

# Tuning of Geant4 FTF model using NA61/SHINE experimental data

A. Galoyan and V. Uzhinsky, 22.09.2023

## Latest data by the NA61/SHINE collaboration

Pi-, **PP 20 -158** Eur. Phys. J. C74 (2014) 2794 (Received: 14 October 2013)

Pi,K,P,antiP, **PP 20 -158** Eur. Phys. J. C77 (2017) 671 (Received: 9 May 2017)

Pi,K,P,antiP, **P+C, 31** Eur. Phys. J. C76 (2016) 84 (Received: 12 October 2015)

Pi-, **7Be+9Be, 13 – 150** Eur. Phys. J. C80 (2020) 961 (Received: 14 August 2020)

Pi,K,P,anti-P, **7Be+9Be** Eur. Phys. J. C81 (2021) 73 (Received: 5 October 2020)

Pi-, **Ar+Sc, 13 – 150 A GeV/c** Eur. Phys. J. C81 (2021) 397 (Received: 22 January 2021)

[Arxiv:hep-exp:2308.16683](https://arxiv.org/abs/2308.16683) (31 Aug. 2023)

**Measurements of  $\pi^\pm$ ,  $K^\pm$ , p and anti-p spectra in 40Ar+45Sc collisions at 13A to 150A GeV/c**

**There are too many comparisons with models!**

**Tune model parameter:  $E1 = P1 + P2$ ;  $E2 = P1 - P2$**

**Our model developed in Geant4 – Geant4 FTF (Fritiof)**

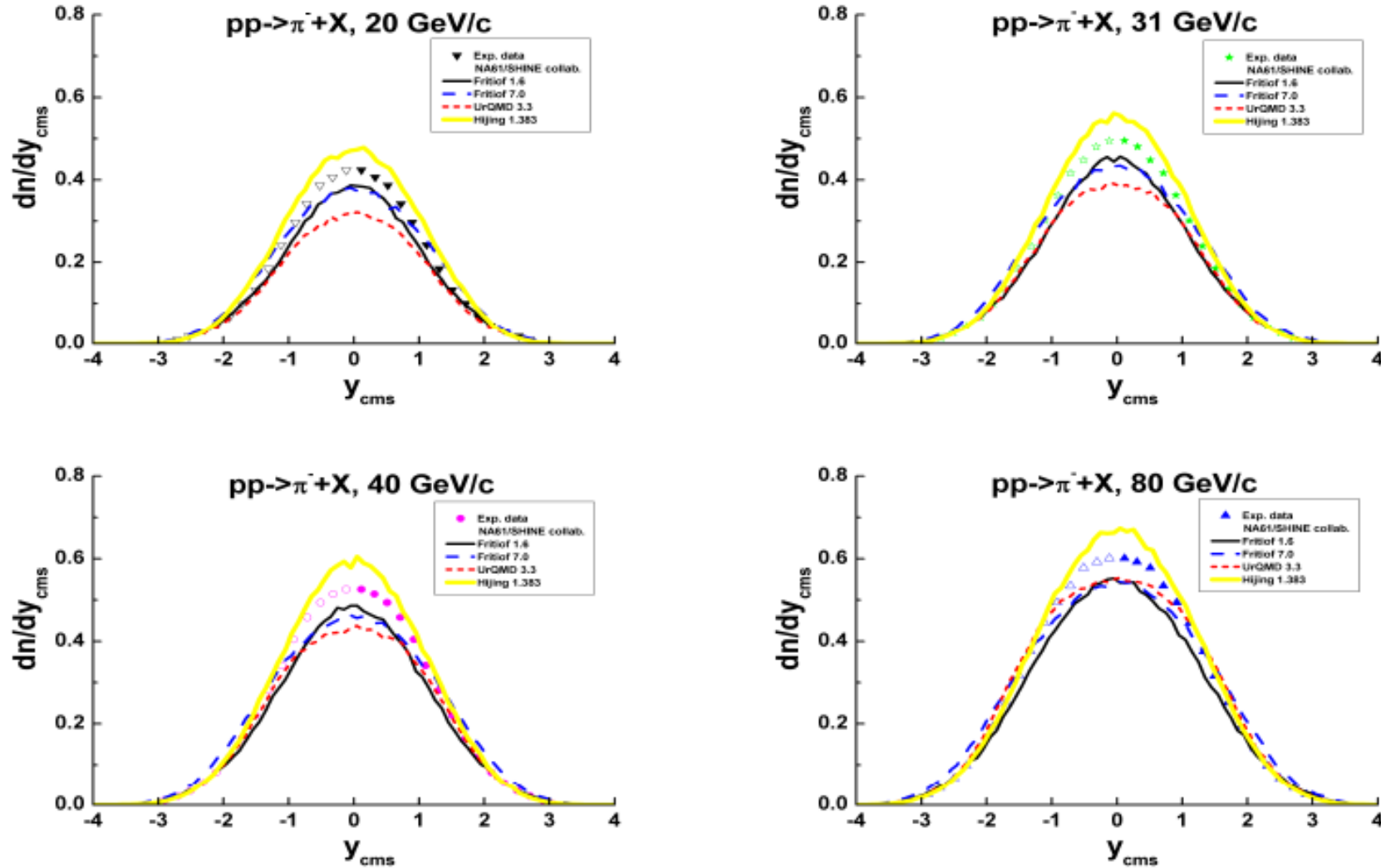
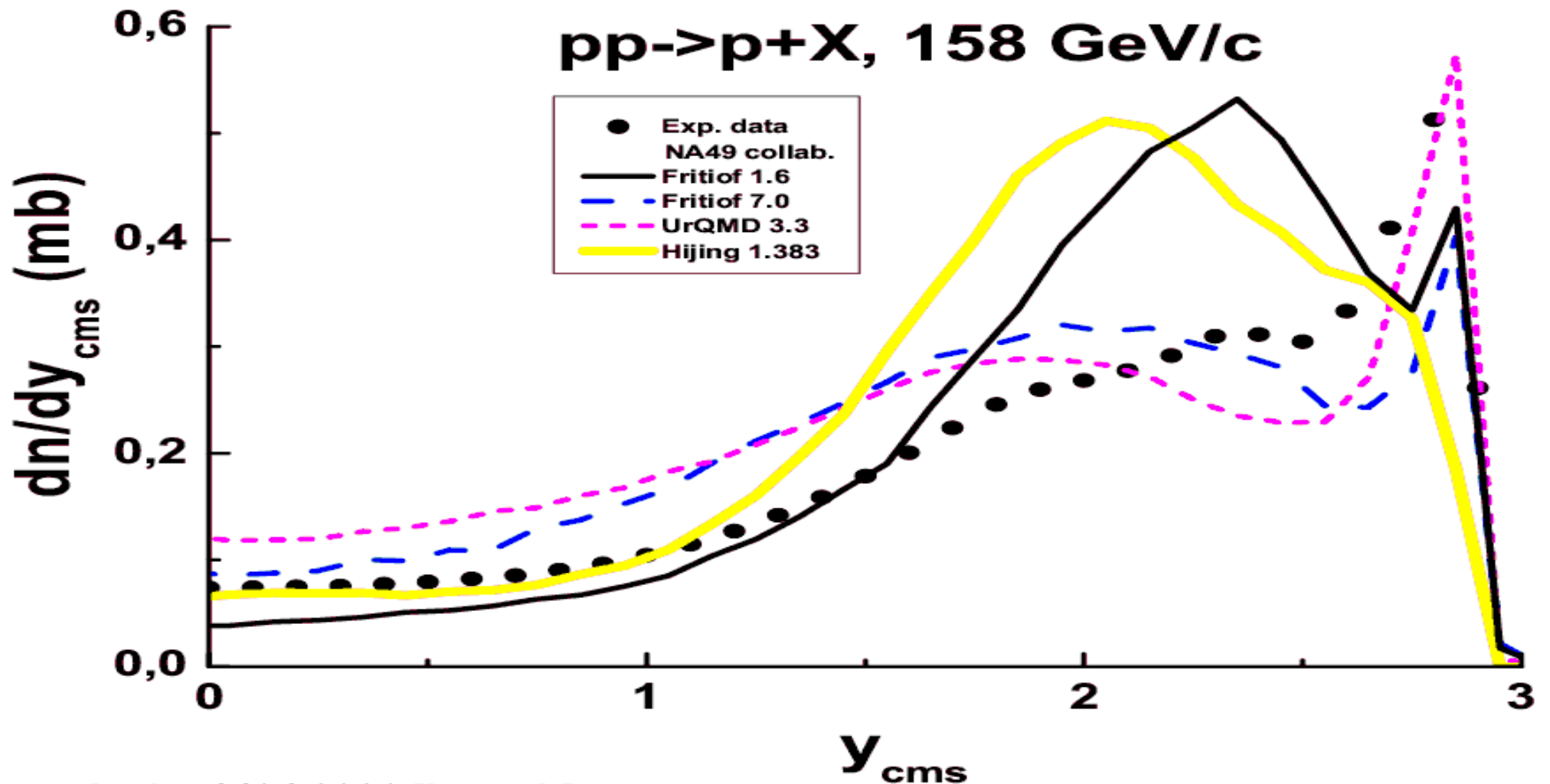


Figure 1: Rapidity distributions of  $\pi^-$ -mesons in  $pp$  interactions. Closed points are the NA61/SHINE experimental data [1], the open points are the data reflected at mid-rapidity. Lines are model calculations.

# Problem

Fritiof 1.6, Fritiof 7.0, Hijing, UrQMD 3.3, pp-interaction: NA49 exp. data



Arxiv: 1404.2026 [hep-ph] Toward Description of pp and pC Interactions at High Energies: Problems of Fritiof-based Models

**All Fritiof-based models have problems, though, they can be tuned!**

# NA61/SHINE data on PP interactions at 20 – 158 GeV/c

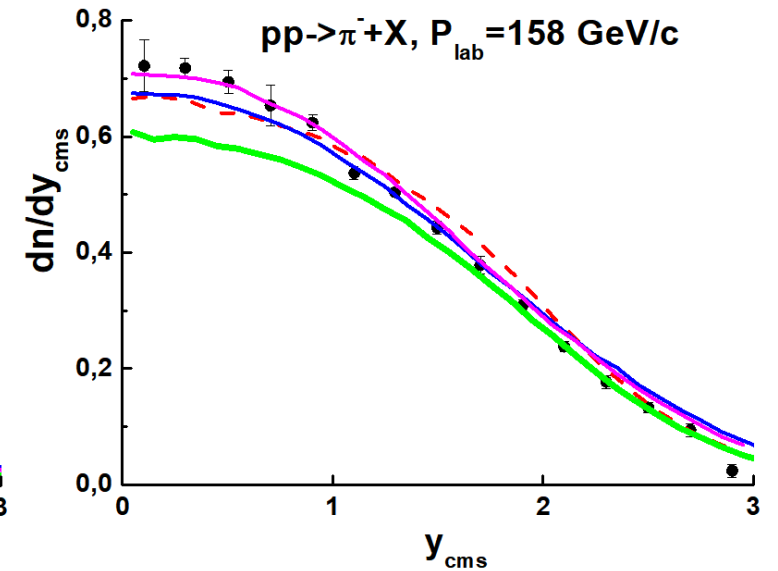
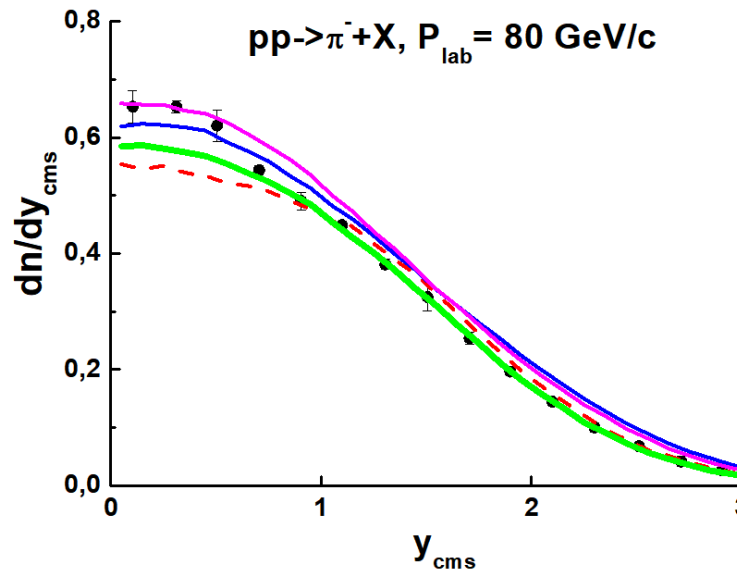
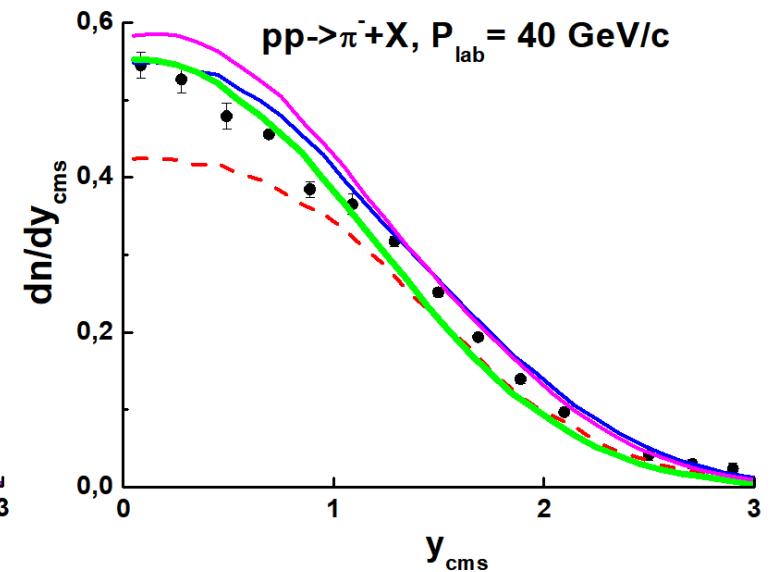
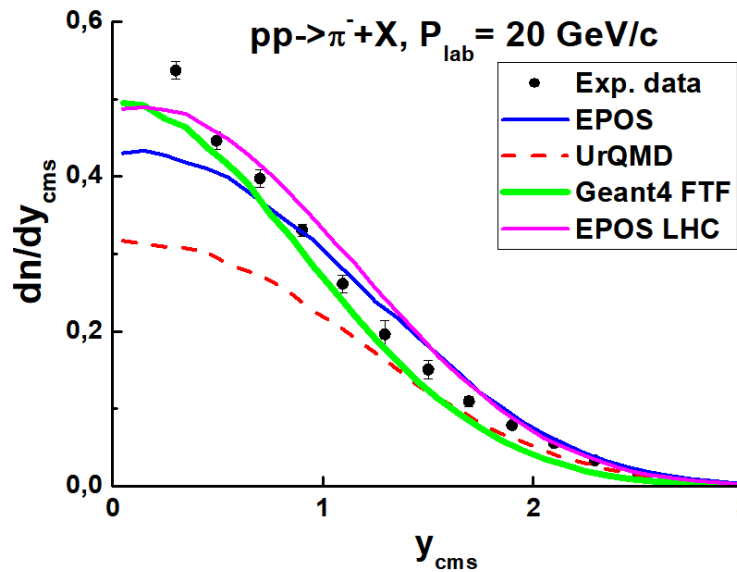
PP int.

