

Centrality determination in run8

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Motivation for centrality determination

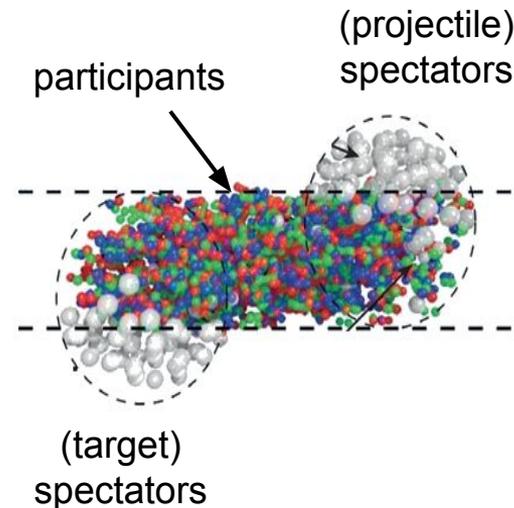
- Evolution of matter produced in heavy-ion collisions depends on its initial geometry

- **Goal of centrality determination:**

map (on average) the collision geometry parameters
to experimental observables (centrality estimators)

- Centrality class S_1 - S_2 : group of events corresponding to a given fraction (in %) of the total cross section:

$$C_S = \frac{1}{\sigma_{inel}^{AA}} \int_{S_1}^{S_2} \frac{d\sigma}{dS} dS$$



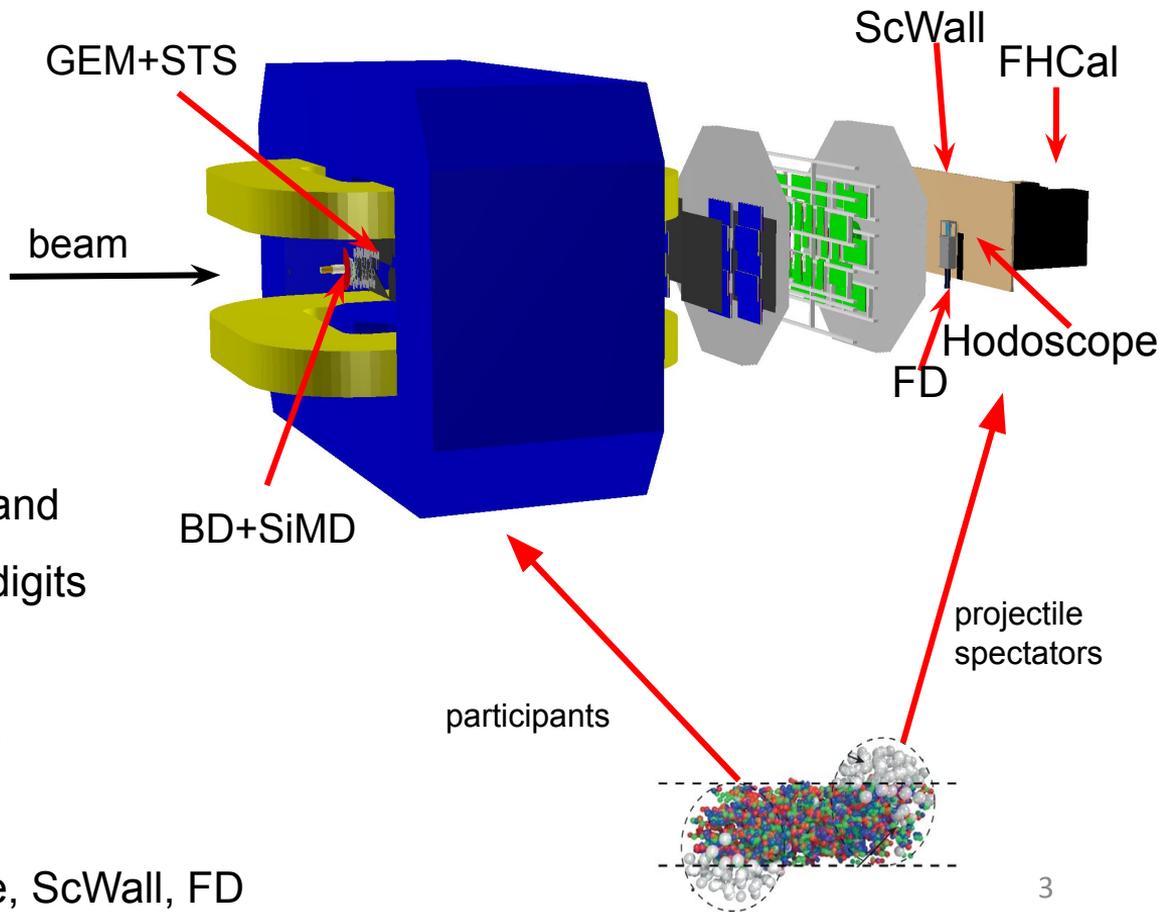
BM@N subsystems for centrality determination

Data:

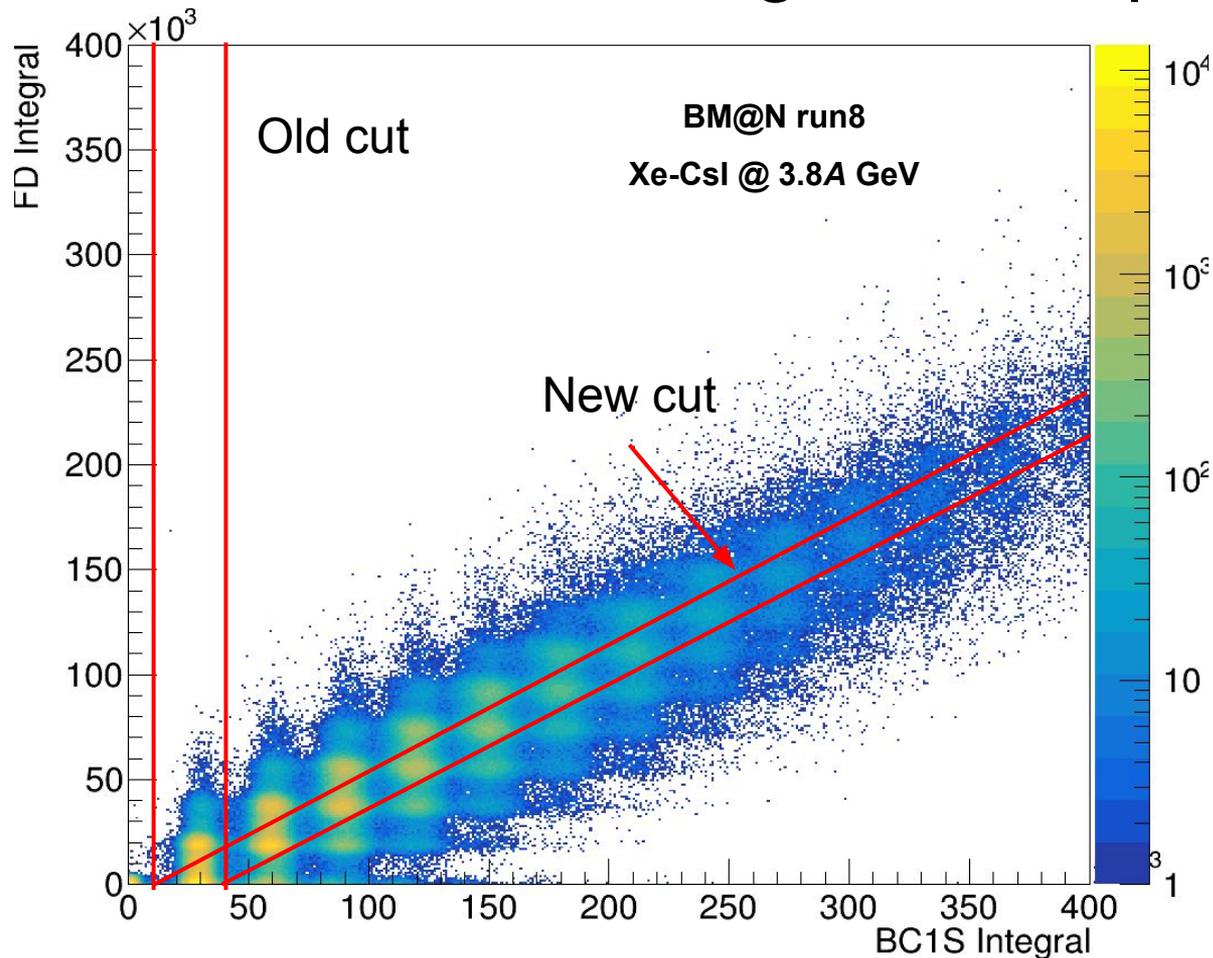
- run8 Xe-Csl @3.8A GeV
- CCT2
- $v_{tx}Chi2/v_{tx}Ndf > 0.1$
- $10000 < BC1Integral < 40000$
(old cut)
- or
- BC1Integral VS FDIntegral cut and
Graphic cut for N_{tracks} and STS digits
(new cuts)

