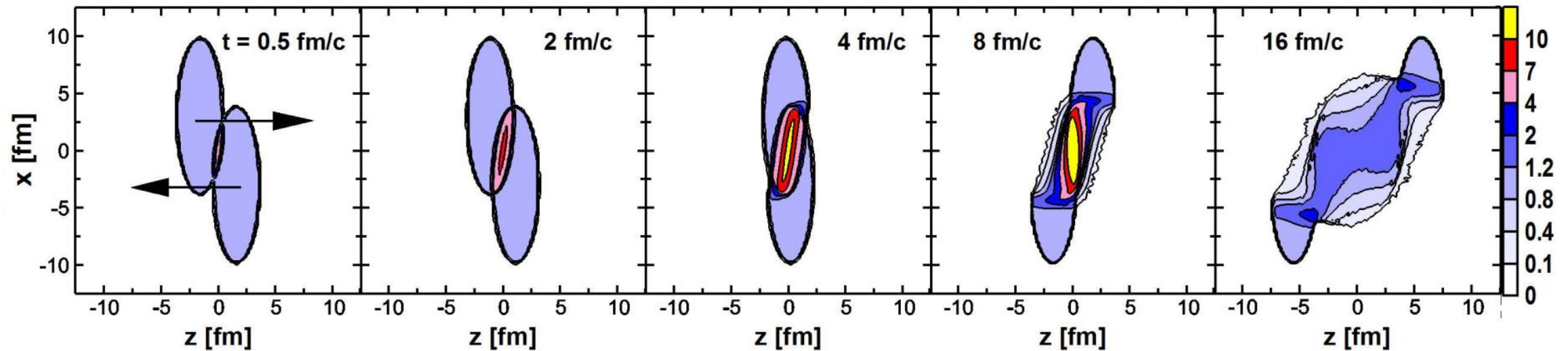


# Light-nuclei production in heavy-ion collisions at NICA energies in generator THESEUS based on 3-fluid dynamical model

Marina Kozhevnikova (VBLHEP, JINR)

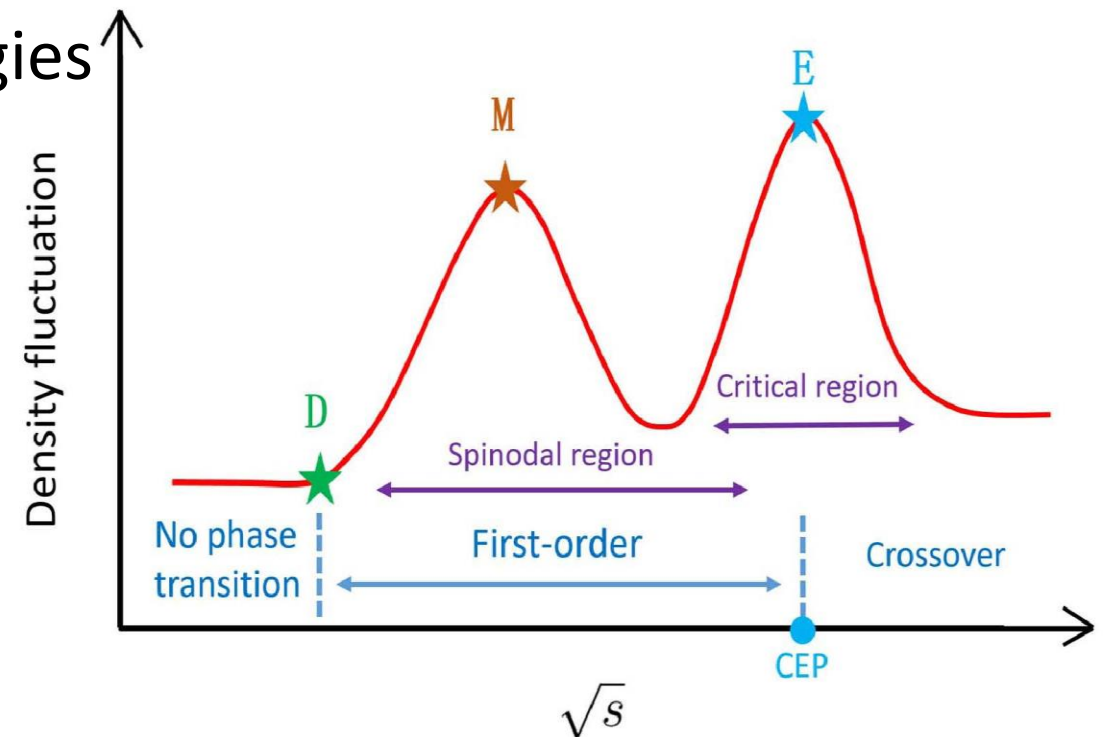
In collaboration with Yu. B. Ivanov



# Light nuclei in heavy-ion collisions

## Why are they interesting?

- ❖ Abundant production at NICA and FAIR energies
- ❖ Very scarce data at NICA and FAIR energies
- ❖ Signal of spinodal instability
- ❖ Signal of critical endpoint (CEP)
- ❖ Medium effects



Kai-Jia Sun, et al., PLB 781 (2018) 499

# 3FD model

**Target-like fluid:**  $\partial_\mu J_t^\mu = 0$        $\partial_\mu T_t^{\mu\nu} = -F_{tp}^\nu + F_{ft}^\nu$   
 Leading particles carry bar. charge      exchange/emission

**Projectile-like fluid:**  $\partial_\mu J_p^\mu = 0$ ,       $\partial_\mu T_p^{\mu\nu} = -F_{pt}^\nu + F_{fp}^\nu$

**Fireball fluid:**  $J_f^\mu = 0$ ,       $\partial_\mu T_f^{\mu\nu} = F_{pt}^\nu + F_{tp}^\nu - F_{fp}^\nu - F_{ft}^\nu$   
 Baryon-free fluid      Source term      Exchange  
 The **source term** is delayed due to a formation time  $\tau$

**Total energy-momentum conservation:**

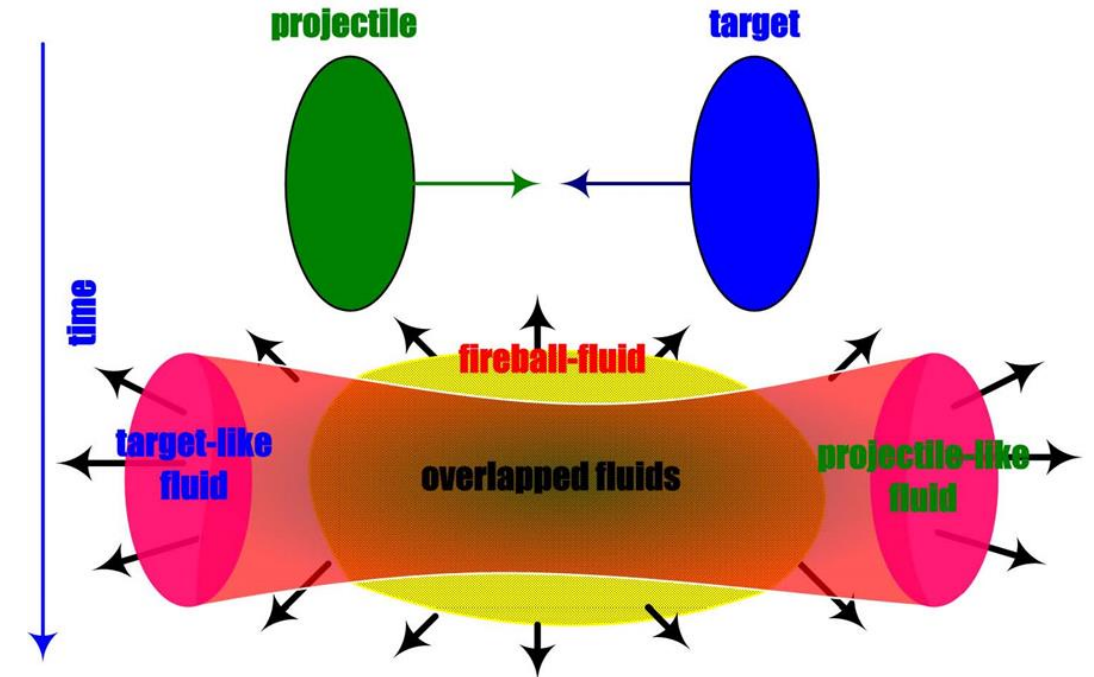
$$\partial_\mu (T_p^{\mu\nu} + T_t^{\mu\nu} + T_f^{\mu\nu}) = 0$$

