Status of Laser Gravitational Wave Antennas

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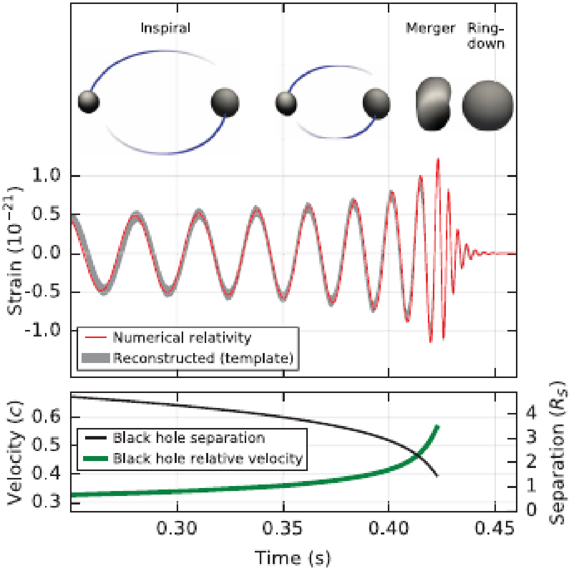
Session of Nuclear Division of Russian Academy of Science
Dubna, 1 — 5 April 2024

Outline

GW150914: 14 September 2015



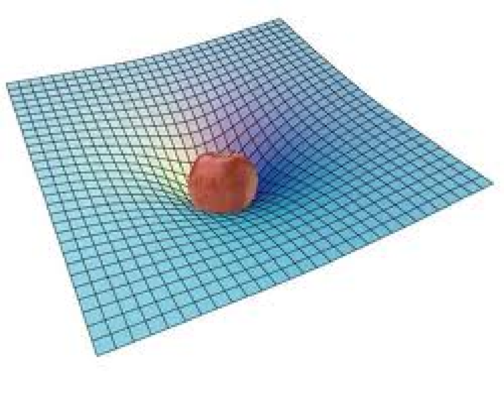
Masses of black holes 29 $M_\odot$, 36 $M_\odot$ at distance 1,3 billions of light years

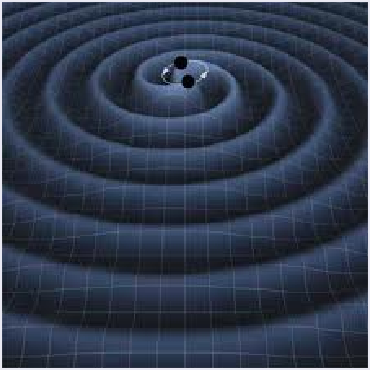
During 100 msec $\simeq 3M_\odot$ transforms to GW

Bottom: The Keplerian eff. black hole separation in units of Schwarzschild radii ($R_S = 2GM/c^2$) and the eff. relative velocity given by the post-Newtonian parameter $v/c = (GM\pi f/c^3)^{1/3}$,

Theory of General Relativity and GW Detectors

Flying pieces of space-time curvature

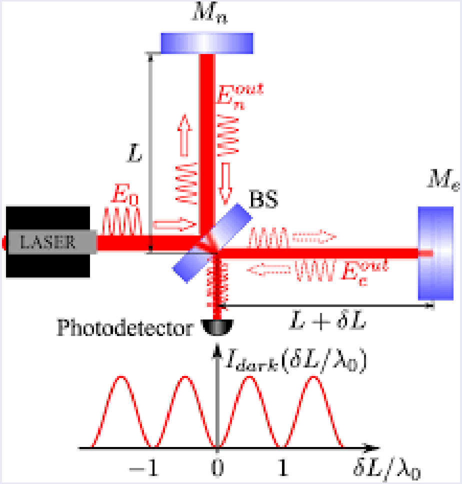


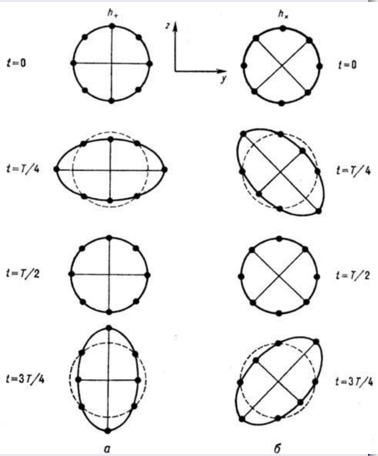


1993 г. Nobel Prize (Russell Hulse and Joseph Taylor) for discovery of GW via change of frequency of double pulsar rotation.

