#### **Results of DSS collaboration with unpolarized and polarized deuteron beams at Nuclotron**



V.P.Ladygin on behalf of the DSS collaboration 5-th Nuclotron Users workshop, 5-6 October, 2017

# Outline

**1. Motivation** 

2. Results on **dp**-elastic scattering obtained at Nuclotron JINR with unpolarized beam

3. First results on the energy scan of the vector Ay and tensor Ayy and Axx analyzing powers in dp-elastic scattering at Nuclotron

- 4. Further plans at Nuclotron
- **5. Conclusion**

**DSS collaboration: Bulgaria-JINR-Japan-Romania-Russia-Slovakia** 

## **Motivation of the dp interaction studies**

- Nucleon-nucleon interaction at short distances (including its mass off-shell behaviour)
- Relativistic effects
- Transition to the nonnucleonic degrees of freedom
- Contribution of three-nucleon forces (3NFs)

#### stalled from E.L.Bratkovskaya



Few nucleons systems as a tool for dense matter studies

Alternative way to obtain the information on the EOS at extreme densities (neutron stars) is the studies of the few nucleon systems.



**Relativistic effects in 2NF and contribution of 3NF play very important role.** (A.Akhmal et al, Phys.Rev. C58 (1998) 1804)

#### **Short range correlations (SRCs)**



 

 Summary of the theoretical analysis of the experimental findings practically all of which were predicted well before the data were obtained

 More than ~90% all nucleons with momenta k≥300 MeV/c belong to two nucleon SRC correlations

 BNL + Jlab +SLAC

 Probability for a given proton with momenta 600> k > 300 MeV/c to belong to pn correlation is ~ 18 times larger than for pp correlation

 BNL + Jlab

 Probability for a nucleon to have momentum > 300 MeV/c in medium nuclei is ~25% BNL + Jlab 04 +SLAC 93

 Probability of non-nucleonic components within SRC is small - < 20% - 2N SRC mostly build of two nucleons not 6q, ΔΔ,...

 BNL + Jlab +SLAC

 Three nucleon SRC are present in nuclei with a significant probability

Poor data base on the spin parts of the 2N and 3N shortrange correlations. This motivates the neccessity to study light nuclei structure at short distances. Experiments at Nuclotron allow to reach  $p_T \sim 1$  GeV/c

#### **Non-nucleonic degrees of freedom**



When the distances between the nucleons are comparable with the size of the nucleon, the nucleon-nucleon interaction is a non-local.

The fundamental degrees of freedom, quark and gluons in the frame of QCD, begin also to play a role at the internucleonic distances comparable with the size of the nucleon.

They can manifest as  $\Delta\Delta$ , NN\*, N\*N\*, 6q etc.components.

Data: V.Punjabi et al., Phys.Lett.B350 (1995) 178 L.S.Azhgirey et al., Phys.Lett.B391 (1997) 22 L.S.Azhgirey et al., Phys.Lett.B387 (1996) 37

#### **Fundamental (quark) degrees of freedom**

At high energy s and large transverse momenta  $p_t$  the constituent counting roles (CCR) predict the following behavior of the differential cross section for the binary reactions:

$$\frac{d\sigma}{dt}(ab \rightarrow cd) = \frac{f(t/s)}{s^{n-2}} \quad ; \quad \mathbf{n} = \mathbf{N}_{a} + \mathbf{N}_{b} + \mathbf{N}_{c} + \mathbf{N}_{d}$$

(Matveev, Muradyan, Tavkhelidze, Brodsky, Farrar et al.)



Yu. N. Uzikov JETP Lett, 81 (2005) 303-306 For the reaction dd  $\rightarrow$  <sup>3</sup>Hen  $N_A + N_B + N_C + N_D - 2 = 22$ For the reaction dp  $\rightarrow$  dp  $N_A + N_B + N_C + N_D - 2 = 16$ 

The regime corresponding to CCR can occur already at  $T_d \sim 500 \text{ MeV}$ 

#### **Three Nucleon Forces**

- Modern NN potentials (CD-Bonn, AV-18, Njimegen etc.) accurately reproduce the NN data set up to about 350 MeV. However they fail in the description of the triton binding energy and data on unpolarized dp-elastic scattering and breakup.
- Incorporation of three nucleon forces (3NF), when interaction depends on the quantum numbers of the all three nucleon, allows to reproduce the binding energy of the three-nucleon bound systems and the data on unpolarized **dp**- interaction.



