

Density and pressure distribution of proton

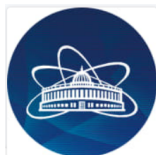
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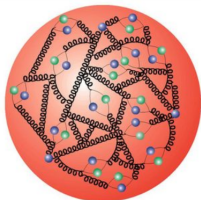
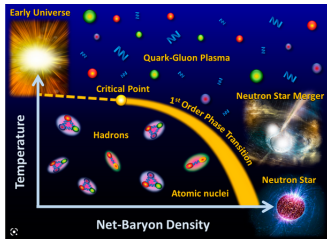
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- Introduction and Motivation
- Formalism
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 - Guess Function
 - Pressure from Statistical Approaches
- Results and Discussion
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Introduction and Motivation



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The pressure distribution inside the proton

Y. D. Baryshev , L. Glazovitch & T. X. Gao

Nature 557, 396–399 (2018) | [View this article](#)

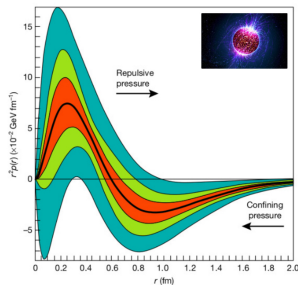


Figure: 5. The pressure distribution inside the proton.

Formalism (Pressure from form factors)

Forces inside hadrons: Pressure, surface tension, mechanical radius, and all that

Maxim V. Polyakov and Peter Schweitzer

em:	$\partial_\mu J_{\text{em}}^\mu = 0$	$\langle N' J_{\text{em}}^\mu N \rangle$	\longrightarrow	$Q_{\text{prot}} = 1.602176487(40) \times 10^{-19} \text{C}$
	<i>vector</i>			$\mu_{\text{prot}} = 2.792847356(23) \mu_N$
weak:	PCAC	$\langle N' J_{\text{weak}}^\mu N \rangle$	\longrightarrow	$g_A = 1.2694(28)$
	<i>axial</i>			$g_p = 8.06(0.55)$
gravity:	$\partial_\mu T_{\text{grav}}^{\mu\nu} = 0$	$\langle N' T_{\text{grav}}^{\mu\nu} N \rangle$	\longrightarrow	$M_{\text{prot}} = 938.272013(23) \text{MeV}/c^2$
	<i>tensor</i>			$J = \frac{1}{2}$
				$D = ?$

Figure: 2. The global properties of the proton are defined in terms of matrix elements of the conserved currents associated with respectively electromagnetic, weak, and gravitational interaction.

Forces inside hadrons: Pressure, surface tension, mechanical radius, and all that

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$$T^{ij}(\vec{r}) = s(r) \left(\frac{r^i r^j}{r^2} - \frac{1}{3} \delta^{ij} \right) + p(r) \delta^{ij}. \quad (1)$$

$$s(r) = \frac{1}{4m} r \frac{d}{dr} \frac{1}{r} \frac{d}{dr} \tilde{D}(r),$$

$$p(r) = \frac{1}{6m} \frac{1}{r^2} \frac{d}{dr} r^2 \frac{d}{dr} \tilde{D}(r)$$

$$\tilde{D}(r) = \int \frac{d^3 \Delta}{(2\pi)^3} e^{-i\Delta r} D(-\Delta^2).$$

Formalism (Guess Function)

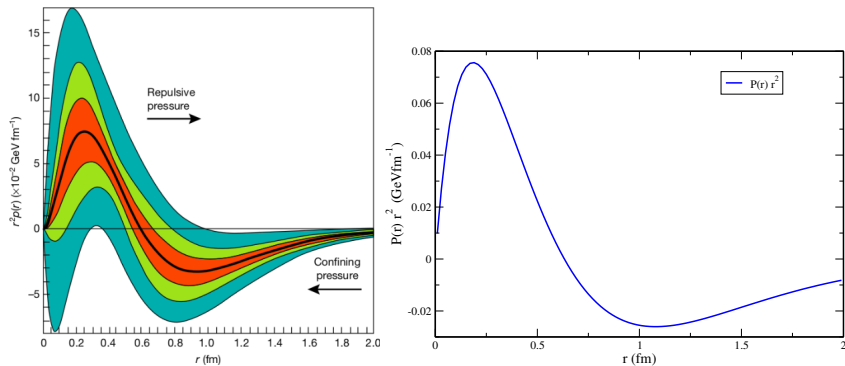


Figure: 3.The Pressure distribution inside the proton by using guess function.