## Physical Input:

- ▶ Equation of State
- ▶ Friction
- ▶ Freeze-out energy density  $\varepsilon_{\text{frz}} = 0.4 \text{ GeV/fm}^3$



**3FD:** Yu.B. Ivanov, V.N. Russkikh, V.D. Toneev,  
 PHYSICAL REVIEW C 73, 044904 (2006)



## EoS:

- ▶ hadronic EoS (no phase transition)
- ▶ hadronic+QGP EoS with 1st-order PT
- ▶ hadronic+QGP EoS with crossover

**EoS:** A. Khvorostukhin, V.V. Skokov, V.D. Toneev, K. Redlich,  
 EPJ C48, 531 (2006)

# THESEUS event generator and 3FD

## 3FD:

- ❖ The output = Lagrangian test particles (i.e. fluid droplets) for each fluid  $\alpha$  (= p, t or f).
- ❖ Fluid droplet = element of freeze-out surface
- ❖ Observables = integration of hadron distribution functions over freeze-out surface

This is inconvenient for application of experimental acceptance

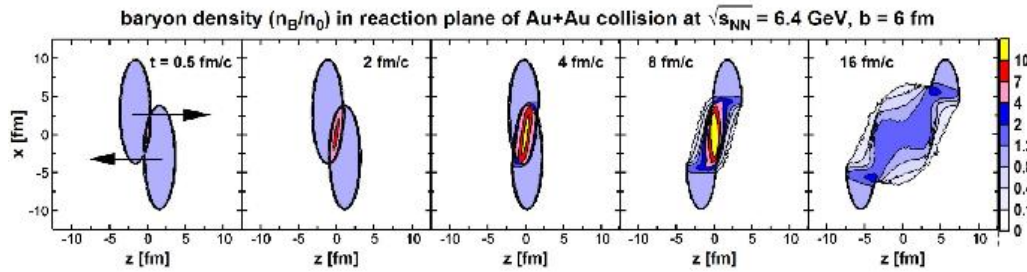
## THESEUS:

- ❖ In 2016 the THESEUS event generator was introduced (Three-fluid Hydrodynamics-based Event Simulator Extended by UrQMD (Ultra-relativistic Quantum Molecular Dynamics) final State interactions).

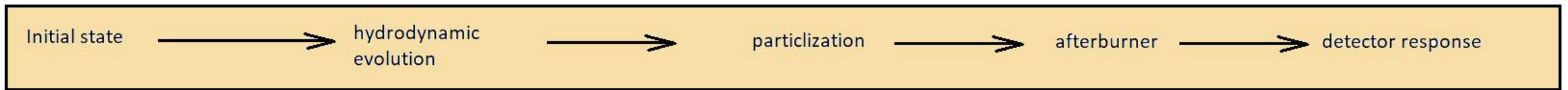
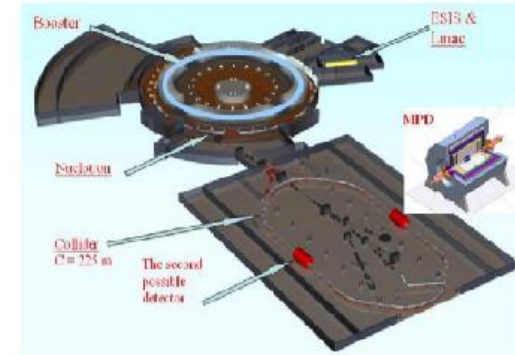
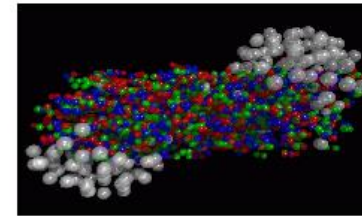
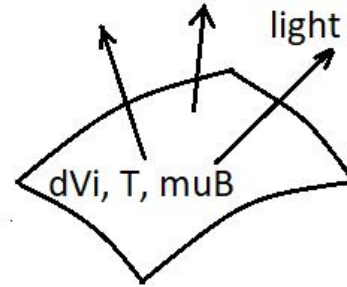
(3FD+Particlization+UrQMD): P. Batyuk et al., PHYSICAL REVIEW C 94, 044917 (2016)

- ❖ **THESEUS = 3FD + Monte Carlo hadron sampling + afterburner via UrQMD**
- ❖ THESEUS presents the 3FD output in terms of a set of observed particles.

# Hydrodynamic modelling of nuclear collisions for NICA / FAIR



hadrons  $\{x, y, z, E, p_x, p_y, p_z, \text{etc.}\}$



3-fluid hydrodynamical model  
(Y.Ivanov et al.)



