

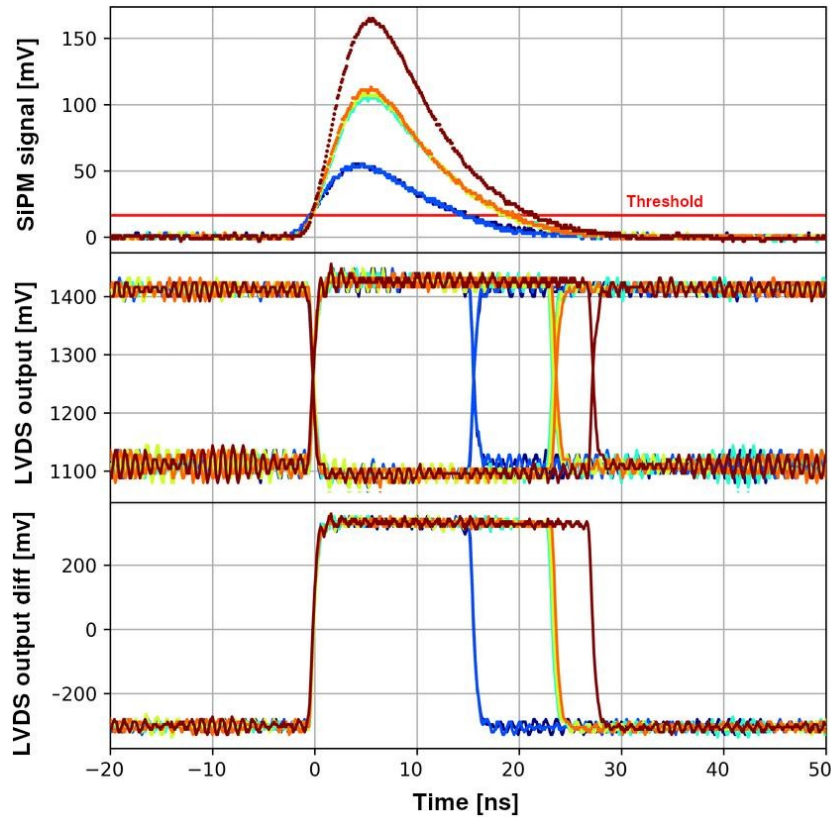
# Analytical description of signals from HGND scintillator cells with SiPM readout and results of the time resolution measurements

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on behalf of HGND team



11th BM@N Collaboration Meeting  
28–30 November 2023 LHEP JINR

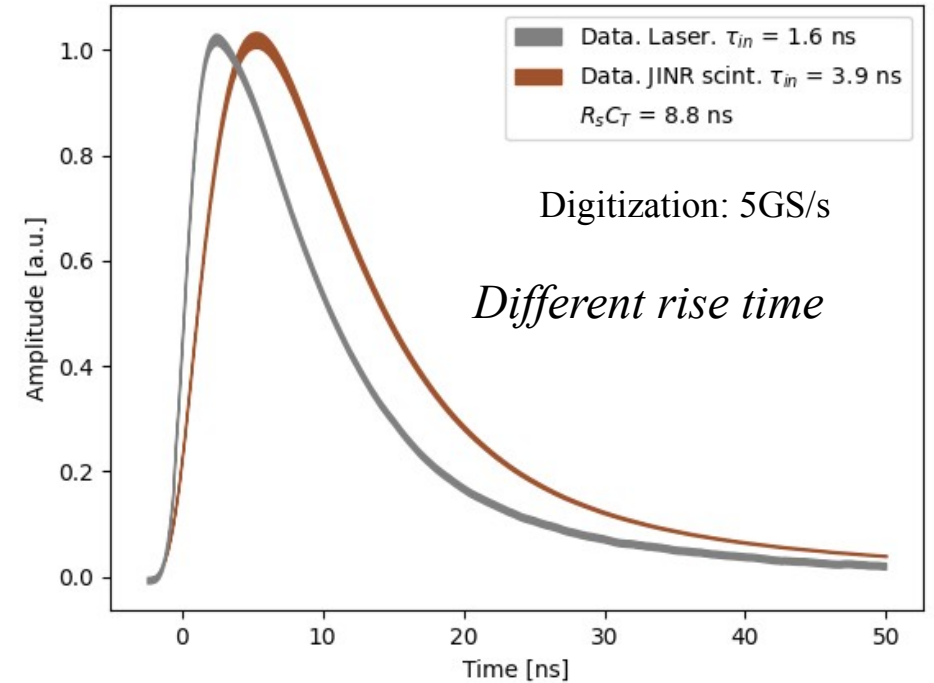
# Time & Amplitude determination in HGND



**Readout scheme**

1. Plastic scintillator light flash
2. SiPM EQR15 11-6060D-S
3. High-speed comparator with differential LVDS output
4. FPGA-based TDC (100 ps bin width)

= Response time + ToT



## Tasks

- Amplitude will be measured indirectly through ToT. It is necessary to convert ToT into amplitude
- It is necessary to correct for the time-amplitude dependence (slewing correction)
- Requires the ability to calibrate readout channels using an LED and recalculate calibration parameters to apply to scintillator signals
- Physical description of signals is required

SiPM: NDL EQR15 11-6060D-S

- Active area  $6 \times 6 \text{ mm}^2$
- Pixel size  $15 \times 15 \text{ }\mu\text{m}^2$
- Total pixels: 160 000
- PDE: 45%
- Gain:  $4 \times 10^5$



# Analytical description of light signals captured by SiPM: main behavior

$$N_{ph}(t) = N_{ph}^0 e^{-t/\tau_{in}}$$

$N_{ph}^0$  – initial number of photons,  $\tau_{in}$  – light decay constant.