$$y = p(r)r^2 = 0.2593 (4 - 6.325r)r \exp(-6.325r/2), \quad (2)$$

Formalism (Pressure from Statistical Approaches)

Let us assume the proton being an ideal fermi gas system in a grand canonical ensemble.

$$\Phi(T, V, \mu) = -PV = -k_B T \ln Z_{GCE(tot)}, \quad (3)$$

From the second law of thermodynamics,

$$TdS = dU + PdV - \mu dN. \quad (4)$$

$$d\Phi = -PdV - SdT - Nd\mu. \quad (5)$$

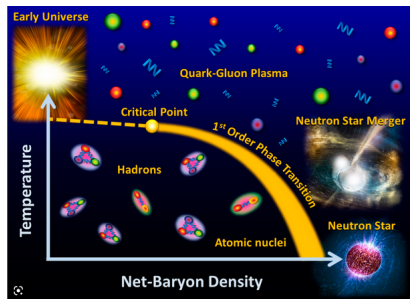
The fermi dirac distribution function is given by:

$$f(\epsilon_i) = \frac{1}{e^{(\epsilon_i - \mu)/k_B T} + 1}$$

For ultra-relativistic case at temperature $T \approx 0$, for energy states $\epsilon_i < \mu$, all the states will be occupied.

$$P(r)V = \frac{g}{h^3} \int_V \int_0^\infty \left(\frac{pv}{3}\right) f(\epsilon_i) d\tau d^3p$$

$$P(r) = \frac{4\pi g}{h^3} \int_0^{p_f(r)} \left(\frac{pv}{3}\right) p^2 dp$$



Case-1 $\mu \neq 0, T = 0$ case,

$$P(r) = \frac{g}{24\pi^2} \mu^4, \quad \mu(r) = \left[\frac{24\pi^2}{g} P(r) \right]^{\frac{1}{4}}. \quad (6)$$

For number density and the energy density are,

$$n(r) = \frac{g}{6\pi^2} \mu(r)^3, \quad (7)$$

$$\epsilon(r) = \frac{g}{8\pi^2} \mu(r)^4. \quad (8)$$

Case-2 $\mu = 0, T \neq 0$ case,

$$P = \frac{\epsilon}{3} = \frac{g}{\pi^2} \frac{7}{8} \zeta(4) T^4. \quad (9)$$

$$n = \frac{N}{V} = \frac{g}{\pi^2} \frac{3}{4} \zeta(3) T^3. \quad (10)$$

$$\epsilon = \frac{3g}{\pi^2} \frac{7}{8} \zeta(4) T^4. \quad (11)$$

Results and Discussion

$$1 \text{ GeV}^4 = 2.0852 \times 10^{37} \text{ Jm}^{-3} \quad (12)$$

Alexei Bazavov, Tanmoy Bhattacharya, Carleton DeTar, H-T Ding, Steven Gottlieb, Rajan Gupta, P Hegde, UM Heller, Frithjof Karsch, Edwin Laermann, et al.
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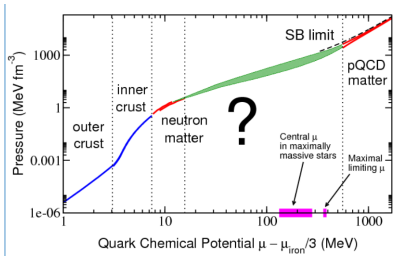
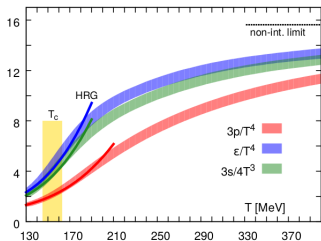


Figure: 4. On the left, thermodynamic properties calculated with Lattice QCD, pressure, energy and entropy densities. On the right, the band region of the known limits of the stellar EoS on a logarithmic scale. On the horizontal axis we have the quark chemical potential with vertical axis the pressure (right).

