

# On $x_F$ -distribution of the double longitudinal-spin asymmetry in $J/\psi$ production at NICA

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## Outline

- NRQCD model
- Definition of the  $A_{LL}$
- $x_F$ -distribution of the  $A_{LL}$  at NICA
- Summary

## A sketch of NRQCD formalism

The NRQCD framework [G. T. Bodwin, E. Braaten, and G. P. Lepage, Phys. Rev. D **51**, 1125 (1995)] describes heavy quarkonia in terms of Fock state decompositions. In case of orthoquarkonium state the wave function can be written as power series expansion in the velocity parameter  $v \sim 1/\ln M_Q$ :

$$|\mathcal{H}\rangle = \mathcal{O}(v^0)|Q\bar{Q}[{}^3S_1^{(1)}]\rangle + \mathcal{O}(v)|Q\bar{Q}[{}^3P_J^{(8)}]g\rangle + \mathcal{O}(v^2)|Q\bar{Q}[{}^1S_0^{(8)}]g\rangle \quad (1)$$

$$+ \mathcal{O}(v^2)|Q\bar{Q}[{}^3S_1^{(1,8)}]gg\rangle + \dots \quad (2)$$

In the NRQCD effects of short and long distances are separated, and then the cross-section of heavy-quarkonium production via a partonic subprocess  $a + b \rightarrow \mathcal{H} + X$  can be presented in a factorized form:

$$d\hat{\sigma}(a + b \rightarrow \mathcal{H} + X) = \sum_n d\hat{\sigma}(a + b \rightarrow Q\bar{Q}[\textcolor{magenta}{n}] + X) \times \langle \mathcal{O}^\mathcal{H}[\textcolor{magenta}{n}] \rangle, \quad (3)$$

where  $\textcolor{magenta}{n}$  denotes the set of quantum numbers of the  $Q\bar{Q}$  pair, and its nonperturbative transitions into  $\mathcal{H}$  is described by the NMEs  $\langle \mathcal{O}^\mathcal{H}[\textcolor{magenta}{n}] \rangle$ .

In the general case, the partonic cross-section of quarkonium production from the  $Q\bar{Q}$  Fock state  $\textcolor{magenta}{n} = {}^{2S+1}L_J^{(1,8)}$  has the form:

$$d\hat{\sigma}(a + b \rightarrow Q\bar{Q}[{}^{2S+1}L_J^{(1,8)}] \rightarrow \mathcal{H}) = d\hat{\sigma}(a + b \rightarrow Q\bar{Q}[{}^{2S+1}L_J^{(1,8)}]) \times \frac{\langle \mathcal{O}^\mathcal{H}[{}^{2S+1}L_J^{(1,8)}] \rangle}{N_{col}N_{pol}},$$

where  $N_{col} = 2N_c$  for color-singlet state,  $N_{col} = N_c^2 - 1$  for color-octet state, and  $N_{pol} = 2J + 1$ .

## Double-spin asymmetry

The double longitudinal-spin asymmetry is defined as

$$A_{LL} = \frac{\sigma_{++} - \sigma_{+-}}{\sigma_{++} + \sigma_{+-}} = \frac{\Delta\sigma}{\sigma},$$

LO Collinear Parton Model + LO NRQCD-factorization:

$$\Delta\sigma = \sum_{\textcolor{red}{n}} \left\langle \mathcal{O}^X[\textcolor{red}{n}] \right\rangle \sum_{i,j} \Delta f_i \otimes \Delta f_j \otimes \Delta\hat{\sigma}_{ij}[\textcolor{red}{n}],$$

$$\sigma = \sum_{\textcolor{red}{n}} \left\langle \mathcal{O}^X[\textcolor{red}{n}] \right\rangle \sum_{i,j} f_i \otimes f_j \otimes \hat{\sigma}_{ij}[\textcolor{red}{n}].$$

Un-polarized partonic cross-sections  $\hat{\sigma}_{ij}[\textcolor{red}{n}]$  are well-known at LO (e.g. [P.L. Cho, A.K. Leibovich (1996)] and [R. Gastmans, W. Troost and T. T. Wu, Phys. Lett. B **184**, 257-260 (1987)]).