**Solution 1** – Process as convolution of photoelectron current  $f(t)$  with SiPM impulse response function  $g(t)$

$$f(t) = I_{p.e.} = \eta e \frac{dN_{ph}}{dt} \quad g(t) = \frac{1}{R_s C_T} e^{-t/R_s C_T}$$

$\eta$  – PDE,  $e$  – electron charge,  $R_s$  – load resistance + low intrinsic SiPM resistance,  $C_T$  – total SiPM capacitance.

$$V(t) = R_s (f * g)(t) = -\frac{\eta e N_{ph}^0}{C_T \tau_{in}} \int_0^t e^{-\frac{x}{\tau_{in}}} e^{-\frac{t-x}{R_s C_T}} dx = \frac{\eta e N_{ph}^0 R_s}{R_s C_T - \tau_{in}} \left( e^{-t/R_s C_T} - e^{-t/\tau_{in}} \right). \quad (1)$$

**Solution 2** – Process as differential equation

$$\frac{dq}{dt} = I_{p.e.} + I_{recharge} \quad V_{bias} - R_s I_{recharge} = \frac{q}{C_T} \quad q(0) = C_T V_{bias}$$

$$V(t) = R_s I_{recharge} = \frac{\eta e N_{ph}^0 R_s}{R_s C_T - \tau_{in}} \left( e^{-t/R_s C_T} - e^{-t/\tau_{in}} \right). \quad (2)$$

# Analytical description of light signals captured by SiPM: addressing derivative discontinuity

- Phase shift to the fast exponent by a value

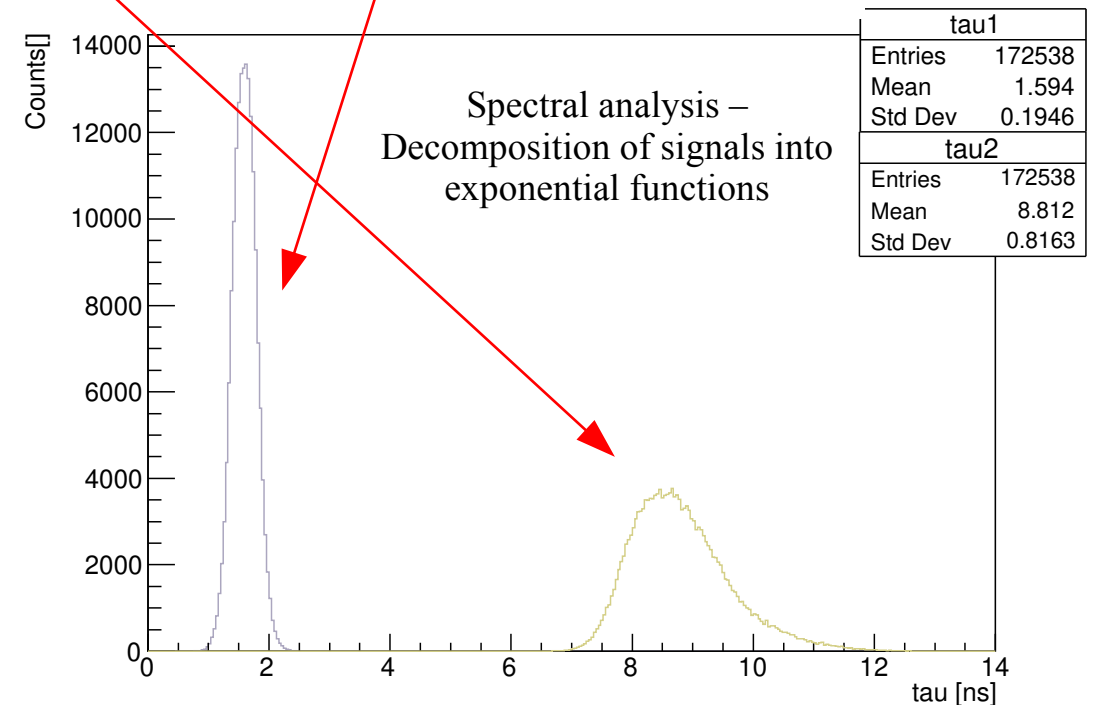
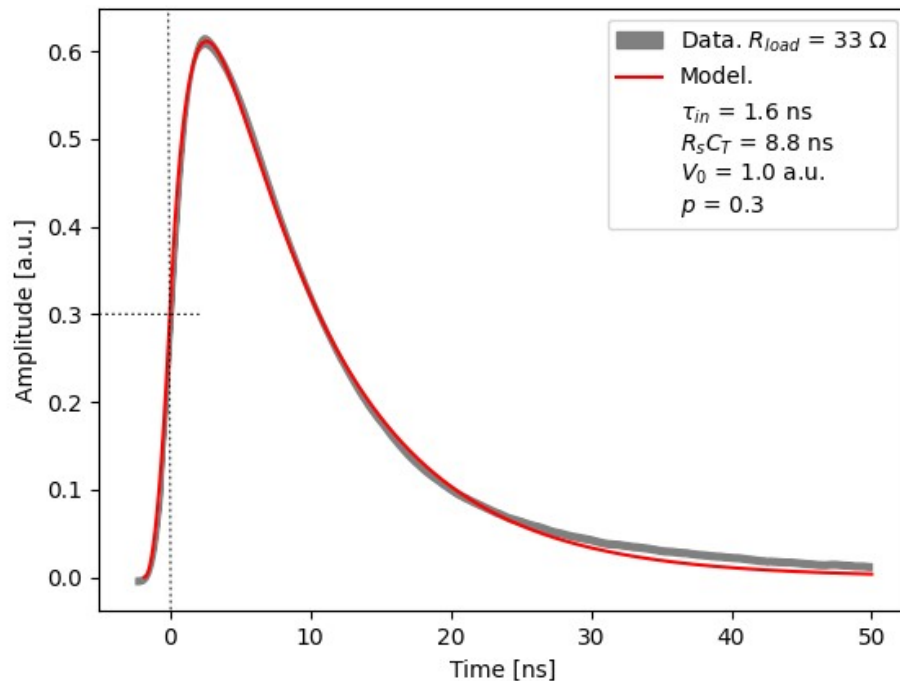
$$\tau_{in} \ln(1 - p)$$