Geant4 FTF

EPOS 1.99

EPOS LHC

UrQMD



EPOS O.K.  $P_{lab} > 40$  GeV/c. UrQMD 3.3 works only at 158 GeV/c.

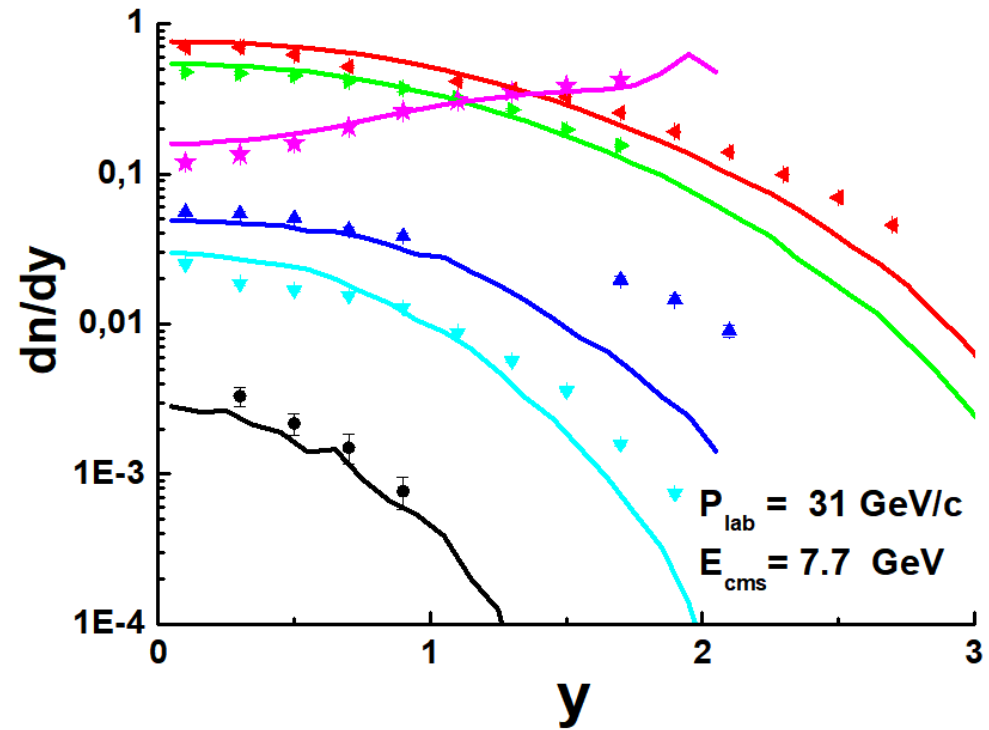
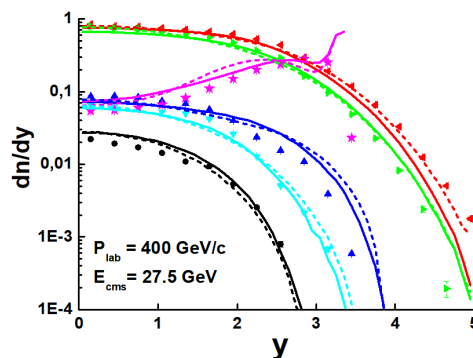
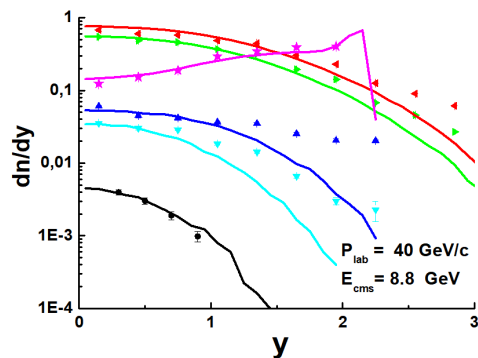
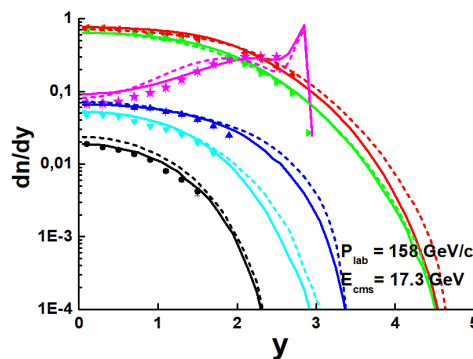
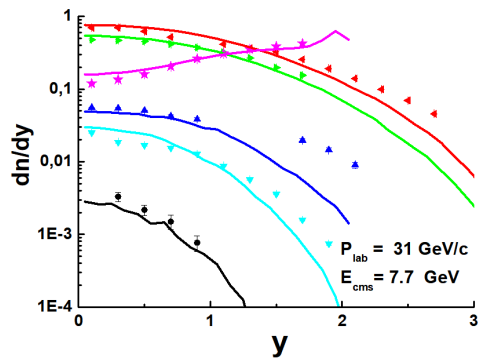
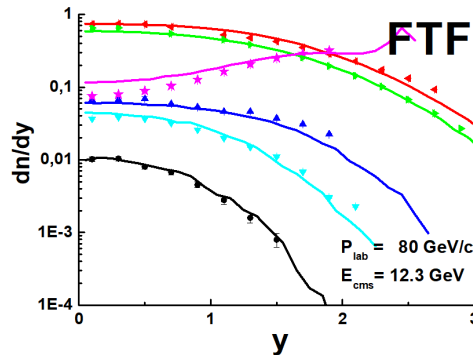
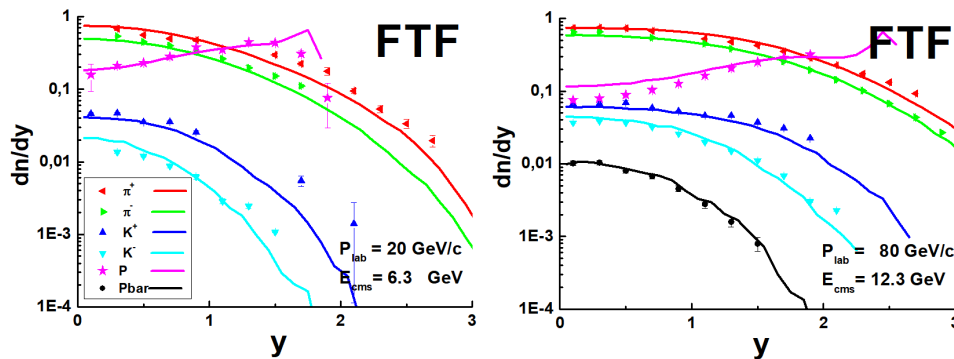
Geant4 FTF gives the best results. Only at 159 GeV/c there is a problem.

# Inclusive one-particle distributions ...

Measurements of  $\pi^\pm$ ,  $K^\pm$ , p and  $\bar{p}$  spectra in proton-proton interactions at 20, 31, 40, 80 and 158 GeV/c with the NA61/SHINE spectrometer at the CERN SPS

NA61/SHINE Collaboration

Eur. Phys. J. C (2017) 77:671



**FTF cannot describe  $K^+$ ,  $K^-$  production at 20, 31 and 40 GeV/c. At higher energies all O.K.**

**What is the matter?**

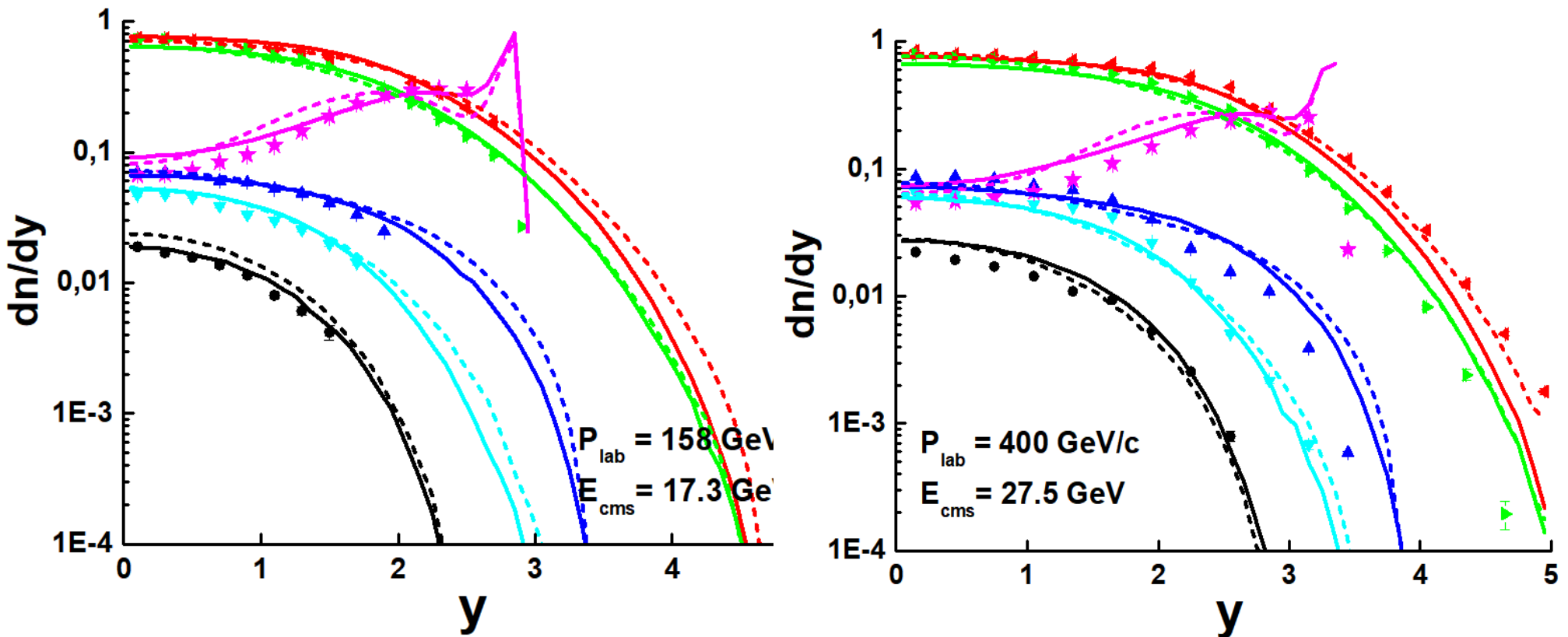
**Who is wrong – Exp. Or Theory.?**

# Inclusive one-particle distributions ...

Measurements of  $\pi^\pm$ ,  $K^\pm$ ,  $p$  and  $\bar{p}$  spectra in proton-proton interactions at 20, 31, 40, 80 and 158 GeV/c with the NA61/SHINE spectrometer at the CERN SPS

Eur. Phys. J. C (2017) 77:671

NA61/SHINE Collaboration



Pythia 6.4 – dashed lines, G4 FTF – solid lines

**Pythia 6.4 and FTF give close predictions for all energies, except proton spectra.**

**Proton spectra???**

# How to improve the description of protons and kaons?

## FTF model : basic assumptions

B.Andersson et al. Nucl. Phys. B281 289 (1987)

B.Nilsson-Almqvist, E.Stenlund, Comp. Phys. Comm. 43 387 (1987).

Fig. 1: Processes of string's creations considered in the FTF model.

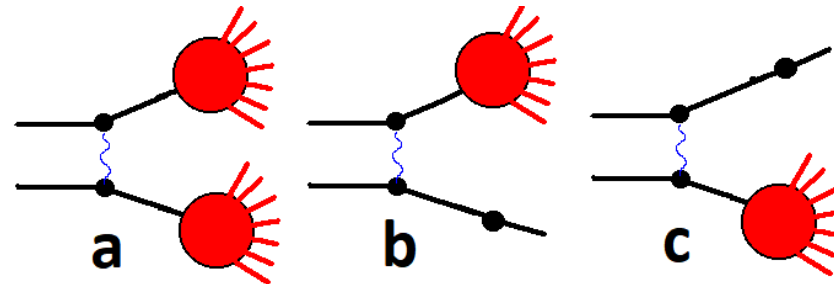
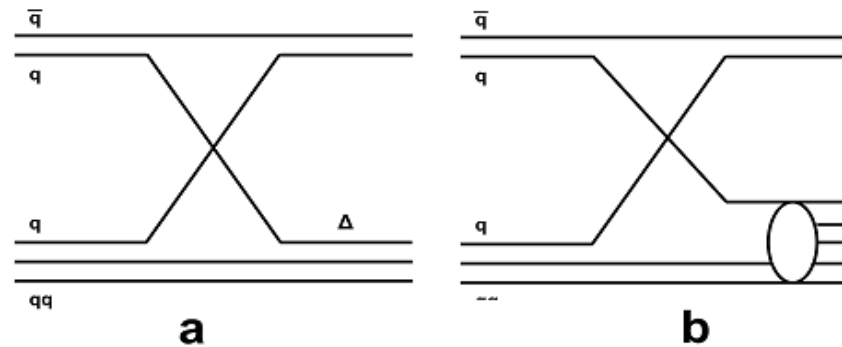


Fig. 2 Additional quark exchange processes in the FTF model.



String mass distribution

$$dW/dP^- = (1 - f) \frac{1}{\ln(P_{max}^-/P_{min}^-)} 1/P^- + f \frac{1}{P_{max}^- - P_{min}^-},$$

$$P^- = \sqrt{M^2 + P_T^2 + P_z^2} - P_z \simeq (M^2 + P_T^2)/2 P_z \quad (P_z \rightarrow \infty) \quad f = 0.55$$

# FTF model: string fragmentation details

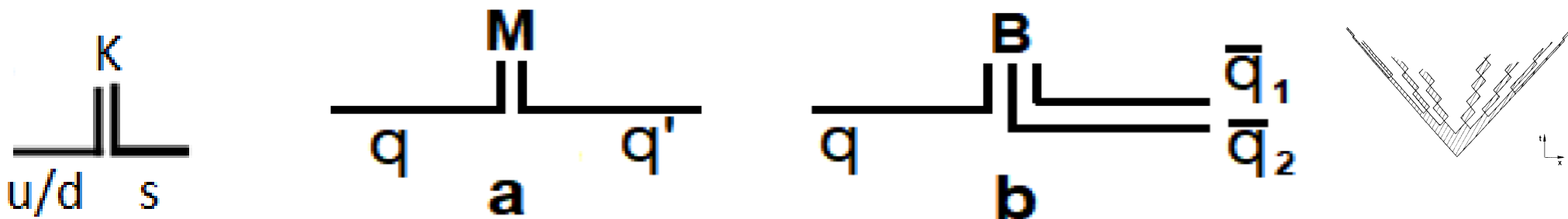


Figure 9: Vertices of quark fragmentations.

