

# Status of the muon reconstruction

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# Outline

- Available track reconstruction methods
- Results on data-MC comparison for runs 110-150, 2016
- Track quality cuts and background rejection
- New, "loose", method of the hit selection
- New reconstruction performance
- Muon reconstruction status and plans

# Muon track reconstruction

**Track parametrisation:**  $R(\vec{t}) = \vec{R}_0 + c(t - t_0)\vec{V}$

$\vec{V}$  is unit vector in polar coordinates,  $\vec{R}_0$  and  $t_0$  are taken in plane Z=0

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**Initial approximation:**

$$V_{init}^{\vec{}} = (1/|\sum_{t_i < t_j} \vec{R}_{ij}|) \sum_{t_i < t_j} \vec{R}_{ij} \quad \text{where } i \text{ and } j \text{ are ordered in time and belong to different strings}$$

Initial values for  $\vec{R}_0$  and  $t_0$  are obtained using hit with largest amplitude

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**Minimisation function:**

$$Q = \sum_{i=1}^{N_{hit}} \left[ \frac{(t_i^{est} - t_i)^2}{\sigma_t^2} + \frac{A(a_i)D(d_i)}{d_0} \right] \quad \text{inspired by ANTARES paper: } \underline{\a href="https://arxiv.org/abs/1105.4116">https://arxiv.org/abs/1105.4116$$

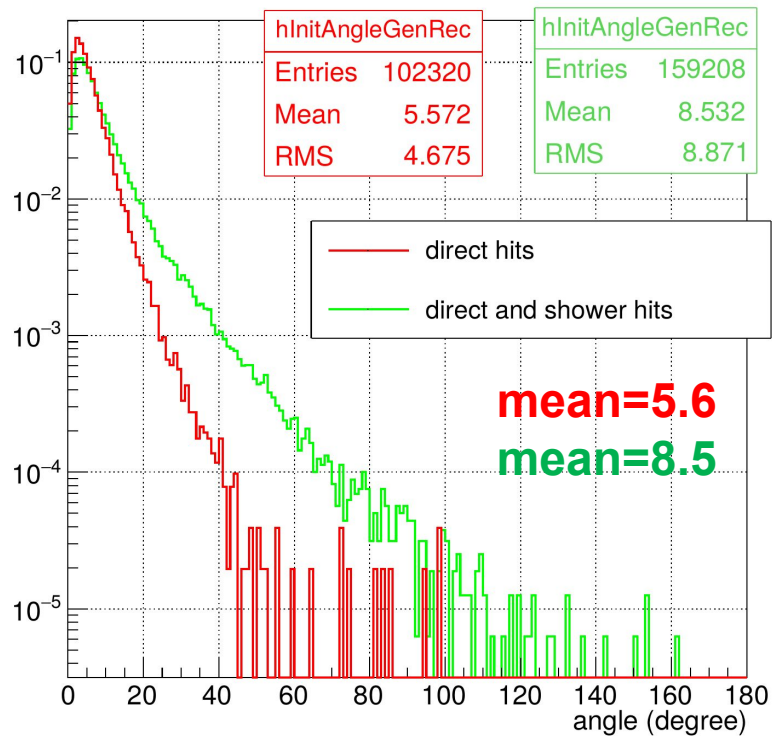
Direct cerenkov approximation for the time estimation  
A and D are amplitude and distance functions

# Performance with MC truth

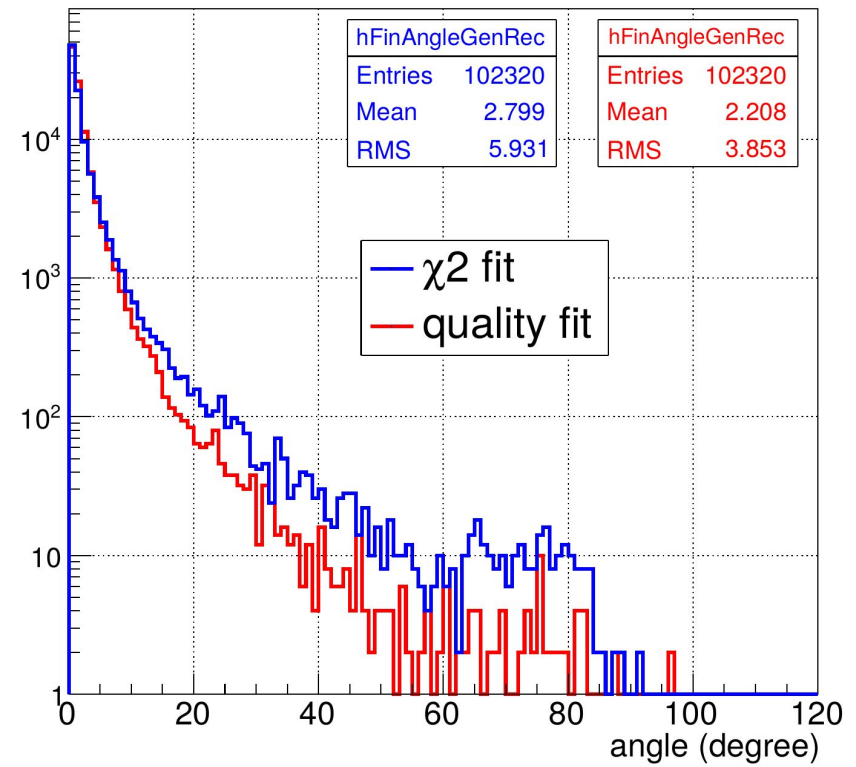
Events with at least 6 hits on 3 strings are selected (here and further in this talk)

## MC truth -based selection of direct cerenkov hits and shower hits

mismatch angle for initial approximation



fit results for direct hits



**median angle for quality fit: 1.3**

# Hotspot hit selection I

Pairs of adjacent hits (hotspots) are selected if:

- Two hits in adjacent modules fall into causality window:  $|\Delta T| < (n\Delta R/c) + t_s$ ,  $\Delta R = 15$  m,  $t_s$  - "safety time window" = 30 ns
- Hits 1 and 2 should have total charge deposit  $> A_1$  and  $> A_2$

It is important to adjust parameters  $t_s$ ,  $A_1$  and  $A_2$  to have low noise contribution

- Main parameters for noise suppression are  $A_1$  and  $A_2$
- $A_{1,2} > 1.5$  p.e. provide purity better than 98%

# Hotspot hit selection II

Hotspots are merged as follows:

1. All possible pairs are constructed at each string (same impulse may belong to 2 hotspots)
2. Combinations of hotspots (groups) of not less than 6 OM's in total are considered
3. Initial trajectory approximation is reconstructed for each group
4. Quality function is calculated for initial trajectory approximation
5. Group which gives the smallest [quality function/nHits] ratio is selected for further analysis

# Hotspot hit selection III

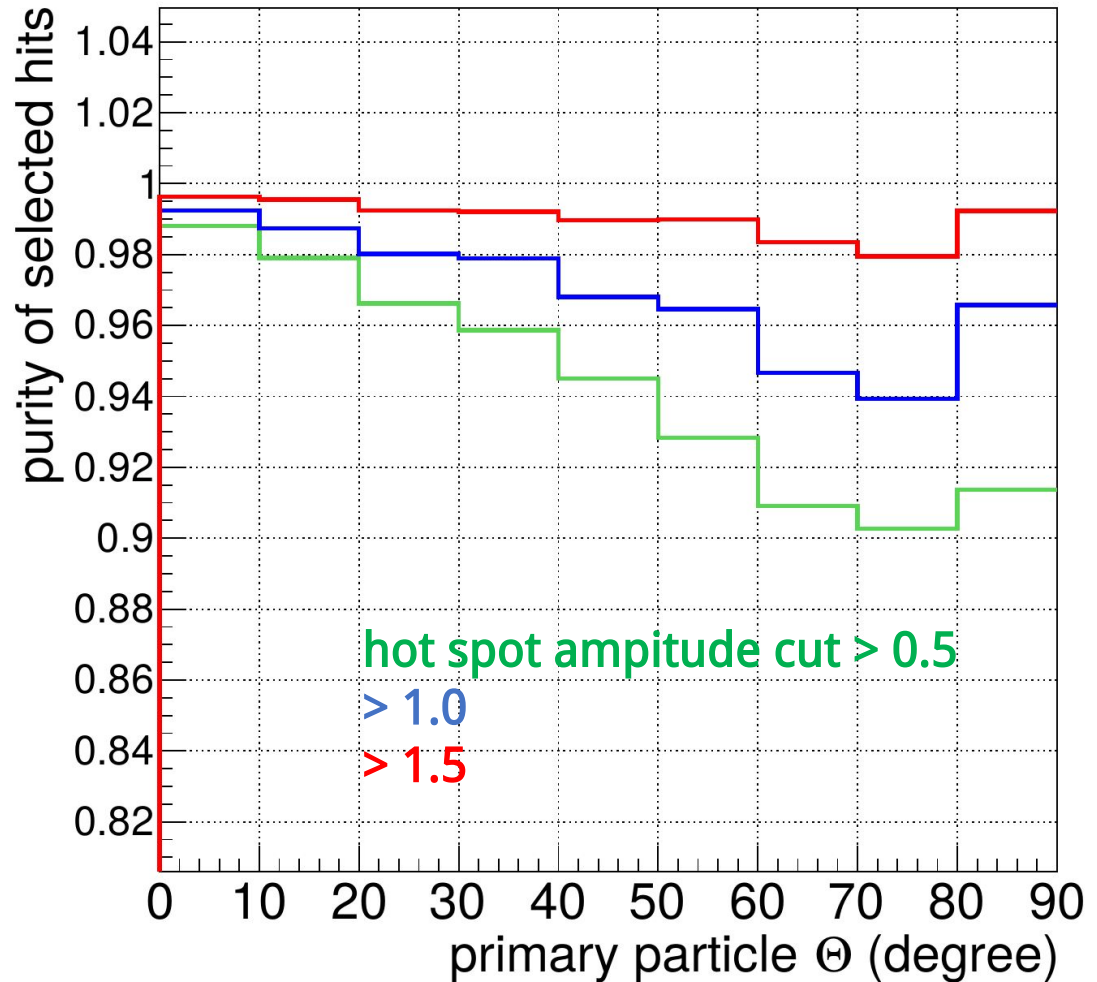
Purity of merged groups:

- Fraction of signal hits (direct or shower) in obtained global groups

Few symmetric amplitude cuts:

$$A_{1,2} > 0.5, 1.0, 1.5 \text{ (p.e.)}$$

With  $A_{1,2} > 1.5$  purity of  $> 98\%$  is achieved



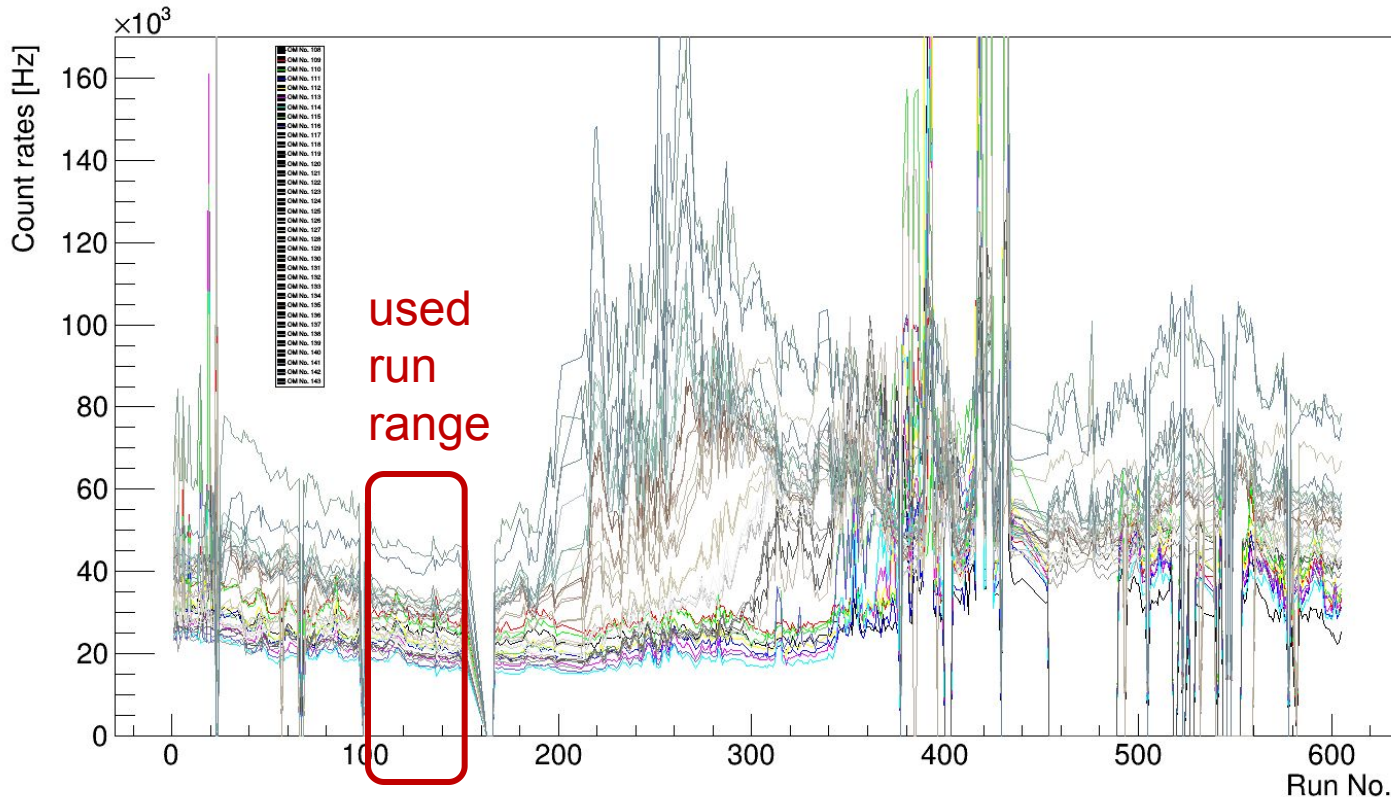
# **Atmospheric muon reconstruction in data and MC**



# Analysed datasets

## DATA: year 2016, run period 110-150

- 27 runs from this period were processed
- ~272h (11 days) exposition time
- relevant time, amplitude and OM position calibrations are applied