THESEUS generator

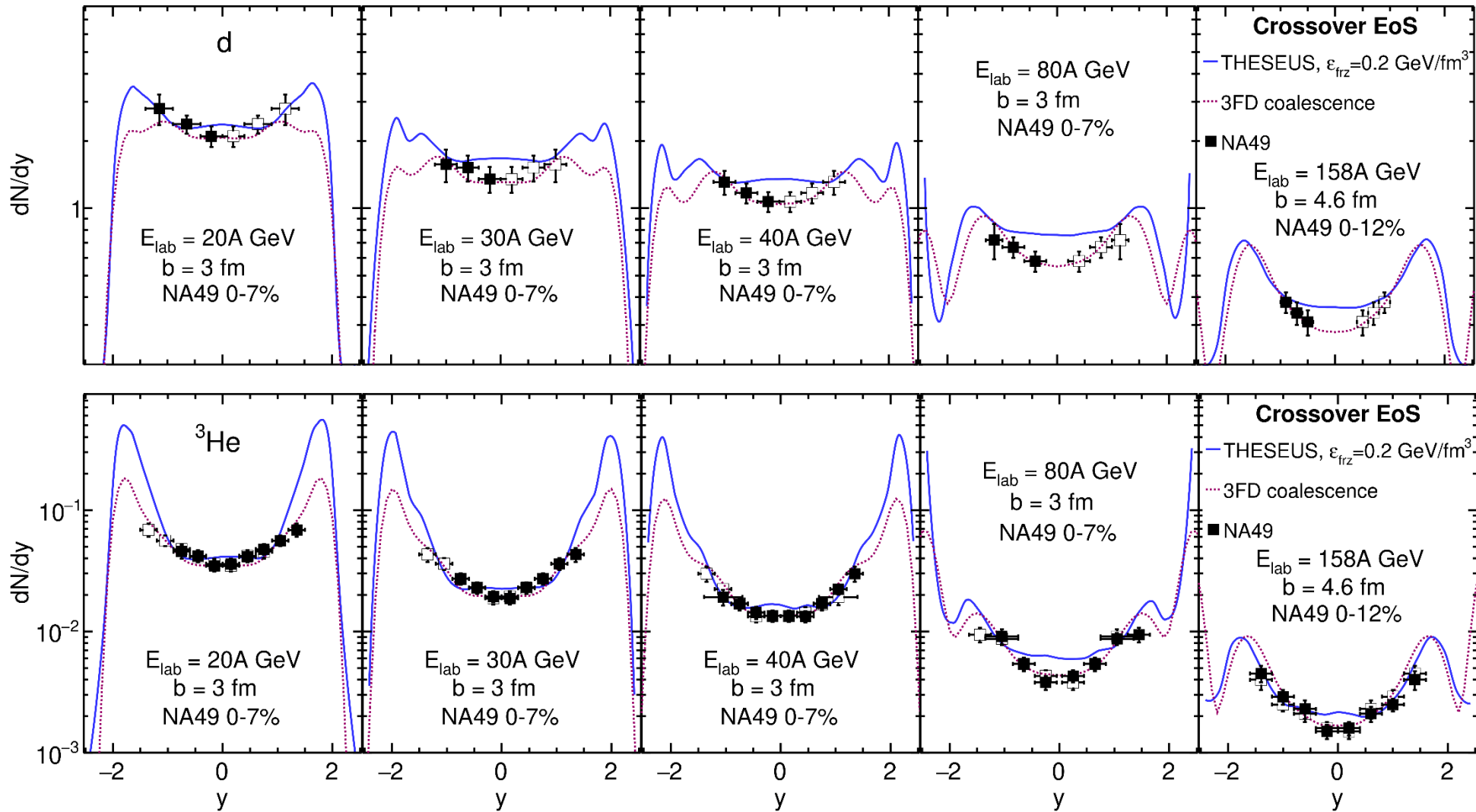


(optionally) UrQMD, etc.  
(Iu. Karpenko, H.Elfner)



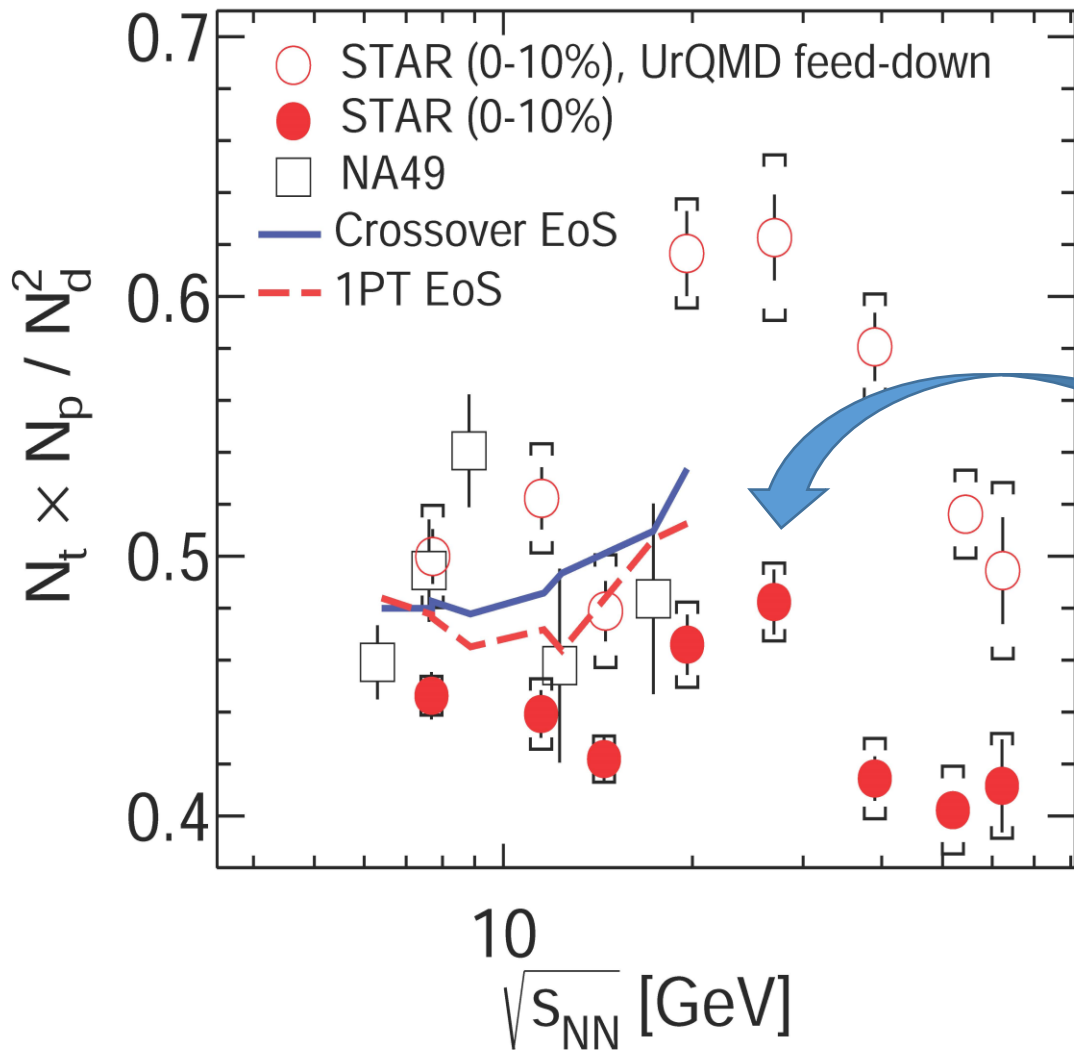
GEANT, MPD, BM@N  
(O.Rogachevsky,  
P.Batuyk, S.Merts et al.)

# THESEUS-v2: rapidity distributions, $\varepsilon_{\text{frz}} = 0.2 \text{ GeV}/\text{fm}^3$ .



**Puzzle:** reproduction of the  $^3\text{He}$  data is better than that of deuterons, in spite of that  $^3\text{He}$  heavier.

# $N(t) \times N(p) / N^2(d)$ ratio



M. Kozhevnikova, Yu. B. Ivanov, PRC 107, 024903 (2023)

**CEP? Spinodal instability?**

THESEUS models growth to energies of 20–30 GeV, although there is neither CEP nor spinodal instability?

Accurate subtraction of weak-decays feed-down from proton yield is important

# Directed flow $v_1(y)$

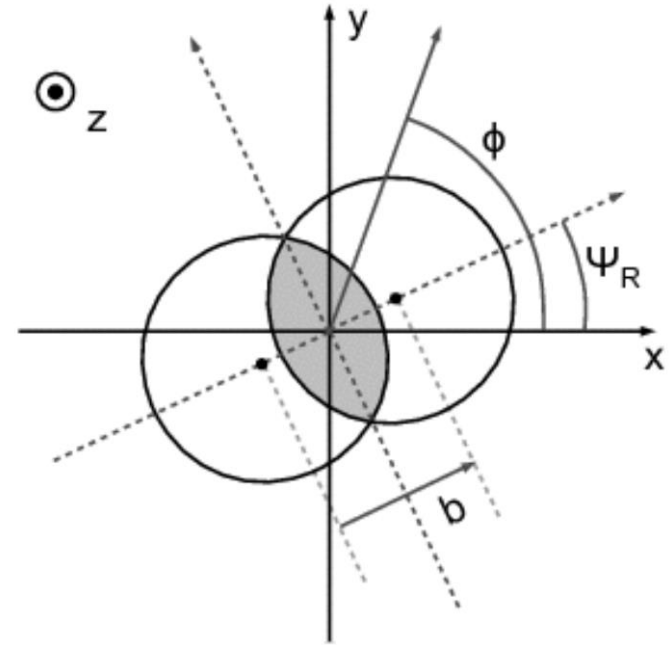
The single particle distribution function:

$$E \frac{d^3 N}{d^3 p} = \frac{1}{2\pi} \frac{d^2 N}{p_T dp_T dy} \left( 1 + \sum_{n=1}^{\infty} 2v_n \cos(n(\phi - \Psi_{RP})) \right)$$

