

Electroweak radiative corrections to polarized top quark pair production

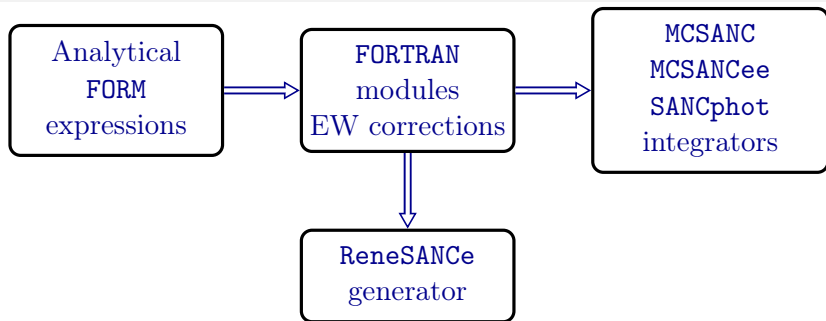
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on behalf of SANC team

JINR; INP BSU

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The SANC framework and products family



Publications:

SANC – CPC 174 481-517

MCSANC – CPC 184 2343-2350; JETP Letters 103, 131-136

SANCphot – arXiv:2201.04350

ReneSANCe – CPC 256 107445; CPC 285 108646

SANC products are available at <http://sanc.jinr.ru/download.php>

ReneSANCe is also available at <http://renesance.hepforge.org>

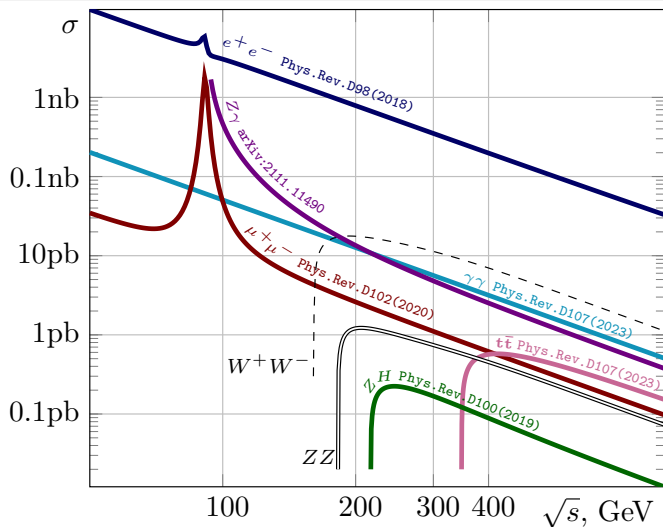
SANC advantages:

- full one-loop electroweak corrections
- higher order corrections
- massive case
- accounting for polarization effects
- full phase space operation
- results of ReneSANCe event generator and SANC integrators are thoroughly cross checked

Processes of interest

- Bhabha ($e^+e^- \rightarrow e^-e^+$), Phys. Rev. D 98, 013001.
- ZH ($e^+e^- \rightarrow ZH$), Phys. Rev. D 100, 073002.
- s-channel ($e^+e^- \rightarrow \mu^-\mu^+$, $e^+e^- \rightarrow \tau^-\tau^+$), Phys. Rev. D 102, 033004.
- s-channel ($e^+e^- \rightarrow t\bar{t}$), Phys. Rev. D 107, 113006.
- Photon-pair ($e^+e^- \rightarrow \gamma\gamma$), Phys. Rev. D 107, 073003.
- Muon-electron scattering ($\mu^+e^- \rightarrow \mu^+e^-$), Phys. Rev. D 105, 033009.
- Møller ($\mu^+\mu^+ \rightarrow \mu^+\mu^+$), JETP Lett. 115, 9.
- $Z\gamma$ ($e^+e^- \rightarrow Z\gamma$).
- ZZ ($e^+e^- \rightarrow ZZ$).
- publication, available in release of the generator
- publication, in preparation for next release of the generator
- in preparation

Basic processes of SM for e^+e^- annihilation



The cross sections are given for polar angles between $10^\circ < \theta < 170^\circ$ in the final state.

Motivation

- Direct measurement of the top-quark mass.
- Both the photon and Z boson couplings of the top quark can be unambiguously measured using asymmetries.
- Importance for the search of BSM signals.