- Tucson-Melbourne
- Brazil
- Urbana-IX
- Fujita-Miyazawa ( $N\Delta$ )
- Chiral Effective Field Theory

Needs to be very careful: according to the theorem of W.N.Polyzou and W.Gloeckle, Few Body Syst. 9 (1990) 97, off-shell behaviour of 2NF can imitate 3NF effect.

Triton binding energy without 3NF: Y.Fujiwara et al., Phys.Rev.C66 (2002) 021001(R)

# **Cross section in dp- elastic scattering at intermediate energies**



The differential cross section in elastic Nd scattering at the energy of 135 (left figure) and 250 (right figure) MeV/u.

K. Sekiguchi et al., Phys. Rev. Lett. 95, 162301 (2005)

K. Hatanaka et al., Phys. Rev. C 66, 044002 (2002)

The cross section data for **dp**- elastic scattering are reproduced well up to 150 MeV taking into account 3NF. Manifestation of three-nucleon forces effect in the cross-section of **dp**-elastic scattering at this energy: up to 30% in the vicinity of Sagara discrepancy.

But the problems in the description are at higher energies.

## Deuteron analyzing powers in dp- elastic scattering at intermediate energies (140, 200, 270 MeV)



Polarization data for dp- elastic scattering are not described even with the 3NFs inclusion (except for Ay). The spin part of 3NFs is missed!

#### **Status of dp- elastic scattering**

- Inclusion of modern 3NFs allows to describe cross section and deuteron vector analyzing power of **dp**- elastic scattering up to 135 MeV/nucleon, while the tensor observables are not described.
- The data at higher energies (up to 300 MeV/nucleon) are not described even taking into account relativistic effects.
- The reason of the discrepancy is nowadays called the importance of the short range 3NFs which are still not included.
- 1. The systematic study of hadronic reactions induced by deuterons at Nuclotron will allow to study the structure of 2N and 3N forces, including their short-range parts.
- 2. Development of the relativistic models for the description of 12 these reactions is required.



The purpose of the **DSS** experimental program is to obtain the information about **2NF** and **3NF** (*including their spin* – *dependent parts*) from two processes:

1.dp-elastic scattering at the energies between 300 - 2000 MeV;

2.dp-breakup with registration of two protons at deuteron energies of 300 - 500 MeV.

#### **Nuclotron-M accelerator complex**



## **Experiments at Internal Target Station at Nuclotron DSS-project**



Internal Target Station is very well suited for the measurements of the deuteron- induced reactions observables at large scattering angles.

## Setup to study dp- elastic scattering at ITS at Nuclotron in 2005



- Deuterons and protons in coincidences using scintillation counters
- Internal beam and thin CH<sub>2</sub> target (C for background estimation)
- Polarization measurement at 270 MeV
- Analyzing powers measurement at **880** and **2000** MeV
- The data were taken for three spin modes of PIS: unpolarized, "2-6" and "3-5"  $(p_z, p_{zz}) = (0,0)$ , (1/3,1) and (1/3,-1)

#### **Analyzing powers in dp- elastic scattering at 880 MeV**



Dashed lines are the multiple scattering model calculations using CD -Bonn DWF (N.B.Ladygina, Phys.Atom.Nucl.71 (2008) 2039) Solid lines are the Faddeev calculations using CD-Bonn potential (H.Witala, private communication)

Dott-dashed lines are the optical-potential calculations using Dibaryon DWF (M.Shikhalev, Phys.Atom.Nucl.72 (2009) 588) Published in P.K.Kurilkin et al., Phys.Lett.B715 (2012) 61-65

# **A**<sub>y</sub> and **A**<sub>yy</sub> in **dp**- elastic scattering at 2000 MeV



Open squares are the data obtained at Nuclotron JINR. Open circles are the Synchrophasotron data (V.V.Glagolev, Eur. Phys. J. A48 (2012) 182)

Solid symbols are the data obtained by ANL group (Haji-Saied et al., Phys.Rev.C.36 (1987) 2010).

