(0)}$ (MeV)	$ab$	$l$	$p_0$ (MeV)	$\Gamma_{R \rightarrow ab}^{(0)}$ (MeV)	$\Lambda_{ab}$ (GeV)
$\mathcal{D}_{03}$	2376	77	$np$	2	730	9	0.35
			$\sigma d$	2	350	2	0.18
			$\pi \mathcal{D}_{12}$	1	173–176	31	0.12
$\mathcal{D}_{12}$	2150	110	$\pi d$	1	221–223	33	0.15
$\Delta$	1232	117	$\pi N$	1	226–229	117	0.16
$\sigma$	303	126	$\pi\pi$	0	72–80	126	0.09

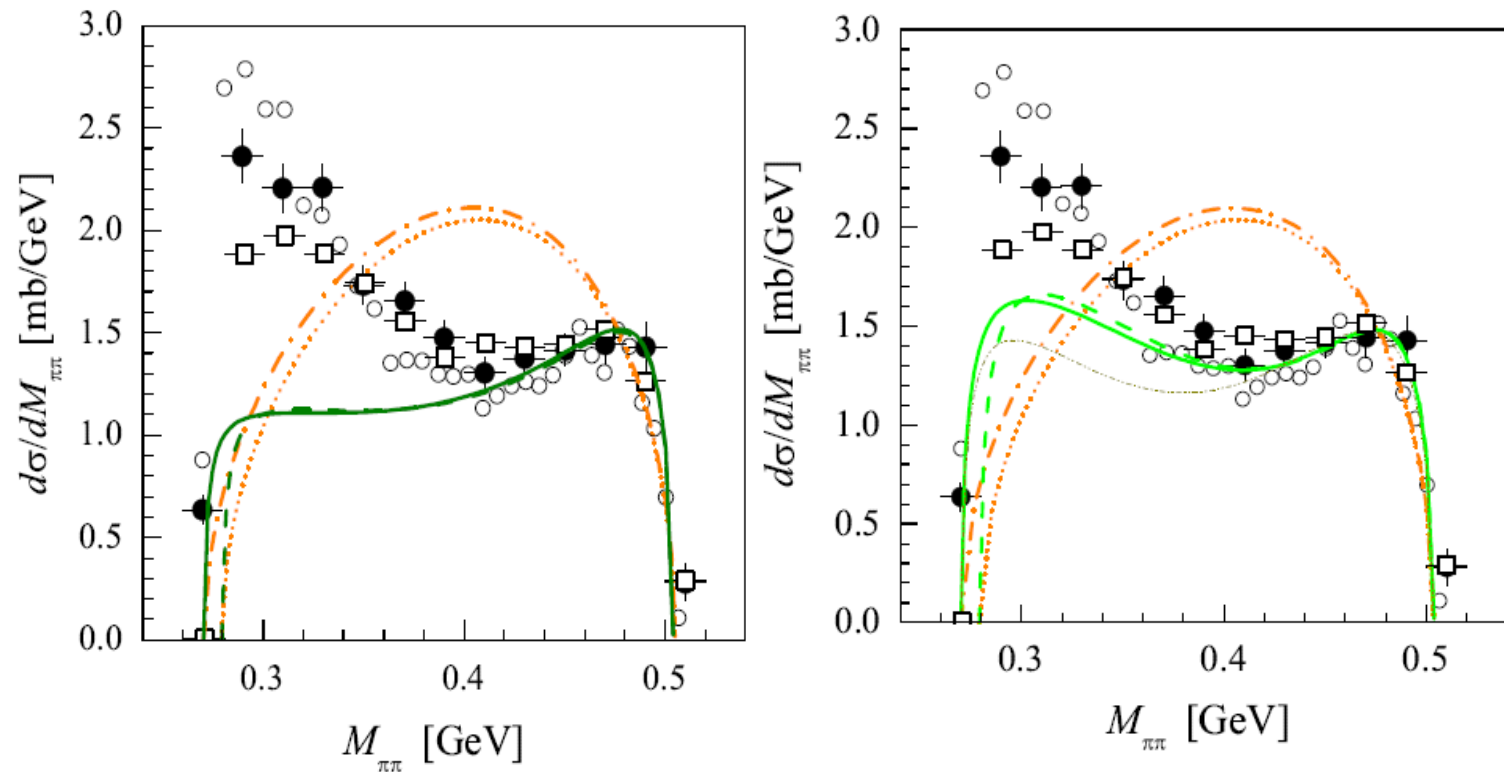


FIG. 2: (Color online) The  $\pi\pi$  invariant-mass distributions in the reactions  $pn \rightarrow d\pi^+\pi^-$  (multiplied by 2, solid line) and  $pn \rightarrow d(\pi^+\pi^-)_0$  (dashed line) at  $\sqrt{s} = 2.38$  GeV resulted from the  $\mathcal{D}_{03} \rightarrow \mathcal{D}_{12}\pi$  decay in the intermediate state. The theoretical calculations are compared to the experimental data on  $2d\sigma/dM_{\pi^+\pi^-}$  (filled circles) and  $d\sigma/dM_{\pi^+\pi^-} - \frac{1}{2}d\sigma/dM_{\pi^+\pi^0}$  (open squares) from Ref. [9], as well as the data on  $2d\sigma/dM_{\pi^0\pi^0}$  from Ref. [8] (open circles). The latter data have been multiplied by 0.45 (see Appendix). The model parameters are those listed in Tab. I, except for the parameter  $\Gamma_{\mathcal{D}_{03} \rightarrow \mathcal{D}_{12}\pi}^{(0)}$ , which has been adjusted to reproduce the experimental data at high invariant masses. Also shown are the pure phase-space distributions for  $\pi^0\pi^0$  (dash-dotted line) and  $\pi^+\pi^-$  (dotted line) production normalized to the respective total cross sections.

FIG. 3: (Color online) The same as in Fig. 2, but for the  $\mathcal{D}_{03} \rightarrow \Delta\Delta$  decay in the intermediate state. The coupling constant  $g_{\Delta\Delta}$  has been adjusted to reproduce the experimental data at high invariant masses. The thin dash-dot-dotted line shows the result of the calculation for  $\pi^0\pi^0$  production without account for the nucleon recoil in the  $\Delta \rightarrow \pi N$  decay (as in Ref. [17]).