The first coefficient of Fourier expansion, i.e. **directed flow**:

$$v_1^{(a)}(y) = \frac{\int d^2 p_T (p_x/p_T) E dN_a/d^3 p}{\int d^2 p_T E dN_a/d^3 p}$$

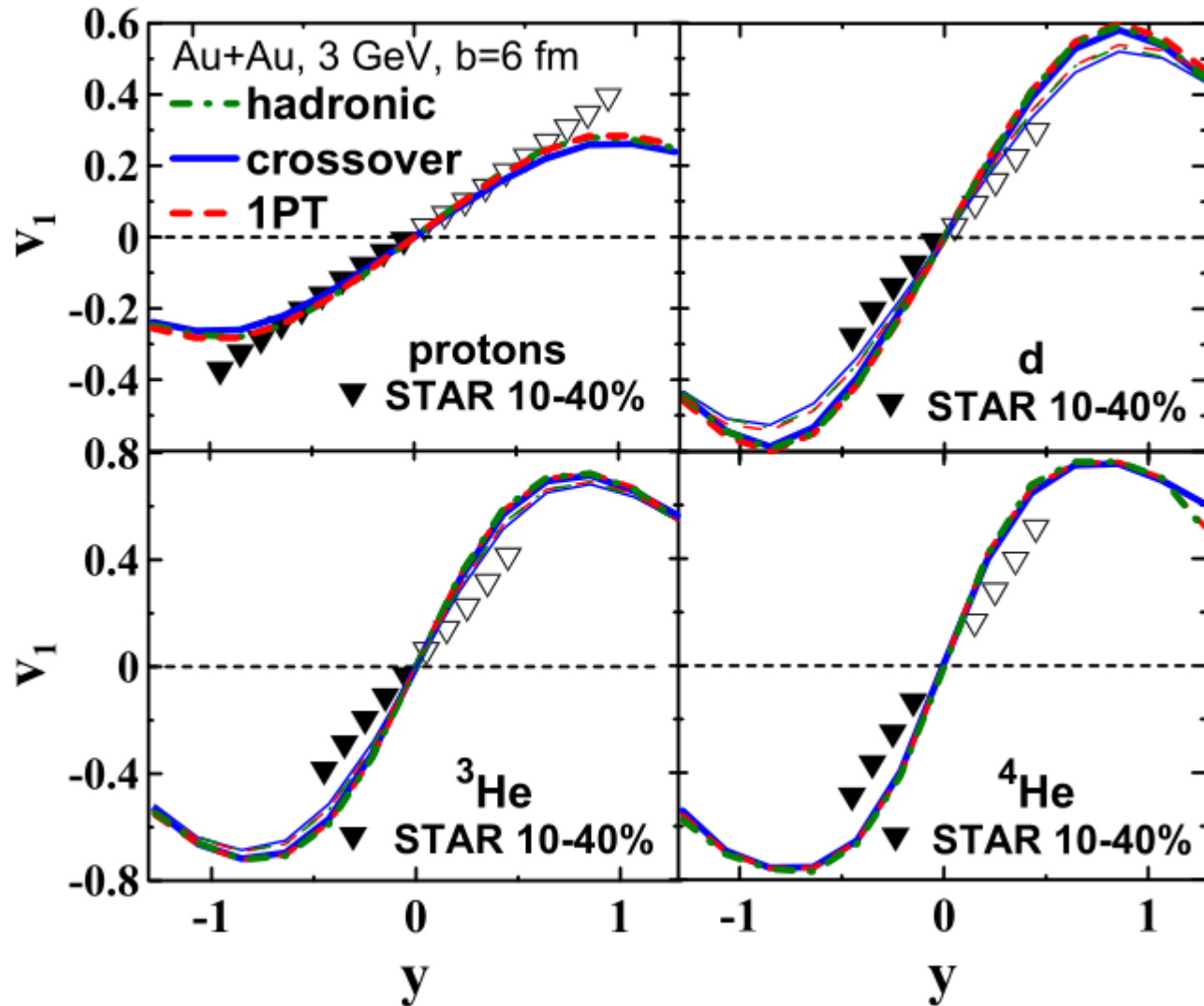
$$v_1 = \langle \cos \phi \rangle, \text{ where } \phi - \text{azimuthal angle.}$$



**In THESEUS:**  $v_1(y)$  is calculated in terms of sums over hadrons rather than integrals over momenta.



# Preliminary directed flow $v_1(y)$ : protons and light nuclei



**Fig.:** Directed flow of **protons** and **light nuclei** as function of rapidity in semicentral ( $b = 6$  fm) Au+Au collisions.  
Thin lines – **without decays of  $\text{He}4^*$** .

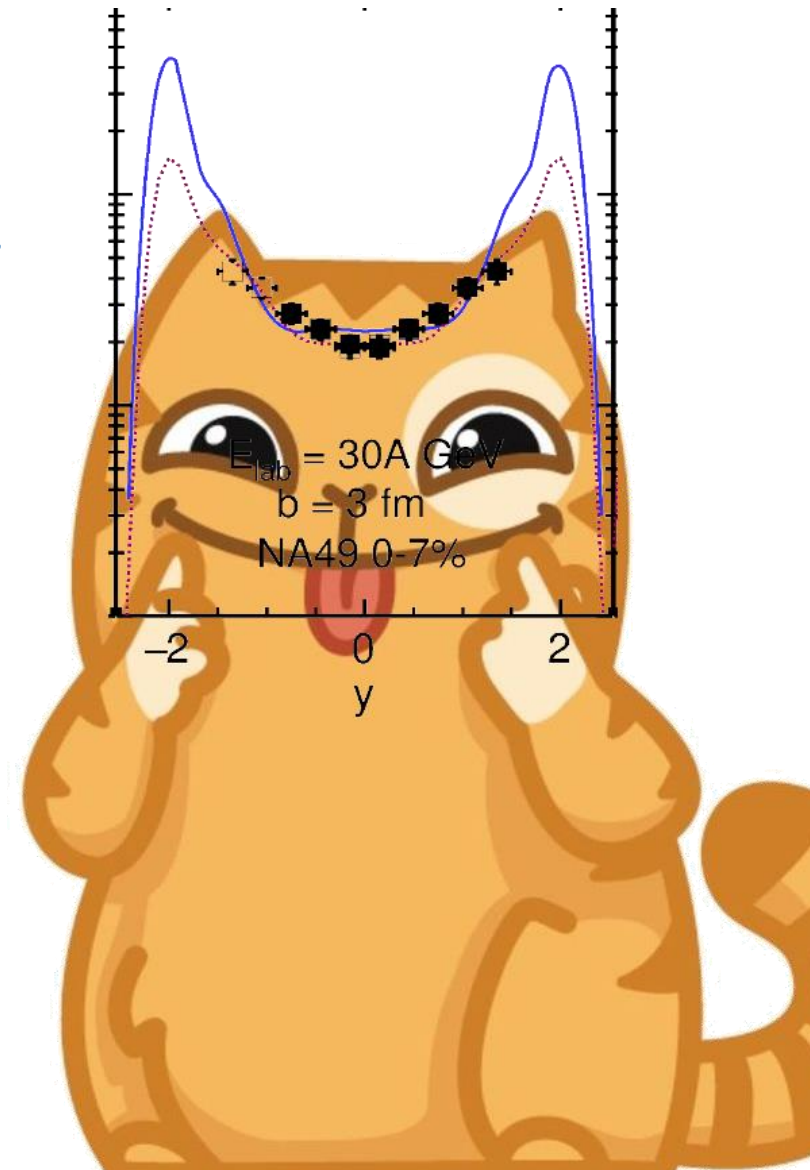
# Summary

- ▶ The thermodynamical approach approximately reproduces data on light nuclei with a single parameter,  $\varepsilon_{\text{frz}} = 0.2 \text{ GeV/fm}^3$ .
- ▶ The functional dependencies (on  $y$ ,  $v_1$ , mass of light nuclei and others) qualitatively are reproduced.
- ▶ Medium effects are currently studied