## Monte Carlo:

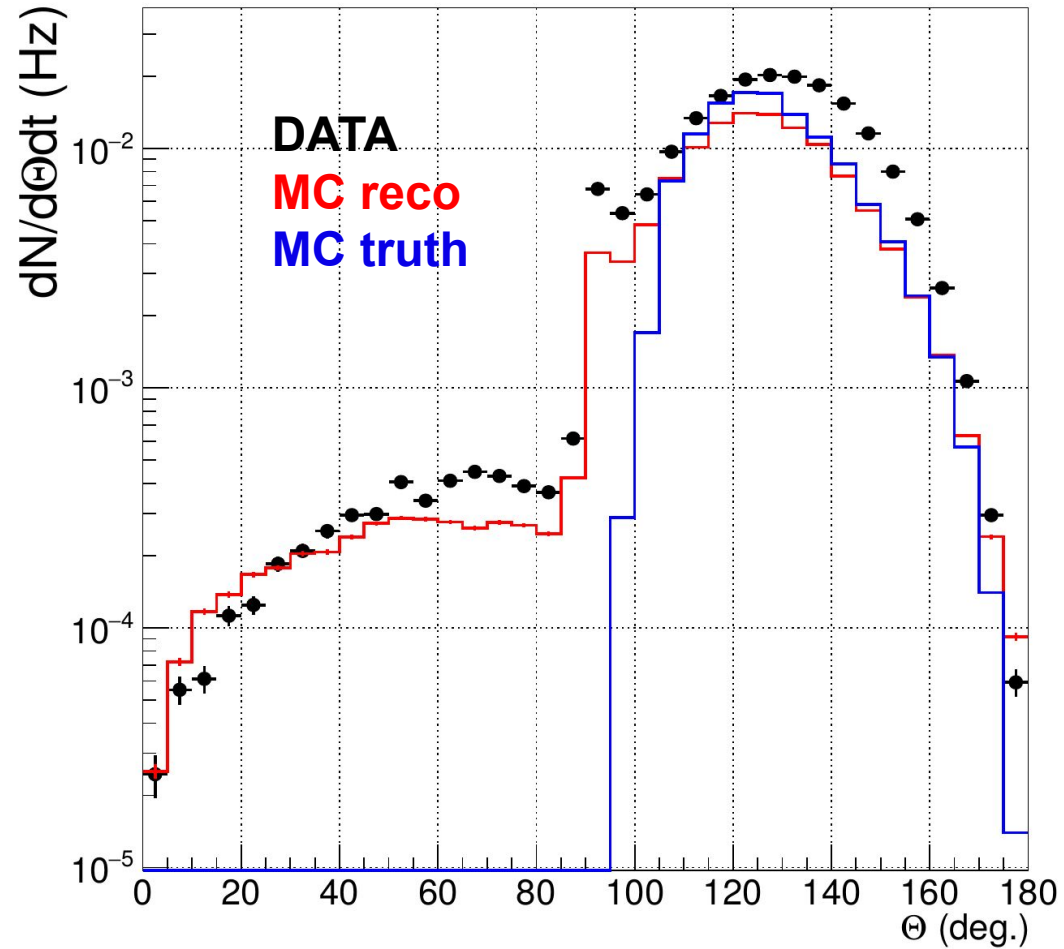
### upgoing atmospheric neutrino MC

- neutrino energy  $> 500$  GeV
- exposition time  $1.26e10$  sec
- ideal geometry and calibration,
- realistic OM noise

### downgoing atmospheric muon MC

- Muon flux from CORSIKA
- $8.3e6$  sec ( $\sim 90$  days) exposition time
- ideal geometry and calibration,
- realistic OM noise

# Rate of reconstructed tracks



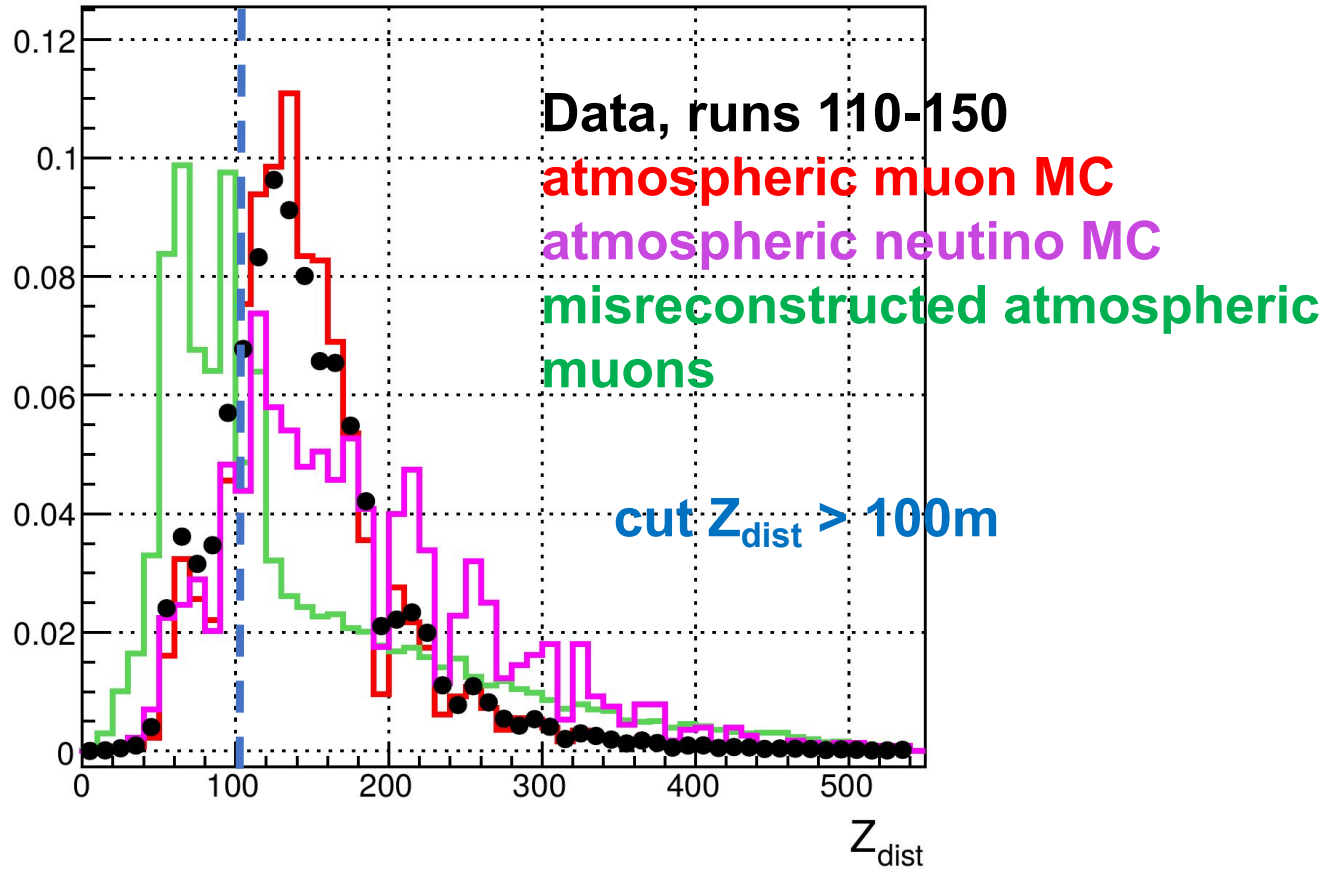
Absolute rates for data and MC:  
~ 11 days of exposition in data  
~ 90 days of exposition in MC

Total data rate is 1.5 times larger  
than MC (to be understood)

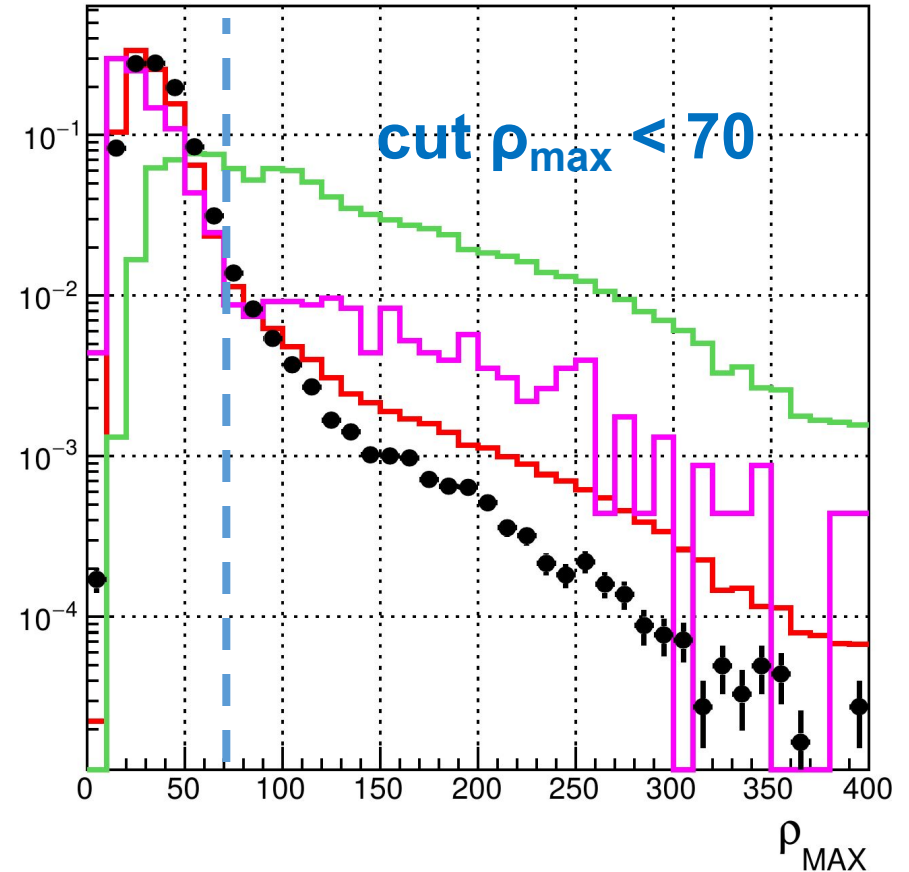
**Fraction of misreconstructed as upgoing  
tracks is ~ 3.3% both for data and MC**

# Track quality variables I

$Z_{\text{dist}}$  - largest distance between projections of used OM's on the track