Radiative corrections to top-pair production

In unpolarized case the theoretical uncertainty for observables of top quark pair production at the one-loop level $\mathcal{O}(\alpha)$ were estimated for the first time in:

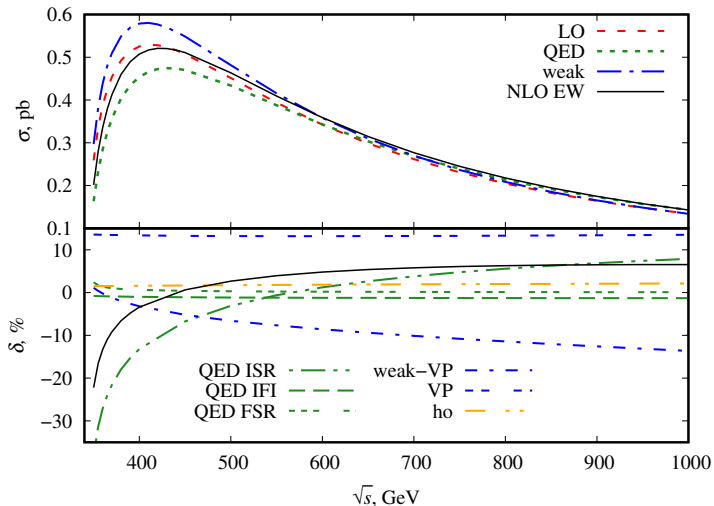
J. Fujimoto and Y. Shimizu, Mod. Phys. Lett. A 3 (1988) 581.

Beam polarization effects were investigated using the GRACE-Loop system in:

P. H. Kiem, E. Kou, Y. Kurihara, and F. Le Diberder, 1503.04247, N. M. U. Quach, Y. Kurihara, K. H. Phan, and T. Ueda, Eur. Phys. J. C 78 (2018), no. 5 422.

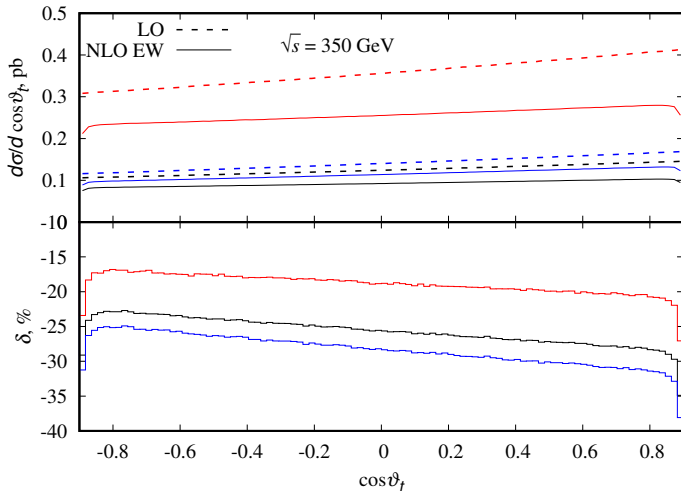
$e^+e^- \rightarrow t\bar{t}$, energy dependence

The LO and NLO EW corrected unpolarized cross sections and the relative corrections in parts as a function of the c.m.s. energy.



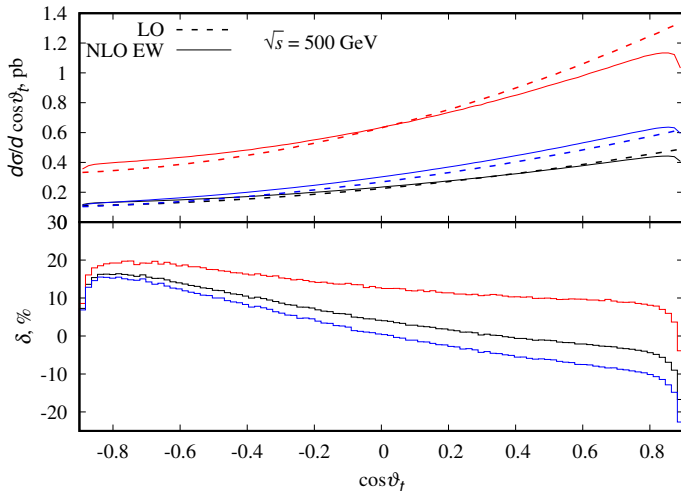
$e^+e^- \rightarrow t\bar{t}$, angle dependence, $\sqrt{s} = 350$ GeV

The unpolarized (black), and fully polarized, with $(P_{e^+}, P_{e^-} = +1, -1)$ (red) and $(-1, +1)$ (blue), initial beams for the energy $\sqrt{s} = 350$ GeV.