# Acknowledgments

- ▶ We are grateful to **David Blaschke** for convincing us to apply the thermodynamic approach to modeling the light-nuclei production in heavy-ion collisions.
- ▶ We are especially grateful to **Iu. Karpenko** for the expertise, interesting suggestions and discussions.

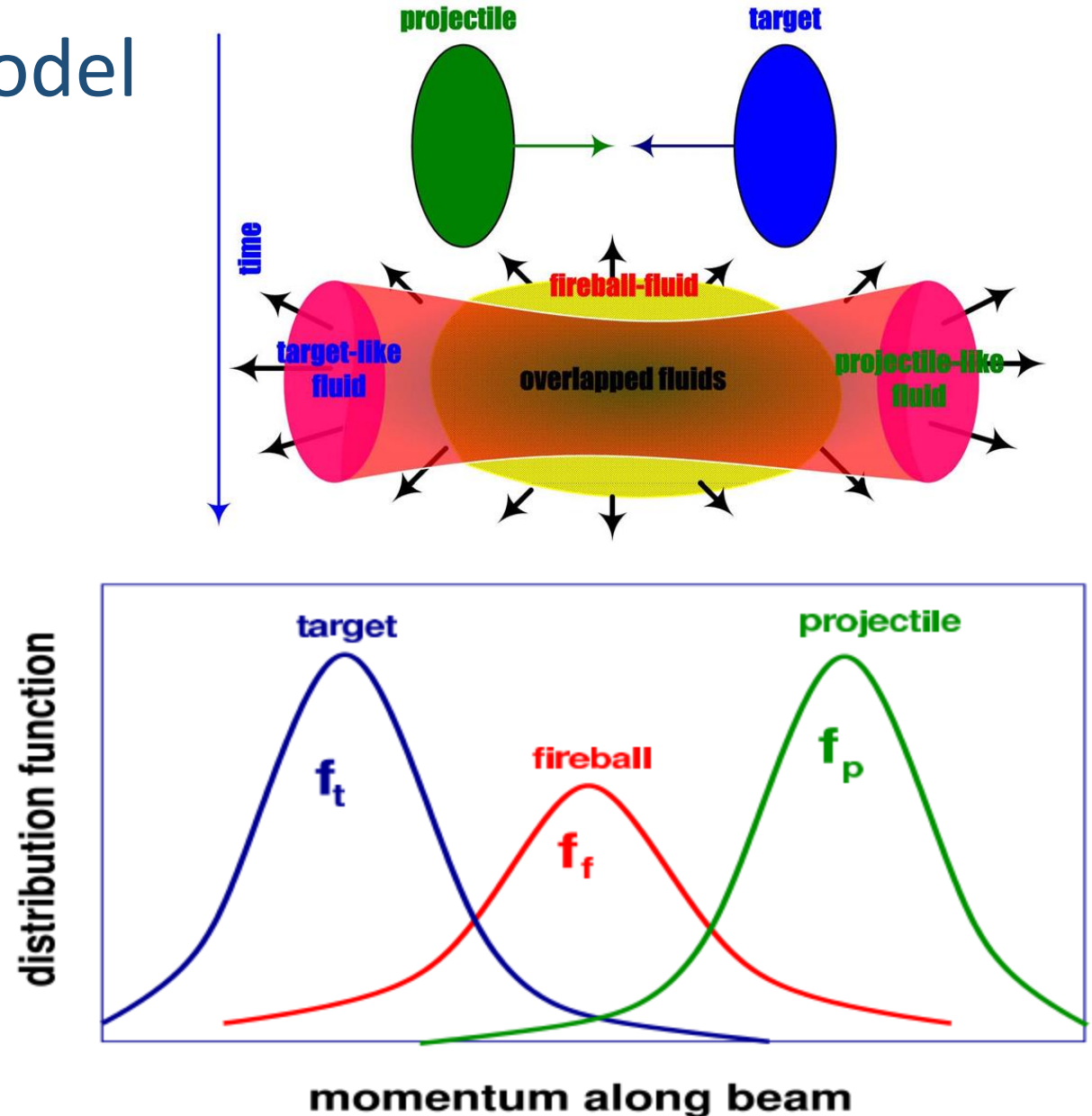
Thank you  
for your attention!



# Three-fluid dynamics (3FD) model

The 3FD approximation simulate the early, nonequilibrium stage of the strongly-interacting matter:

- ▶ baryon-rich fluids: nucleons of the projectile (p) and the target (t) nuclei;
- ▶ fireball (f) fluid: newly produced particles which dominantly populate the midrapidity region.



# THESEUS-v2: updates

No light-nuclei in 3FD originally.

The main update: To include light nuclei in thermodynamics we recalculate the baryon chemical potential taking into account light nuclei production, proceeding from the local baryon number conservation:

$$\begin{aligned}
 & n_{\text{primordial}} N(x; \mu_B, T) + \sum_{\text{hadrons}} n_i(x; \mu_B, \mu_S, T) \\
 = & n_{\text{observable}} N(x; \mu'_B, T) + \sum_{\text{hadrons}} n_i(x; \mu'_B, \mu_S, T) \\
 & + \sum_{\text{nuclei}} n_c(x; \mu'_B, \mu_S, T).
 \end{aligned}$$

The list of light-nuclei species is shown in Table.

Nucleus( $E$ [MeV])	$J$	decay modes, in %
$d$	1	Stable
$t$	1/2	Stable
${}^3\text{He}$	1/2	Stable
${}^4\text{He}$	0	Stable
${}^4\text{He}(20.21)$	0	$p = 100$
${}^4\text{He}(21.01)$	0	$n = 24, p = 76$
${}^4\text{He}(21.84)$	2	$n = 37, p = 63$
${}^4\text{He}(23.33)$	2	$n = 47, p = 53$
${}^4\text{He}(23.64)$	1	$n = 45, p = 55$
${}^4\text{He}(24.25)$	1	$n = 47, p = 50, d = 3$
${}^4\text{He}(25.28)$	0	$n = 48, p = 52$
${}^4\text{He}(25.95)$	1	$n = 48, p = 52$
${}^4\text{He}(27.42)$	2	$n = 3, p = 3, d = 94$
${}^4\text{He}(28.31)$	1	$n = 47, p = 48, d = 5$
${}^4\text{He}(28.37)$	1	$n = 2, p = 2, d = 96$
${}^4\text{He}(28.39)$	2	$n = 0.2, p = 0.2, d = 99.6$
${}^4\text{He}(28.64)$	0	$d = 100$
${}^4\text{He}(28.67)$	2	$d = 100$
${}^4\text{He}(29.89)$	2	$n = 0.4, p = 0.4, d = 99.2$

**Table:** Stable light nuclei and low-lying resonances of the  ${}^4\text{He}$  system (from BNL properties of nuclides).