$\rho_{\text{max}}$  - maximum distance from the track to the used OM

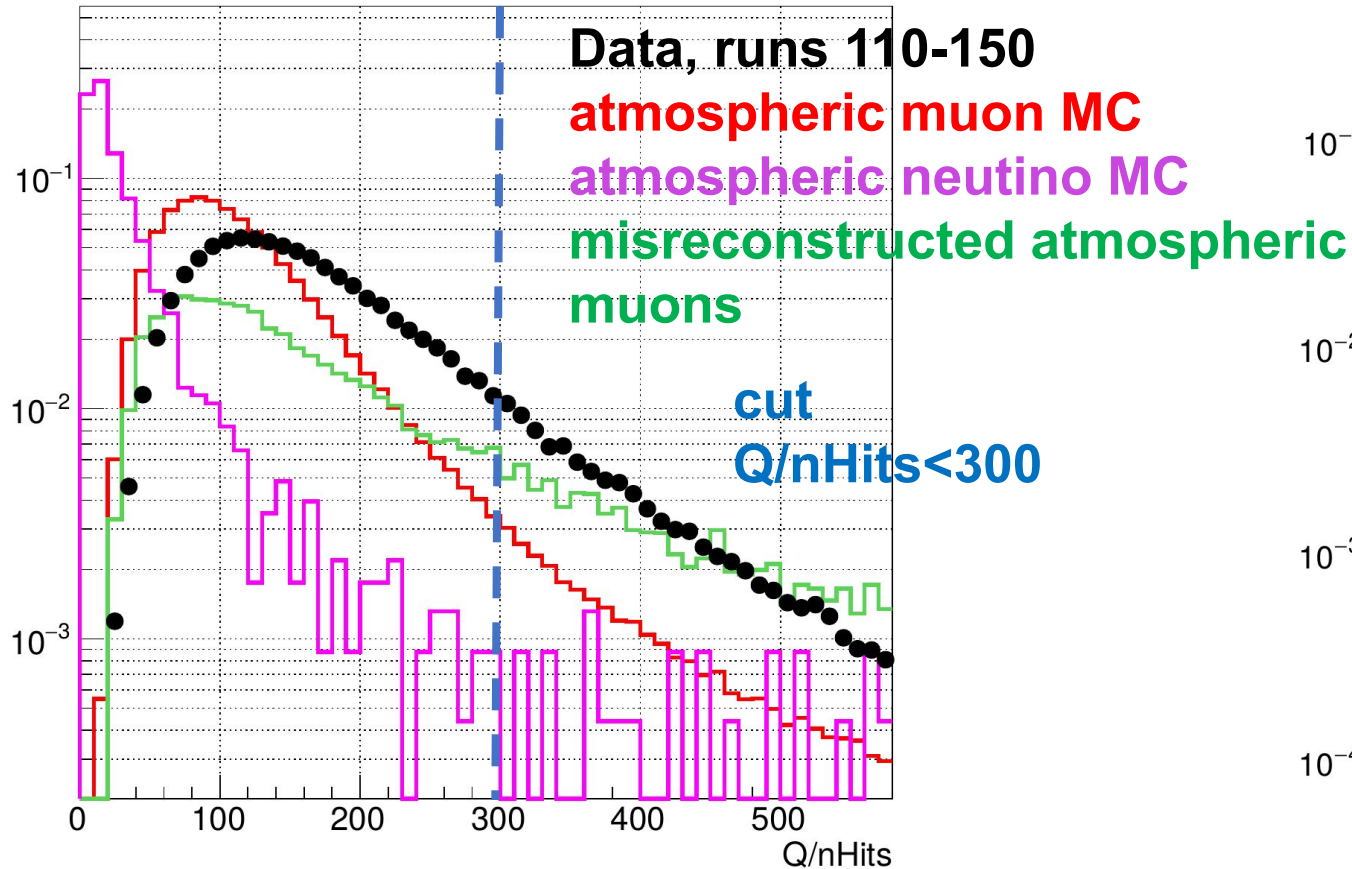


good data-MC agreement

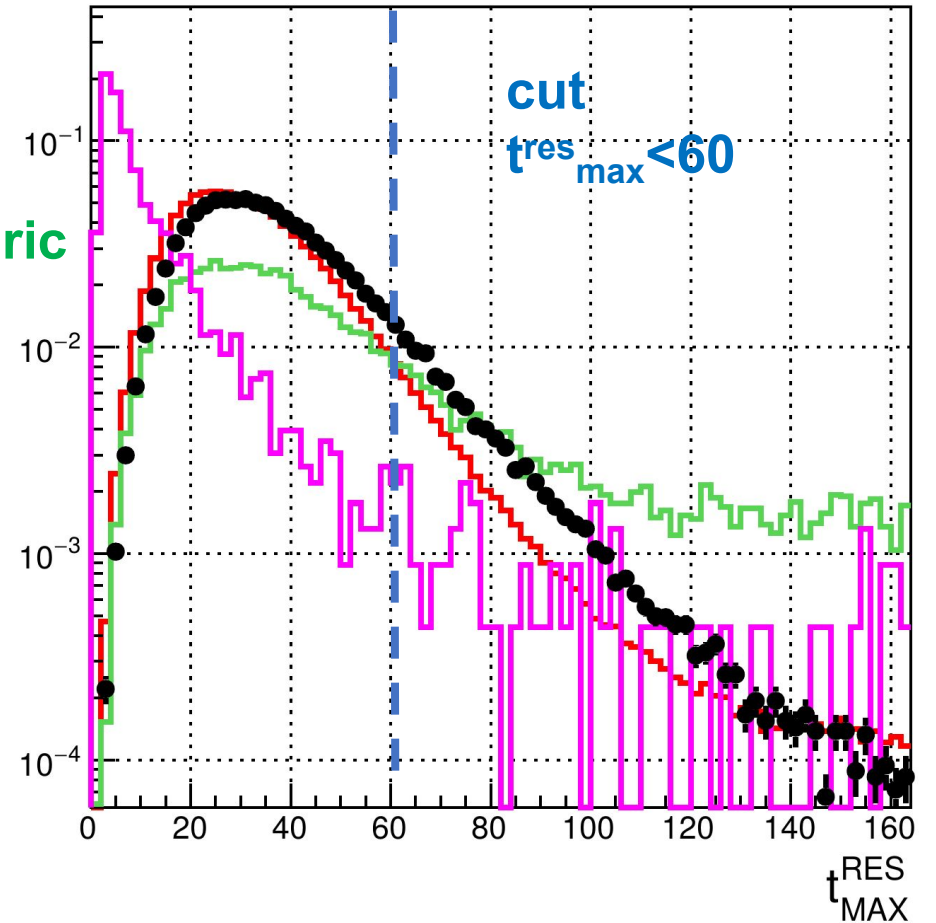
# Track quality variables II

**Q/nHits** - quality function divided by the number of used hits

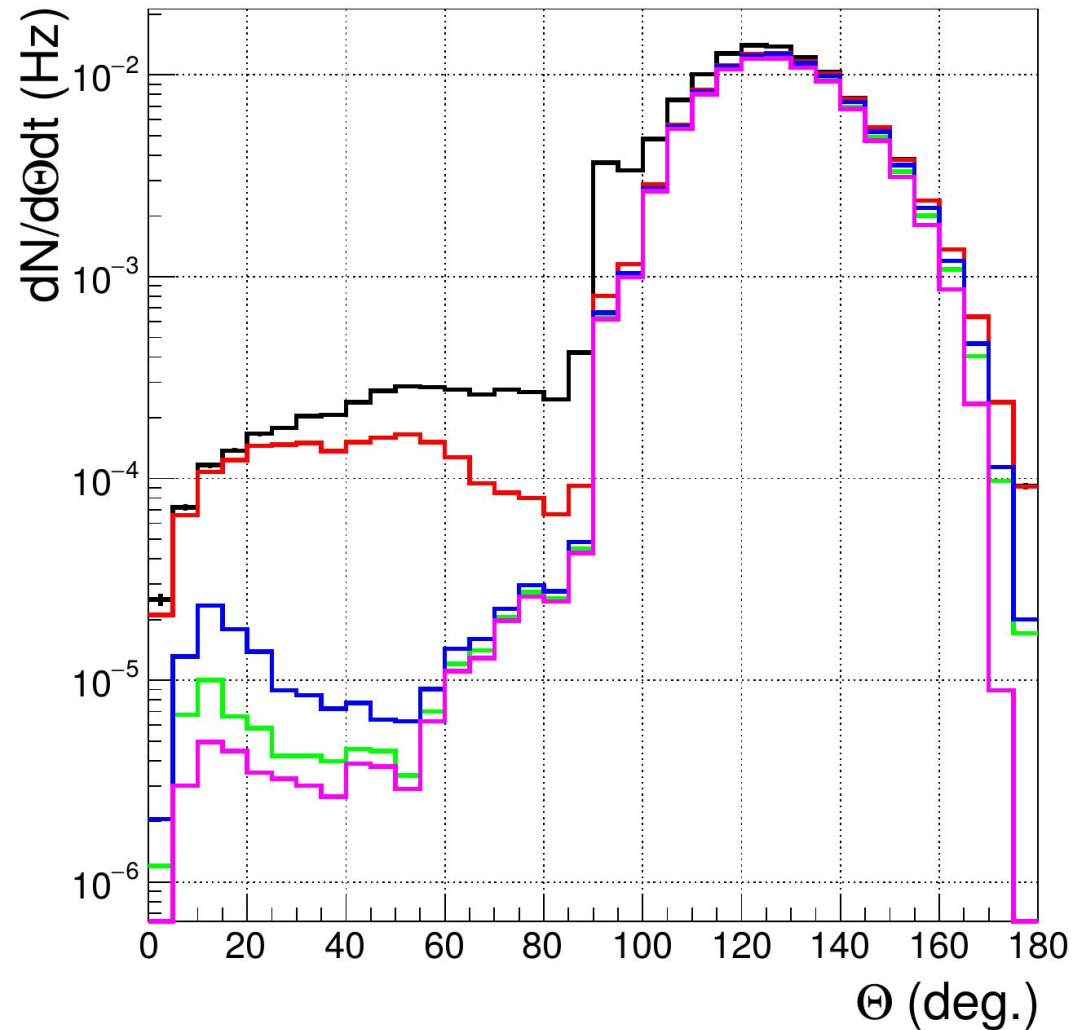
$t_{\max}^{\text{res}}$  - maximum residual time among used hits



poor data-MC agreement for quality



# Track quality variables III



Effect of cuts on polar angle distribution

**all tracks**

**$Z_{\text{dist}} > 100\text{m}$**

**$\rho_{\text{max}} < 70 \ \&\& \ Z_{\text{dist}} > 100\text{m}$**

**$t_{\text{max}}^{\text{res}} < 60 \ \&\& \ \rho_{\text{max}} < 70 \ \&\& \ Z_{\text{dist}} > 100\text{m}$**

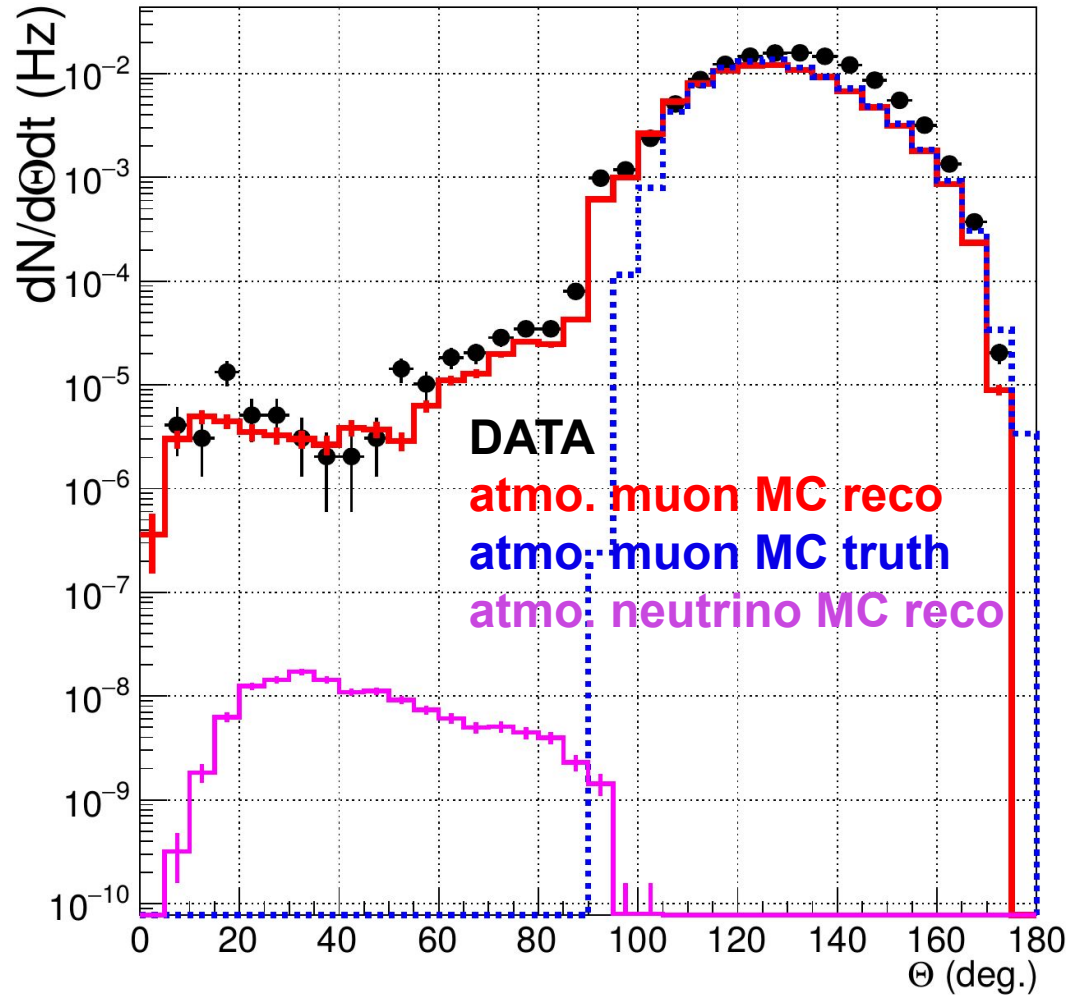
**$Q/n\text{Hits} < 300 \ \&\& \ t_{\text{max}}^{\text{res}} < 60 \ \&\& \ \rho_{\text{max}} < 70 \ \&\&$**

**$Z_{\text{dist}} > 100\text{m}$**

**Fraction of misreconstructed as upgoing tracks  
is reduced to  $\sim 0.2\%$  (MC)**

**76% of downgoing tracks have survived**

# Rate after quality cuts



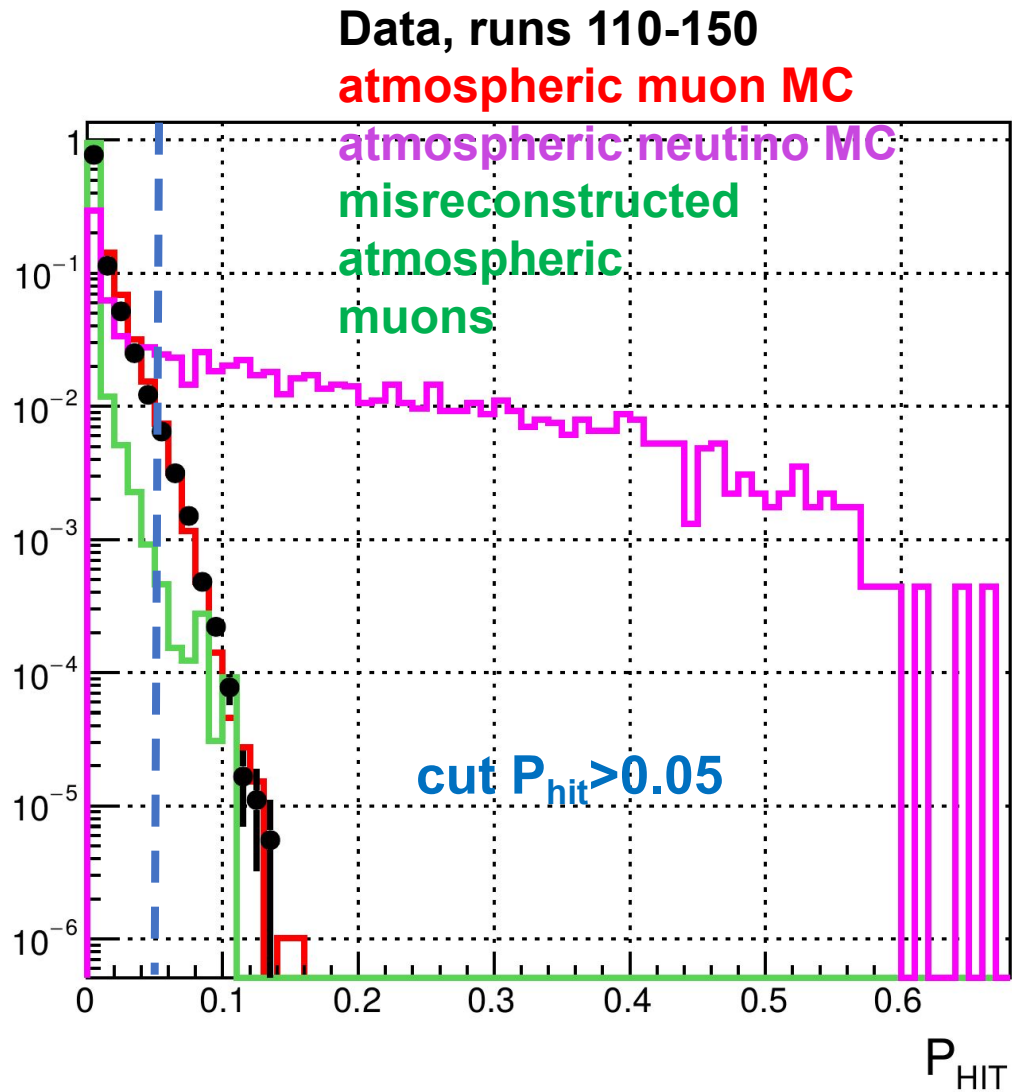
Absolute muon rates in comparison to atmospheric neutrino rate

Total rate of muon tracks  $\sim 0.15$  Hz

Background from misreconstructed groups is still  $>100$  times larger than neutrino signal

Neutrino signal efficiency  $\sim 85\%$

# $P_{hit}$ variable



$P_{hit}$  - probability that muon with current trajectory has fired the collection of OMs used in the fit