Dashed and solid lines are the relativistic multiple scattering model calculations using CD- Bonn DWF taking into account single scattering and single+double scattering, respectively.

#### **Energy dependence of the dp-elastic scattering analyzing powers at fixed scattering angles in the c.m.s.**



- Full symbols are the data obtained at JINR
- Open symbols are the data obtained at RIKEN, Saclay and ANL
- The study of the energy dependence of the analyzing powers in dp- elastic scattering at large p<sub>T</sub> is one of the tools to study spin effects in cold dense matter

#### dp- elastic scattering cross section at 1400 MeV



A.A.Terekhin et al., JINR Preprint P1-2017-33 (2017), to be published in Phys.Atom.Nucl. (2017).

**Relativistic multiple scattering model calculation: N.B.Ladygina, Eur.Phys.J, A52 (2016) 199** 

#### **New Source of Polarized Ions**



New source will provide up to 2\*10<sup>10</sup> ppp and higher values of polarization than POLARIS.

- Part of the IUCF source was used for the construction. The putting into operation of new SPI was in 2016.
- Large variety of the spin modes. For instance, DSS project would like to use the spin modes with the following ideal values of (p<sub>z</sub>,p<sub>zz</sub>): (0,0), (0,-2), (+1,+1) and (-1,+1).

#### Figure of merit will increase by a factor ~ 10<sup>3</sup>

#### **Upgrade of the Delta-LNS (DSS) setup at ITS at Nuclotron**



New infrastructure, cabling New HV system (Mpod) New VME DAQ 40 counters for dp-elastic scattering studies 8 dE-E detectors for dp -breakup studies



#### Results from the commissioning run at Nuclotron at 270 MeV (June 2016)



- Deuterons and protons in coincidences using scintillation counters
- Internal beam and thin CH<sub>2</sub> target (C for background estimation)
- Measurements at 270 MeV
- The setup was ready to take the polarized data.

# Setup to study dp- elastic scattering at ITS at Nuclotron in 2016-2017.



- Deuterons and protons in coincidences using scintillation counters
- Internal beam and thin CH<sub>2</sub> target (C for background estimation)
- Permanent polarization measurement at 270 MeV (between each energy).
- Analyzing powers measurement at 400-1800 MeV
- The data were taken for three spin modes of SPI: unpolarized, "2-6" and "3-5"  $(p_z, p_{zz}) = (0,0)$ , (1/3,1) and (1/3,-1).
- Typical values of the polarization was 70-75% from the ideal values. (talk of Ya.Skhomenko).

#### Angular dependence of the vector analyzing power Ay in dpelastic scattering at 400 MeV



Full squares are the data fom Nuclotron (December 2016)

Curves are the relativistic multiple sacttering model calculations N.B.Ladygina, Eur.Phys.J, A42 (2009) 91

#### Angular dependence of the tensor analyzing power Ayy in dp-elastic scattering at 400 MeV



Full squares are the data fom Nuclotron (December 2016)

Curves are the relativistic multiple sacttering model calculations N.B.Ladygina, Eur.Phys.J, A42 (2009) 91

#### Angular dependence of the tensor analyzing power Axx in dp-elastic scattering at 400 MeV



Full squares are the data fom Nuclotron (December 2016)

Curves are the relativistic multiple sacttering model calculations N.B.Ladygina, Eur.Phys.J, A42 (2009) 91

#### Energy dependence of the vector analyzing power Ay in dpelastic scattering at 700-1800 MeV

![](_page_27_Figure_1.jpeg)

Full circles are the new preliminary data fom Nuclotron (2016-2017). Full squares are the data fom Nuclotron (2005). Open symbols are the world data.

#### Energy dependence of the tensor analyzing power Ayy in dpelastic scattering at 700-1800 MeV

![](_page_28_Figure_1.jpeg)

Full circles are the new preliminary data fom Nuclotron (2016-2017). Full squares are the data fom Nuclotron (2005). Open symbols are the world data.

# Experimental setup for dp-breakup.

![](_page_29_Figure_1.jpeg)

![](_page_29_Picture_2.jpeg)

**Replace of the PMTs 85 and 63 by Hamamatsu PMTs** 

# dp breakup reaction.

![](_page_30_Figure_1.jpeg)

This slide presents tensor analyzing power Ayy (top) and differential cross section in selected breakup configurations at 200 MeV (bottom).

