



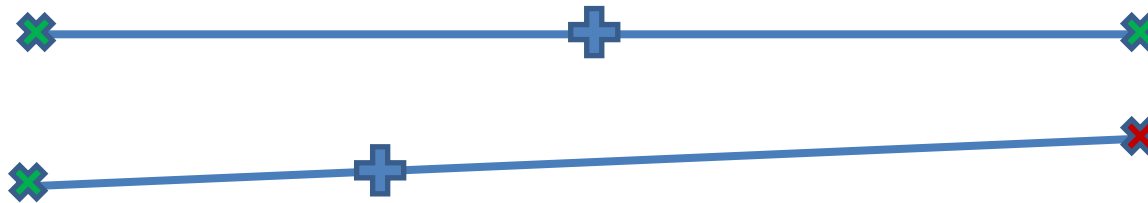
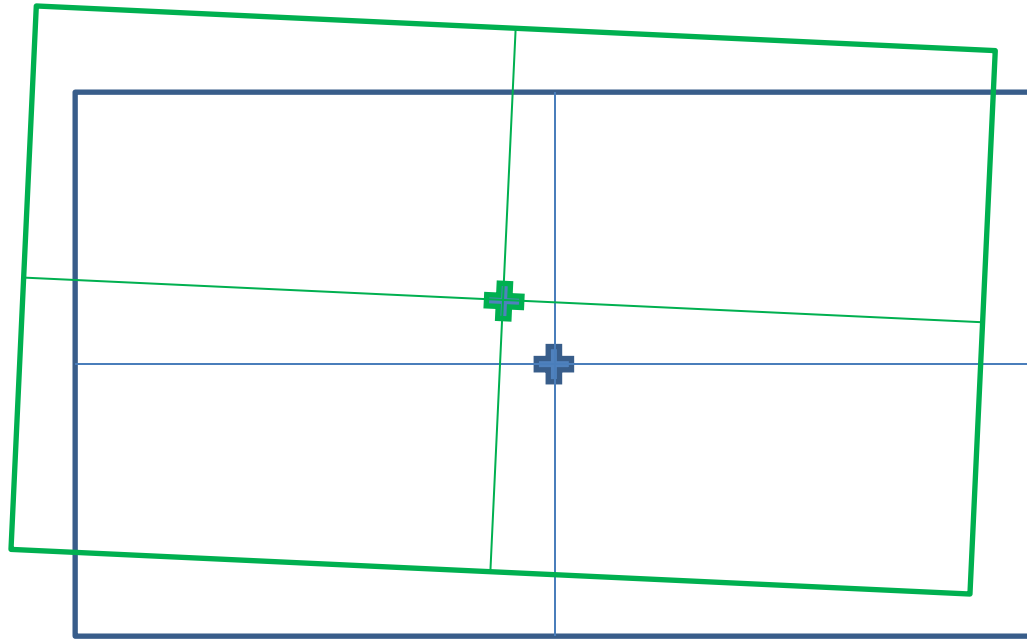
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