Subsystems

- Participants: **Tracking system**
GEM+STS, BD, SiMD
- Spectators: FHCaI, Hodoscope, ScWall, FD



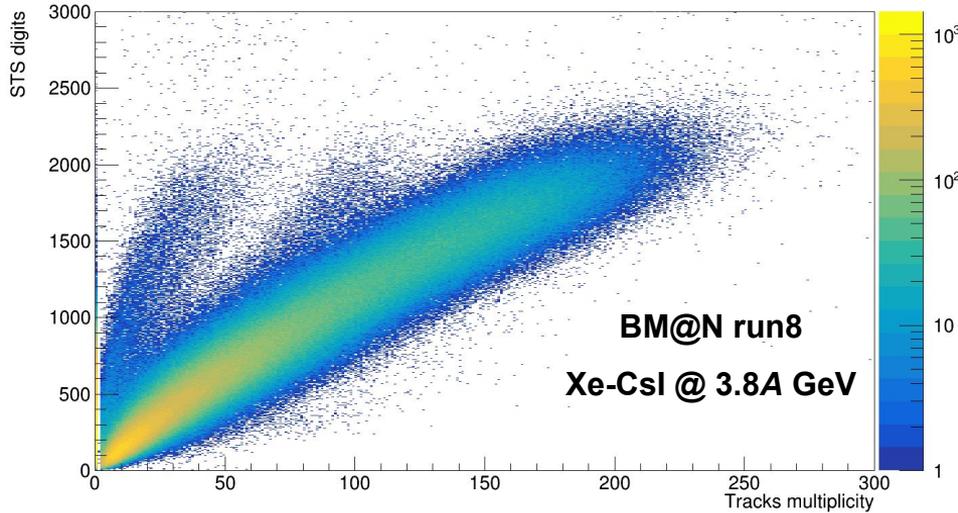
BC1 Integral cut improvement



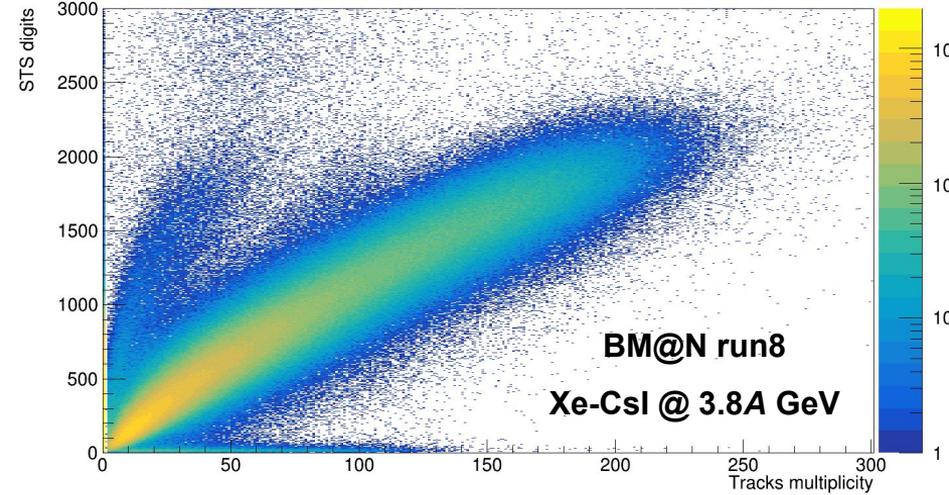
- Suggestions by S.Sedykh:
- New cut saves all events where only one collision occurs
- Difference: 23% \longrightarrow 43% of all events

Additional graphic cut

BC1 old cut

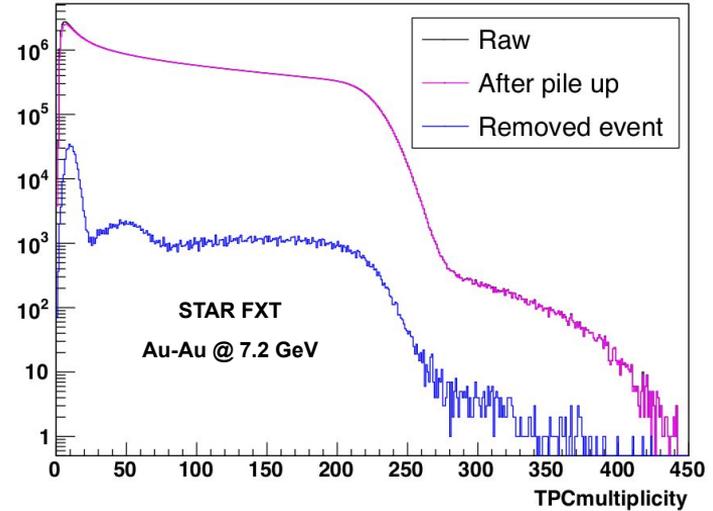
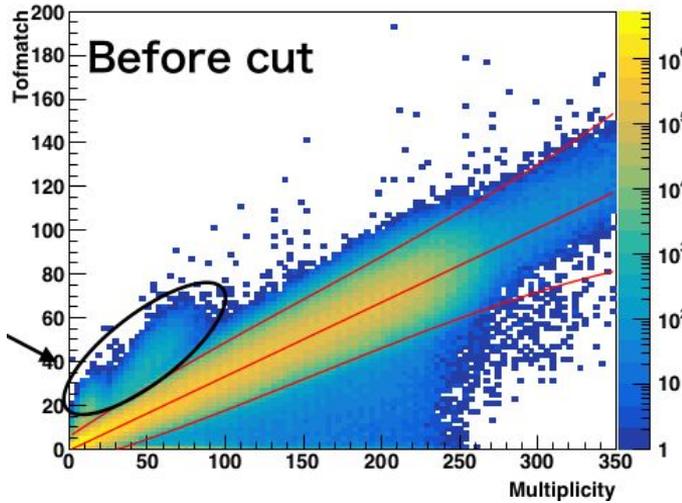


BC1 new cut



- There are some additional structures of events with unusual behaviour which may affect physical results
- Those events can be declined using graphic cut

Additional graphic cut

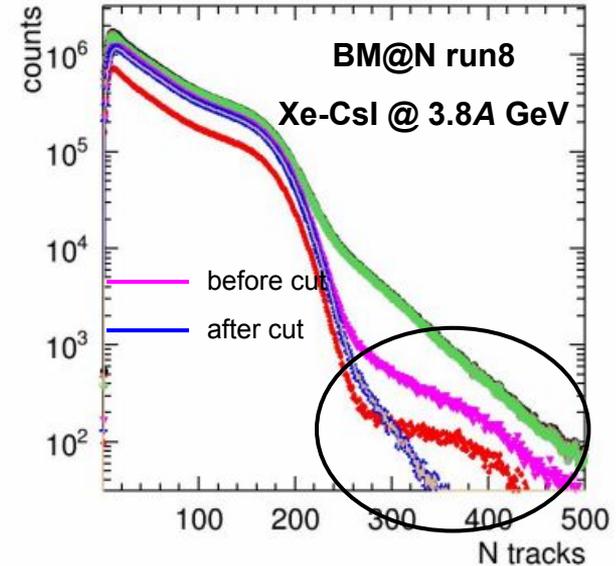
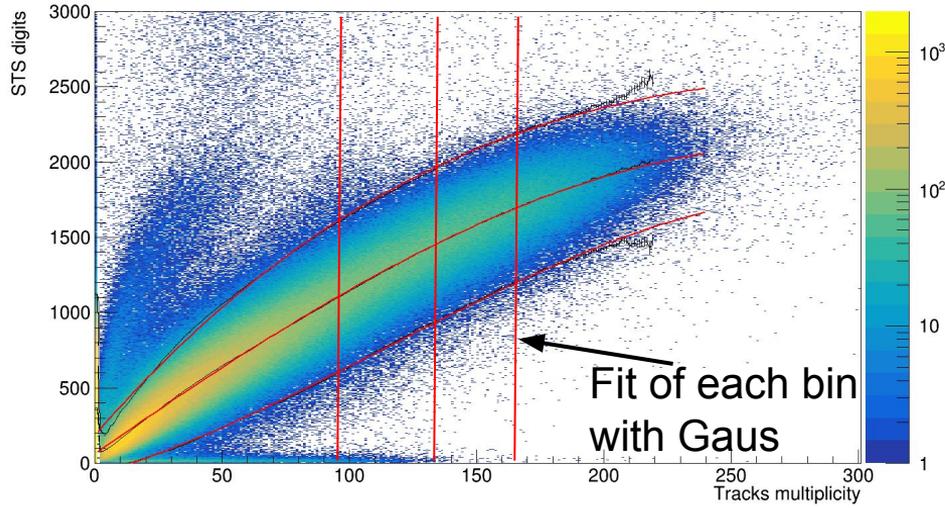


results from STAR by K.Okubo

- In the STAR's case number of tracks matched with TOF were used to reject events with unusual behaviour

