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# Centrality selection through fluctuation measures

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# Main topic of the grant

- Prepare for the forthcoming studies of the diagram of strongly interacting matter by analysis of sensitivity of known fluctuation observables to the event selection techniques
- Check feasibility of the proposed centrality determination (based on multiplicity, energy deposition in FHCals, combined) procedures for the fluctuations analysis
- NB: sensitivity of the considered observables to the track reconstruction efficiencies and corrections methods have been studied by the SPbU group previously (RFBR project 18-02-40097) for the centrality classes determined by the impact parameter

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# Event selection

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# Centrality estimation

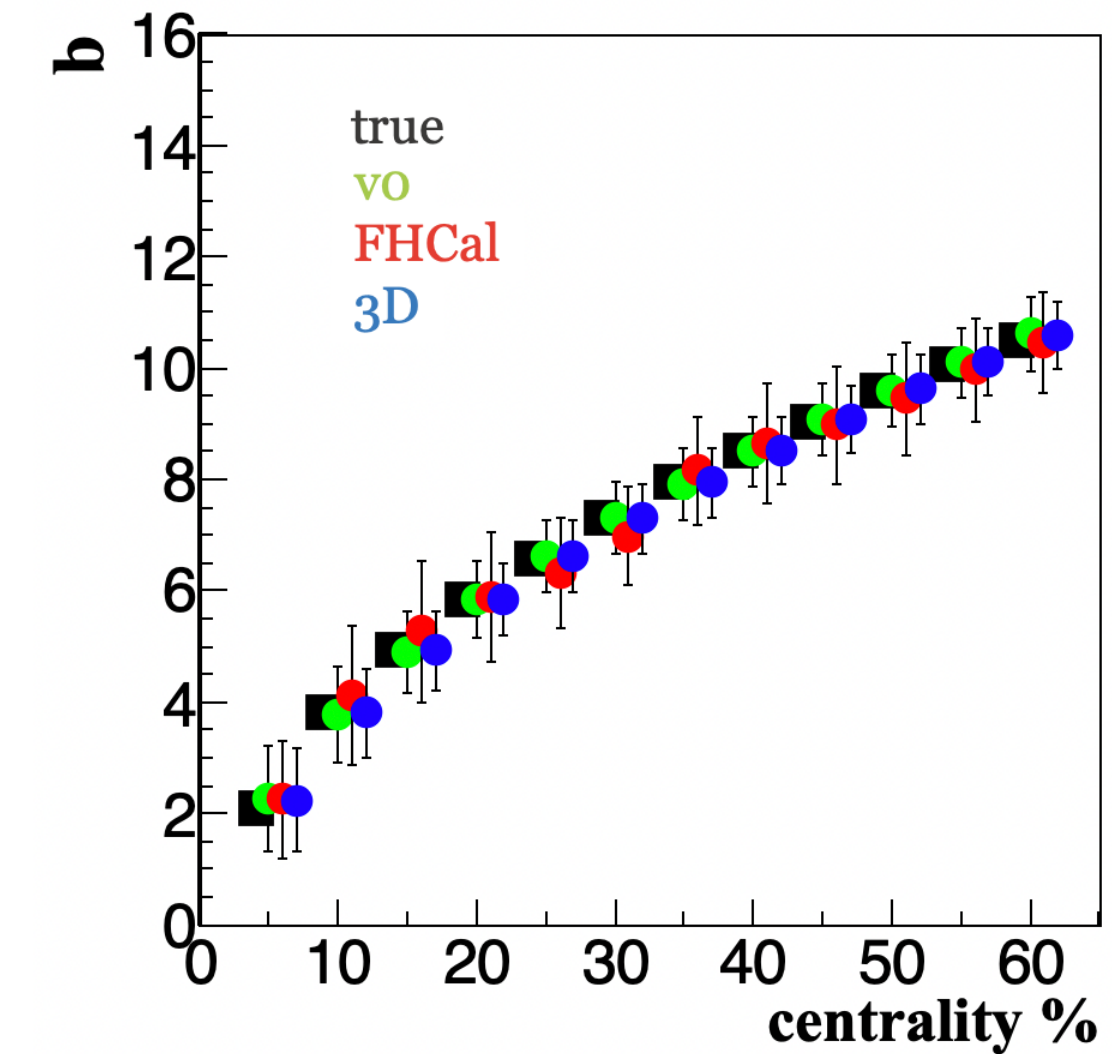
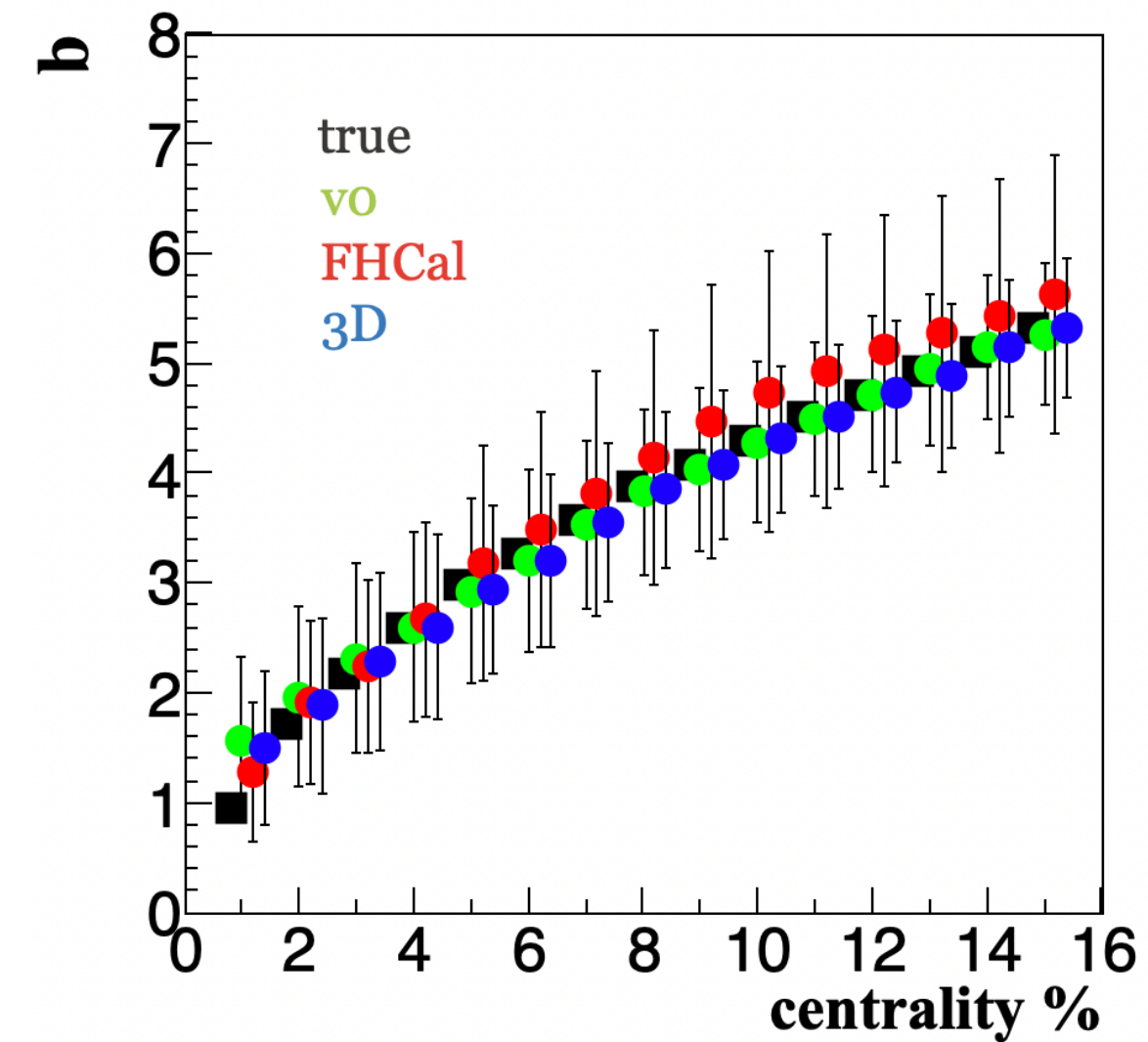
- impact parameter (ideal case)
- multiplicity in two forward sub-events  $-1.2 < \eta < -0.8$  and  $0.8 < \eta < 1.2$  (for simplicity we call it 'V0' method)
- FHCAL method (by INR group)
- 3d method: combines multiplicity and FHCAL (by INR group)
  
- detailed description of the methods were given by A. Seryakov (10.10.23 <https://indico.jinr.ru/event/4066/>)

# Centrality estimation

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## Findings:

- All methods are able to reproduce mean values of impact parameters (except for 0-1%)

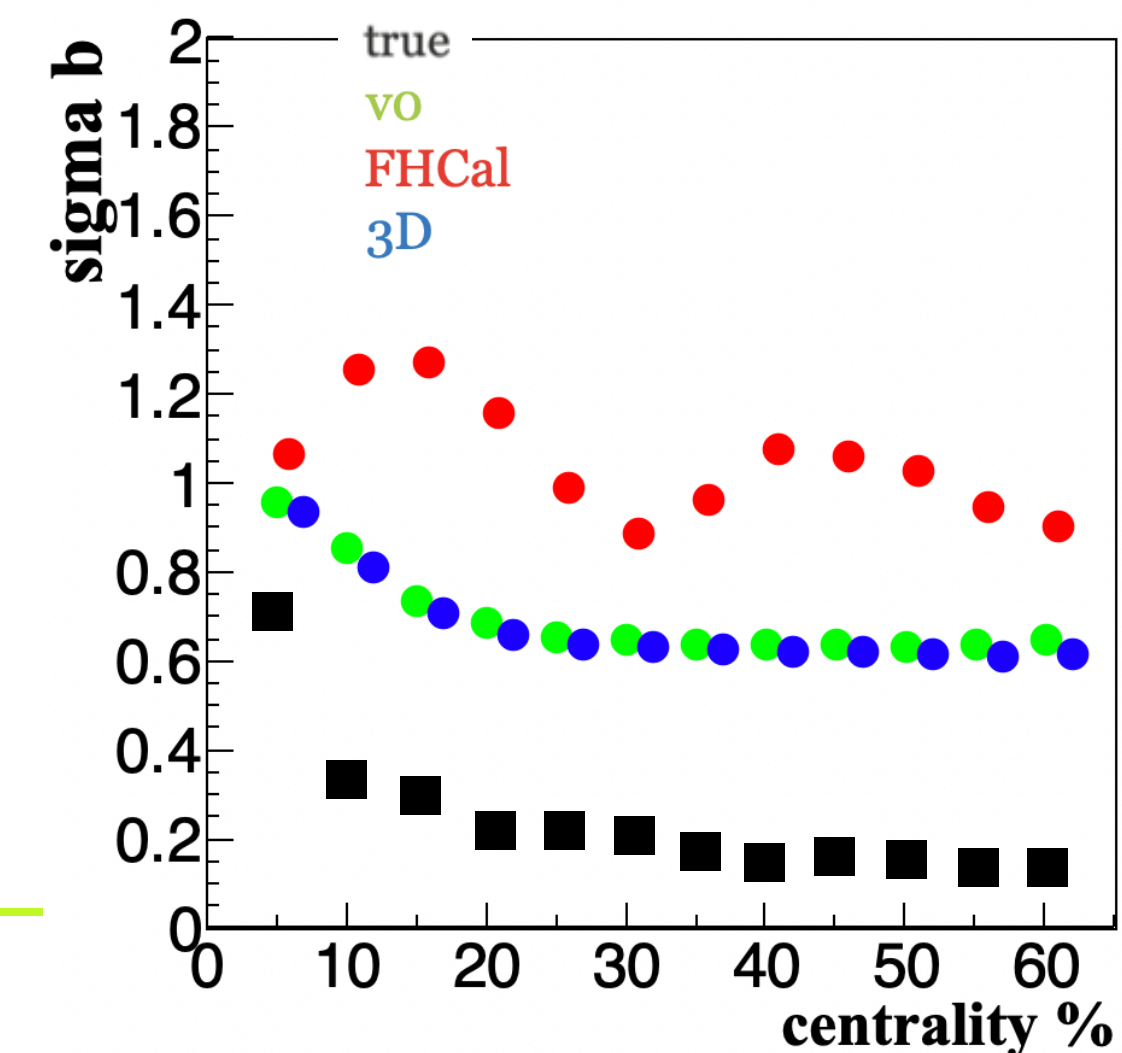
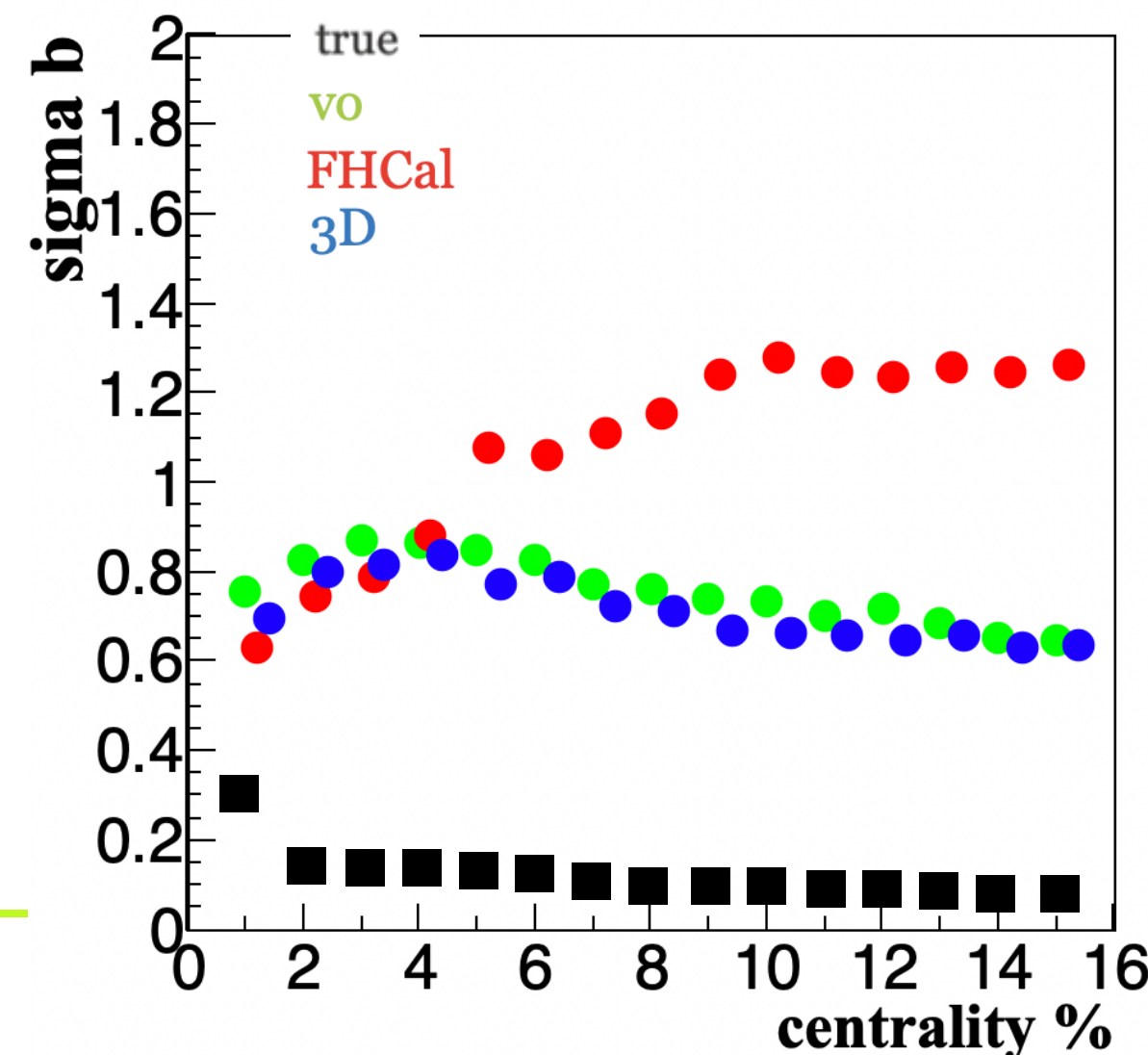
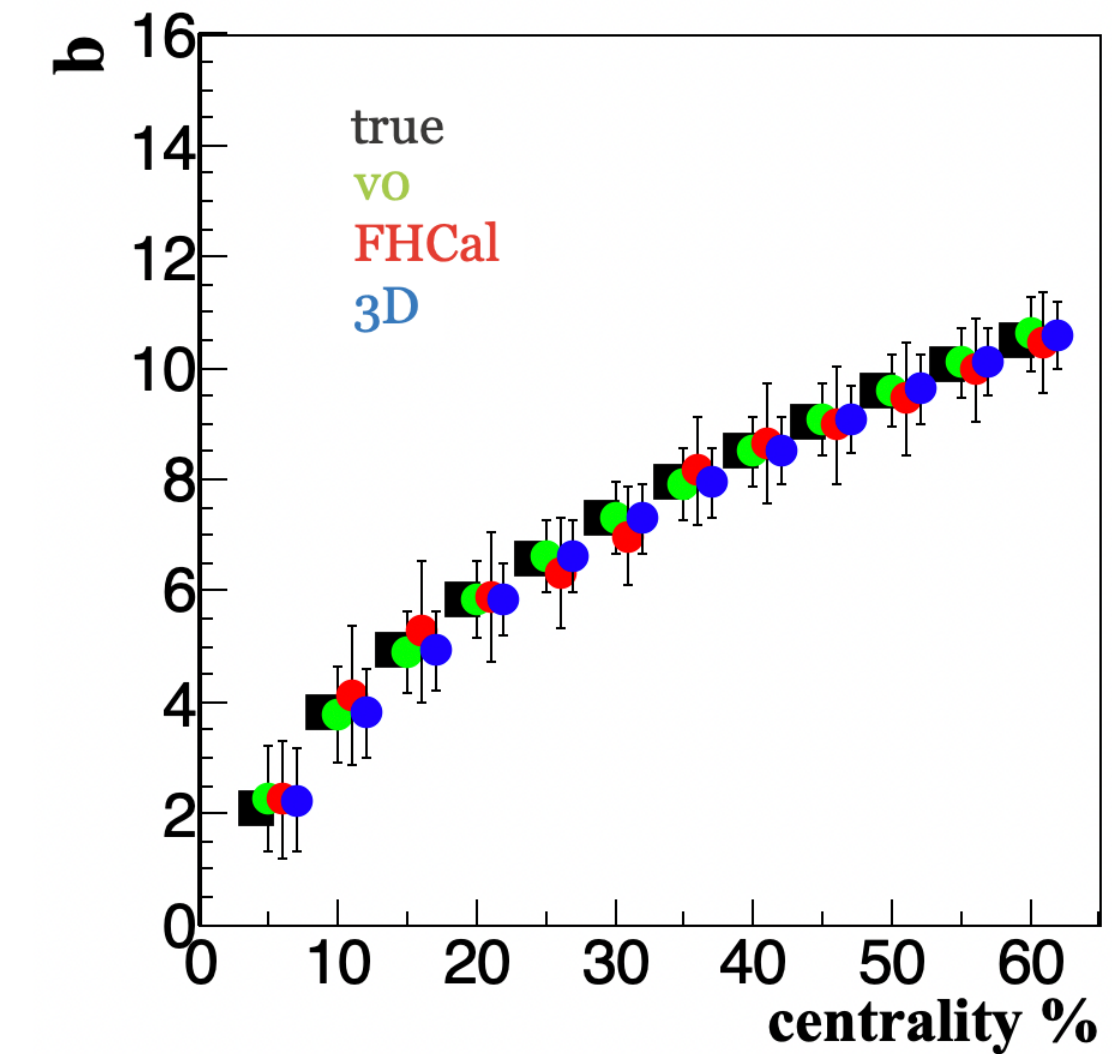
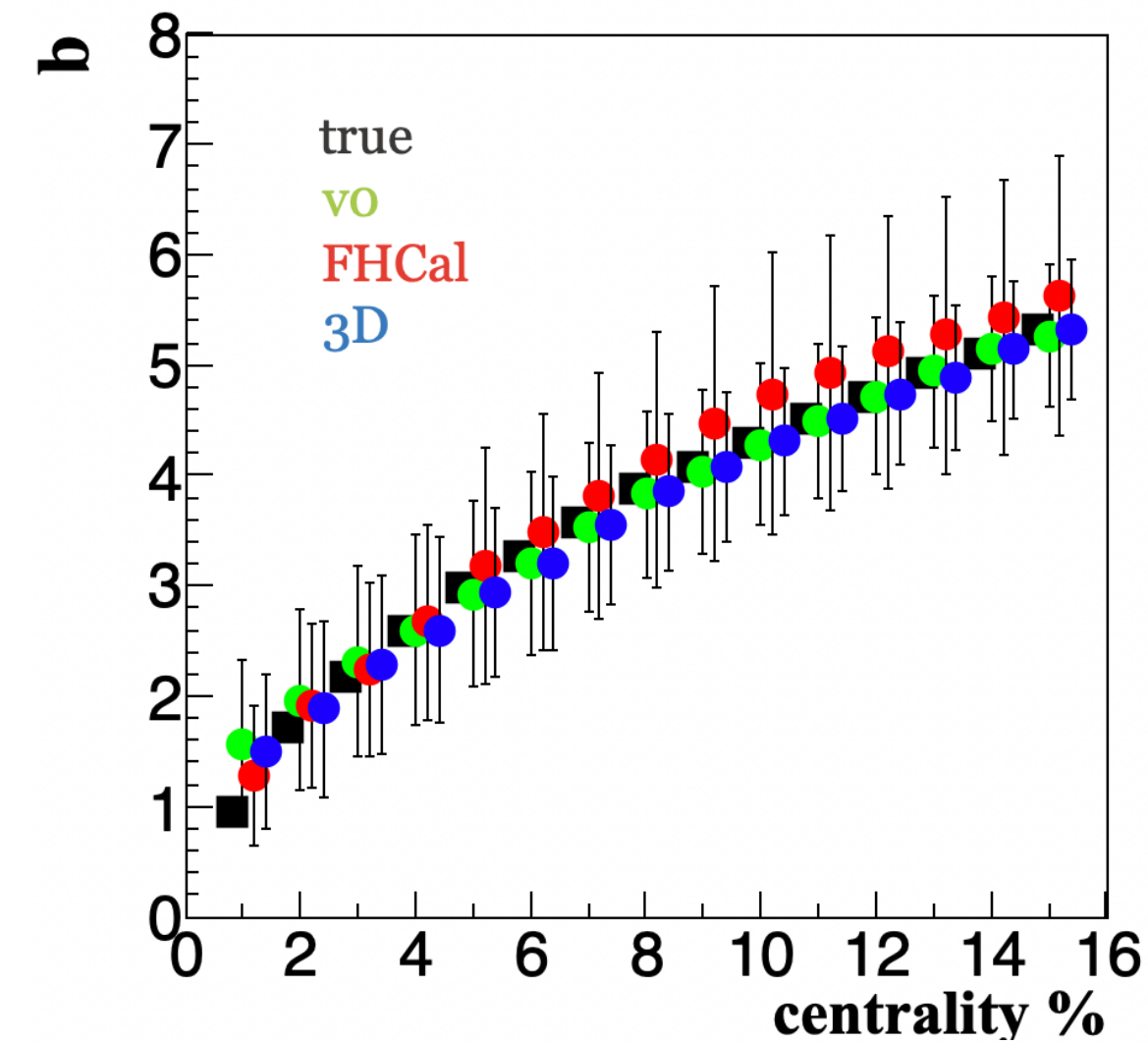


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- But the shape and the width of the impact parameter distributions for selected by proxy classes are not so nicely reproduced