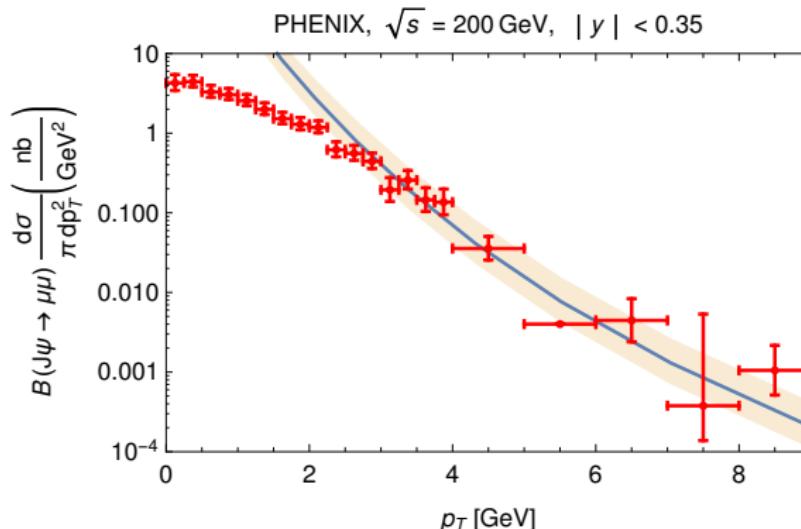
Details on LO calculations of  $\Delta\hat{\sigma}_{ij}[\textcolor{red}{n}]$  can be found in [Klasen, Kniehl, Steinhauser, Phys.Rev.D **68** (2003) 034017, hep-ph/0306080]

## PDFs and octet LDMEs

LO LDMEs from [Braaten, Kniehl, Lee, Phys.Rev.D**62** (2000) 094005] together with [NNPDF30\\_nlo\\_as\\_0119\\_nf\\_6](#) PDF set and [NNPDFpol11\\_100](#) polarized PDF set. Within NRQCD LO fits determine only linear combination of octet LDMEs:

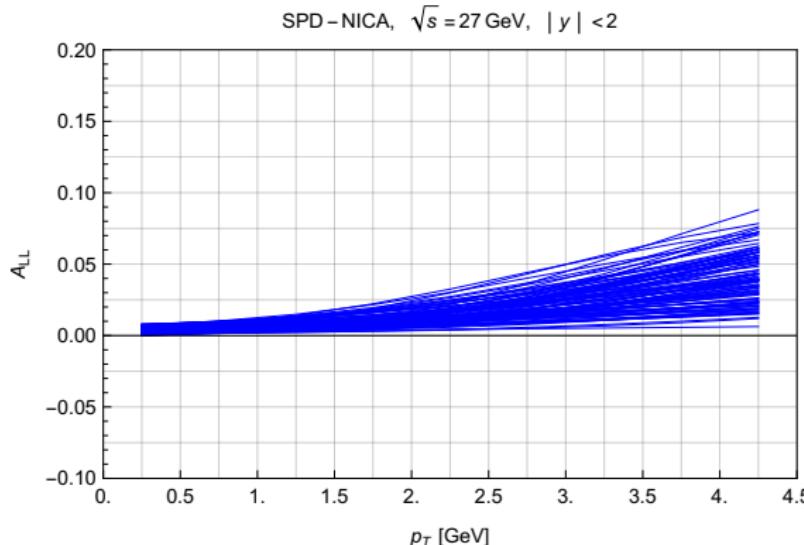
$$\mathcal{M}_8 = \left\langle \mathcal{O}^{J/\psi} \left[ {}^1 S_0^{(8)} \right] \right\rangle + \frac{r}{m_c^2} \left\langle \mathcal{O}^{J/\psi} \left[ {}^3 P_0^{(8)} \right] \right\rangle, \quad r = 3.5, \quad m_c = 1.5$$

The  $J/\psi$   $p_T$ -spectrum from RHIC (direct and feed-down contributions):