Additional graphic cut

BC1 new cut



see talk by A.Demanov

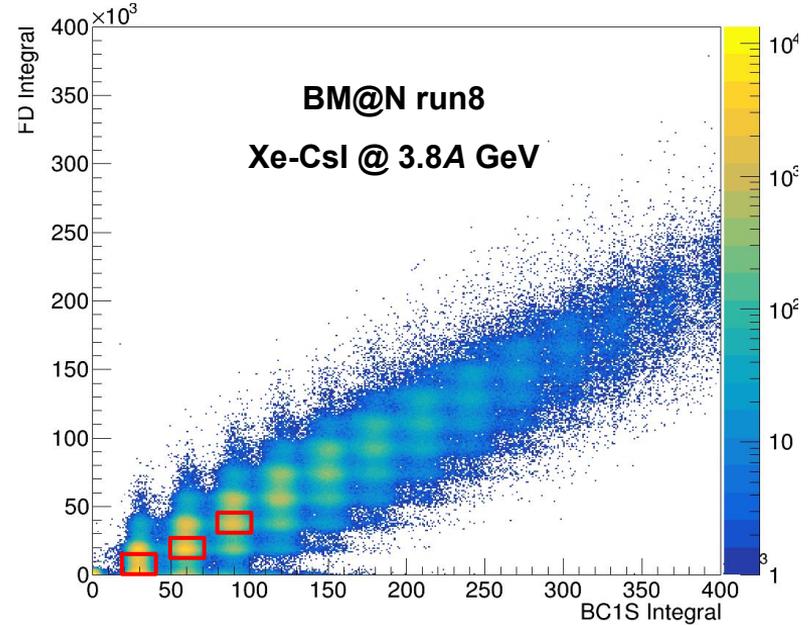
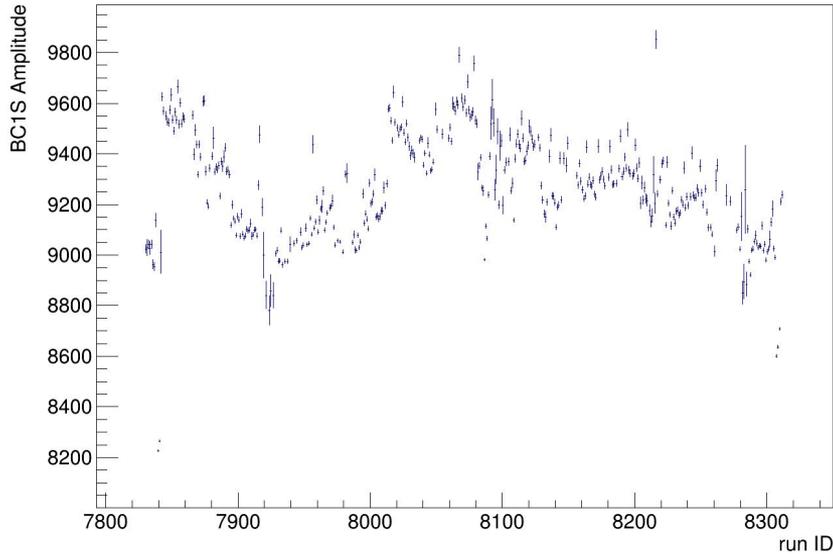
- Graphic cut was performed to throw out all events with unusual behaviour:

$$STS_{\max}(N_{\text{tracks}}) = 4.6e-05 * N^3 - 0.052 * N^2 + 19.4 * N + 188 \quad (\text{mean} + 3\sigma)$$

$$STS_{\min}(N_{\text{tracks}}) = -9.6e-05 * N^3 + 0.033 * N^2 + 4.8 * N - 74 \quad (\text{mean} - 3\sigma)$$

- Difference: 23% \longrightarrow 41% of all events

Future improvements



- Calibrate BC1 Amplitude over all runs to improve FD vs BC1 Integrals correlation
- Use areas of each peak instead of line on this correlation
- Finally, we should adjust before/after protection window for physics analysis

Centrality determination based on Monte-Carlo sampling of produced particles

For **multiplicity of produced particles** used in HADES, CBM, NA61/SHINE

Get $(N_{\text{part}}, N_{\text{coll}})$ from MC-Glauber

Calculate $N_a = fN_{\text{part}} + (1-f)N_{\text{coll}}$

Sample multiplicity of produced particles (S_i) N_a times from NBD (μ, k)

Result: total S_{tot}

MC-Glauber distribution

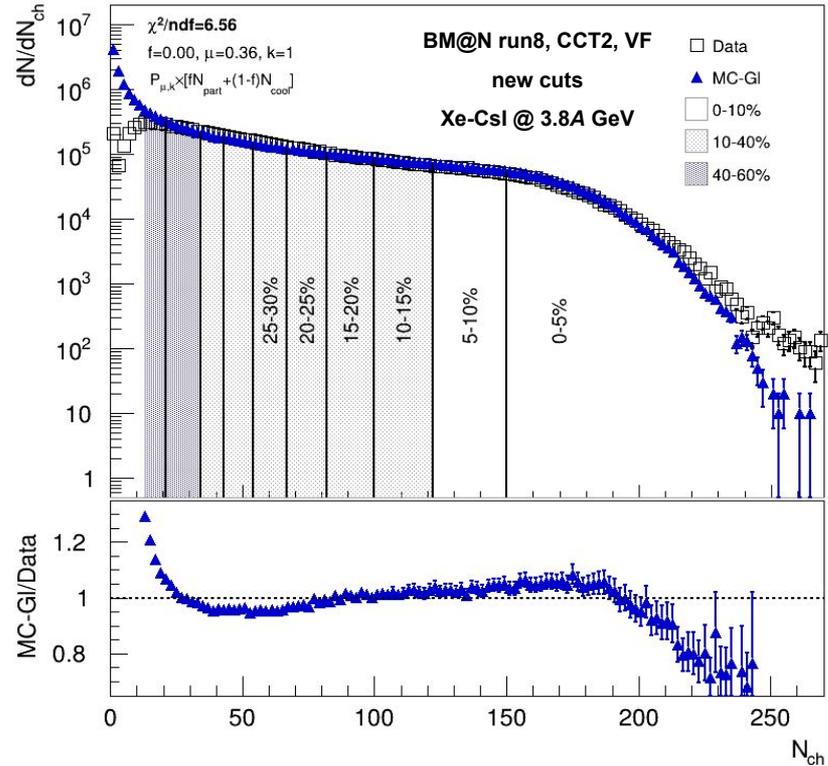
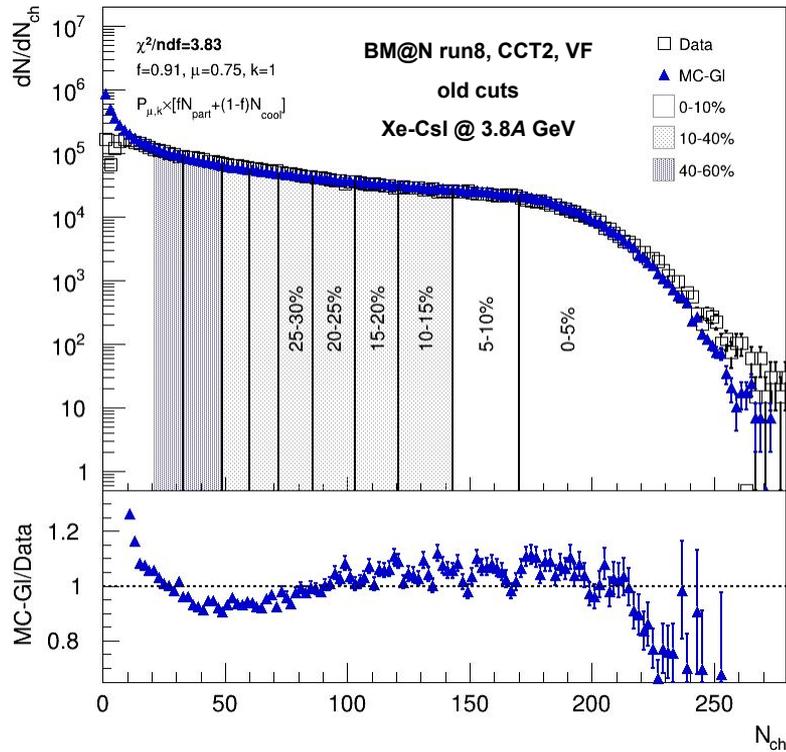
Full Monte-Carlo (real data) distribution

