

# Incoherent and coherent diffractive photoproduction of $J/\psi$ and $\Upsilon$ on heavy nuclei

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New Trends in High Energy Physics, Budva, Montenegro, 24-30 September 2018

- 1 Color dipole cross section and exclusive photoproduction of vector mesons
- 2 Diffractive processes on the nuclear target & multiple scattering expansion
- 3 Incoherent and coherent diffraction in ultraperipheral and peripheral heavy ion collisions

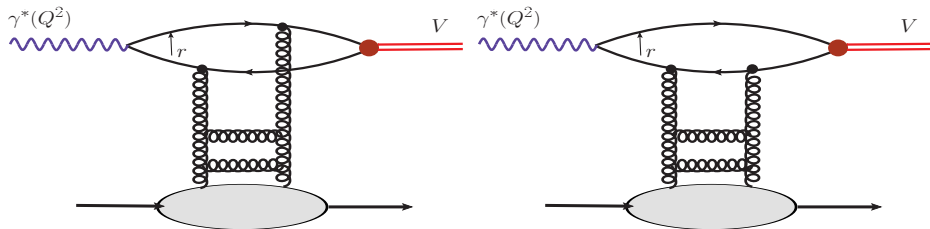


Agnieszka Łuszczak, W. S. “Incoherent diffractive photoproduction of  $J/\psi$  and  $\Upsilon$  on heavy nuclei in the color dipole approach,” Phys. Rev. C **97**, no. 2, 024903 (2018) [arXiv:1712.04502 [hep-ph]].



A. Cisek, W. S. and A. Szczurek, Phys. Rev. C **86** (2012) 014905 [arXiv:1204.5381 [hep-ph]].

## Color dipole/ $k_{\perp}$ -factorization approach



### Color dipole representation of forward amplitude:

$$A(\gamma^*(Q^2)p \rightarrow Vp; W, t = 0) = \int_0^1 dz \int d^2\mathbf{r} \psi_V(z, \mathbf{r}) \psi_{\gamma^*}(z, \mathbf{r}, Q^2) \sigma(x, \mathbf{r})$$

$$\sigma(x, \mathbf{r}) = \frac{4\pi}{3} \alpha_S \int \frac{d^2\kappa}{\kappa^4} \frac{\partial G(x, \kappa^2)}{\partial \log(\kappa^2)} \left[ 1 - e^{i\kappa\mathbf{r}} \right], \quad x = M_V^2/W^2$$

- impact parameters and helicities of high-energy  $q$  and  $\bar{q}$  are conserved during the interaction.
- scattering matrix is “diagonal” in the color dipole representation.

## When do small dipoles dominate ?

- the photon shrinks with  $Q^2$  - photon wavefunction at large  $r$ :

$$\psi_{\gamma^*}(z, r, Q^2) \propto \exp[-\varepsilon r], \quad \varepsilon = \sqrt{m_f^2 + z(1-z)Q^2}$$

- the integrand receives its main contribution from ( $M_V \sim 2m_f$ )

$$r \sim r_S \approx \frac{6}{\sqrt{Q^2 + M_V^2}}$$

Kopeliovich, Nikolaev, Zakharov '93

- a large quark mass (bottom, charm) can be a hard scale even at  $Q^2 \rightarrow 0$ .
- for small dipoles we can approximate

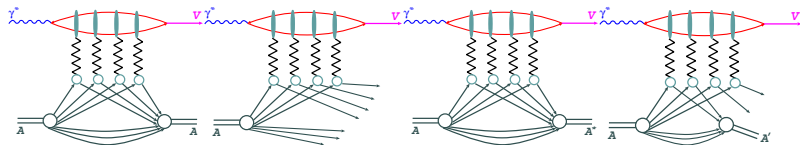
$$\sigma(x, r) = \frac{\pi^2}{3} r^2 \alpha_S(q^2) xg(x, q^2), \quad q^2 \approx \frac{10}{r^2}$$

- for  $\varepsilon \gg 1$  we then obtain the asymptotics

$$A(\gamma^* p \rightarrow Vp) \propto r_S^2 \sigma(x, r_S) \propto \frac{1}{Q^2 + M_V^2} \times \frac{1}{Q^2 + M_V^2} xg(x, Q^2 + M_V^2)$$

- probes the gluon distribution, which drives the energy dependence.
- From DGLAP fits:  $xg(x, \mu^2) = (1/x)^{\lambda(\mu^2)}$  with  $\lambda(\mu^2) \sim 0.1 \div 0.4$  for  $\mu^2 = 1 \div 10^2 \text{GeV}^2$ .