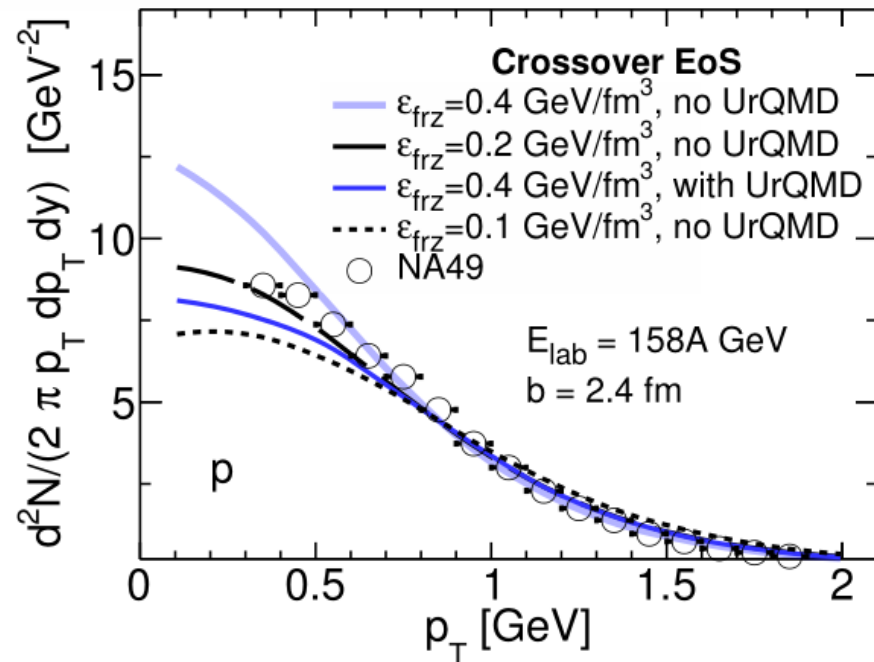
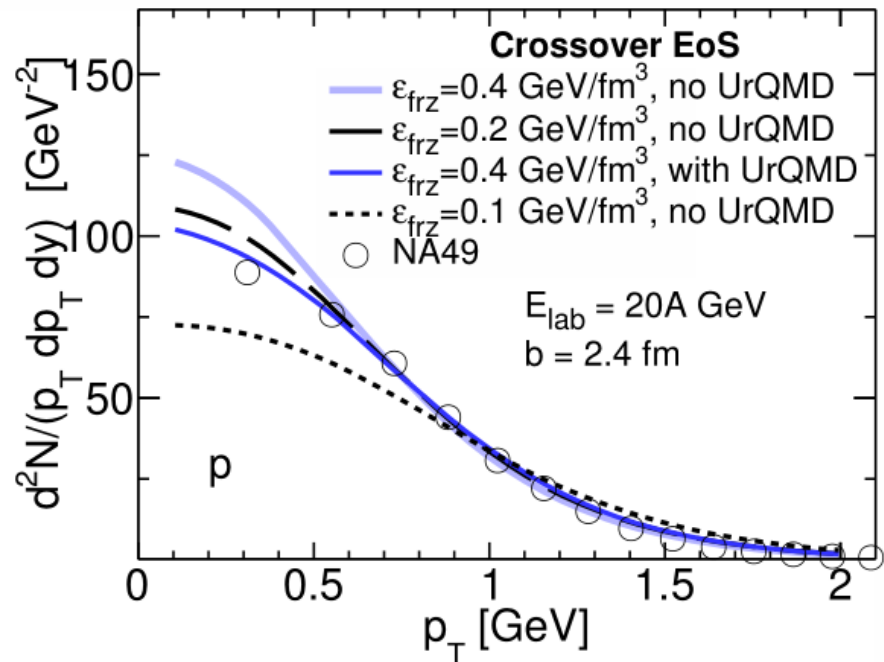
# THESEUS-v2: afterburner for light nuclei

There is no UrQMD afterburner stage for light nuclei, so we imitate the afterburner by later freeze-out for light nuclei.

- ▶ To choose suitable late freeze-out we fit protons by means of the late freeze-out:

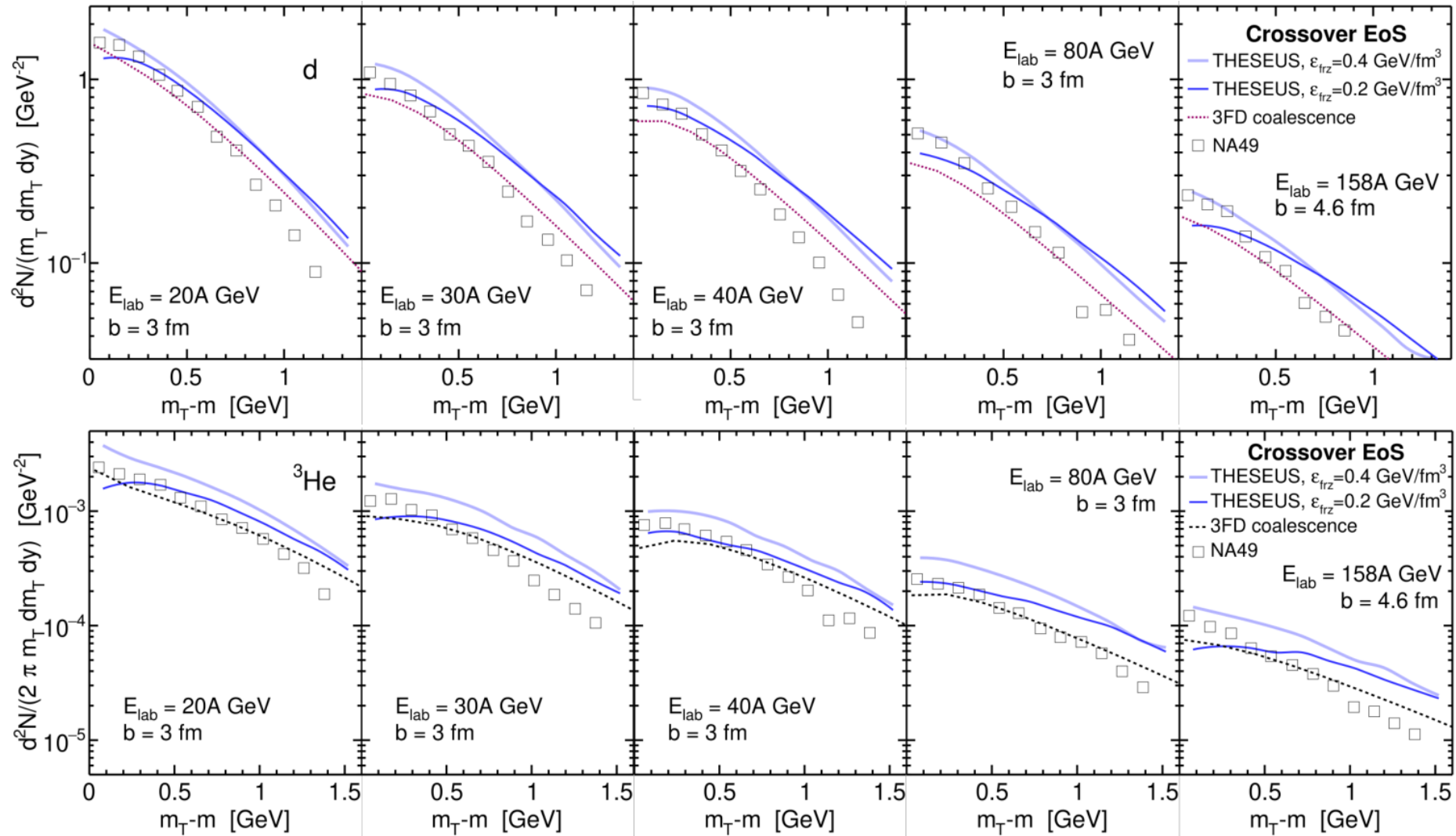
$$\varepsilon_{\text{frz}} = 0.2 \text{ GeV/fm}^3.$$

- ▶ We choose protons because they are closely related to the light nuclei.



