



# Research of neutron transportation through neutron guide tubes and magnetic fields of the UCN source at the pulsed reactor

*Based on master's dissertation*

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Dubna

*Special thanks to*

*A.I.Frank - supervisor*

*G.V.Kulin - consultant*

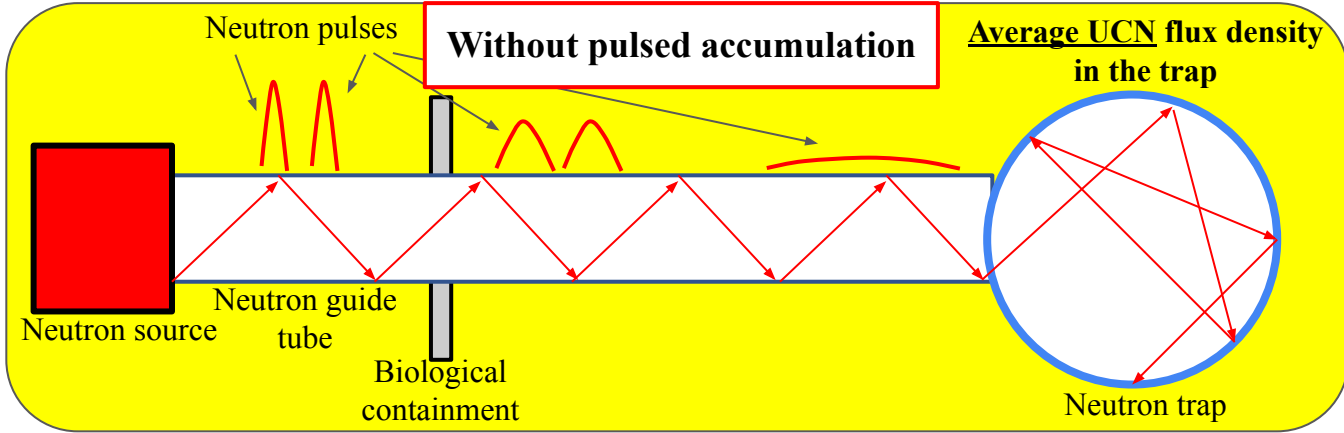
*M.A.Zakharov - consultant*

*A.Y.Nezvanov - reviewer*

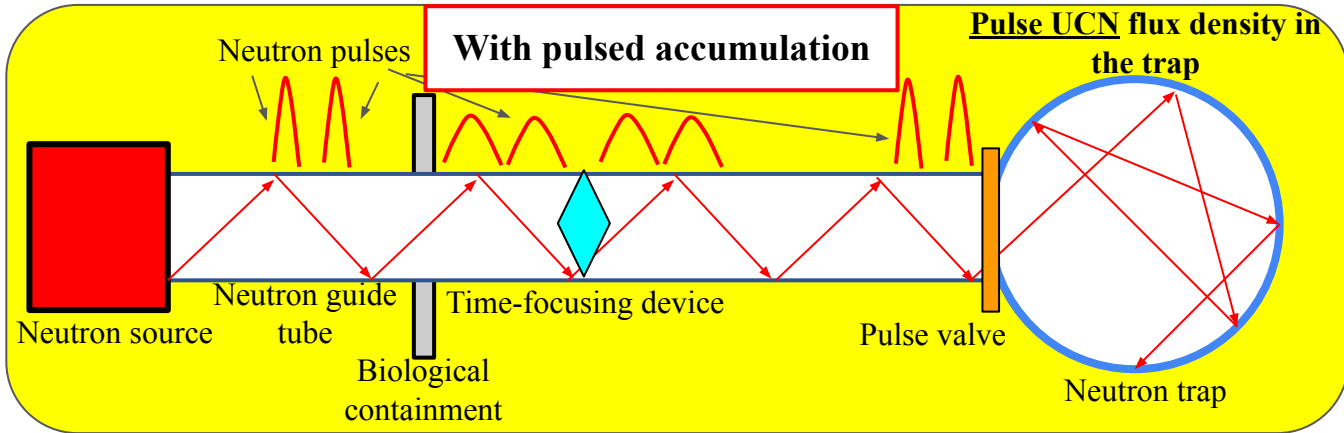
# Motivation

- 1) To introduce you the problem of the UCN source on a pulsed reactor
- 2) To show you my contribution to problem solving

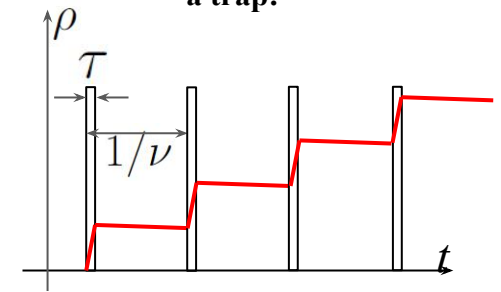
# Concept of UCN Source on pulsed reactor



➡ To experimental installations ➡



Pulsed neutron accumulation in a trap:



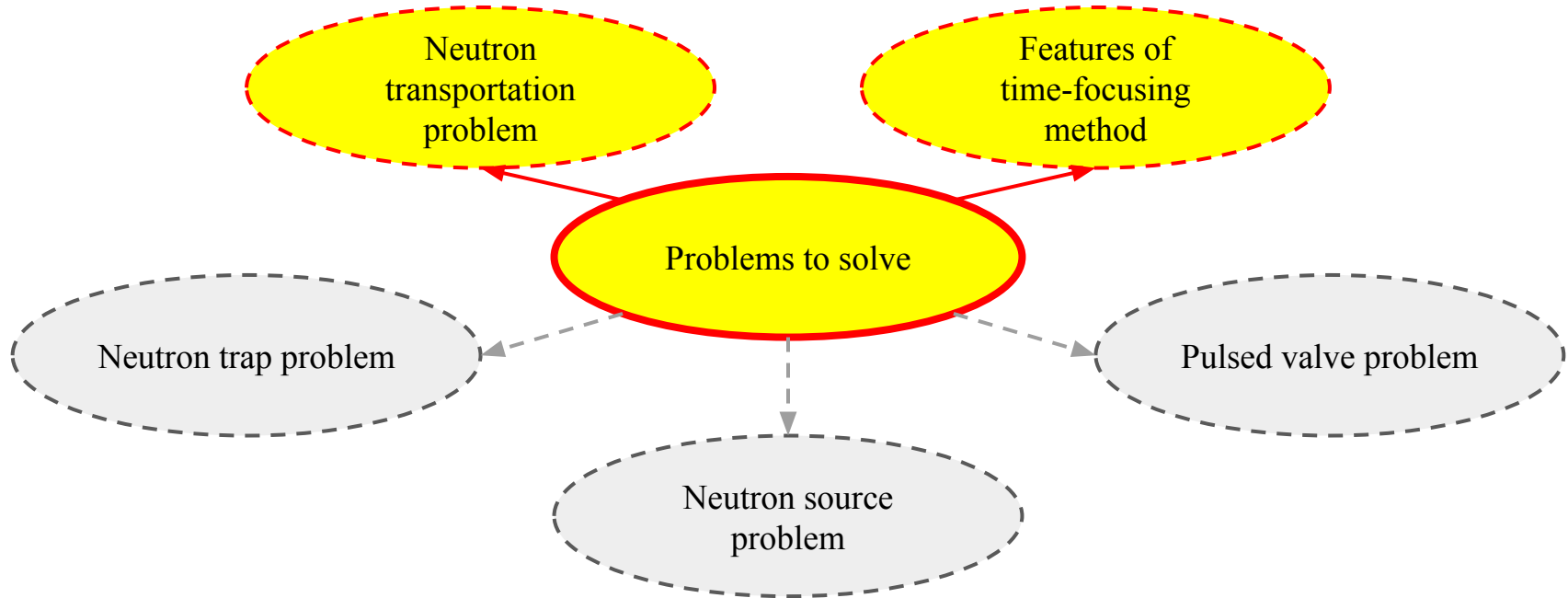
$\rho$  - neutron flux density in a trap  
 $\nu$  - pulse rate  
 $\tau$  - pulse duration

**Pulsed reactor feature:**  
 its **pulse** flux density is greater than **average** flux density

[1] Ф.Л. Шапиро, ЭЧАЯ, 2, 4, 975 (1972).

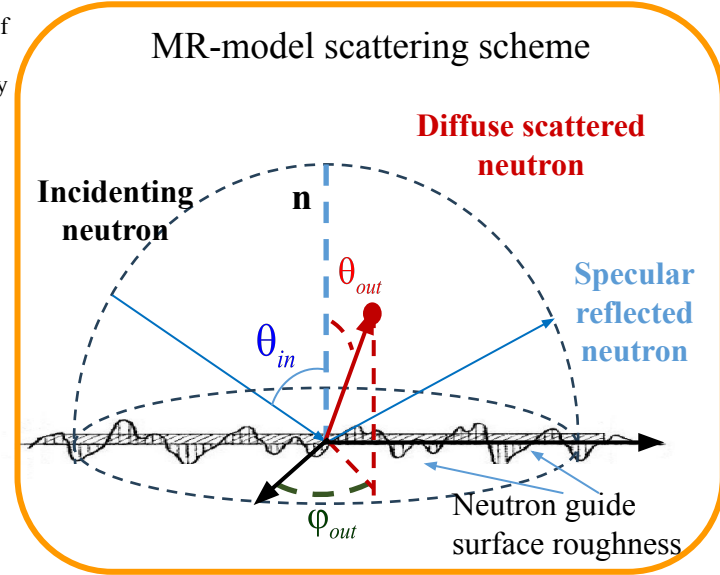
[2] A.I. Frank *et al.*, *Phys. Part. Nuclei* 53, 33 (2022).

# Barriers for pulse accumulation with time-focusing device



# Neutron transportation problem

Mean square amplitude of roughness less than 5 nm for neutrons with Velocity less than 50 m/s



Guide tube defects

Macroscopic waveness

Microscopic roughness

Lead to

- Measurement methodology wasn't found

- Well known measurement methodology (AFM)  
- Well known experimentally proved scattering theory [3] (MR-model)

Non specular changing velocity direction

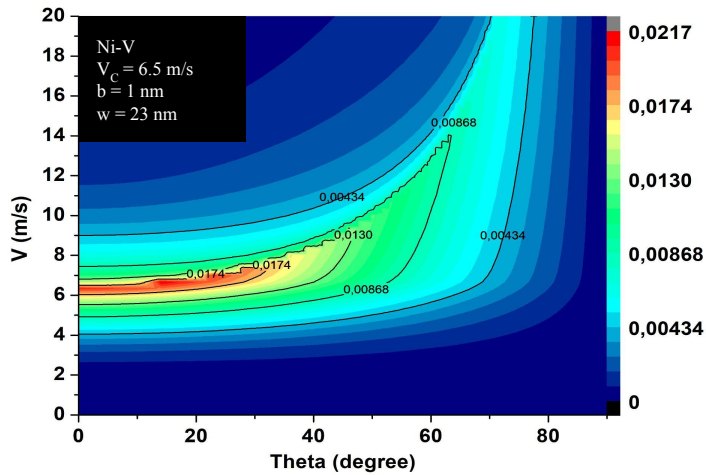
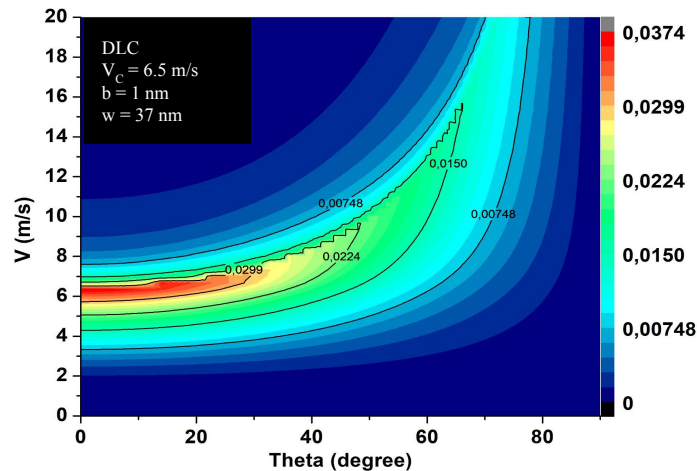
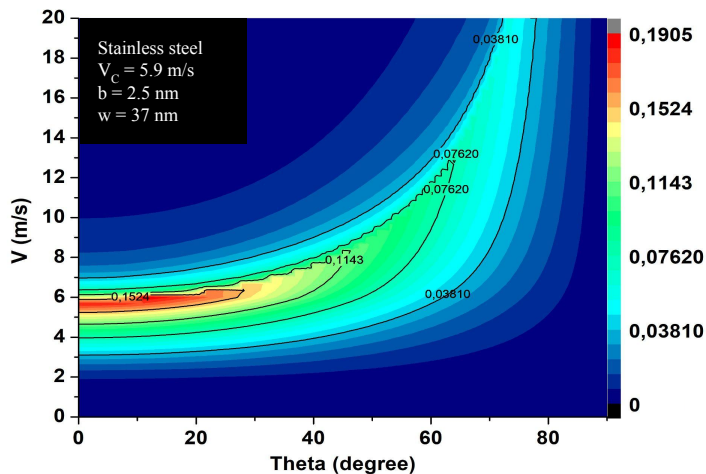
Leads to