## Diffractive processes on the nuclear target



### diffractive processes on nuclear targets:

- coherent diffraction – nucleus stays in the ground state
- complete breakup of the nucleus, final state free protons & neutrons
- intact nucleus, but an excited state
- partial breakup of the nucleus, a variety of possible fragments

### they all have in common:

- large rapidity gap between vector meson and nuclear fragments
- lack of production of additional particles

## Off-forward amplitude

### Amplitude at finite transverse momentum transfer $\Delta$

$$\begin{aligned}\mathcal{A}(\gamma^* A_i \rightarrow VA_f^*; W, \Delta) &= 2i \int d^2 \mathbf{B} \exp[-i\Delta \mathbf{B}] \langle V | \langle A_f^* | \hat{\Gamma}(\mathbf{b}_+, \mathbf{b}_-) | A_i \rangle | \gamma \rangle \\ &= 2i \int d^2 \mathbf{B} \exp[-i\Delta \mathbf{B}] \int_0^1 dz \int d^2 \mathbf{r} \Psi_V^*(z, \mathbf{r}) \Psi_\gamma(z, \mathbf{r}) \langle A_f^* | \hat{\Gamma}(\mathbf{B} - (1-z)\mathbf{r}, \mathbf{B} + z\mathbf{r}) | A_i \rangle.\end{aligned}$$

$$\mathbf{B} = z\mathbf{b}_+ + (1-z)\mathbf{b}_- = \mathbf{b} - (1-2z)\frac{\mathbf{r}}{2}$$

$$\begin{aligned}\mathcal{A}(\gamma^* A_i \rightarrow VA_f^*; W, \Delta) &= 2i \int d^2 \mathbf{b} \exp[-i\mathbf{b}\Delta] \int d^2 \mathbf{r} \rho_{V\gamma}(\mathbf{r}, \Delta) \langle A_f^* | \hat{\Gamma}(\mathbf{b} + \frac{\mathbf{r}}{2}, \mathbf{b} - \frac{\mathbf{r}}{2}) | A_i \rangle, \\ \rho_{V\gamma}(\mathbf{r}, \Delta) &= \int_0^1 dz \exp[i(1-2z)\frac{\mathbf{r}\Delta}{2}] \Psi_V^*(z, \mathbf{r}) \Psi_\gamma(z, \mathbf{r}).\end{aligned}$$

## Incoherent diffraction: summing over nuclear states

$$\frac{d\sigma_{\text{incoh}}}{d\Delta^2} = \sum_{A_f \neq A} \frac{d\sigma(\gamma A_i \rightarrow VA_f^*)}{d\Delta^2}.$$

Closure in the sum over nuclear final states:

$$\sum_{A \neq A_f} |A_f\rangle \langle A_f| = 1 - |A\rangle \langle A|,$$

$$\frac{d\sigma_{\text{incoh}}}{d\Delta^2} = \frac{1}{4\pi} \int d^2r d^2r' \rho_{V\gamma}^*(r', \Delta) \rho_{V\gamma}(r, \Delta) \Sigma_{\text{incoh}}(r, r', \Delta),$$

$$\Sigma_{\text{incoh}}(r, r', \Delta) = \int d^2b d^2b' \exp[-i\Delta(\mathbf{b} - \mathbf{b}')] C\left(\mathbf{b}' + \frac{\mathbf{r}'}{2}, \mathbf{b}' - \frac{\mathbf{r}'}{2}; \mathbf{b} + \frac{\mathbf{r}}{2}, \mathbf{b} - \frac{\mathbf{r}}{2}\right)$$