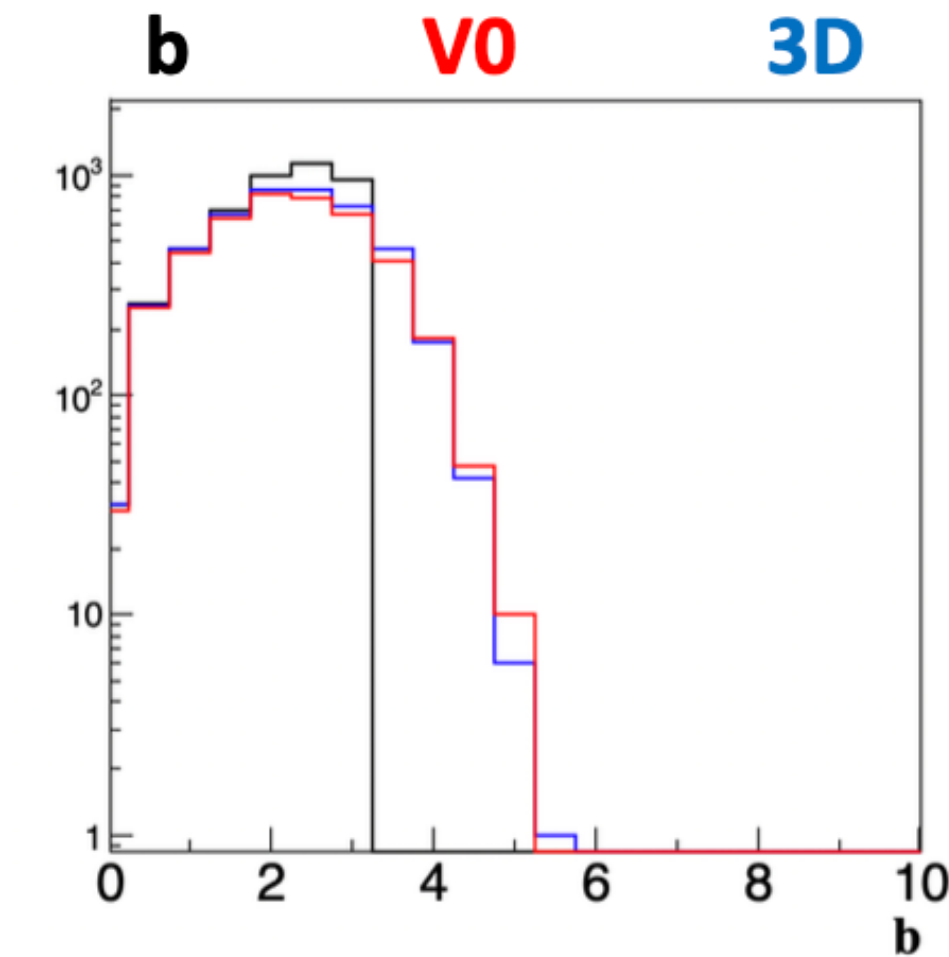
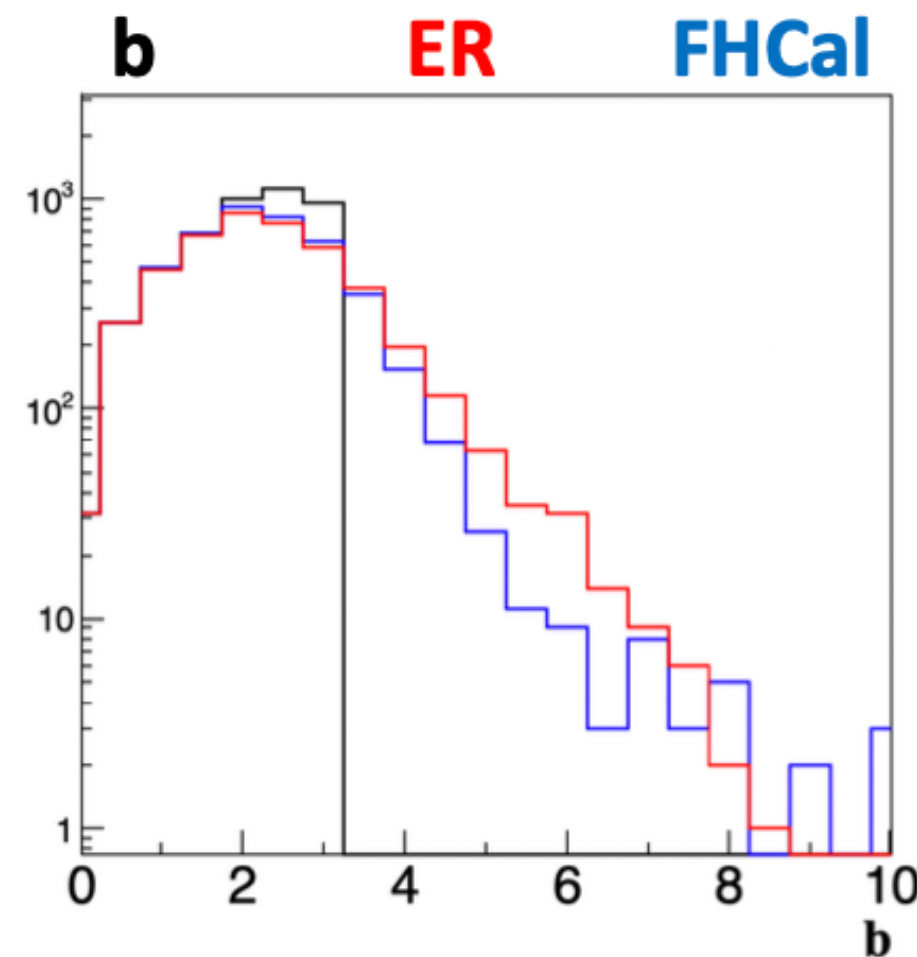


# Centrality estimation

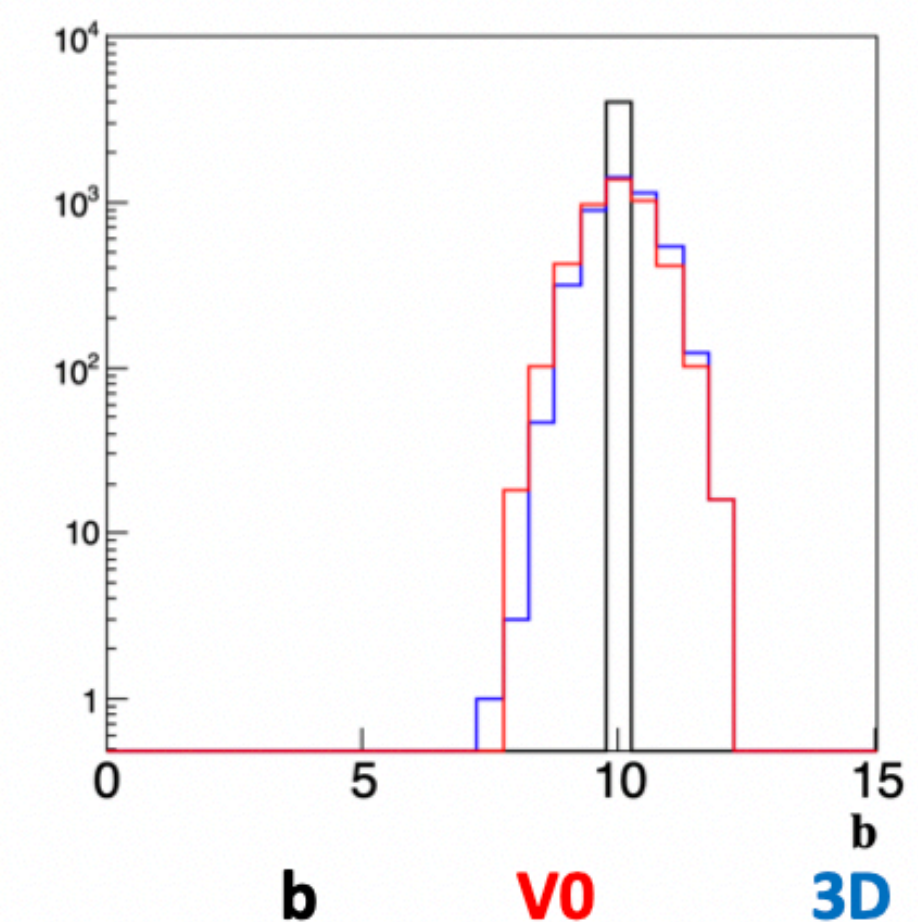
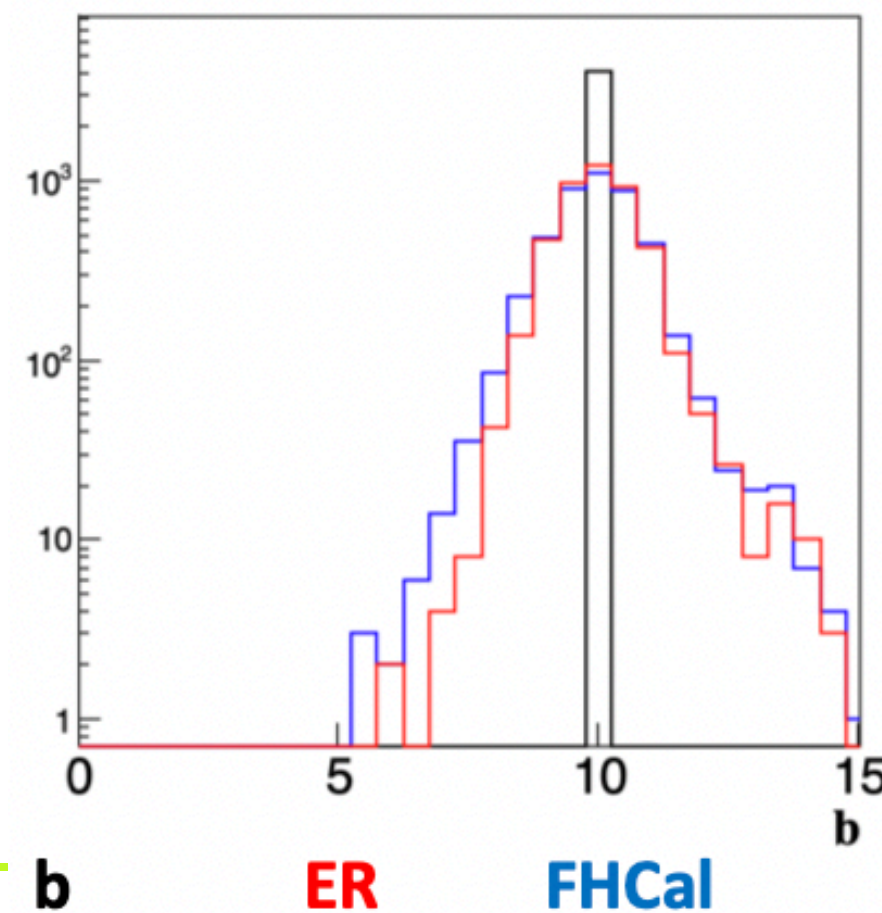
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## Findings:

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0-5% centrality



50-55% centrality

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# Observables for fluctuations studies



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# Fluctuations

To study fluctuations = to study a distribution of a given observable

Any distribution is fully parametrized by (full, infinite) set of moments or factorial moments or cumulants or factorial cumulants

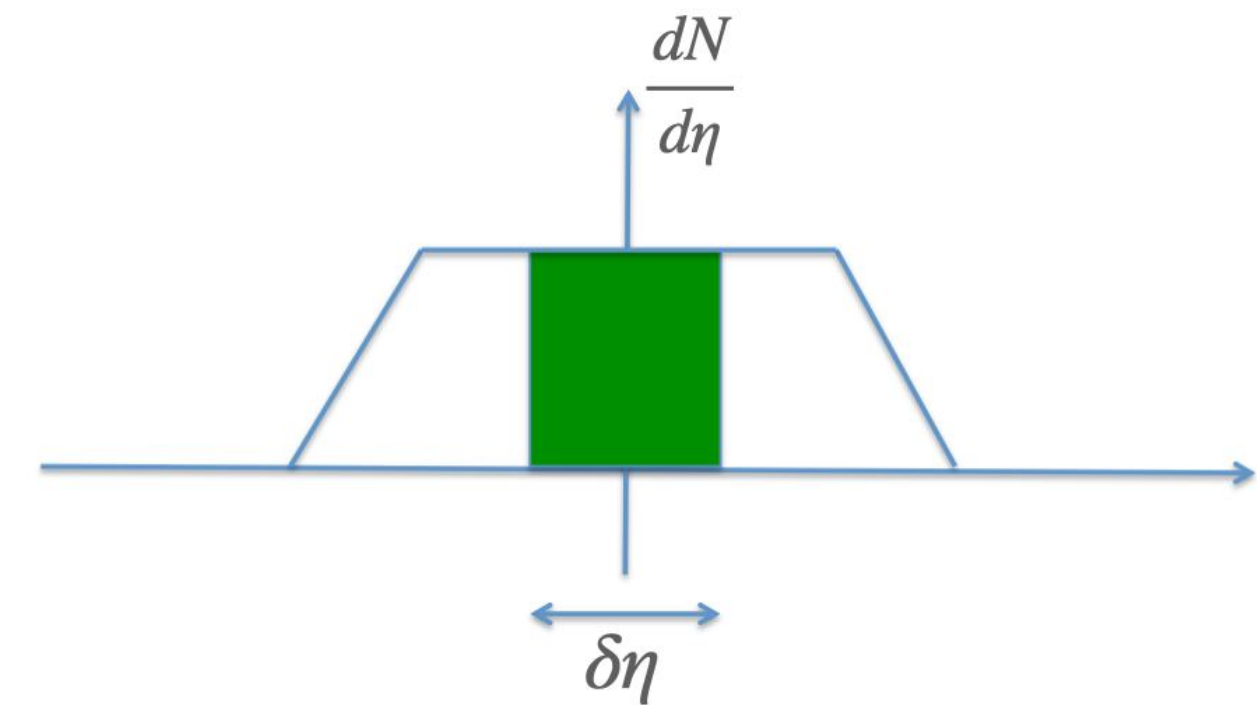
Experimentally

- 1) one typically looks at a few of them with the lowest order (i.e. mean, variance, skewness, kurtosis etc.)
- 2) one tries to combine them in a way to suppress ‘trivial’ effects (e.g. ratio of cumulants)
- 3) one can have a joint distribution of  $x$  observables, i.e. under the term ‘fluctuations’ one can also study ‘correlations’ (in this project we limit  $x$  to 2)
- 4) ‘correlations’ can be studied between observables in the same kinematic acceptance (1 subevent of the full event) or between observables in the separated kinematic acceptances ( $x$  subevents)
- 5) the size of subevents can be varied

# Observables

For 1 subevent:

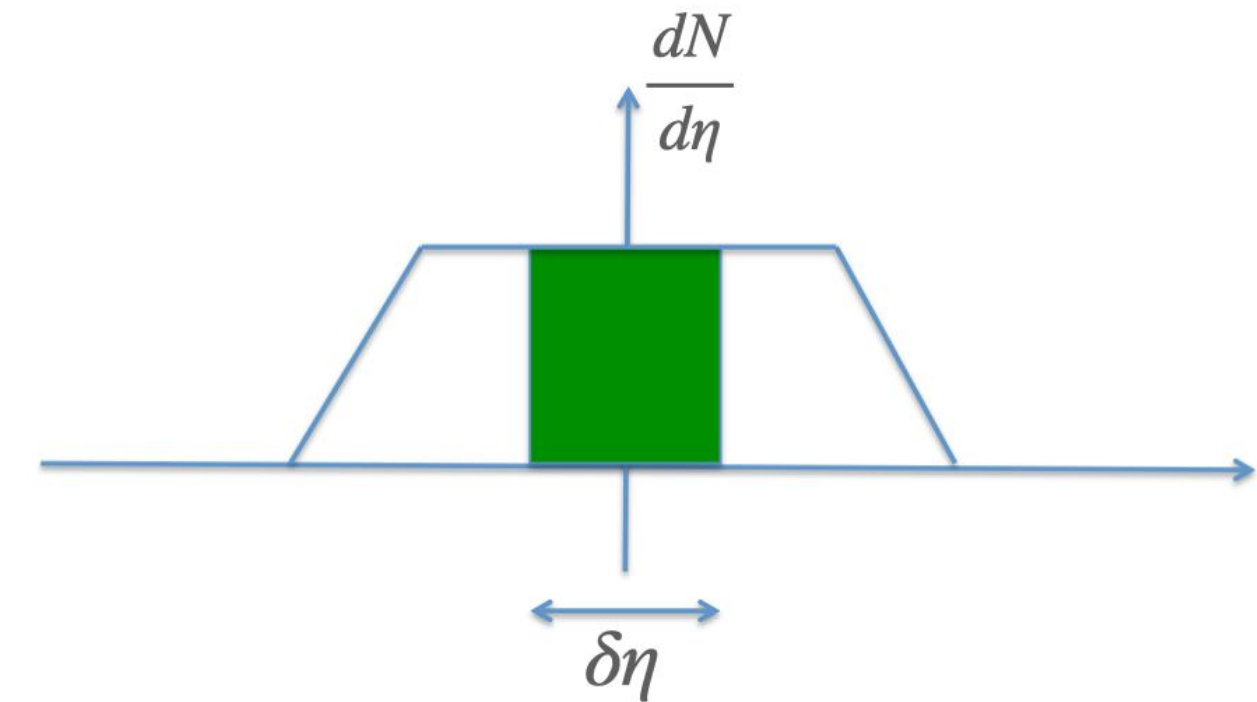
- multiplicity of charged hadrons ( $N$ )
- net electric charge ( $N_+ - N_-$ )
- sum of transverse momenta of charged hadrons ( $P_T = \sum_{i=1}^N p_{T,(i)}$ )
- mean transverse momentum in an event ( $M(p_T) = \frac{P_T}{N}$ )



# Fluct. measures

For 1 subevent:

- mean multiplicity (event-average)  $\langle N \rangle = \frac{\sum_{j=1}^{n_{events}} N_j}{n_{events}}$
- scaled variance (event-average)  $\omega[N] = \frac{\langle N^2 \rangle - \langle N \rangle^2}{\langle N \rangle}$
- net charge cumulants  $\kappa_i = \frac{d^i}{dz^i} \ln \left( \sum_{N_+ - N_-} P(N_+ - N_-) z^n \right)_{z=1}$
- scaled variance (event+track-average)  $\omega[[p_T]] = \frac{\langle\langle p_T^2 \rangle\rangle - \langle\langle p_T \rangle\rangle^2}{\langle\langle p_T \rangle\rangle}$
- strongly intensive quantities:
  - $\Delta[P_T, N] = \frac{\langle N \rangle \omega[P_T] - \langle P_T \rangle \omega[N]}{\langle N \rangle \omega[[p_T]]}$
  - $\Sigma[P_T, N] = \frac{\langle N \rangle \omega[P_T] + \langle P_T \rangle \omega[N] - 2(\langle N \cdot P_T \rangle - \langle N \rangle \langle P_T \rangle)}{\langle N \rangle \omega[[p_T]]}$

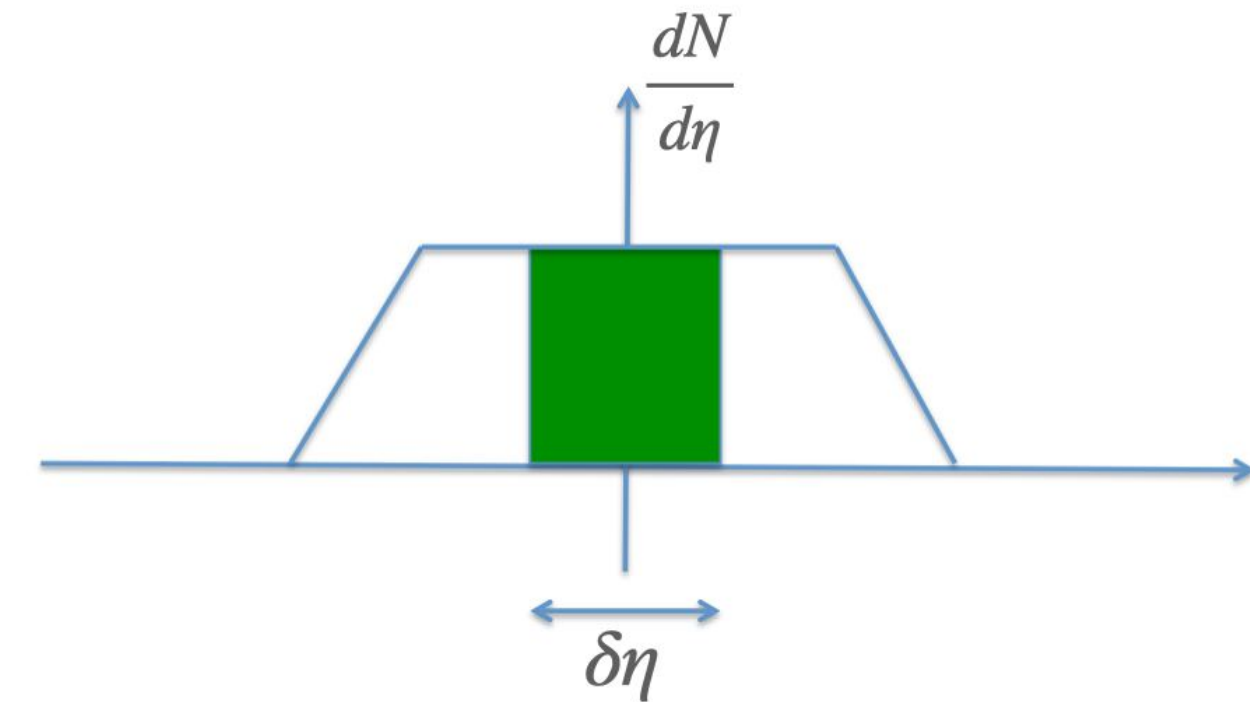


M. Gorenstein, M. Gazdzicki, Phys. Rev. C84, 014904 (2011)

# Fluct. measures

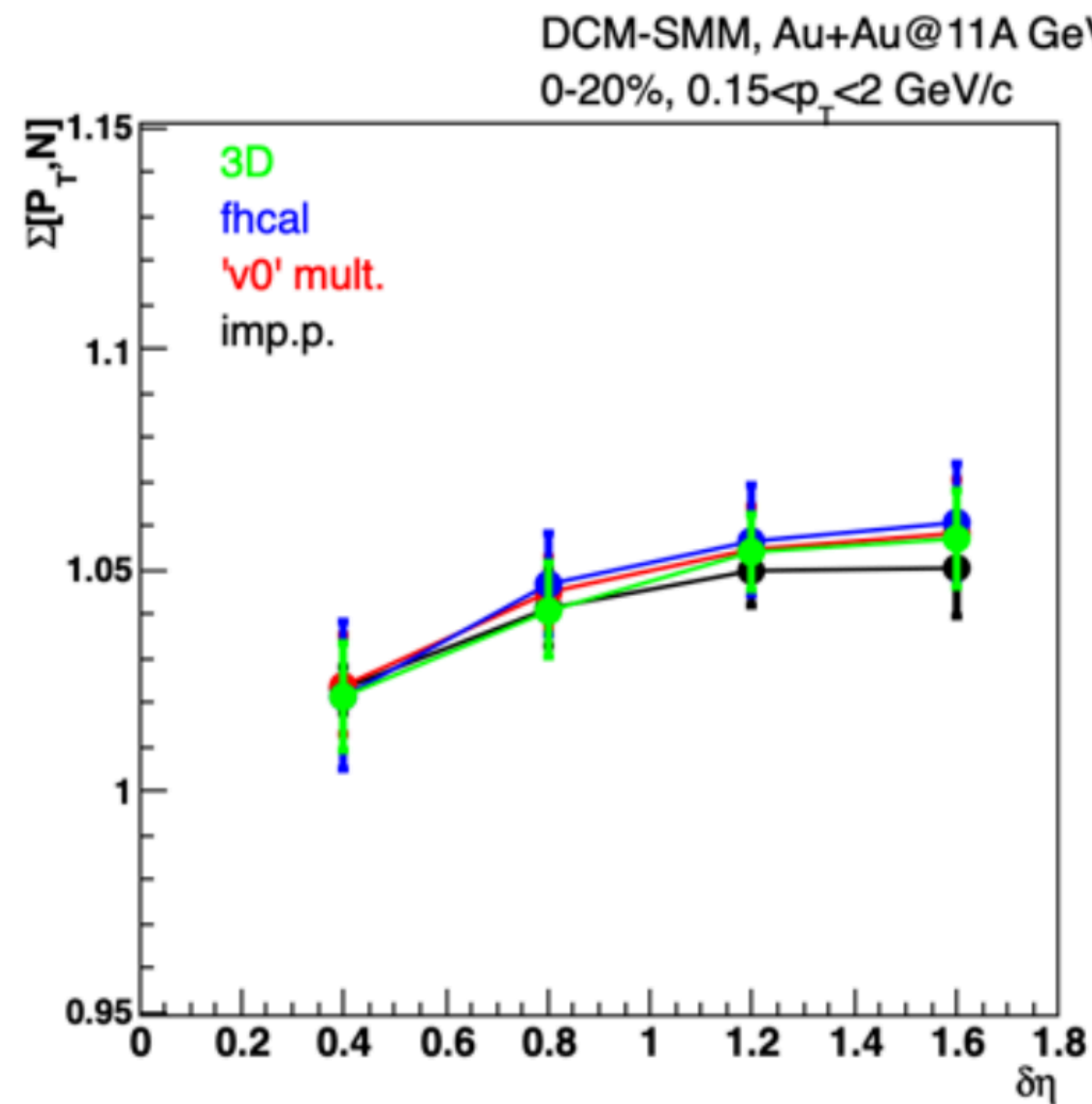
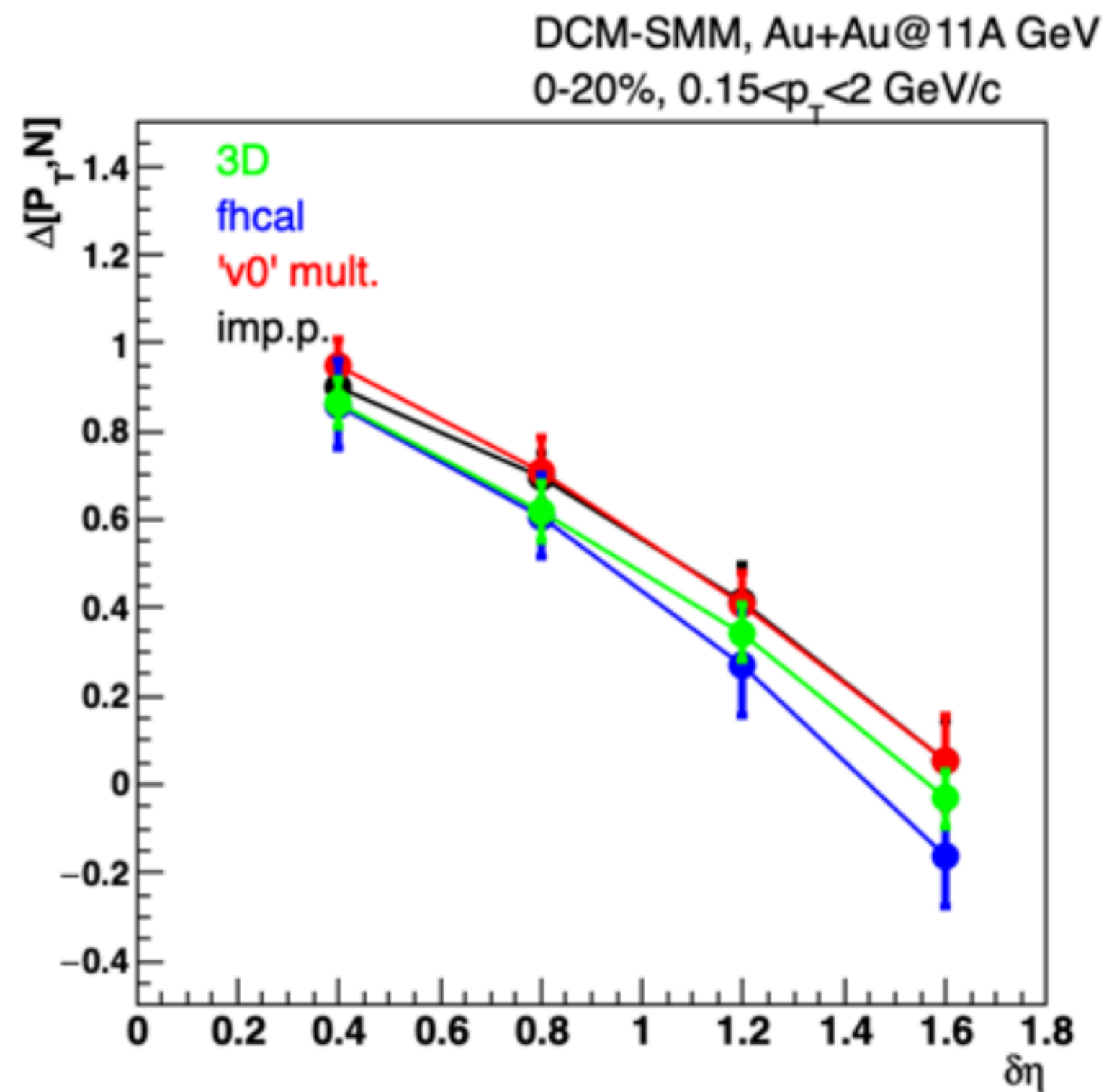
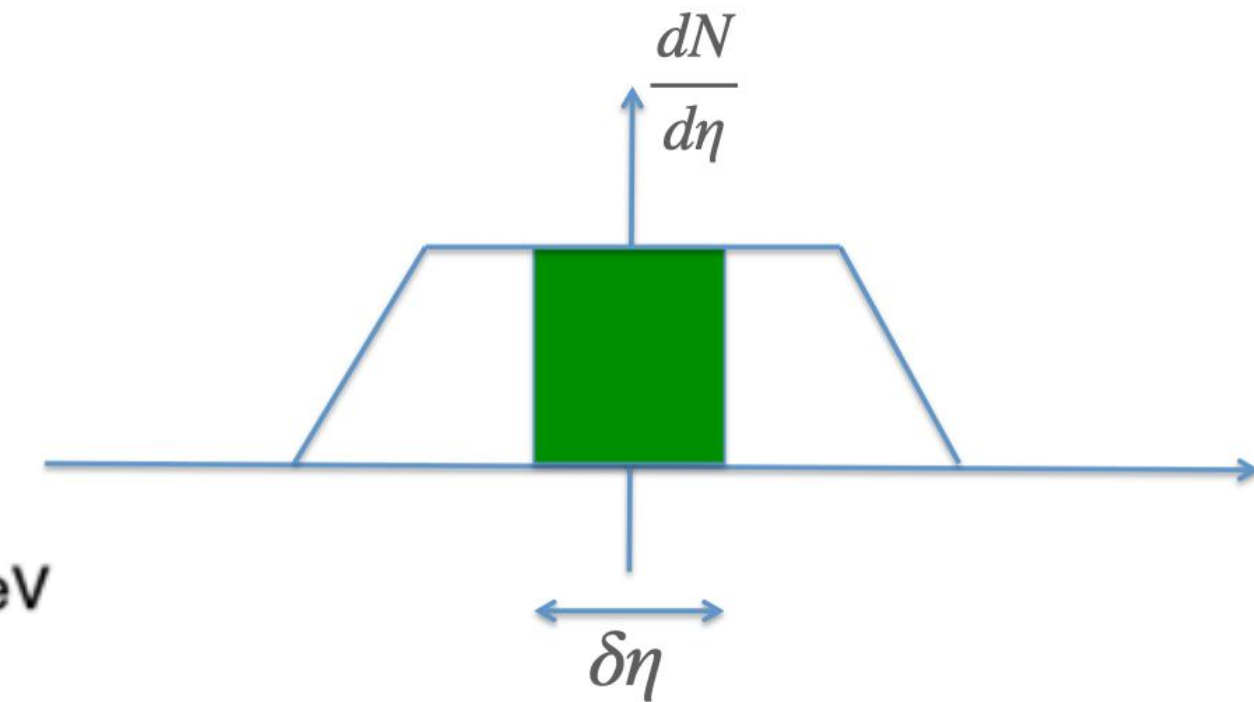
## Findings:

- Current version of 3D method have to be modified to exclude auto-correlations. The multiplicity for it has to be measured in separate rapidity windows  $([-1.2,-0.8] \cup [0.8,1.2])$
- Standard FHCAL method (energy vs max.E) produces better or equal results to ER method (energy vs radius of the fit).
- For very central events FHCAL\* is recommended to use as a centrality proxy.
- For periphery – V0\*, however there will be an effect which has to be taken into account.
- High moment fluctuations can't be measured for peripheral events
- Adding a multiplicity V0 cut on periphery makes solely FHCAL selection better, but there is a room for improvement and careful studies.



# Fluct. measures

Dependence on width of the subevent:

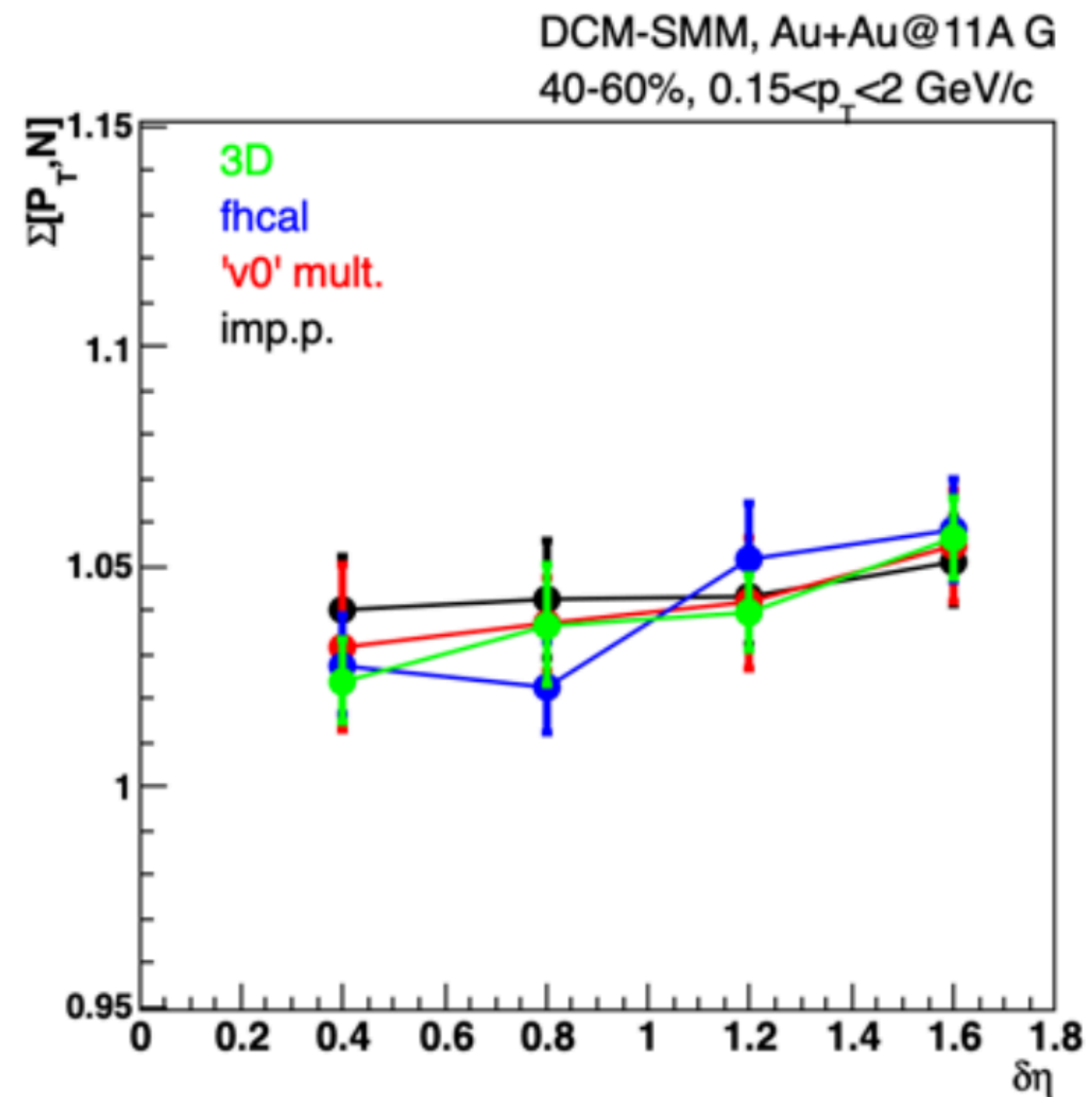
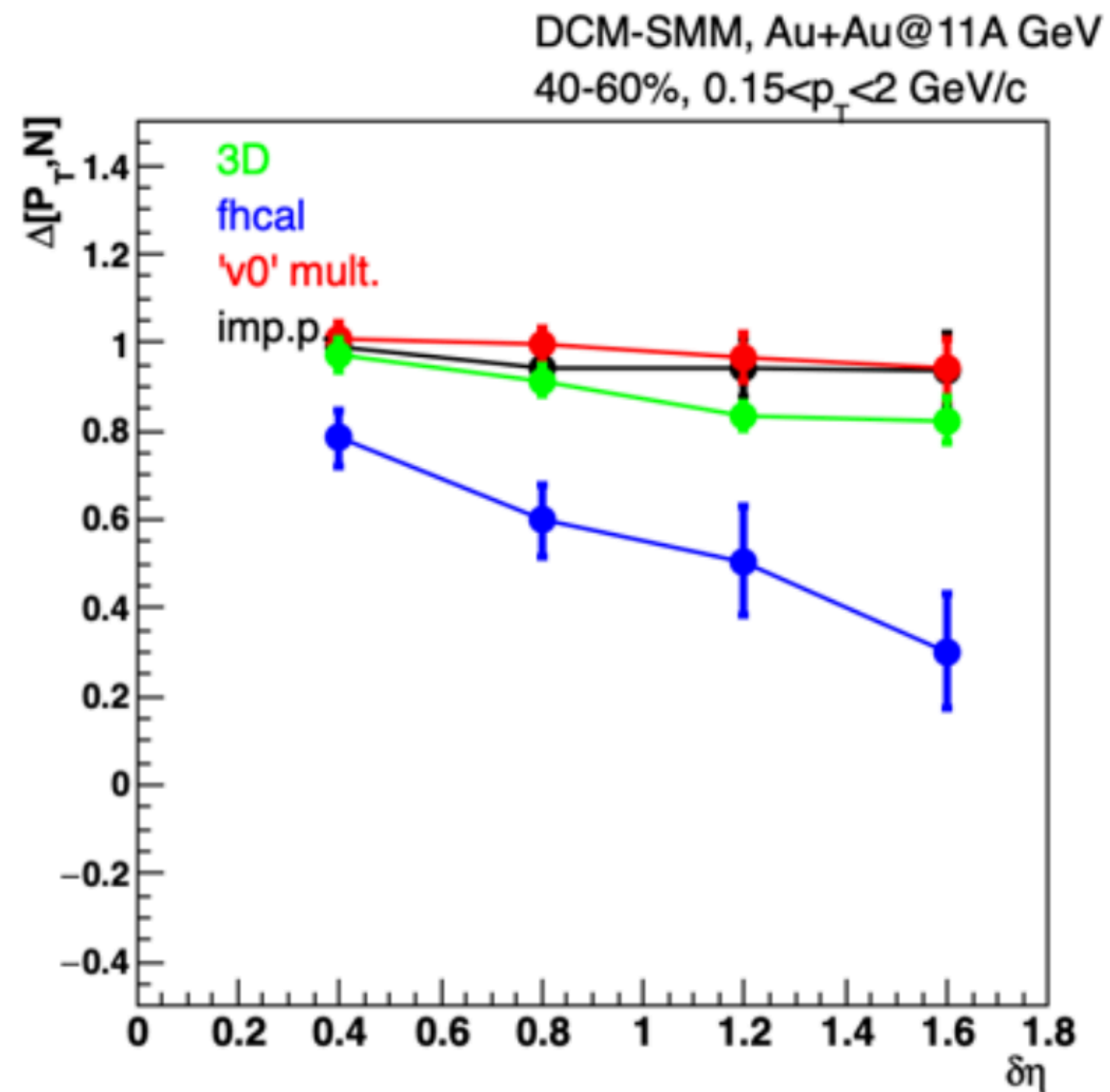
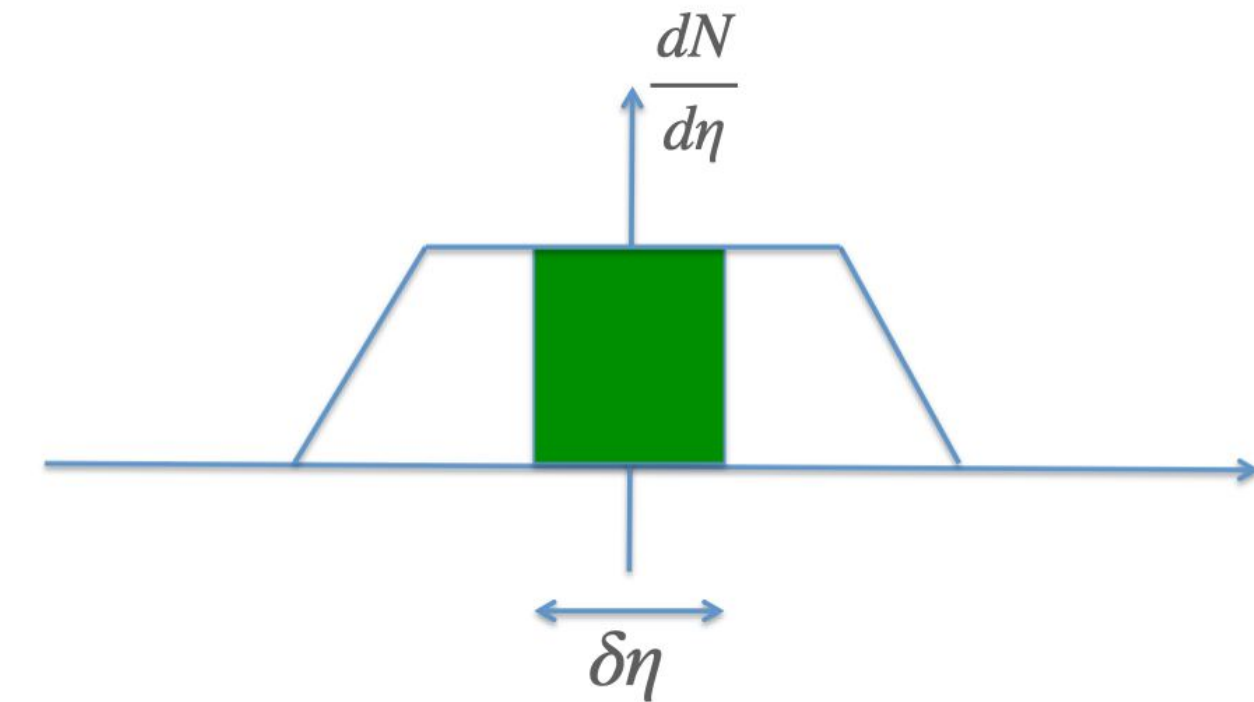


## Findings:

- Both  $\Delta[P_T, N]$  and  $\Sigma[P_T, N]$  tend to 1 with a decrease of acceptance
- 'True' results for  $\Delta[P_T, N]$  are best reproduced by the 'v0' method
- 'True' results for  $\Sigma[P_T, N]$  are consistent with all methods

# Fluct. measures

Dependence on width of the subevent:



## Findings:

- Both  $\Delta[P_T, N]$  and  $\Sigma[P_T, N]$  tend to 1 with a decrease of acceptance
- For more peripheral events FHCAL method is not applicable for  $\Delta[P_T, N]$

# Observables

For 1 subevent:

- $p_T$  ‘correlator’ ( $C_n = \frac{\sum_{i_1=1}^N \cdots \sum_{i_n=1, i_1 \neq i_2 \neq \dots \neq i_n}^N (p_{T,(i_1)} - M(p_T)) \cdots (p_{T,(i_n)} - M(p_T))}{N(N-1) \cdots (N-n)}$ )

This measure can be considered as complementary to anisotropic flow studies (it is sensitive to the initial stage of the collision) (—>recent interest to  $v_n$ - $p_T$  correlations) [G. Giacalone et al., Phys. Rev. C 103, 024910 \(2021\)](#)

Higher order cumulants are sensitive to EoS that are inserted into hydro simulations

- $C_2$  by ALICE, STAR, ATLAS etc.

[ALICE, Eur. Phys. J. C 74, 3077 \(2014\)](#)

[STAR, Phys. Rev. C 99, 044918 \(2019\)](#)

- recent  $C_3$  and  $C_4$  by ALICE

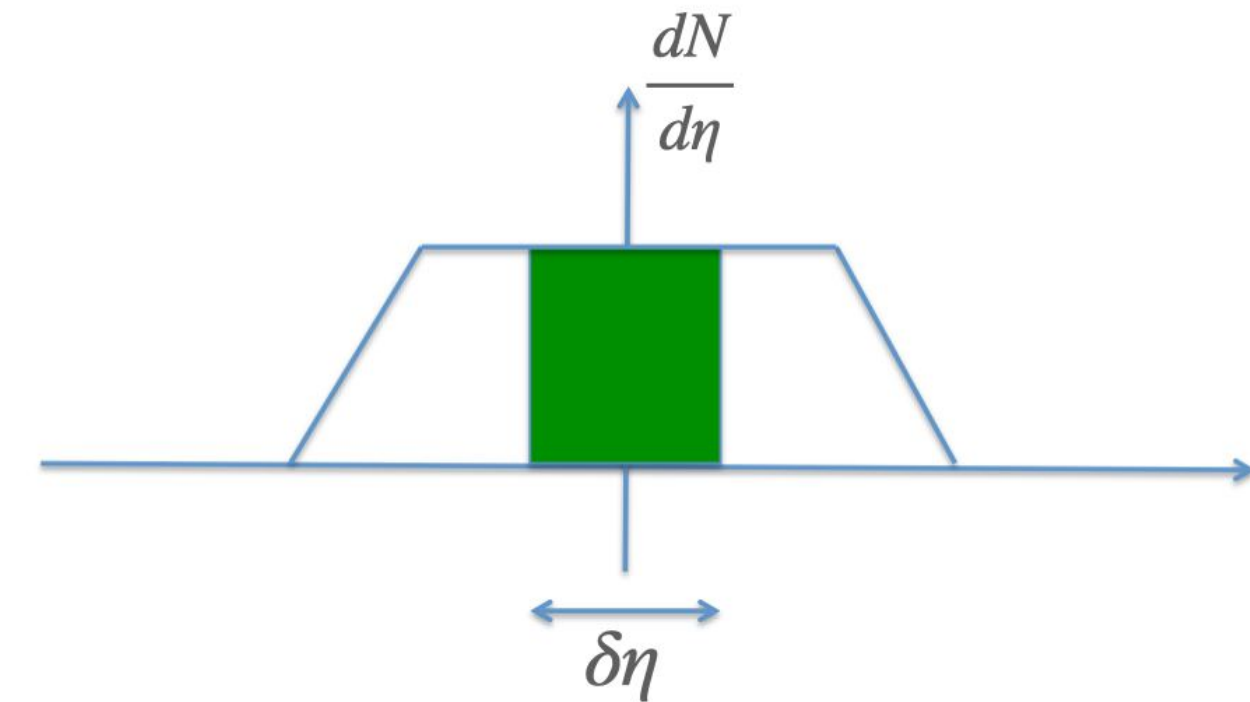
[ALICE, e-Print: 2308.16217 \[nucl-ex\]](#)

[ATLAS, ATLAS-CONF-2023-061](#)

# Fluct. measures

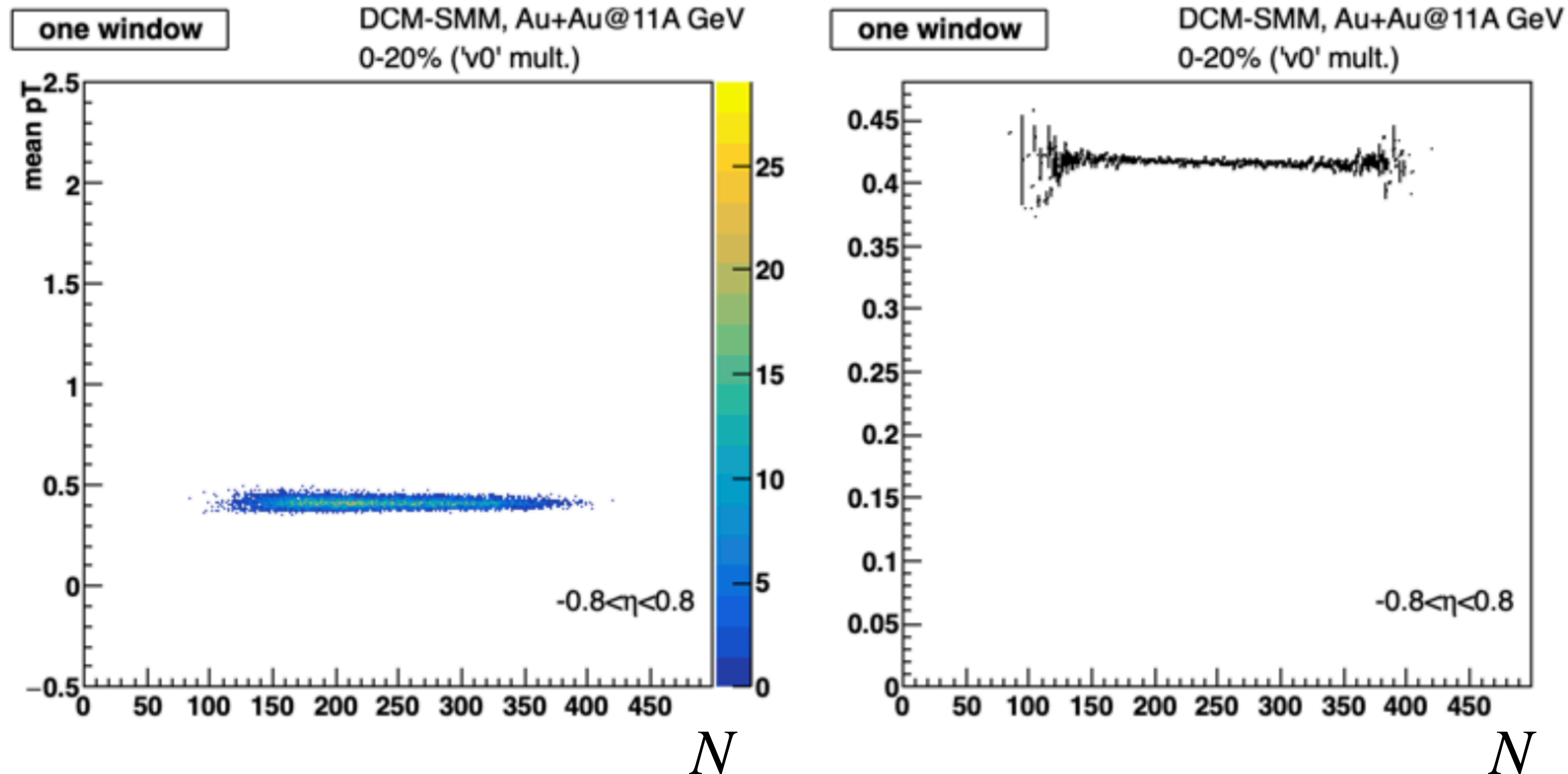
For 1 subevent:

- $p_T$  ‘correlator’ of the order 1 is  $M(p_T) = \frac{P_T}{N}$
- typically studied as a function of multiplicity