Transportation losses

It is necessary to evaluate the transmission of neutron guide tubes at least with roughness

[3] A. Steyerl Effect of surface roughness on the total reflexion and transmission of slow neutrons., Z. Physik, **254**, 169 (1972)

# Probabilities of the diffuse scattering for different materials depending on the angle of incidence and neutron velocity in MR-model

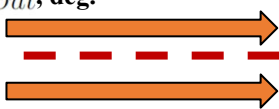
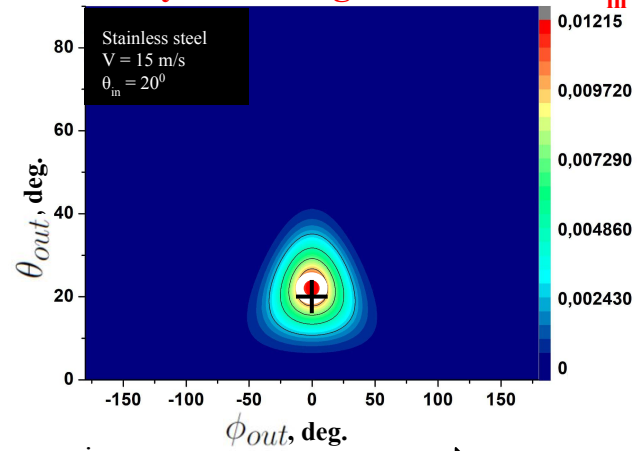
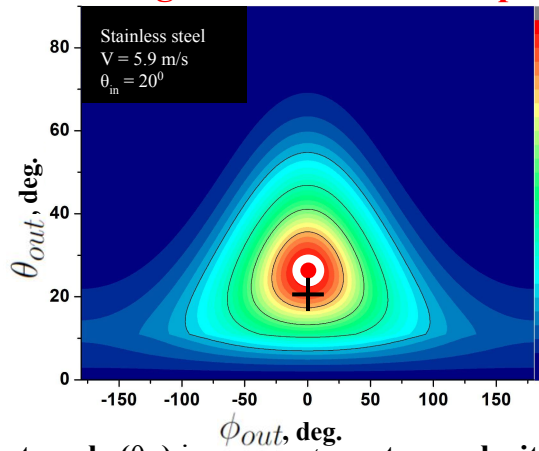
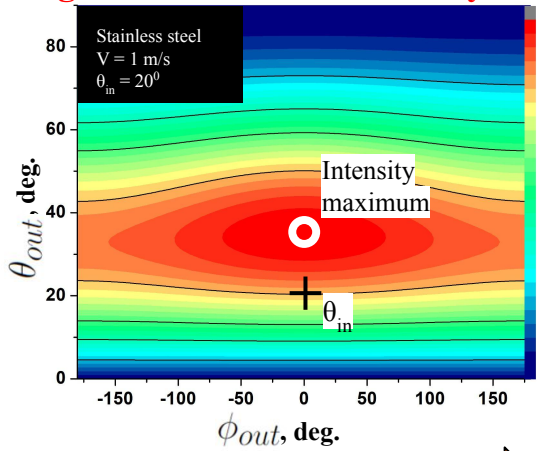


Material	$b$ , nm	$w$ , nm	$V_c$ , m/s
Stainless steel	2.5	37	5.9
DLC	1	37	6.5
Ni-V	1	23	6.5

Material parameters

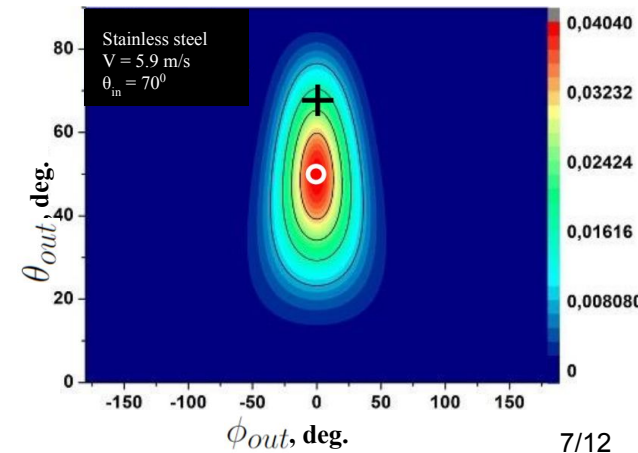
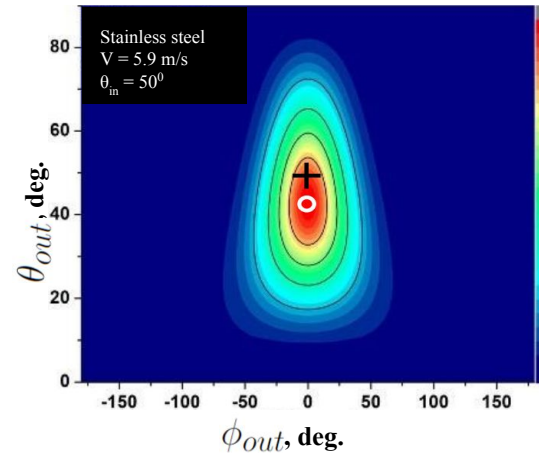
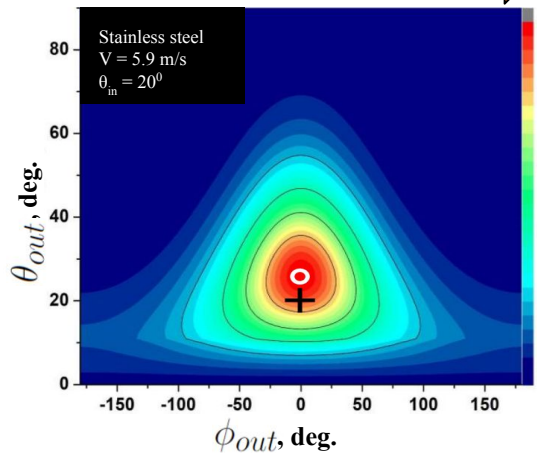
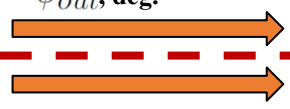
$b$  – mean square roughness amplitude  
 $w$  – correlation length of roughness distribution  
 $V_c$  - material critical velocity