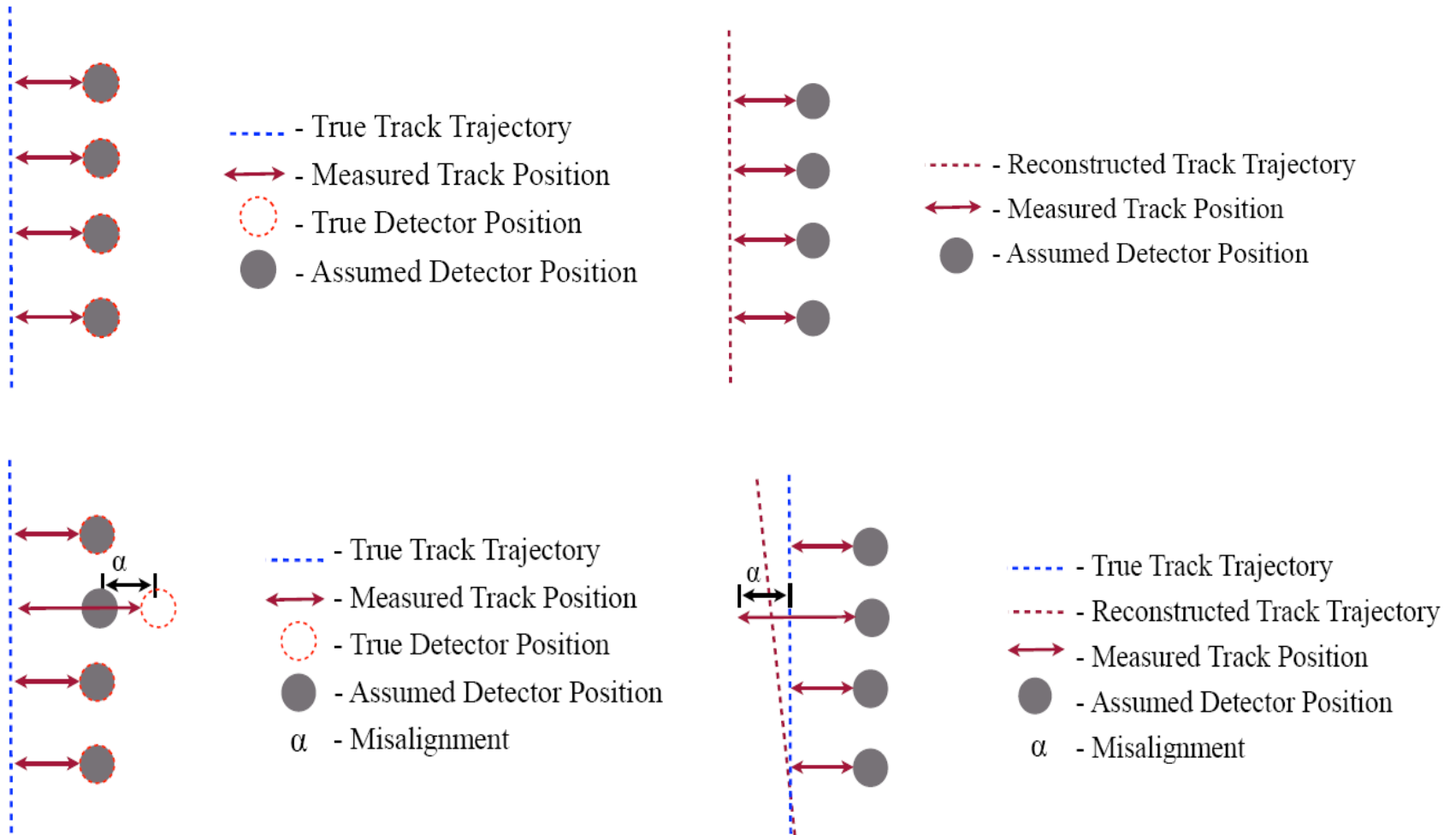
Status of geometry alignment of BM@N tracking detectors