Only ground state nuclear averages:

$$C(\mathbf{b}'_+, \mathbf{b}'_-; \mathbf{b}_+, \mathbf{b}_-) = \langle A | \hat{f}^\dagger(\mathbf{b}'_+, \mathbf{b}'_-) \hat{f}(\mathbf{b}_+, \mathbf{b}_-) | A \rangle - \langle A | \hat{f}(\mathbf{b}'_+, \mathbf{b}'_-) | A \rangle^* \langle A | \hat{f}(\mathbf{b}_+, \mathbf{b}_-) | A \rangle.$$

## Nuclear averages as in Glauber & Matthiae

$$\hat{f}(\mathbf{b}_+, \mathbf{b}_-) = 1 - \prod_{i=1}^A [1 - \hat{f}_{N_i}(\mathbf{b}_+ - \mathbf{c}_i, \mathbf{b}_- - \mathbf{c}_i)],$$

in the limit of the dilute uncorrelated nucleus all we need are:

$$\begin{aligned} M(\mathbf{b}_+, \mathbf{b}_-) &= \int d^2c T_A(c) \Gamma_N(\mathbf{b}_+ - \mathbf{c}, \mathbf{b}_- - \mathbf{c}) \\ \Omega(\mathbf{b}'_+, \mathbf{b}'_-; \mathbf{b}_+, \mathbf{b}_-) &= \int d^2c T_A(c) \Gamma_N^*(\mathbf{b}'_+ - \mathbf{c}, \mathbf{b}'_- - \mathbf{c}) \Gamma_N(\mathbf{b}_+ - \mathbf{c}, \mathbf{b}_- - \mathbf{c}) \end{aligned}$$

$$\begin{aligned} C(\mathbf{b}'_+, \mathbf{b}'_-; \mathbf{b}_+, \mathbf{b}_-) &= \left[ 1 - \frac{1}{A} \left( M^*(\mathbf{b}'_+, \mathbf{b}'_-) + M(\mathbf{b}_+, \mathbf{b}_-) \right) + \frac{1}{A} \Omega(\mathbf{b}'_+, \mathbf{b}'_-; \mathbf{b}_+, \mathbf{b}_-) \right]^A \\ &\quad - \left[ \left( 1 - \frac{1}{A} M^*(\mathbf{b}'_+, \mathbf{b}'_-) \right) \left( 1 - \frac{1}{A} M(\mathbf{b}_+, \mathbf{b}_-) \right) \right]^A \end{aligned}$$



## Multiple scattering expansion of the incoherent cross section

Diffraction cone of the free nucleon:  $B \ll R_A^2$

$$\sigma(x, \mathbf{r}, \mathbf{\Delta}) = \sigma(x, r) \exp\left[-\frac{1}{2} B \mathbf{\Delta}^2\right]$$

Multiple scattering expansion for  $\Delta^2 R_A^2 \gg 1$

$$\frac{d\sigma_{\text{incoh}}}{d\mathbf{\Delta}^2} = \sum_n \frac{d\sigma^{(n)}}{d\mathbf{\Delta}^2} = \frac{1}{16\pi} \sum_n w_n(\mathbf{\Delta}) \int d^2\mathbf{b} T_A^n(\mathbf{b}) |I_n(x, \mathbf{b})|^2,$$

$$w_n(\mathbf{\Delta}) = \frac{1}{n \cdot n!} \cdot \left(\frac{1}{16\pi B}\right)^{n-1} \cdot \exp\left(-\frac{B}{n} \mathbf{\Delta}^2\right),$$

and

$$\begin{aligned} I_n(x, \mathbf{b}) &= \langle V | \sigma^n(x, r) \exp\left[-\frac{1}{2} \sigma(x, r) T_A(\mathbf{b})\right] | \gamma \rangle \\ &= \int_0^1 dz \int d^2\mathbf{r} \Psi_V^*(z, \mathbf{r}) \Psi_\gamma(z, \mathbf{r}) \underbrace{\sigma^n(x, r) \exp\left[-\frac{1}{2} \sigma(x, r) T_A(\mathbf{b})\right]}_{\text{nuclear absorption}}. \end{aligned}$$

## Dipole cross section from Xfitter

### BGK-form of the dipole cross section

$$\sigma(x, r) = \sigma_0 \left( 1 - \exp \left[ - \frac{\pi^2 r^2 \alpha_s(\mu^2) x g(x, \mu^2)}{3\sigma_0} \right] \right), \mu^2 = C/r^2 + \mu_0^2$$