Evaluate χ^2 between $dN/dE_{\text{MC/data}}$ and dN/dE_{Gl}

Scan phase space of parameters to find their values for minimum of χ^2

Extract relation between geometry parameters and centrality estimator

Comparison with older results ($E_{\text{kin}}=3.8 \text{ GeV}$)



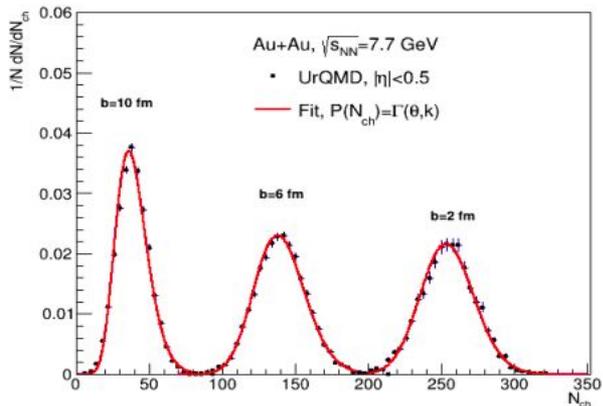
- Glauber fit improved in comparison with previous results
- CCT2 has good efficiency up to 60% centrality
- New centrality classes is used in analysis (see talk by M.Mamaev)

The Bayesian inversion method (Γ -fit): main assumptions

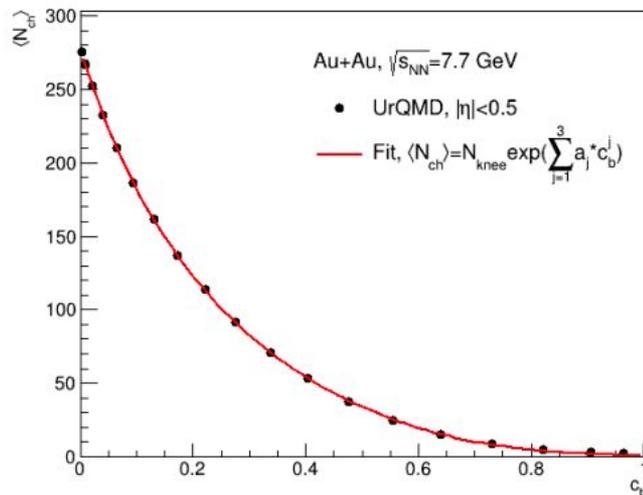
- Relation between multiplicity N_{ch} and impact parameter b is defined by the fluctuation kernel:

$$P(N_{ch}|c_b) = \frac{1}{\Gamma(k(c_b))\theta^k} N_{ch}^{k(c_b)-1} e^{-N_{ch}/\theta}$$

$$c_b = \int_0^b P(b') db' \simeq \frac{\pi b^2}{\sigma_{inel}} \quad \text{-- centrality based on impact parameter}$$



The results of fitting the multiplicity distribution for a fixed impact parameter



The dependence of the average value of multiplicity on centrality and the results of its fit

$$\frac{\sigma^2}{\langle N_{ch} \rangle} = \theta \simeq const$$

$$\langle N_{ch} \rangle = N_{knee} \exp\left(\sum_{j=1}^3 a_j c_b^j\right), \quad k = \frac{\langle N_{ch} \rangle}{\theta}$$

Five fit parameters

N_{knee}, θ, a_j

Reconstruction of b

- Normalized multiplicity distribution $P(N_{ch})$

$$P(N_{ch}) = \int_0^1 P(N_{ch}|c_b)dc_b$$

- Find probability of b for fixed range of N_{ch} using Bayes' theorem:

$$P(b|n_1 < N_{ch} < n_2) = P(b) \frac{\int_{n_1}^{n_2} P(b|N_{ch})dN_{ch}}{\int_{n_1}^{n_2} P(N_{ch})dN_{ch}}$$

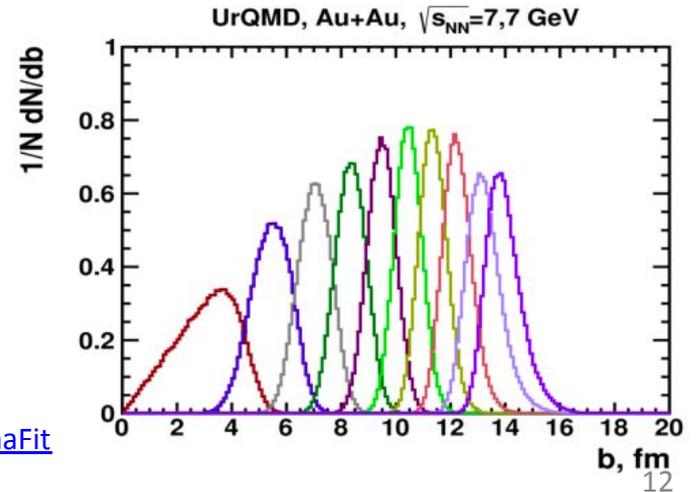
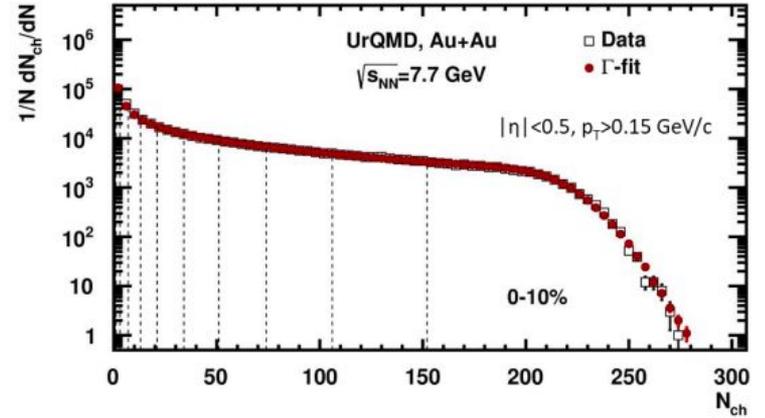
- The Bayesian inversion method consists of 2 steps:**

- Fit normalized multiplicity distribution with $P(N_{ch})$
- Construct $P(b|N_{ch})$ using Bayes' theorem with parameters from the fit

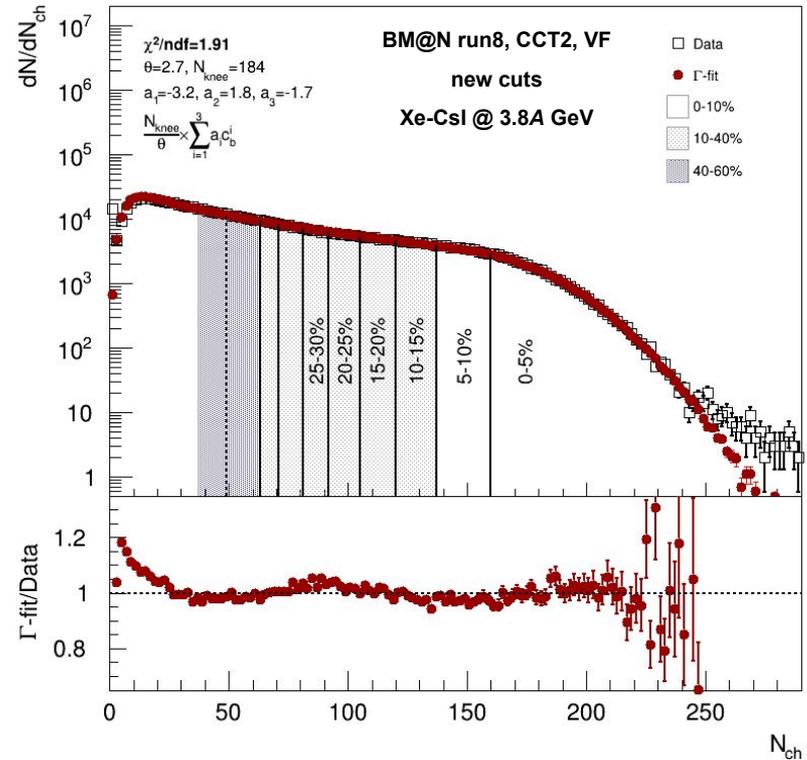
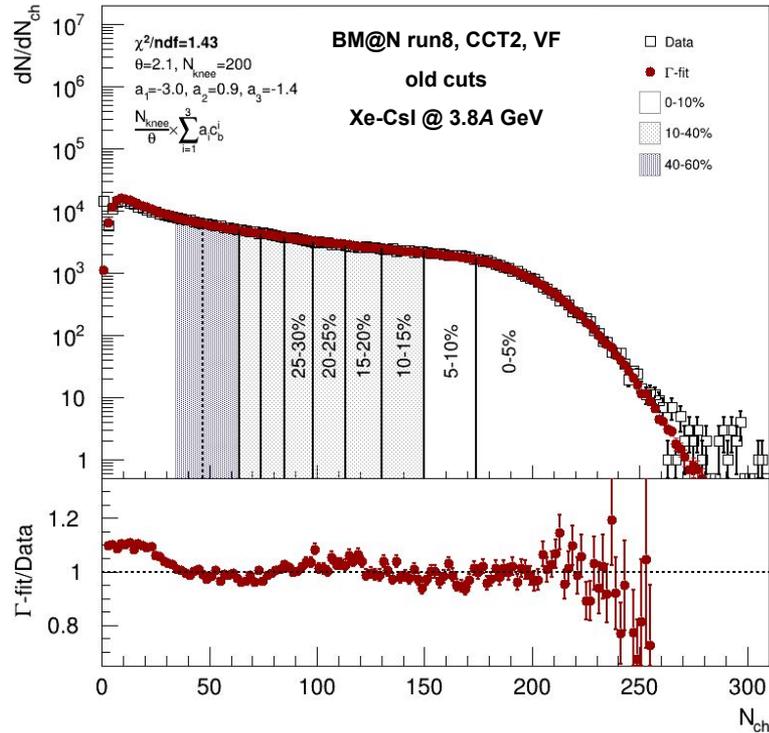
R. Rogly, G. Giacalone and J. Y. Ollitrault, Phys.Rev. C98 (2018) no.2, 024902