# Angular distribution intensity of neutrons during diffuse reflection depending on velocity $V$ and angle of incidence $\theta_{in}$

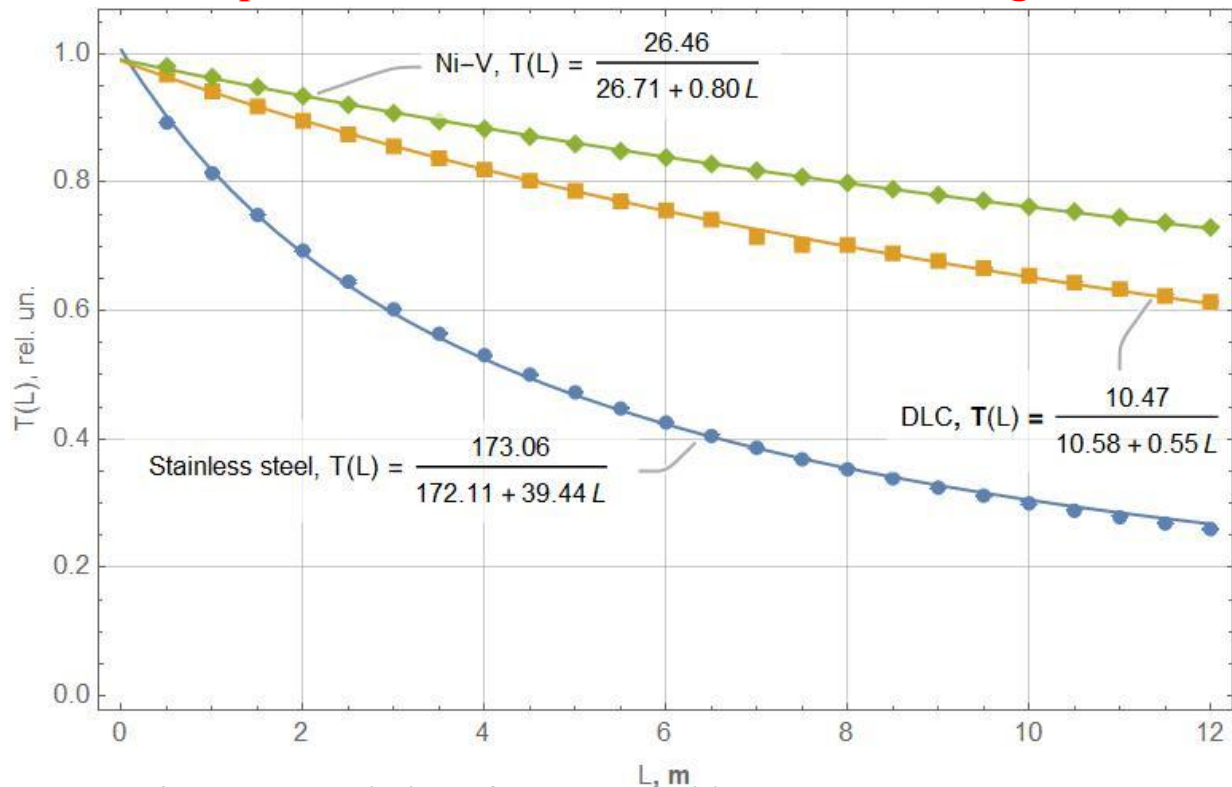


Incident angle ( $\theta_{in}$ ) is *constant*, neutron velocity ( $V$ ) increasing

Incident angle ( $\theta_{in}$ ) increasing, neutron velocity ( $V$ ) is *constant*



# Dependence of the transmission of a neutron guide tube on its length in MR-model



**Starting velocity distribution:**

$$V^{\text{start}} = 15 \text{ m/s}$$

$$V_{xy}^{\text{start}} \in [0; V_c]$$

**Guide tube geometrical parameters:**

Radius = 0.04 m

$L \in [0.5; 12]$  m

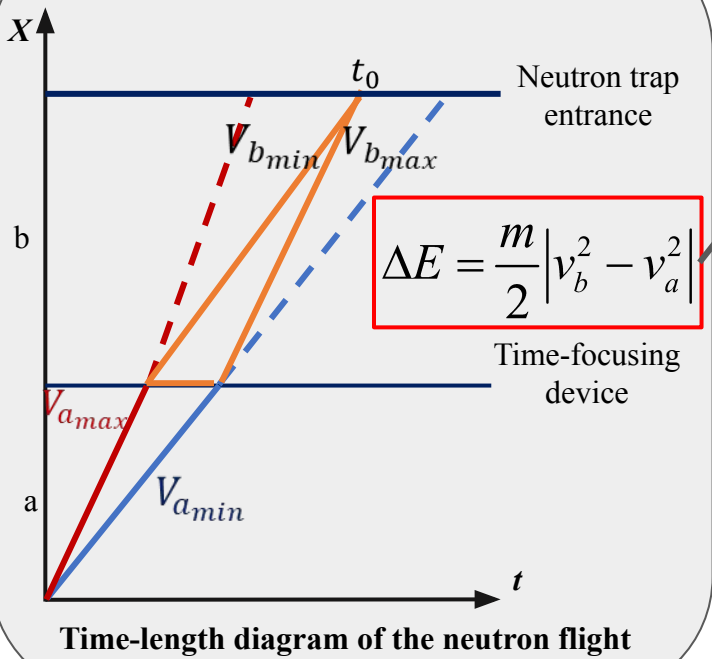
Material	$b, \text{ nm}$	$w, \text{ nm}$	$V_c, \text{ m/s}$
Stainless steel	2.5	37	5.9
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Ni-V	1	23	6.5

$T = \langle N_{\text{end}} \rangle / N_{\text{start}}$  - transmission of a neutron guide,  
 $N_{\text{end}}$  - neutron amount in the end of calculations,  
 $N_{\text{start}}$  - neutron amount in the start of calculation,  
 $L$  - guide tube length.



