

Electroweak corrections to dilepton production at LHC: the Drell-Yan, the photon fusion, and the inverse emission

V. A. Zykunov (JINR, GSU)

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Despite the fact that the Standard Model (SM) keeps for oneself the status of consistent and experimentally confirmed theory, the search of New Physics (NP) manifestations is continued:

- ★ **the supersymmetry,**
- ★ **M-theory,**
- ★ **DM-particles,**
- ★ **axions,**
- ★ **feebly interacting particles,**
- ★ **extra spatial dimensions,**
- ★ **extra neutral gauge bosons, etc.**

One of powerful tool in the modern experiments at LHC is the investigation of **Drell–Yan dilepton production**

$$pp \rightarrow \gamma, Z \rightarrow l^+ l^- X \quad (1)$$

at **large invariant mass** of lepton pair: $M \geq 1$ TeV.

Drell-Yan process (1970, BNL)

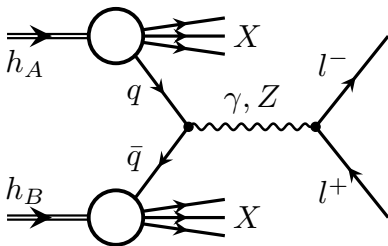


Figure 1: Drell-Yan process with neutral current

- ★ \sqrt{S} is total energy in c.m.s. of hadrons
- ★ M is dilepton l^+l^- invariant mass ($l = e, \mu$)
- ★ y is dilepton rapidity

- ★ The measured Drell–Yan cross sections and forward-backward asymmetries are consistent with the SM predictions at

$$\sqrt{S} = 7\text{--}8 \text{ TeV} (19.7 \text{ fb}^{-1}) \text{ for } M \leq 2 \text{ TeV},$$

$$\sqrt{S} = 13 \text{ TeV} (85 \text{ fb}^{-1}) \text{ for } M \leq 3 \text{ TeV}$$

- ★ differential cross section $\frac{d\sigma}{dM}$,
 - ★ double-differential cross section $\frac{d^2\sigma}{dMdy}$,
 - ★ forward-backward asymmetry A_{FB} .
- ★ NNLO RCs are taken into account by using of **FEWZ**,
 - ★ NNLO PDFs are **CT10 NNLO** and **NNPDF2.1**.

Some modern codes for NLO and NNLO RC for DY process at hadronic colliders (in the ABC order)

- ★ DYNNLO (S. Catani, L. Cieri, G. Ferrera et al.)
- ★ FEWZ (R. Gavin, Y. Li, F. Petriello, S. Quackenbush)
- ★ HORACE (C. Carloni Calame, G. Montagna, et al.)
- ★ MC@NLO (S. Frixione, F. Stoeckli, P. Torrielli et al.)
- ★ PHOTOS (N. Davidson, T. Przedzinski, Z. Was et al.)
- ★ POWHEG (L. Barze, G. Montagna, P. Nason et al.)
- ★ RADY (S. Dittmaier, A. Huss, C. Schwinn et al.)
- ★ READY (V. Zykunov, RDMS CMS)
- ★ SANC (Dubna: A. Andonov, A. Arbuzov, D. Bardin et al.)
- ★ WINHAC (W. Placzek, S. Jadach, M. W. Krasny et al.)
- ★ WZGRAD (U. Baur, W. Hollik, D. Wackerroth et al.)

Code READY and a set of prescriptions

In the following the scale of radiative corrections and their effect on the observables of Drell–Yan processes will be discussed using FORTRAN program **READY**: (**R**adiative corr**E**ctions to **L**arge invariant mass **D**rell–**Y**an process).

We used the following set of prescriptions:

- ★ standard PDG set of SM input electroweak parameters,
- ★ “effective” quark masses ($\Delta\alpha_{had}^{(5)}(m_Z^2) = 0.0276$),
- ★ 5 active flavors of quarks in proton,
- ★ CTEQ, CT10, and MHHT14 sets of PDFs,
- ★ choice for PDFs: $Q = M_{sc} = M$.