In the assumption of direct cerenkov signal

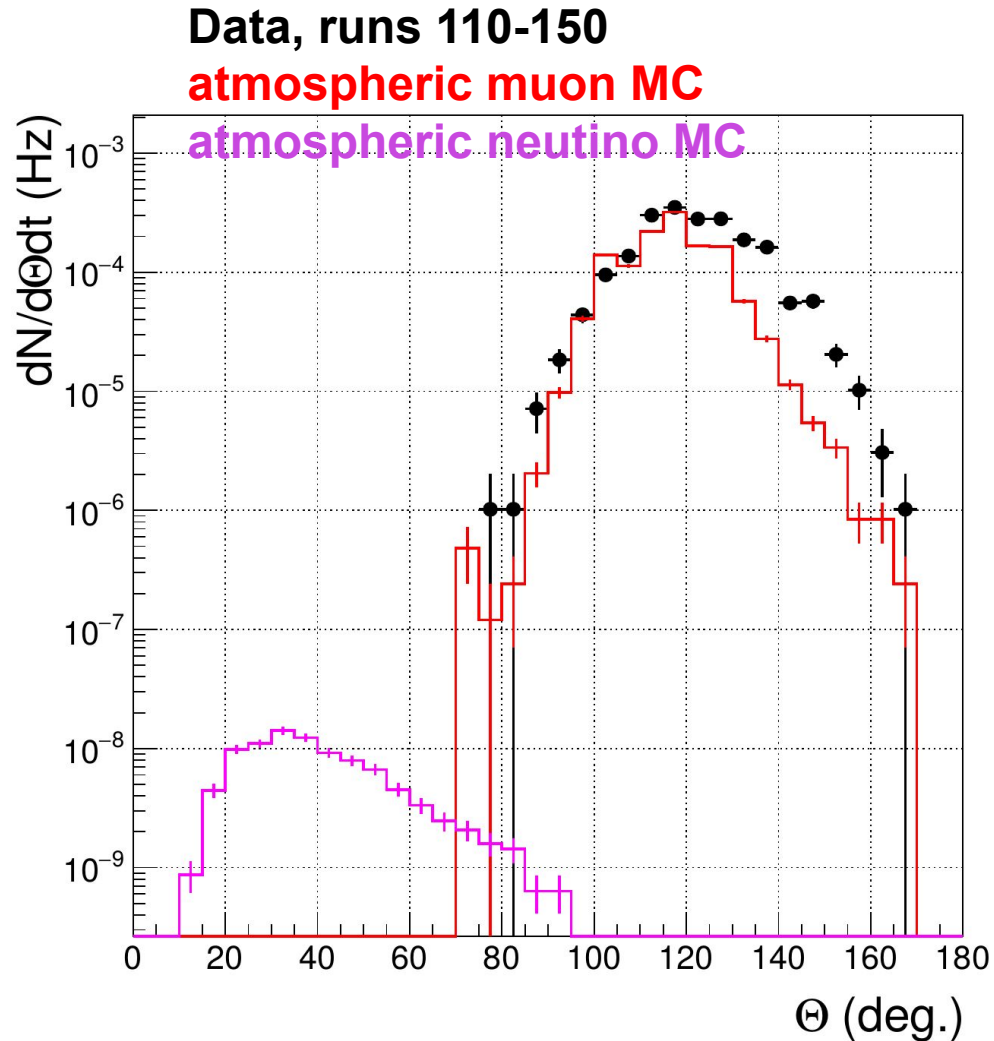
$$P_{hit} = \left( \prod_{i=1}^{N_{hit}} p_i(r) \right)^{1/N_{hit}}$$

Good agreement between data and MC

Strong discriminating power between downgoing groups and upgoing tracks

Cut of  $P_{hit} > 0.05$  was applied to data and MC sets

# Results



Misreconstructed tracks are removed

99% of muon groups is removed

Neutrino signal efficiency: 55%

No upgoing events in data

Need to increase the data sample  
and loosen the hit selection



# **Further development of the reconstruction**

# New method for hit selection

Available hit selection procedure is too tight

Sensitivity is small - candidate neutrino events were rejected

Need to modify hit selection to obtain good purity of hits used for the fit with as high as possible efficiency of the selection

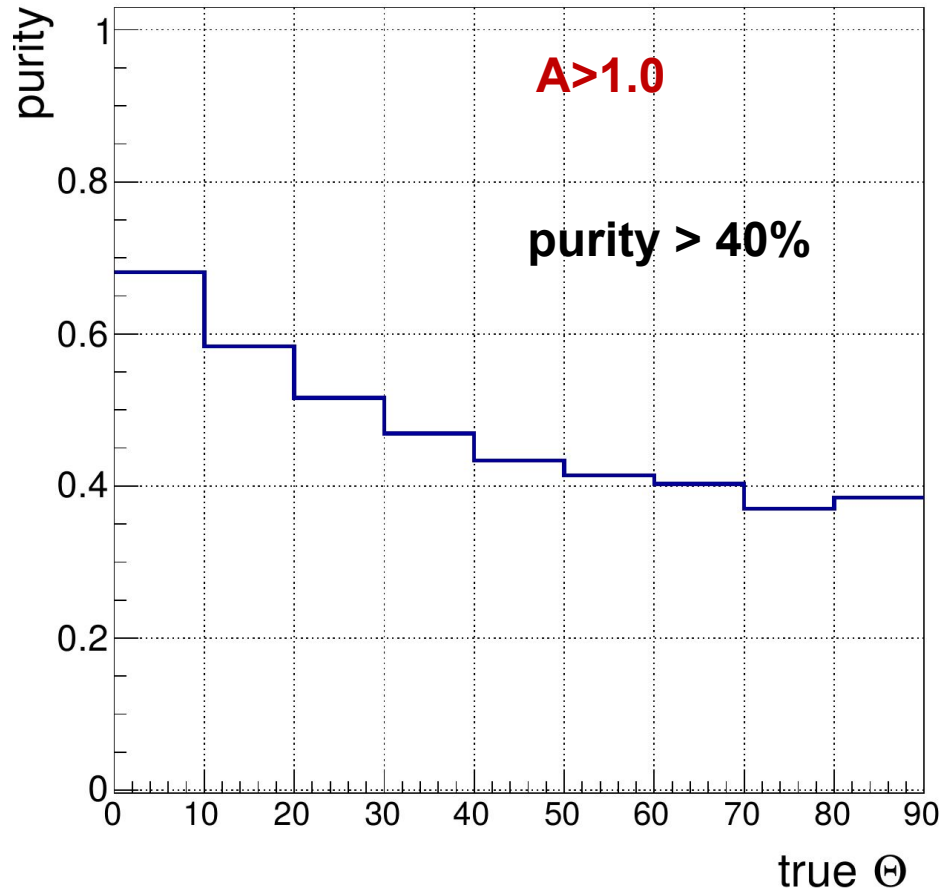
**purity** - fraction of signal hits in selected group for events with at least 6 selected hits

**efficiency** - fraction of hits with  $A > 1.6$  pe which were picked by the algorithm for events with at least 6 signal hits

The study was done on upgoing atmospheric neutrino MC sample  
6 hits on at least 3 strings selection

# Causality criterium

First step - apply causality criterium



$$|\Delta T| < (n\Delta R/c) + t_s; \quad t_s = 30 \text{ ns}$$

Loop over all impulses in the event

- Construct causally connected group starting from each impulse
- All pairs inside the group must be causally connected
- Each group is passed to further processing
- After further processing the group which has the best quality/nHits ratio is selected for trajectory fit

**At least 6 hits at 3 strings:  
54% of events pass this selection**

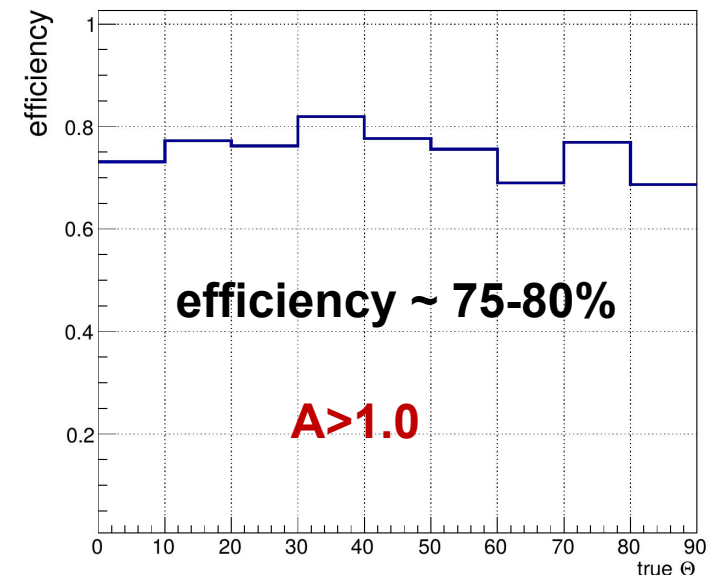
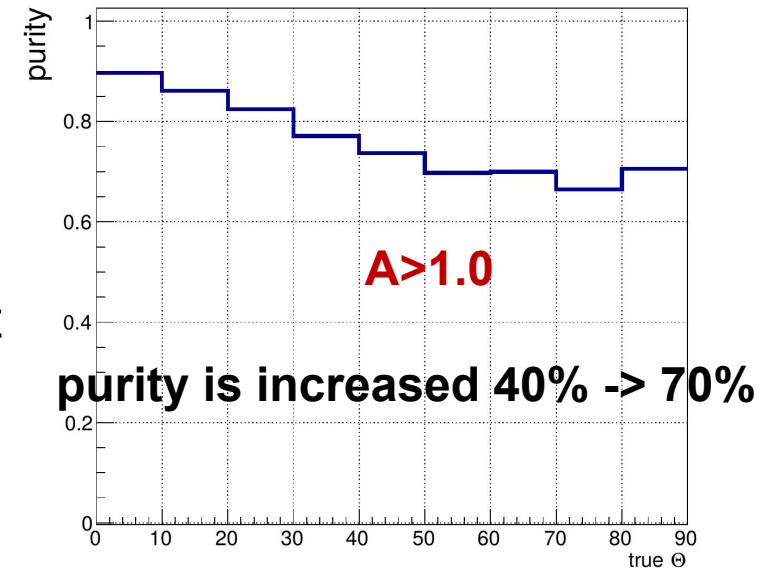
# Removal of residuals I

Do the following procedure 7 times with gradual tightening of cuts on  $t_{res}$  and  $\rho$

- Loop over the collection of hits inside the group
- Exclude hit and estimate the trajectory direction without it
- Calculate residual time ( $t_{res}$ ) and distance ( $\rho$ ) for the hit
- Exclude hit from the group if  $t_{res} < \text{cut}$  or  $\rho < \text{cut}$
- Most tight cuts:  $t_{res} < 300$  s,  $\rho < 60$  m

If there are still  $> 6$  hits in the group go to the next stage

With this procedure purity is increased to 70%



# Removal of residuals II

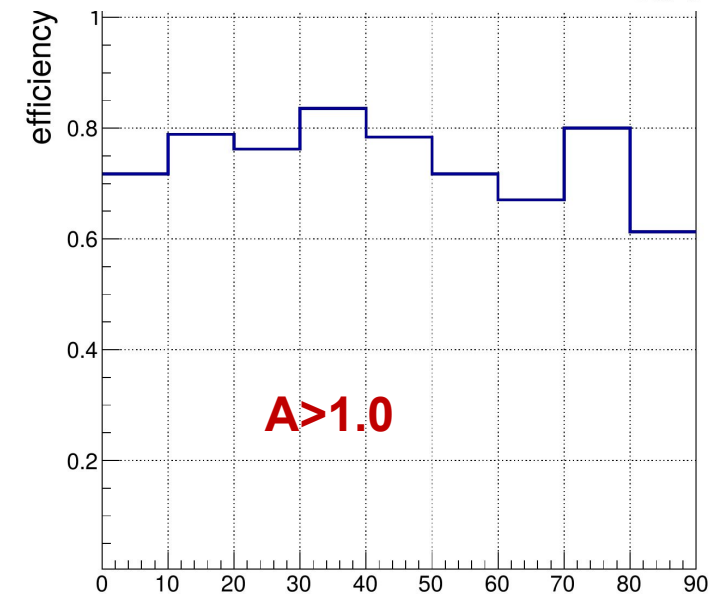
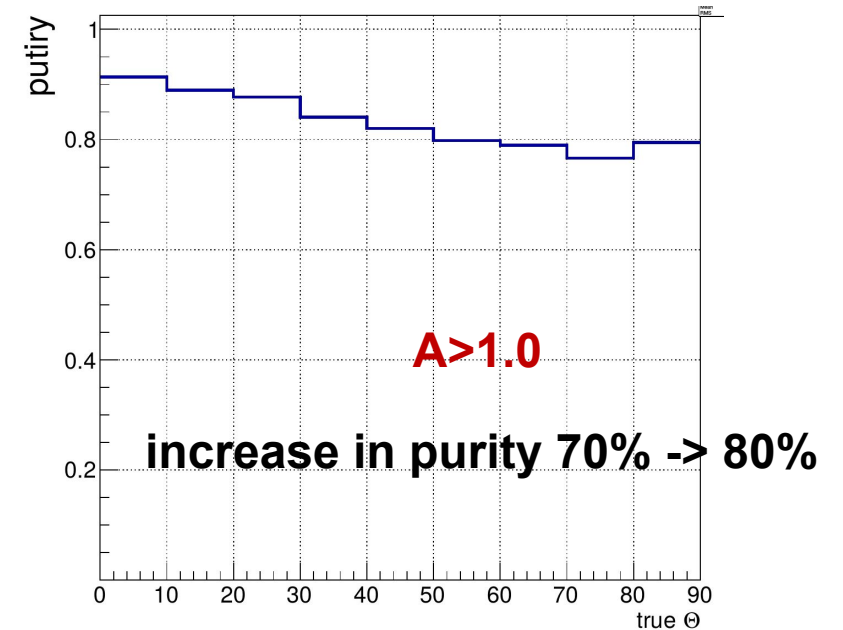
Almost similar procedure using  $p_{hit}$  variable

Do the following procedure 5 times  
with gradual tightening of cuts on  $p_{hit}$

- Estimate the trajectory direction
- Loop over hits
- Exclude ones with very low probability for the hit
- In 5 steps, tightest cut  $p_{hit} > 1e-5$

That's the final step. After that group with  
the best quality/nHits ratio is selected