•The light shaded band (blue) contains the theoretical predictions based on CD-Bonn, AV18, Nijm I, II and Nijm 93.

•The darker band (magenta) represents predictions when these NN forces are combined with the TM 3NF.

•The solid line is for AV18+Urbana IX and the dashed line for CD Bonn+TM

One can see that the inclusion of **3NF** have great impact on the values of analyzing power and cross section.

 $\Theta_1$  – polar angle of the 1-st proton.

 $\Theta_2$  – polar angle of the 2-nd proton.

S – arc length along the kinematical curve.

 $\Phi_{12}$  – azimuth angle with respect to the horizontal plane.

#### Dp breakup reaction at 400 MeV, $\theta_{p1} = 39^{\circ}(\pm 2.3^{\circ}), \theta_{p2} = 43^{\circ}(\pm 2.3^{\circ})$

![](_page_31_Figure_1.jpeg)

dp → ppn, two protons registered at angles:  $\theta_{p1} = 39^{\circ} (\pm 2.3^{\circ}), \theta_{p2} = 43^{\circ} (\pm 2.3^{\circ})$ one Arm is fixed at 43°, 2<sup>nd</sup> moving (27°, 31°, 35°, 39°, 43°)

# dp breakup reaction, polarized

![](_page_32_Figure_1.jpeg)

Detector placement is determined by polar  $\theta$  and azimuthal  $\varphi$  angles. Azimuthal angle  $\varphi$  have anticlockwise direction. Detector setup for the case of analyzing power investigation.

# AP of dp breakup reaction at 400 MeV, pp-quasi elastic data

![](_page_33_Figure_1.jpeg)

Angular dependence of the vector analyzing power  $iT_{11}$  at energy of **200** MeV/n. Data obtained at Nuclotron JINR are rgpresented by full blue symbols (72.3° and 76.5° in cm). Other symbols – world data.

# dp breakup reaction at 400 MeV, analyzing power data

Spherical analyzing powers  $iT_{11}$  and  $T_{20}$ . Detector configuration is determined by polar  $\theta_1$  and  $\theta_2$ , and azimuthal angles  $\varphi$ . Azimuthal angle is related to the angle of the detector which is closest to beam direction.

pp -quasi elastic 72.3° and 76.5°

Conf.	θ₁ [°]	<b>θ</b> <sub>2</sub> [°]	φ [°]	iTıı	/T <sub>20</sub>	iT11 combined	T <sub>20</sub> combined
detectors – 5, 4	34.8	52.5	135	$0.10\pm0.02$	0	-	-
detectors – 6, 3	36.8	50.4	45	$0.11 \pm 0.06$	0	-	-
detectors – 1, 6	34.8	36.8	135	$0.55\pm0.15$	$0.13\pm0.30$		
detectors – 5, 2	34.8	36.8	135	$0.39\pm0.13$	$-0.09 \pm 0.27$	0.47 ± 0.10	0.02 ± 0.20

#### **Results combined**

#### **Further DSS plans**

Final analysis of the systematic data on the cross section and analyzing powers  $A_y$ ,  $A_{yy}$  and  $A_{xx}$  in dp- elastic scattering between 270 MeV and 2000 MeV at ITS.

Preparation of the experiments on the systematic studies of the analyzing powers  $A_y$ ,  $A_{yy}$  and  $A_{xx}$  in dp- elastic scattering between 270 MeV and 700 MeV using new SPI at Nuclotron to study the manifestion of the short-range 3NFs.

Preparation for the taking of new polarized data for the **dp** (**pd**)- nonmesonic breakup at the energies between **300** and **500** MeV for different kinematic configurations at **ITS** with polarized beams.

Preparation of the experiment on the energy scan of the nucleon analyzing power  $A_v^p$  in pd- elastic scattering between 135 MeV and 1000 MeV at ITS.

Preparation of the experiments with extracted polarized deuteron beam (SS of SRC - see Proceedings of IBSHEPP-XXII, SPIN-2014 and DSPIN15 ).

# Conclusion

Upgraded Nuclotron with new **SPI** provides quite unique opportunity for the studies of the spin effects and polarization phenomena in few body systems.