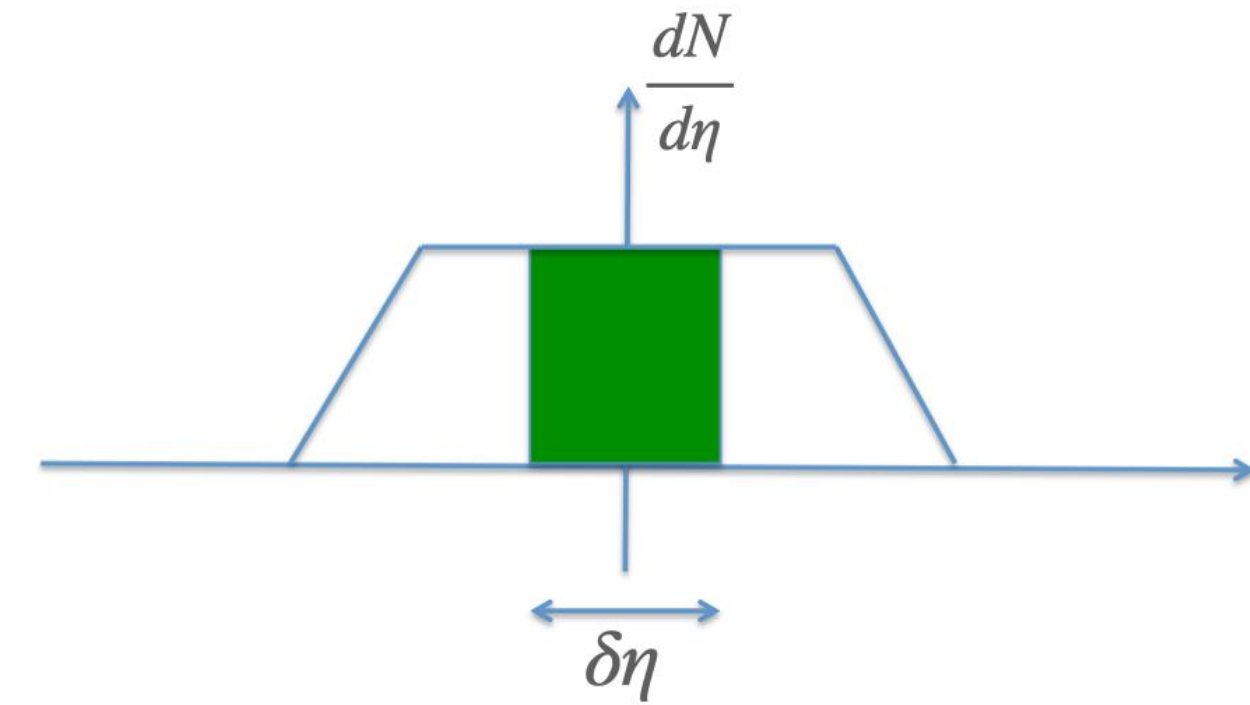
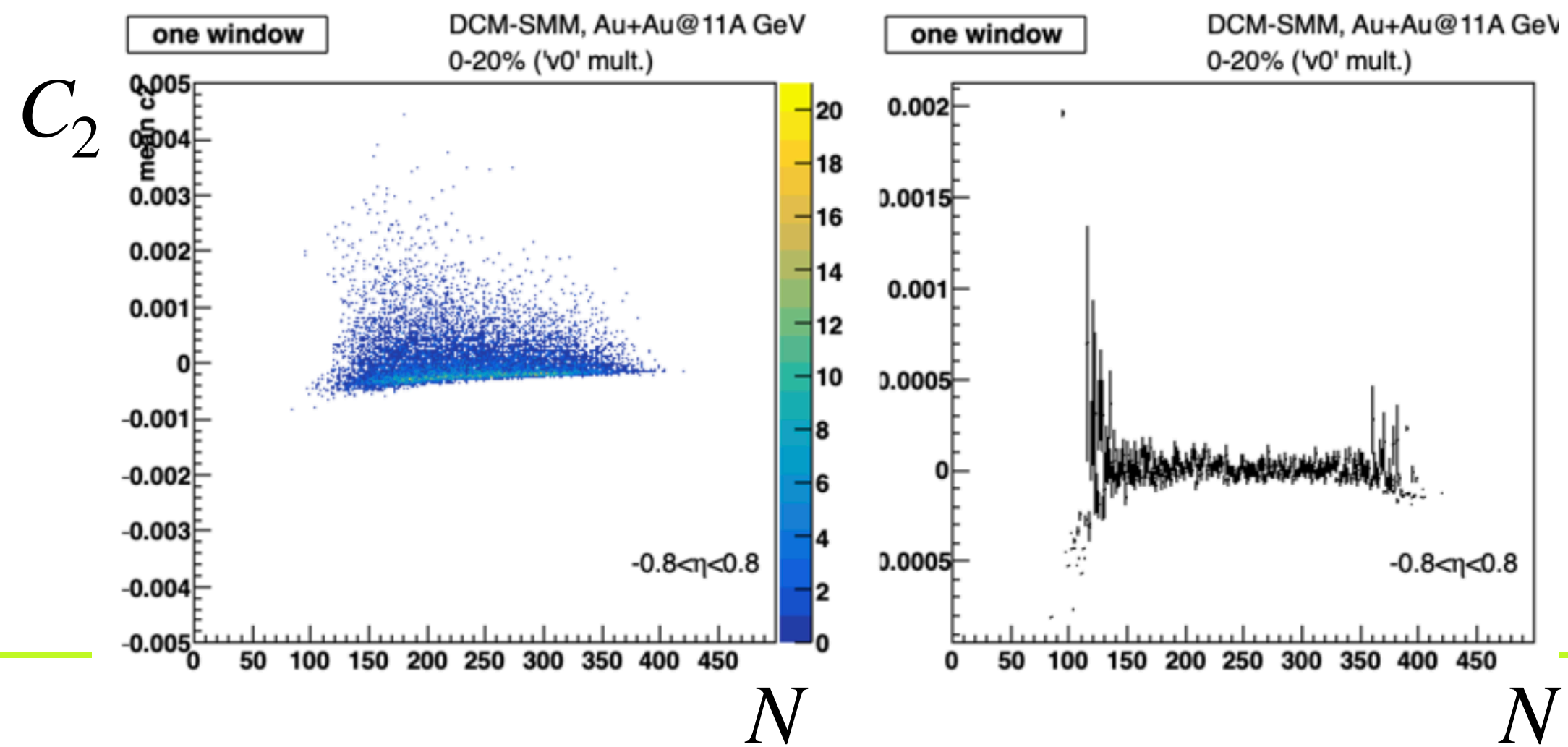
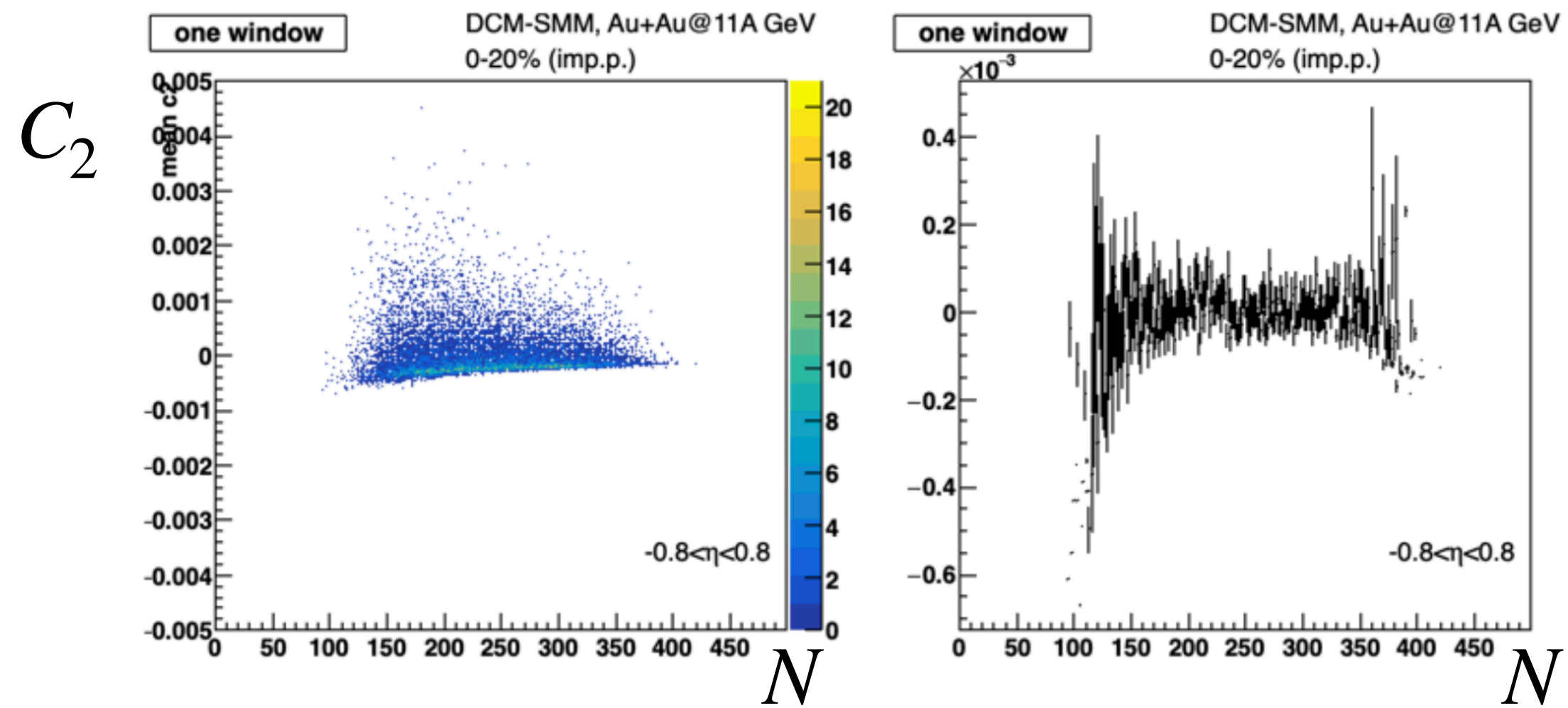
## Findings:

- Slightly negative correlations for ‘true’ central events
- Well reproduced by all centrality selection methods





# Fluct. measures



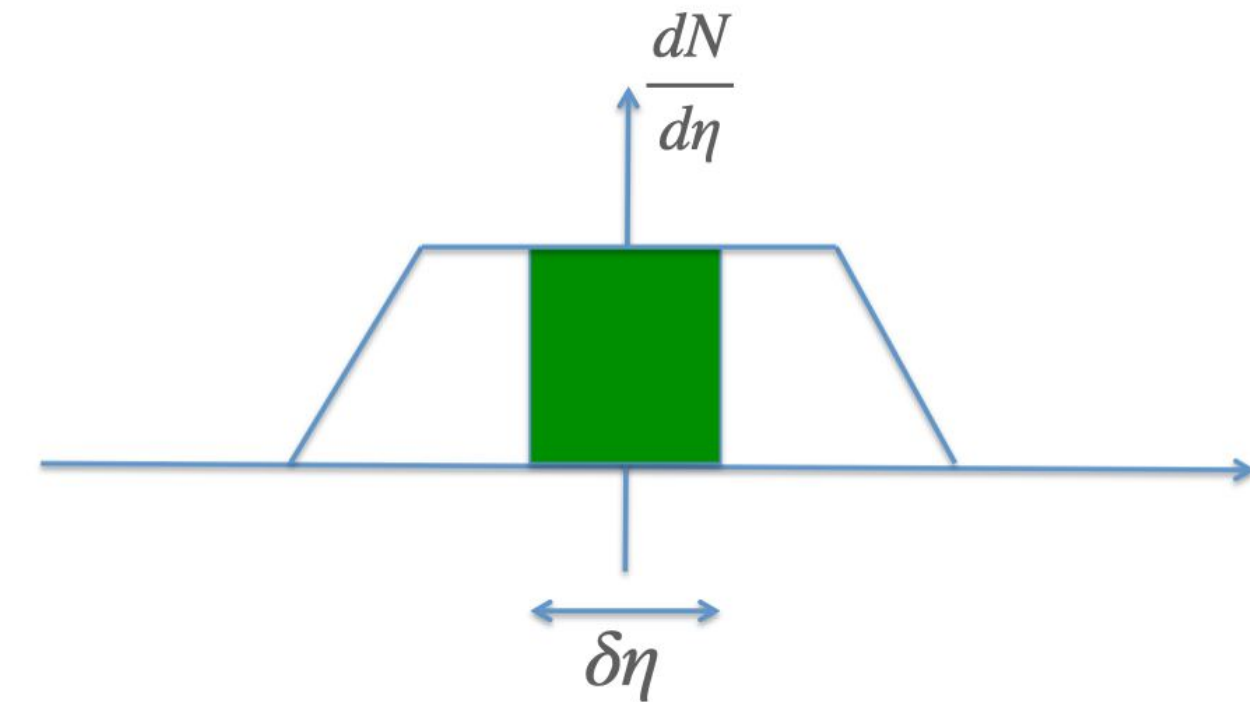
Findings:

- $C_2$  is well reproduced for central events
- Clearly larger statistics is needed for more precise conclusions

# Fluct. measures

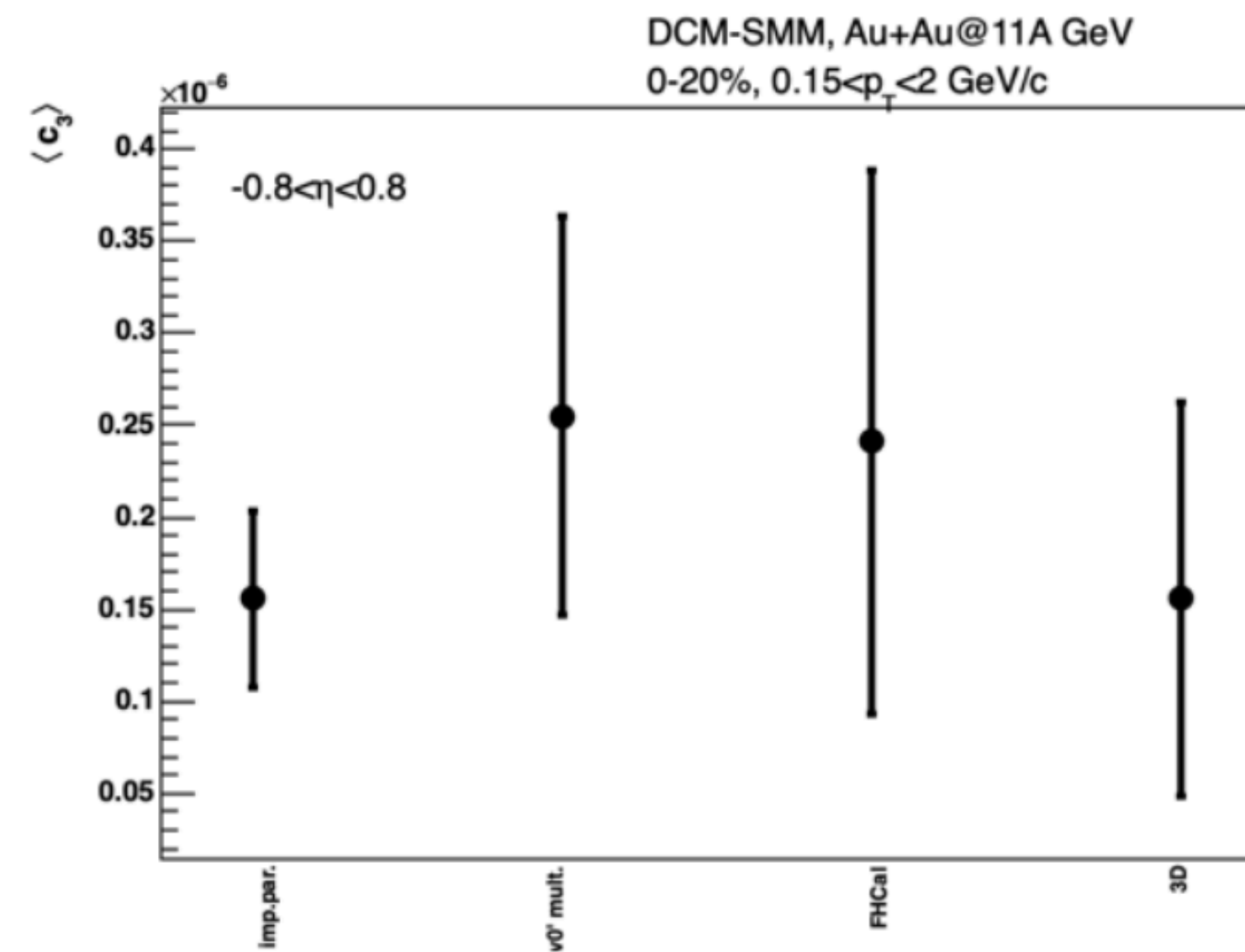
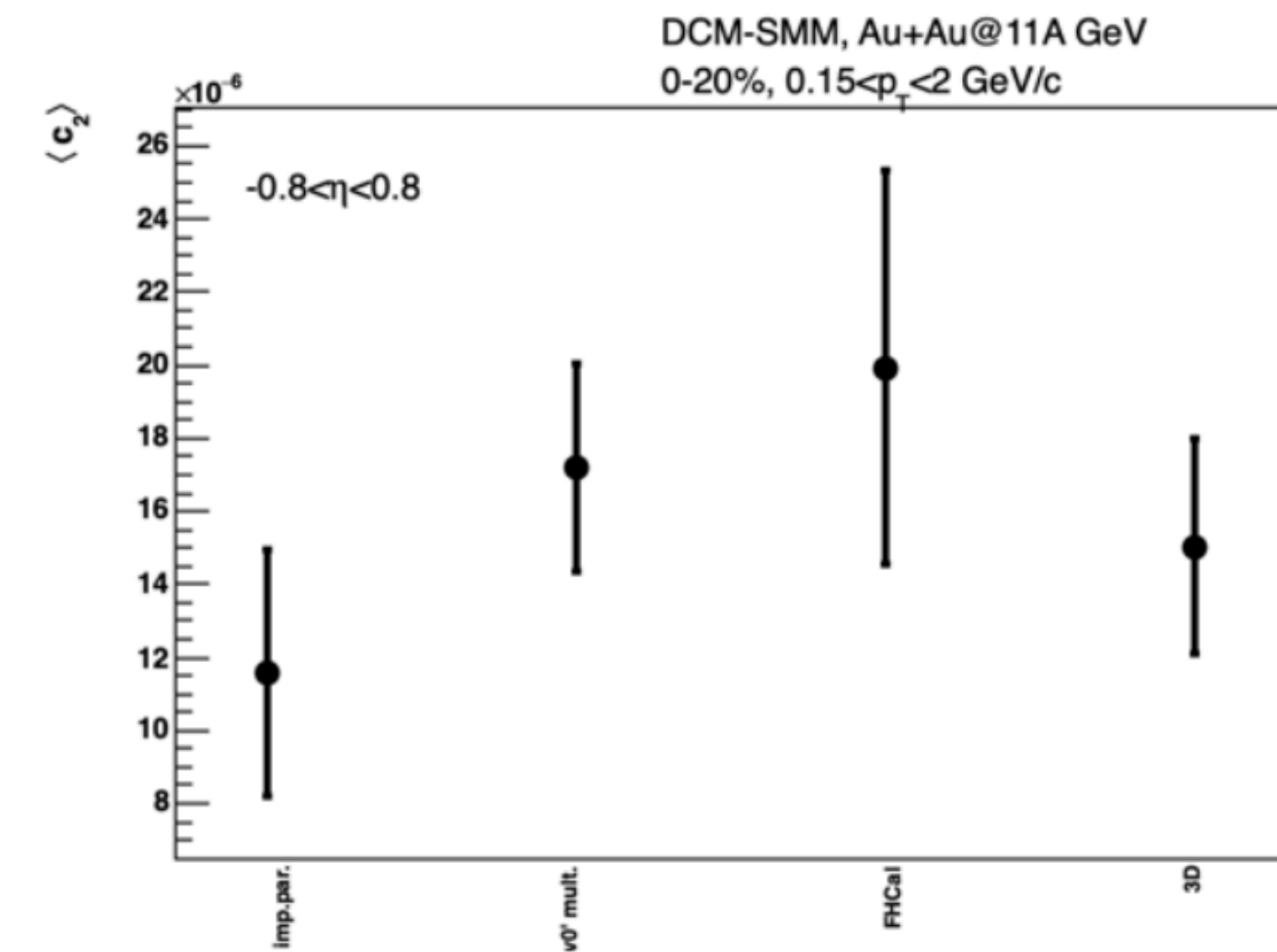
For 1 subevent:

- $p_T$  ‘correlators’  $C_2$  and  $C_3$  with an integrated multiplicity

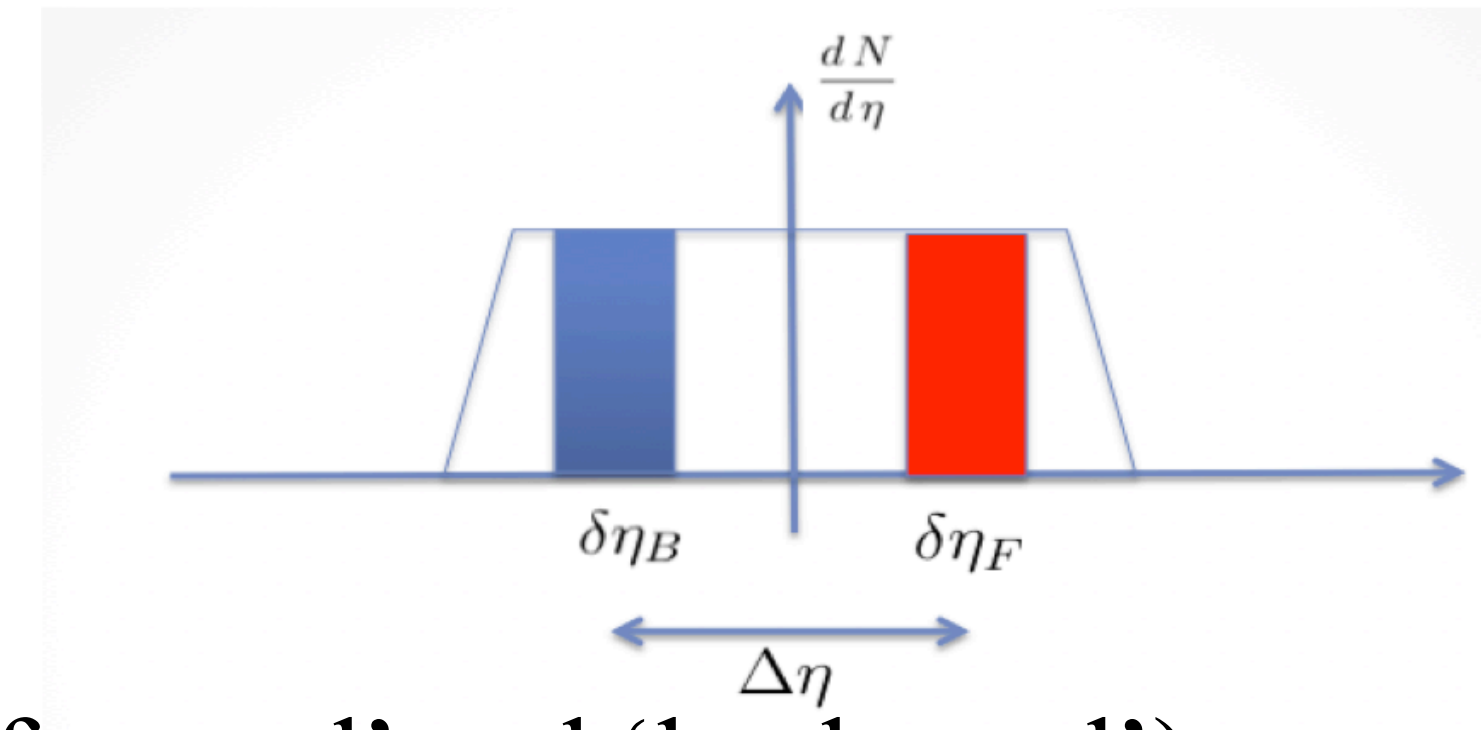


## Findings:

- $C_2$  and  $C_3$  are well reproduced for central events (within stat. uncert.)
- For more peripheral events FHCAL method deviates significantly



# Observables

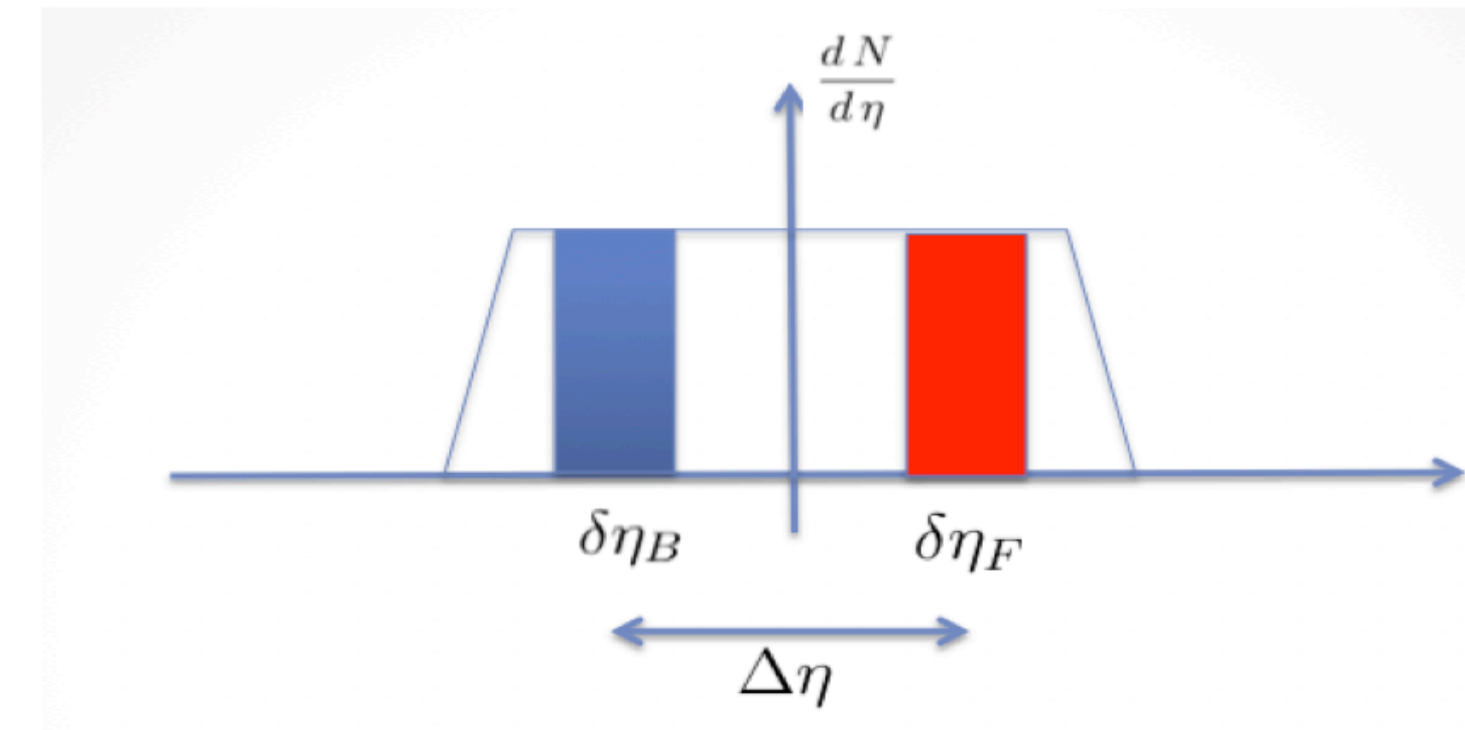


For 2 subevents (typically, two pseudorapidity intervals called ‘forward’ and ‘backward’):

- multiplicity of charged hadrons  $(N)_{F,B}$
- net electric charge  $(N_+ - N_-)_{F,B}$
- sum of transverse momenta of charged hadrons  $(P_T = \sum_{i=1}^N p_{T,(i)})_{F,B}$
- mean transverse momentum in an event  $(M(p_T) = \frac{P_T}{N})_{F,B}$

In this project we limit ourselves to F-B multiplicities correlations and F-B  $p_T$  ‘correlators’