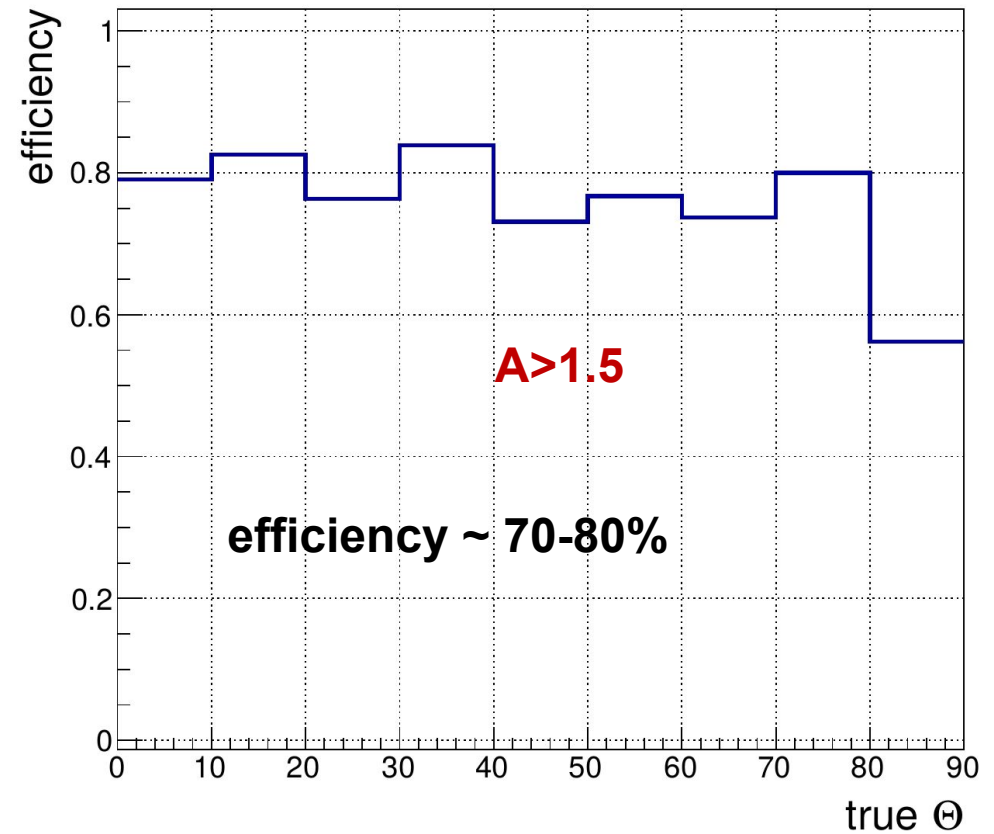
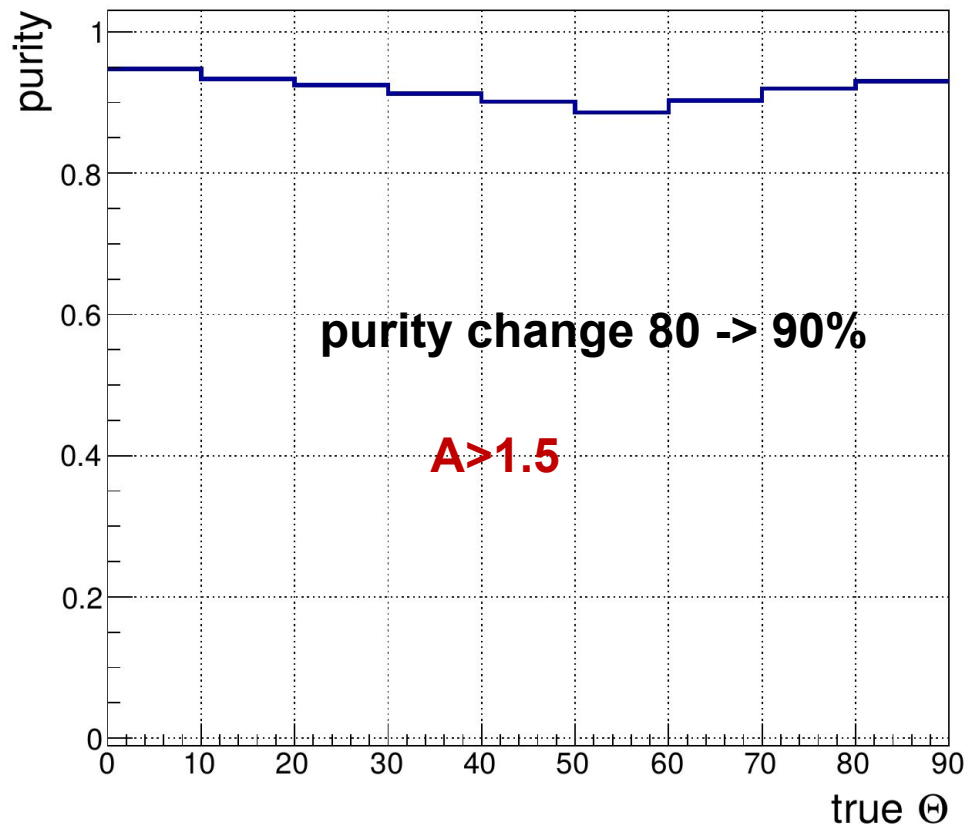
10% of events pass 6 hits at 3 strings selection



# Amplitude cut dependence

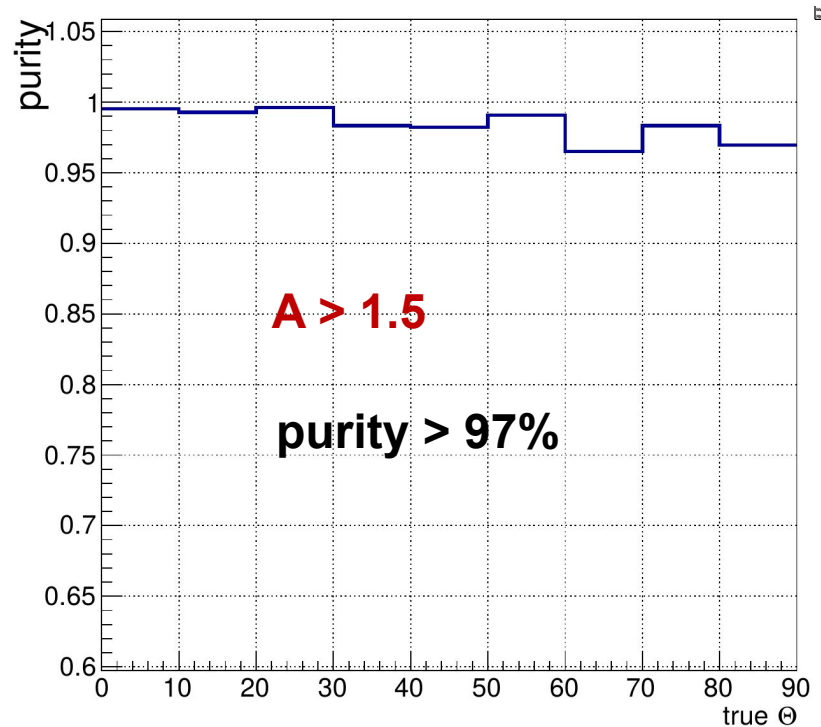
To compare with the old method we increase the threshold from **1.0** to **1.5**

6 hits at 3 strings selection: 3.5% of the sample is selected



# Comparison with the old method

6 hits on 3 strings: 0.02% have survived



change in performance:

~15 times increase in event yield  
worse purity: 97% -> 90%

Less stable fit -> less tracks will be passing the quality criteria

**Robust fit method should be developed**

# Track reconstruction results

Mismatch angle after the quality cuts

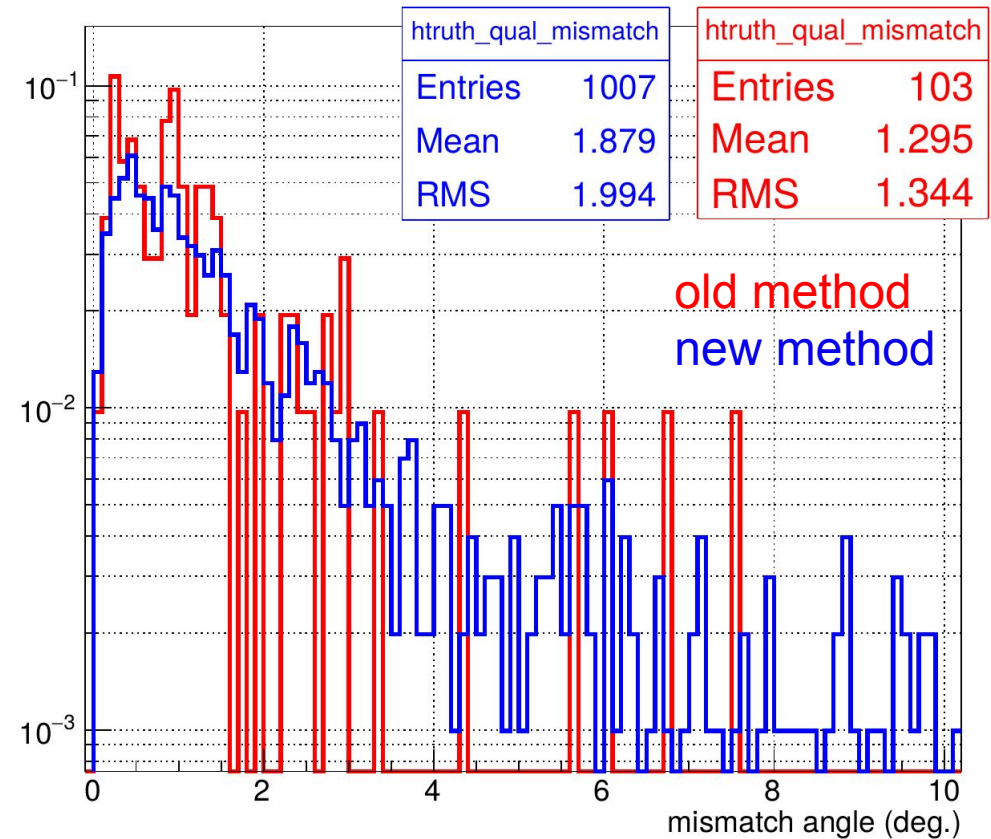
New method, median: 1.3 degrees

Old method, median: 1.0 degree

10 times increase in sensitivity

Tail:

new method - 4.5% of tracks have mismatch angle > 10 degrees



These methods should be complimentary and run in parallel with different thresholds

**Fit method should be improved - use robust fitting (not sensitive to outliers)**

**Another way - exclude outliers and refit (slower)**



# Code status

First version of the reconstruction is implemented in BARS

- Hotspot method for hit selection
- Track reconstruction
- Almost no quality parameters

Current priority: commit recent developments to BARS

- Hit selection modules:
  - New method for hit selection
- Reconstruction modules:
  - More minimisation functions
  - Functions to exclude outliers
  - Fill various quality data members in BRecParameters
  - Add references to used impulses to BRecParameters
- Monitoring package:
  - Hit selection monitor
  - Reconstruction monitor (theta, phi, quality, etc...)
- Automation of processing

# Muon reconstruction action items I

- Automatic processing
  - New programs/reconstruct-muon program from Alexander
  - Should also include monitoring
  - Two settings - MC and data
- Neutrino events bank
  - Process as much data as possible
  - Select good candidates to neutrino events using cut-based analysis
- Precise vertical track reconstruction
- Understand the data-MC discrepancy
  - Polar angle distributions
  - Quality distribution, etc..
- Processing time optimisation

# Muon reconstruction action items II

- Background rejection
  - An MVA-based (NN, BDT) rejection of background would enhance the sensitivity
  - Several variables with background rejection potential have been identified
- Optimisation
  - There are many parameters in hit selection and minimisation (many are hardcoded)
  - Current parameters are chosen "by eye"
  - An optimisation for range of energies and polar angles should be done to maximise the sensitivity
- Study the sensitivity to miscalibrations and misalignment
- Likelyhood fit
  - Second stage of the fit should be added - likelyhood maximisation

**BACKUP**

## Fit with quality function

**Quality function:** 
$$Q = \sum_{i=1}^{N_{hit}} \left[ \frac{(t_i^{est} - t_i)^2}{\sigma_t^2} + \frac{A(a_i)D(d_i)}{d_0} \right]$$
 [inspired by <https://arxiv.org/abs/1105.4116>]

- $\sigma_t=3$  ns - jitter of PMT signal development
- $t_i^{est}$  - estimation of arrival time in direct cerenkov light approximation
- $t_i$  and  $d_i$  - actual time of hit and distance of OM from the track
- Amplitude function,  $A(a_i) = a_0 a_i / \sqrt{a_0^2 + a_i^2}$  , uses amplitude  $a_i$  corrected for the angular sensitivity of the OM
- Distance function,  $D(d_i) = \sqrt{d_1^2 + d_i^2}$
- Chosen parameter values:  $\sigma_t=3$  ns,  $a_0=500$  p.e.,  $d_0 = 5$  m ,  $d_1 = 10$  cm