The realization of the DSS program at ITS will allow to obtain the crucial data on the spin structure of 2-nucleon and 3- nucleon short range correlations.

The first natural step in these studies, namely, the energy scan of the deuteron analyzing powers in **dp**- elastic scattering has been performed in 2016-2017.

Next experiments using polarized deuterons and protons at ITS are in preparation (SR 3NF and S3RC).

The extention of the studies to the high energies is possible with the extracted polarized deuteron and proton beams.

# **Thank you for the attention!**

# Our work is dedicated to the memory of L.S.Zolin

![](_page_38_Picture_1.jpeg)

Professor Leonid Zolin for many years was one of the leading scientists in the field of polarization phenomena in nuclear reactions at relativistic energies and in the development of the deuteron beam polarimetry at JINR (Synchrophasotron-Nuclotron).

# Experimental setup for dp-breakup.

![](_page_39_Figure_1.jpeg)

![](_page_39_Picture_2.jpeg)

**Replace of the PMTs 85 and 63 by Hamamatsu PMTs** 

# dp breakup reaction.

![](_page_40_Figure_1.jpeg)

This slide presents tensor analyzing power Ayy (top) and differential cross section in selected breakup configurations at 200 MeV (bottom).

•The light shaded band (blue) contains the theoretical predictions based on CD-Bonn, AV18, Nijm I, II and Nijm 93.

•The darker band (magenta) represents predictions when these NN forces are combined with the TM 3NF.

•The solid line is for AV18+Urbana IX and the dashed line for CD Bonn+TM

One can see that the inclusion of **3NF** have great impact on the values of analyzing power and cross section.

 $\Theta_1$  – polar angle of the 1-st proton.

 $\Theta_2$  – polar angle of the 2-nd proton.

S – arc length along the kinematical curve.

 $\Phi_{12}$  – azimuth angle with respect to the horizontal plane.

![](_page_41_Picture_0.jpeg)

Correlations of the proton energies with the cut on missing mass (940MeV±10MeV) of deuteron energy 400 MeV.

# Conclusion

Upgraded Nuclotron with new **PIS** could provide quite unique opportunity for the studies of the spin effects and polarization phenomena in few body systems.

The realization of the DSS program at ITS will allow to obtain the crucial data on the spin structure of 2-nucleon and 3- nucleon short range correlations.

The first natural step in these studies is the energy scan of the deuteron analyzing powers in **dp**- elastic scattering.

The extent of the studies to the high energies is possible with the extracted polarized deuteron beam ( for example with the **BM@N** setup).

# **Thank you for the attention!**

# **Stage 1 of BM@N setup for spin studies**

![](_page_44_Figure_1.jpeg)

(DC) trackers are neccessary

# Transportation line of the Nuclotron extracted beam to the BM@N spectrometer

![](_page_45_Figure_1.jpeg)

#### **Polarization observables for polarized deuteron induced reactions**

![](_page_46_Figure_1.jpeg)

- The measurements of the tensor analyzing power  $T_{20}$  and spin correlation  $C_{y,y}$  in the <sup>3</sup>He(d,p)<sup>4</sup>He reaction in the kinetic energy range between 1.0 and 1.75 GeV can be performed at the BM@N area.
- The polarization observables for the p(d,p)d, d(d,p)t and  $d(A,p(0^{\circ}))X$  at intermediate and high energies also can be studied.
- Non-nucleonic degrees of freedom and baryonic resonances properties can be studied in the  $d(A,d(0^{\circ}))X$  and  $d(A,\pi^{-}(0^{\circ}))X$  reactions at different energies.
- The tensor analyzing power T<sub>20</sub> can be studied for the meson production in the d(A,3He(0°))X reactions.

#### **Preliminary GEANT simulation for** <sup>3</sup>**He(d,p)**<sup>4</sup>**He**

#### BM@N GEANT model

#### Beam profile at 1-st GEM station

XY, pHe4SiO2, 1 BmnGemStation, FF=2.1

![](_page_47_Figure_4.jpeg)

## **dd** → <sup>3</sup>**Hen(**<sup>3</sup>**Hp)** reactions at Nuclotron energies

![](_page_48_Figure_1.jpeg)

The relativistic multiple scattering model can be successfully used to describe the  $dd \rightarrow {}^{3}Hen({}^{3}Hp)$  reactions in a GeV region at the Nuclotron. The calculations require a large amount of CPUs. The results are published in N.B.Ladygina, Few Body Systems 53 (2012) 253.