We impose the experimental restriction conditions

★ on the detected lepton angle $-\zeta^* \leq \cos \theta \leq \zeta^*$ (or on the rapidity $|y(l)| \leq y(l)^*$); for CMS detector the cut values of ζ^* (or $y(l)^*$) are determined as

$$\zeta^* \approx 0.986614 \quad (\text{or } y(l)^* = 2.5),$$

- ★ the second standard CMS restriction $p_T(l) \geq 20 \text{ GeV}$,
- ★ the “bare” setup for muon identification requirements (no smearing, no recombination of muon and photon/gluon).

Mathematical Content

At the edges of kinematical region (extra large \sqrt{S} , M) the important task is make the RC procedure both accurate and fast. For the latter it is desirable to obtain **the set of compact formulas** for the EWK and QCD RCs.

Leading effect of **Weak RCs** in the region of large M is described by the Sudakov Logarithms (**SL; V. Sudakov, 1956**):

$$\log \frac{m_B^2}{|r|} \quad (B = Z, W; \quad r = s, t, u). \quad (2)$$

Collinear Logarithms (**CL**) play leading role in description of **QED RCs and QCD RCs**:

$$\log \frac{m_f^2}{|r|} \quad (f = e, \mu, q; \quad r = s, t, u). \quad (3)$$

Notations, invariants, coupling constants

The standard set of **Mandelstam invariants** for the partonic elastic scattering:

$$s = (p_1 + p_2)^2, \quad t = (p_1 - k_1)^2, \quad u = (k_1 - p_2)^2. \quad (4)$$

The propagator for j -boson depends on its mass and width:

$$D^{js} = \frac{1}{s - m_j^2 + im_j\Gamma_j}. \quad (5)$$

Suitable combinations of coupling constants are:

$$\lambda_{f+}^{ij} = v_f^i v_f^j + a_f^i a_f^j, \quad \lambda_{f-}^{ij} = v_f^i a_f^j + a_f^i v_f^j, \quad (6)$$

$$v_f^\gamma = -Q_f, \quad a_f^\gamma = 0, \quad v_f^Z = \frac{I_f^3 - 2s_W^2 Q_f}{2s_W c_W}, \quad a_f^Z = \frac{I_f^3}{2s_W c_W}.$$

Main features of EWK and QCD RCs calculation

The notations, the Feynman rules and renormalization details are inspired by review of **M. Böhm, H. Spiesberger, and W. Hollik, 1986**:

- ★ **the t'Hooft–Feynman gauge,**
- ★ **on-mass renormalization scheme** ($\alpha, \alpha_s, m_W, m_Z, m_H$ and the fermion masses as independent parameters),
- ★ **ultrarelativistic approximation.**

QCD result can be obtained from QED case by substitution:

$$Q_q^2 \alpha \rightarrow \sum_{a=1}^{N^2-1} t^a t^a \alpha_s = \frac{N^2 - 1}{2N} I \alpha_s \rightarrow \frac{4}{3} \alpha_s, \quad (7)$$

here $2t^a$ – Gell-Man matrices, and $N = 3$.

Two mechanisms: DY and $\gamma\gamma$ -fusion

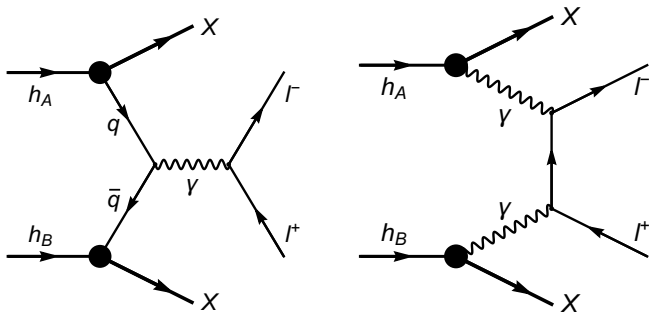


Figure 2: Dilepton production in hadron collisions: left – the Drell–Yan process with virtual photon, right – the photon-photon fusion.

$\gamma\gamma$ -fusion Born: diagrams and cross sections

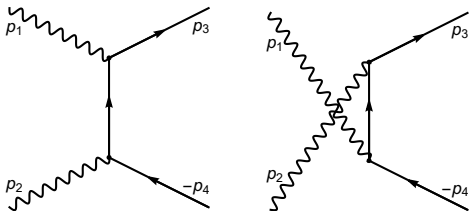


Figure 3: Feynman diagrams of $\gamma\gamma \rightarrow l^-l^+$ process at Born level.