**Minimisation is performed with MIGRAD package from ROOT**

# Merging of groups

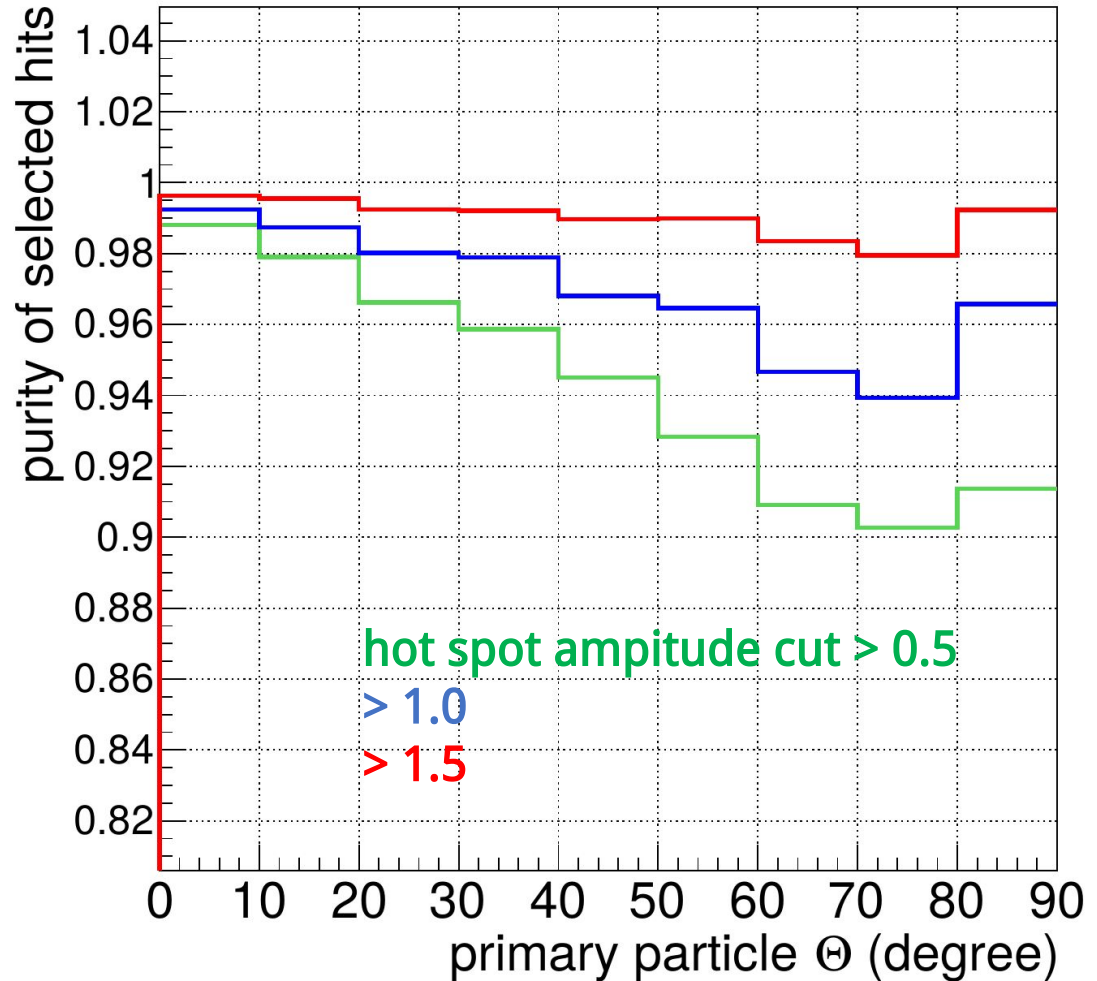
Purity of merged groups:

- Fraction of signal hits (direct or shower) in obtained global groups

Few symmetric amplitude cuts:

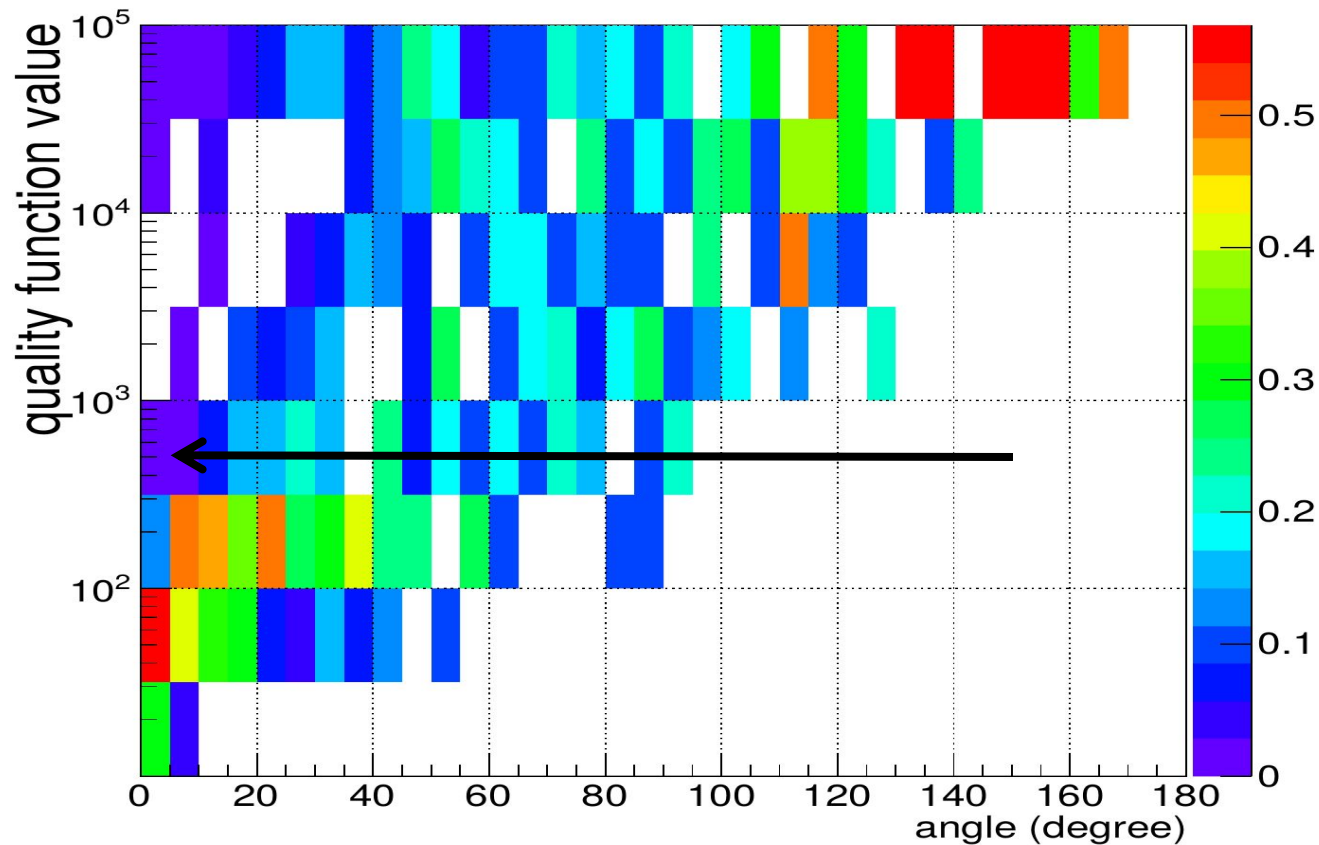
$$A_{1,2} > 0.5, 1.0, 1.5 \text{ (p.e.)}$$