# Focusing method using an adiabatic spin flipper

## The idea of focusing method [4]



$$U(x, y, z) = \pm \mu |B(x, y, z)|$$

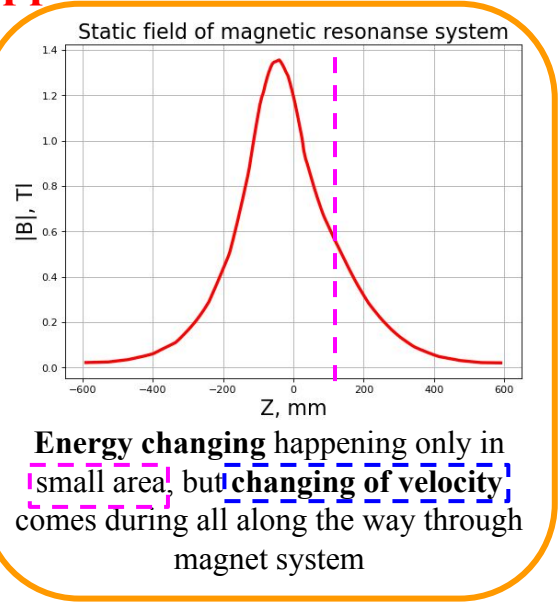
$$\Delta E = \pm 2\mu |B(x, y, z)|$$

$$\vec{F} = \vec{\nabla} U(x, y, z)$$

$\vec{\nabla} \vec{B} = 0$

Besides the longitudinal gradients, there are radial gradients

Increasing of longitudinal velocity spectre wideness



Increasing of the time of flight dispersion

**The idea is proposed:**

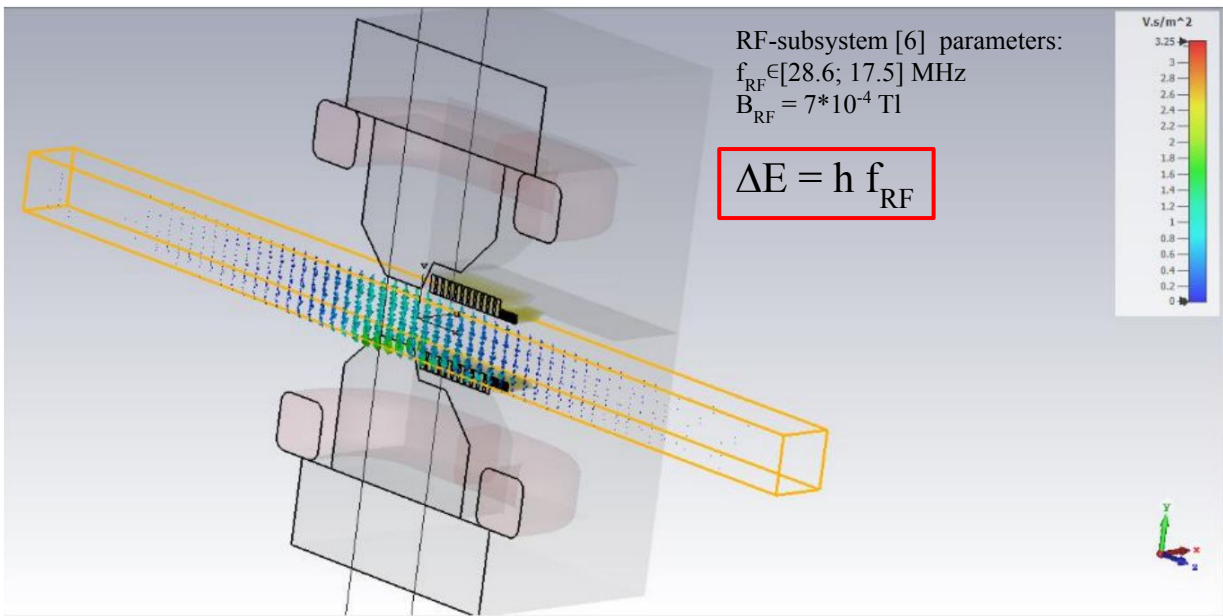
[4] Frank A. I., Gahler R. Time Focusing of Neutrons // April 2000 Physics of Atomic Nuclei 63(4):545-547.

**The method has been experimentally tested:**

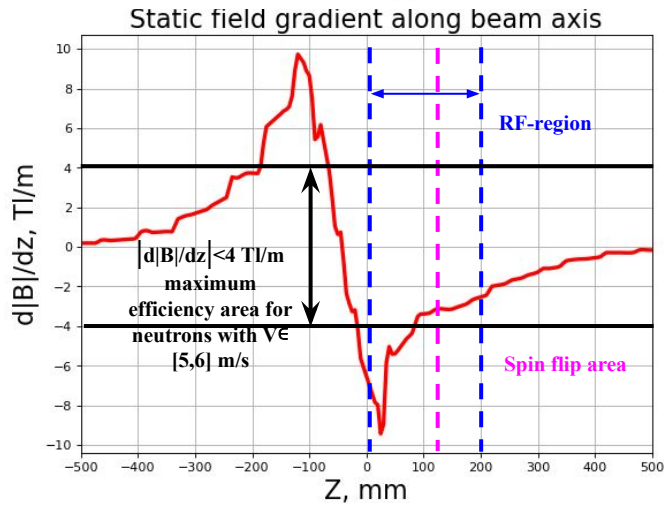
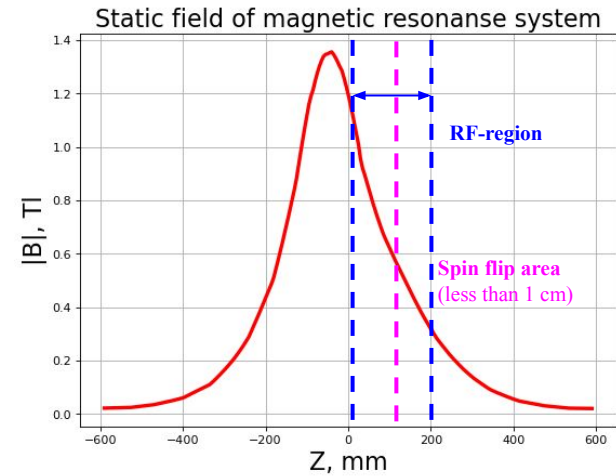
[5] Arimoto Y., Gertenbort P., Imajo S., etl Demonstration of focusing by a neutron accelerator// PHYSICAL REVIEW A 86, 023843 (2012).