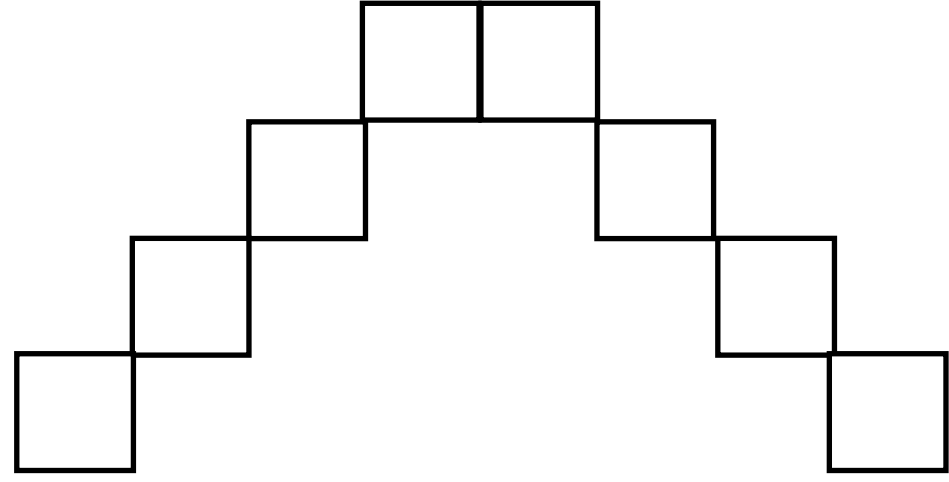
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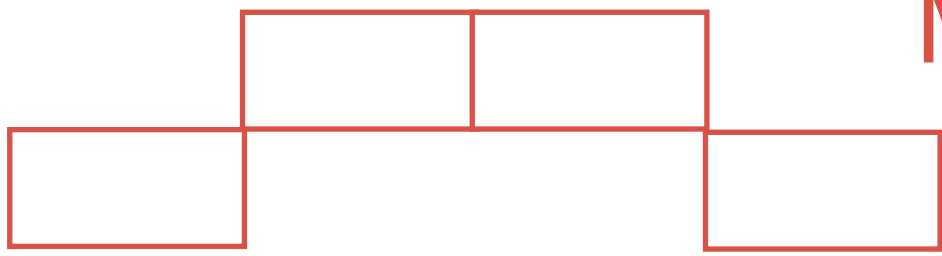
- correlation coefficient  $b_{corr} = \frac{\langle N_F \cdot N_B \rangle - \langle N_F \rangle \cdot \langle N_B \rangle}{\langle N_F^2 \rangle - \langle N_F \rangle^2}$  (not strongly intensive) ALICE, JHEP 05, 097 (2015)
- strongly intensive  $\Sigma[N_F, N_B] = \frac{\langle N_B \rangle \omega[N_F] + \langle N_F \rangle \omega[N_B] - 2 (\langle N_F \cdot N_B \rangle - \langle N_F \rangle \cdot \langle N_B \rangle)}{\langle N_F + N_B \rangle}$  M. Gorenstein, M. Gazdzicki, Phys. Rev. C84, 014904 (2011)  
E. Andronov, Theor.Math.Phys. 185, 1383 (2015)
- asymmetry  $C = \frac{N_F - N_B}{\sqrt{N_F + N_B}}$  PHOBOS, Phys.Rev. C 74, 011901(R) (2006)
- almost strongly intensive  $\sigma^2(C) = \langle C^2 \rangle - \langle C \rangle^2 \approx \Sigma[N_F, N_B]$  (under certain assumptions valid for high multiplicities)

# Subevents configurations



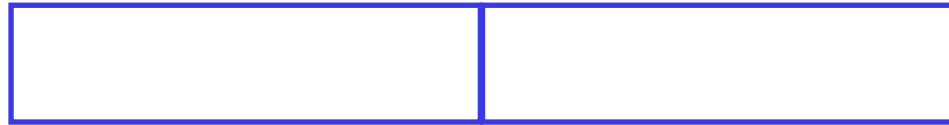
Small windows

$$\delta\eta = 0.2$$



Medium windows

$$\delta\eta = 0.4$$

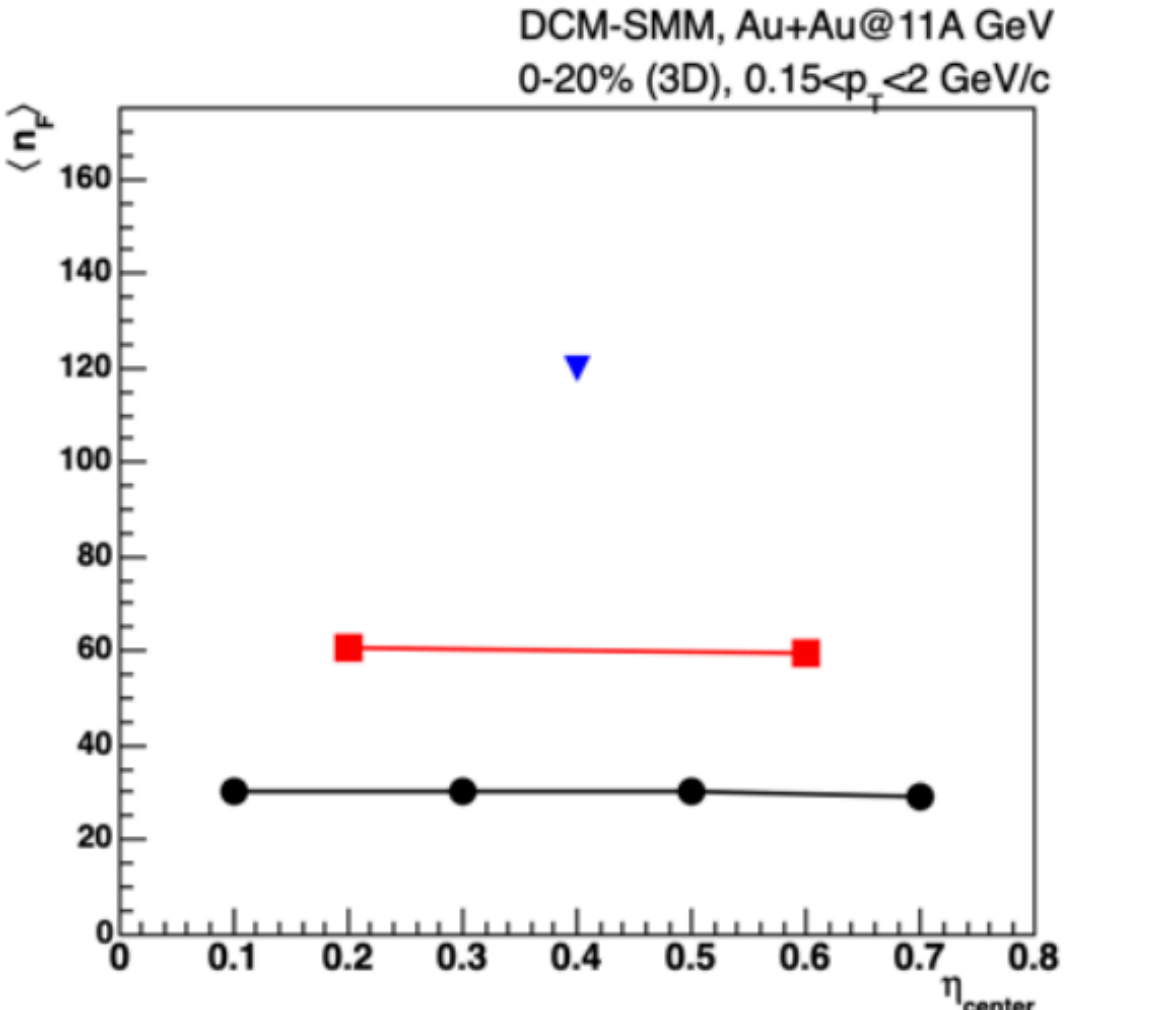
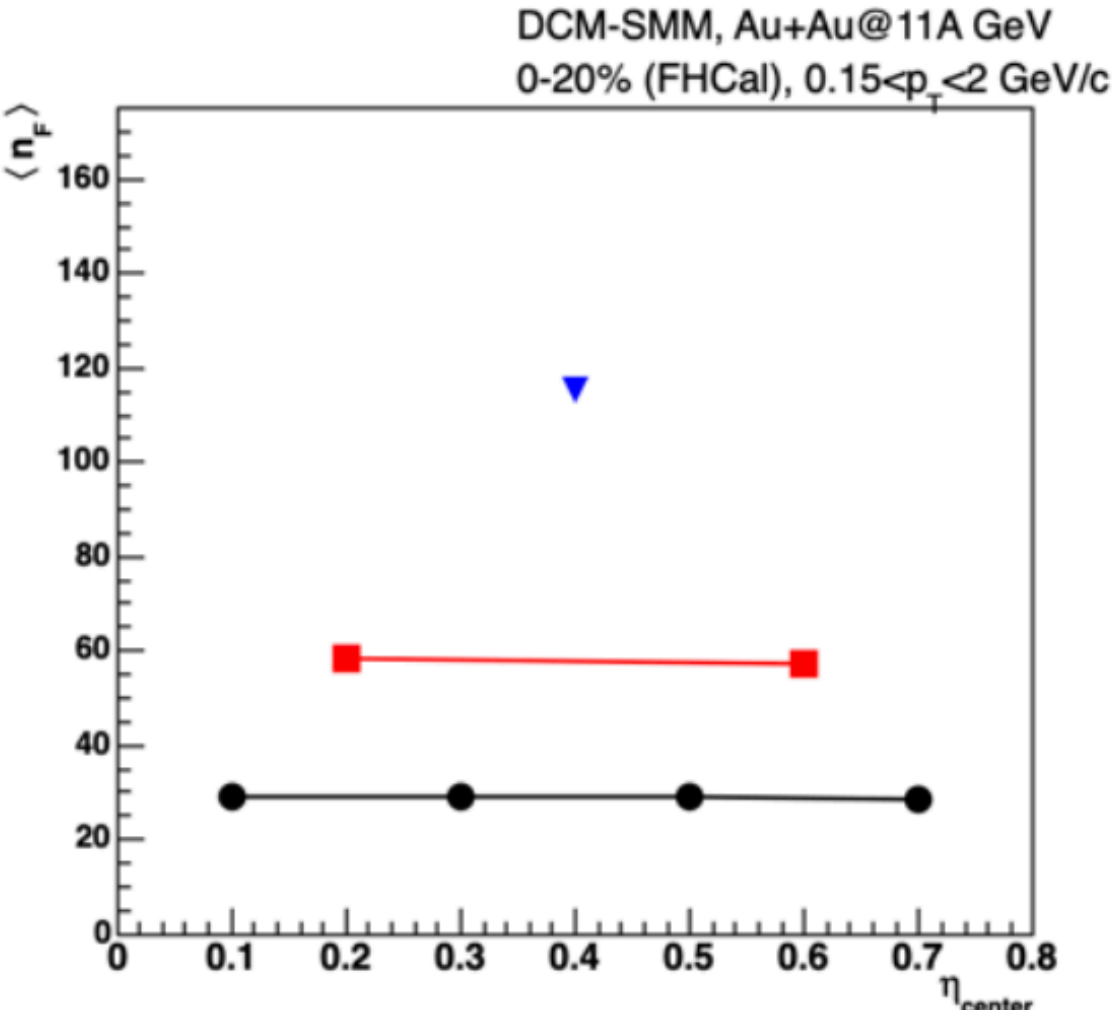
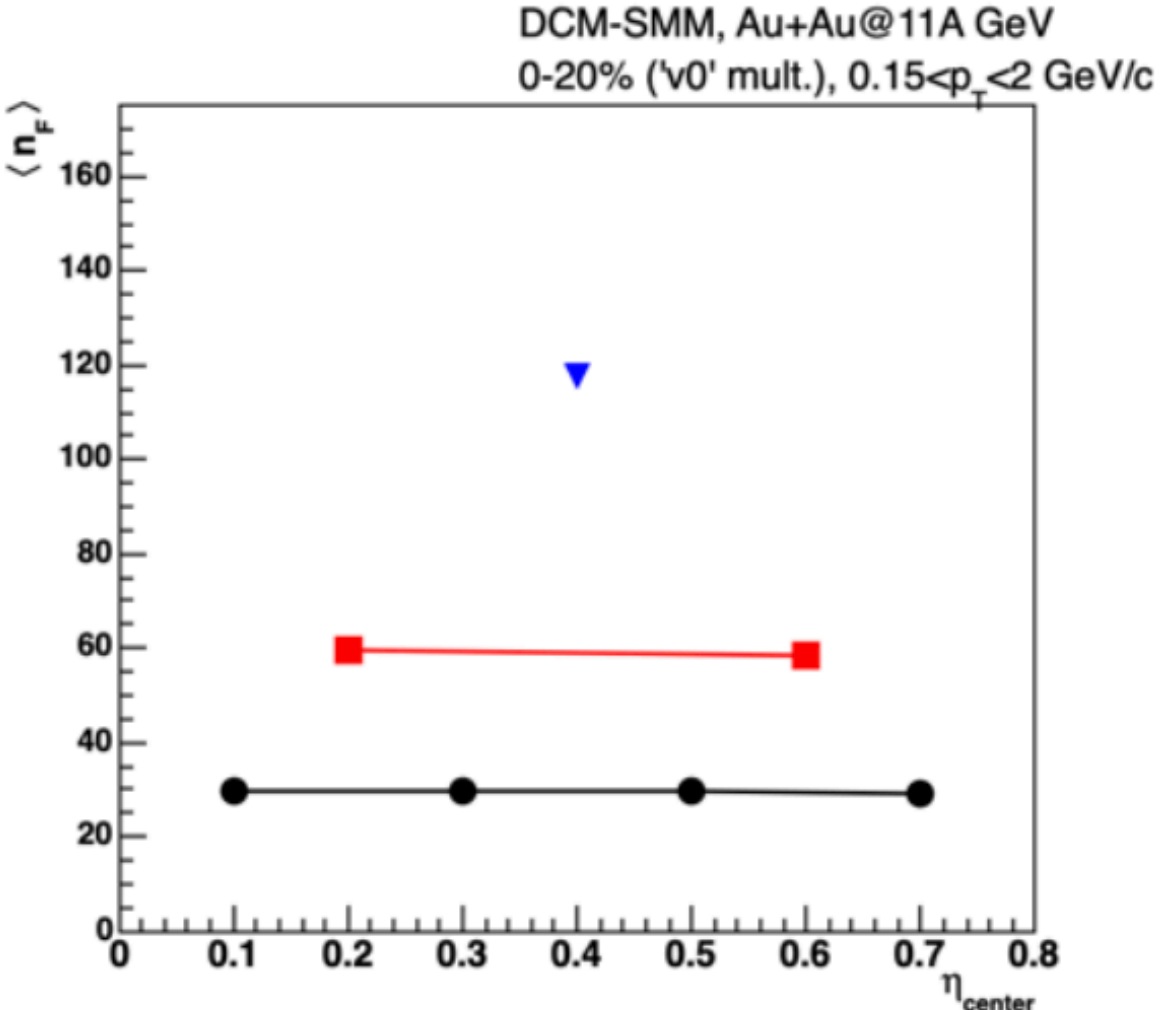
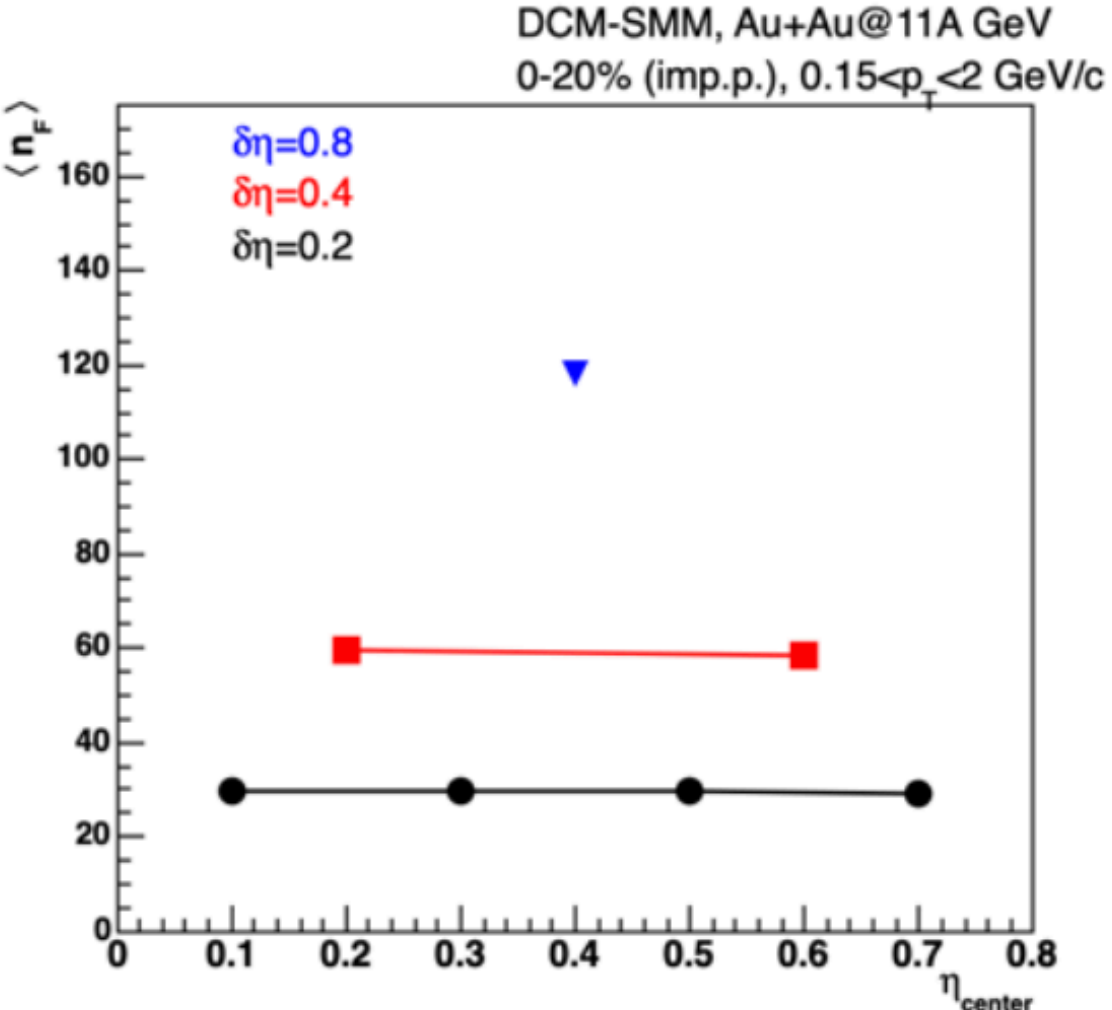


Large windows

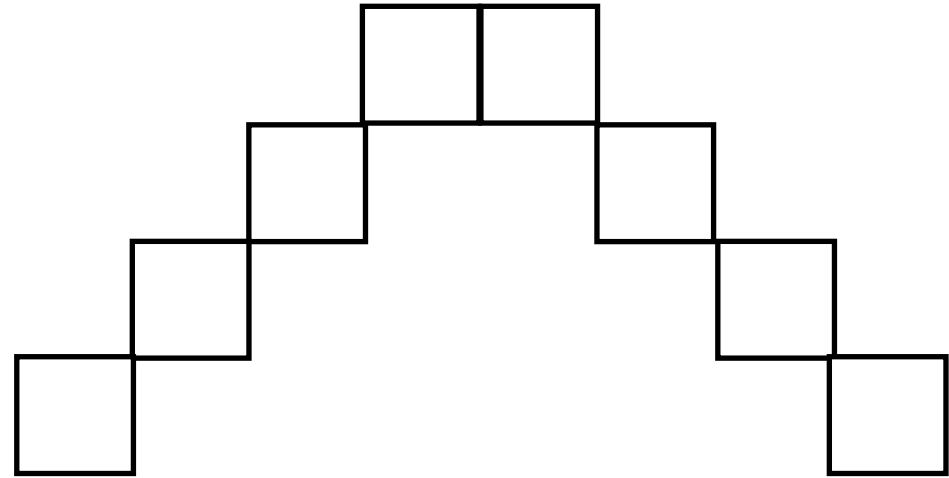
$$\delta\eta = 0.8$$

Findings:

- mean multiplicities in forward windows are well reproduced

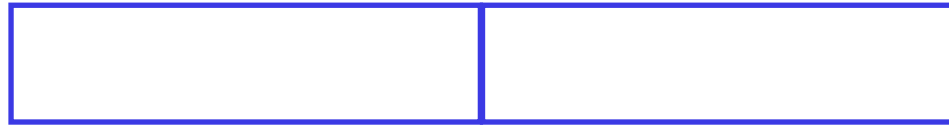
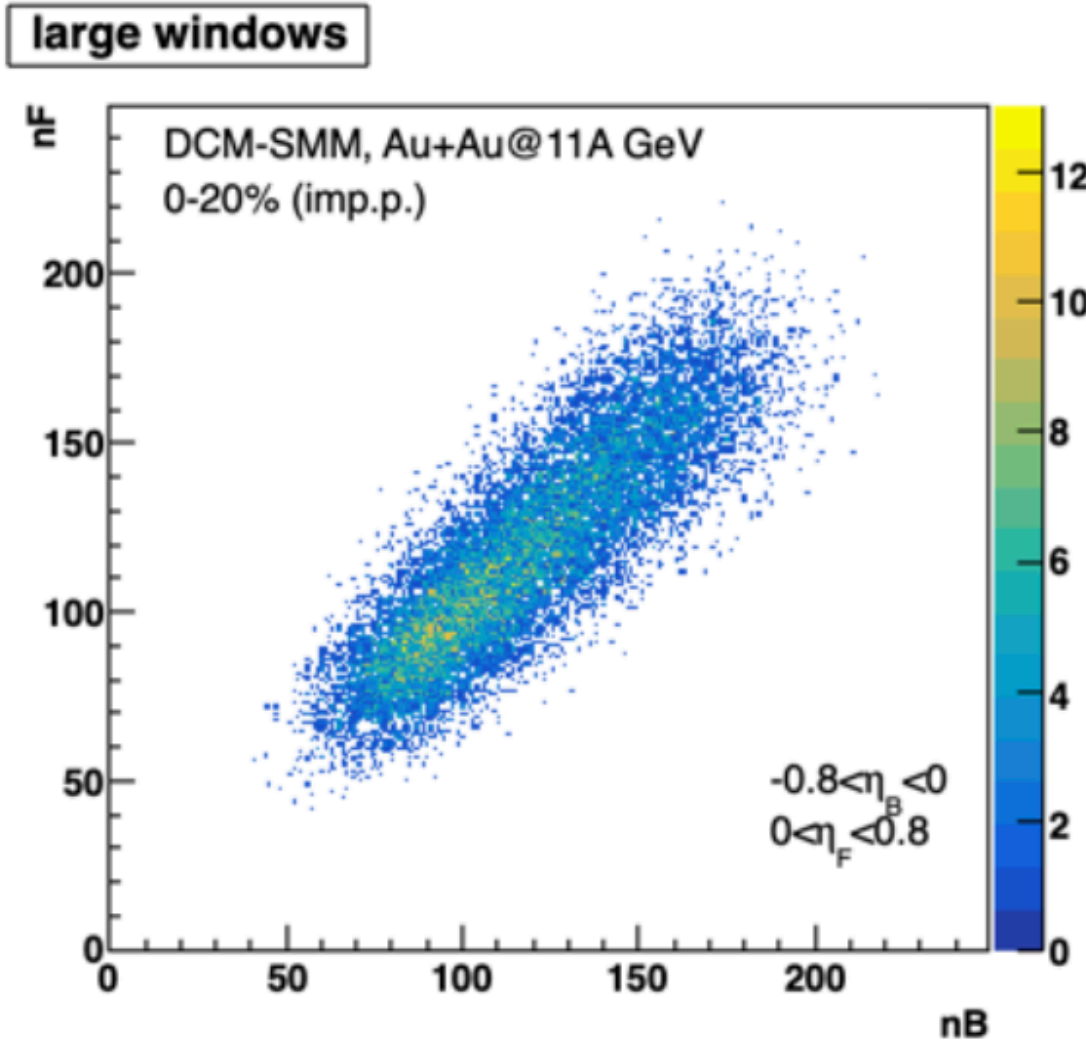
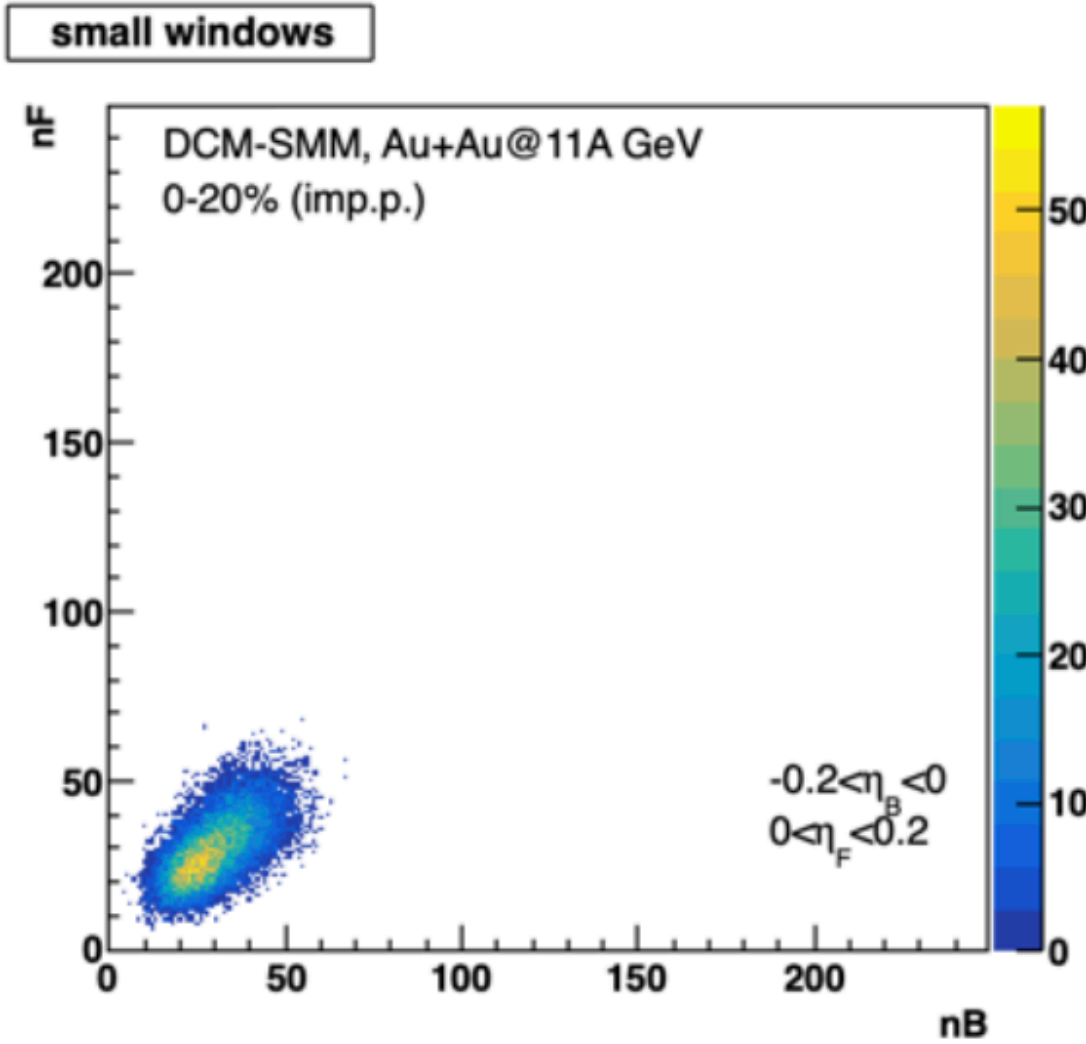