- Match conditions with parabolic solution at time 0

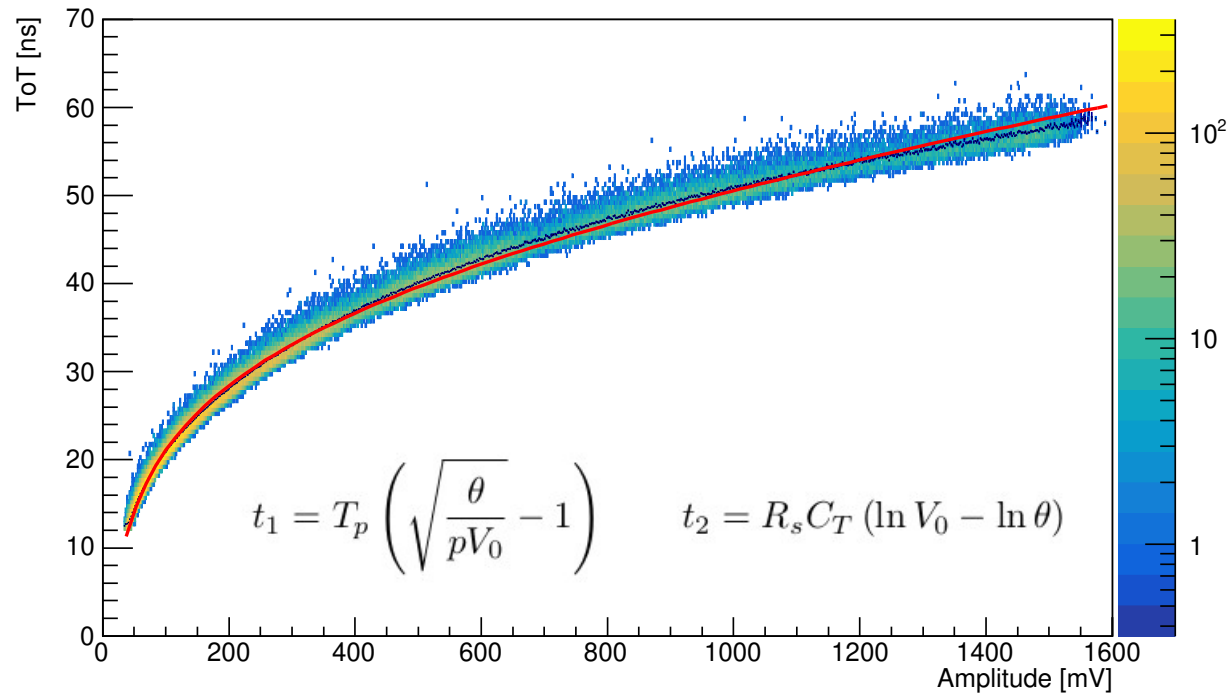
$$V_0 = \frac{\eta e N_{ph}^0 R_s}{R_s C_T - \tau_{in}} \quad T_p = \frac{2p\tau_{in} R_s C_T}{(1 - p)R_s C_T - \tau_{in}}$$