# Magnetic resonance system

Picture of magnet [6] from CST Studio

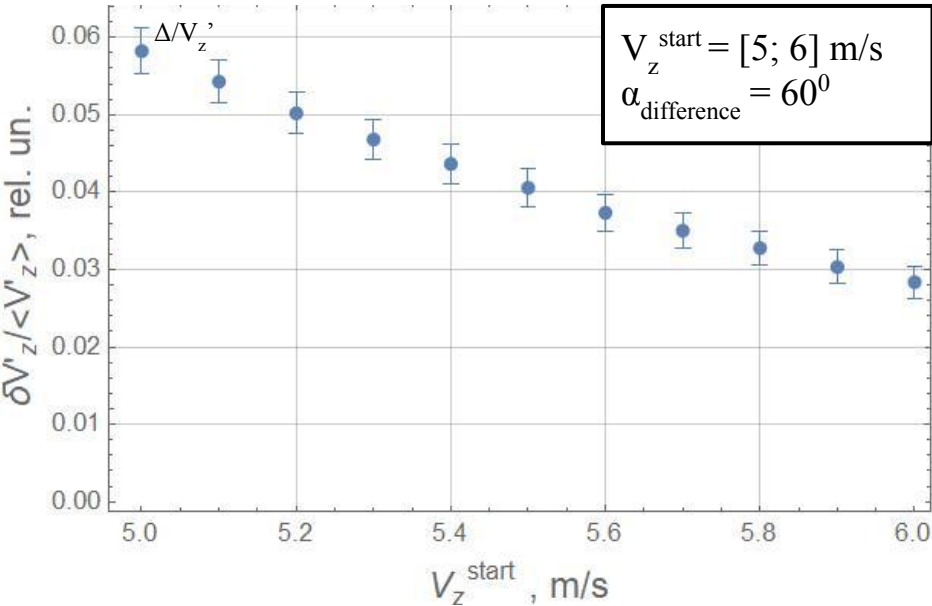
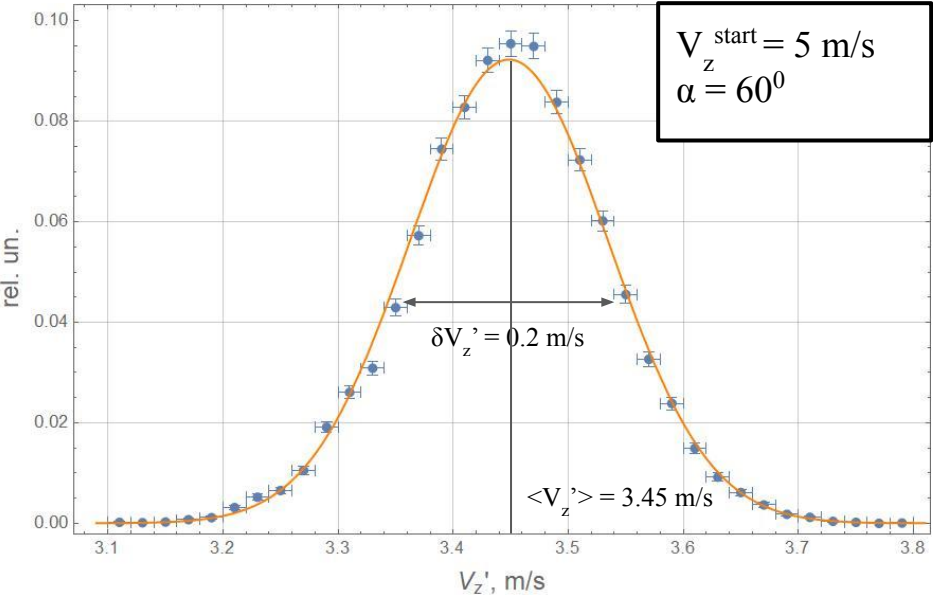


It is necessary to evaluate the dispersion of the longitudinal velocity spectrum after passing through the magnetic resonance system



[6] Y. Arimoto, T. Yoshioka, H. M. Shimizu, et al. Longitudinal-gradient magnet for time focusing of ultra-cold neutrons// Physics Procedia 17 (2011) 20–29.

# Dispersion of the longitudinal velocity spectrum after exiting the magnetic resonance system depending on the fixed longitudinal velocity before entering the system



- $V_z^{\text{start}}$  - fixed starting longitudinal velocity
- $V_z'$  - neutron longitudinal velocity after exiting magnetic system
- $\delta V_z'$  - FWHM of longitudinal velocity distribution after exiting magnetic system
- $\langle V_z' \rangle$  - mean of longitudinal velocity distribution after exiting magnetic system
- $\alpha$  - beam divergence
- $\Delta = 0.01 \text{ m/s}$  - calculation method error

$$\frac{\delta T}{T} = \frac{\delta V}{V}$$

# Main results

- 1) A software product has been created that allows to evaluate the small roughness effect on the neutron guide tube transmission.
- 2) Transmission curves were obtained for the most popular neutron guide tube materials: stainless steel, DLC, Ni-V.
- 3) A software product has been created that allows to estimate the longitudinal velocity spectrum distribution after passing through a magnetic resonance system.
- 4) An estimate of the blurring of the longitudinal velocity spectrum after passing through a magnetic resonance system is obtained.