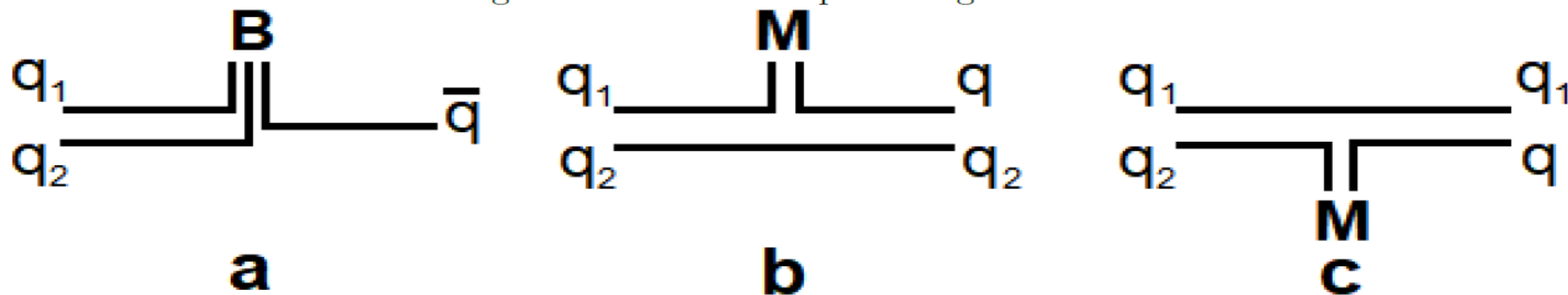
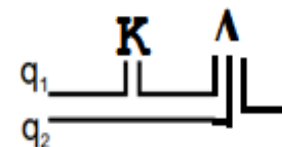


Figure 10: Vertices of diquark fragmentations.

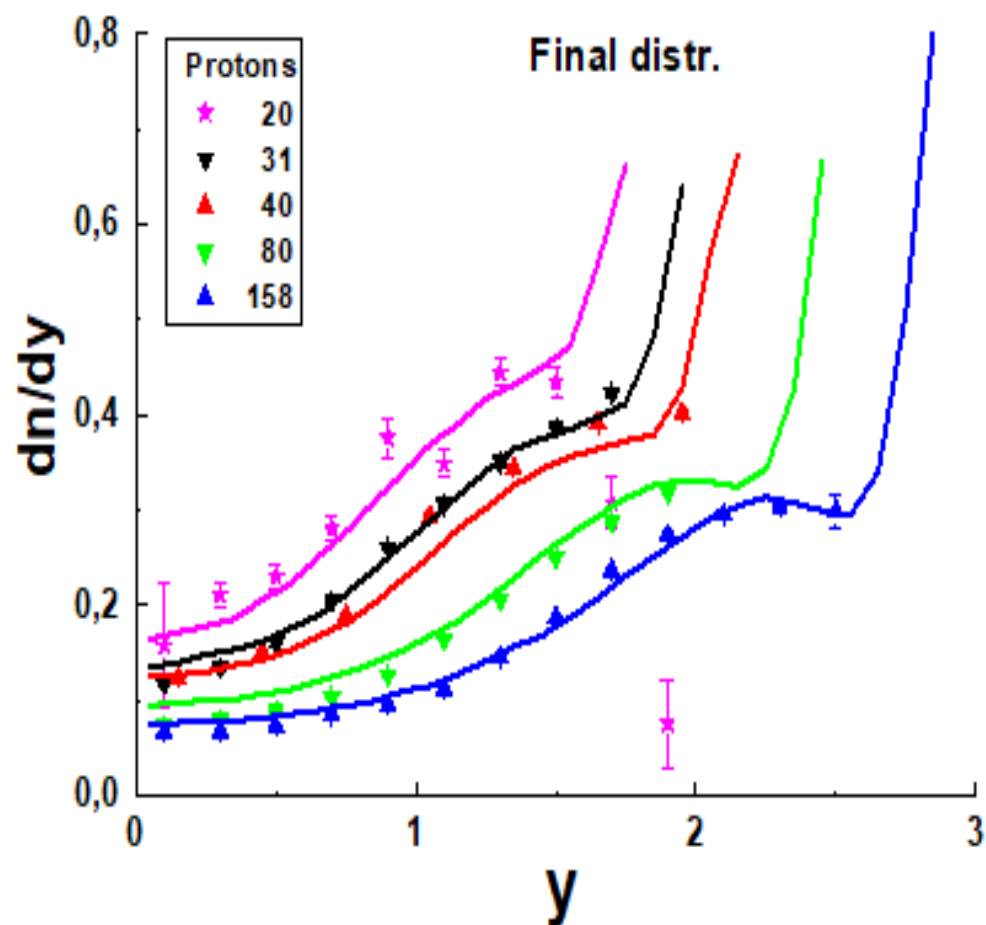
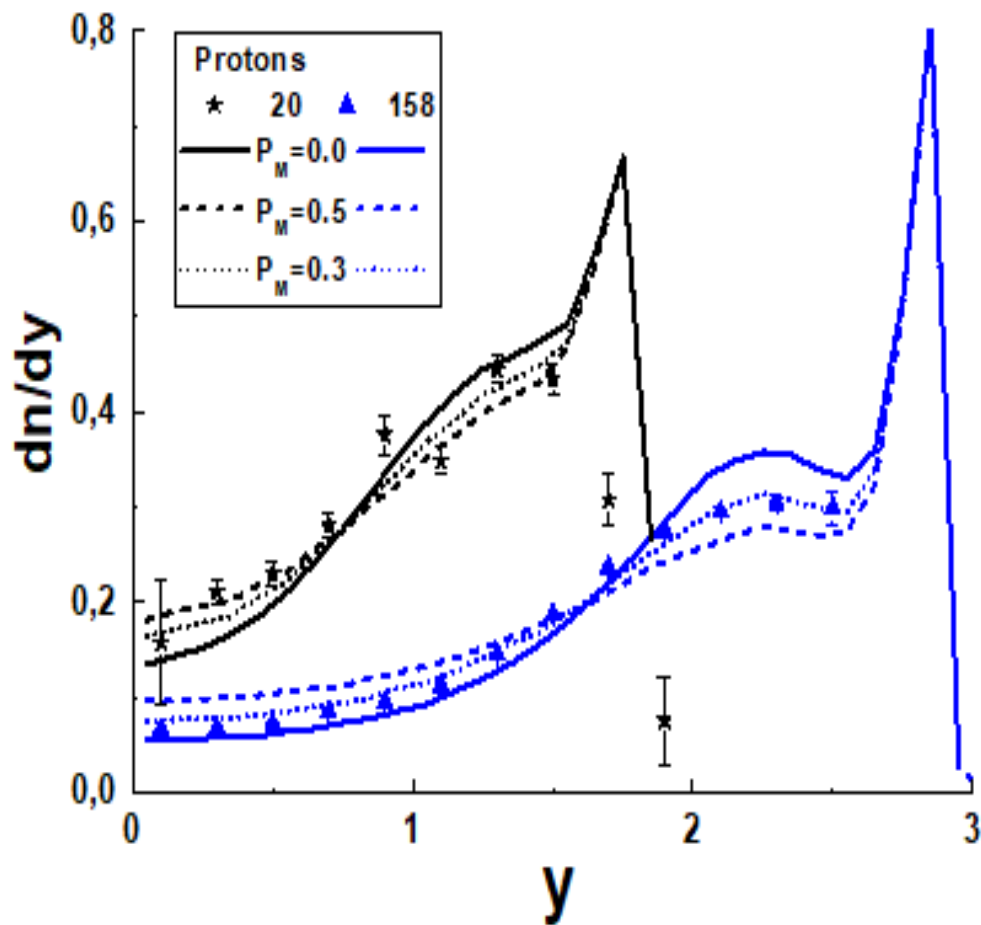
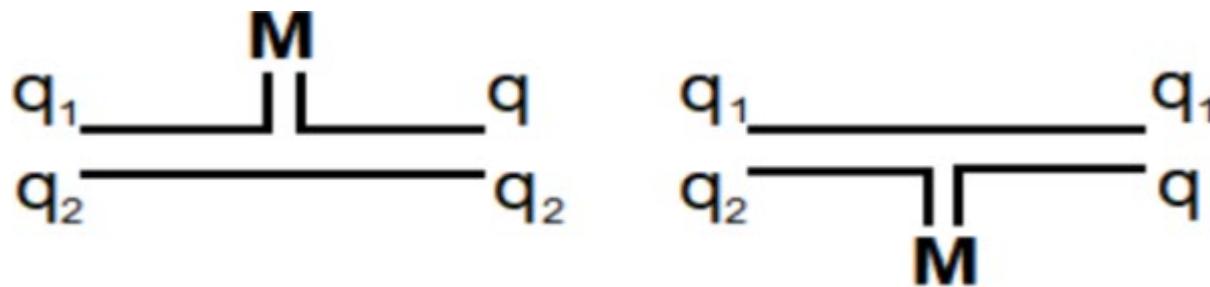


**For mesons**  $f(z) \propto z^{-1} (1-z)^a \exp(-b m_T^2/z)$ ,  $a = 1$ ,  $b = 0.7 (GeV)^{-2}$ ,  $m_T^2 = m_h^2 + P_T^2$ .

**For baryons, a'la Kaidalov**  $f(z) = \frac{c}{(z_{max} - z_{min})^c} (z - z_{min})^{c-1}$ ,  $c = 2 + P_T^2$ .



# Proton production, Geant4 FTF model: tune of $P_M$

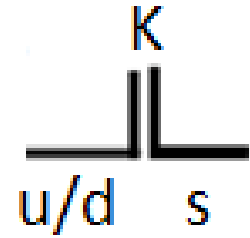
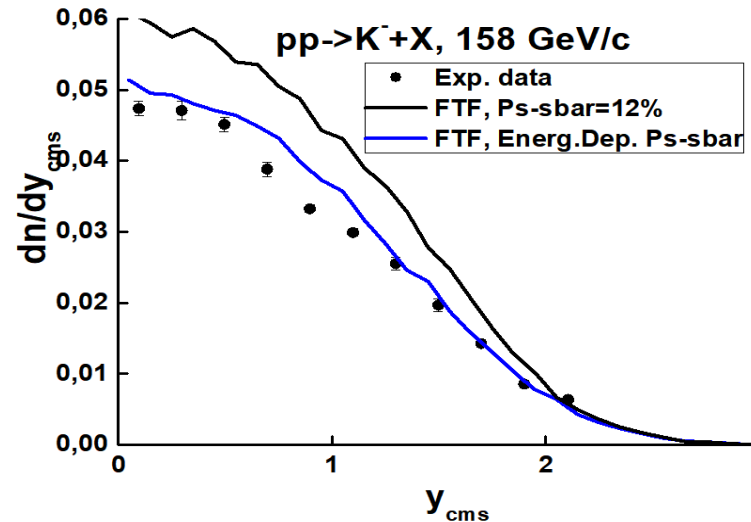
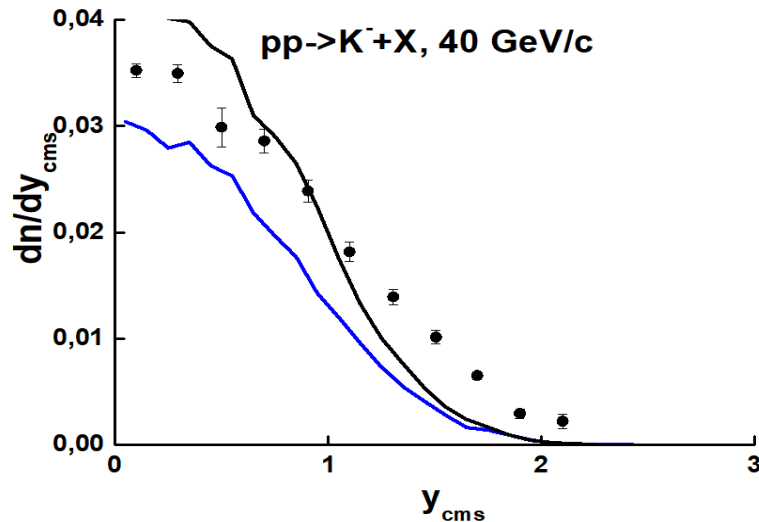
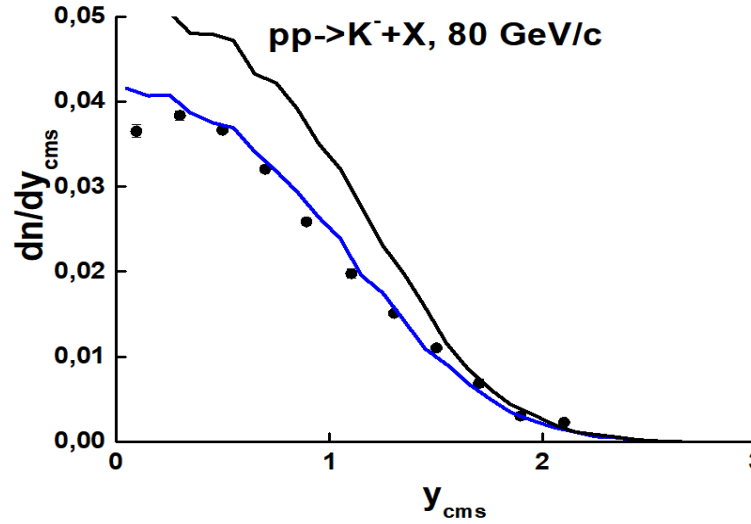
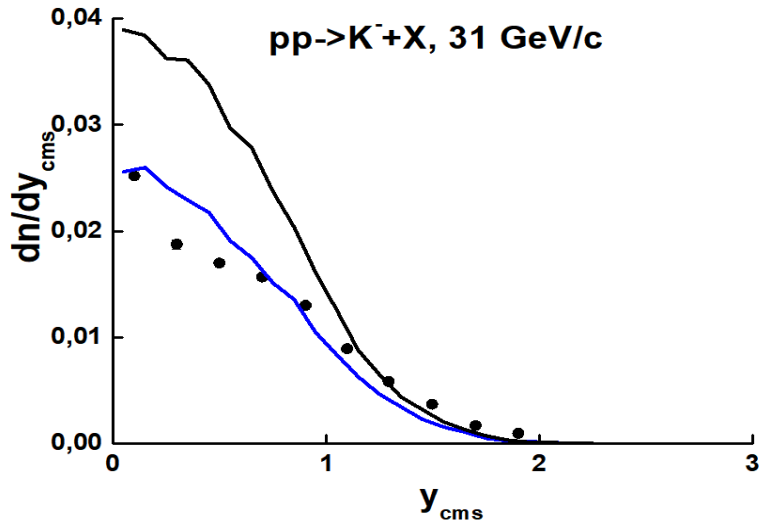


**Meson's production by diquarks is the main feature of Geant4 FTF!**

# Strange particle production, Geant4 FTF model: tune of Ps-sbar (12 %)

The Schwinger model of quark' pair production from the vacuum in a strong color field.

$$\exp\left(-\frac{\pi m_{\perp}^2}{\kappa}\right) = \exp\left(-\frac{\pi m^2}{\kappa}\right) \exp\left(-\frac{\pi p_{\perp}^2}{\kappa}\right)$$



**Black lines:**  
Ps-sbar = 12 %

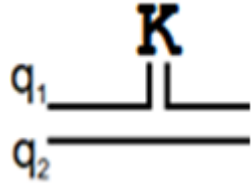
**Blue lines:**  
Ps-sbar = 0.12\*  
[1 - (Mth/Mstr)<sup>2.5</sup>]