- Final form of analytic description

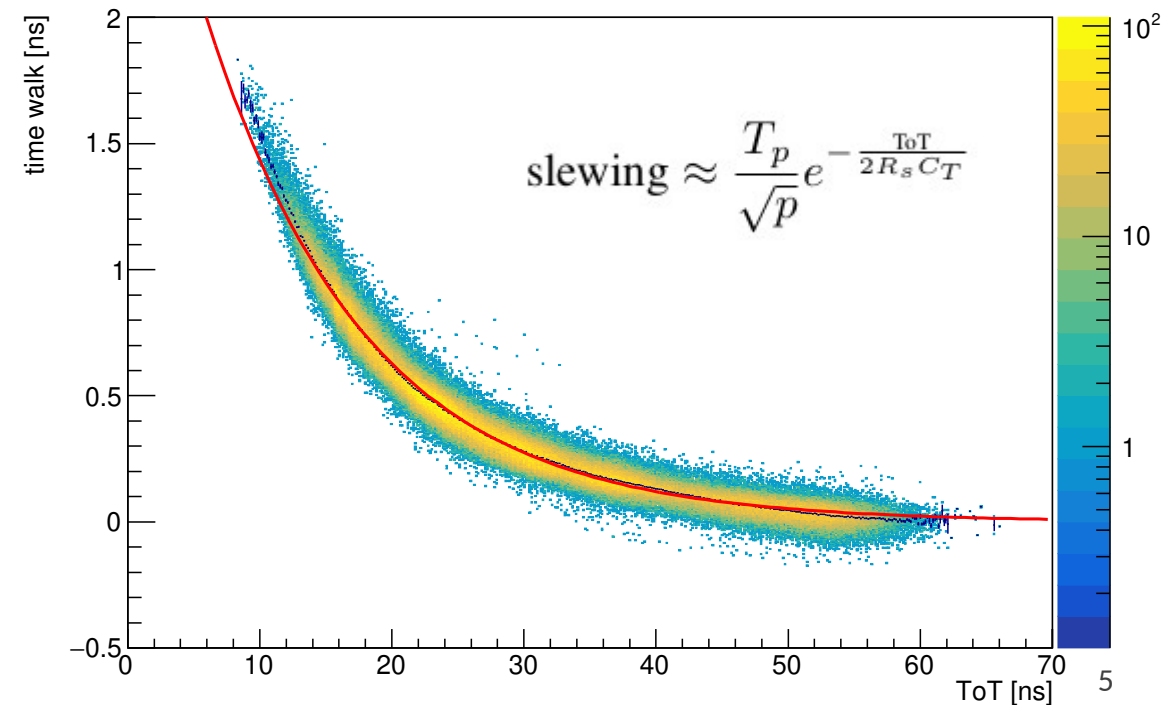
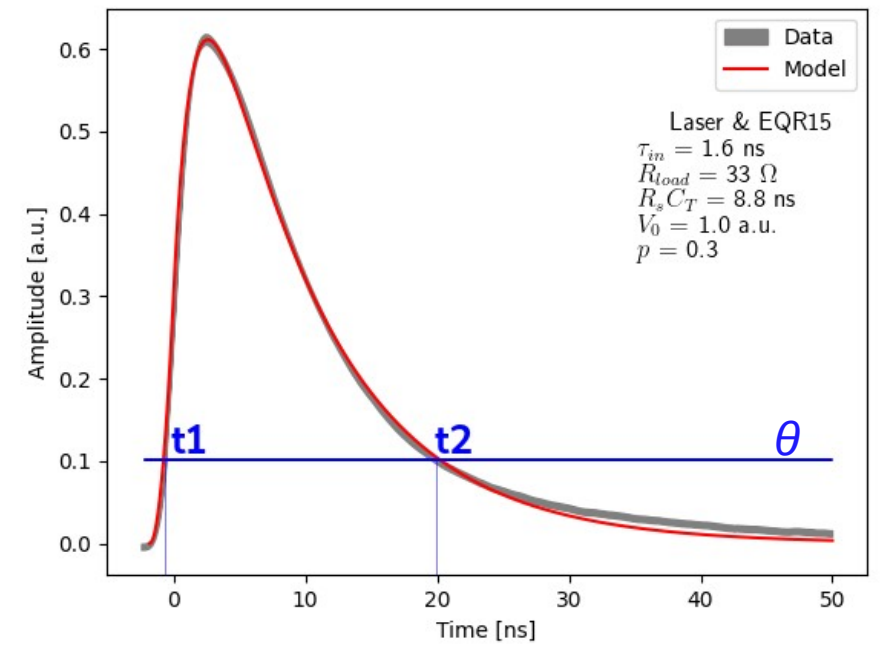
$$V(t) = \begin{cases} pV_0 \left( \frac{t}{T_p} + 1 \right)^2 & \text{if } -T_p < t < 0 \\ V_0 \left( e^{-\frac{t}{R_s C_T}} - (1 - p)e^{-\frac{t}{\tau_{in}}} \right) & \text{if } t \geq 0 \end{cases}$$