- the *soft* ansatz, as used in the original BGK model

$$xg(x, \mu_0^2) = A_g x^{-\lambda_g} (1-x)^{C_g},$$

- the *soft + hard* ansatz

$$xg(x, \mu_0^2) = A_g x^{-\lambda_g} (1-x)^{C_g} (1 + D_g x + E_g x^2),$$

- fit I: BGK fit with fitted valence quarks for  $\sigma_r$  for H1ZEUS-NC data in the range  $Q^2 \geq 3.5 \text{ GeV}^2$  and  $x \leq 0.01$ . NLO fit. *Soft gluon*.
- fit II: BGK fit with valence quarks for  $\sigma_r$  for H1ZEUS-NC data in the range  $Q^2 \geq 0.35 \text{ GeV}^2$  and  $x \leq 0.01$ . NLO fit. *Soft + hard gluon*.
- fits from A. Łuszczak and H. Kowalski, Phys. Rev. D **95** (2017).

## Further input to our calculation

### Overlap of light-cone wave functions

$$\Psi_V^*(z, r)\Psi_\Upsilon(z, r) = \frac{e_Q\sqrt{4\pi\alpha_{em}}N_c}{4\pi^2z(1-z)} \left\{ m_Q^2 K_0(m_Q r)\psi(z, r) - [z^2 + (1-z)^2]m_Q K_1(m_Q r)\frac{\partial\psi(z, r)}{\partial r} \right\}.$$

- “boosted Gaussian” wave functions as in Nemchik et al. ('94)

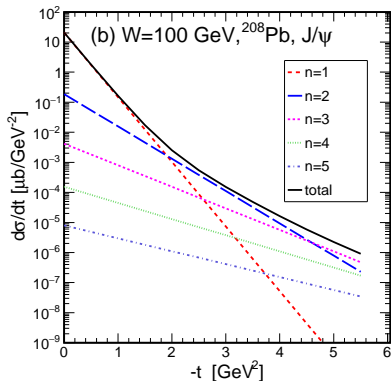
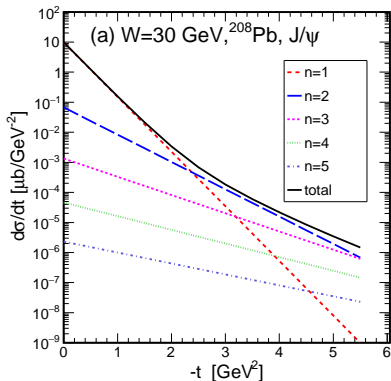
$$\psi(z, r) \propto z(1-z) \exp\left[-\frac{M_Q^2 R^2}{8z(1-z)} - \frac{2z(1-z)r^2}{R^2}\right]$$

- parameters  $m_Q, R$  & normalization as in Kowalski et al. (2006) for  $J/\psi$  and Cox et al. (2008) for  $\Upsilon$ .

### diffractive slope on a free nucleon:

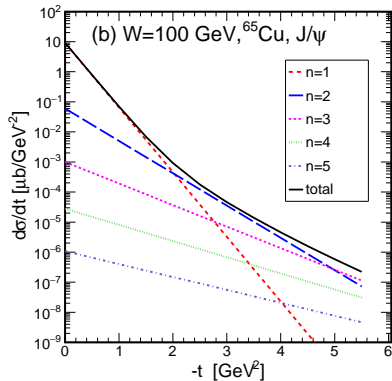
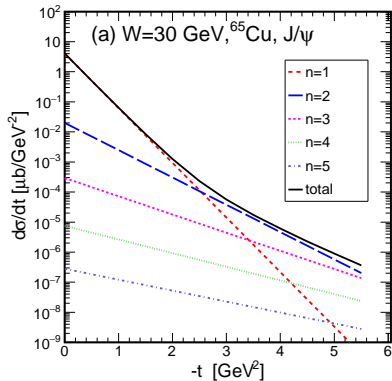
$B = B_0 + 4\alpha' \log(W/W_0)$  with  $W_0 = 90 \text{ GeV}$ , and  $\alpha' = 0.164 \text{ GeV}^{-2}$ .  
We take  $B_0 = 4.88 \text{ GeV}^{-2}$  for  $J/\psi$  and  $B_0 = 3.68 \text{ GeV}^{-2}$  for  $\Upsilon$ .