**Dependence  
of Ps-sbar  
on a string  
mass ?**

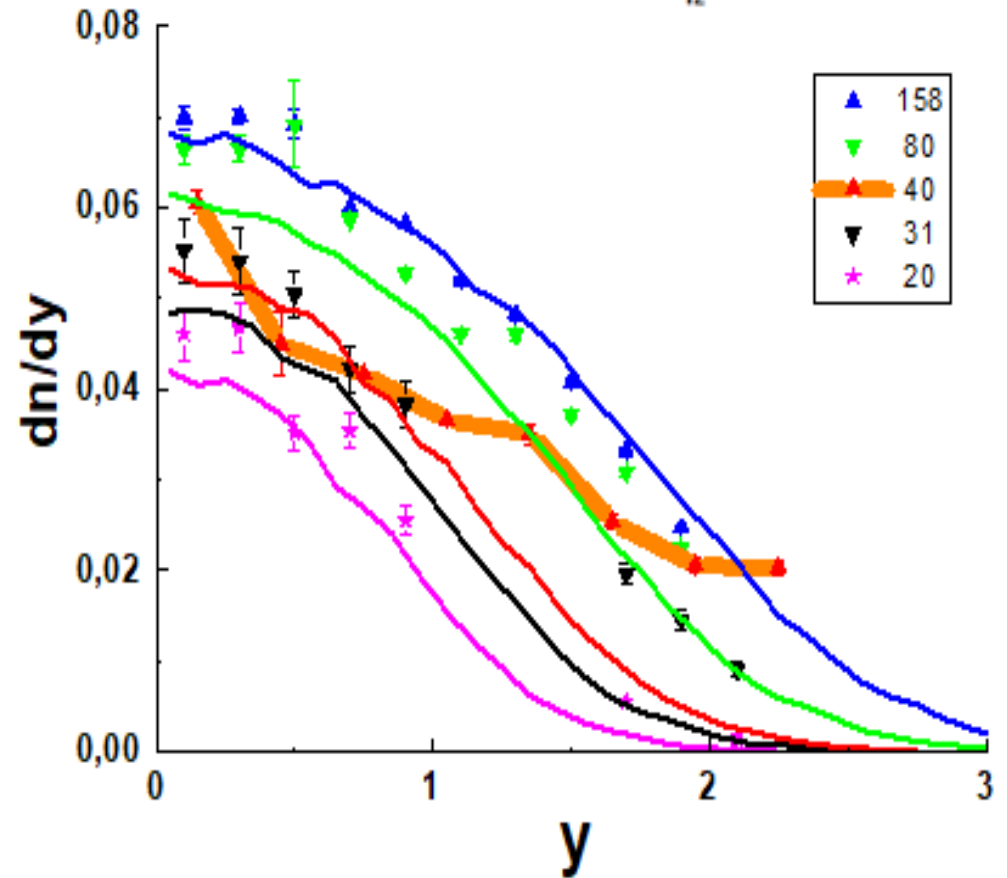
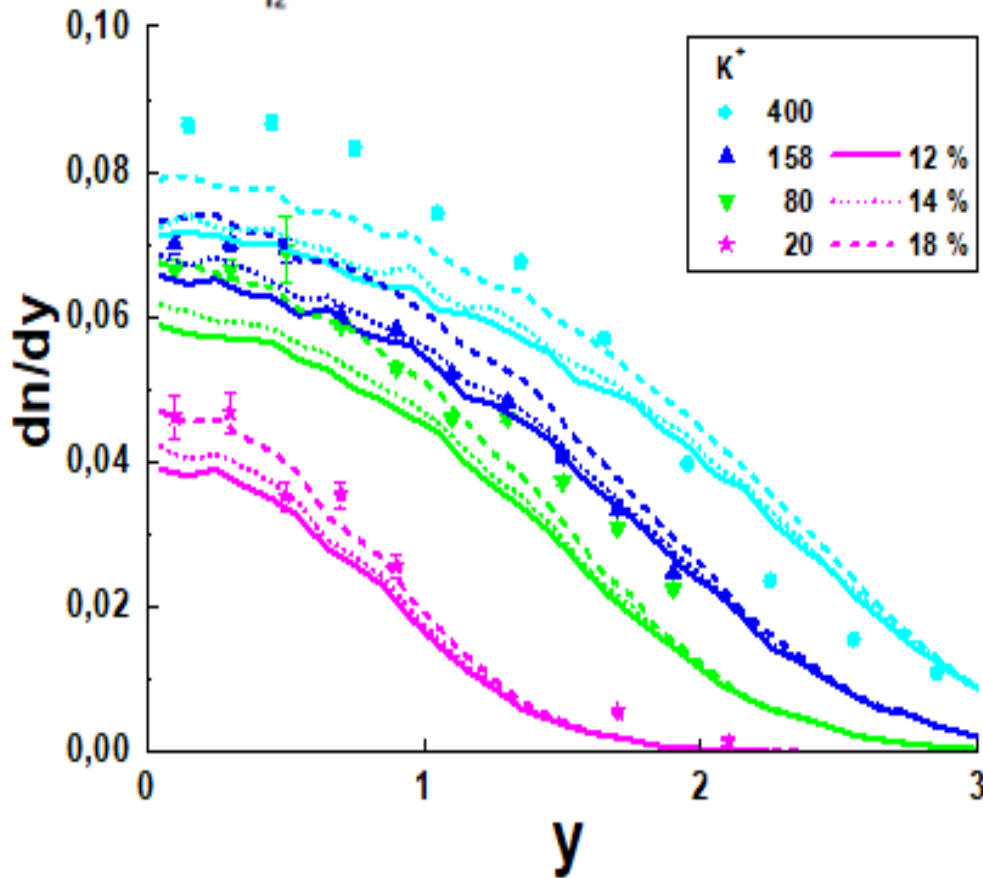
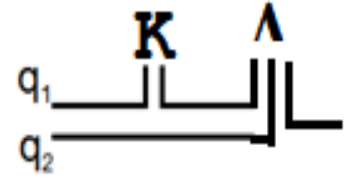
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**Ps-sbar can be different for diquarks!**



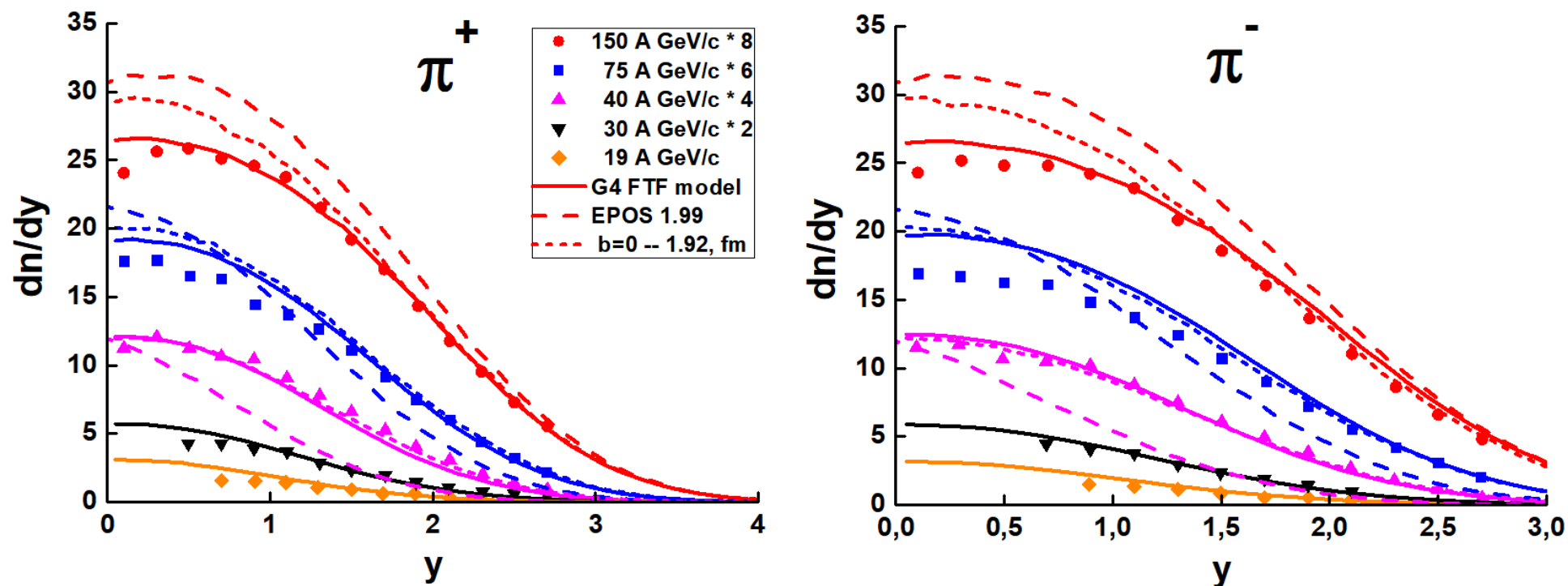
**It is impossible to choose Ps-sbar! Exp. Data scatter too strongly!**

Maybe a consideration of other data will help?

NA61/SHINE data on Be-7 + Be-9  $\pi B_{max}^2 = (C/100) \sigma_{AB}^{in}$   
20 % centrality, dn/dy of  $\pi$  mesons

**EPOS 1.99 and Geant4 FTF models**

**EPOS well describes the data at 150 A GeV**



Dashed lines – EPOS calculations, solid ones – Geant4 FTF.

**Geant4 FTF O.K.** EPOS shows a strange energy dependence of the distributions and their form especially at low energies. Changing the centrality selection helps a lot.

**Maybe a consideration of other data will help?**

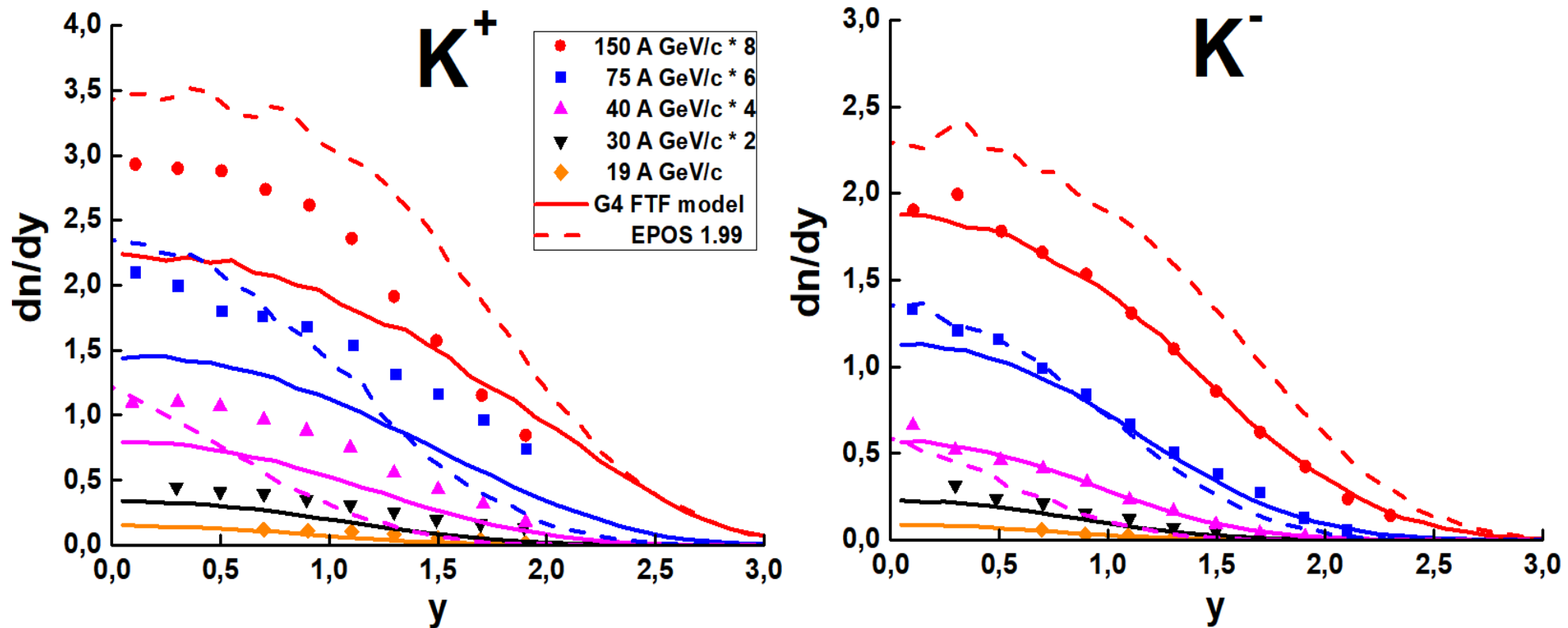
**NA61/SHINE data on Be-7 + Be-9**

**20 % centrality, dn/dy of  $\pi$  mesons**

**EPOS 1.99 and Geant4 FTF models**

**cannot describe  $K^+$  meson production**

**Geant4 FTF model well describes  $K^-$  production**



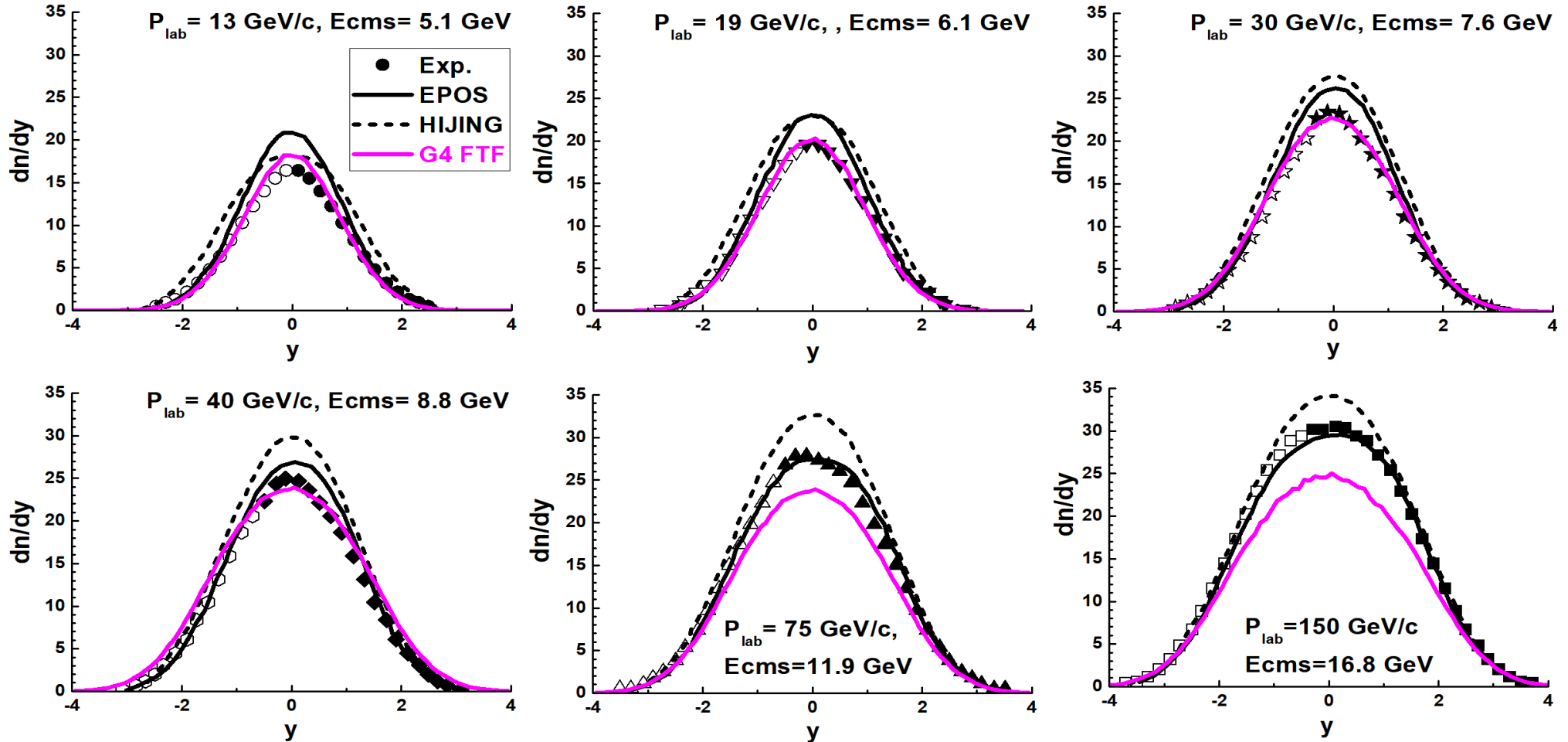
**Dashed lines – EPOS calculations, solid ones – Geant4 FTF.**