With  $A_{1,2} > 1.5$  purity of  $> 98\%$  is achieved



# Muon reconstruction for upgoing neutrino II

Quality function demonstrates correlation with mismatch angle

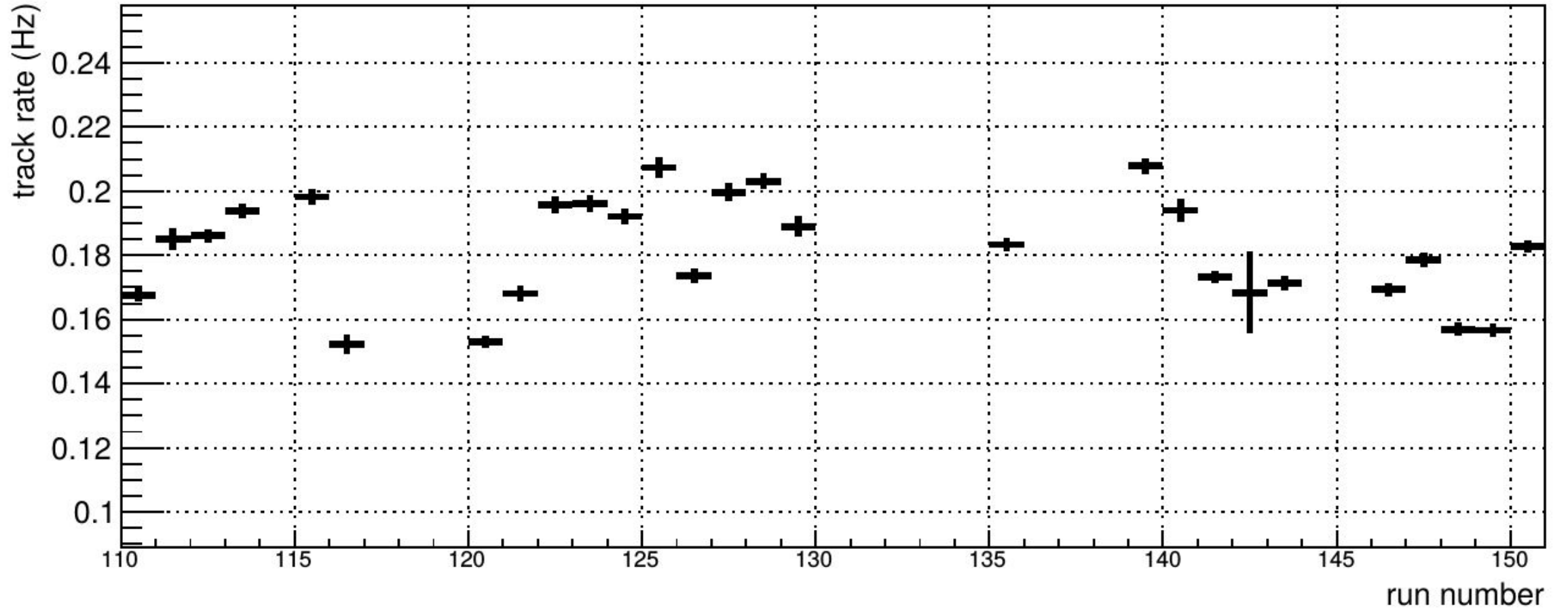


Plots shows distribution of quality function for series of mismatch angle values

Tracks of good quality are defined as:  $QF < 500$

# Results III

reconstructed track rate vs. run number

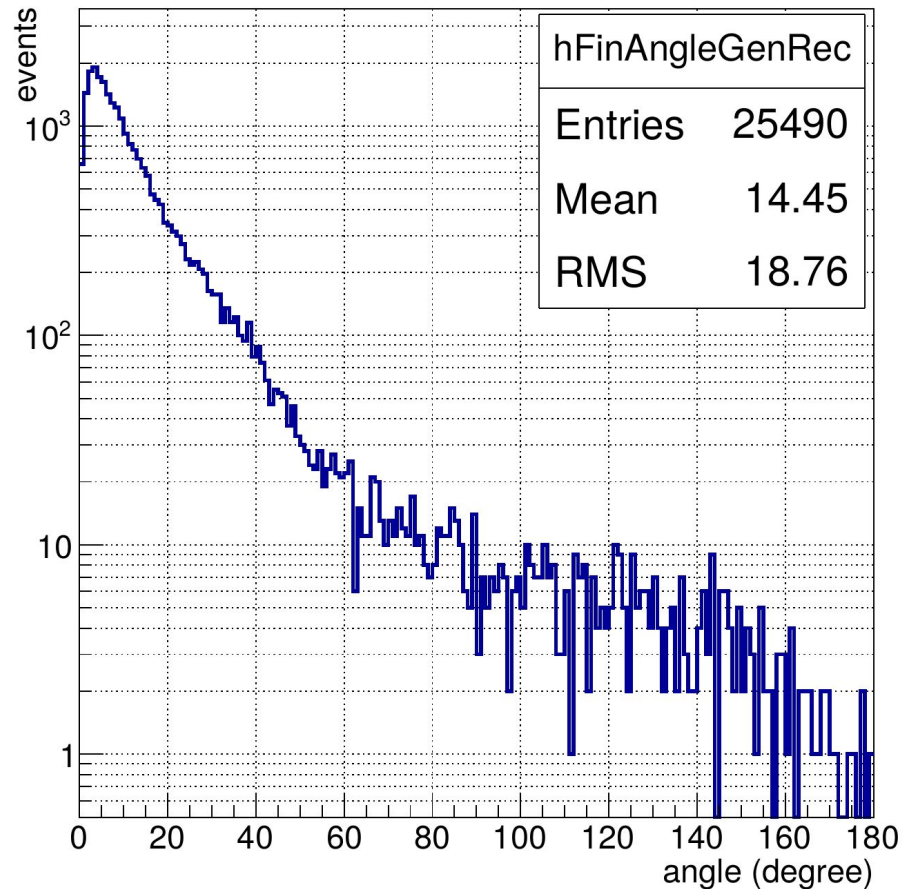




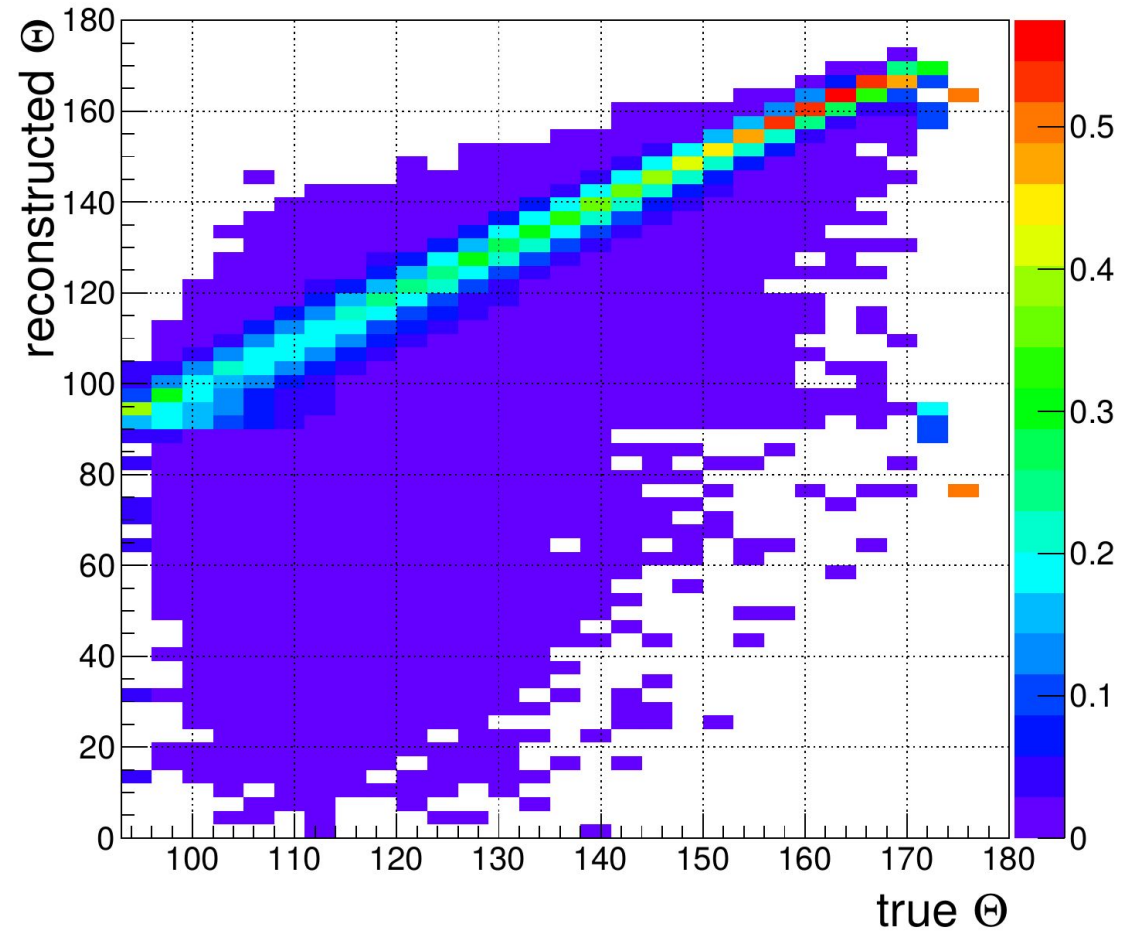
# Performance of reconstruction in MC

Selection on further slides:  $A_{1,2} > 1.5/1.5$ ; at least 6 hits on 3 strings

mismatch angle



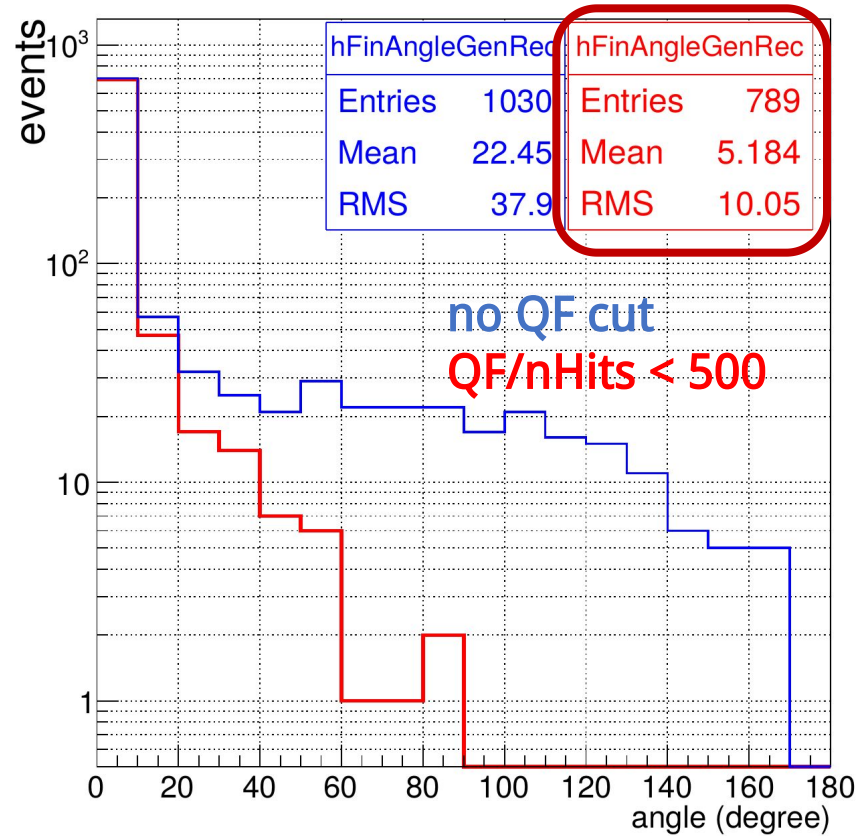
response matrix



# Upgoing muons : applying quality function cut

Event selection:  $A_{1,2} > 1.5$  p.e,  $t_s = 30$ ns, at least 6 hits on 3 strings

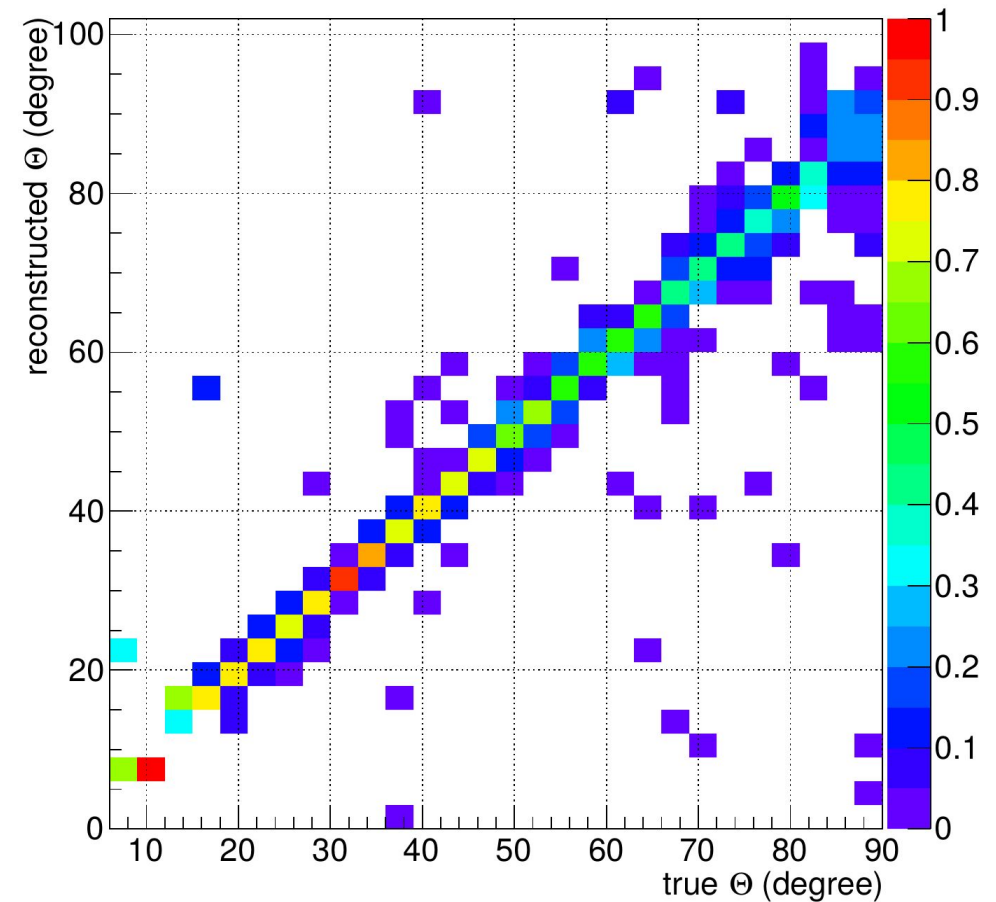
mismatch angle



median without quality cut: 2.9

median with quality cut: 1.8

response matrix



# Muon track reconstruction

**Track parametrisation:**  $R(\vec{t}) = \vec{R}_0 + c(t - t_0)\vec{V}$

$\vec{V}$  is unit vector in polar coordinates

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**Initial approximation:**

$$V_{init}^{\vec{}} = (1/|\sum_{t_i < t_j} \vec{R}_{ij}|) \sum_{t_i < t_j} \vec{R}_{ij} \quad \text{where } i \text{ and } j \text{ are ordered in time and belong to different strings}$$

Initial values for  $\vec{R}_0$  and  $t_0$  are obtained using first (in time) hit

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**Minimisation function:**

$$Q = \sum_{i=1}^{N_{hit}} \left[ \frac{(t_i^{est} - t_i)^2}{\sigma_t^2} + \frac{A(a_i)D(d_i)}{d_0} \right] \quad \text{inspired by ANTARES paper: } \underline{\underline{\a href="https://arxiv.org/abs/1105.4116">https://arxiv.org/abs/1105.4116$$

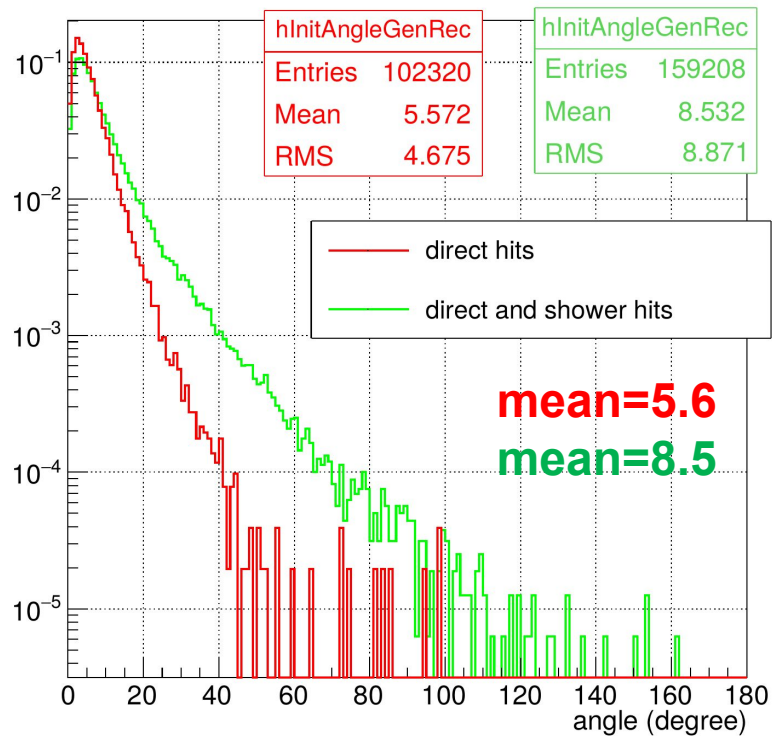
Direct cerenkov approximation for the time estimation  
 $A$  and  $D$  are amplitude and distance functions

# Performance with MC truth

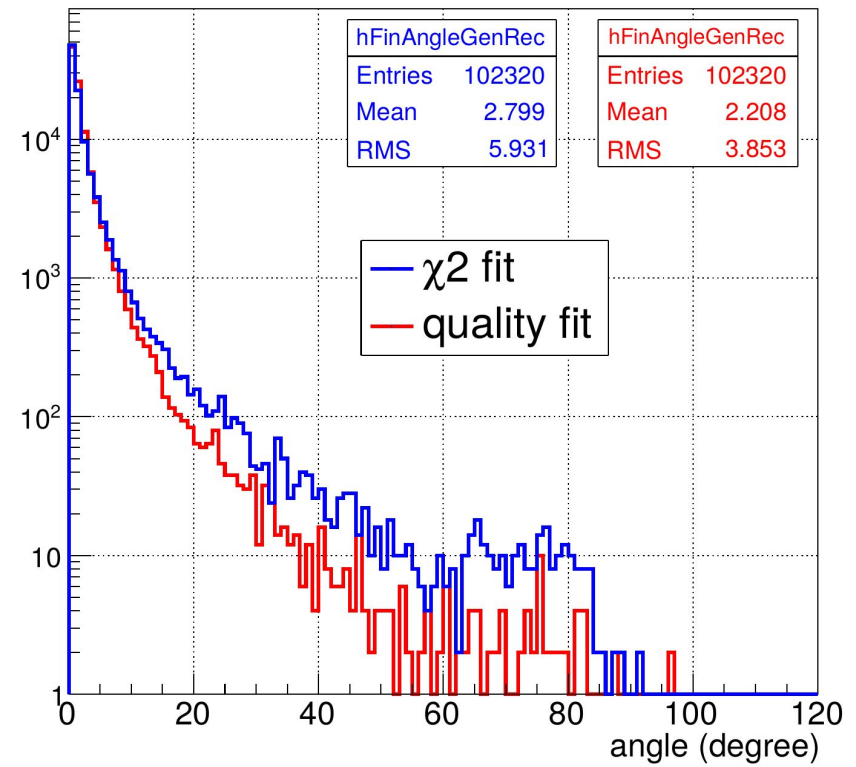
Events with at least 6 hits on 3 strings are selected (here and further in this talk)