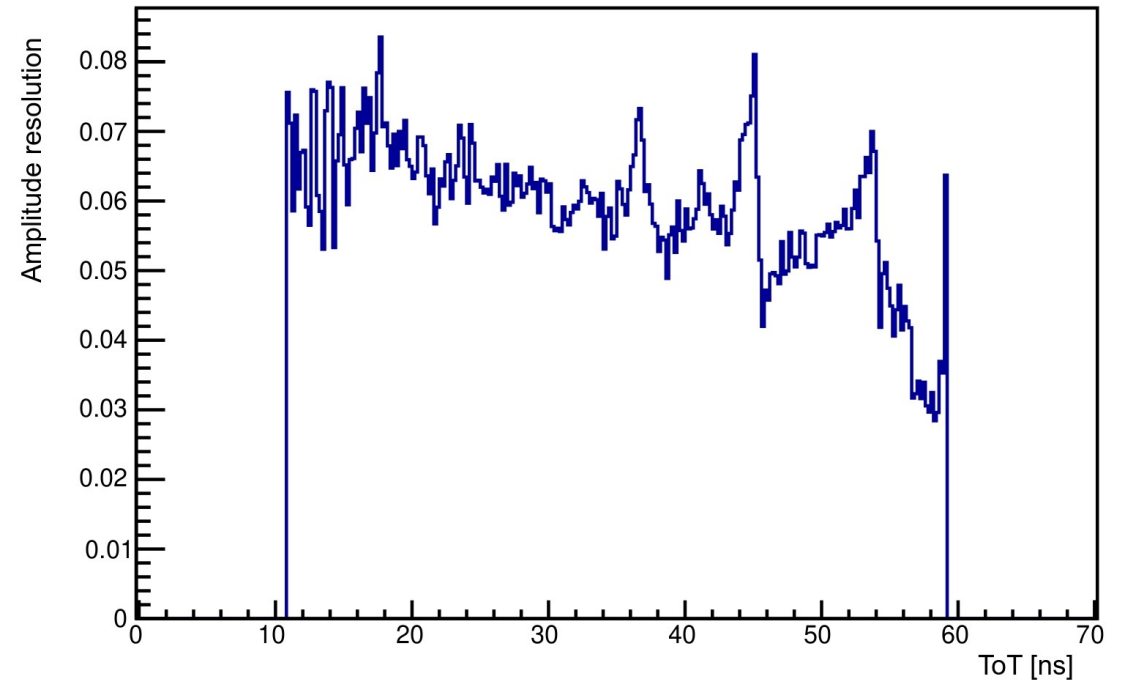
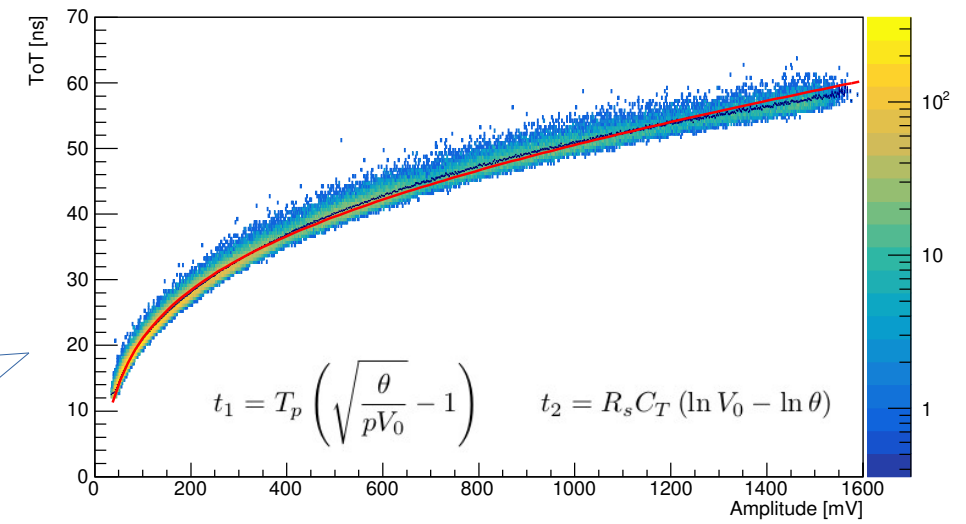
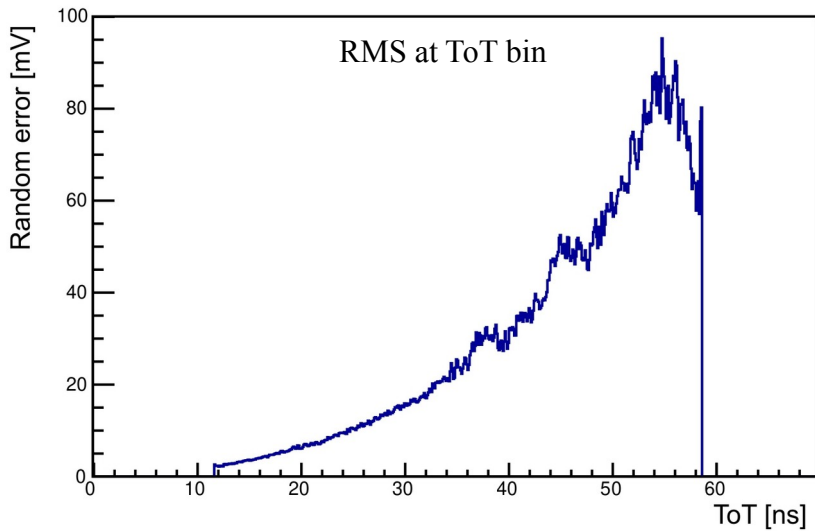
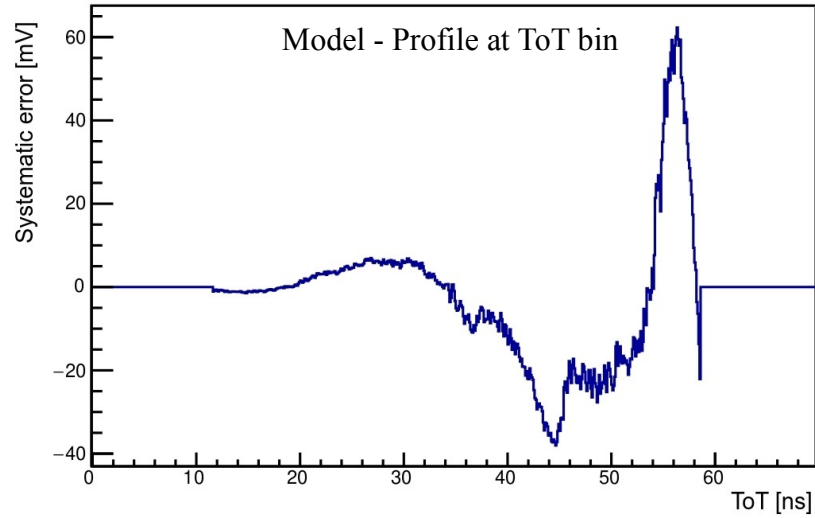
# Analytical description of light signals captured by SiPM: parametrisation of slewing and ToT