# Subevents configurations and $\langle N_F \rangle$



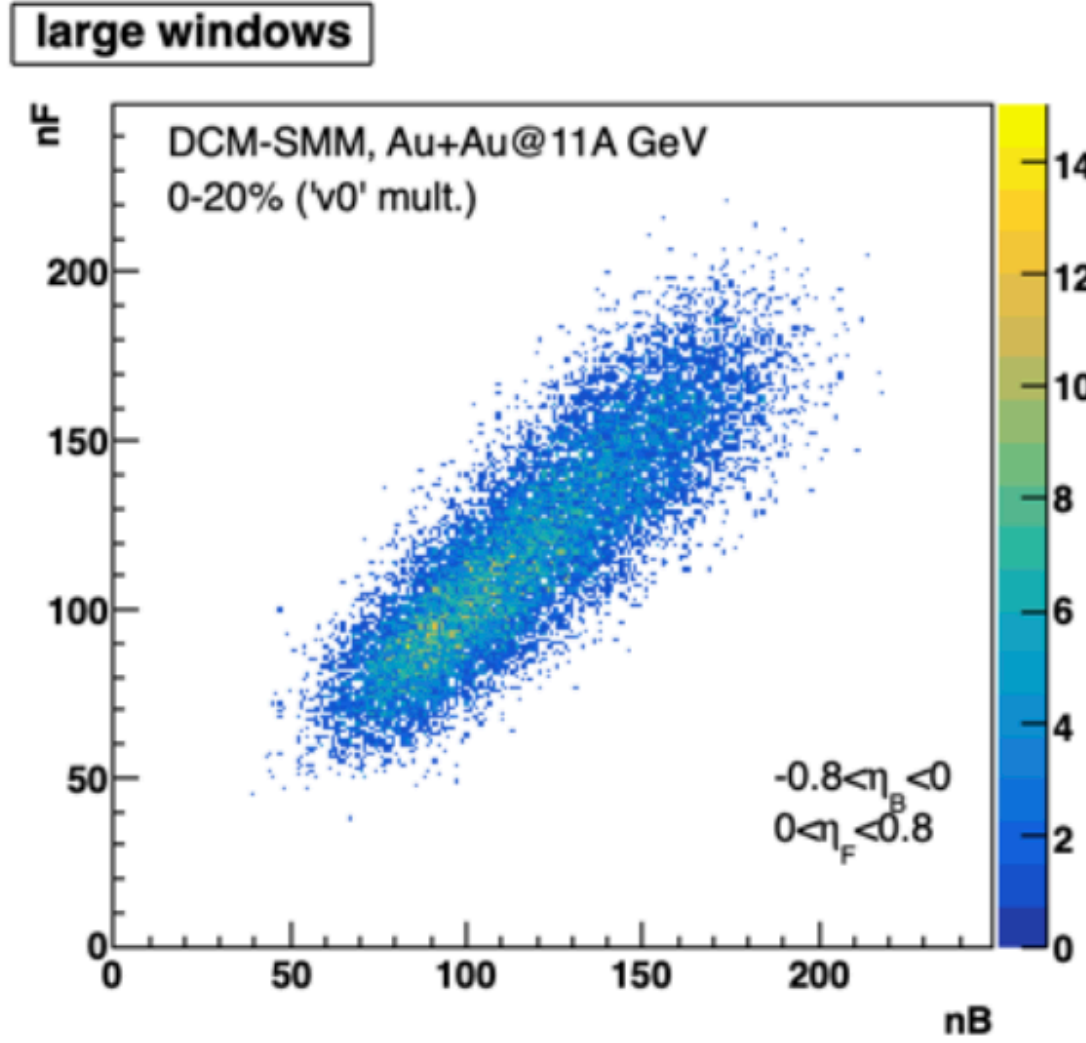
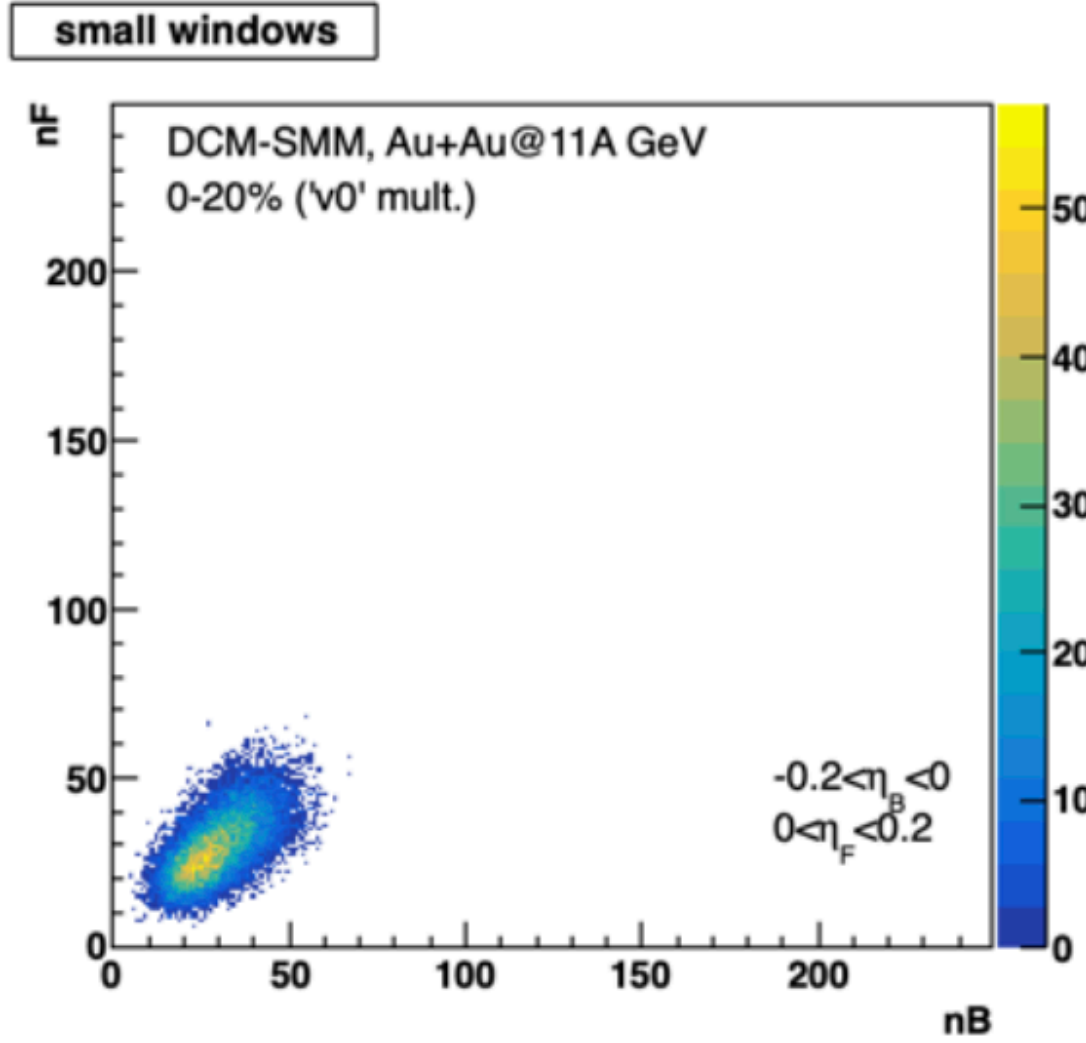
Small windows

$$\delta\eta = 0.2$$



Large windows

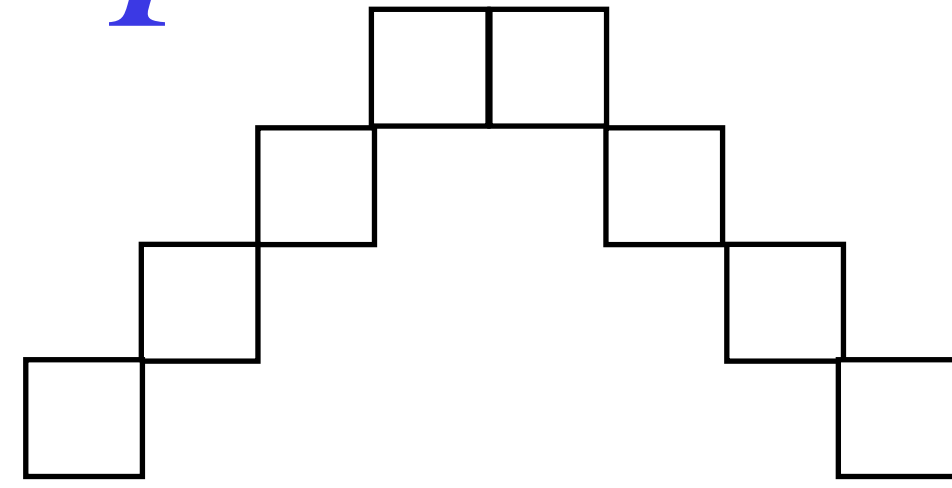
$$\delta\eta = 0.8$$



Findings:

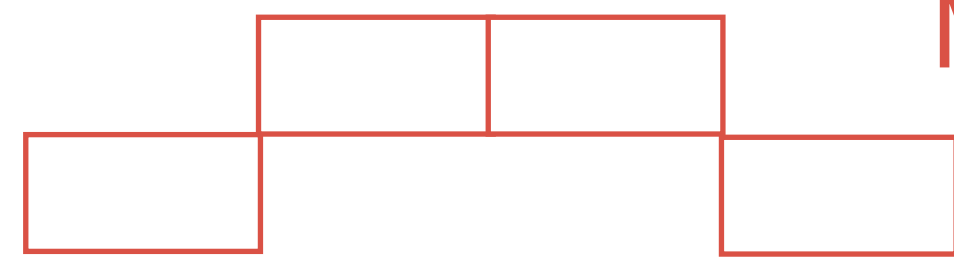
- the shape of the correlation ‘cloud’ looks similar to the true distribution

# $\omega[N_F]$



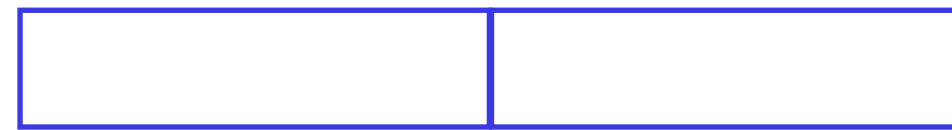
Small windows

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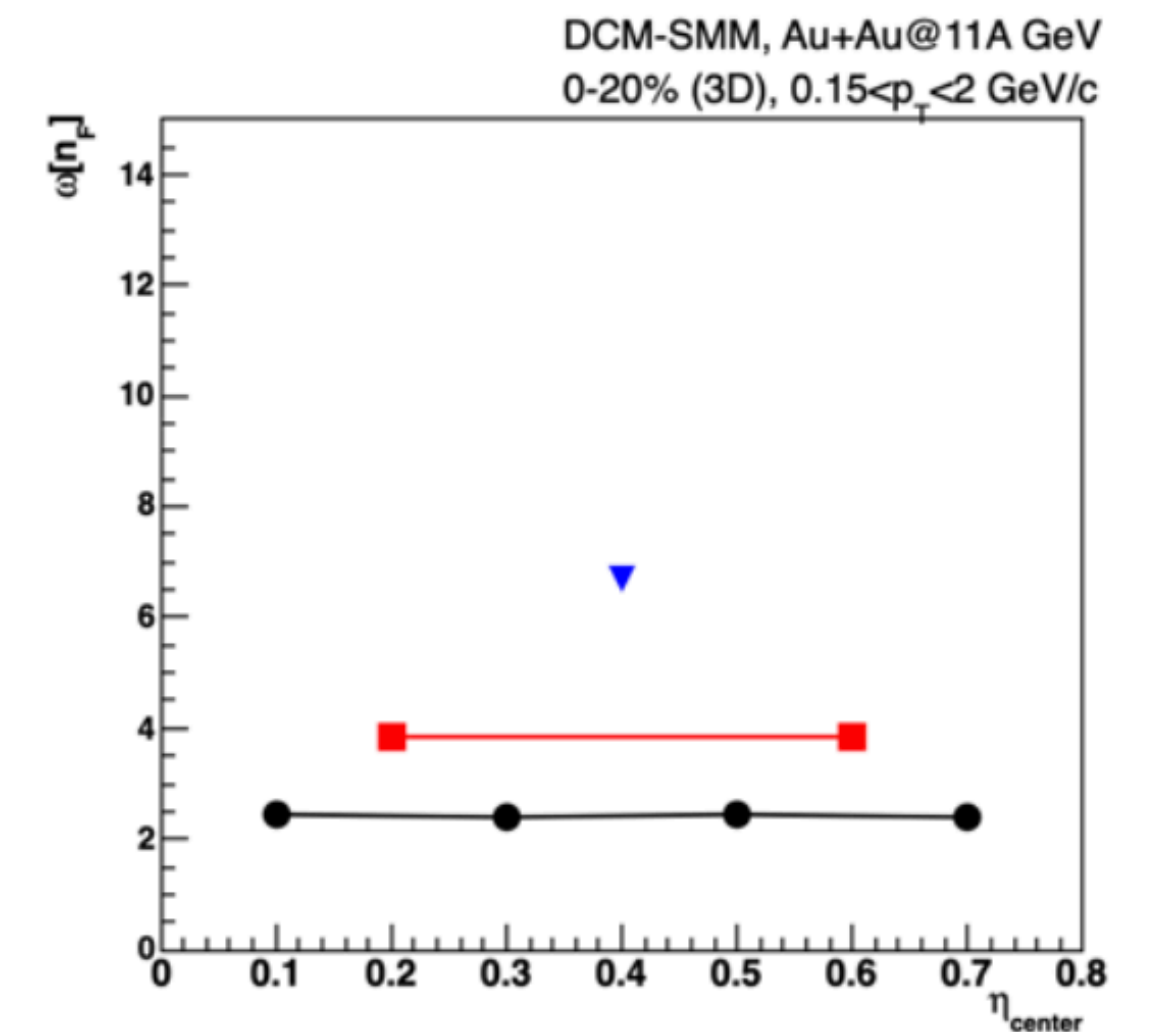
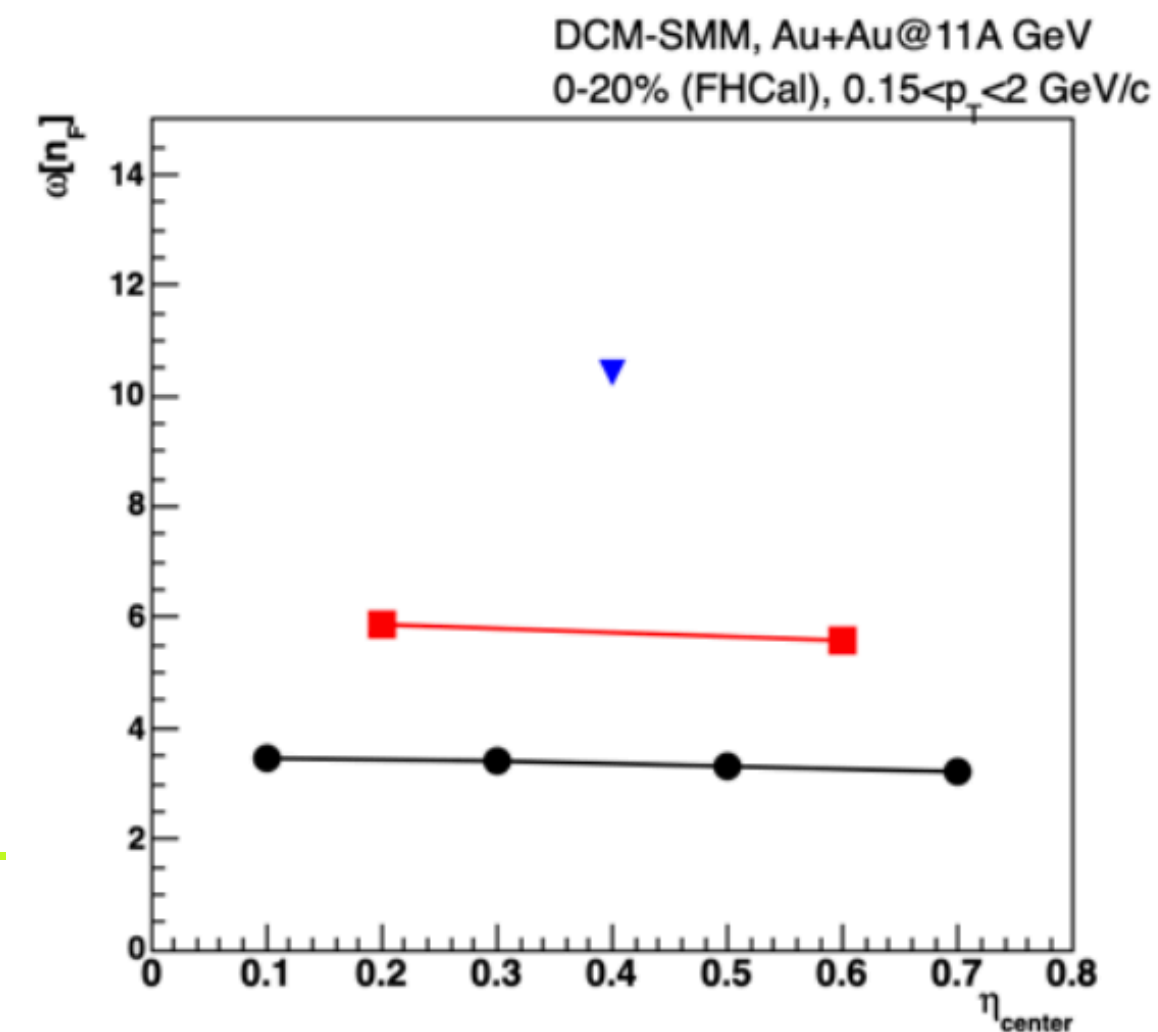
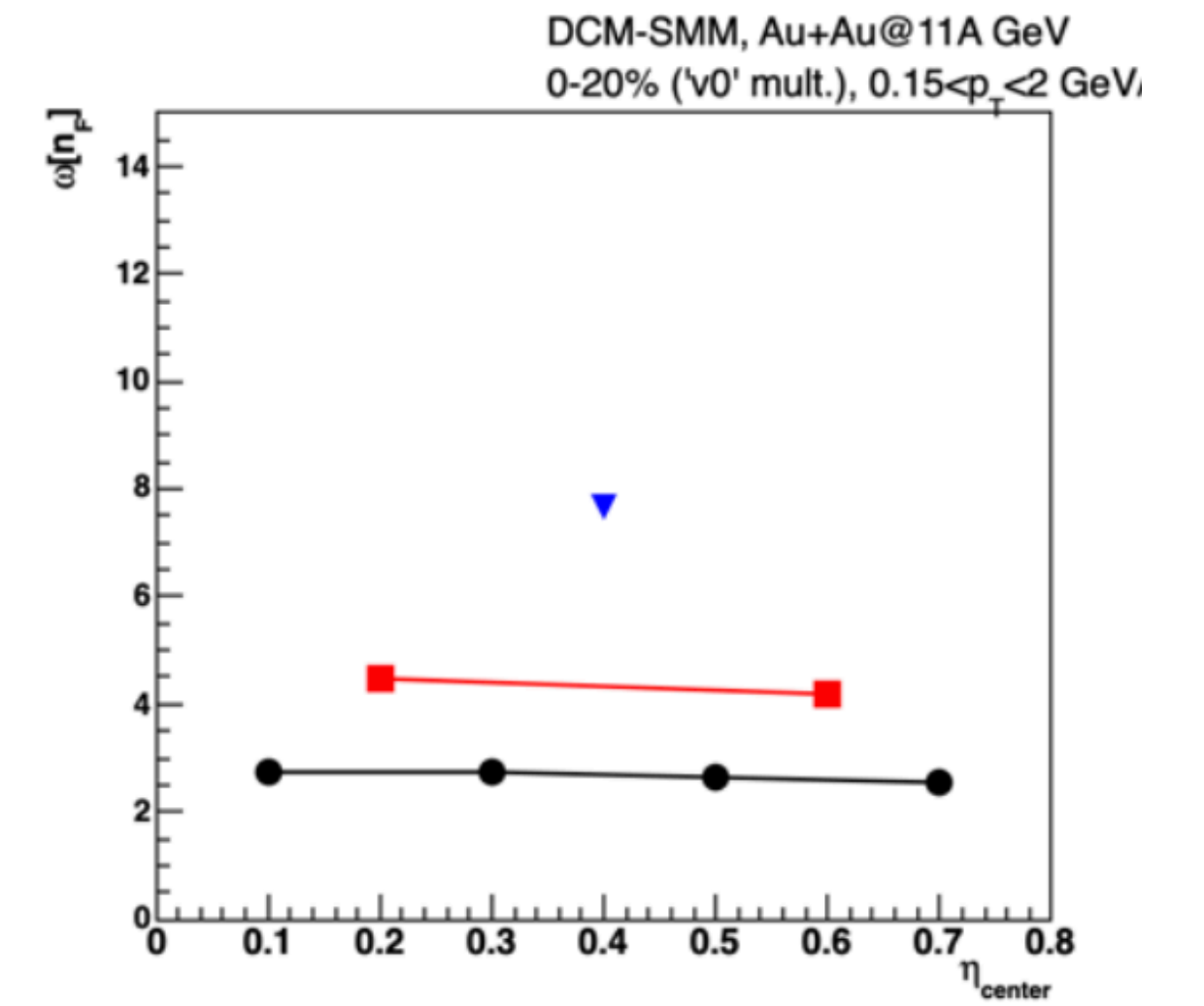
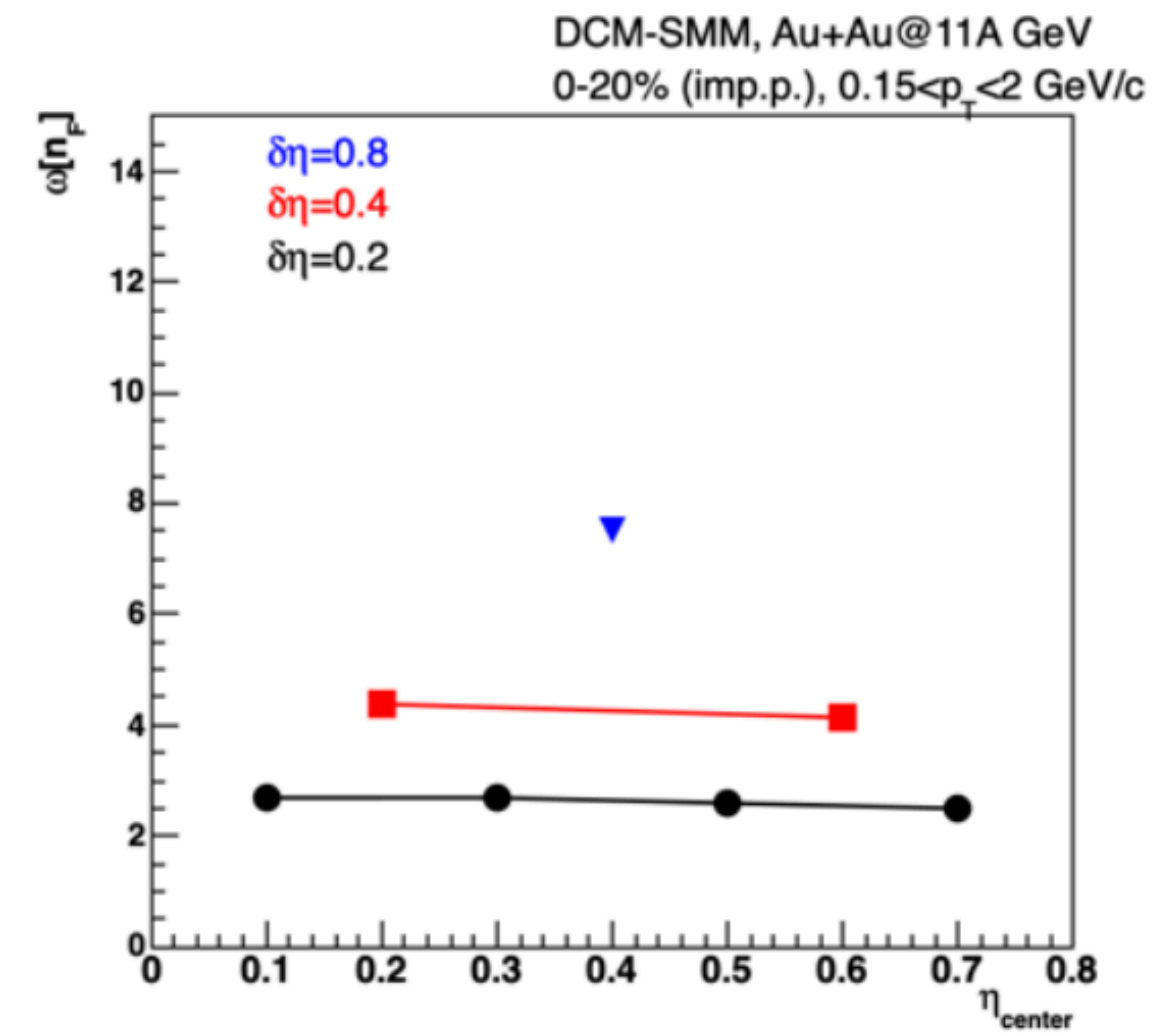