**EPOS shows a strange energy dependence of the distributions and their form especially at low energies.**

# NA61/SHINE data on Ar-40 + Sc-45 and FTF model

## 5 % centrality, $dn/dy$ of $\pi^-$ mesons

A. Galoyan, A. Ribon, V. Uzhinsky, *Eur.Phys.J.C* 82 (2022) 181



**NA61: HIJING overestimates all data. No tuning!**

**NA61: EPOS overestimates data at  $E_{cms} < 10$  GeV, at  $> 10$  GeV – OK.**

**Geant4 FTF – OK at  $E_{cms} < 10$  GeV, underestimates at  $E_{cms} > 10$  GeV, after improvements.**

**Main problem – Centrality!**

**QGP**

**at**

**7 or 10 GeV?**

**Latest data:** Arxiv:hep-exp:2308.16683 (31 Aug. 2023)

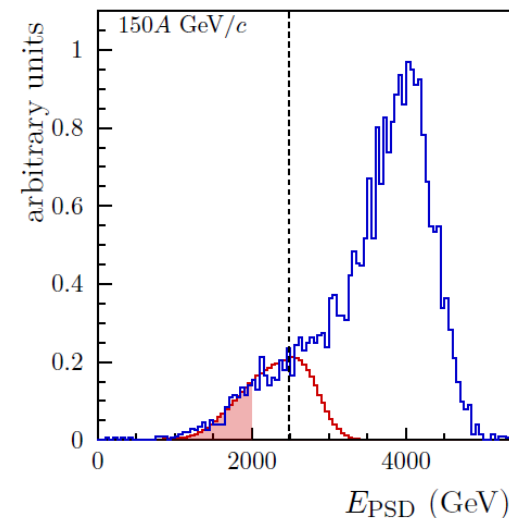
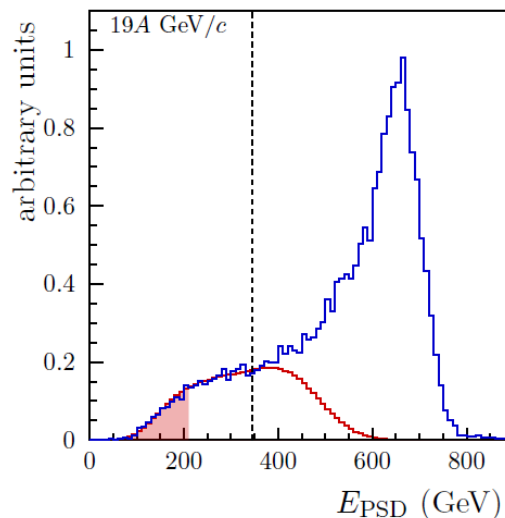
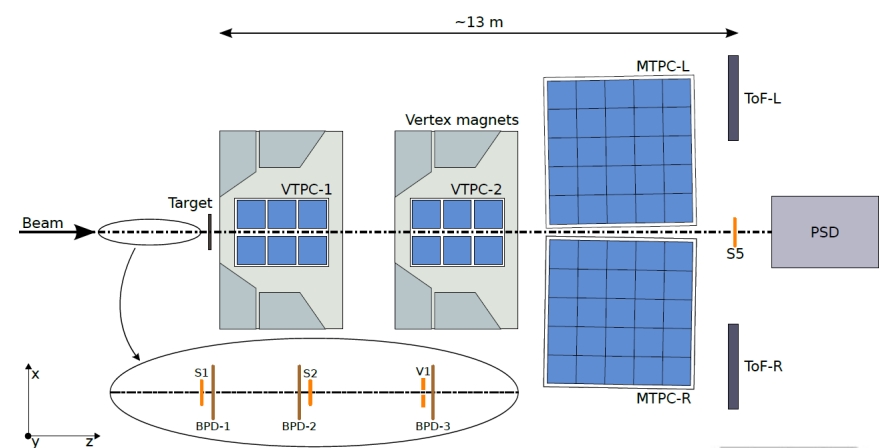
**Measurements of  $\pi^\pm$ ,  $K^\pm$ , p and anti-p spectra in 40Ar+45Sc collisions at 13A to 150A GeV/c**

**2 questions have to be solved:**

**a) What is the impact parameter range, or what are criteria for selections of events with various centralities?**

**b) Be or not to Be the nucleon diffraction dissociation?**

$$\pi B_{max}^2 = (C/100) \sigma_{AB}^{in} - 70 \text{ GeV} \quad \mathbf{2000 \text{ GeV is missed!}}$$

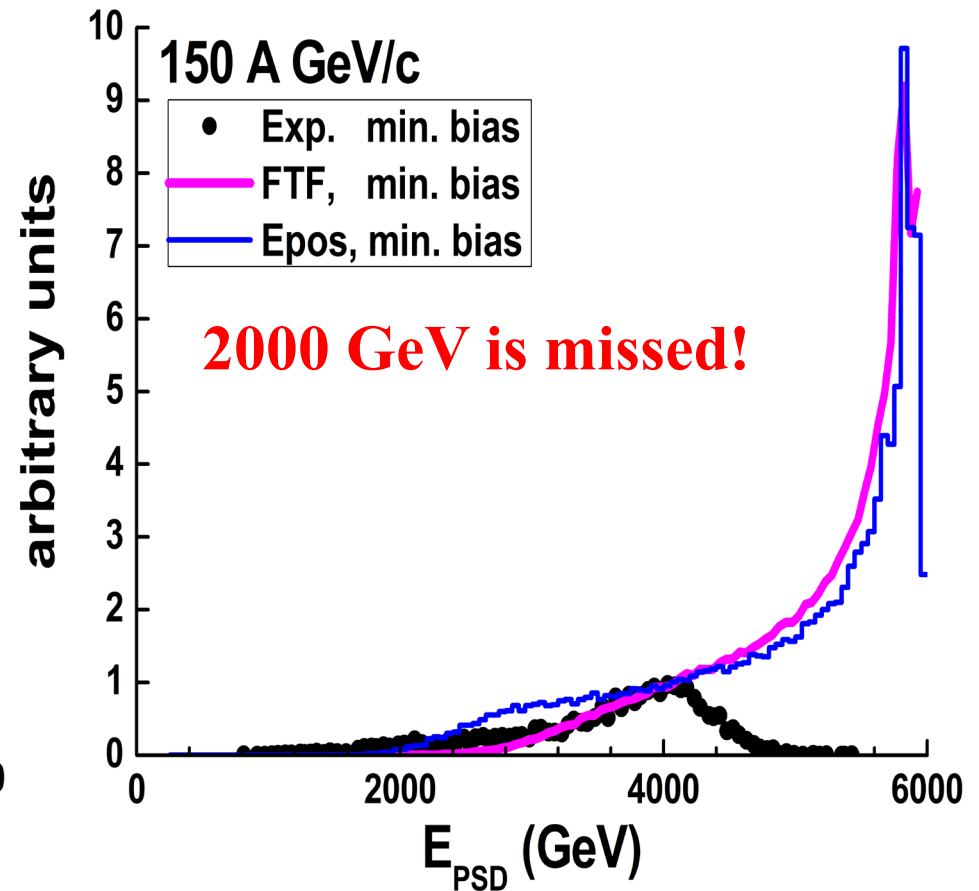
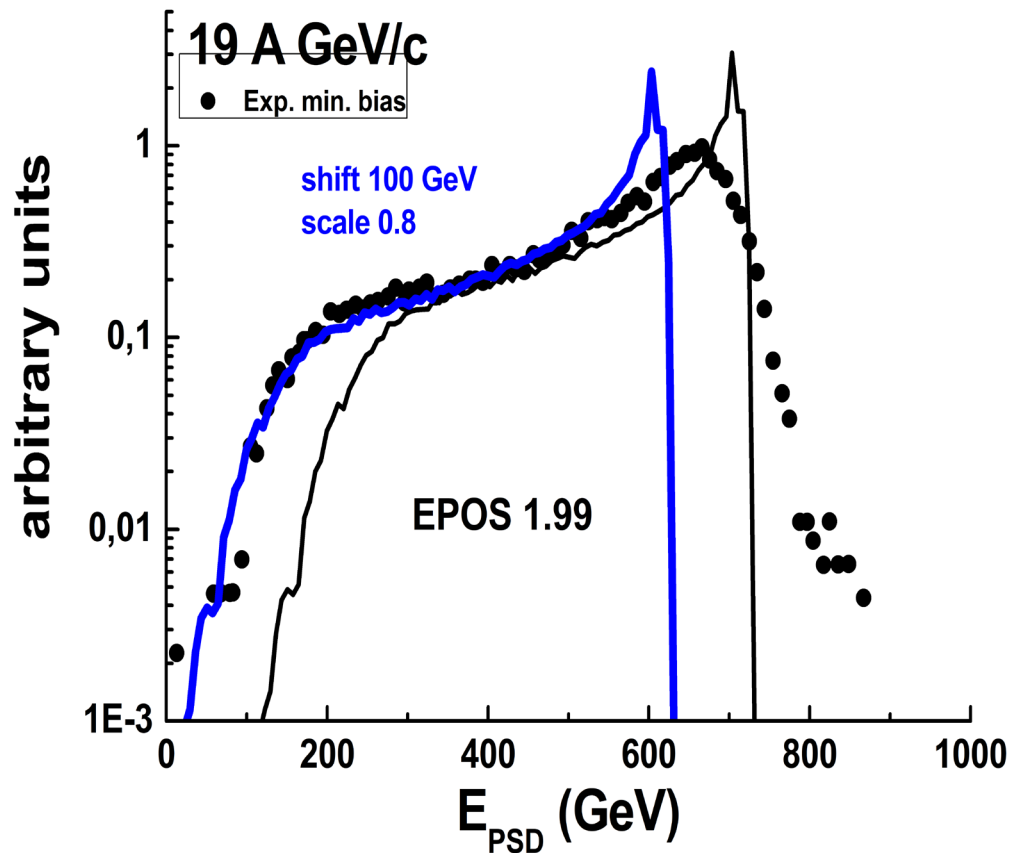


— T1 trigger    — T2 trigger (scaled)    ■ 5% centrality    --- Normalization region

|    |    |    |    |    |    |    |    |
|----|----|----|----|----|----|----|----|
| 29 | 30 | 31 | 32 |    |    |    |    |
| 44 | 17 | 18 | 19 | 20 | 23 |    |    |
| 42 | 26 | 11 | 2  | 3  | 4  | 21 | 24 |
| 42 | 27 | 8  | 10 | 11 | 12 | 22 | 25 |
| 41 | 26 | 25 | 24 | 23 | 26 |    |    |
| 40 | 39 | 38 | 37 |    |    |    |    |

150A GeV/c

# Questions? 5 % centrality ? Bmax ?



As seen, there is no a correspondence between Exp. data and EPOS one in high part of Epsd after E-shift and scale

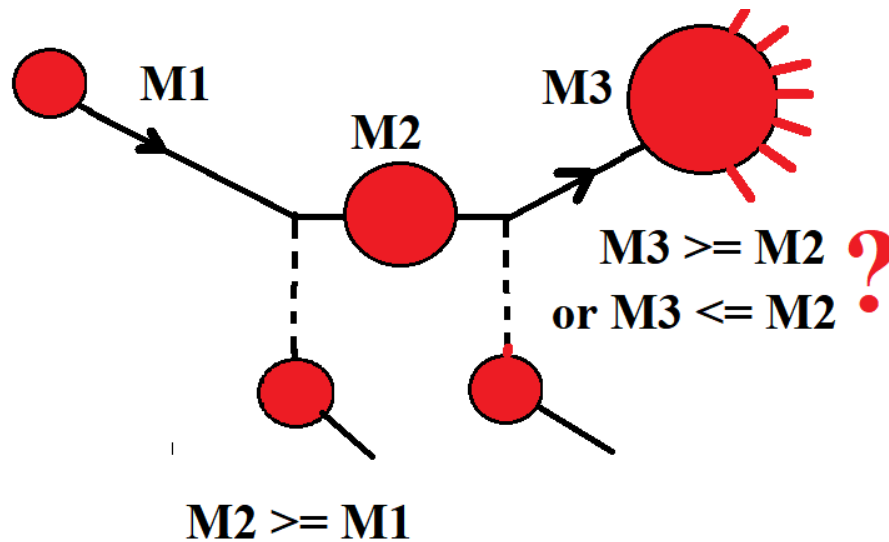
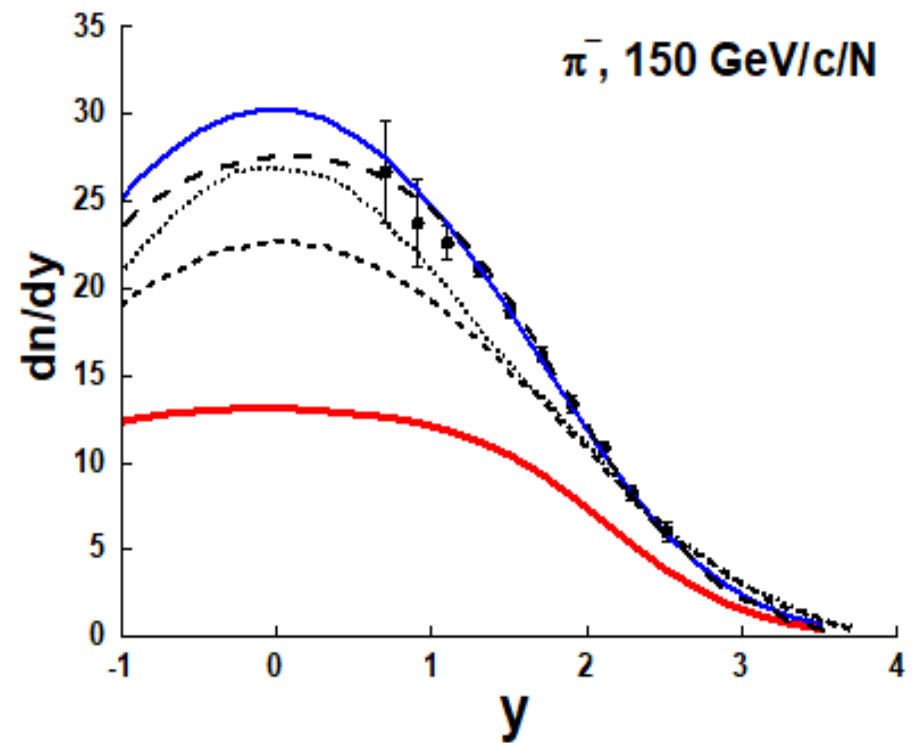
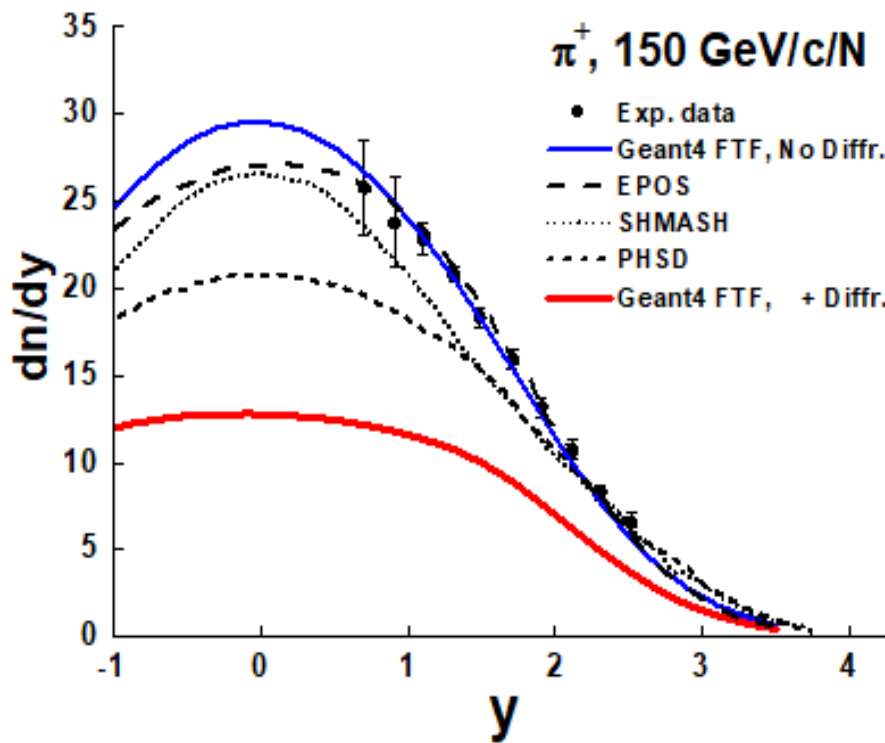
Nuclear residual fragmentation in EPOS is not adequate to Exp.