## **Polarization effects in the dd** → <sup>3</sup>**Hen(<sup>3</sup>Hp) reactions at Nuclotron energies**

![](_page_49_Figure_1.jpeg)

The relativistic multiple scattering model was successfully used to describe the  $dd \rightarrow {}^{3}Hen({}^{3}Hp)$  reactions in a GeV region at the Nuclotron. The calculations require a large amount of CPUs. The results were published in FBS, PRC, PPN.

## N.Ladygina - theory A.Kurilkin – experiment

#### The deuteron energy of 500 MeV. ICTUP $\Theta_1 = 24.7^\circ, \Theta_8 = 53.3^\circ,$ $\Theta_2 = 24.7^\circ, \Theta_4 = 33.3^\circ,$ $\Theta_1 = 24.7^\circ, \Theta_3 = 33.3^\circ,$ $\phi_{18} = 135.4^{\circ}$ $\varphi_{24} = 46.5^{\circ}$ $\phi_{12} = 44.6^{\circ}$ EdotIII/MoV EdetVIII/MeV EdetIV(MeV 80 100 120 140 160 180 110 120 130 140 150 160 170 180 60 80 100 120 140 160 180 EdetIII(MeV) EdetI(MeV) EdetI(MeV)

Correlations of the proton energies with the cut on missing mass (940MeV±10MeV) of deutron energy 500 MeV.

## Measurement of the deuteron beam polarization at ITS using DSS detection system at 270 MeV

![](_page_51_Figure_1.jpeg)

#### dp- elastic events selection

![](_page_51_Figure_3.jpeg)

The correlation of the energy-loss signal for a pair of the deuteron and proton detector. The solid line is a graphical cut for the dp-elastic events selection. The time difference between deuteron and proton detector for  $CH_2$  target. The dotted line is a time gate for the dp-elastic events selection.

## Measurement of the deuteron beam polarization at ITS using DSS detection system at 270 MeV

![](_page_52_Figure_1.jpeg)

Vector Ay and tensor analyzing powers  $A_{yy}$ ,  $A_{xx}$  and  $A_{xz}$  of dp- elastic scattering as a function of deuteron scattering angle in c.m.s. at deuteron beam energy of 270 MeV.  $\Box$ ,  $\Delta$ - the world data. Extrapolated values of the analyzing powers are marked by  $\bullet$ .

Cubic spline interpolation:  $(x_i,y_i)$  Ha [A,B]  $f(x) = ax^3 + bx^2 + cx + d$ f''(A) = f''(B) = 0

K.Sekiguchi et al., Phys. Rev. C65 (2002) 034003 K.Sekiguchi et al., Phys. Rev.C70 (2004) 014001 K.Suda, et al., Nucl. Instr. Meth. in Phys. Res. A572 (2007) 745

## Measurement of the deuteron beam polarization at ITS using DSS detection system at 270 MeV

![](_page_53_Figure_1.jpeg)

Tensor  $p_{yy}$  and vector  $p_y$  polarization of the beam for "2-6" and "3-5" spin modes of PIS POLARIS as a function of the deuteron scattering angle in the cms.

![](_page_53_Figure_3.jpeg)

• Reference deuteron beam polarimeter at Nuclotron. P.K.Kurilkin et al., Nucl. Instr. and Meth. A 642 (2011) 45

#### Long term stability of the beam polarization at 270 MeV

![](_page_54_Figure_1.jpeg)

Tensor  $p_{yy}$  and vector  $p_y$  components of the deuteron beam polarization for "2-6" and "3-5" spin modes of PIS POLARIS as a function of the measuring time.

# A<sub>y</sub>, A<sub>yy</sub> and A<sub>xx</sub> in dp- elastic and quasielastic scattering at 880 and 2000 MeV

![](_page_55_Figure_1.jpeg)

- The analyzing powers in **dp**-elastic scattering are large enough to provide both the vector and tensor polarimetry at high energies.
- The analyzing powers values for elastic and quasielastic deuteron scattering are comparable. Therefore, polarimeter can used in the counting mode (without event-by-event analysis).