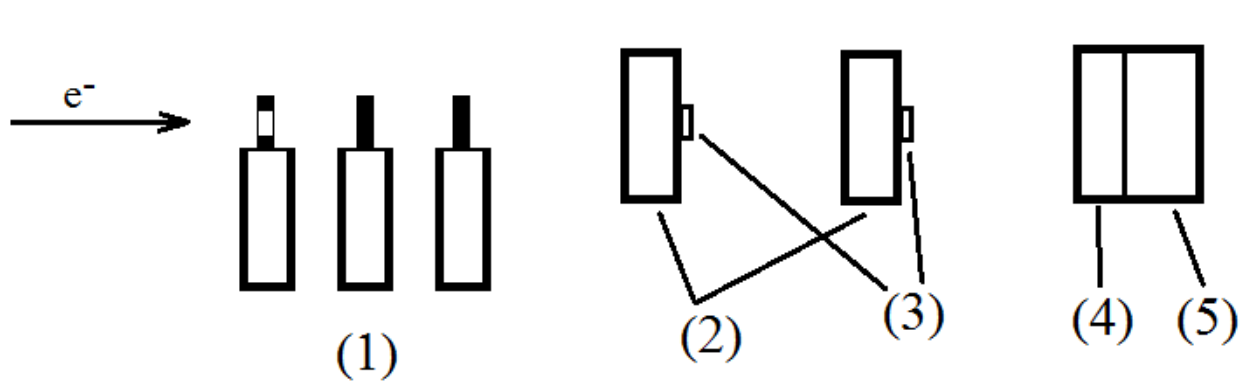
*Comparison of Laser data with model*



# Analytical description of light signals captured by SiPM: estimation of amplitude resolution



# Analytical description of light signals captured by SiPM: Results of beam tests



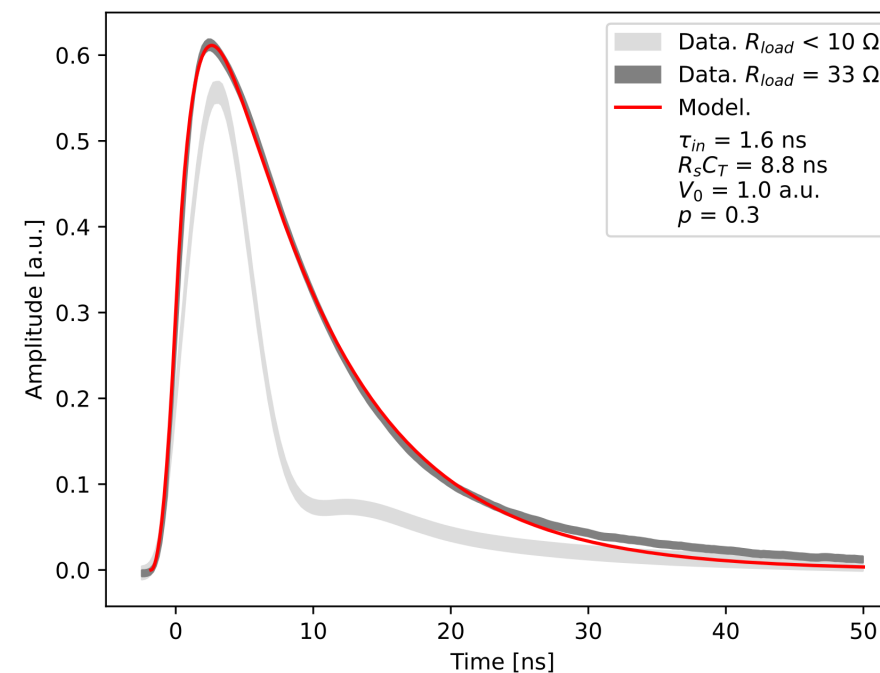
280 MeV electron beam of the "Pakhra" synchrotron (LPI, Troitsk)

- (1) Beam counters
- (2) Scintillator samples
- (3) SiPM
- (4) Quartz Cherenkov radiator
- (5) MCP PMT

Light source	Decay time [ns]	Time res. w/o corr. [ps]	Time resolution [ps]	Amplitude res. [%]
Laser	$1.6 \pm 0.2$	88	45	8
EJ-230 sc.	$2.8 \pm 0.5$	146	74	20
JINR sc.	$3.9 \pm 0.7$	261	117	16

# Conclusion and next steps

- The analytical description of ToT is based on physical principles - parameters of light sources and SiPM response.
- The electronics are tuned so as not to distort the smooth physical behavior. The load resistance is chosen to be large enough to cover the spurious response pulse of the silicon photomultiplier and small enough to avoid a long tail.
- Time resolution is significantly improved by applying slewing correction.
- It is possible to recalculate the calibration parameters taken from the LED for application to the light signals of a plastic scintillator (in the case of an undistorted SiPM impulse response).
- The method will be tested on larger amount of channels.