Large windows

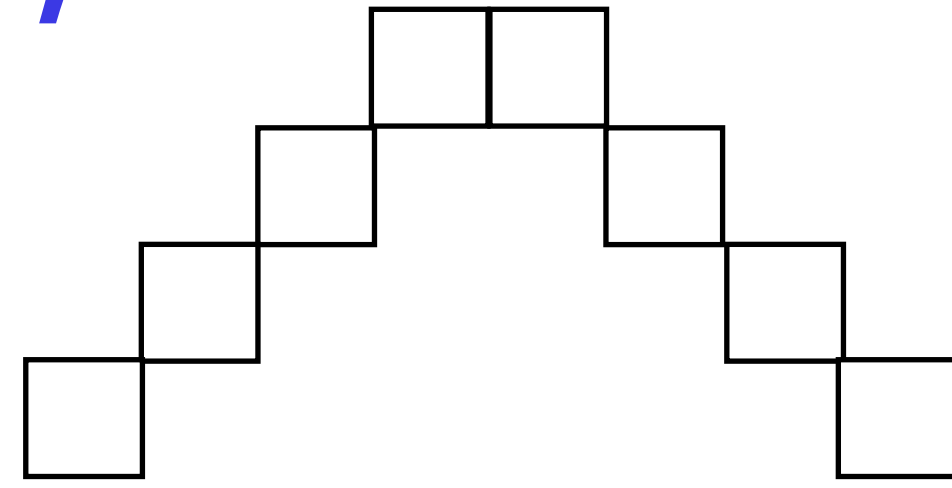
$$\delta\eta = 0.8$$

Findings:

- scaled variances for forward windows are deviated for 3D method

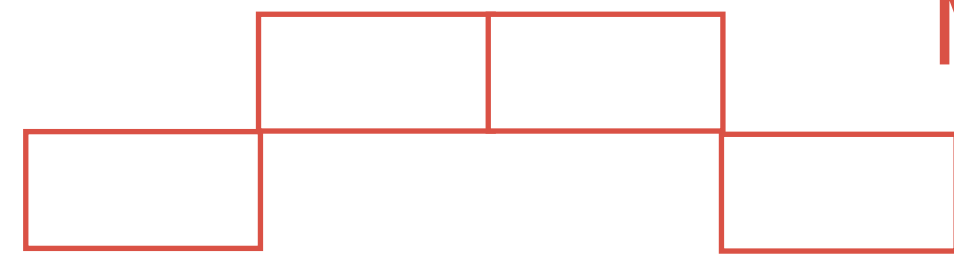


# $b_{corr}$



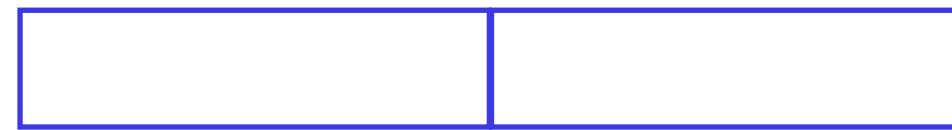
Small windows

$$\delta\eta = 0.2$$



Medium windows

$$\delta\eta = 0.4$$

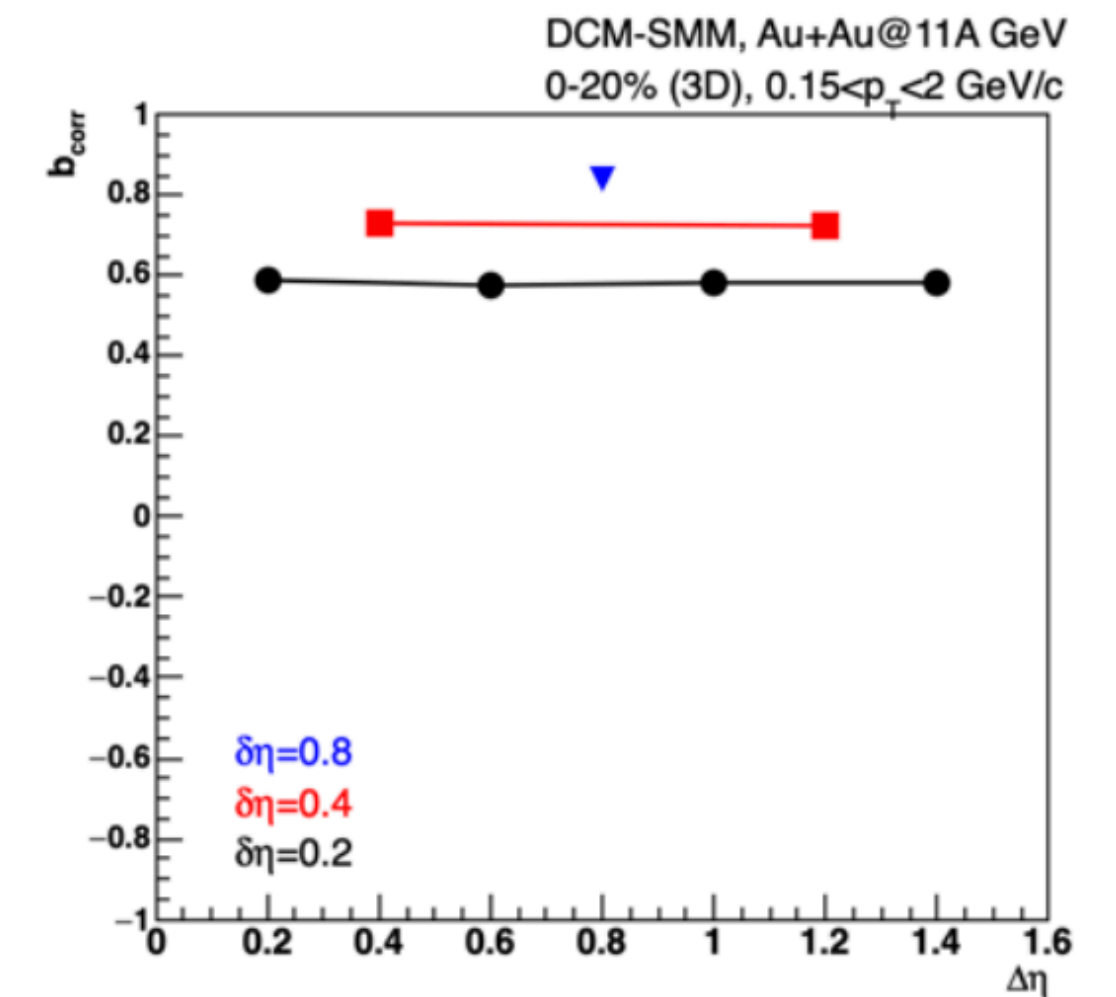
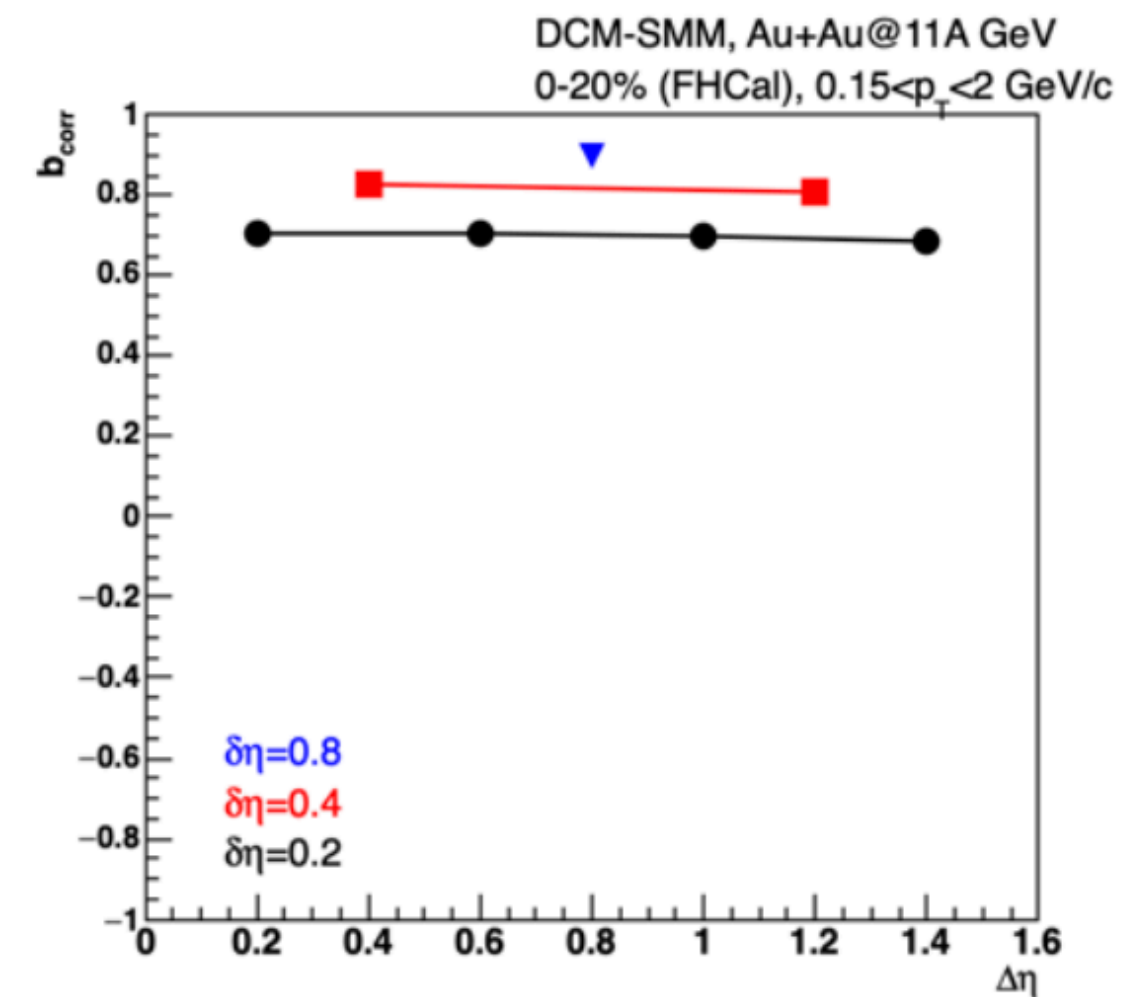
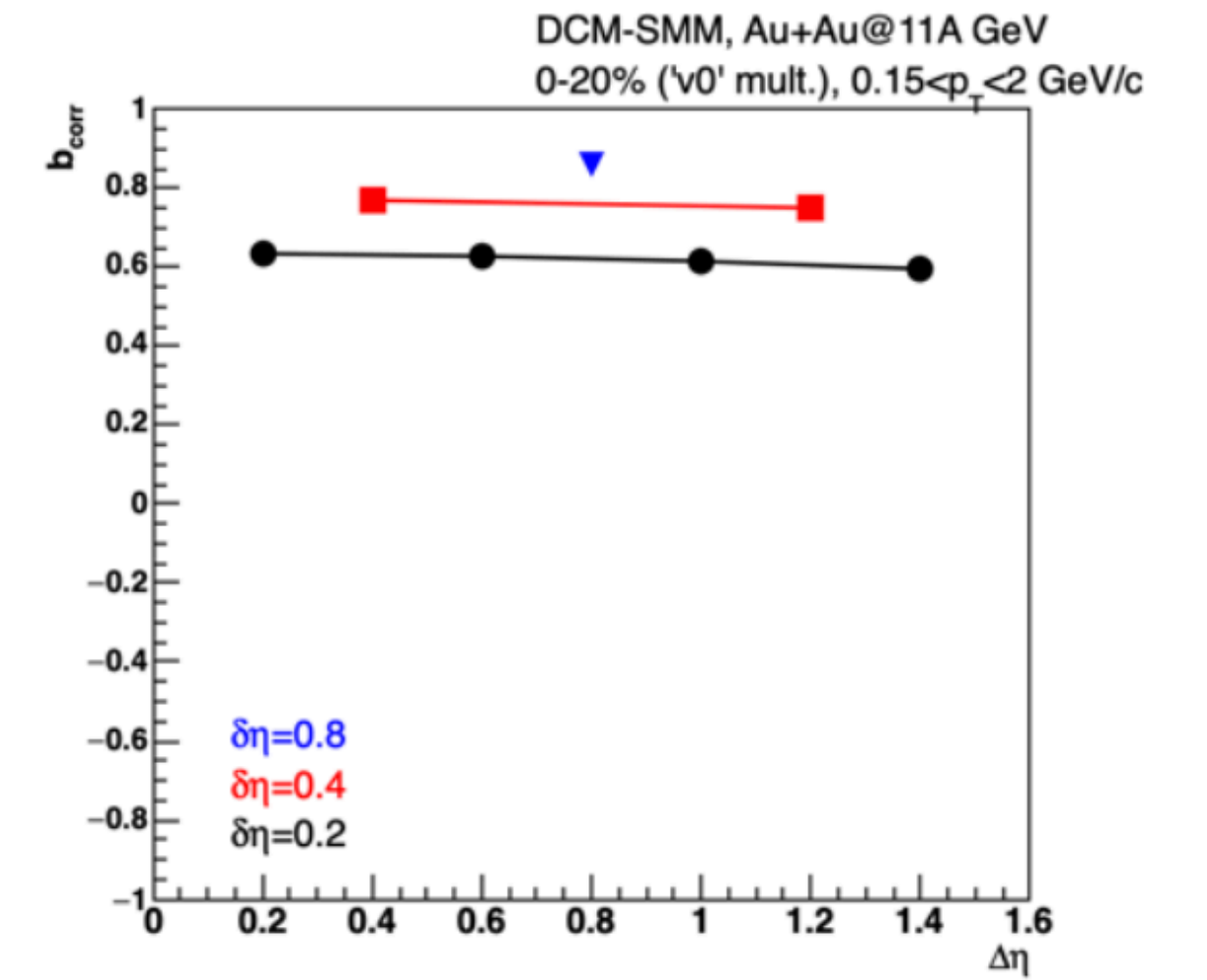
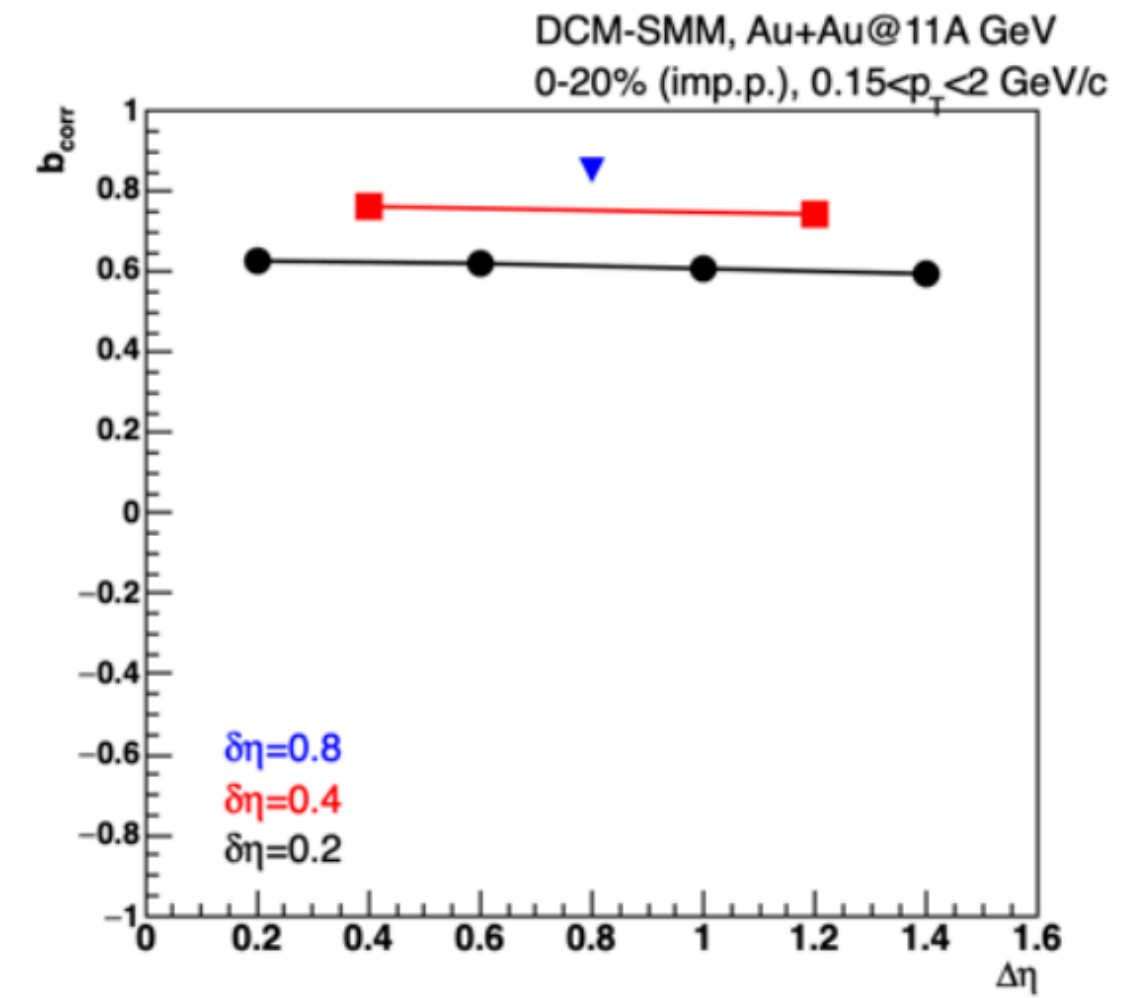


Large windows

$$\delta\eta = 0.8$$

Findings:

- deviations for FHCAL and 3d method are present

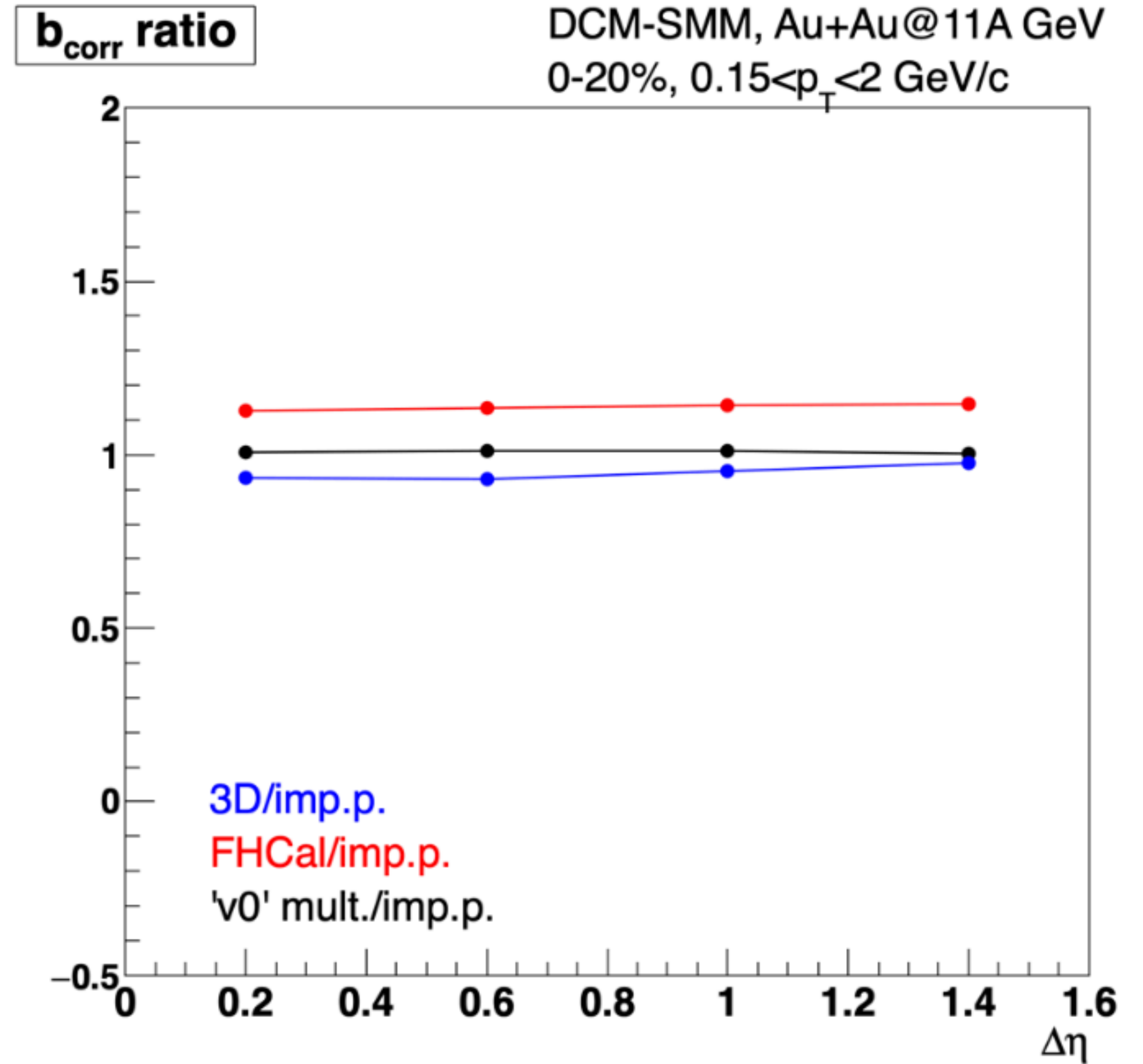




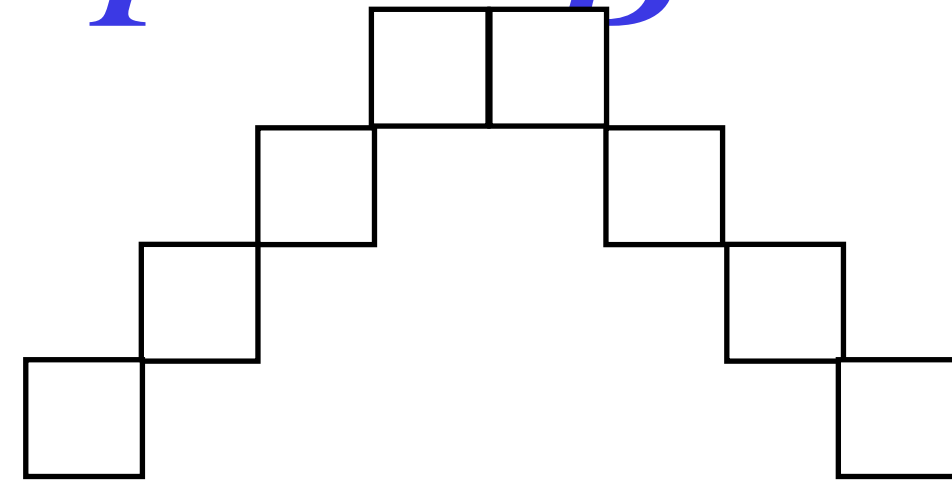
# $b_{corr}$

## Findings:

- for central events all methods produce results that are close to the 'true' one
- for peripheral events FHCAL and 3d deviate even stronger (backup)