Zarif Sharipov

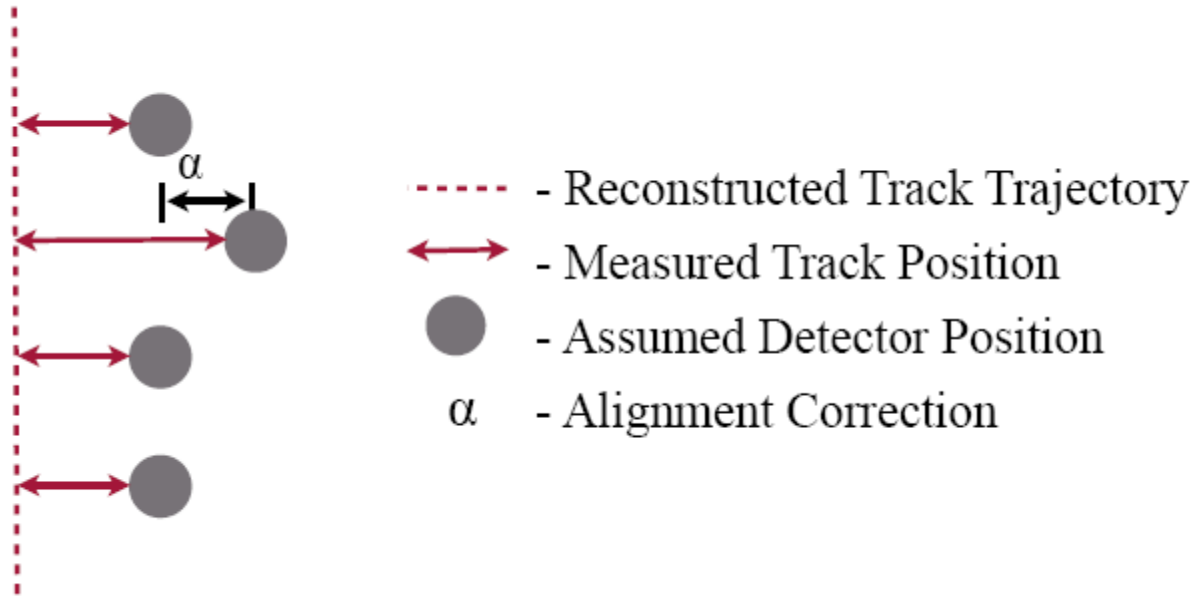
Introduction to Alignment



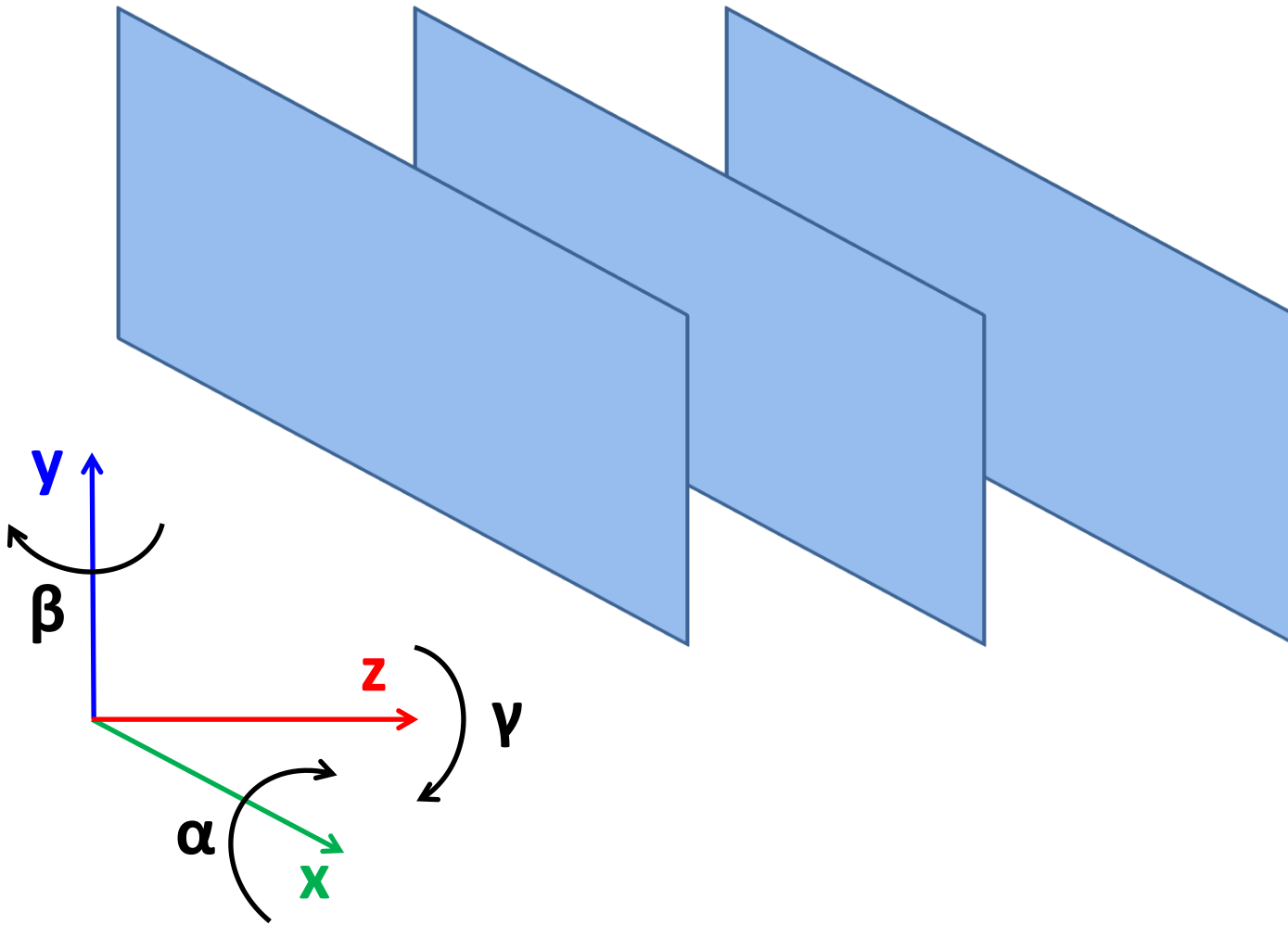