Implementation for MPD and BM@N by D. Idrisov: <https://github.com/Dim23/GammaFit>

Example of application in MPD: P. Parfenov et al., Particles 4 (2021) 2, 275-287

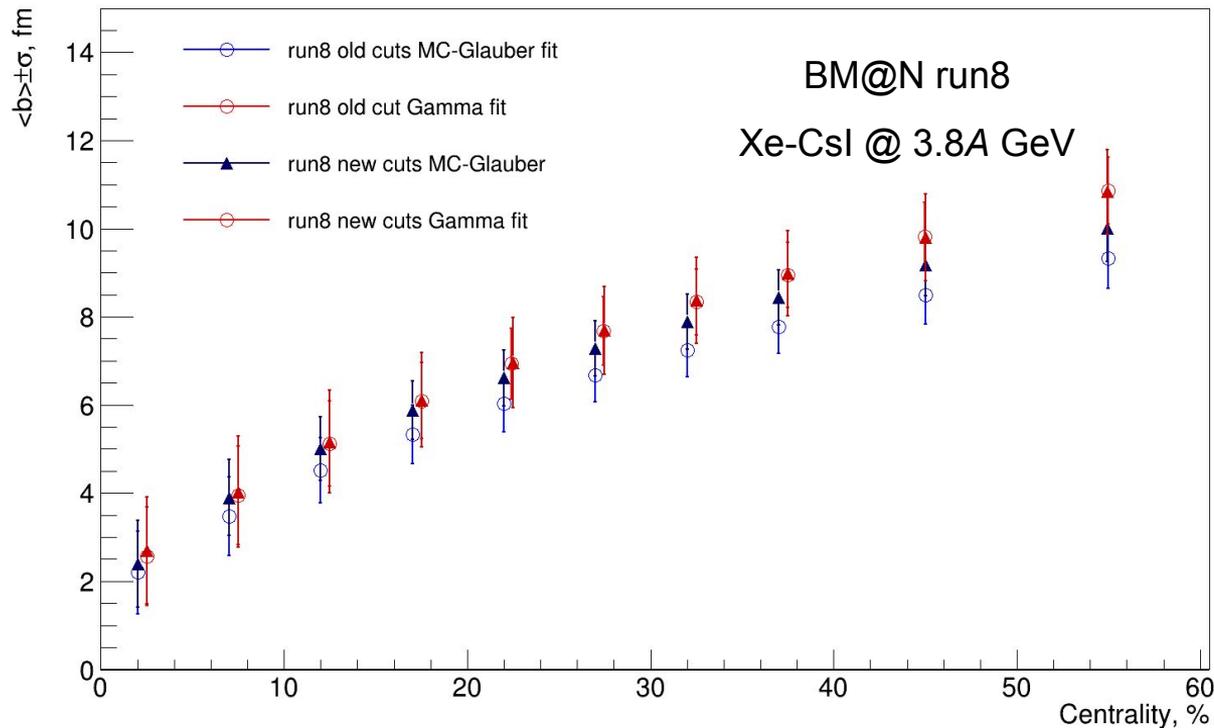


Comparison with older results ($E_{\text{kin}}=3.8 \text{ GeV}$)



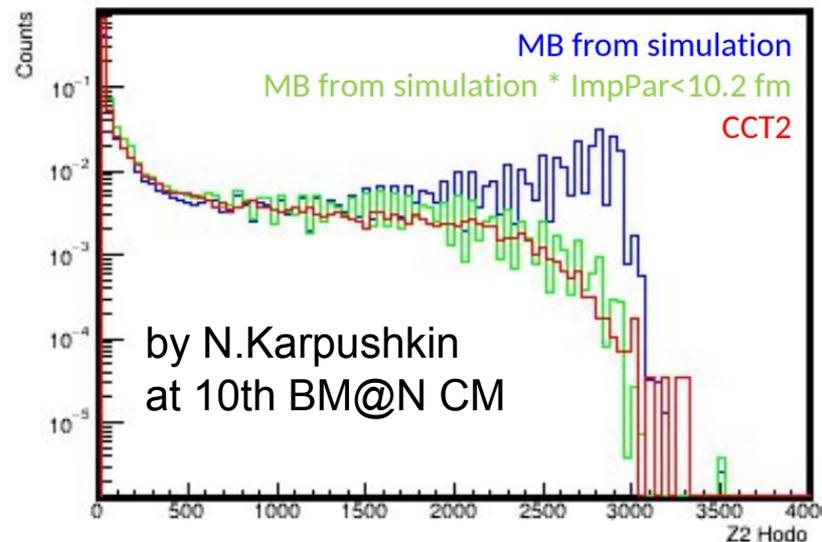
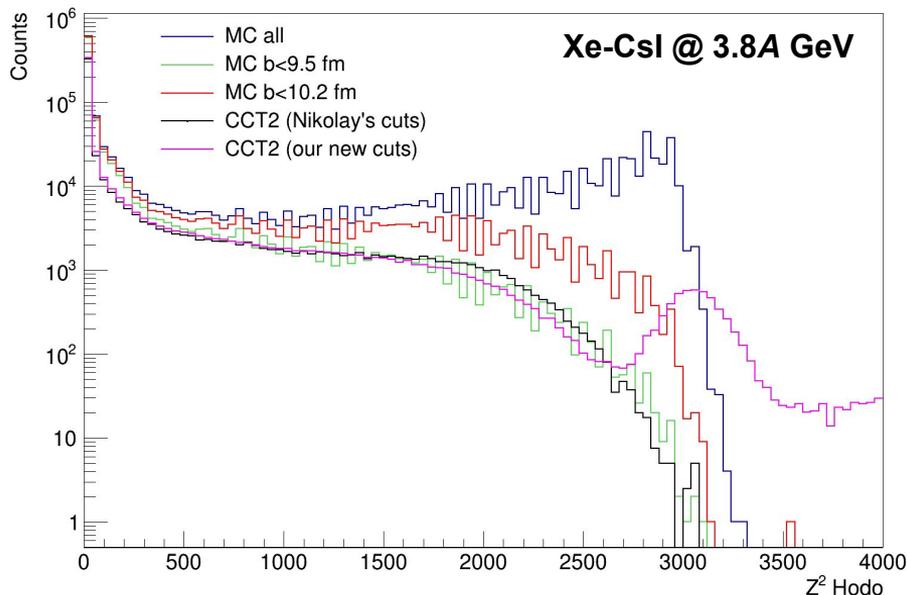
- For the new cuts fit also a little bit better
- These classes can be used during physics analysis
- Trigger efficiency at the peripheral events should be taken into account