**Thanks!**

# **Additional materials**

# Micro-roughness neutron scattering

*The probability of diffuse scattering at angles  $\theta$ ,  $\phi$  is determined by the expression from [3]:*

$$I(\theta_{out}, \phi_{out}) = \frac{k_c^4}{4 \cos(\theta_{in})} |S(\theta_{in})|^2 |S(\theta_{out})|^2 F(\theta_{in}, \theta_{out}, \phi_{out})$$

$$S(\theta) = \frac{2 \cos(\theta)}{\cos(\theta) + \sqrt{\cos^2(\theta) - k_c^2/k^2}}$$

$$F(\theta_{in}, \theta_{out}, \phi_{out}) = \frac{b^2 w^2}{2\pi} \exp\left(-\frac{\zeta^2 w^2}{2}\right)$$

$$\zeta^2 = k^2 (\sin^2(\theta_{in}) + \sin^2(\theta_{out}) - 2 \sin(\theta_{in}) \sin(\theta_{out}) \cos(\phi_{out}))$$

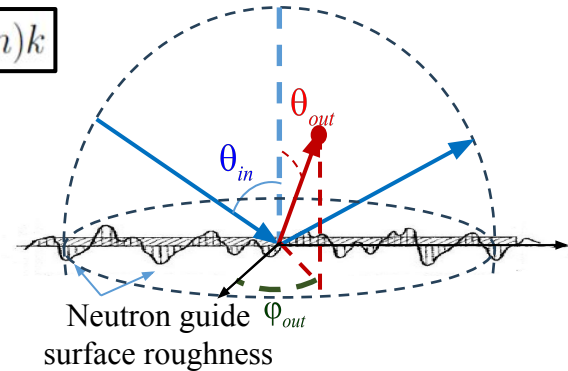
$b$  – mean square roughness amplitude

$w$  – correlation length of roughness distribution

The existing model of neutron scattering on roughnesses (MR-model) describes non-specular scattering on small roughnesses in a large range of angles.

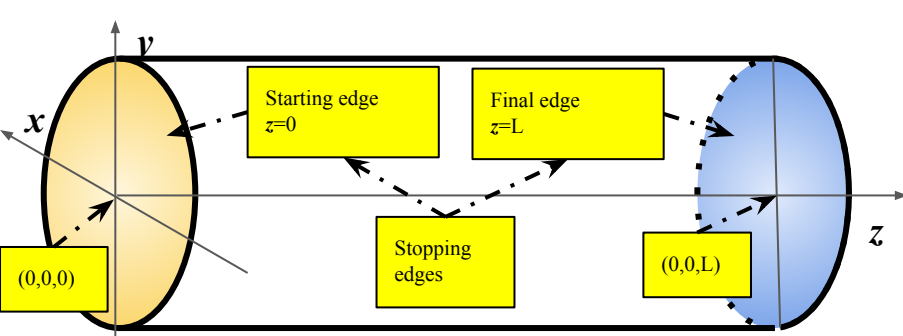
Criterion of applicability:  $kb \ll 1$

$$V = (\hbar/m)k$$

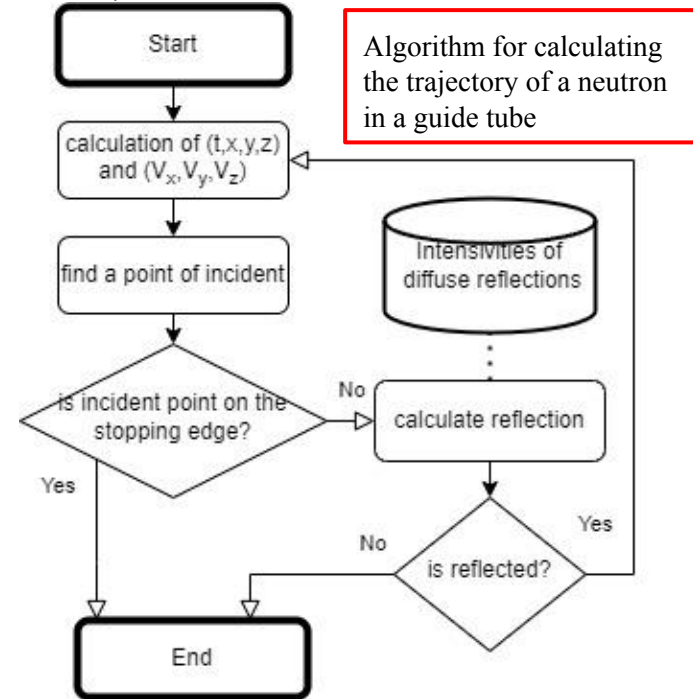


It is necessary to evaluate the transmission of neutron guides with roughness

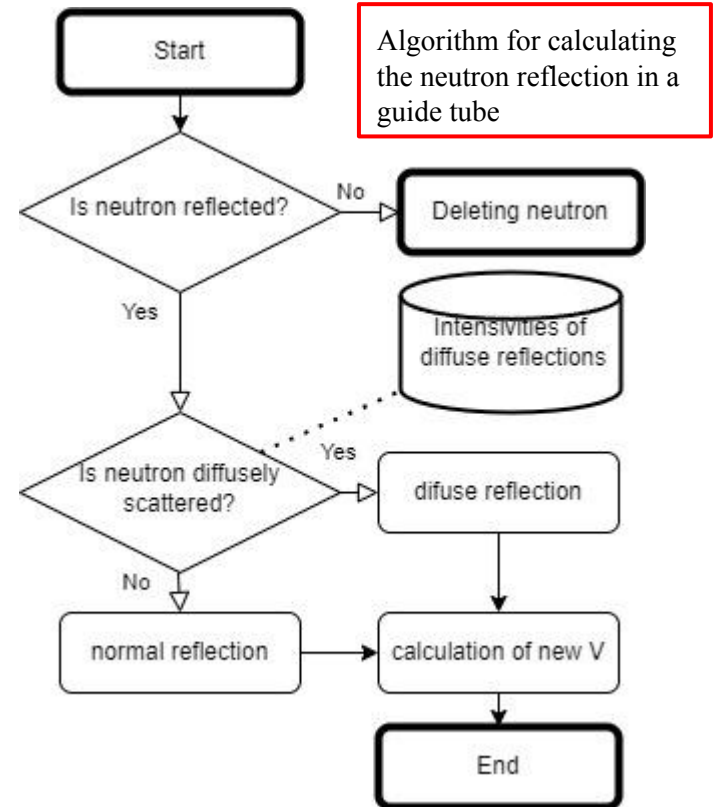
# Model of neutron movement in a guide tube