## MC truth -based selection of direct cerenkov hits and shower hits

mismatch angle for initial approximation



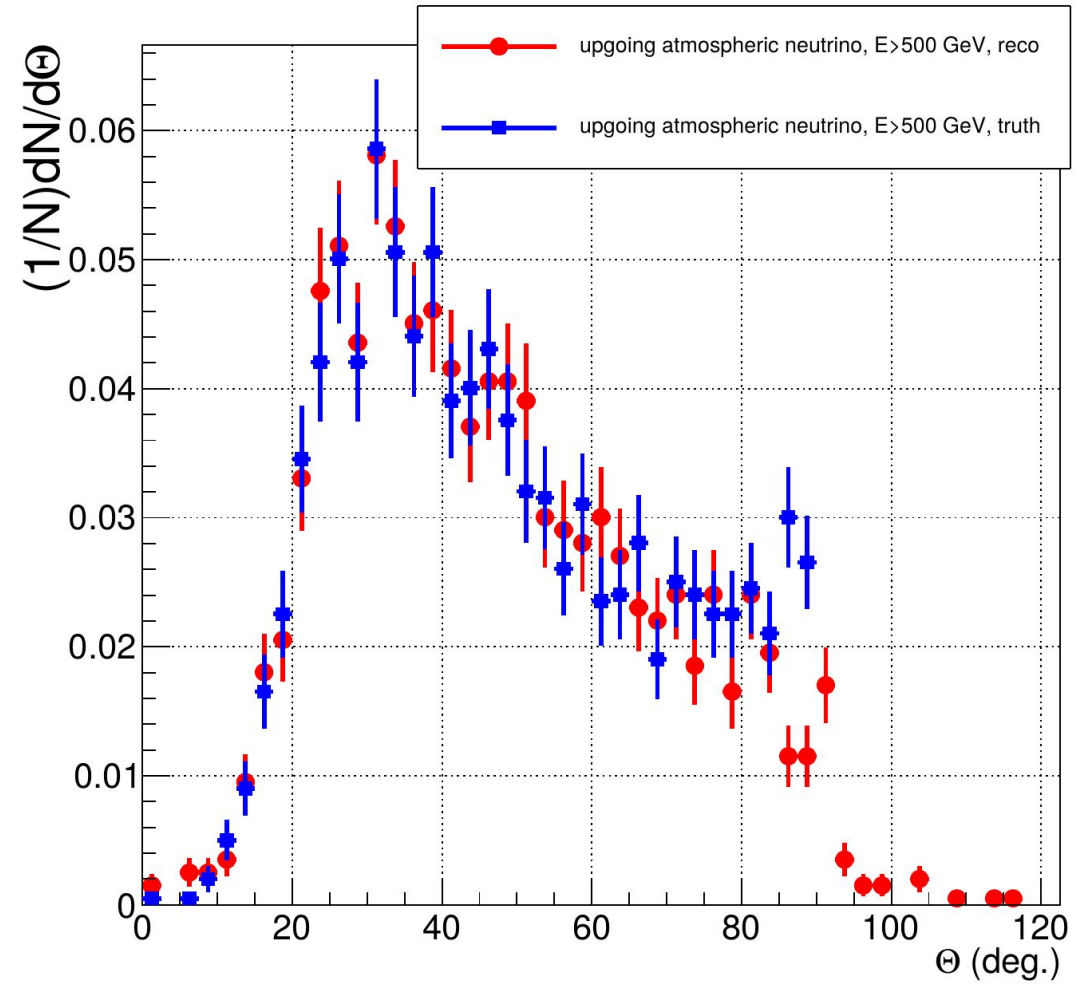
fit results for direct hits



**median angle for quality fit: 1.3**

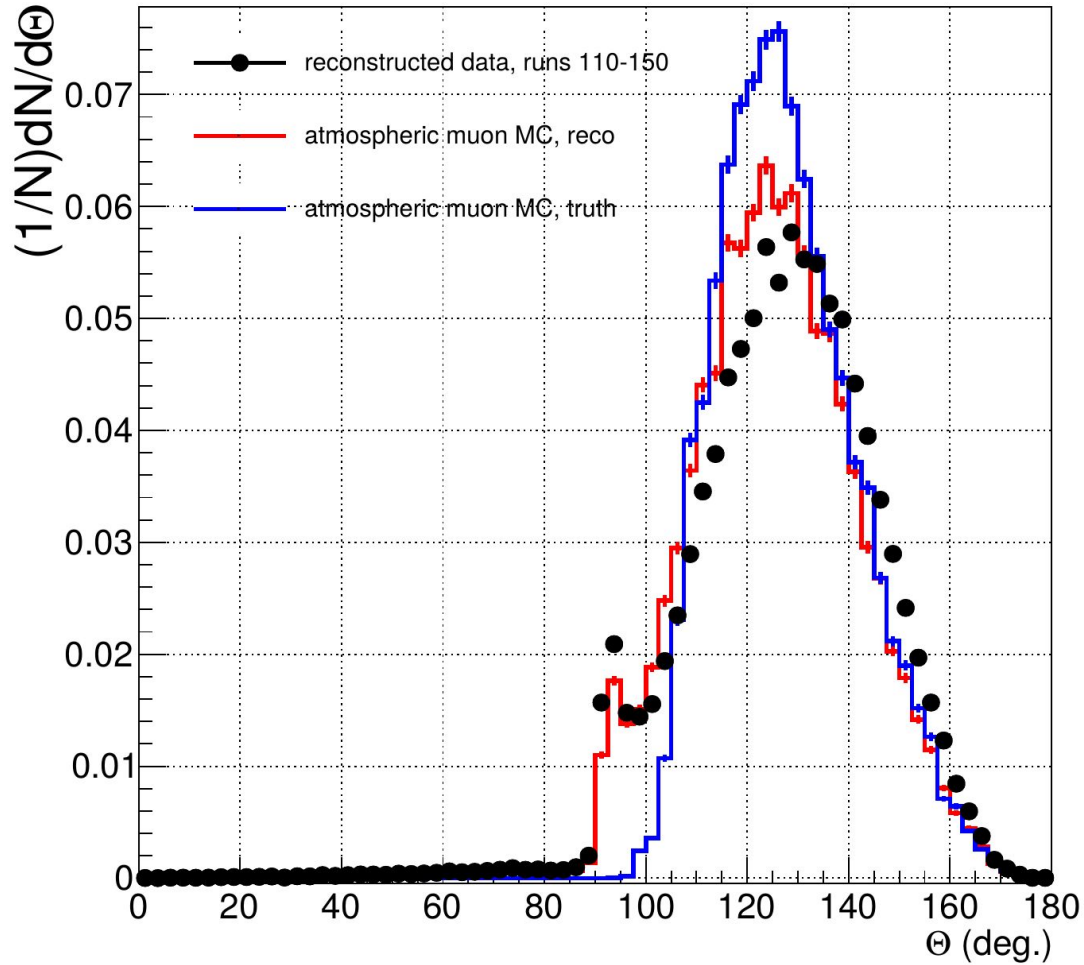
# Reconstructed polar angle

MC reconstructed (red)  
and  
true (blue)  
polar angle

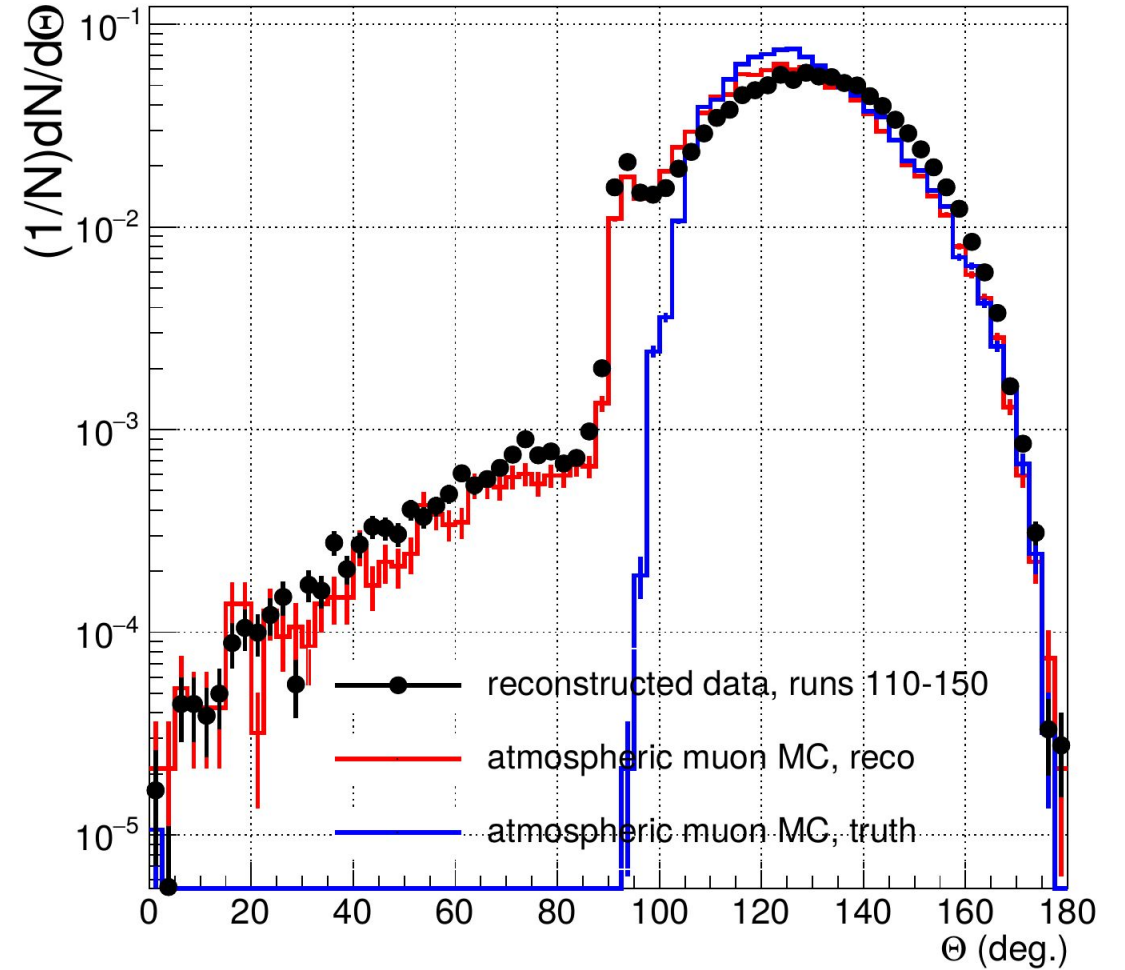


# Results I

normal scale

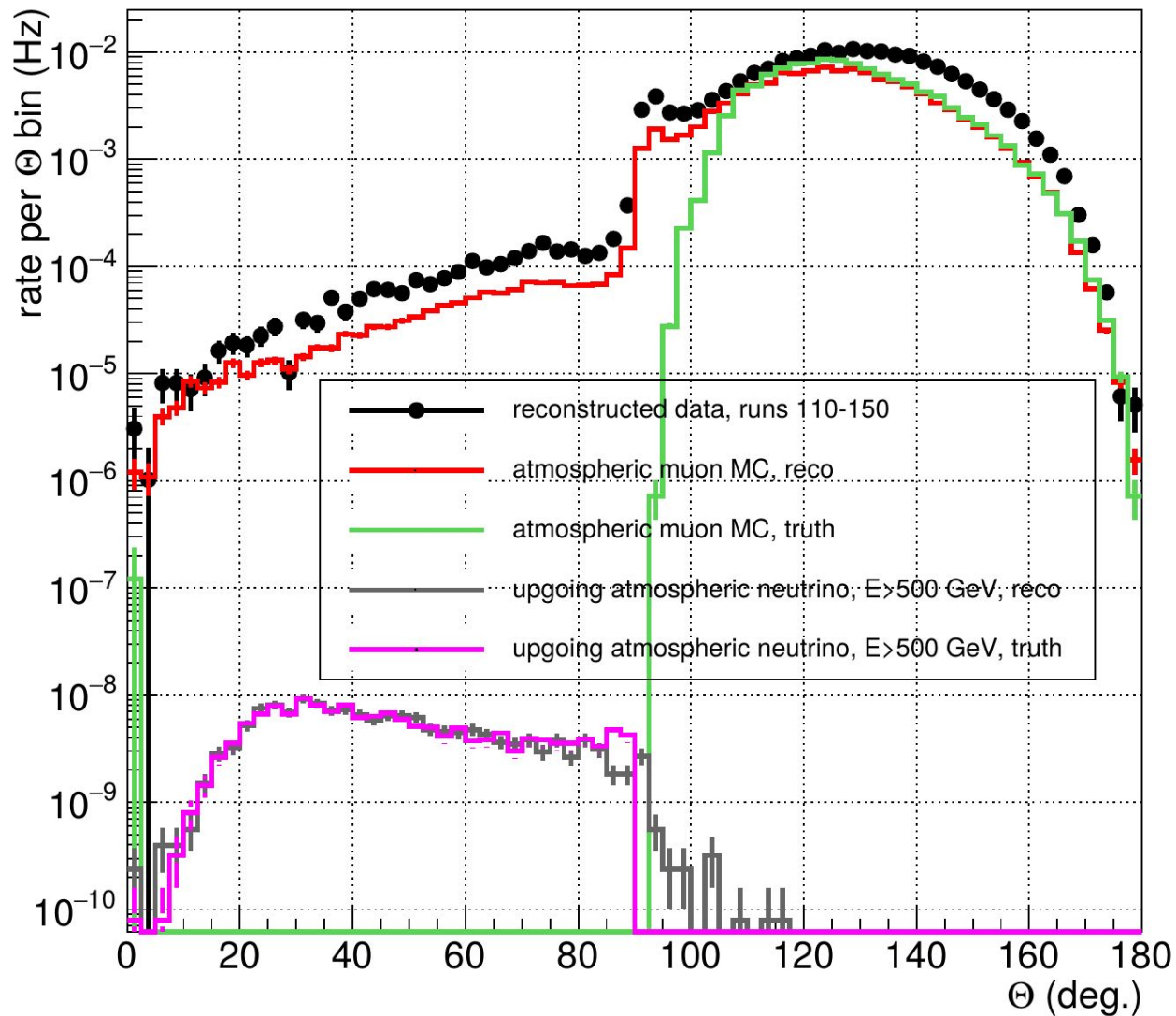


log scale



**Fraction of misreconstructed as upgoing tracks is  $\sim 1.5\%$  both for data and MC**

# Results IV



Polar angle distributions scaled by the exposition time

Data rate is  $\sim 1.5$  times larger than MC

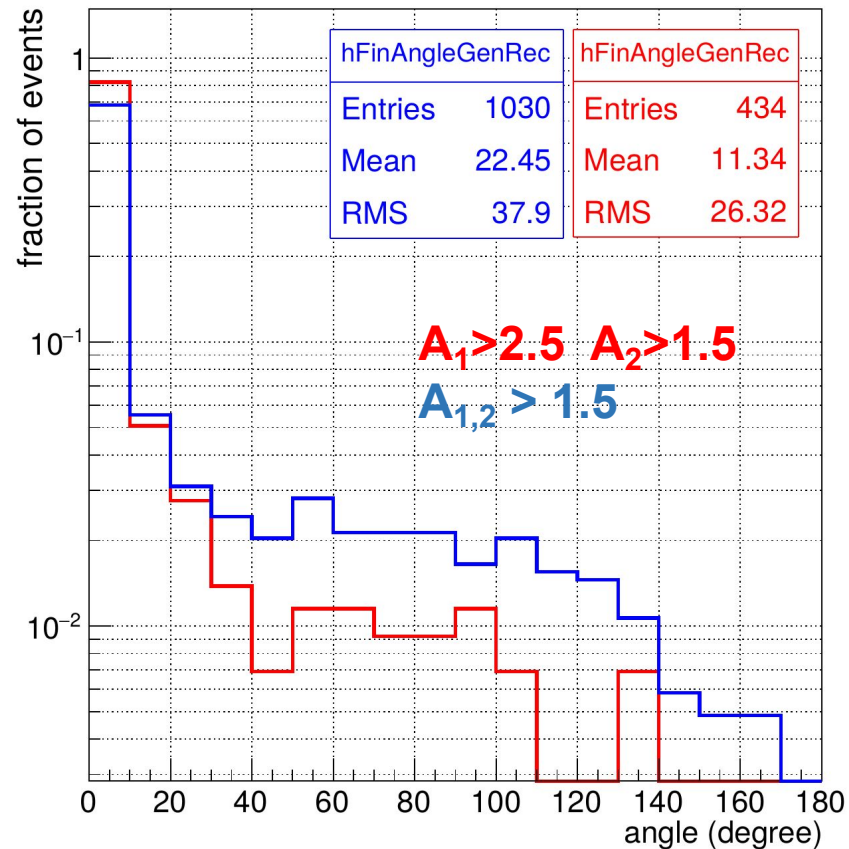
Upgoing atmospheric neutrino rate is  $10^3$  times smaller than current background from misreconstructed muons

More advanced background suppression methods are to be developed

# Muon reconstruction for upgoing neutrino

Event selection:  $A_{1,2} > 1.5$  p.e,  $t_s = 30$ ns, **at least 6 hits on 3 strings**

mismatch angle



polar angle response matrix