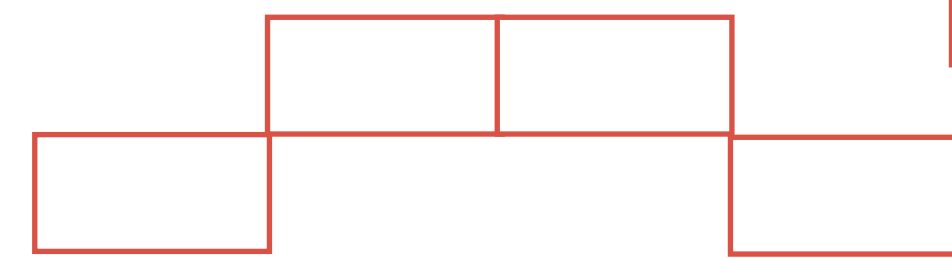


# $\Sigma[N_F, N_B]$



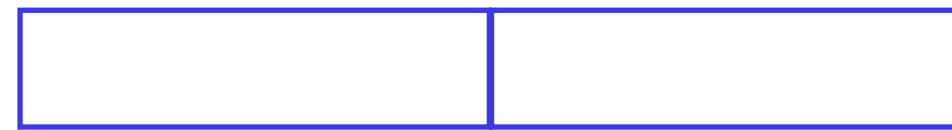
Small windows

$$\delta\eta = 0.2$$



Medium windows

$$\delta\eta = 0.4$$

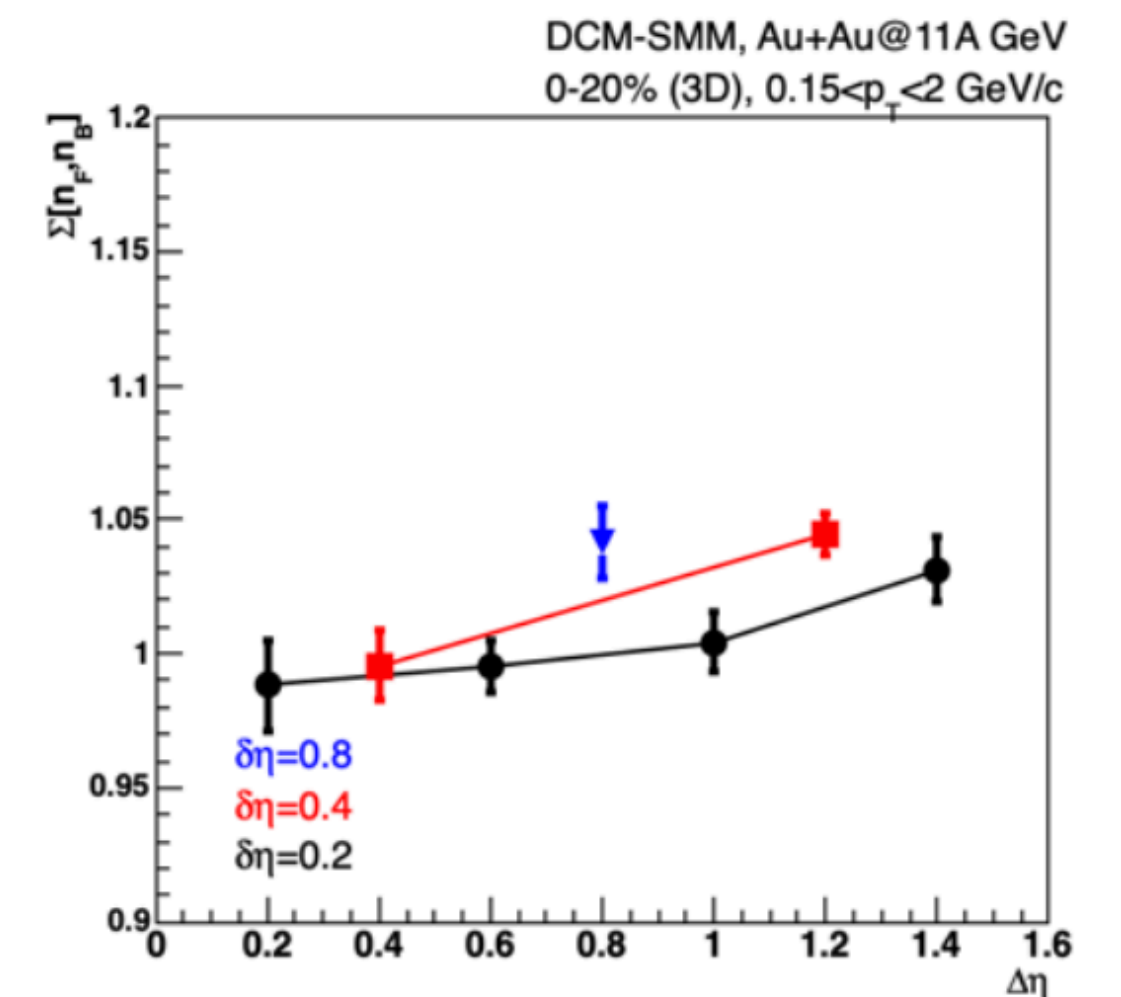
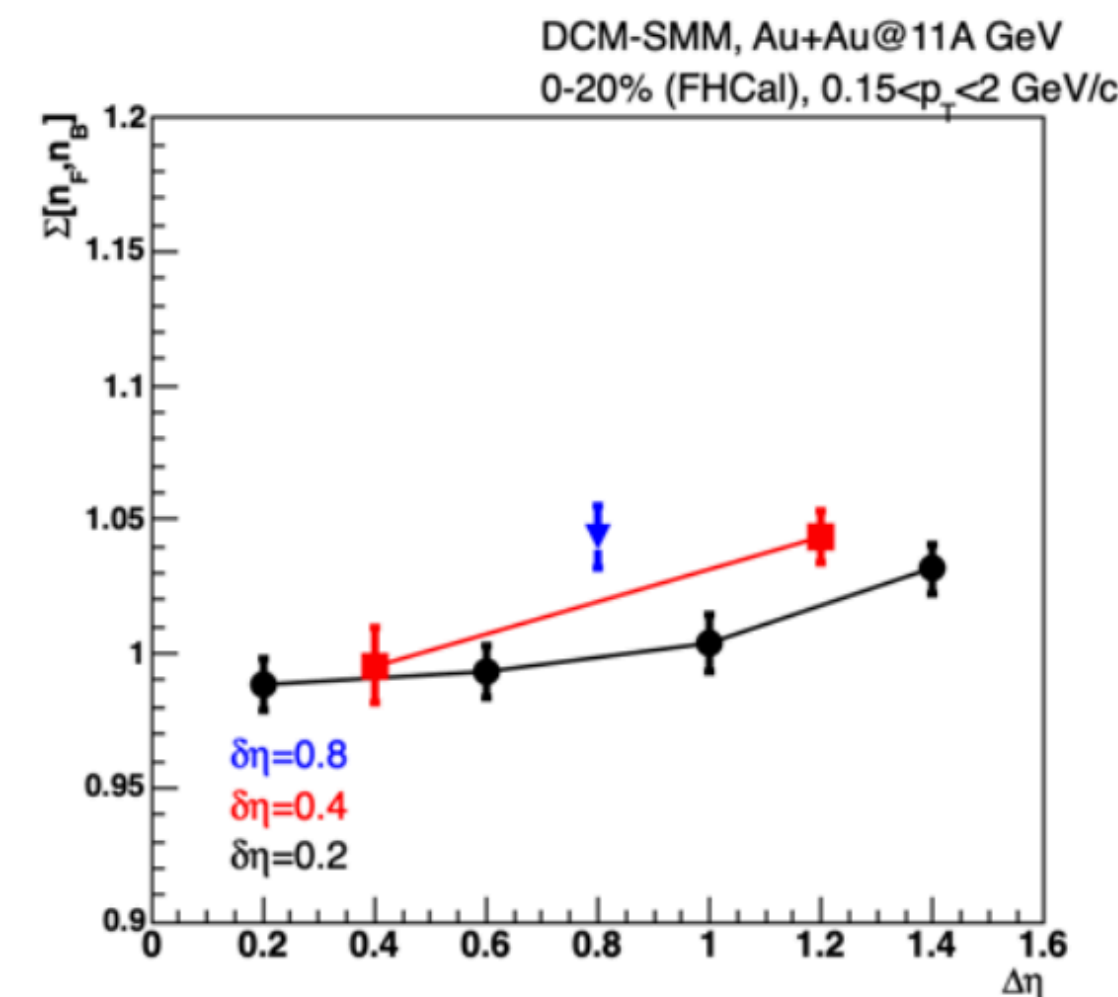
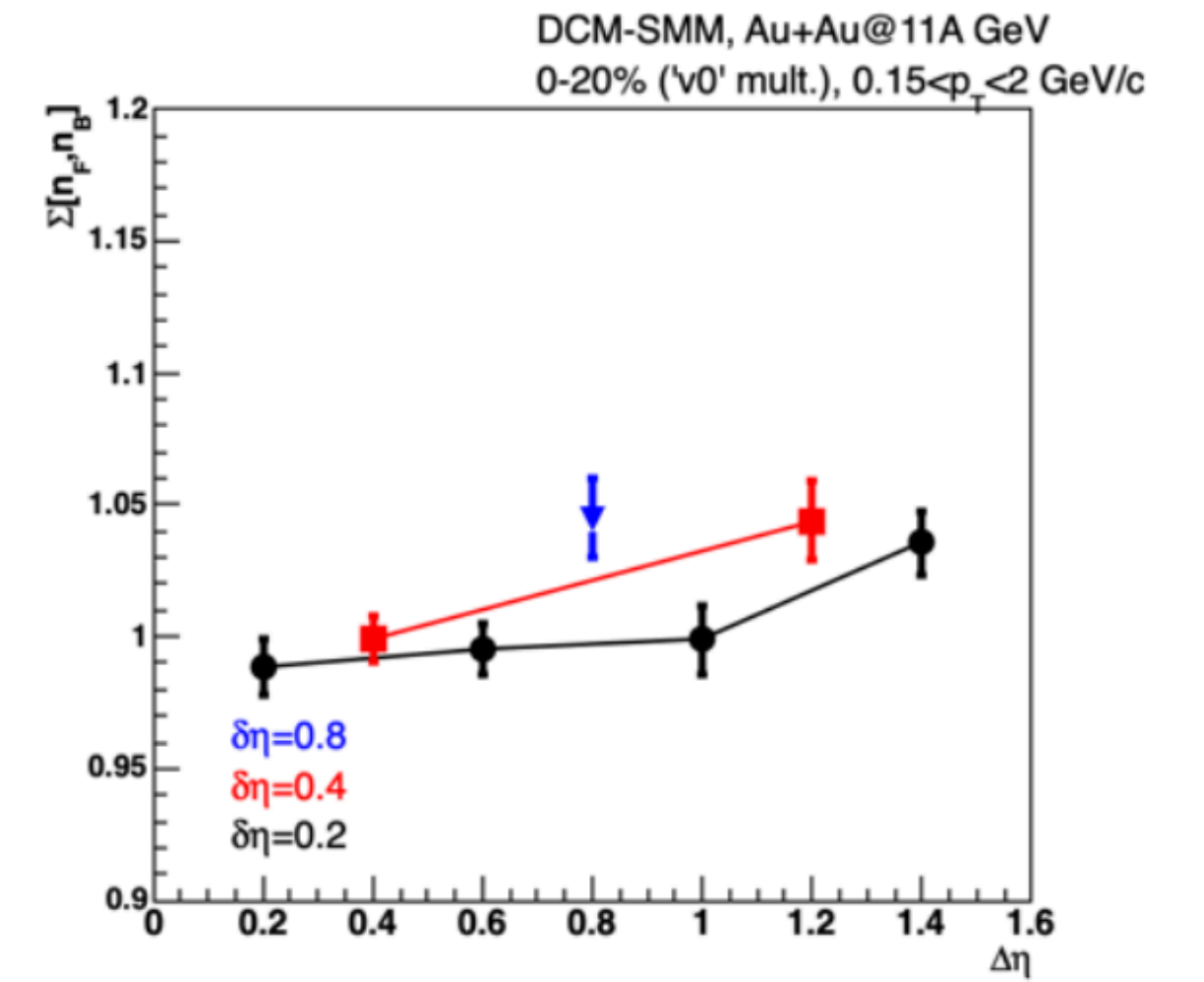
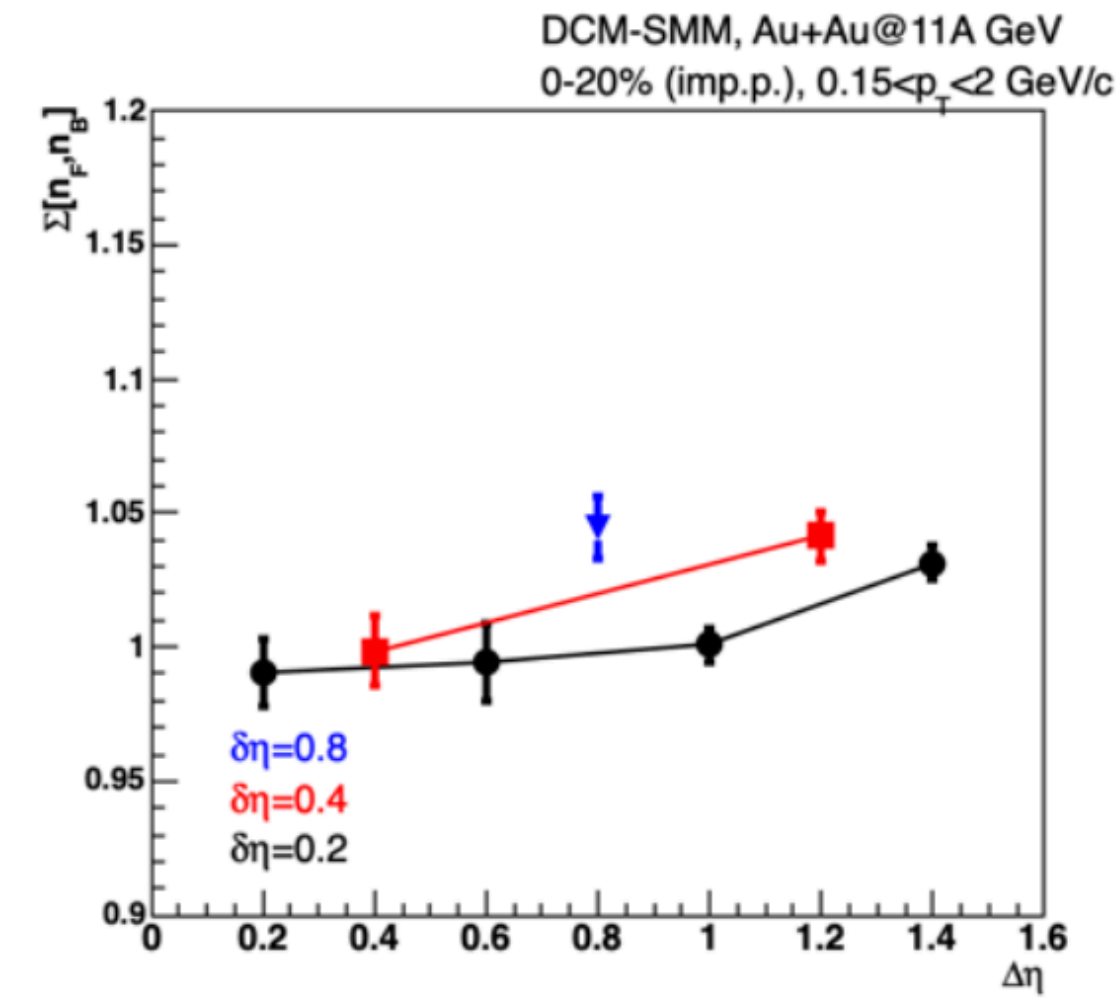


Large windows

$$\delta\eta = 0.8$$

## Findings:

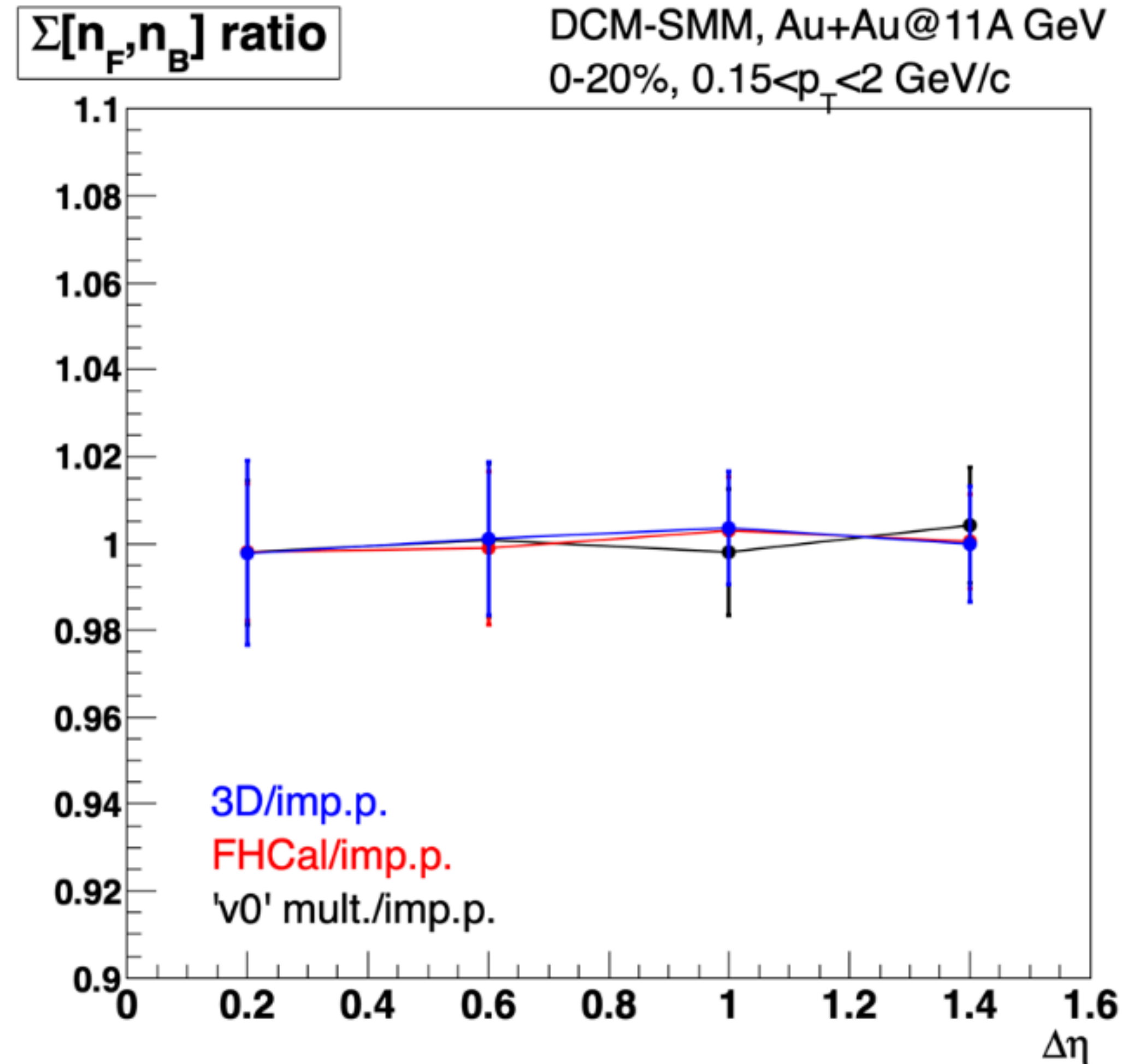
- very stable results for central and peripheral (backup)



# $\Sigma[N_F, N_B]$

## Findings:

- for all events all methods produce results that are close to the 'true' one
- the same is true for  $\sigma^2(C)$  (backup)



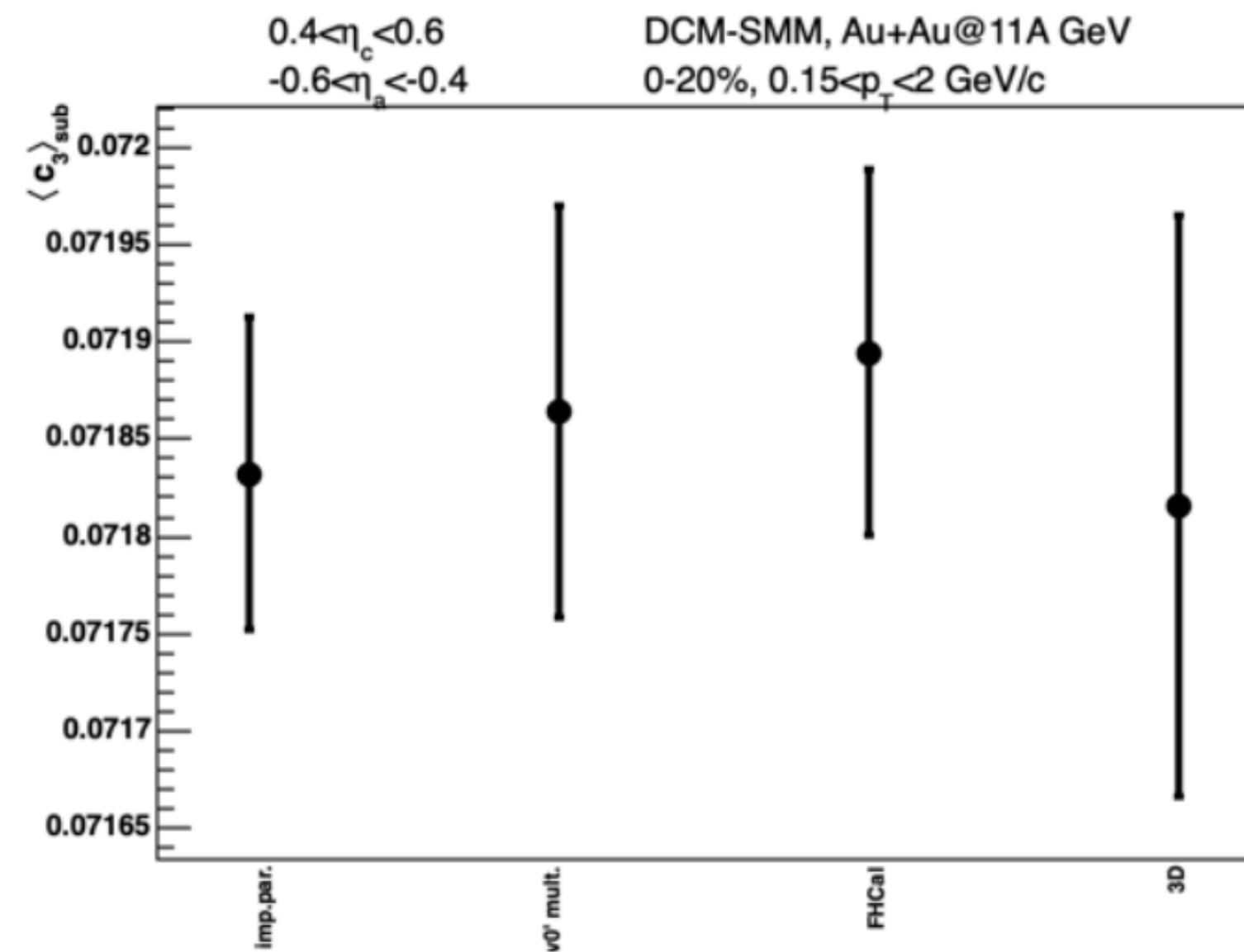
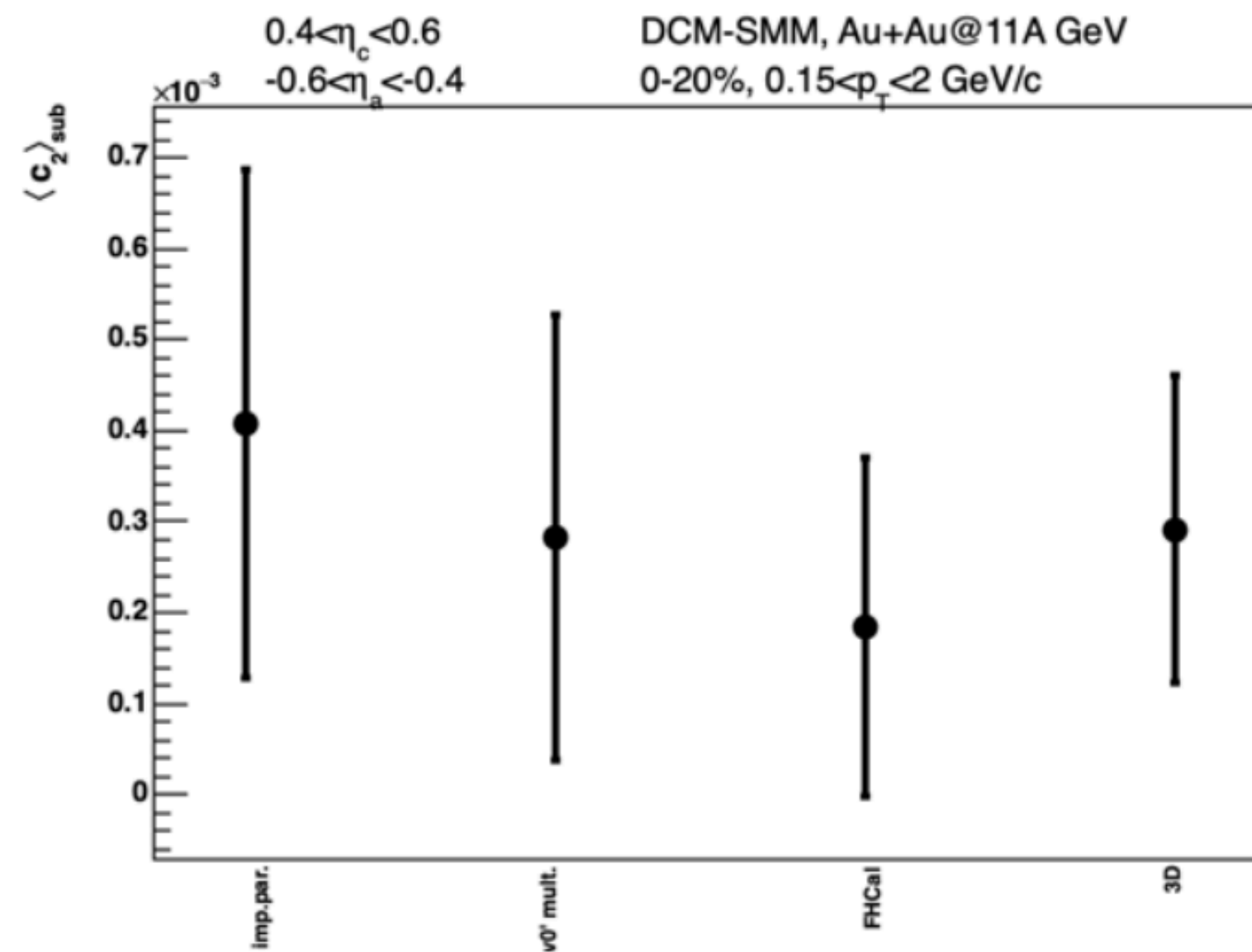
# $C_{2,sub}$ and $C_{3,sub}$

S. Bhatta, C. Zhang, J. Jia, Phys. Rev. C 105, 024904 (2022)

For 2 subevents:

You may construct the same  $p_T$  ‘correlators’ using particles from separated subevents in order to suppress short-range correlations effects (similar to introduction of pseudorapidity gap in flow studies)

We selected  $-0.6 < \eta < -0.4$  and  $0.4 < \eta < 0.6$  so that both subevents are separated from each other and from centrality estimation acceptance



## Findings:

- $C_{2,sub}$  and  $C_{3,sub}$  are larger than  $C_2$  and  $C_3$
- $C_{2,sub}$  and  $C_{3,sub}$  are well reproduced for central events (within stat. uncert.)
- For more peripheral events FHCAL method deviates significantly

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# Short summary

- Presented results indicate a different sensitivity of fluctuation measures to the centrality estimation procedure
- Strongly intensive observables tend to suppress this influence (not  $\Delta[P_T, N]$ , too sensitive)
- Pure FHCAL method has to be enhanced with additional info on multiplicity (otherwise only for central events)
- The current implementation of the 3D method will be reevaluated using multiplicity from forward subevents
- New 3d and higher order moments would be studied using official MC productions

# Thank you for your attention!

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backup