Parton level:

$$d\sigma_0^{\gamma\gamma} = \frac{2\pi\alpha^2}{s^2} \frac{t^2 + u^2}{tu} dt. \quad (8)$$

Hadron level ($C = \cos\theta$):

$$\frac{d^3\sigma_0^h}{dMdydC} = 8\pi\alpha^2 f_\gamma^A(x_1) f_\gamma^B(x_2) \frac{t^2 + u^2}{SM^5(1 - C^2)} \Theta. \quad (9)$$

DY vs $\gamma\gamma$: diff. cross section $d\sigma/dM$

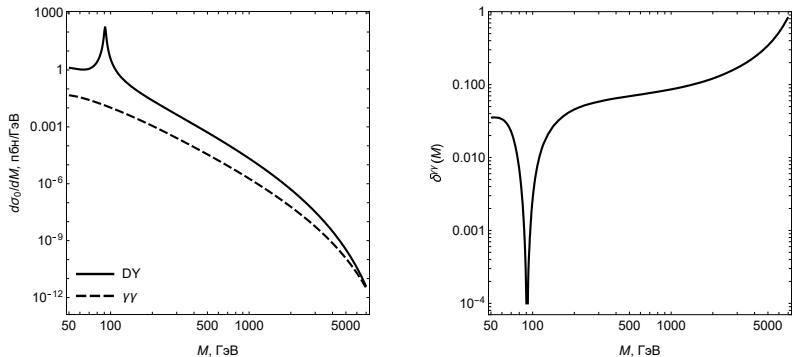


Figure 4: Left – differential Born cross section via M , right – the relative correction $\delta^{\gamma\gamma}(M)$ via M :

$$\delta^{\gamma\gamma}(M) = \frac{d\sigma_0^{\gamma\gamma}/dM}{d\sigma_0^{\text{DY}}/dM}. \quad (10)$$

DY vs $\gamma\gamma$: double diff. cross section $d^2\sigma/dMdy$

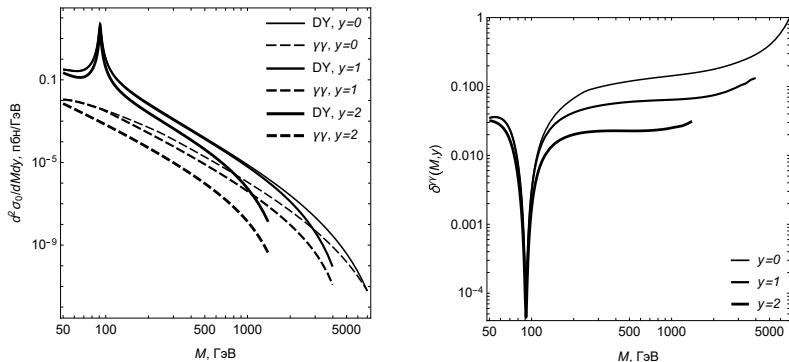


Figure 5: Left – double differential cross sections via M at different y . right – the relative corrections $\delta^{\gamma\gamma}(M, y)$ via M at different y .

Virtual diagrams: γ and Z

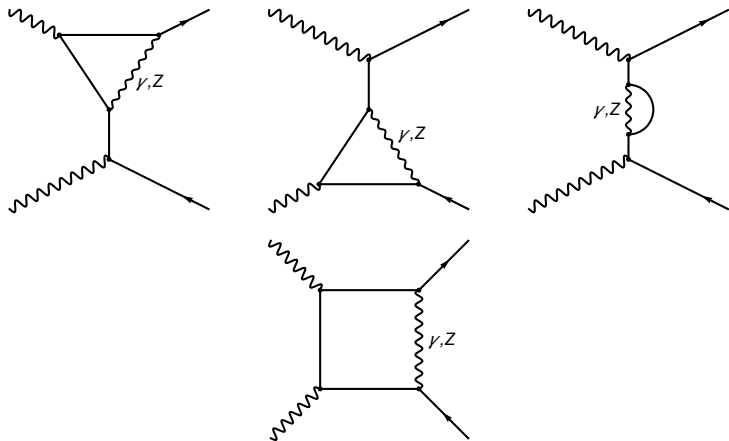


Figure 6: Half of Feynman diagrams set for $\gamma\gamma \rightarrow l^-l^+$ process with additional virtual γ and Z -boson: vertices, electron self energies, boxes. The rest diagrams are obtained by $p_1 \leftrightarrow p_2$.