Introduction to Alignment



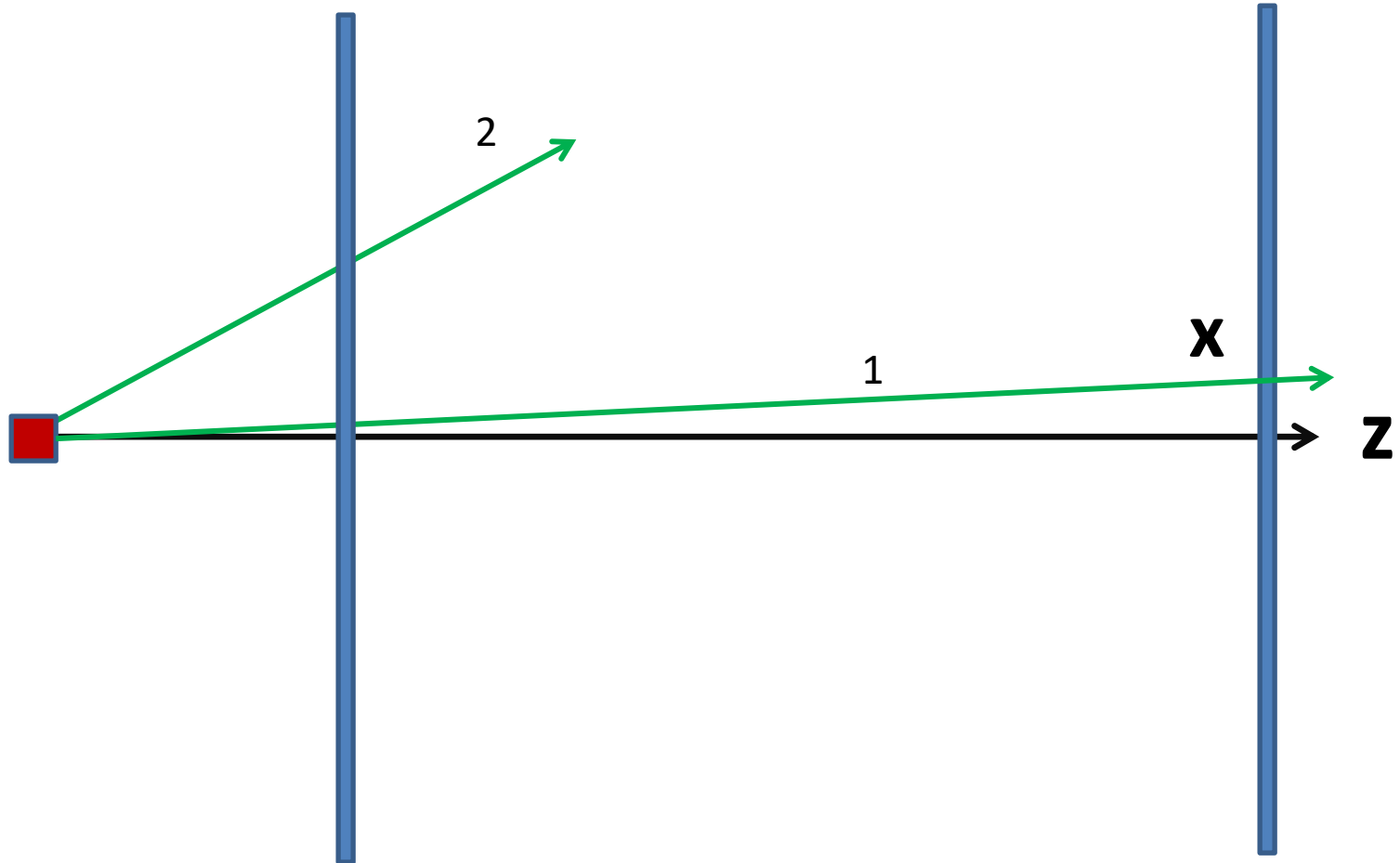
Introduction to Alignment