$$\pi B_{max}^2 = (C/100) \sigma_{AB}^{in}$$



# Ar-40 + Sc-45 20 % centrality

## The nucleon diffraction in nucleus-nucleus interactions ?

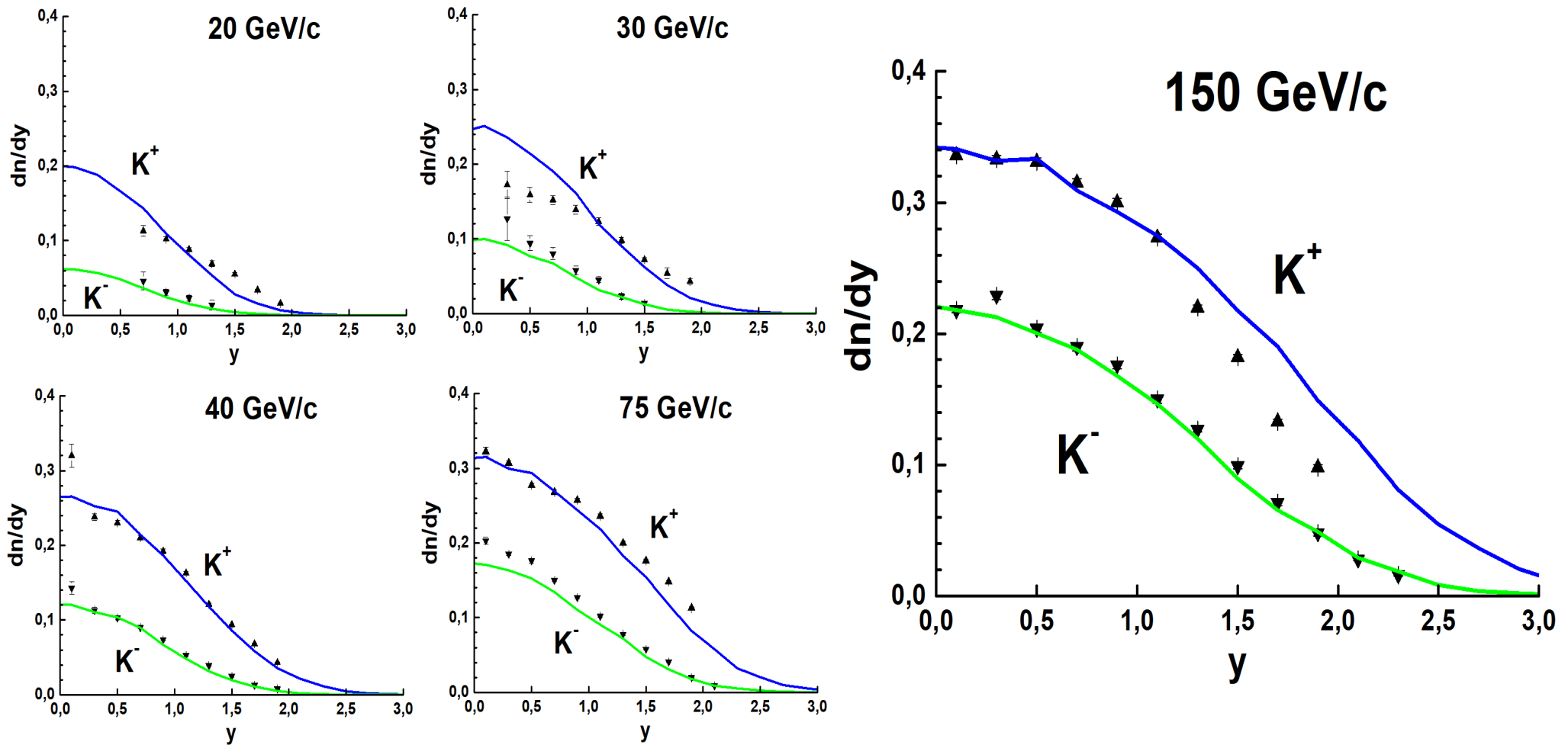


**No diffraction  
at all!?**

**It is corresponds  
to QGSM.**

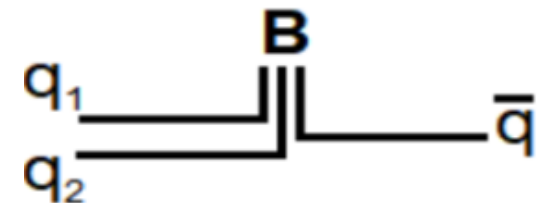
# Ar-40 + Sc-45 20 % centrality

## Strangeness in the nucleus-nucleus interactions

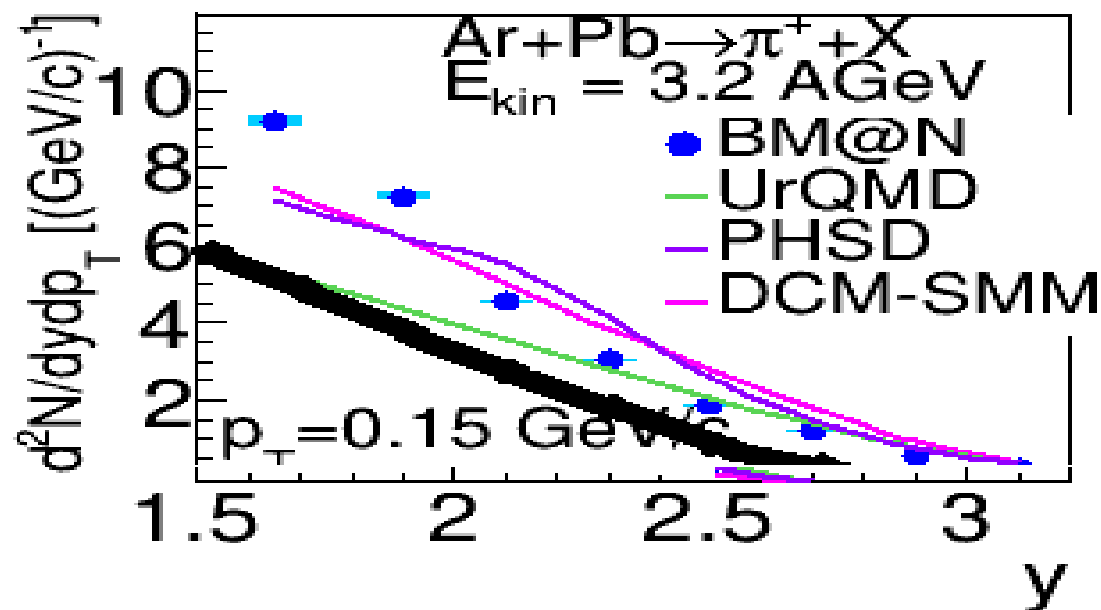
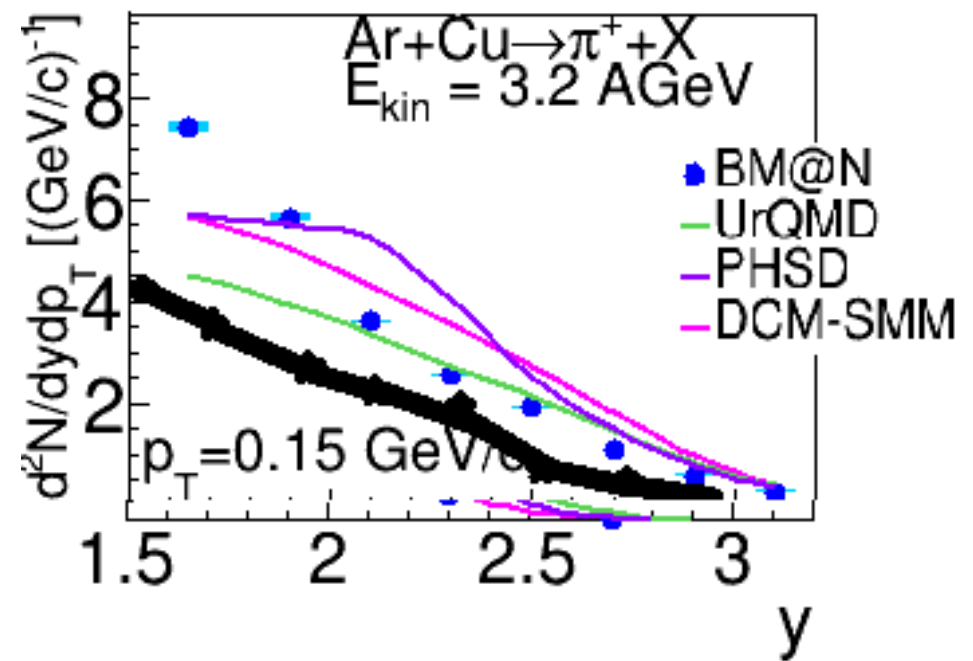
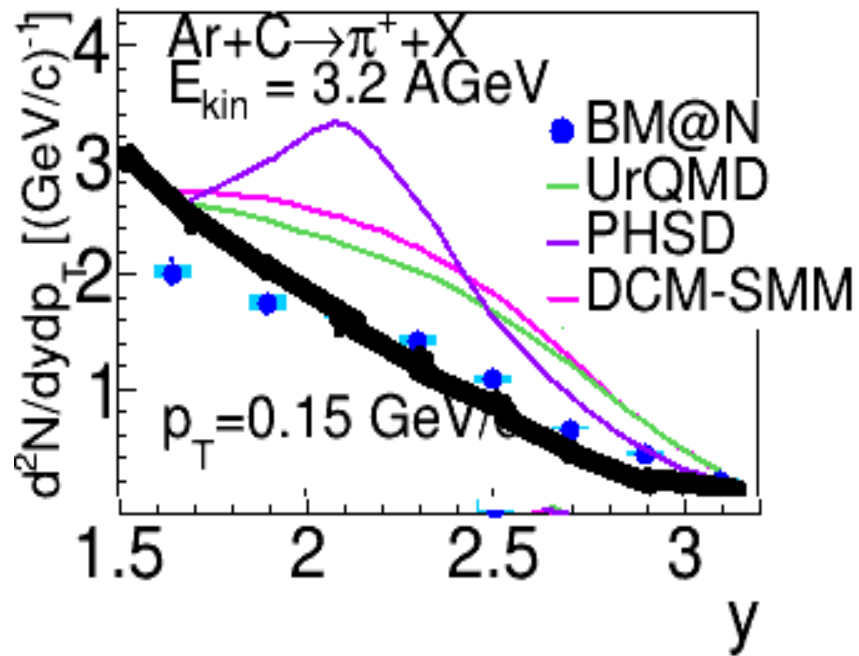