Idea of laser GW antenna

M.E. Hertsenshtein and V.I. Pustovoit, Zh.Eks.Ter.Fiz. **43**, 605 (1962)

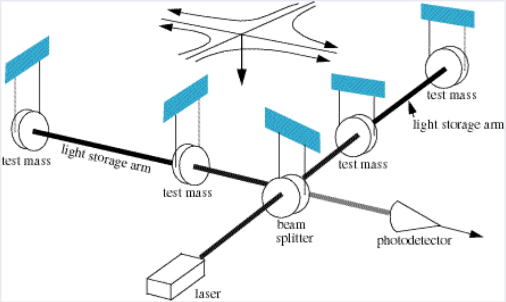




Лазерная гравитационная антенна

Схема и вид

1992 г. — Kip Thorne, Ronald Driver (CIT) and Rainer Weiss (MIT) предложили LIGO.



Scale of displacements

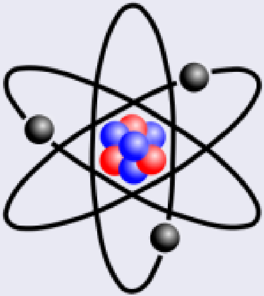
From Earth to atom

$\sim \quad 1.3 \cdot 10^7$ m $=$ 13000 km

$\Rightarrow$

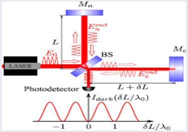
$\sim 10^{-1}$ m

$\Rightarrow$



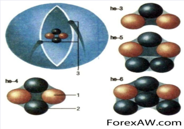
$\sim 7 \cdot 10^{-10}$ m $= 7$ A

From atom to LIGO: $d_{LIGO} \simeq 10^{-4} d_n$



d_{LIGO} 10^{-19} m

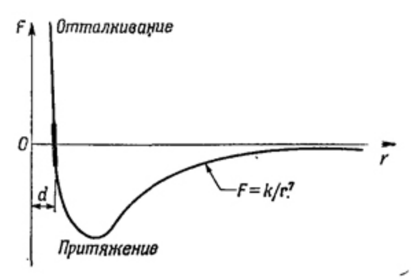
$\simeq$



$\sim 2 \cdot 10^{-15}$ m $=$ $5 \cdot 10^{-5}$ A

Atoms on surface

Surface fluctuations (rough estimate)



At room temperature $\Delta x \simeq 10^{-10}$ m.
On spot 10 cm $\times$10 cm — about $N = 10^{18}$ atoms.
Surface fluctuations (“breathing”)

$$\Delta X \simeq \frac{\Delta x}{\sqrt{N}} \simeq 10^{-19}\ \text{m} \qquad (1)$$

More accurate calculations

LIGO: mean position of spot $D = 10$ cm fluctuates for $\tau \simeq 0.01$ c
$\Delta X_{\text{therm}} \simeq 10^{-19}$ m
It is about в 10 *billions (!) times smaller* than atom,
or в *10 thousands (!) times smaller* than nucleus
Is it possible to measure?

What displacement we can measure?

V.B. Braginsky, V.I. Panov and V.D. Popelnyuk, 1981

Superconducting capacity meter, gap 4 microns:

$$\Delta X \simeq 10^{-19}\ \text{m}, \quad \text{gap 4 microns}, \quad \text{for } \tau = 10\ \text{c}$$

"Initial" LIGO, 2011

Laser beam measures coordinate averaged over spot $D = 6$ cm

$$\Delta X \simeq 4 \times 10^{-18}\ \text{m}, \quad \text{distance } L = 4\ \text{km}, \quad \text{for time } \tau \simeq 0.01\ \text{c}$$

Advanced LIGO, 2023

$$\Delta X \simeq 0.5 \times 10^{-19}\ \text{м}, \quad \text{distance } L = 4\ \text{km}, \quad \text{for time } \tau \simeq 0.01\ \text{c (!)}$$

International G.-W. Observatory Network (IGWN)

Advanced LIGO A+

A+ status for O4 (March 2023)

- ✓ ***O4 A+ systems delivered, installed, tested; commissioning in progress***
  - ✓ Improved squeezed light injection
    - ✓ OPO Upgrade
    - ✓ High-T Faraday isolators
    - ✓ Adaptive mode matching
  - ➤ *Up to 5.4 dB squeezing achieved! (LLO, 10 Feb 2023)*
  - ✓ Frequency-Dependent Squeezing (FDS)
    - ✓ Squeezed light injection, Civil + Vacuum
    - ✓ Filter cavity optics, seismic isolation, suspensions, baffles, sensing, control/data system
  - ➤ *Quantum noise suppressed throughout signal band!*
  - ✓ Civil construction
  - ✓ Vacuum system expansion

(excerpted from M. Zucker NSF talk)