Virtual diagrams: W

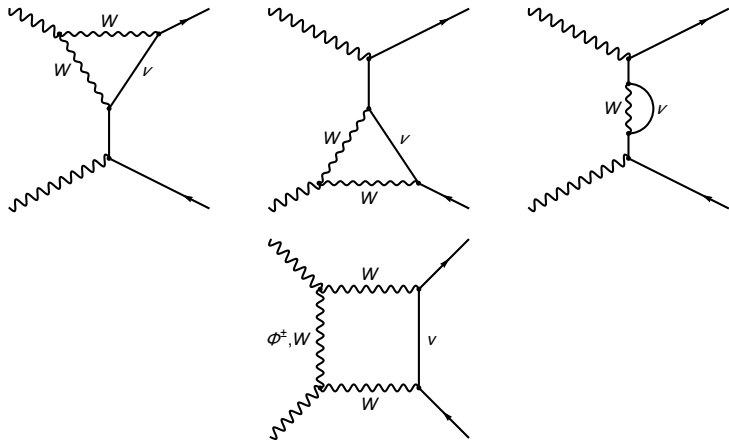


Figure 7: Half of Feynman diagrams set for $\gamma\gamma \rightarrow l^- l^+$ process with additional virtual W -boson: vertices, electron self energies, boxes. The rest diagrams are obtained by $p_1 \leftrightarrow p_2$.

Bremsstrahlung diagrams

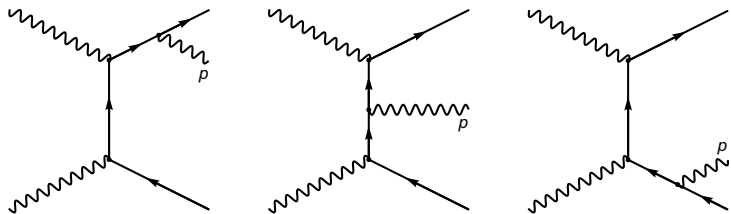


Figure 8: Half of Feynman diagrams set for $\gamma\gamma \rightarrow l^- l^+ \gamma$ process. The rest diagrams are obtained by $p_1 \leftrightarrow p_2$.

Virtual + soft contribution

The virtual and soft contributions are factorized before Born cross section (**M. Böhm and T. Sack, 1986**):

$$\delta_{\text{QED}} = \frac{\alpha}{\pi} \left(\log \frac{4\omega^2}{s} (L - 1) + \frac{\pi^2}{3} - \frac{3}{2} + \frac{tu}{t^2 + u^2} [f(t, u) + f(u, t)] \right),$$

where the function

$$f(t, u) = \frac{s^2 + t^2}{2tu} L_{st}^2 - \frac{3u}{2t} LL_{st} - L_{st}.$$

is entering in the cross section symmetrically (with $t \leftrightarrow u$), and the **collinear “big” log** and **angle log** look like:

$$L = \log \frac{s}{m^2}, \quad L_{st} = \log \frac{s}{-t}. \quad (11)$$

Weak contributions: Z and W

The **weak corrections** are factorized too:

$$\begin{aligned}\delta_Z &= -\frac{\alpha}{\pi}(v_Z^2 + a_Z^2) \frac{tu}{t^2 + u^2} [G_Z(t, u) + G_Z(u, t)], \\ \delta_W &= -\frac{\alpha}{\pi} \frac{1}{4s_W^2} \frac{tu}{t^2 + u^2} [G_W(t, u) + G_W(u, t)].\end{aligned}$$

Assuming the **HE asymptotic** $\sqrt{s} \gg m_Z$ we get:

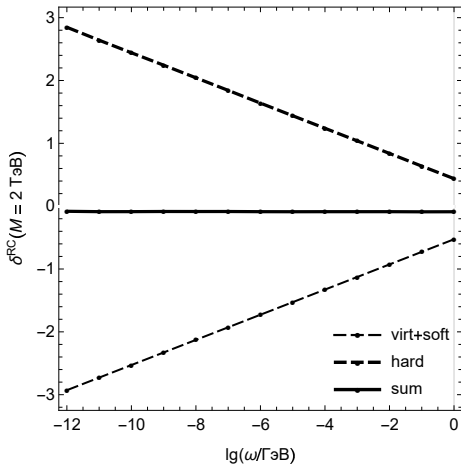
$$G_Z^{\text{HE}}(t, u) = \frac{t^3 L_{st}^2}{2u^3} + \frac{tL_{tZ}}{2u} (L_{sZ} + L_{st} - 1) - \frac{tL_{sZ}}{u} - \frac{t^2 L_{st}}{u^2} + \frac{t(27 - 2\pi^2)}{12u},$$

$$G_W^{\text{HE}}(t, u) = \frac{t^2}{su} (\pi^2 - L_{sW}^2) + \frac{t}{u} \left(\frac{\pi^2}{3} + L_{tW}^2 \right) - \frac{3u}{2t} L_{tW} - L_{st} + \frac{5u}{4t},$$

where **Sudakov logs** look like:

$$L_{tB} = \log \frac{-t}{m_B^2}, \quad L_{sB} = \log \frac{s}{m_B^2}; \quad B = Z, W.$$

Independence of unphysical parameter ω



Relative correction
definition:

$$\delta^{\text{RC}}(M) = \frac{d\sigma_{\text{RC}}^{\gamma\gamma}/dM}{d\sigma_0^{\gamma\gamma}/dM}.$$

Figure 9: The relative corrections δ^{RC} to differential cross section $\frac{d\sigma}{dM}$ (virtual and soft, hard, their sum) via ω ($M=2$ TeV).

ElectoMagnetic corrections to diff. cross section $d\sigma/dM$

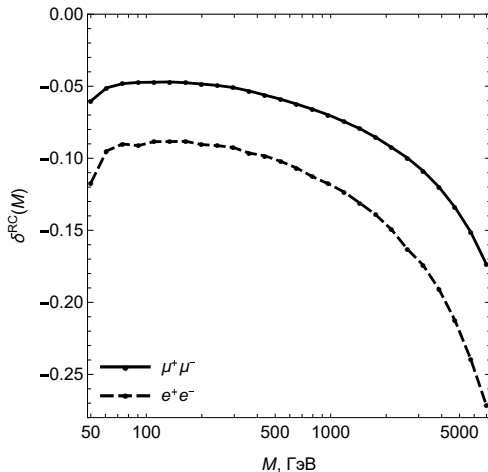


Figure 10: Total relative electromagnetic corrections $\delta^{\text{RC}}(M)$ via M .

ElectoMagnetic corrections to double diff. cross section

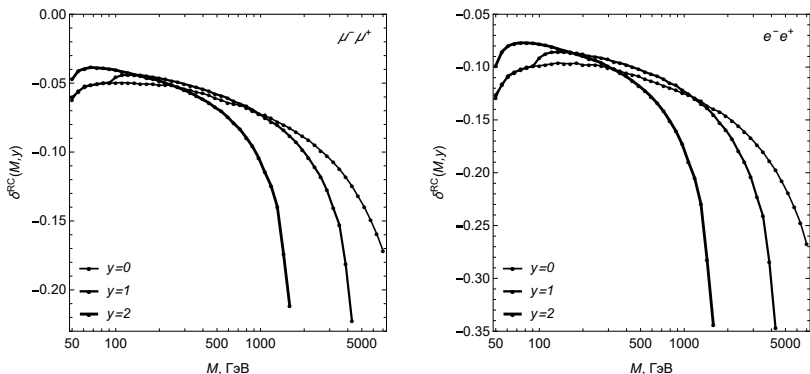


Figure 11: Total relative electromagnetic corrections $\delta^{\text{RC}}(M, y)$ to $\frac{d^2\sigma_0}{dMdy}$ via M at different y .