**K<sup>-</sup> O.K.    K<sup>+</sup>, we hope, can be better!    No QGP!**

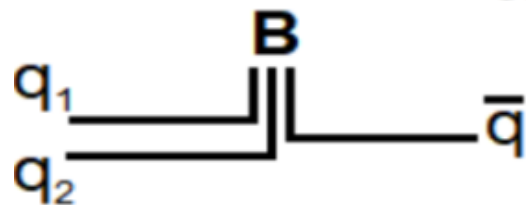
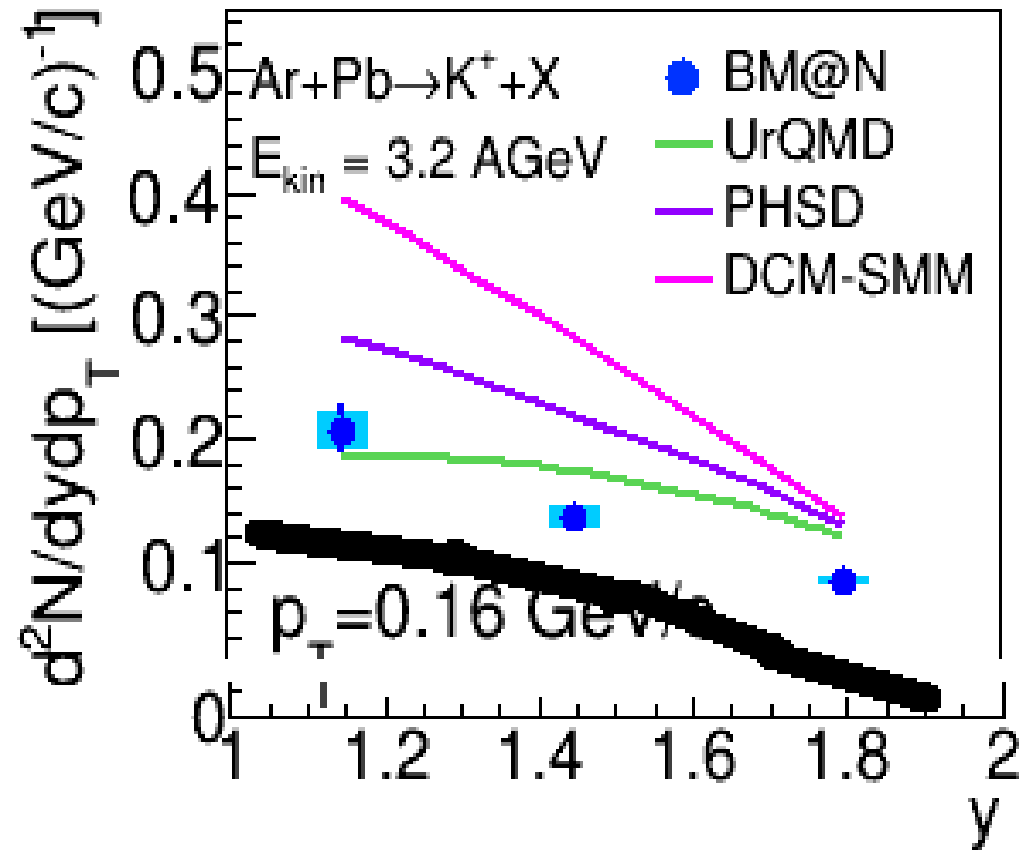
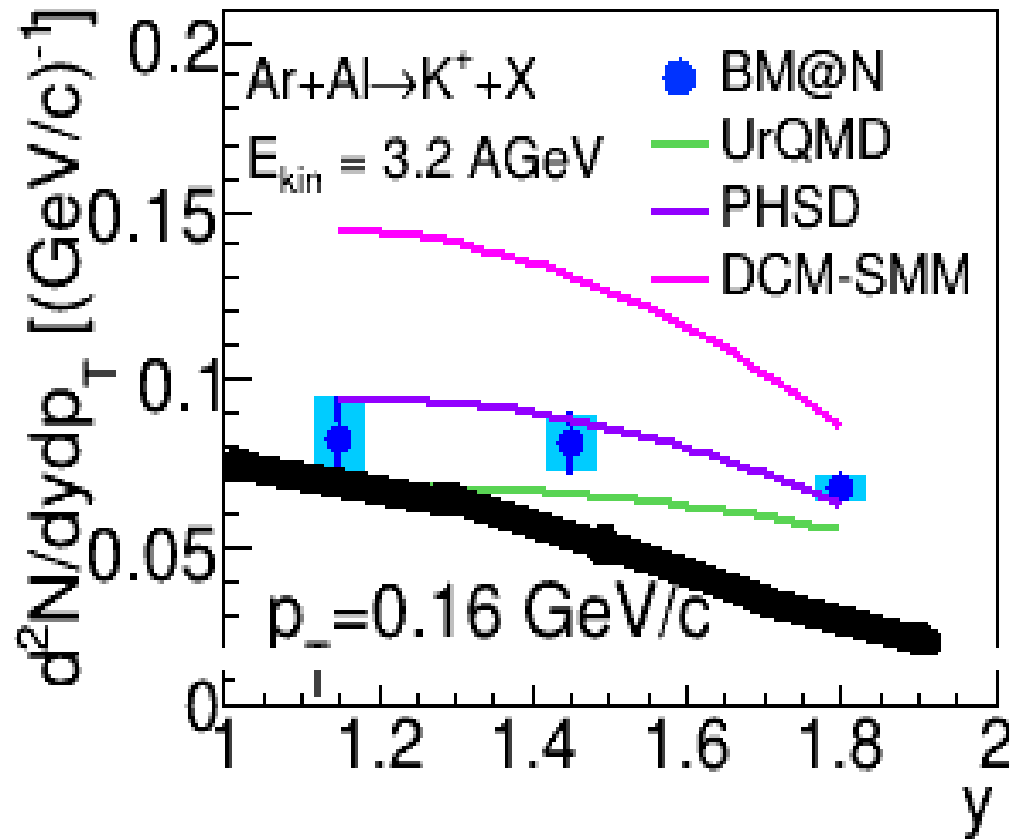
**Ps-sbar's are different!**



**Production of  $\pi^+$  and  $K^+$  mesons in argon-nucleus interactions at 3.2 AGeV**



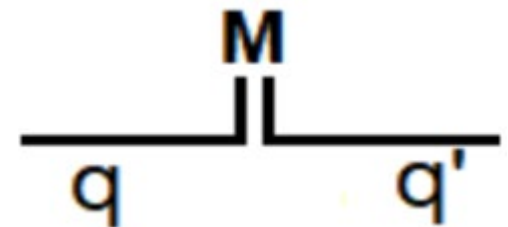
**Production of  $\pi^+$  and  $K^+$  mesons in argon-nucleus interactions at 3.2 AGeV**



Pssbar = 18 %



Pssbar = 20 %



Pssbar = 12 %

# Summary

1. Selection of events with various centralities can be a problem in MC models;
2. Reproduction of nuclear fragment properties must be checked;
3. Description of proton spectra is a problem in all MC model, **except GEANT4 FTF**;
4. Strangeness suppression must be different in various interactions!

**Prob s-sbar: pp – 12 %, pA – 18 %, AA – 30 %**

**Why?**

## Hypotheses:

1. Misidentification of  $\text{Pi}^+$  or protons as  $\text{K}^+$ ;
2. Secondary interactions --  $\text{Rho} + \text{N} \rightarrow \text{K}^+, \text{K}^-, \text{Lambda}$ ;
3. QGP;
4. Nuclear medium effect;
5. Change of the string tension parameter in nuclear medium;
6. Fragmentation of strings in instantons;
7. Color electric **Permittivity** in a medium.

Strangeness enhancement due to string fluctuations [PRD101 \(2020\)](#)  
H. J. Pirner,<sup>1</sup> B. Z. Kopeliovich,<sup>2</sup> and K. Reygers

Permittivity in electromagnetism

$$F = \frac{1}{4\pi\epsilon_a} \cdot \frac{|q_1 q_2|}{r_{12}^2}$$

**Cornell-like potentials**  $V_{\text{Cornell}} = -\frac{0.641}{r} + 0.113 \cdot r$   $V_{\text{Martin}}(r) = -8.054 + 6.870 \cdot r^{0.1}$

Baryons and tetraquarks using instanton-induced interactions; [2308.05638](#)

Nicholas Miesch,\* Edward Shuryak,+ and Ismail Zahed

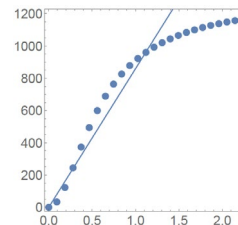
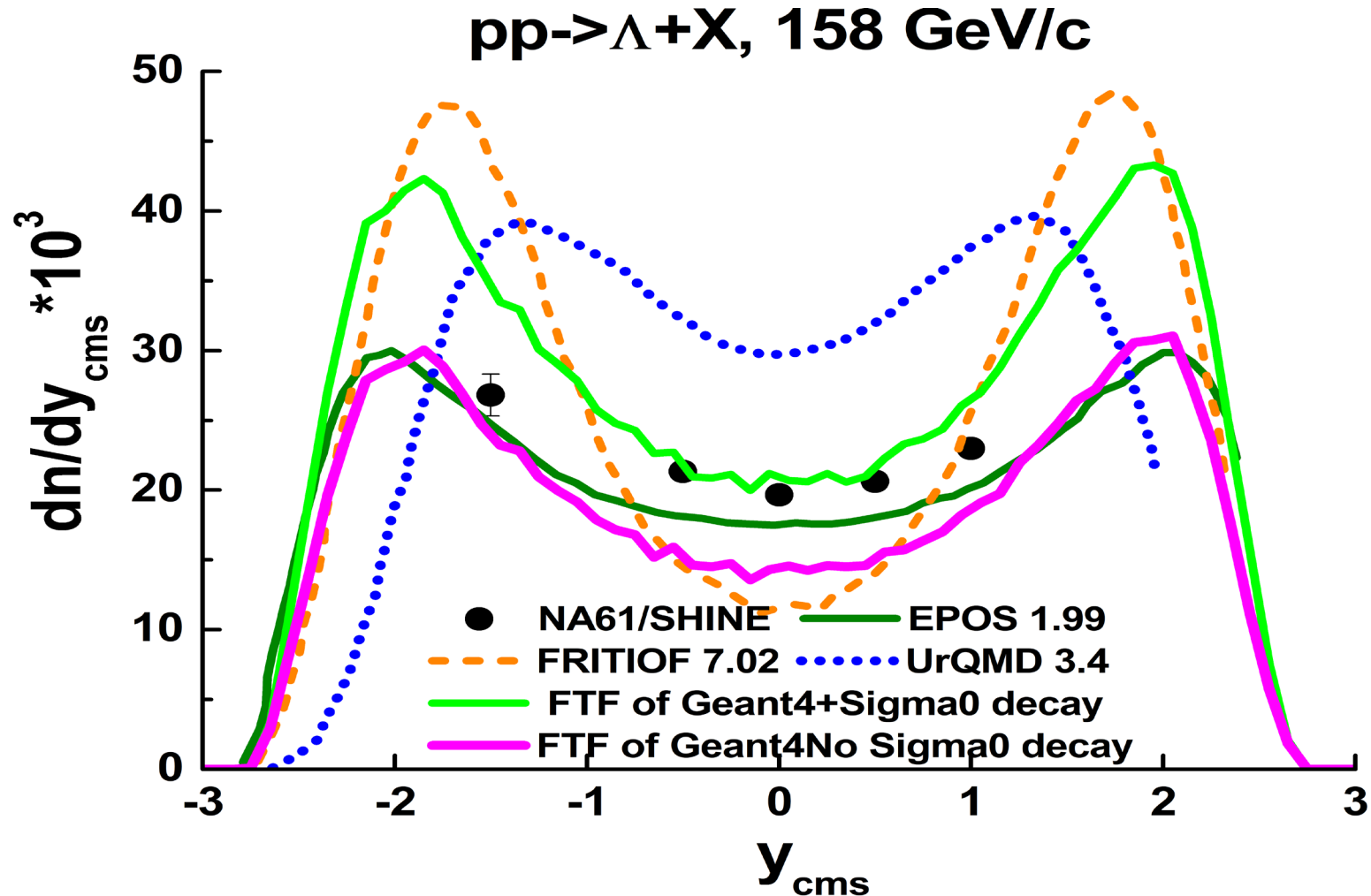


FIG. 5. The points show the instanton-induced effective potential in baryons  $V(R_6)$ , (MeV) vs  $R_6$  (fm).. The tension force is of the order of 1 GeV/fm (shown by a line for comparison)

# Production of $\Lambda$ -hyperons in inelastic p+p interactions at 158 GeV/c

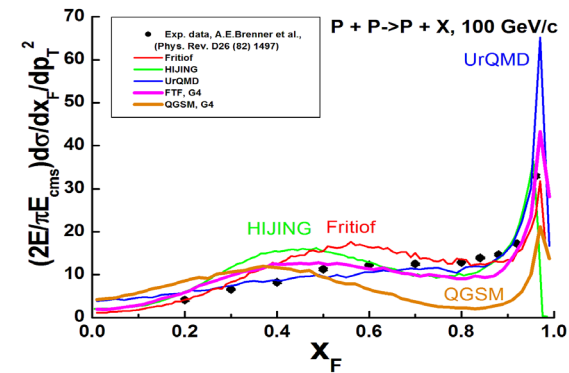
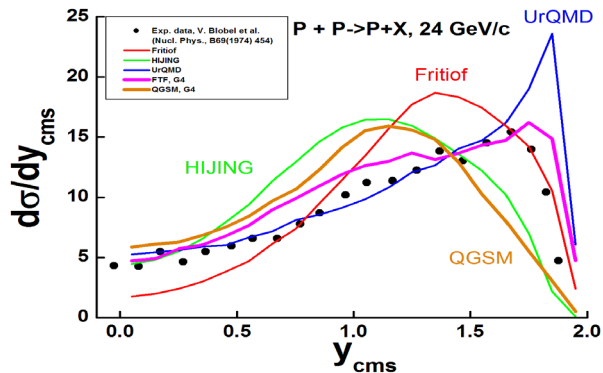
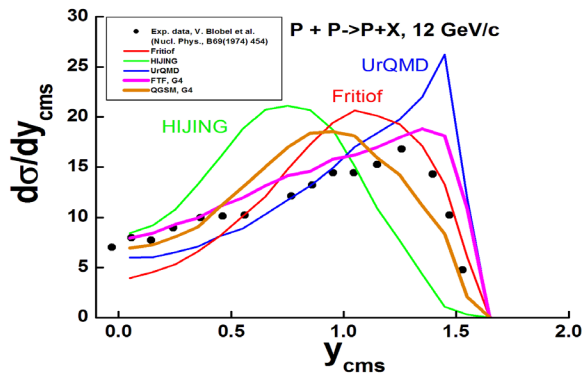
NA61/SHINE Collaboration

Eur. Phys. J. C (2016) 76:198



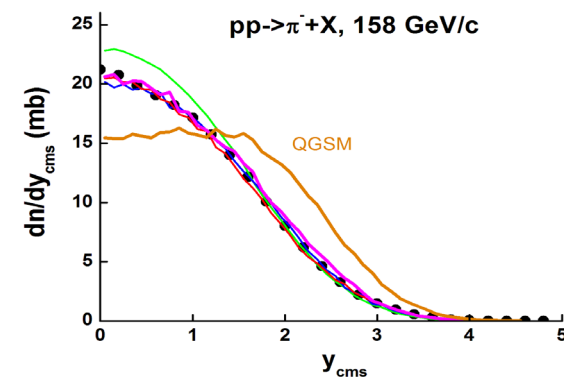
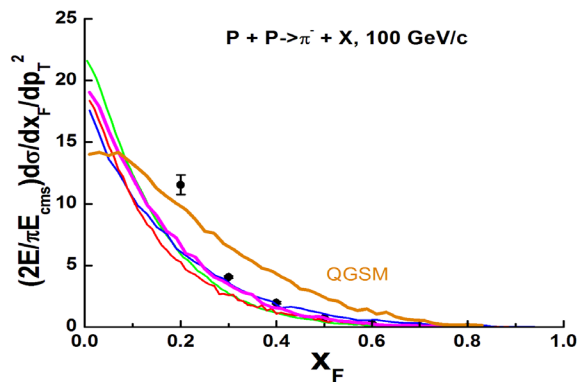
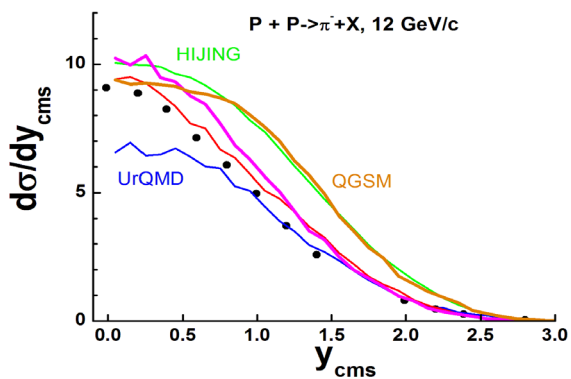
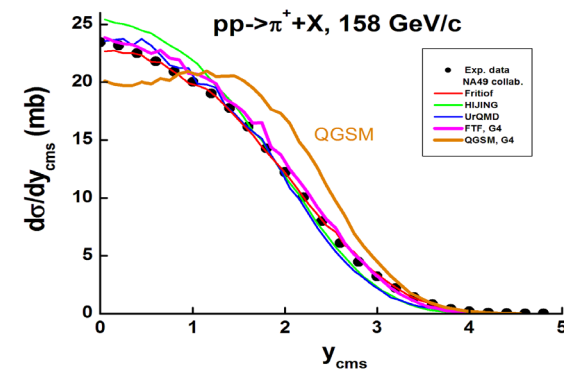
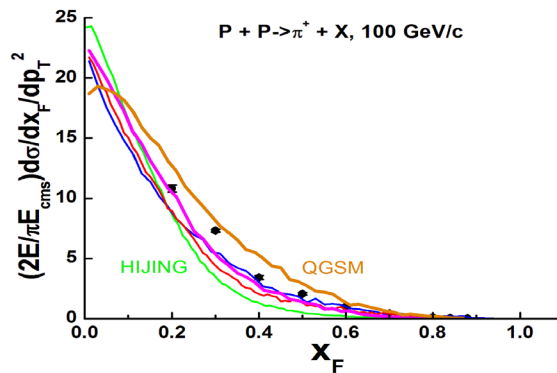
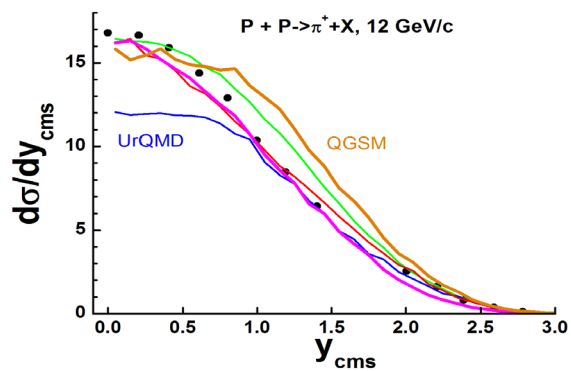
Fritiof 1.6, Fritiof 7.0, Hijing, UrQMD 3.3, pp-interactions