**Thank you for your attention!**



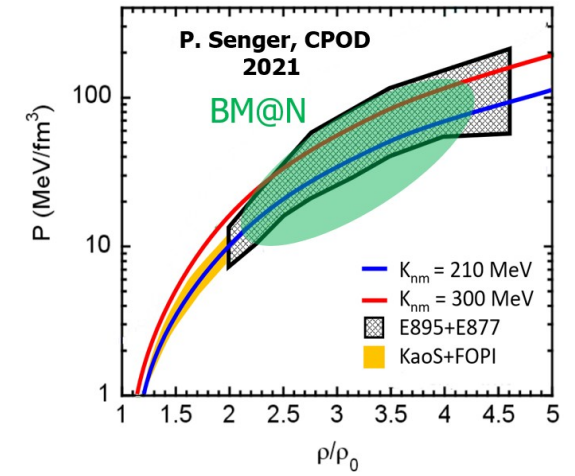
**BACKUP**

# New High-Granular Neutron detector of the BM@N experiment

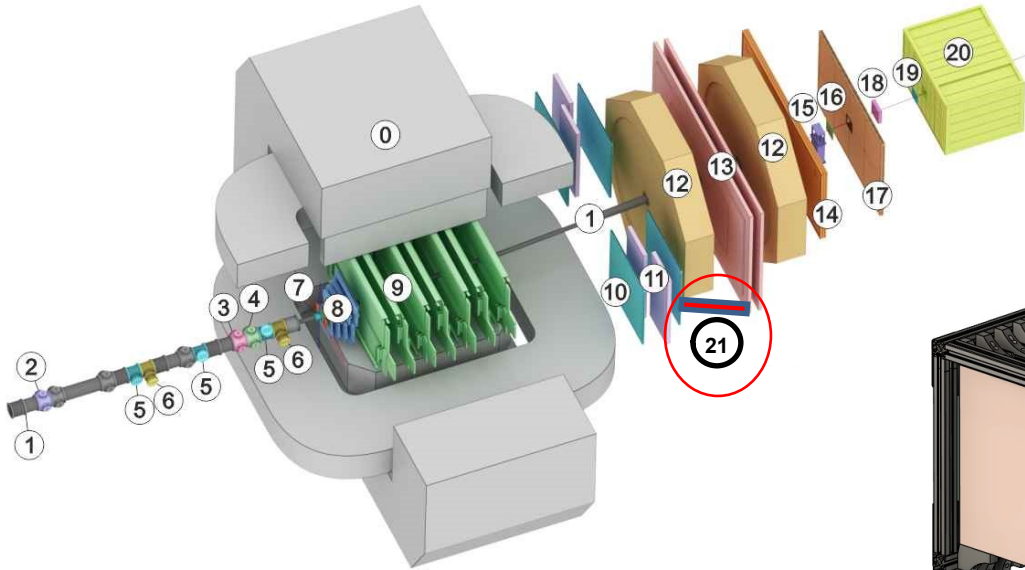
**Goal:** understanding the symmetry energy term of the EoS of strongly interacting matter in the uncovered energy region  $(2-4) \rho_0$

**How:** by calculating anisotropic neutron flow and extracting  $v_{1,2}^n / v_{1,2}^{ch}$

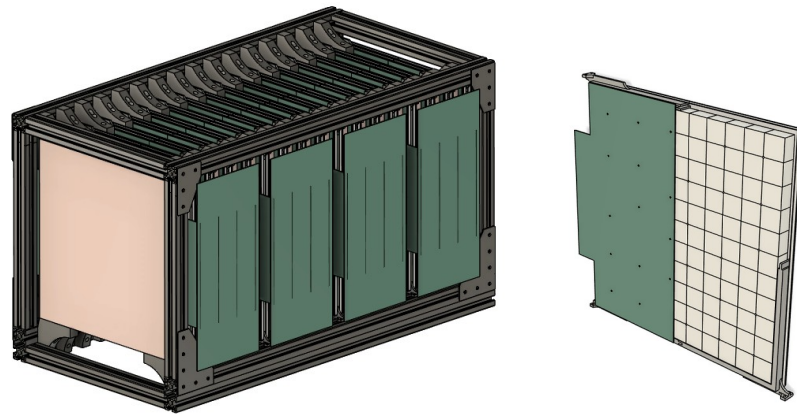
**Measure:** kinetic energy of neutrons by ToF