Comparison between impact parameter distributions



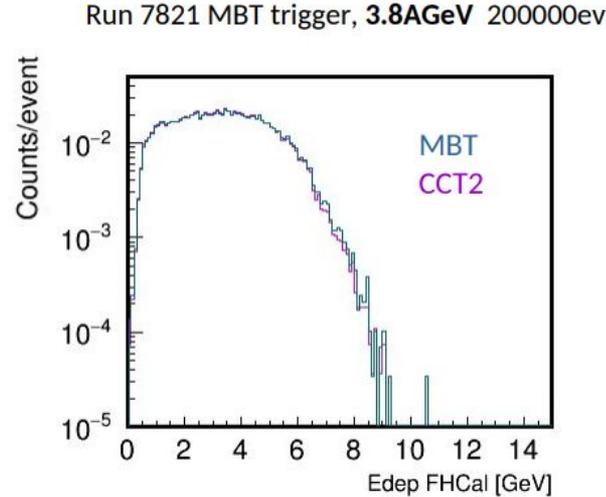
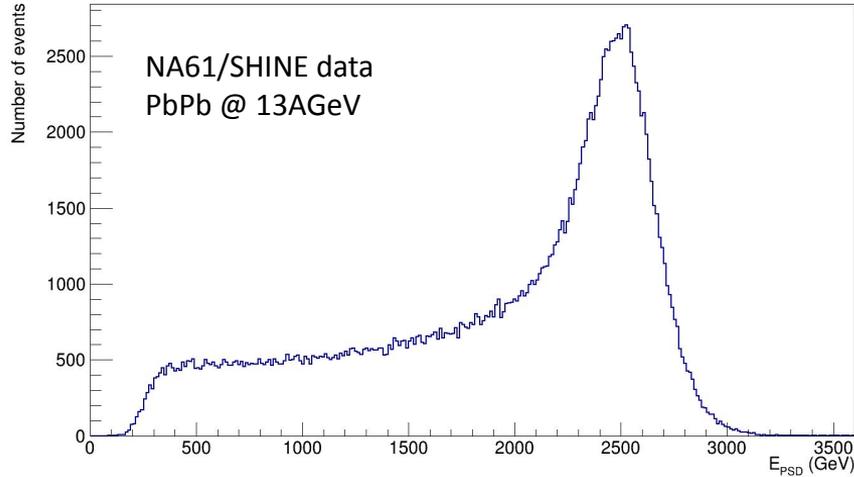
- For Γ -fit all centrality classes are comparable
- Γ -fit and MC-Glauber fit are now in more agreement with each other

Estimation of trigger efficiency



- Results do not agree with Nikolay's results from the last CM
- Looks like CCT2 trigger has good efficiency for the events with up to 60% centrality

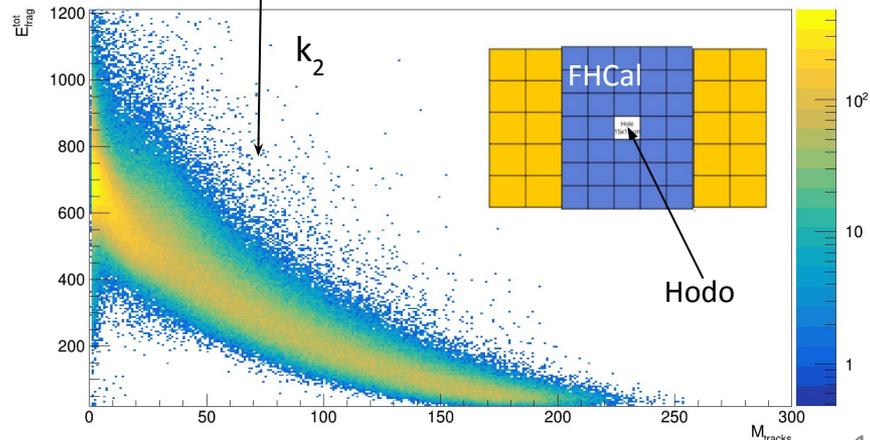
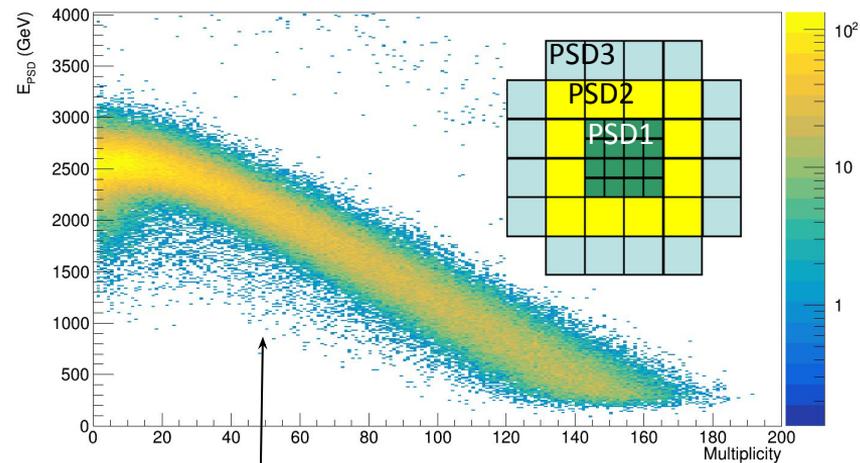
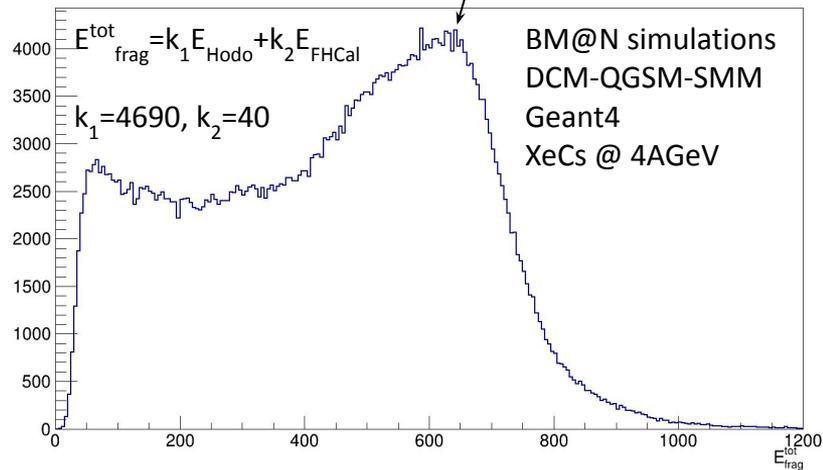
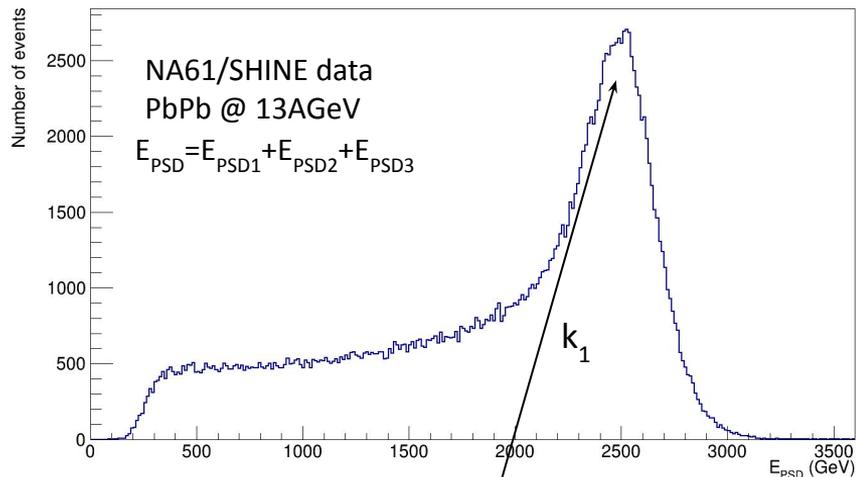
How to reconstruct “real” energy of spectators?



by N.Karpushkin
at 10th BM@N CM

- In the NA61/SHINE experiment the peak of PSD energy distribution is located at $E_{\text{beam}} * A_{\text{Pb}} \sim 2700$ GeV
- In our case we don't see range of energies in FHCAL corresponding to collision energy and colliding system
- Is it possible to reconstruct “real” energy of spectators using E_{dep} ?
- If so is there any way to do so for Hodoscope?