# Description of baryon spectra is the problem in all MC models

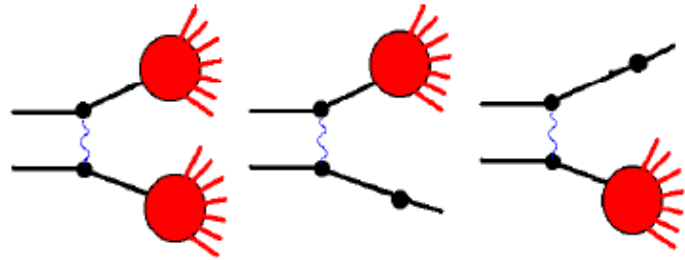


Exp. Data: V. Blobel et al., Nucl. Phys., B69(1974) 454.

## There are some problems with a description of meson spectra

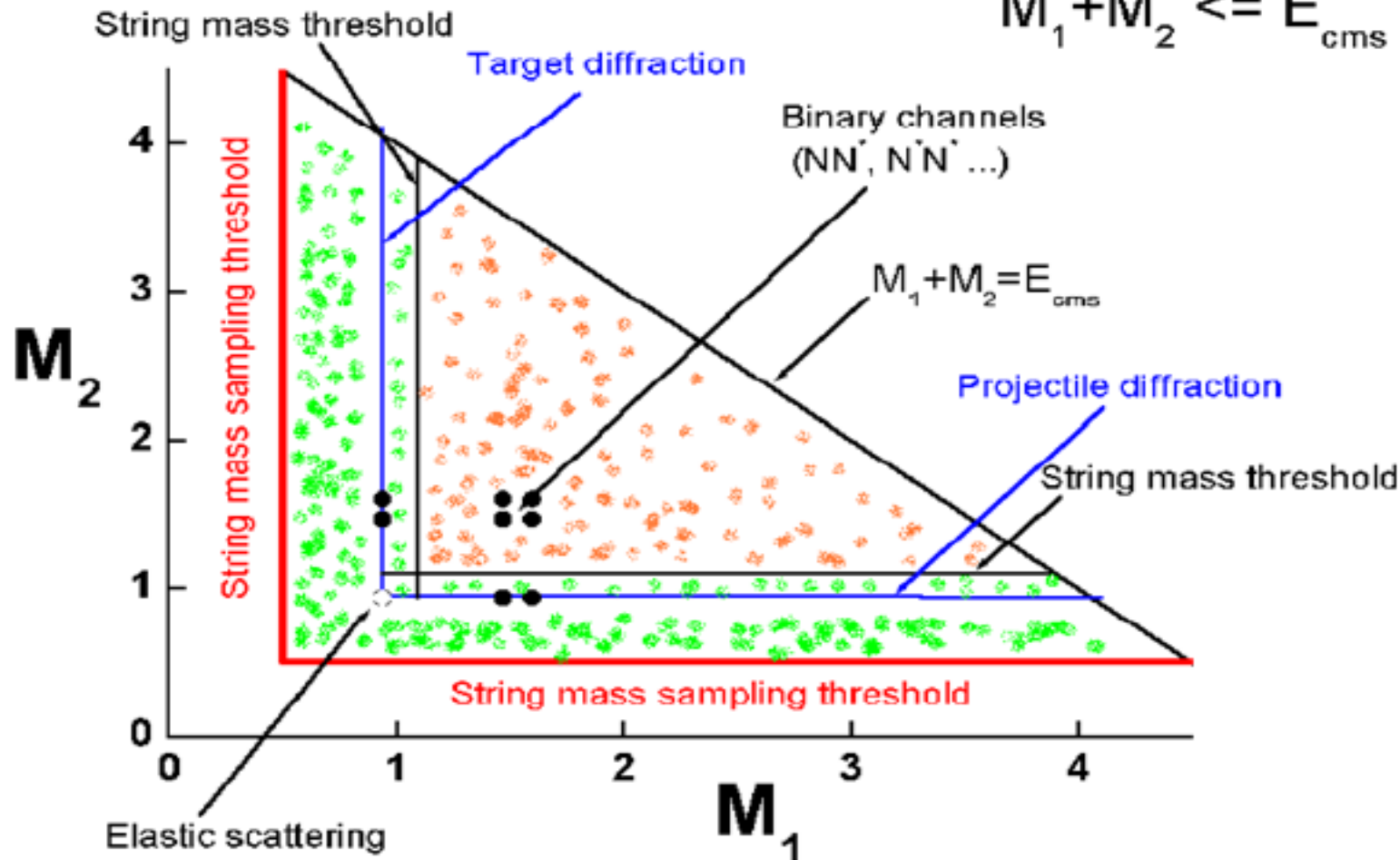


# FTF model : basic assumptions

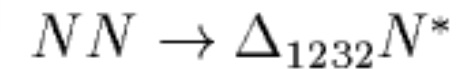
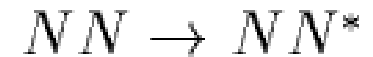


B.Andersson et al. Nucl. Phys. B281 289 (1987)  
 B.Nilsson-Almquist, E.Stenlund,  
 Comp. Phys. Comm. 43 387 (1987).

$$M_1 + M_2 \leq E_{\text{cms}}$$



UrQMD Md=1.46



Fritiof 1.6 – Md=1.2; Fritiof 7.0 Md=1.2; Hijing Md~2 **Lines**

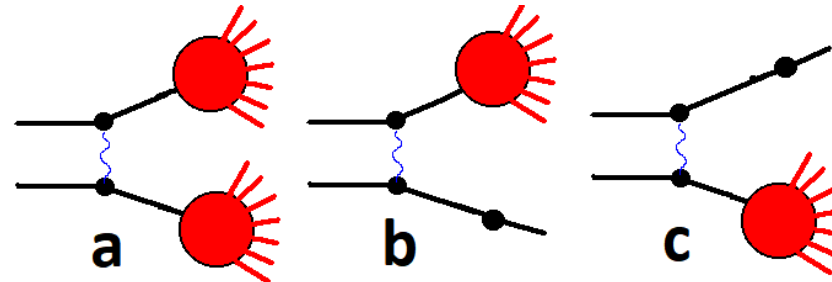


# FTF model : basic assumptions

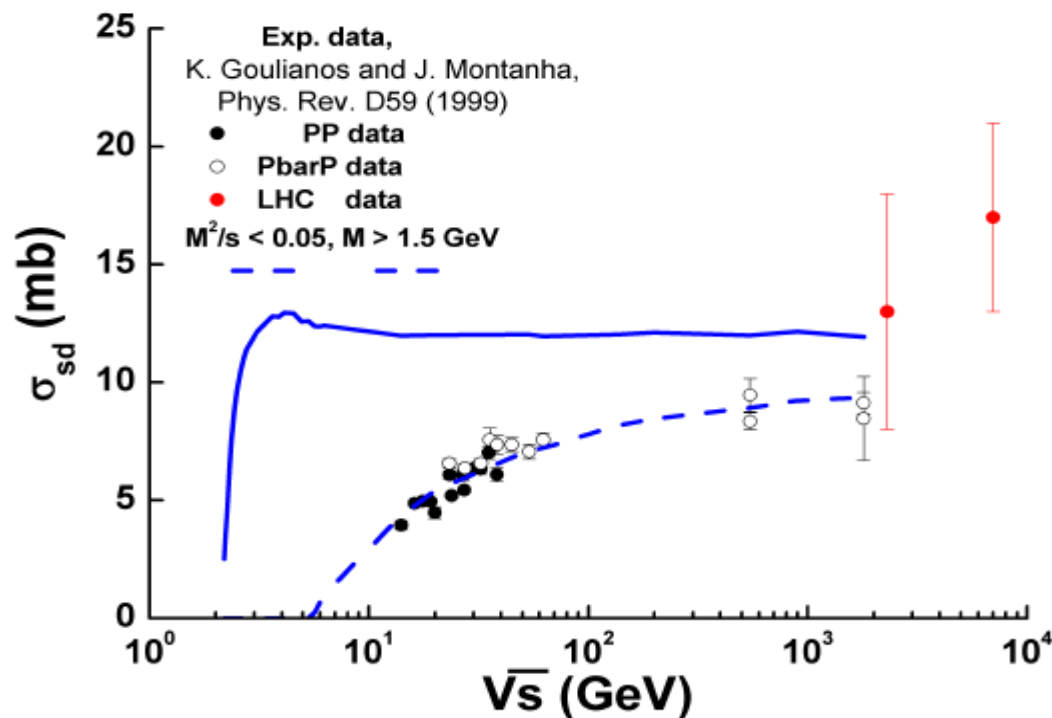
B.Andersson et al. Nucl. Phys. B281 289 (1987)

B.Nilsson-Almqvist, E.Stenlund, Comp. Phys. Comm. 43 387 (1987).

Processes of string's creations considered in the FTF model.

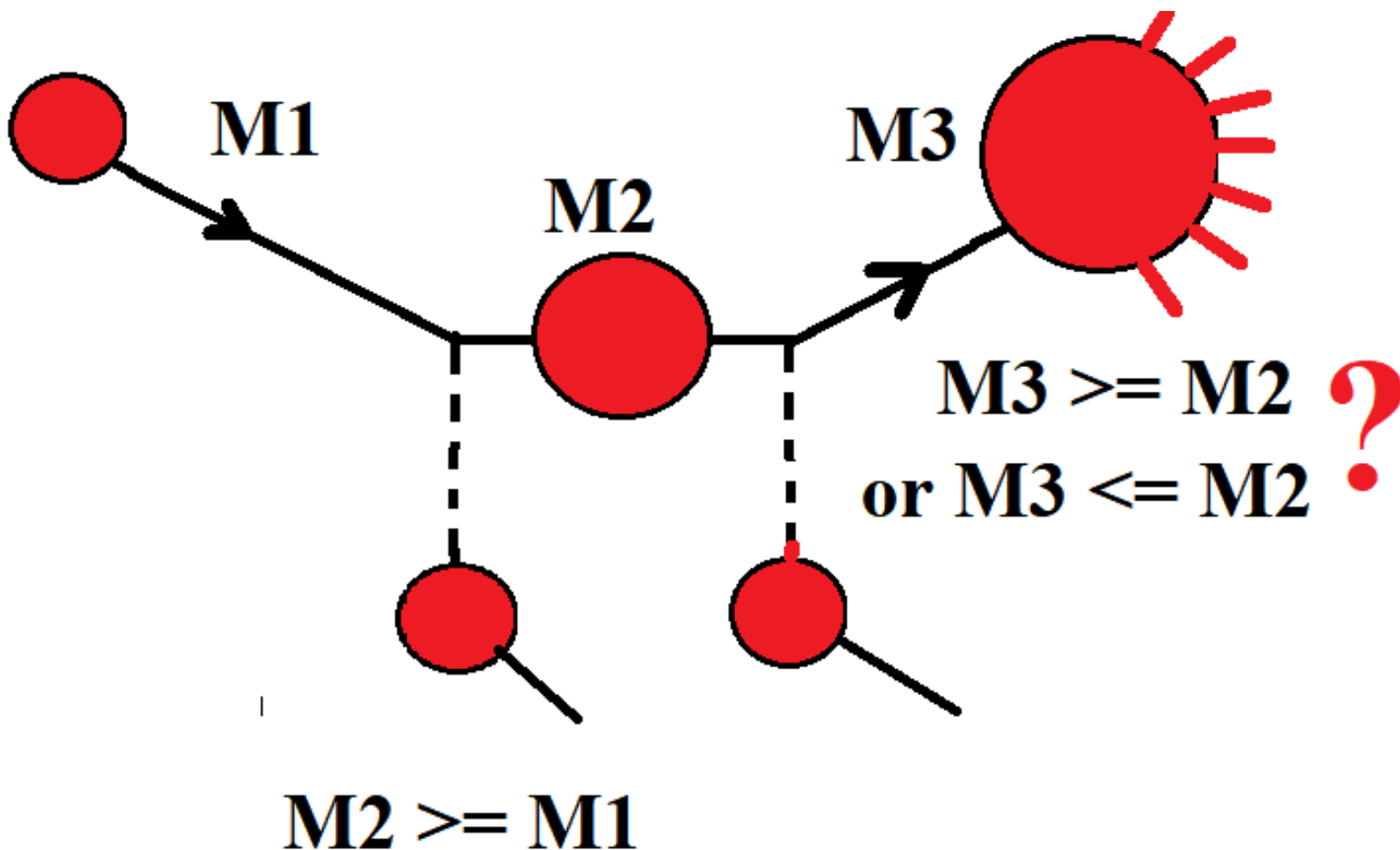


**Special parameterizations of the diffraction cross sections are implemented in the HIJING and FTF models.**



Energy dependence of the cross section of single one-vertex diffraction in pp interactions. Solid line is FTF model approximation. Dashed line is FTF model calculations with accounting of experimental restrictions on masses of produced systems -  $M, M^2/s \leq 0.05$  and  $M \geq 1.5 \text{ GeV}$ . Points are experimental data gathered in [22], see there the exact references.

# hA and AA interactions?



**36 years old question!**

**Now,  $M3 \Rightarrow M2$  !**