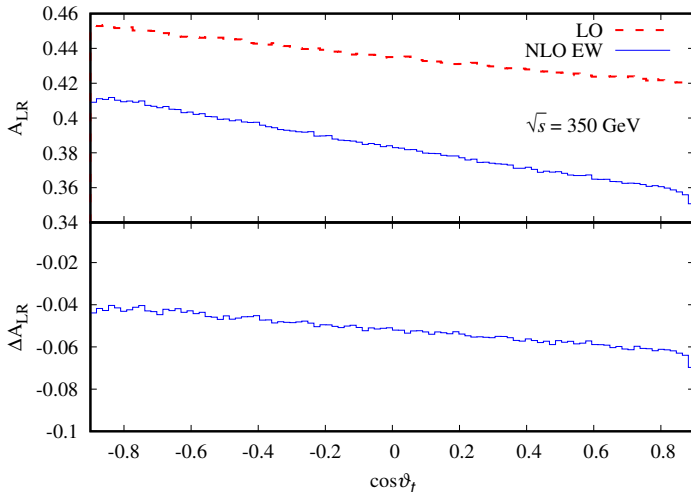
$e^+e^- \rightarrow t\bar{t}$, angle dependence, $\sqrt{s} = 500$ GeV

The unpolarized (black), and fully polarized, with $(P_{e^+}, P_{e^-} = +1, -1)$ (red) and $(-1, +1)$ (blue), initial beams for the energy $\sqrt{s} = 500$ GeV.



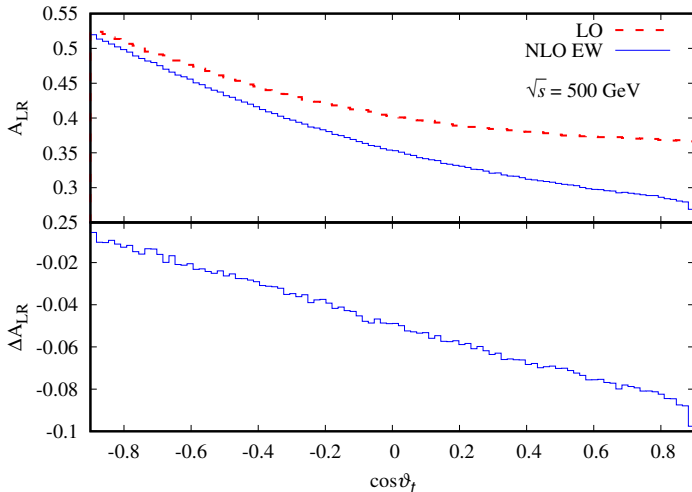
$e^+e^- \rightarrow t\bar{t}$, Left-Right Asymmetry, $\sqrt{s} = 350$ GeV

The asymmetry $A_{LR} = \frac{\sigma_{LR} - \sigma_{RL}}{\sigma_{LR} + \sigma_{RL}}$, in the Born and one-loop approximations.



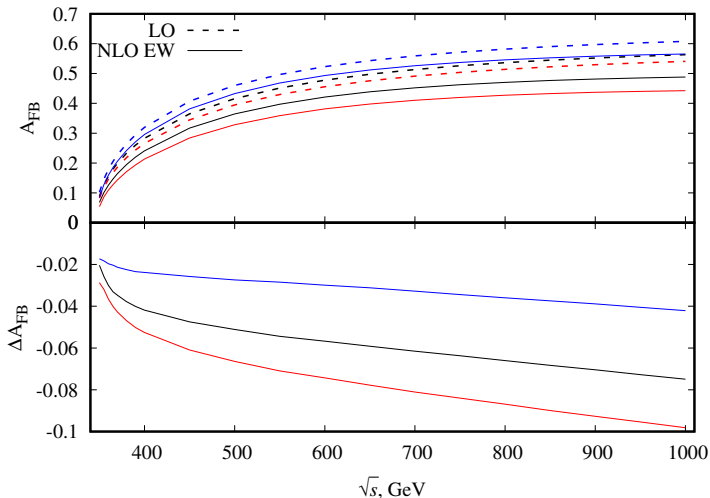
$e^+e^- \rightarrow t\bar{t}$, Left-Right Asymmetry, $\sqrt{s} = 500$ GeV