Results and Discussion

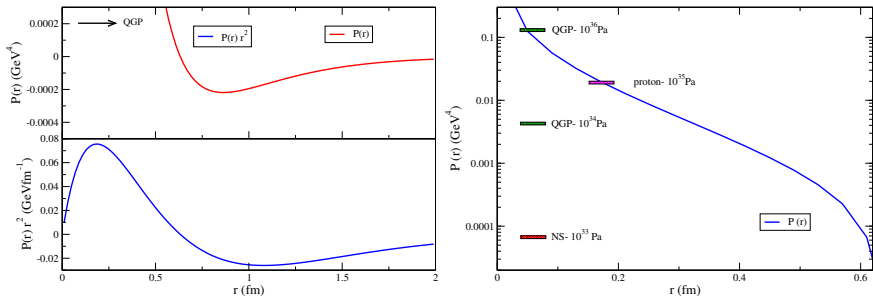
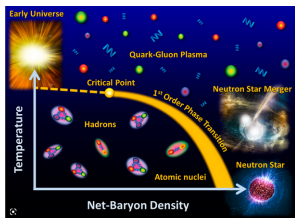


Figure: 5. The pressure distribution inside the proton (Left) and the comparison of pressure value with QGP and NS cases (right).



	$P(\text{GeV})^4$
QGP	$10^{34} - 10^{36} \text{ Pa}$ 0.004 – 0.124
NS	10^{33} Pa 6.69×10^{-5}
proton	10^{35} Pa 0.0199

Results and Discussion

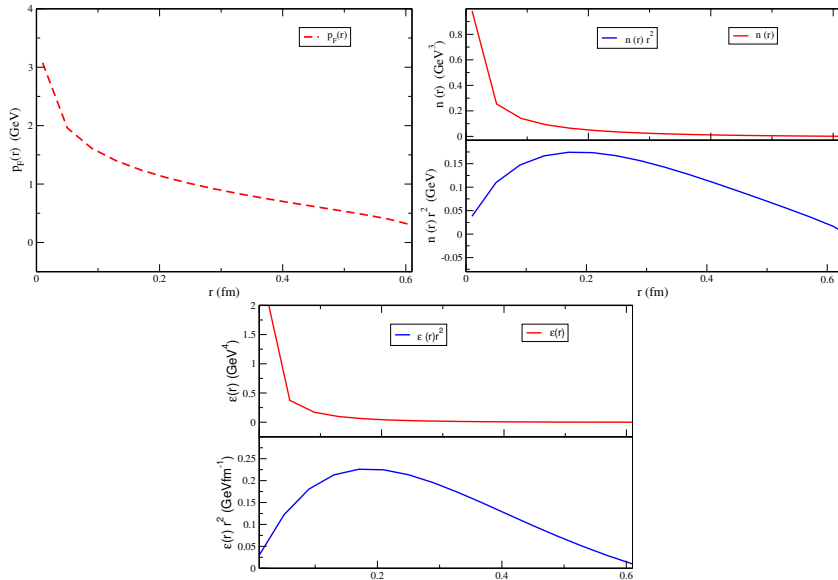
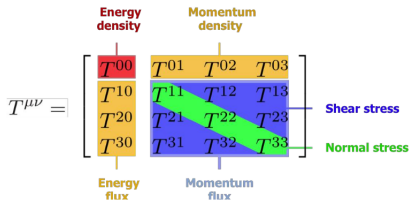


Figure: 6. (a)Freni momentum , (b)the number density (c) the energy density for the proton case.

Conclusion

- "V. D. Burkert. et al. "The pressure distribution inside the proton", Nature, 054911 2018 and M. V. Polyakov et al., "Forces inside hadrons: pressure, surface tension, mechanical radius, and all that" focused on the proton pressure distribution in terms of radial distance from the form factors point of view.
- We have estimated these profiles from the guess function and statistical perspectives.
- We described the parameterization of the analytical guess function.
- We assumed that our proton system is assumed as a degenerate quark fluid motion.
- From the above pressure guess function, our tuning parameter is effective chemical potential in terms of the proton radius.
- We derived the other thermodynamics quantities and compared the results with others: QGP, and NS cases.
- The proton's central peak pressure is larger than the neutron star case.

Thank you!



$$T_{ij}(\vec{r}) = s(r) \left(\frac{r_i r_j}{r^2} - \frac{1}{3} \delta_{ij} \right) + p(r) \delta_{ij}$$