Introduction to Alignment

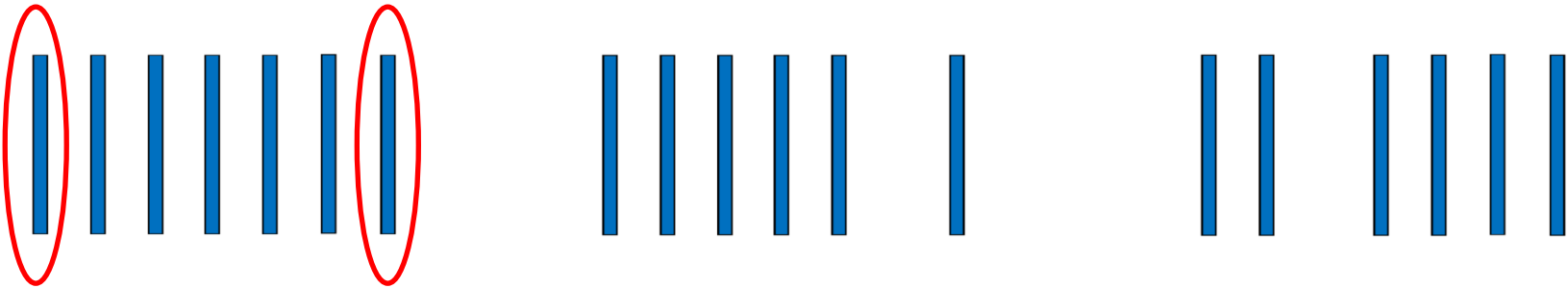
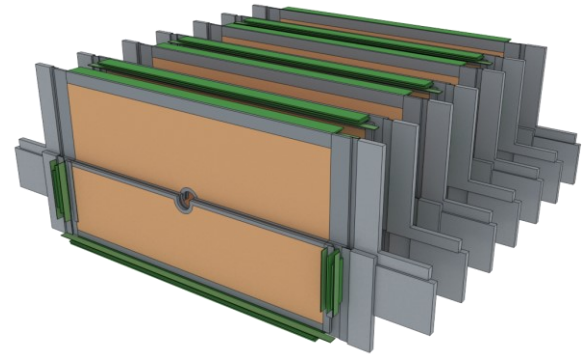