**Fig.:** Transverse-momentum spectra of protons in central Au+Au collisions.

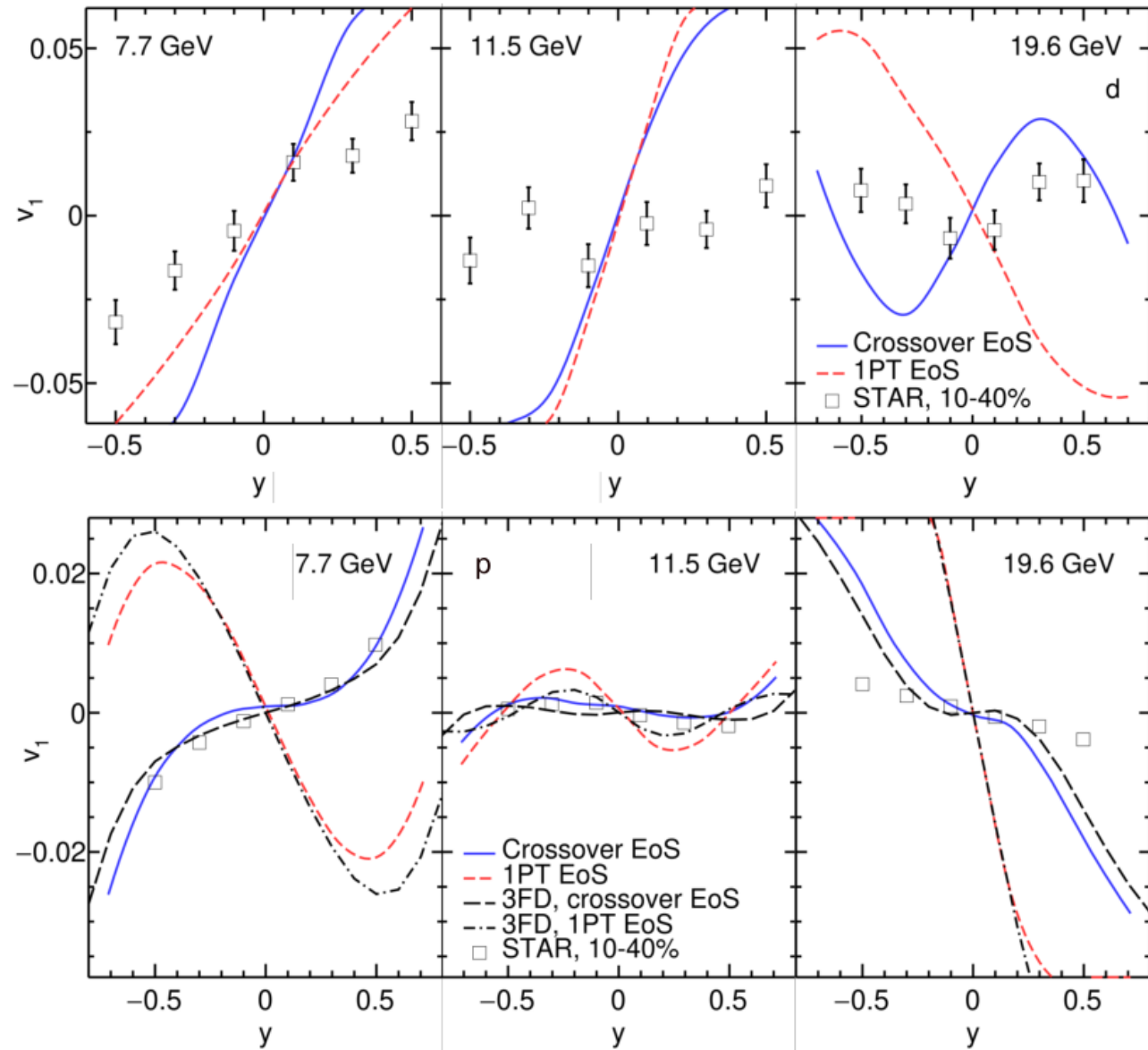
# $m_T$ -spectra: deuterons and Helium 3



The slopes change. The curves become in better agreement with data at low  $m_T$ .