ElectroWeak corrections to $\frac{d\sigma_0}{dM}$ and $\frac{d^2\sigma_0}{dMdy}$

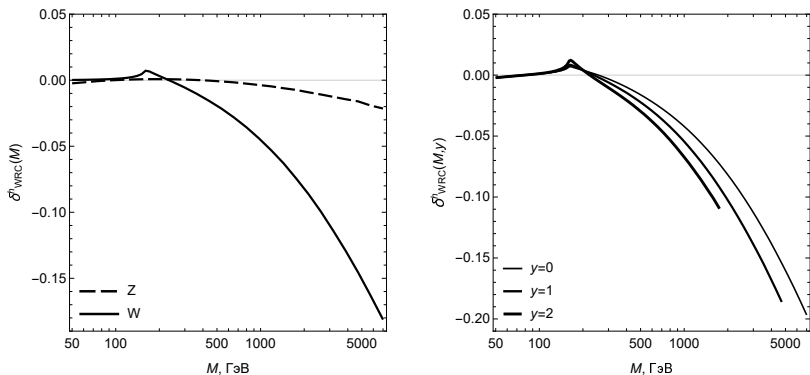
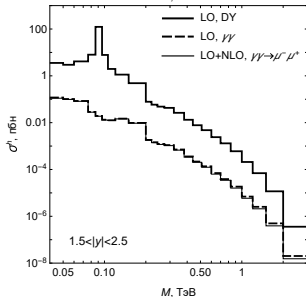
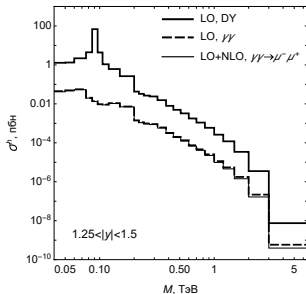
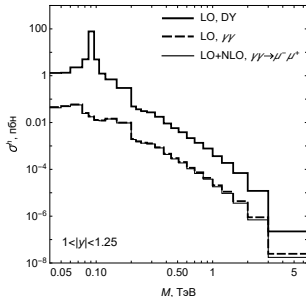
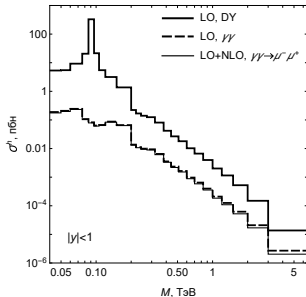


Figure 12: Left (right) – relative electroweak corrections to differential cross section (to double differential cross section at different y) via M .

Total cross sections: standard CMS bins



Forward-backward asymmetry

Forward-backward asymmetry A_{FB} is important observable in dilepton production **with a dual nature – electroweak and kinematical**:

$$A_{\text{FB}} = \frac{\sigma_{\text{F}}^h - \sigma_{\text{B}}^h}{\sigma_{\text{F}}^h + \sigma_{\text{B}}^h}, \quad (12)$$

where according **J. Collins & D. Soper (1977)**:

σ_{F}^h is “forward” cross section ($\cos\theta^* > 0$),

σ_{B}^h is “backward” cross section ($\cos\theta^* < 0$).

In the Collins–Soper system $\cos\theta^*$ looks like:

$$\cos\theta^* = \text{sgn}[x_2(t + u_1) - x_1(t_1 + u)] \frac{tt_1 - uu_1}{M\sqrt{s}(u + t_1)(u_1 + t)}.$$

Forward, Backward (and Experimental) borders

For the case of nonradiative kinematics the $\cos\theta^*$ has especially simple view:

$$\cos\theta^* = \text{sgn}[x_1 - x_2] \frac{u - t}{s} = \text{sgn}[e^y - e^{-y}] \frac{(1 + \mathcal{C})e^{-y} - (1 - \mathcal{C})e^y}{(1 + \mathcal{C})e^{-y} + (1 - \mathcal{C})e^y}.$$

Solving $\cos\theta^* = 0$ we get **two conditions** for border dividing the regions of σ_F^h and σ_B^h :

$$y = 0, \quad \mathcal{C} \equiv \cos\theta = \text{th } y.$$

The CMS experimental condition $|\cos\theta| < \zeta^*$ is trivial but the second one $|\cos\alpha| < \zeta^*$ is rather sophisticated:

$$\cos\left(\arccos\frac{\cos\theta - \text{th } y}{r} + \arcsin\frac{\sin\theta \text{th } y}{r}\right) = \pm\zeta^*,$$