Possibilities of spectators fragments as estimators



Summary

- Simple steps for the pileup rejection are introduced
- The first version of it is performed

- MC-Glauber and Γ -fit fitting procedures is applied for centrality determination for the BM@N run8 data
- Relation between impact parameter and centrality classes is extracted
- These results are used in the physics analysis
- CCT2 trigger efficiency is estimated to be high up to 60% centrality

Work in progress

- Establish the final events selection procedure
- Use spectators detectors for the centrality determination
- Compare centrality classes and geometry parameters corresponding to them for different centrality estimators

Backup

Overview of centrality determination methods

Method type	MC-Glauber based	Model independent (e.g. Γ -fit method)	Based on ML
Used in	STAR, ALICE, HADES, CBM, MPD, etc.	ALICE, CMS, ATLAS <small>J. Y. Ollitrault et al. Phys.Rev. C 98 (2018) 024902</small>	Becoming popular <small>Fupeng L. et al. J.Phys.G 47 (2020) 11, 115104</small>
Advantages	Commonly used, well established procedure	Universality due to model independence	The most modern and fast methods
Disadvantages	MC-Glauber model provides non-realistic N_{part} simulations at low energies <small>M. O. Kuttan et al. e-Print: 2303.07919 [hep-ph]</small>	In strong connection with σ_{inel} which dependence on energy is not well studied at low energies (same problem for MC-Glauber based methods)	There no way to control the physicality of the methods

MC Glauber model

MC Glauber model provides a description of the initial state of a heavy-ion collision

- Independent straight line trajectories of the nucleons
- A-A collision is treated as a sequence of independent binary NN collisions
- Monte-Carlo sampling of nucleons position for individual collisions

Main model parameters

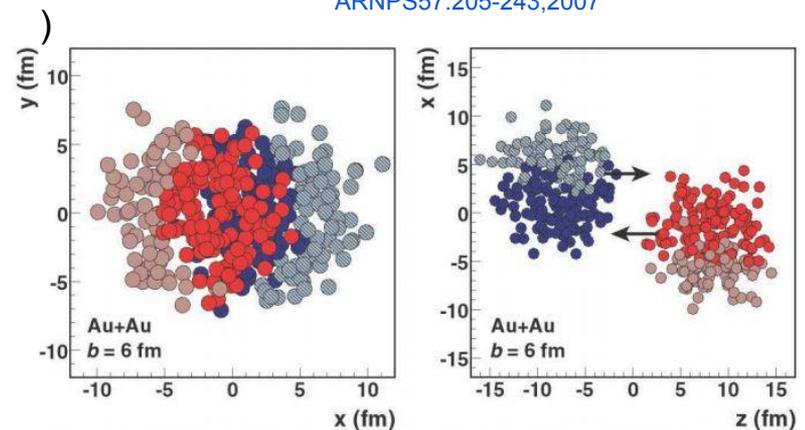
- Colliding nuclei
- Inelastic nucleon-nucleon cross section ($\sigma_{\text{inel}}^{\text{NN}}$) (depends on collision energy)
- Nuclear charge densities (Wood-Saxon distribution)

$$\rho(r) = \rho_0 \cdot \frac{1 + w(r/R)^2}{1 + \exp\left(\frac{r-R}{a}\right)}$$

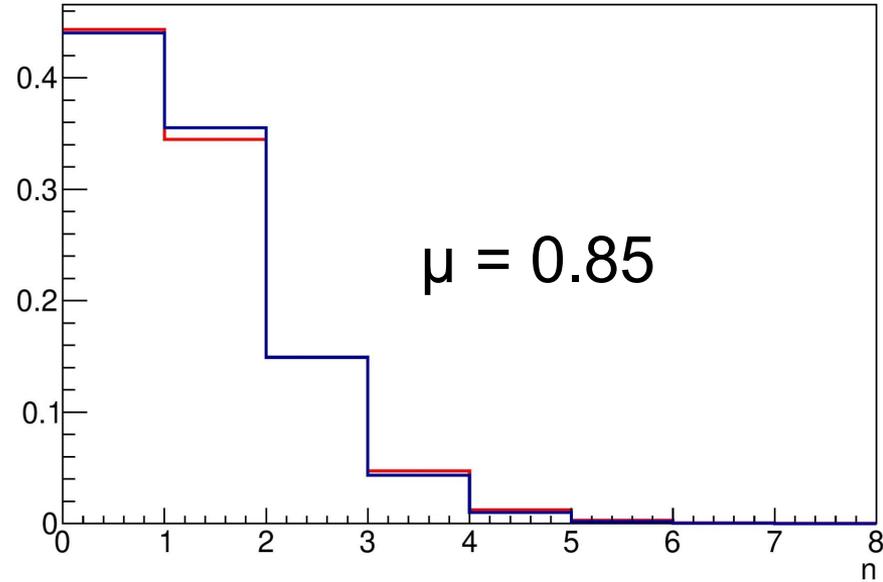
Geometry parameters

- b – impact parameter
- N_{part} – number of nucleons participating in the collision
- N_{spec} – number of spectator nucleons in the collision
- N_{coll} – number of binary NN collisions