# Inclusion of the intermediate $\sigma$ -meson production

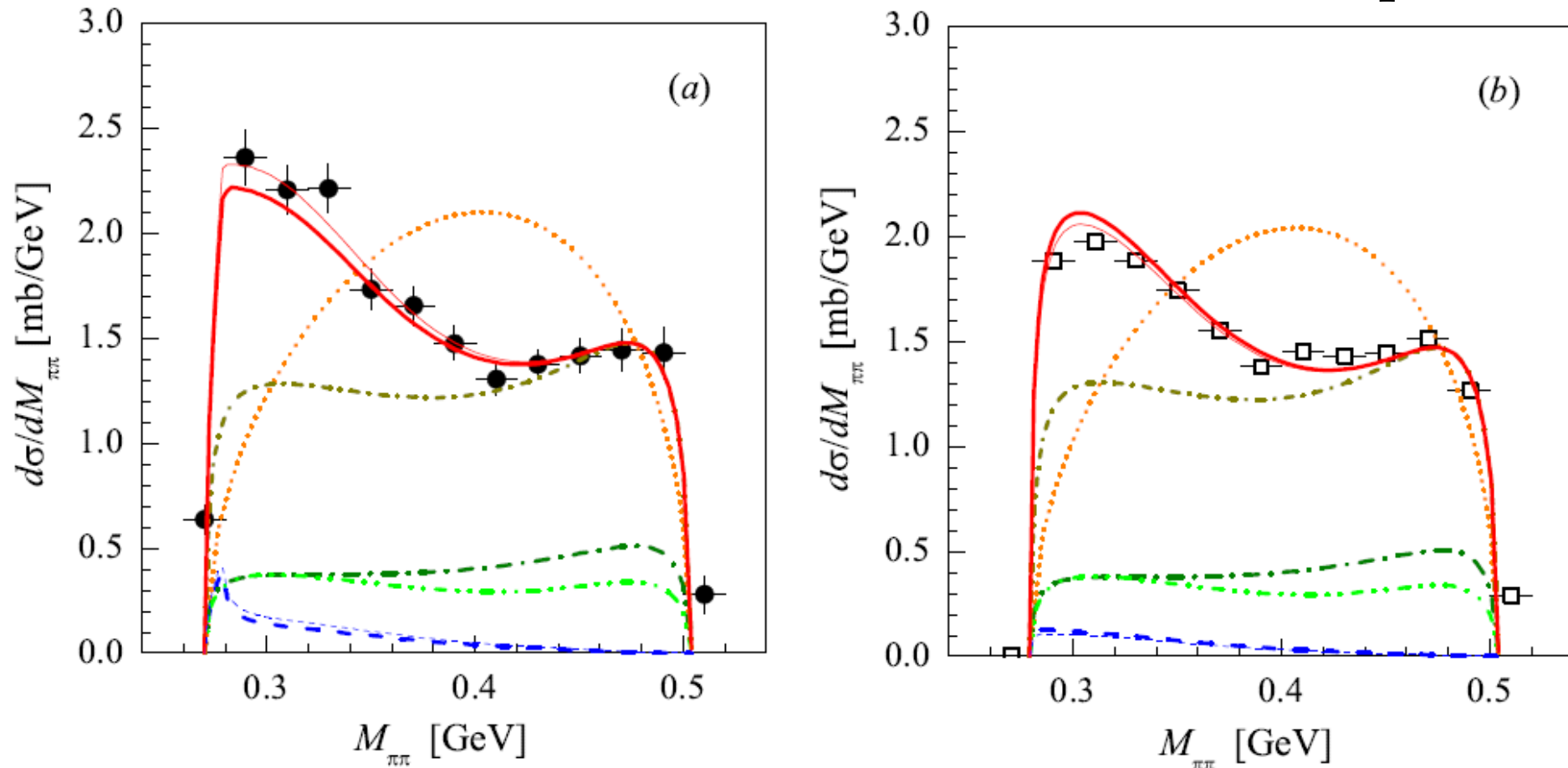


FIG. 6: (Color online) The  $\pi\pi$  invariant-mass distributions in the reactions (a)  $pn \rightarrow d\pi^0\pi^0$  (multiplied by 2) and (b)  $pn \rightarrow d(\pi^+\pi^-)_0$  at  $\sqrt{s} = 2.38$  GeV calculated with the model parameters from Tab. I. Shown are the distributions resulted from the  $\mathcal{D}_{03} \rightarrow \mathcal{D}_{12} + \pi$  decay (dash-dotted lines), the  $\mathcal{D}_{03} \rightarrow \Delta + \Delta$  decay (dash-dot-dotted lines), the  $\mathcal{D}_{03} \rightarrow d + \sigma$  decay (dashed lines), and the coherent sum of these three  $\mathcal{D}_{03}$  decay routes (solid lines). Upper dash-dotted lines (with short dashes) show the summed contribution of the  $\mathcal{D}_{12} + \pi$  and  $\Delta + \Delta$  excitation mechanisms. Dotted lines correspond to the pure phase-space distributions. Thin dashed and solid lines correspond to the  $\sigma$ -excitation mechanism and the total distributions with  $\alpha = 0.23$  (see Eq. (15)). The theoretical calculations are compared to the experimental data on  $2d\sigma/dM_{\pi^0\pi^0}$  (filled circles) and  $d\sigma/dM_{\pi^+\pi^-} - \frac{1}{2}d\sigma/dM_{\pi^+\pi^0}$  (open squares) taken from Ref. [9].