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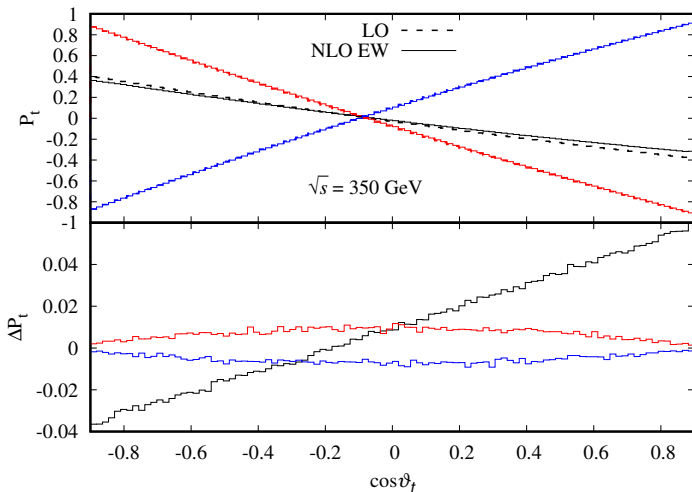
$e^+e^- \rightarrow t\bar{t}$, Forward-Backward Asymmetry

The asymmetry $A_{\text{FB}} = \frac{\sigma_{\text{F}} - \sigma_{\text{B}}}{\sigma_{\text{F}} + \sigma_{\text{B}}}$, in the Born and one-loop approximations. The black lines are for the unpolarized initial beams while the red and blue ones are for the fully polarized cases ($P_{e^+}, P_{e^-} = +1, -1$) and $(-1, +1)$.



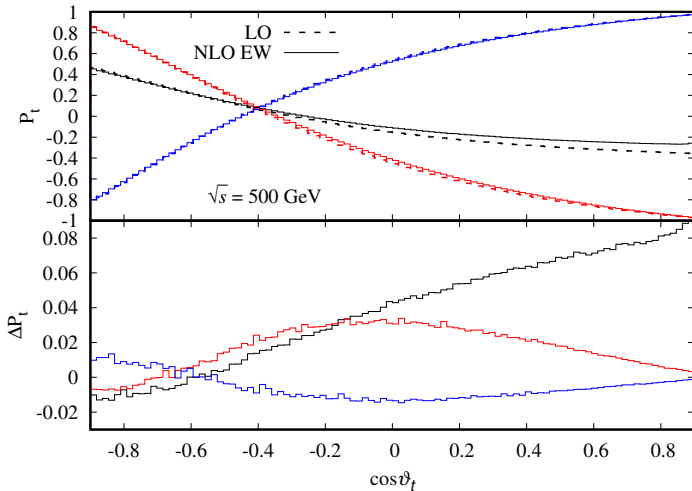
$e^+e^- \rightarrow t\bar{t}$, Final-State Fermion Polarization, $\sqrt{s} = 350$ GeV

Top quark polarization P_t in the Born and one-loop approximations. The black lines are for the unpolarized initial beams while the red and blue ones are for the fully polarized cases ($P_{e^+}, P_{e^-} = +1, -1$) and $(-1, +1)$.

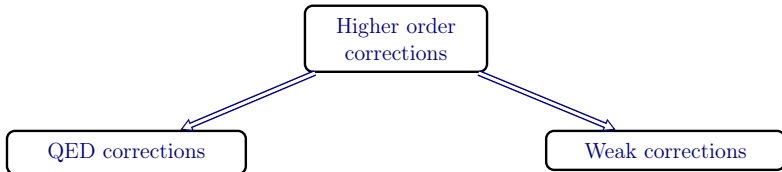


$e^+e^- \rightarrow t\bar{t}$, Final-State Fermion Polarization, $\sqrt{s} = 500$ GeV

Top quark polarization P_t in the Born and one-loop approximations. The black lines are for the unpolarized initial beams while the red and blue ones are for the fully polarized cases ($P_{e^+}, P_{e^-} = +1, -1$) and $(-1, +1)$.