# Diffractive incoherent photoproduction on the nuclear target

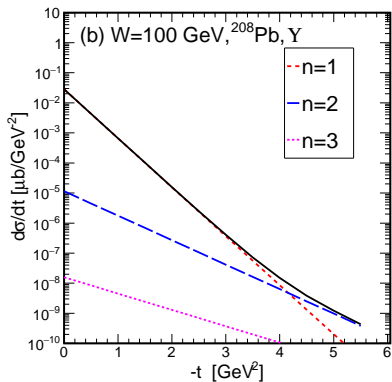
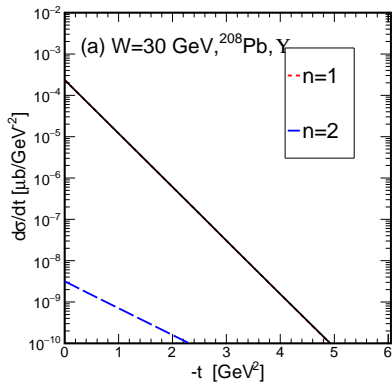


$-t = \Delta^2$ , single scattering has the same diffractive slope as on the free nucleon, multiple scatterings have smaller slopes.

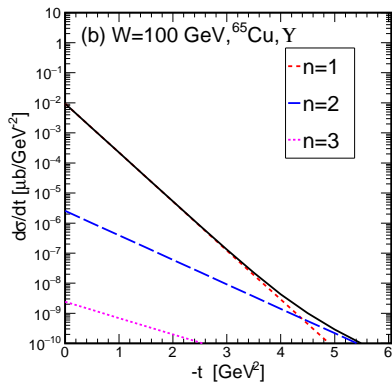
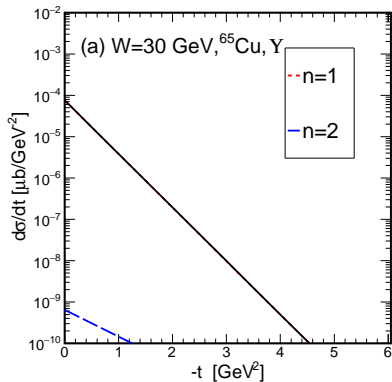
# Diffractive incoherent photoproduction on the nuclear target



# Diffractive incoherent photoproduction on the nuclear target



# Diffractive incoherent photoproduction on the nuclear target



## Incoherent diffraction at low $\Delta^2$

at low  $\Delta^2$  the single scattering dominates, and one should rather use its exact form:

$$\frac{d\sigma_{\text{incoh}}}{d\Delta^2} = \frac{1}{16\pi} \left\{ w_1(\Delta) \int d^2\mathbf{b} T_A(\mathbf{b}) |I_1(x, \mathbf{b})|^2 - \underbrace{\frac{1}{A} \left| \int d^2\mathbf{b} \exp[-i\Delta\mathbf{b}] T_A(\mathbf{b}) I_1(x, \mathbf{b}) \right|^2}_{\text{vanishes for } \Delta^2 R_A^2 \gg 1} \right\}.$$

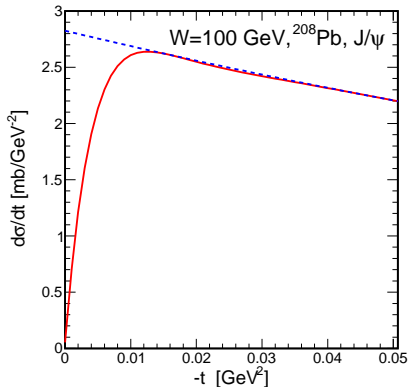
$$I_1(x, \mathbf{b}) = \langle V | \underbrace{\sigma(x, r) \exp\left[-\frac{1}{2}\sigma(x, r) T_A(\mathbf{b})\right]}_{\text{nuclear absorption}} | \gamma \rangle$$

If we were to neglect intranuclear absorption, we would obtain for small  $\Delta^2$ :

$$\frac{d\sigma_{\text{incoh}}}{d\Delta^2} = A \cdot \frac{d\sigma(\gamma N \rightarrow VN)}{d\Delta^2} \Big|_{\Delta^2=0} \cdot \left\{ 1 - \mathcal{F}_A(\Delta^2) \right\}.$$