#### **Relativization schemes**

For the case of the deuteron vertex the internal momentum  $\mathbf{k}$ :

$$k = \sqrt{\frac{m_p^2 + \mathbf{k}_T^2}{4x(1-x)} - m_p^2},$$
  
$$x = \frac{E_p + p_{pl}}{E_d + p_d},$$

where  $\mathbf{E}_d$  and  $\mathbf{p}_d$  are the energy and momentum of the initial deuteron, respectively,  $\mathbf{p}_{\mathbf{p}\mathbf{l}}$  is the longitudinal momentum of the proton,  $\mathbf{m}_{\mathbf{p}}$  and  $\mathbf{E}_{\mathbf{p}}$  are the mass and energy of the proton, respectively.

- Minimal relativization scheme (Dirac, Weinberg, Frankfurt& Strikman)
- Bete-Salpeter equation solving (Tjon&Keisler, Bondarenko et al.)
- Quasi-potential wave functions (Gross, Braun&Tokarev, Kaptari et al.)
- Covariant theory on the light cone (Karmanov et al.)

#### **Deuteron wave function on the light cone**

Relativistic deuteron wave function on light cone is defined by 6 invariant functions  $\mathbf{f_1}, ..., \mathbf{f_6}$  (instead of 2 in the non-relativistic case), each of them depends on 2 scalar variables  $\mathbf{k}$  and  $z = cos(\widehat{\mathbf{kn}})$ :

$$\begin{split} \psi(\mathbf{k},\,\mathbf{n}) \,&=\, \frac{1}{\sqrt{2}}\sigma f_1 + \frac{1}{2} \left[ \frac{3}{k^2} \mathbf{k} (\mathbf{k} \cdot \sigma) - \sigma \right] f_2 + \frac{1}{2} [3\mathbf{n} (\mathbf{n} \cdot \sigma) - \sigma] f_3 + \frac{1}{2k} [3\mathbf{k} (\mathbf{n} \cdot \sigma) \\ &+\, 3\mathbf{n} (\mathbf{k} \cdot \sigma) - 2\sigma (\mathbf{k} \cdot \mathbf{n})] f_4 + \sqrt{\frac{3}{2}} \frac{i}{k} [\mathbf{k} \times \mathbf{n}] f_5 + \frac{\sqrt{3}}{2k} [[\mathbf{k} \times \mathbf{n}] \times \sigma] f_6, \end{split}$$

$$(\mathbf{n} \cdot \mathbf{k}) = (\frac{1}{2} - \alpha) \cdot \sqrt{\frac{m_p^2 + \mathbf{p}_T^2}{\alpha(1 - \alpha)}}$$

#### V.A.Karmanov, J.Carbonell et al.

![](_page_58_Picture_0.jpeg)

![](_page_58_Picture_2.jpeg)

![](_page_58_Picture_3.jpeg)

SPP and

LU-20

(5 MeV/u)

**Nuclotron** is a presently available facility which can accellerate *Au* up to 4.65 AGeV, *p* up to 12.6 GeV

**DSS** and **BM@N** are the fixed target experiments at the internal and extracted beams of Nuclotron, respectively.

Booster (3-660 MeV/u)

inside Synchrophasotron

voke

# Superconduction gace dependence on the series of the serie

Nuclotron

0.6-4.5 GeV/u

Cryogenics

Multi-Purpose Detector (MPD)

#### Analyzing powers measurement at 2000 MeV

#### The dp- elastic events selection

![](_page_59_Figure_2.jpeg)

The correlation of the energy-loss signal for a pair of the deuteron and proton detector at 70° in c.m.s. The solid line is a graphical cut for the dp-elastic events candidate selection. Selection of the dp elastic events by the time difference  $\Delta T_{d-p}$  between the signal appearance from deuteron and proton detectors with the criteria on the amplitude signal correlation.

#### HE-dp- experiment data analysis

![](_page_60_Figure_1.jpeg)

CH2-C subtraction for amplitude spectrum of P-counter.

The carbon backround arises with the deuteron energy significantly.

## **Scheme of the HE-dp- experiment**

![](_page_61_Figure_1.jpeg)

LE-dp- experiment has been performed with PMT-85 in 2011-2012