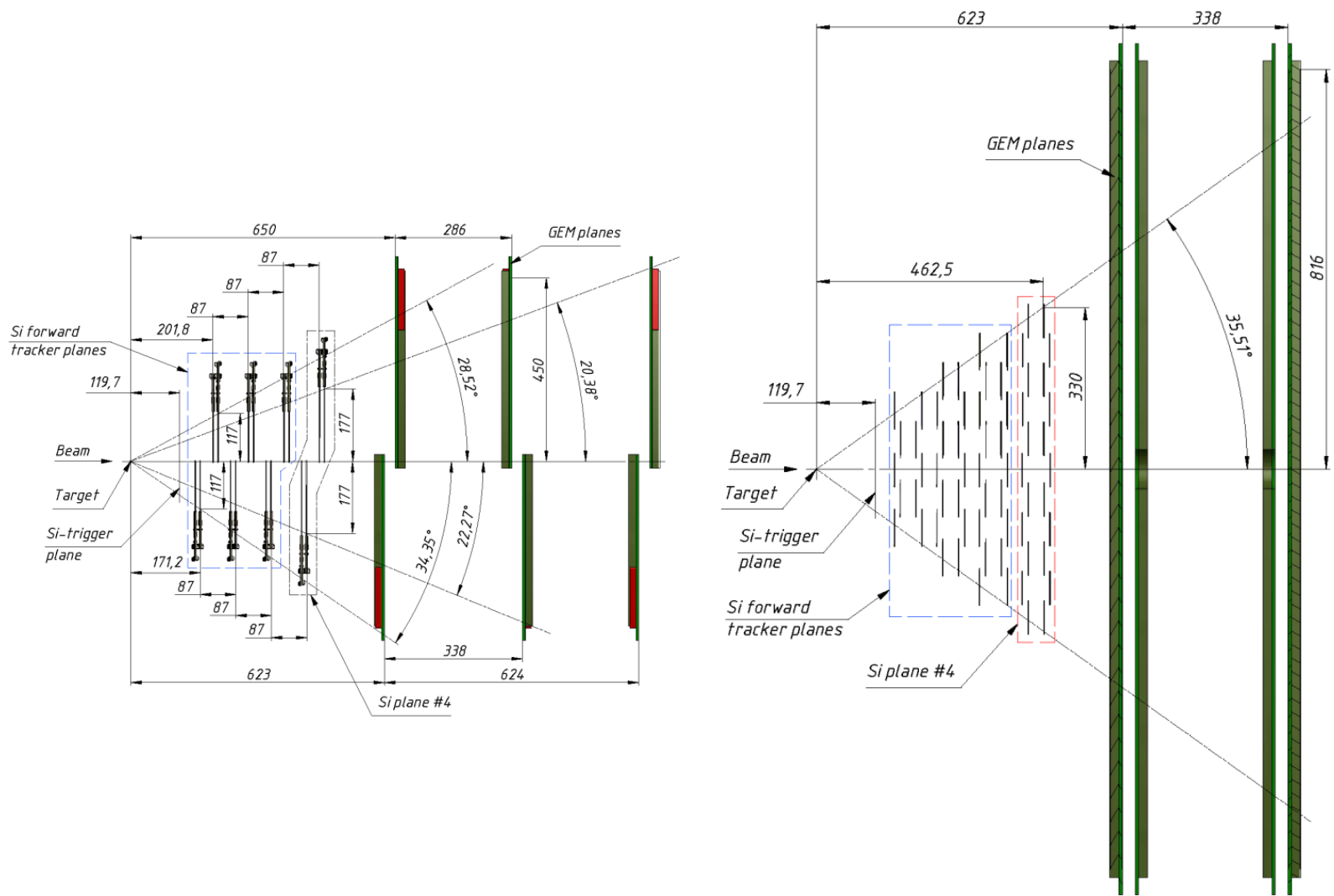
Introduction to Alignment



RUN 7651

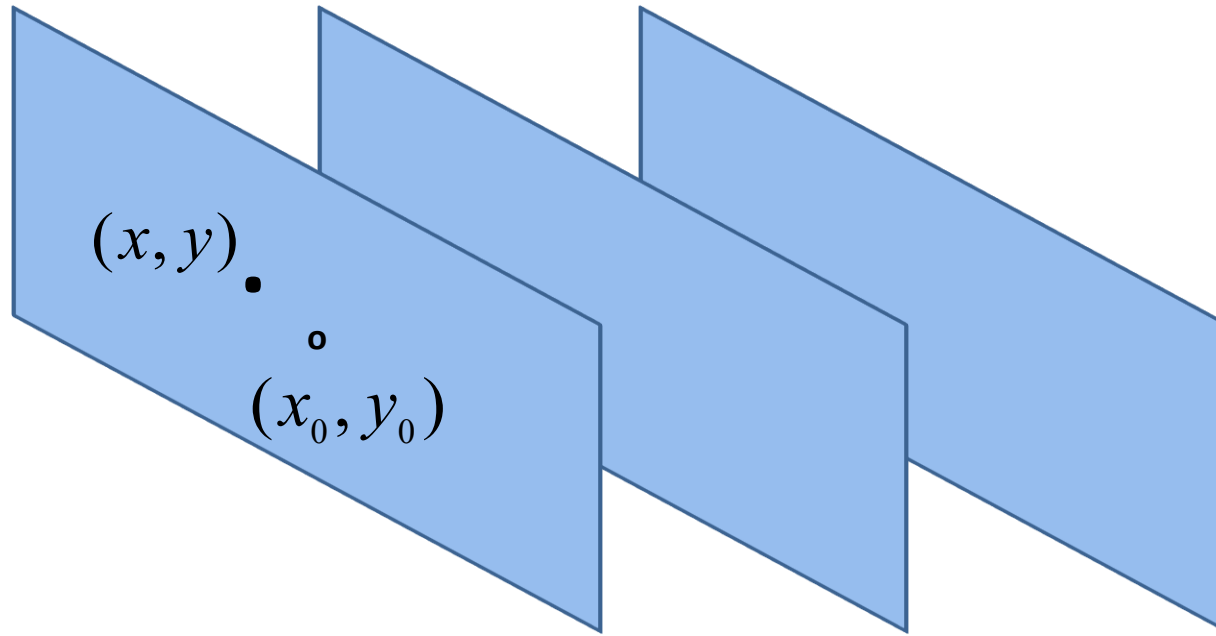
Period: 8
Number: 7651
Beam: $A = -1, Z = -1$
Beam energy: 3.8 GeV
Target: $A = -1, Z = -1$
Field voltage: 0.2701 mV
N_events: 100000





Schematic view of Forward Silicon detectors including 4th Si plane and first large aperture GEM stations in YZ (left) and XZ (right) projections.