Algorithm for calculating the trajectory of a neutron in a guide tube



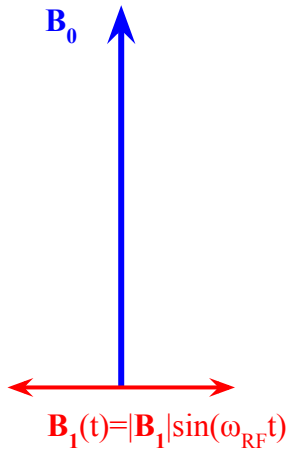
Algorithm for calculating the neutron reflection in a guide tube



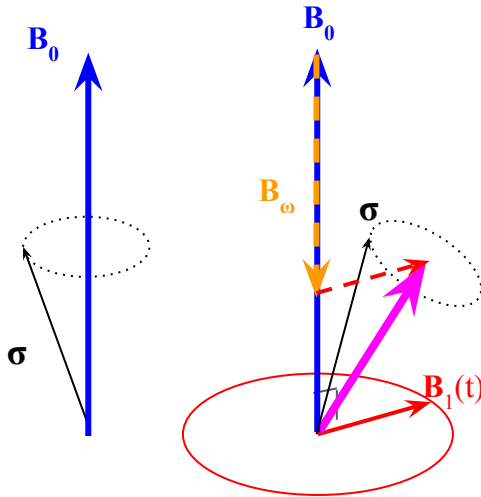


# Polarization evolution in magnetic resonance system

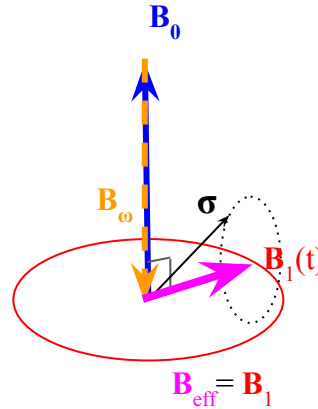
$\mathbf{B}_0 = \mathbf{B}_0(z)$  - gradient static field  
 $\mathbf{B}_1 = \mathbf{B}_1(t)$  - oscillating time-dependent RF field  
 $\mathbf{B}_\omega = -\omega_{\text{RF}}/\gamma$  - fictive field  
 $\mathbf{B}_{\text{eff}} = \mathbf{B}_0 + \mathbf{B}_\omega + \mathbf{B}_1$  - effective field



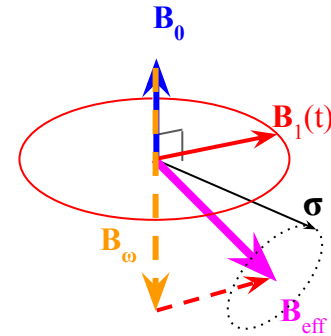
Before RF field



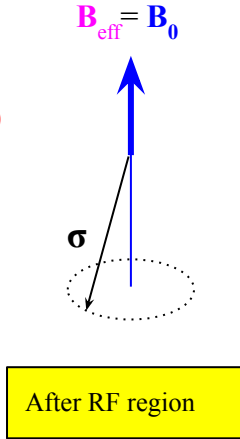
Beginning of RF region



spin-flipping area of RF region



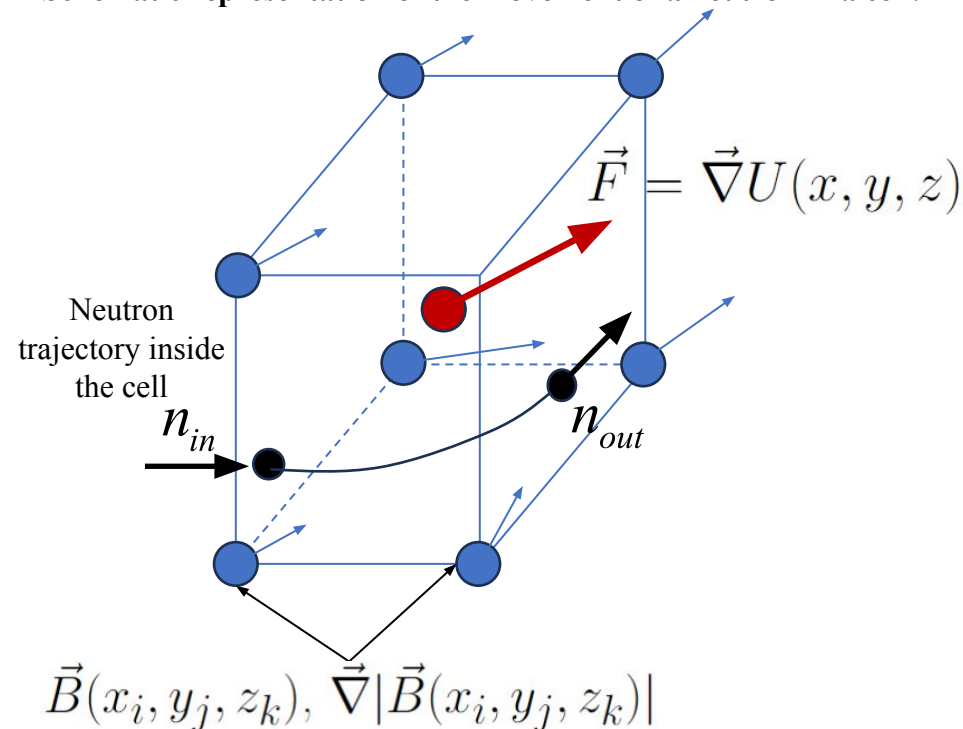
Ending of RF region



After RF region

# Model of neutron movement in a magnetic resonance system

Schematic representation of the movement of a neutron in a cell:



Model basements:

- 1) The magnetic field in the model is specified by a **three-dimensional grid** with magnetic field strengths at the nodes.
- 2) The model assumes movement in a magnetic field as movement through **small cells**, the gradient inside is close to constant.
- 3) **Reflection** from the neutron guide tube is considered **specular**.
- 4) A spin flip occurs when neutron passes through a certain cross section determined from the outside.