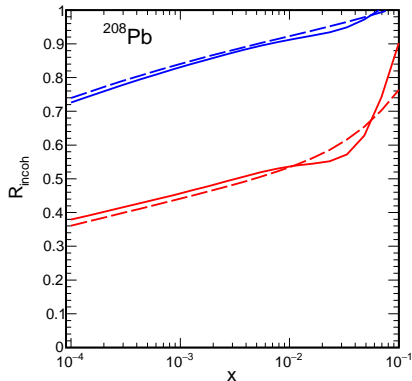


## Diffractive processes on the nuclear target



- solid line: exact single scattering
- dashed: large  $|t|$ -limit of single scattering
- exact result merges into the large  $|t|$  limit quickly, the latter is a good approximation in a broad range of  $t$ .
- cross section dips, but does not vanish at  $t \rightarrow 0$ .
- note: in the small to intermediate  $t$  region nuclear correlations may play a role.

## Diffractive processes on the nuclear target



- blue:  $\Upsilon$ , red:  $J/\psi$
- dashed line: dipole fit I (soft gluon),
- solid line: dipole fit II (soft+hard gluon)
- dependence on dipole cross section in its “applicability region” is rather small.
- nuclear absorption cannot be neglected, even for heavy vector mesons.

$$R_{\text{incoh}}(x) = \frac{d\sigma_{\text{incoh}}/d\Delta^2}{A \cdot d\sigma(\gamma N \rightarrow VN)/d\Delta^2} = \frac{\int d^2\mathbf{b} T_A(\mathbf{b}) \left| \langle V | \sigma(x, r) \exp\left[-\frac{1}{2}\sigma(x, r) T_A(\mathbf{b})\right] | \gamma \rangle \right|^2}{A \cdot \left| \langle V | \sigma(x, r) | \gamma \rangle \right|^2}.$$

## Corrections for real part and skewedness

### numerically important corrections:

- real part of the diffractive amplitude:

$$\sigma(x, r) \rightarrow (1 - i\rho(x))\sigma(x, r), \quad \rho(x) = \tan\left(\frac{\pi\Delta_{\mathbf{P}}}{2}\right), \quad \Delta_{\mathbf{P}} = \frac{\partial \log\left(\langle V|\sigma(x, r)|\gamma\rangle\right)}{\partial \log(1/x)}$$

- amplitude is non-forward also in the longitudinal momenta. Correction factor (Shuvaev et al. (1999)):

$$R_{\text{skewed}} = \frac{2^{2\Delta_{\mathbf{P}}+3}}{\sqrt{\pi}} \cdot \frac{\Gamma(\Delta_{\mathbf{P}} + 5/2)}{\Gamma(\Delta_{\mathbf{P}} + 4)}.$$

- apply K-factor to the cross section:

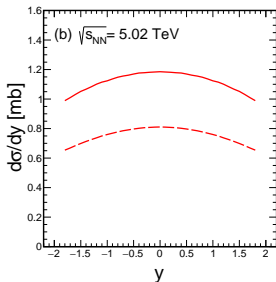
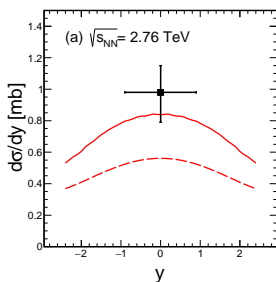
$$K = (1 + \rho^2(x)) \cdot R_{\text{skewed}}^2.$$

Note: absorption factor is really:

$$\int d^2\mathbf{b} T_A^n(\mathbf{b}) \exp\left[-\frac{1}{2}\left(\sigma^*(x, \mathbf{r}') + \sigma(x, \mathbf{r})\right) T_A(\mathbf{b})\right]$$

so that we neglect a real part in the absorption exponentials

# Incoherent diffraction in ultraperipheral heavy ion collisions



solid line: with  $K$ -factor  
dashed line: without  $K$ -factor  
data point from ALICE  
Eur. Phys. J. C **73** (2013)