Higher order improvements



- Leading logarithmic (LL) approximation.
- Corrections to $\Delta\alpha$.
- Shower with matching.

- Corrections to $\Delta\rho$.
- Leading Sudakov logarithms.

Higher order improvements, QED

Basic formula:

$$\sigma^{\text{LLA}} = \int_0^1 dx_1 \int_0^1 dx_2 \mathcal{D}_{ee}(x_1) \mathcal{D}_{ee}(x_2) \sigma_0(x_1, x_2, s) \Theta(\text{cuts}),$$

where $\sigma_0(x_1, x_2, s)$ – is the Born level cross section of the annihilation process with changed momenta of initial particles.

$\mathcal{D}_{ee}(x)$ describes the probability density of finding an electron with an energy fraction x in the initial electron beam.

[Kuraev, E.A.; Fadin, V.S. Sov. J. Nucl. Phys. 1985, 41, 466–472]

Higher order improvements, QED

The leading log is $L = \ln \frac{s}{m_l^2}$.

| | | | |
|---------|---------------------------|---------------------------|-----------------------|
| LO | 1 | | |
| NLO | αL | α | |
| NNLO | $\frac{1}{2}\alpha^2 L^2$ | $\frac{1}{2}\alpha^2 L$ | $\frac{1}{2}\alpha^2$ |
| N^3LO | $\frac{1}{6}\alpha^3 L^3$ | $\frac{1}{6}\alpha^3 L^2$ | ... |

In the LL approximation we can separate pure photonic (marked “ γ ”) and the rest corrections which include pure pair and mixed photon-pair effects (marked as “pair”).

$$e^+e^- \rightarrow t\bar{t}, \sqrt{s} = 350 \text{ and } 500 \text{ GeV}$$

Multiple photon ISR relative corrections δ (%) in the LLA approximation.

| \sqrt{s} , GeV | 350 | 500 |
|---|------------|-----------|
| $\mathcal{O}(\alpha L), \gamma$ | -42.546(1) | -3.927(1) |
| $\mathcal{O}(\alpha^2 L^2), \gamma$ | +8.397(1) | -0.429(1) |
| $\mathcal{O}(\alpha^2 L^2), e^+e^-$ | -0.460(1) | -0.030(1) |
| $\mathcal{O}(\alpha^2 L^2), \mu^+\mu^-$ | -0.277(1) | -0.018(1) |
| $\mathcal{O}(\alpha^3 L^3), \gamma$ | -0.984(1) | +0.021(1) |
| $\mathcal{O}(\alpha^3 L^3), e^+e^-$ | +0.182(1) | -0.012(1) |
| $\mathcal{O}(\alpha^3 L^3), \mu^+\mu^-$ | +0.110(1) | -0.008(1) |
| $\mathcal{O}(\alpha^4 L^4), \gamma$ | +0.070(1) | +0.002(1) |

Higher order improvements, weak

Higher order improvements added to NLO cross section through $\Delta\rho$ parameter: $s_W^2 \rightarrow \bar{s}_W^2 \equiv s_W^2 + \Delta\rho c_W^2$.

| | |
|---------------------------------|--|
| $\mathcal{O}(\alpha)$ | A. Sirlin, PRD22, (1980) 971, W.J. Marciano, A. Sirlin, PRD22 (1980) 2695; G. Degrassi, A. Sirlin, NPB352 (1991) 352, P. Gambino and A. Sirlin, PRD49 (1994) 1160 |
| $\mathcal{O}(\alpha\alpha_s)$ | A. Djouadi, C. Verzegnassi, PLB195 (1987) 265; B. Kiehl, NPB353 (1991) 567; B. Kniehl, A. Sirlin, NPB371 (1992) 141, PRD47 (1993) 883; A. Djouadi, P. Gambino, PRD49 (1994) 3499 |
| $\mathcal{O}(\alpha\alpha_s^2)$ | L. Avdeev et al., PLB336 (1994) 560; K.G. Chetyrkin, J.H. Kuhn, M. Steinhauser, PLB351 (1995) 331; PRL75 (1995) 3394; NPB482 (1996) |
| $\mathcal{O}(\alpha\alpha_s^3)$ | Y. Schroder, M. Steinhauser, PLB622 (2005) 124; K.G. Chetyrkin et al., hep-ph/0605201; R. Boughezal, M. Czakon, hep-ph/0606232 |
| $\mathcal{O}(\alpha^2)$ | G. Degrassi, P. Gambino, A. Sirlin, PLB394 (1997) 188; M. Awramik, M. Czakon, A. Freitas, JHEP0611 (2006) 048 |