where

$$r = \sqrt{1 - 2\cos\theta \text{th } y + \text{th}^2 y}.$$

Forward, Backward (and Experimental) regions

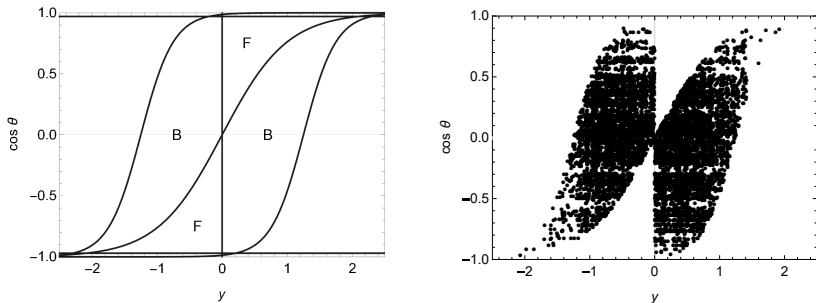


Figure 14: Left – Forward, Backward and CMS regions in y and $\cos\theta$ variables (**borders are:** $y = 0$, $\cos\theta = \text{th } y$, $\cos\theta = \pm\zeta^*$, and $\cos\alpha = \pm\zeta^*$, where $\zeta^* \approx 0.9866$), right – the points sampled by Monte-Carlo generator of VEGAS for **Backward CMS region**.

Interplay of DY and $\gamma\gamma$ for A_{FB} : numerical effect

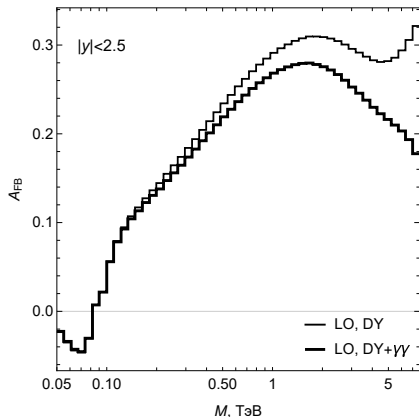


Figure 15: The Born forward-backward asymmetry via M at CMS LHC setup: for **Drell–Yan mechanism** – thin line, for **both mechanisms** (DY and $\gamma\gamma$ -fusion) – thick line.

Interplay of DY and $\gamma\gamma$ for A_{FB} : explanation

As the Born process $\gamma\gamma$ -fusion has **pure electromagnetic nature**, then

$$A_{\text{FB}}^{\gamma\gamma} = 0.$$

Therefore the F- and B- cross sections are equal:

$$\sigma_{\text{F}}^{\gamma\gamma} = \sigma_{\text{B}}^{\gamma\gamma} = \Delta.$$

The $\gamma\gamma$ -fusion cross section has the scale comparable with DY one **at large M region**. Expanding the net asymmetry (DY+ $\gamma\gamma$) in series on Δ we get:

$$A_{\text{FB}}^{\text{DY}+\gamma\gamma} \approx A_{\text{FB}}^{\text{DY}} \left(1 - \frac{2\Delta}{\sigma_{\text{F+B}}^{\text{DY}}} \right).$$

This effect (the decreasing of net asymmetry at large M) is well seen in Fig. 15 starting with $M \sim 300$ GeV.

A_{FB} for Run3 of CMS LHC: $\mu^+\mu^-$, DY

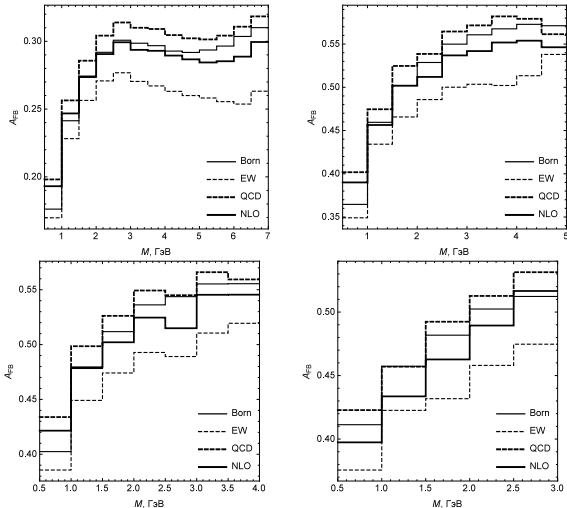


Figure 16: A_{FB} for $\mu^+\mu^-$ -production: top – $|y| < 1$ and $1 < |y| < 1.25$, bottom – $1.25 < |y| < 1.5$ and $1.5 < |y| < 2.5$.