Cross section for AA collision uses Weizsäcker-Williams photon fluxes:

$$\frac{d\sigma_{\text{incoh}}(AA \rightarrow VAX)}{dy} = n_{\gamma/A}(z_+) \sigma_{\text{incoh}}(W_+) + n_{\gamma/A}(z_-) \sigma_{\text{incoh}}(W_-),$$

$$z_{\pm} = \frac{m_V}{\sqrt{s_{NN}}} e^{\pm y}, \quad W_{\pm} = \sqrt{z_{\pm} s_{NN}}.$$

## From ultraperipheral to peripheral nuclear collisions

Recently, the ALICE collaboration has observed a large enhancement of  $J/\psi$  mesons carrying very small  $p_T < 300$  MeV in the centrality classes corresponding to peripheral collisions.

Centrality class 70 ÷ 90%:

13 fm  $< b < 15$  fm, photon fluxes by Contreras Phys. Rev. C **96** (2017)

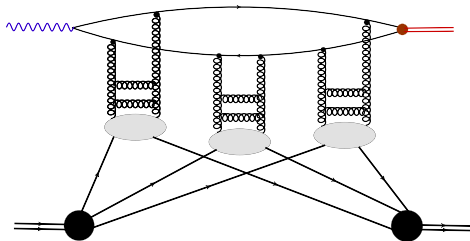
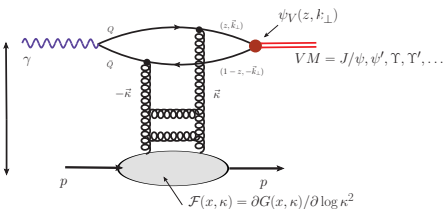
$$\begin{aligned} \frac{d\sigma_{\text{incoh}}(AA \rightarrow VX|70 \div 90\%)}{dy} &= n_{\gamma/A}(z_+|70 \div 90\%)\sigma_{\text{incoh}}(W_+|p_T < p_T^{\text{cut}}) \\ &+ n_{\gamma/A}(z_-|70 \div 90\%)\sigma_{\text{incoh}}(W_-|p_T < p_T^{\text{cut}}) \\ &\approx 15 \mu\text{b}, \end{aligned}$$

The ALICE measurement is [Phys. Rev. Lett. **116** (2016)]:

$$\frac{d\sigma(AA \rightarrow VX|70 \div 90\%; 2.5 < |y| < 4.0)}{dy} = 59 \pm 11 \pm 8 \mu\text{b}.$$

For an estimate of the coherent contribution, see: M. Kłusek-Gawenda and A. Szczurek, Phys. Rev. C **93** (2016)

## VM photoproduction from nucleon to nucleus:

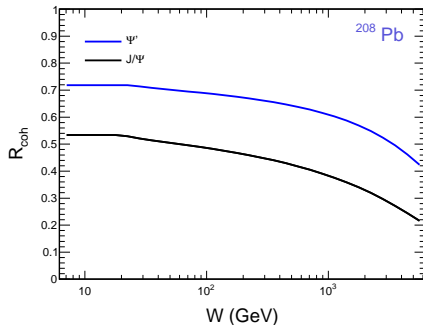
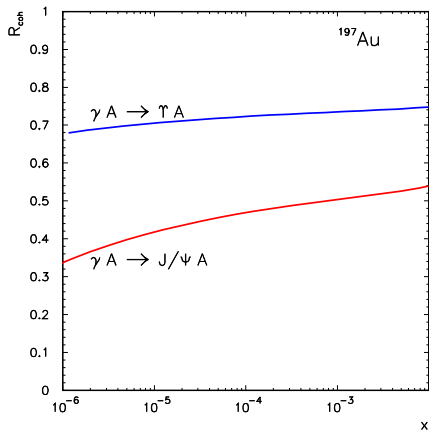


- for heavy nuclei rescattering/absorption effects are enhanced by the large nuclear size
- $q\bar{q}$  rescattering is easily dealt with in impact parameter space
- the final state might as well be a (virtual) photon (total photoabsorption cross section) or a  $q\bar{q}$ -pair (inclusive low-mass diffraction).
- Color-dipole amplitude

$$\Gamma(\mathbf{b}, x, r) = 1 - \frac{\langle A | \text{Tr}[S_q(\mathbf{b})S_q^\dagger(\mathbf{b} + \mathbf{r})] | A \rangle}{\langle A | \text{Tr}[\mathbf{1}] | A \rangle} = 1 - \exp\left[-\frac{1}{2}\sigma(x, r)T_A(\mathbf{b})\right]$$

- inclusion of higher Fock states is possible (shadowing due to large mass diffractive states), and relates to gluon shadowing.