$e^+e^- \rightarrow t\bar{t}$, $\sqrt{s} = 350$ and 500 GeV

Integrated Born and weak contributions to the cross section and higher-order leading corrections in two EW schemes: $\alpha(0)$ and G_μ .

| \sqrt{s} , GeV | 350 | 500 |
|---|------------|------------|
| $\sigma_{\alpha(0)}^{\text{Born}}$, pb | 0.22431(1) | 0.45030(1) |
| $\sigma_{G_\mu}^{\text{Born}}$, pb | 0.24108(1) | 0.48398(1) |
| $\delta_{G_\mu/\alpha(0)}^{\text{Born}}$, % | 7.48(1) | 7.48(1) |
| $\sigma_{\alpha(0)}^{\text{weak}}$, pb | 0.25564(1) | 0.47705(1) |
| $\sigma_{G_\mu}^{\text{weak}}$, pb | 0.26055(1) | 0.48420(1) |
| $\delta_{G_\mu/\alpha(0)}^{\text{weak}}$, % | 1.92(1) | 1.50(1) |
| $\sigma_{\alpha(0)}^{\text{weak+ho}}$, pb | 0.25900(1) | 0.48483(1) |
| $\sigma_{G_\mu}^{\text{weak+ho}}$, pb | 0.25986(1) | 0.48289(1) |
| $\delta_{G_\mu/\alpha(0)}^{\text{weak+ho}}$, % | 0.33(1) | -0.40(1) |

Integrated Born and one-loop cross sections

| P_{e^+}, P_{e^-} | 0,0 | -1, +1 | +1, -1 |
|-------------------------------|------------|------------|------------|
| $\sqrt{s} = 350 \text{ GeV}$ | | | |
| σ^{Born} , pb | 0.22431(1) | 0.25357(1) | 0.64367(1) |
| σ^{NLO} , pb | 0.16623(1) | 0.20520(1) | 0.45972(1) |
| δ^{NLO} , % | -25.90(1) | -19.07(1) | -28.58(1) |
| δ^{QED} , % | -39.87(1) | -40.03(1) | -39.79(1) |
| δ^{VP} , % | 12.84(1) | 17.51(1) | 11.00(1) |
| $\delta^{\text{weak-VP}}$, % | 1.11(1) | 3.43(1) | 0.20(1) |
| δ^{ho} , % | 1.50(1) | 1.55(1) | 1.47(1) |
| $\sqrt{s} = 500 \text{ GeV}$ | | | |
| σ^{Born} , pb | 0.45030(1) | 0.54028(1) | 1.2609(1) |
| σ^{NLO} , pb | 0.45865(1) | 0.60072(1) | 1.2334(1) |
| δ^{NLO} , % | 1.86(1) | 11.12(1) | -2.18(1) |
| δ^{QED} , % | -4.08(1) | -4.56(1) | -3.91(1) |
| δ^{VP} , % | 12.58(1) | 16.33(1) | 10.97(1) |
| $\delta^{\text{weak-VP}}$, % | -6.63(1) | -5.63(1) | -9.24(1) |
| δ^{ho} , % | 1.73(1) | 1.82(1) | 1.69(1) |

Summary

- $e^+e^- \rightarrow t\bar{t}$ process implemented
- Complete one-loop EW corrections
- Initial & final state polarization support
- Easy to investigate various asymmetries
- LL-accuracy improvements to cross section
- Higher order improvements through $\Delta\rho$
- The research is supported by grant of the Russian Science Foundation (project No. 22-12-00021)

Thank you for your attention!