Introduction to Alignment



$$\Delta S^2 = (x - x_0)^2 + (y - y_0)^2$$

$$\chi^2 = \sum_{i=1}^{n_{track}} \sum_{j=1}^{n_{det}} \frac{[\Delta S_{ij}(u_{ij}, \alpha_i^t, \alpha_j^a)]^2}{\sigma_j^2}$$

Alignment for x and y

$$\mathbf{Ax} = \mathbf{B}$$

$$\Delta S_{ij} = u_{ij} - A_i z - B_i + du_j$$

$$\alpha_i = A_i, \quad i = 1, \dots, n_{tr}$$

$$\alpha_i = B_i, \quad i = n_{tr} + 1, \dots, 2n_{tr}$$

$$\alpha_i = du_j, \quad i = 2n_{tr} + 1, \dots, 2n_{tr} + n_{det} - 2$$

$N_d = 6$ - number of detectors
 $N_t = 5$ - number of tracks
 $\alpha_1, \dots, \alpha_{10}$ - parameters of tracks
 $\alpha_{11}, \dots, \alpha_{14}$ - alignment parameters of the detectors

S_2 0 0 0 0 0 S_2 0 0 0 0 0 S_2 0 0 0 0 0 S_2 0 0 0 0 0 S_2	S_1 0 0 0 0 0 S_1 0 0 0 0 0 S_1 0 0 0 0 0 S_1 0 0 0 0 0 S_1	Z_2 Z_3 Z_4 Z_5 Z_2 Z_3 Z_4 Z_5 Z_2 Z_3 Z_4 Z_5 Z_2 Z_3 Z_4 Z_5 Z_2 Z_3 Z_4 Z_5
S_1 0 0 0 0 0 S_1 0 0 0 0 0 S_1 0 0 0 0 0 S_1 0 0 0 0 0 S_1	N_d 0 0 0 0 0 N_d 0 0 0 0 0 N_d 0 0 0 0 0 N_d 0 0 0 0 0 N_d	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
Z_2 Z_2 Z_2 Z_2 Z_2 Z_3 Z_3 Z_3 Z_3 Z_3 Z_4 Z_4 Z_4 Z_4 Z_4 Z_5 Z_5 Z_5 Z_5 Z_5	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	N_t 0 0 0 0 N_t 0 0 0 0 N_t 0 0 0 0 N_t

1. Volker Blobel, Claus Kleinwort. A New method for the high precision alignment of track detectors (<https://arxiv.org/abs/hep-ex/0208021>)
2. https://www.desy.de/~kleinwrt/MP2/doc/html/draftman_page.html