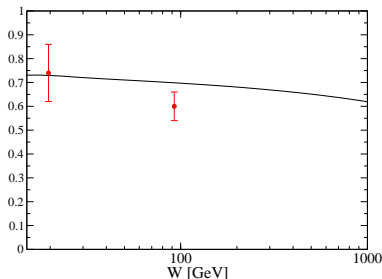
# Coherent diffractive production of $J/\psi, \psi(2S), \Upsilon$ on $^{208}\text{Pb}$



- left panel A. Cisek, WS, A. Szczurek Phys. Rev C86 (2012) 014905.
- Ratio of coherent production cross section to impulse approximation

$$R_{\text{coh}}(W) = \frac{\sigma(\gamma A \rightarrow VA; W)}{\sigma_{IA}(\gamma A \rightarrow VA; W)}, \quad \sigma_{IA} = 4\pi \int d^2b T_A^2(b) \frac{d\sigma(\gamma N \rightarrow VN)}{dt} \Big|_{t=0}$$

## The putative gluon shadowing: $\sqrt{R_{\text{coh}}}$



- an extraction of  $\sqrt{R_{\text{coh}}}$  from ALICE  $PbPb \rightarrow J/\psi PbPb$  data by Guzey et al. (2013).
- in the collinear approach: “gluon shadowing”:  $R_{\text{coh}} \sim [g_A(x, \bar{Q}^2)/(A \cdot g_N(x, \bar{Q}^2))]^2$ .
- the putative “gluon shadowing”:  $R_G = \sqrt{R_{\text{coh}}(x \sim 10^{-3})} \sim 0.7$ .
- for illustration:  $R_G(x, m_c^2) \equiv g_A(x, m_c^2)/(A \cdot g_N(x, m_c^2))$  from popular DGLAP fits:
- EPS09:  $R_G(10^{-3}, m_c^2) \sim 0.6$ , EPS08:  $R_G(10^{-3}, m_c^2) \sim 0.3$
- **Inclusive dijet observables depend on unintegrated nuclear glue nonlinearly.**



# Conclusions

- Coherent diffraction on the nucleus is a sensitive probe of the (unintegrated) gluon distribution of the target nucleus. **Rescattering/saturation effects entail that the unintegrated glue enters inclusive dijet observables nonlinearly.**
- “gluon shadowing” is included via the rescattering of higher  $Q\bar{Q}g$  Fock states. The effective “gluon shadowing” ratio  $R_G(x, m_c^2) \sim 0.74 \div 0.62$ . For  $x \sim 10^{-2} \div 10^{-5}$ . ALICE data appear to indicate somewhat stronger effect  $R_G(10^{-3}, m_c^2) \div 0.6$ .
- we have presented the Glauber-Gribov theory for incoherent photoproduction of vector mesons on heavy nuclei within the color dipole approach.
- We have developed the multiple scattering expansion which involves matrix elements of the operator  $\sigma^n(x, r) \exp[-\frac{1}{2}\sigma(x, r)T_A(\mathbf{b})]$ . We performed calculations for  $J/\psi$  and  $\Upsilon$  photoproduction. Multiple scatterings lead to extended tails in the  $t$ -distributions.
- multiple scattering terms are only important at large  $t$ , beyond the free-nucleon diffraction cone.
- We use the dipole cross section obtained in the Xfitter framework. Our calculations are in agreement with data from ALICE in ultraperipheral lead-lead collisions at  $\sqrt{s_{NN}} = 2.76$  TeV.
- Incoherent diffractive production also contributes to the  $J/\psi$  yield in peripheral inelastic heavy-ion collisions. Rough estimates using photon fluxes of Contreras give about  $\sim 25\%$  of the cross section measured by ALICE.
- In the future: extension to light vector mesons, as well as to finite  $Q^2$  (electron-ion collider).