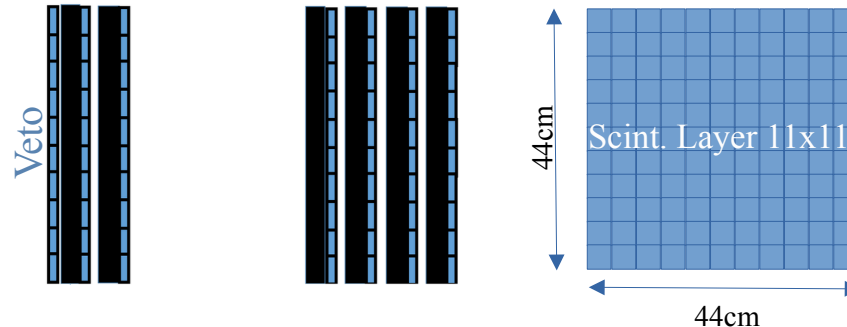
BM@N setup



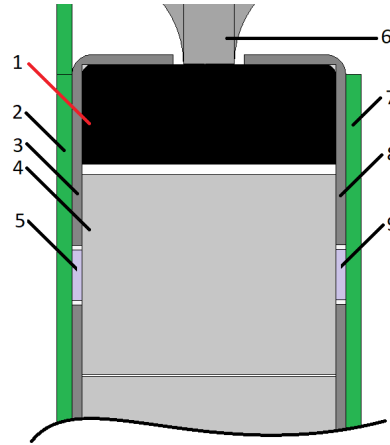
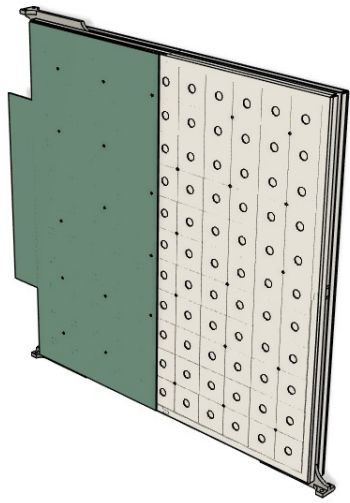
- |                               |                                 |
|-------------------------------|---------------------------------|
| ■ Magnet SP-41 (0)            | ■ TOF 700 (13)                  |
| ■ Vacuum Beam Pipe (1)        | ■ ScWall (14)                   |
| ■ BC1, VC, BC2 (2-4)          | ■ FD (15)                       |
| ■ SiBT, SiProf (5, 6)         | ■ Small GEM (16)                |
| ■ Triggers: BD + SiMD (7)     | ■ CSC 2x1.5 m <sup>2</sup> (17) |
| ■ FSD, GEM (8, 9)             | ■ Beam Profilometer (18)        |
| ■ CSC 1x1 m <sup>2</sup> (10) | ■ FQH (19)                      |
| ■ TOF 400 (11)                | ■ FHCAL (20)                    |
| ■ DCH (12)                    | ■ HGND (21)                     |



15 layers (Cu/Scint)



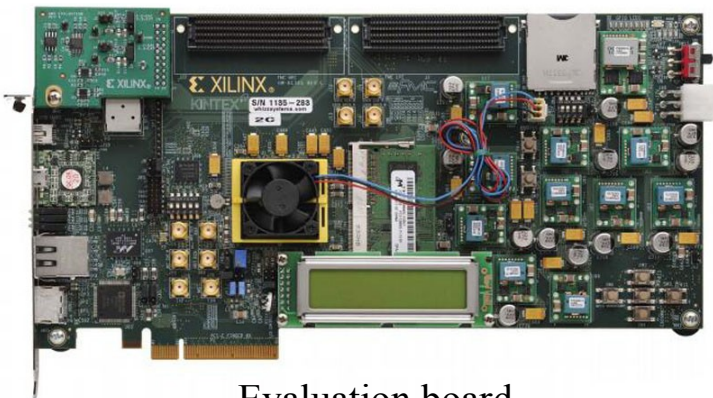
- Transverse size: 44 x 44 cm<sup>2</sup>
- number of layers: 15 + Veto
- total length of the HGND: ~ 95 cm (~3 λ<sub>in</sub>)
- structure of layer:
  - 3 cm Cu (absorber) + 2.5cm Scint. + 0.5cm (SiPM+FEE)
  - size of scintillation detectors (cells): 4x4x2.5 cm<sup>3</sup>
  - total number of cells: 1936
  - light readout: one SiPM 6x6 mm<sup>2</sup> per cell



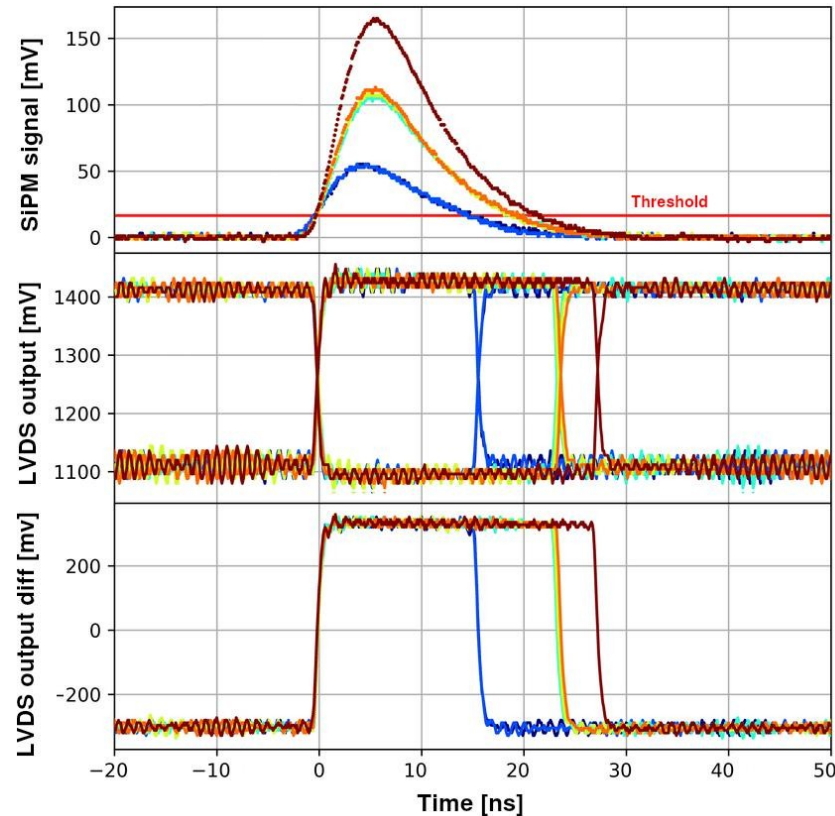
- 1 – the frame of layer case
- 2 – two PCBs with 55 and 66 SiPMs**
- 3 and 8 - aluminum plates for both sides of the frame case with cutouts for SiPMs and LEDs
- 4 – scintillator**
- 5 – SiPM**
- 6 – layer support bracket
- 7 – LED PCB
- 9 – LED**

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Evaluation board  
Xilinx Kintex 7



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$$= \text{Response time} + \text{ToT}$$

Why do we need analytical description of signals?

- Need to correct for time-amplitude dependence
- Need the ability to calibrate readout channels with LED and recalculate calibration parameters to apply to scintillator signals