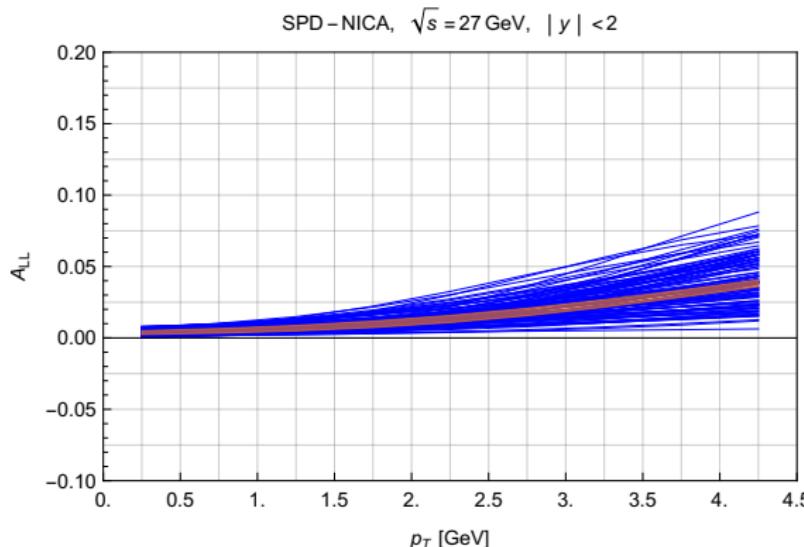
Previous result:  $p_T$ -distibution at  $\sqrt{s} = 27$  GeV

$A_{LL}$  for a hundred replicas of  $\Delta g$ :



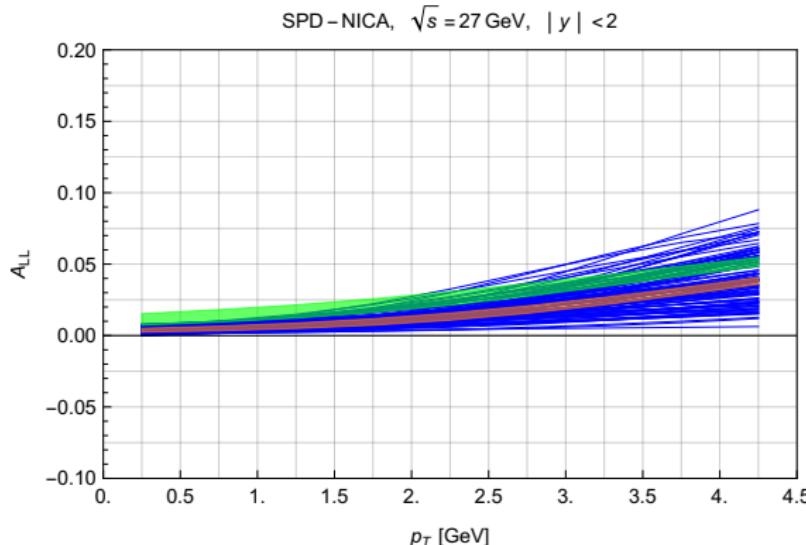
Previous result:  $p_T$ -distibution at  $\sqrt{s} = 27$  GeV

$A_{LL}$  for a hundred replicas of  $\Delta g$ , band – scale variaton for the average on replicas:



Previous result:  $p_T$ -distibution at  $\sqrt{s} = 27$  GeV

$A_{LL}$  for a hundred replicas of  $\Delta g$ , bands – scale and LDME-variation:



## $x_F$ -distributions of LO asymmetry at $\sqrt{s} = 27$ GeV

$A_{LL}$  for a mean of all replicas of  $\Delta g$ , an orange band – scale-variation:

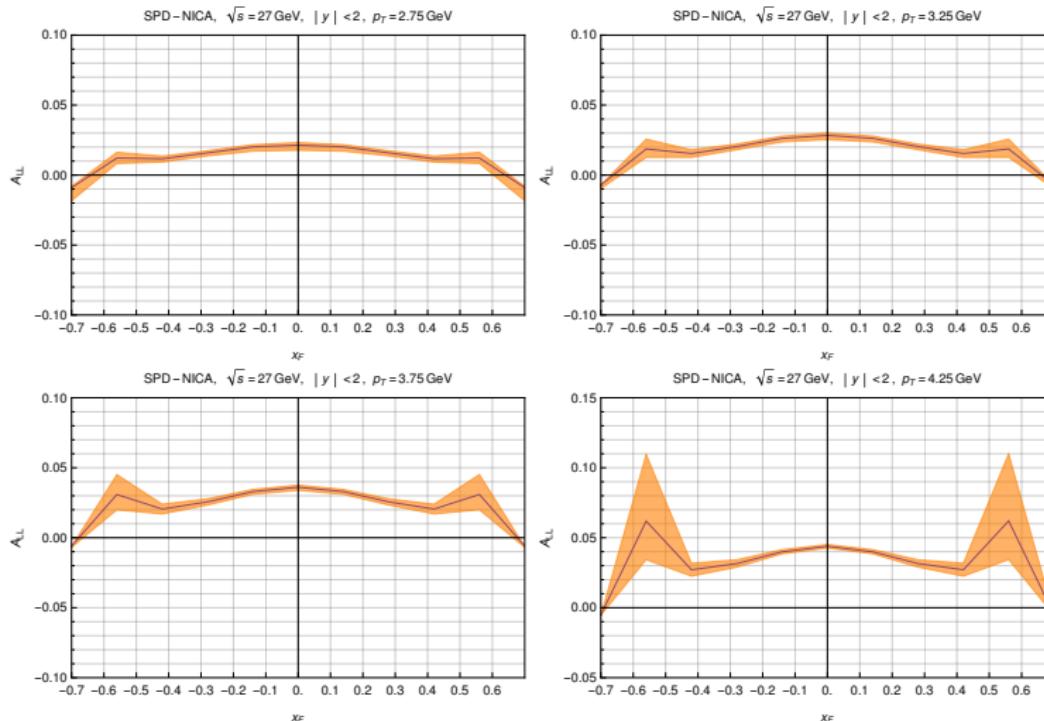
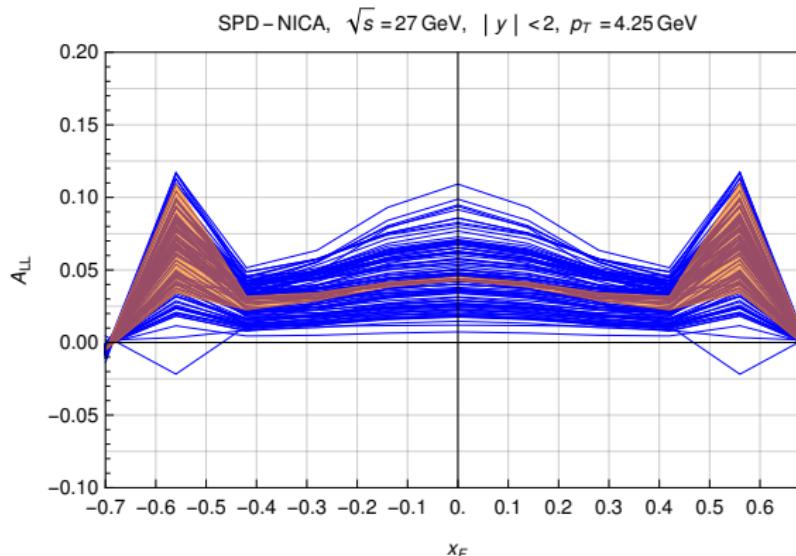


Figure 1: The  $A_{LL}$  for prompt  $J/\psi$  production at  $\sqrt{s} = 27$  GeV,  $|y| \leq 2$  at different  $p_T$ -values: 2.75, 3.25, 3.75 and 4.25 GeV.  $gg + qg$  contributions are taken into account. 9 / 12

$x_F$ -distribution of LO asymmetry at  $\sqrt{s} = 27$  GeV and  $p_T = 4.25$  GeV

The  $x_F$ -distribution of the LO  $A_{LL}$  for a hundred replicas of  $\Delta g$ , band – scale-variation:



## Summary

- We see, that the  $A_{LL}$  does not exceed the value of 10% for the  $p_T \in [0, 4.25]$  GeV.
- We should look closer to the peaks near the borders of the  $x_F$ -distributions and check stability of these numerical calculations.

Thank you for your attention!