Alignment for x, y and z

$$\Delta S_{ij}^2 = (x - x_0)^2 + (y - y_0)^2$$

$$x = A_x z + B_x, \quad y = A_y z + B_y$$

$$x = A_x(z + dz) + B_x$$

$$x = A_x z + A_x dz + B_x$$

$$x = (A_x^0 + dA_x)(z + dz) + B_x,$$

$$y = (A_y^0 + dA_y)(z + dz) + B_y$$

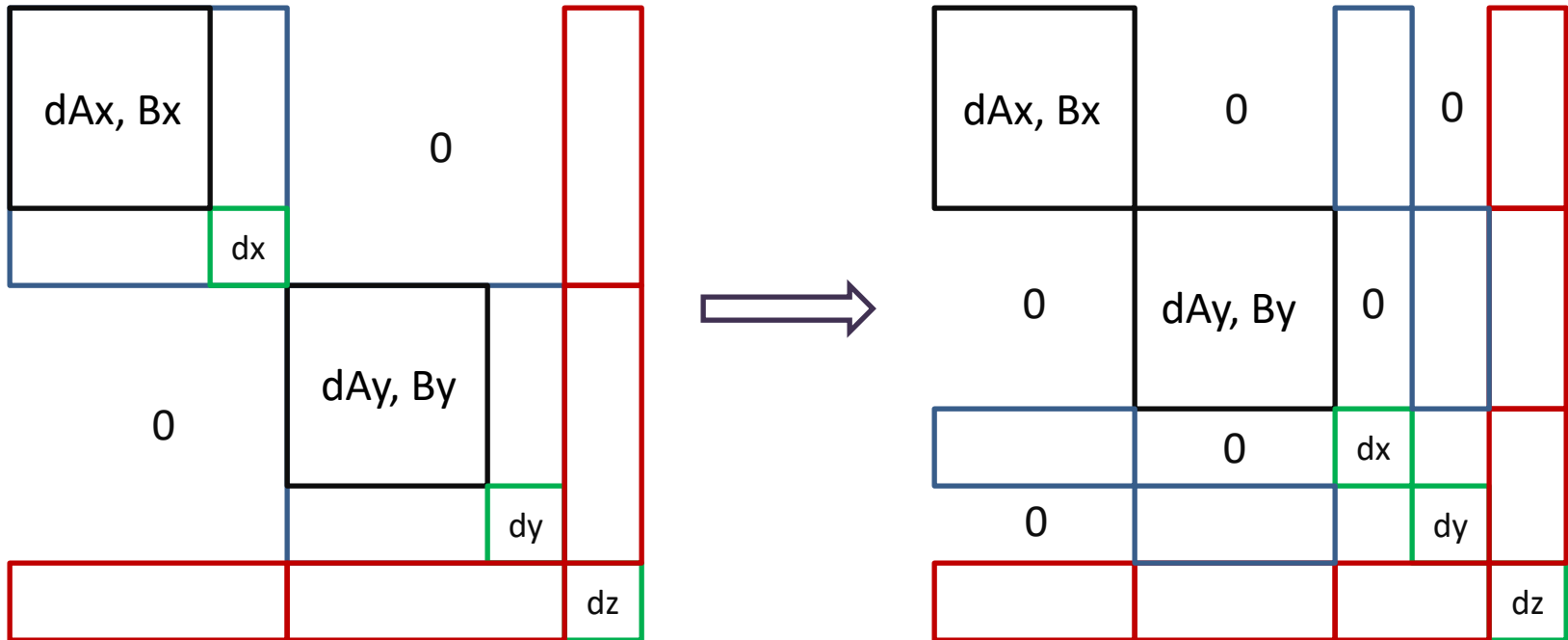
$$x = A_x^0 z + dA_x z + A_x^0 dz + dA_x dz + B_x$$

Alignment for x, y and z

dAx _i					Bx _i					dx _i			
S ₂	0	0	0	0	S ₁	0	0	0	0	Z ₂	Z ₃	Z ₄	Z ₅
0	S ₂	0	0	0	0	S ₁	0	0	0	Z ₂	Z ₃	Z ₄	Z ₅
0	0	S ₂	0	0	0	0	S ₁	0	0	Z ₂	Z ₃	Z ₄	Z ₅
0	0	0	S ₂	0	0	0	0	S ₁	0	Z ₂	Z ₃	Z ₄	Z ₅
0	0	0	0	S ₂	0	0	0	0	S ₁	Z ₂	Z ₃	Z ₄	Z ₅
S ₁	0	0	0	0	N _d	0	0	0	0	1	1	1	1
0	S ₁	0	0	0	0	N _d	0	0	0	1	1	1	1
0	0	S ₁	0	0	0	0	N _d	0	0	1	1	1	1
0	0	0	S ₁	0	0	0	0	N _d	0	1	1	1	1
0	0	0	0	S ₁	0	0	0	0	N _d	1	1	1	1
Z ₂	Z ₂	Z ₂	Z ₂	Z ₂	1	1	1	1	1	N _t	0	0	0
Z ₃	Z ₃	Z ₃	Z ₃	Z ₃	1	1	1	1	1	0	N _t	0	0
Z ₄	Z ₄	Z ₄	Z ₄	Z ₄	1	1	1	1	1	0	0	N _t	0
Z ₅	Z ₅	Z ₅	Z ₅	Z ₅	1	1	1	1	1	0	0	0	N _t

$Ax_1^0 z_2$	$Ax_1^0 z_3$	$Ax_1^0 z_4$...
$Ax_2^0 z_2$	$Ax_2^0 z_3$	$Ax_2^0 z_4$...
...
Ax_1^0	Ax_1^0	Ax_1^0	...
Ax_2^0	Ax_2^0	Ax_2^0	...
...
$\sum_i Ax_i^0$	0
0	$\sum_i Ax_i^0$
...	...	$\sum_i Ax_i^0$...

Alignment for x, y and z



Principle of alignment

1. IMSL Fortran Library

(<https://www.imsl.com/products/imsl-fortran-libraries>)

2. Eigen

(https://eigen.tuxfamily.org/index.php?title=Main_Page)

3. Millepede-II

(https://www.desy.de/~kleinwrt/MP2/doc/html/draftman_page.html)