Glauber Modeling in High Energy Nuclear Collisions:
ARNPS57:205-243,2007

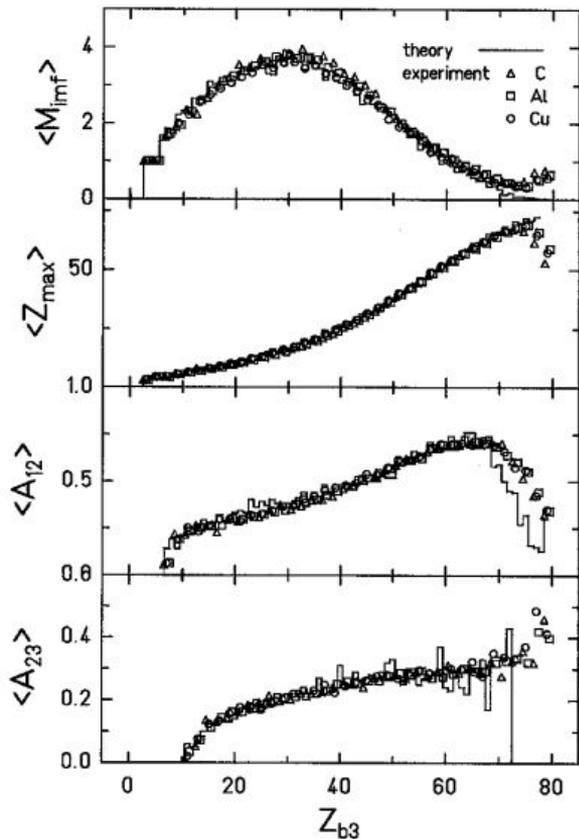


NBD at different values of k

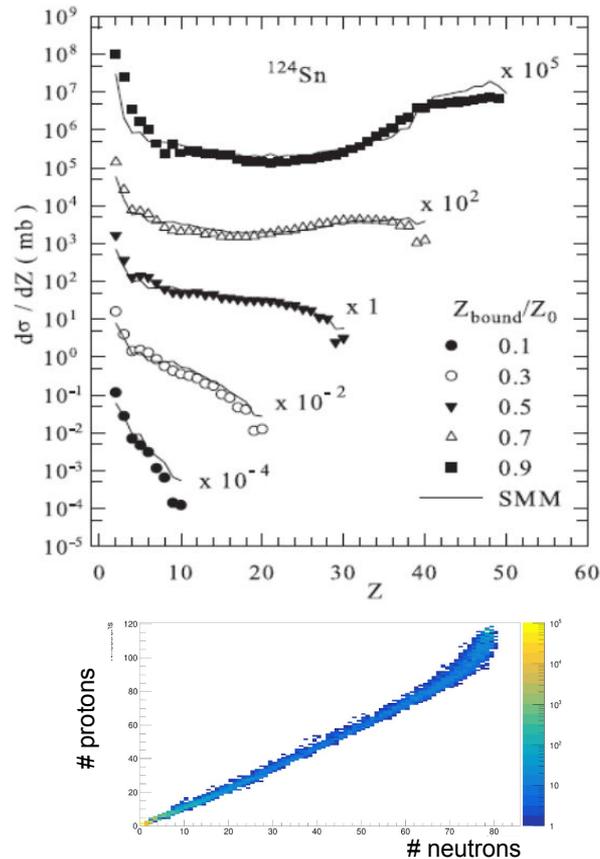


SMM description of the ALADIN's fragmentation data

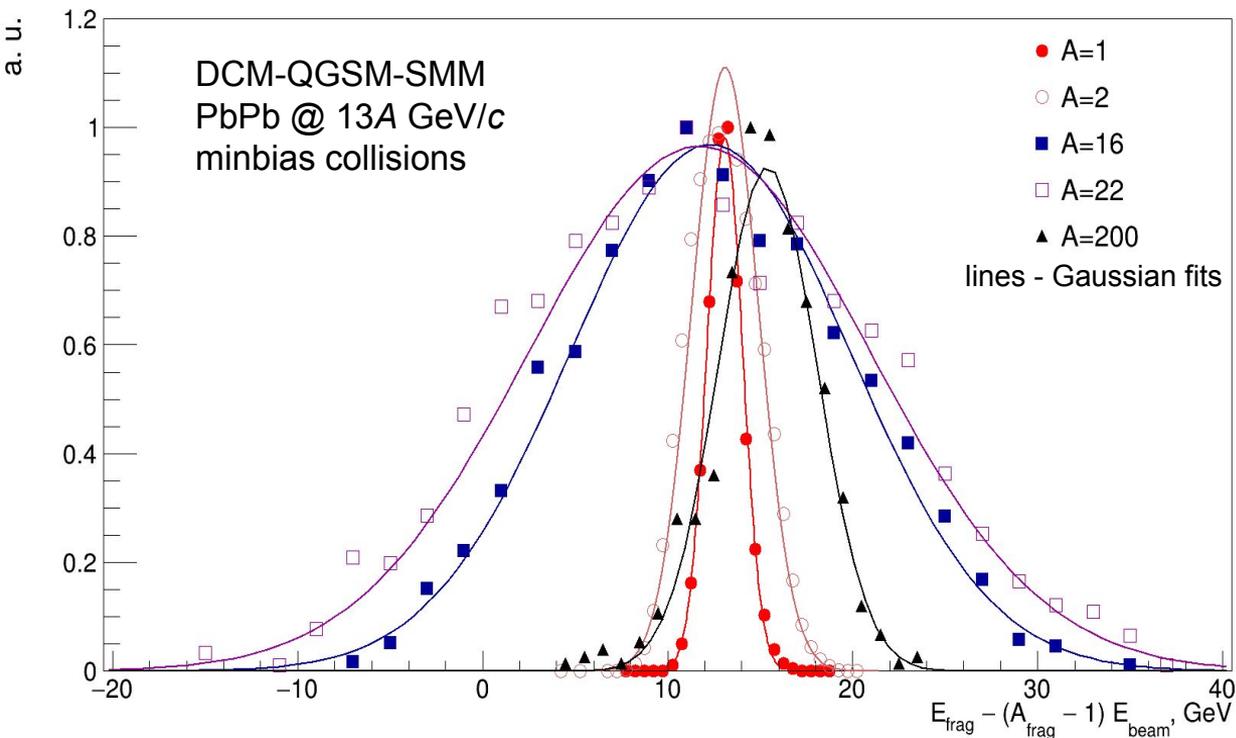
A.S. Botvina et al. NPA 584 (1995) 737



R.Ogul et al. PRC 83, 024608 (2011)



Gaussian approximation for fragments energy

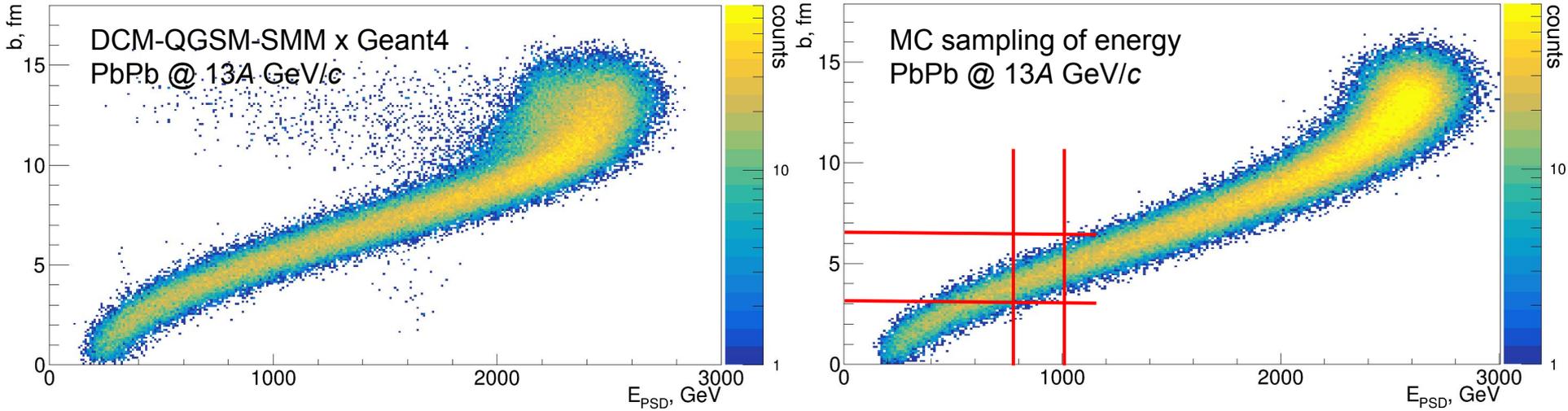


- Distribution of mass numbers of spectators fragments could be fitted by Gauss distribution
- Mean values equal to product of beam energy and fragment's mass
- Total spectators energy distribution is also Gauss:

$$P(E_{\text{tot}}; \mu_{\text{tot}}, k_{\text{tot}}) \approx \prod_{i=1}^{N_{\text{frag}}} P(E_{\text{frag}}^i; \mu_{\text{frag}}^i, k_{\text{frag}}^i) \approx \prod_{i=1}^{N_{\text{spec}}} P(E_{\text{spec}}^j; \mu_{\text{spec}}^j, k_{\text{spec}}^j)$$

- Measured energy distribution follows convolution of two Gauss distributions (sum of fragments energy and detector response)

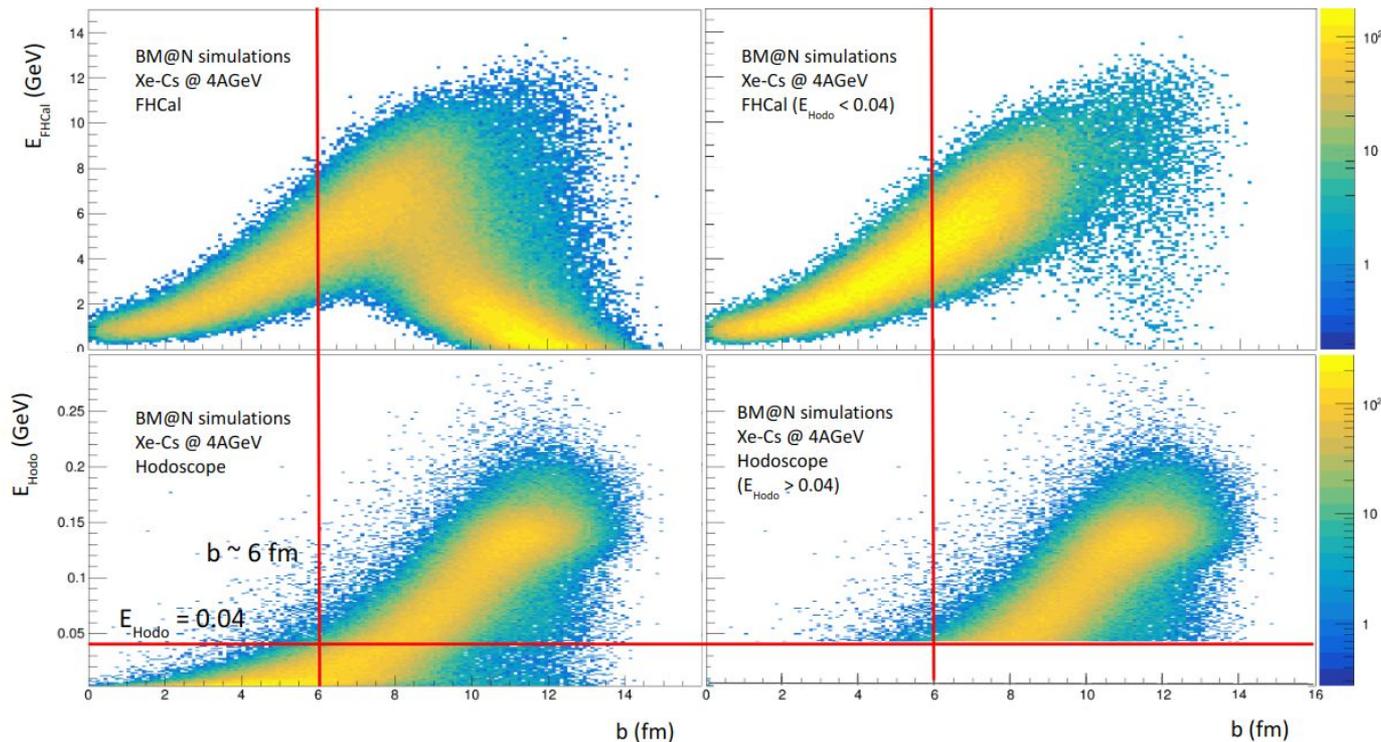
Simplified MC sampling for hadron calorimeters



Segal I. Particles. 2023; 6(2):568-579.

- Shapes of energy and impact parameter distributions are similar
- Width of distribution for energy is larger than for multiplicity
- Possible decrease of width will be study

Possibilities of spectators fragments as estimators



- Physical threshold of switching between estimators could be Hodoscope signal $E_{\text{Hodo}} = 0.04$ (corresponding to $b \sim 6$ fm)
- FHCal energy distribution improved and has more linear correlation with impact parameter (for range $E_{\text{Hodo}} < 0.04$)
- There is good correlation between Hodoscope charge and impact parameter (for range $E_{\text{Hodo}} > 0.04$)