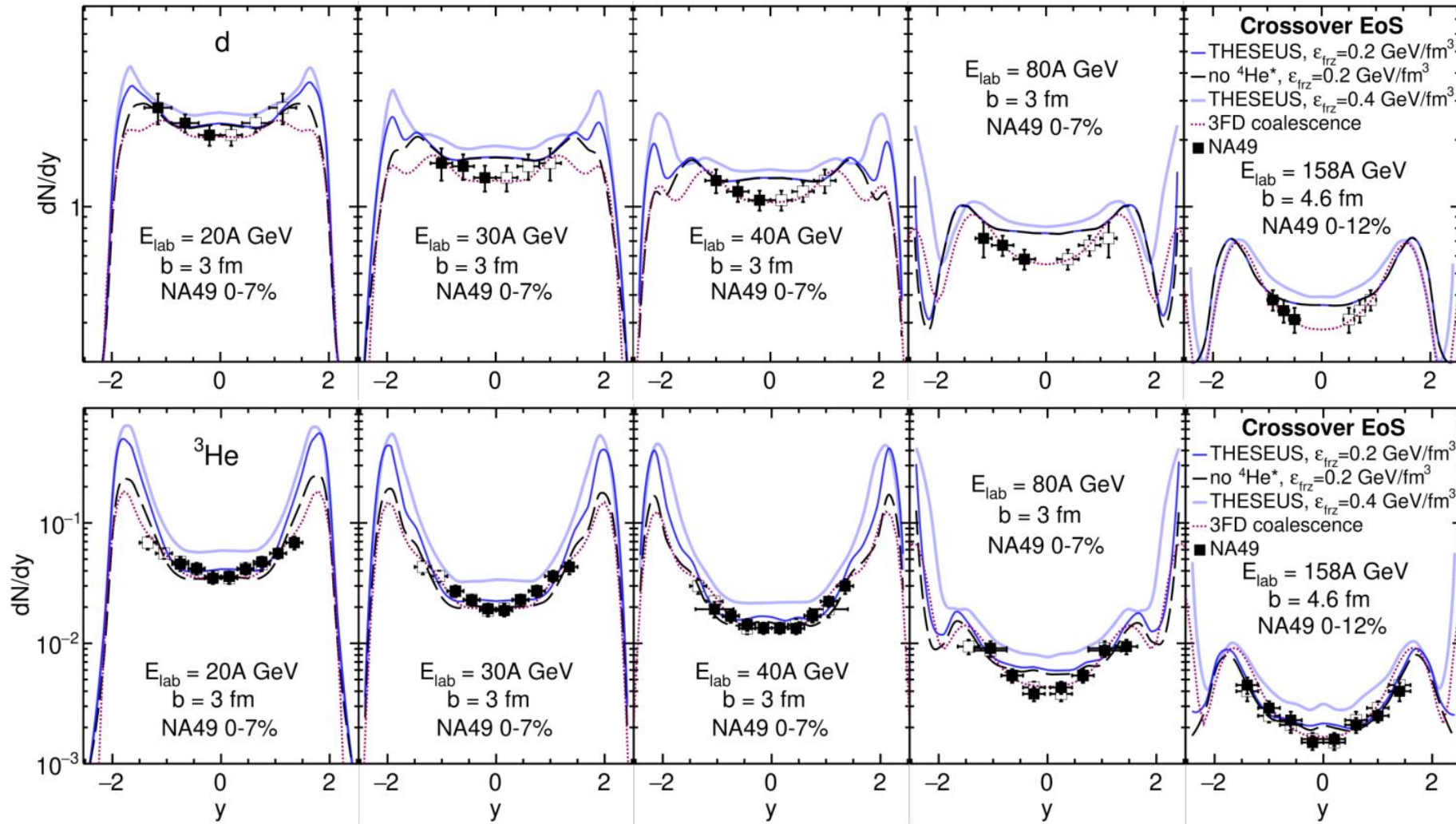


# Directed flow $v_1(y)$ : protons and deuterons



**Fig.:** Directed flow of **deuterons** (upper row of panels) and **protons** (lower row of panels) as function of rapidity in semicentral ( $b = 6$  fm) Au+Au collisions.

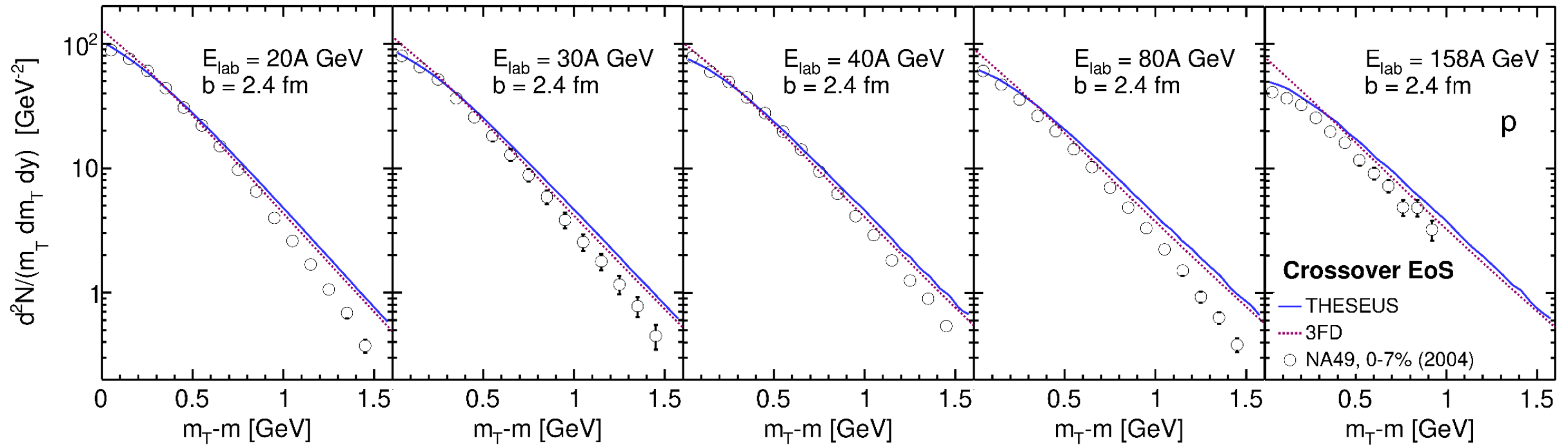
# THESEUS-v2: rapidity distributions, $\varepsilon_{\text{frz}} = 0.2 \text{ GeV}/\text{fm}^3$ .



**Resonances of  $^4\text{He}$  are unimportant in midrapidity at the considered collision energies.**

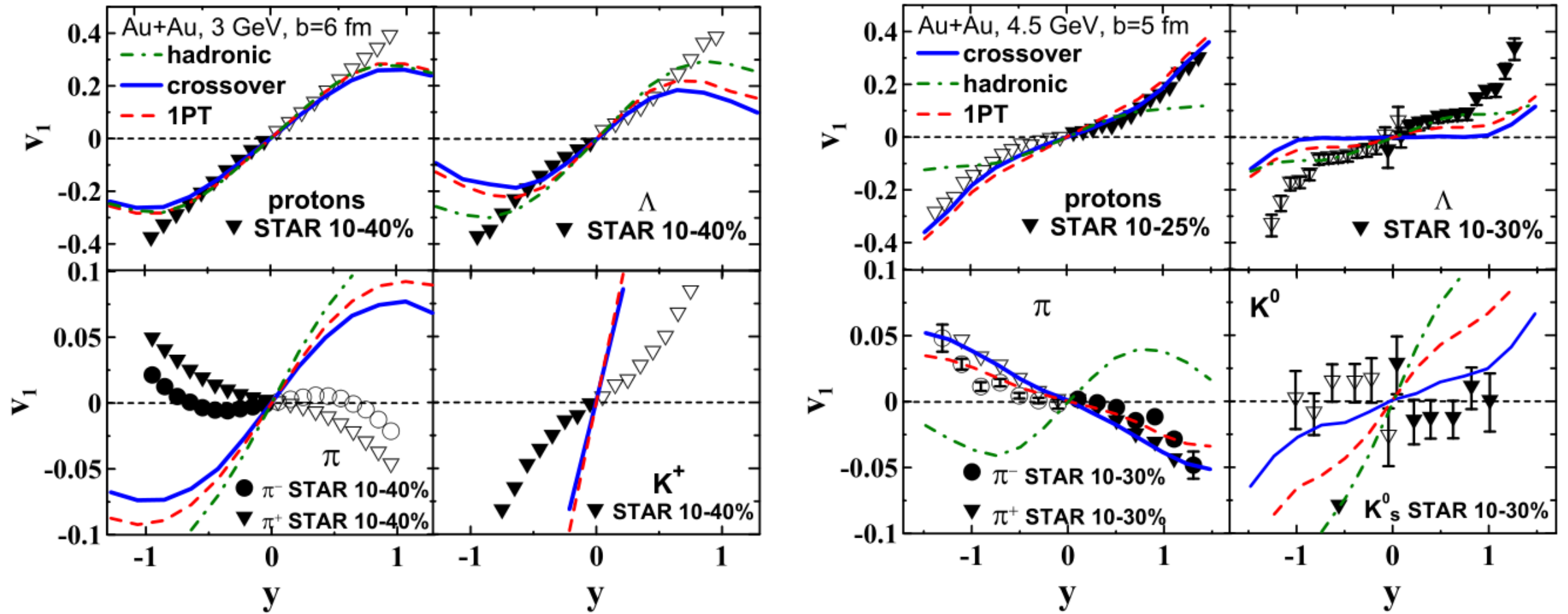
**Puzzle:** reproduction of the  $^3\text{He}$  data is better than that of deuterons, in spite of that  $^3\text{He}$  heavier.

# THESEUS-v2: $m_T$ -spectra of protons.



**$m_T$ -spectra of protons:** thermodynamics works good with soft particles and with hard particles not perfect.

# Directed flow $v_1(y)$ : hadrons



**Fig.:** Directed as function of different hadrons as function of rapidity in semicentral ( $b = 6$  fm) Au+Au collisions.

# Nearest plans

- ▶ Study of  $v_1$  puzzle for deuterons:  $p_T$ -differential  $v_1(p_T)$ ;
- ▶ Including medium effects;
- ▶ Predictions for NICA energies;
- ▶ HADES and AGS data;
- ▶ Hyper-(anti)nuclei.