# Energy dependence of the double-pion production cross sections

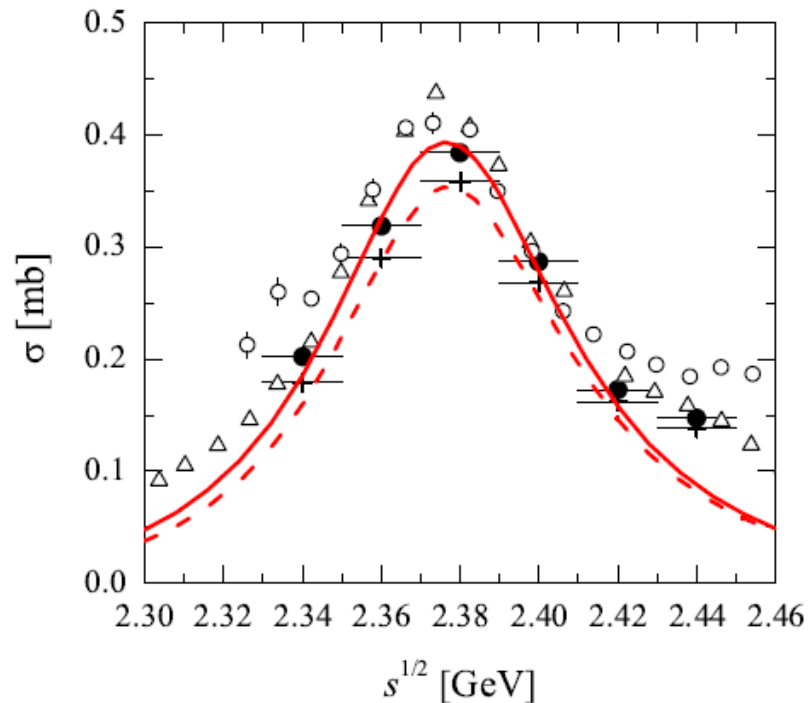


FIG. 7: (Color online) The total cross sections in the reactions  $pn \rightarrow d\pi^0\pi^0$  (multiplied by 2) and  $pn \rightarrow d(\pi^+\pi^-)_0$  as functions of the invariant energy  $\sqrt{s}$ . The solid and dashed lines correspond to the model calculations for  $\pi^0\pi^0$  and  $\pi^+\pi^-$  production, respectively, including the  $\mathcal{D}_{03} \rightarrow \mathcal{D}_{12} + \pi$ ,  $\mathcal{D}_{03} \rightarrow \Delta + \Delta$ , and  $\mathcal{D}_{03} \rightarrow d + \sigma$  decay routes with parameters from Tab. 1 and  $\alpha = 0.23$  (see Eq. (15)). The theoretical calculations are compared to the experimental data on  $2\sigma(pn \rightarrow d\pi^0\pi^0)$  (filled circles) and  $\sigma(pn \rightarrow d\pi^+\pi^-) - \frac{1}{2}\sigma(pp \rightarrow d\pi^+\pi^0)$  (crosses) obtained by an integration of the respective  $M_{\pi\pi}$  distributions measured in Ref. [9]. Also shown are the total cross section data on  $2\sigma(pn \rightarrow d\pi^0\pi^0)$  from Ref. [9] multiplied by a factor of 0.83 (open circles) and from Ref. [8] multiplied by a factor of 0.5 (open triangles) — see Appendix.

## VI. SUMMARY AND OUTLOOK

We have shown that the observed suppression of the near-threshold enhancement (the so-called ABC effect) in the  $\pi\pi$  invariant-mass spectrum in the reaction  $pn \rightarrow d\pi^+\pi^-$  compared to that in the reaction  $pn \rightarrow d\pi^0\pi^0$  can be at least partially explained by the intermediate  $\mathcal{D}_{03}(2380)$  (denoted also as  $d^*(2380)$ ) dibaryon decay with the scalar  $\sigma$ -meson emission. The same mechanism is capable to explain the appearance of the ABC effect itself [18], provided the  $\sigma$  mass and width are shifted downwards to the values of about  $m_\sigma = 290\text{--}320$  MeV and  $\Gamma_\sigma = 75\text{--}150$  MeV due the partial chiral symmetry restoration in the excited  $\mathcal{D}_{03}$  dibaryon. Being a near-threshold resonance, such a renormalized  $\sigma$  meson produces a cusp in the  $\pi^0\pi^0$  production cross section at the  $\pi^+\pi^-$  threshold, thus giving the visible splitting between the neutral and charged dipion production cross sections in the near-threshold region. The free-space  $\sigma$  meson with the parameters  $m_\sigma \simeq \Gamma_\sigma \simeq 500$  MeV produces a similar (though less prominent) cusp but a different shape of the  $M_{\pi\pi}$  distribution, which peaks at the nominal  $\sigma$  mass.

THANK YOU!