A_{FB} for Run3 of CMS LHC: e^+e^- , DY

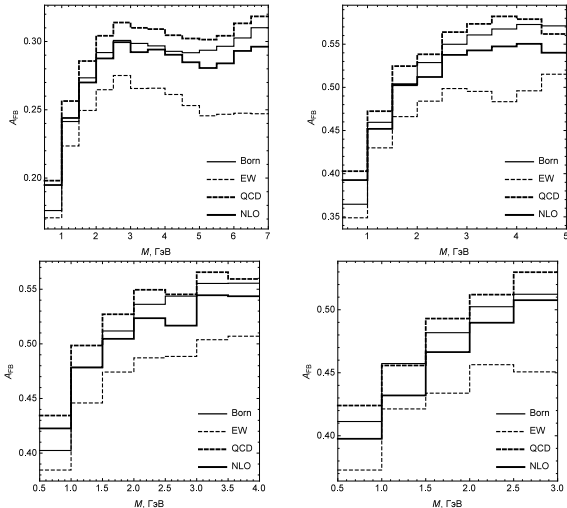


Figure 17: A_{FB} for e^+e^- -production: top – $|y| < 1$ and $1 < |y| < 1.25$, bottom – $1.25 < |y| < 1.5$ and $1.5 < |y| < 2.5$.

A_{FB} for Run3 of CMS LHC: $\mu^+\mu^-$, DY and $\gamma\gamma$

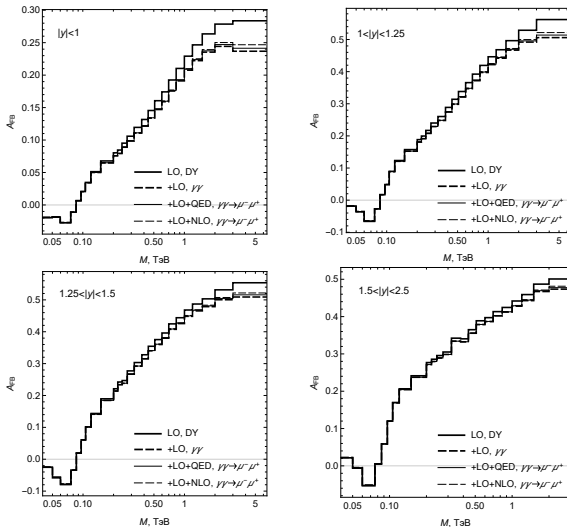


Figure 18: Forward-backward asymmetry A_{FB} for $\mu^+\mu^-$ -production.

One more mechanism: inverse γ emission

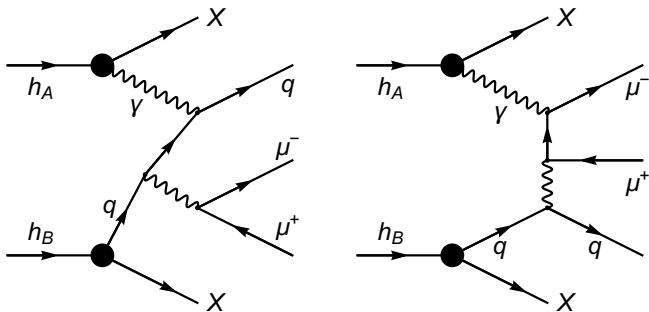


Figure 19: Dilepton production in hadron collisions: left – inverse γ emission with quark, right – inverse γ emission with muon.

Conclusions & Acknowledgement

- ★ **The NLO EWK** corrections to dilepton production with Drell–Yan and $\gamma\gamma$ -fusion mechanisms have been studied.
- ★ It has been ascertained that the considered in Run 3 region radiative corrections change the cross sections and A_{FB} **significantly**.
- ★ I would like to thank the **RDMS CMS group** members for the stimulating discussions and **CERN (CMS Group)** for warm hospitality during my visits.
- ★ This work was supported by the **Convergence-2025** Research Program of Republic of Belarus (Microscopic World and Universe Subprogram).
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