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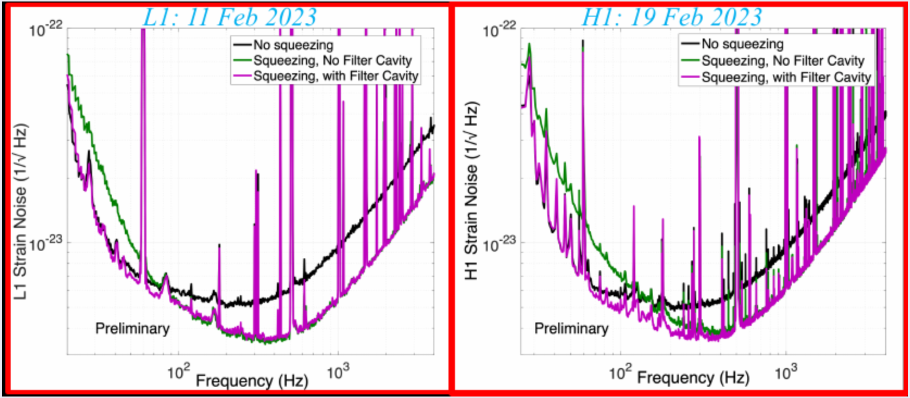
Now O4 operates.

Current sensitivity of Advanced LIGO A+

Sensitivity and squeezing improvement

Frequency Dependent Squeezing Achieved in Lousiana and Hanford Interferometers

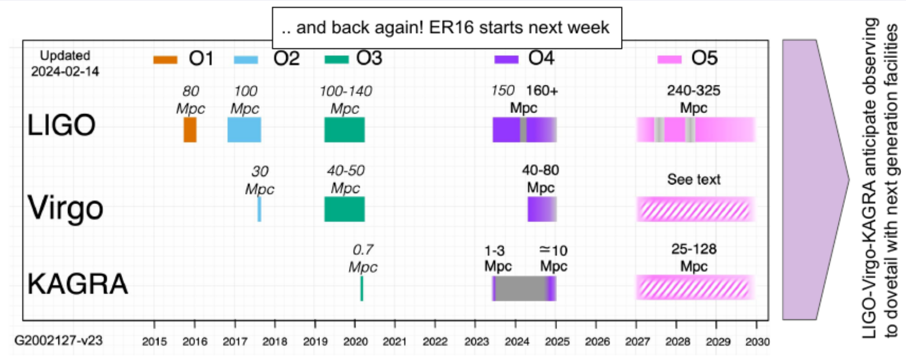


Squeezing is about 5 dB. Filter cavity (300 m) — frequency squeezing.

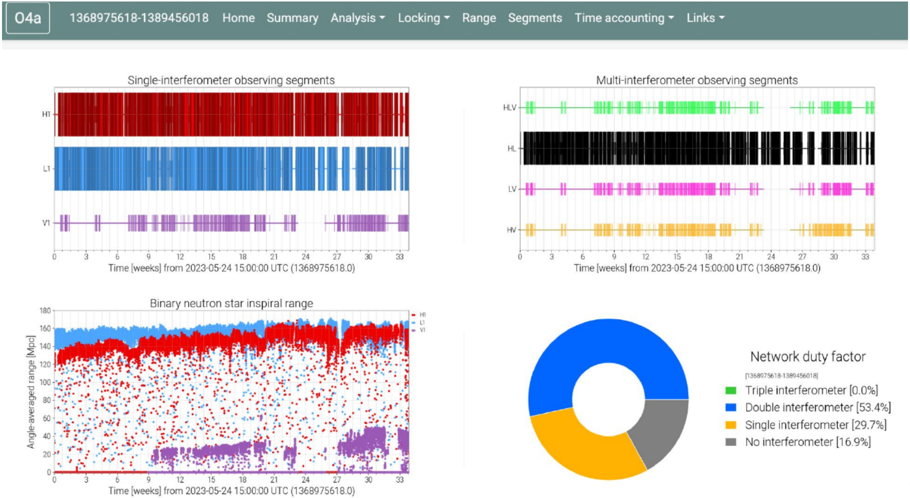
Advanced LIGO A+: schedule for the period 2024 – 2028

Past and future Observation Runs

Expect to be observing   50% of the time



O4a Summary


O4a
1368975618-1389456018 Home Summary Analysis Locking Range Segments Time accounting Links
Single-interferometer observing segments
H1
L1
V1
Time [weeks] from 2023-05-24 15:00:00 UTC (1368975618.0)
Multi-interferometer observing segments
HLV
HL
LV
HV
Time [weeks] from 2023-05-24 15:00:00 UTC (1368975618.0)
Binary neutron star inspiral range
Angle-averaged range [Mpc]
Time [weeks] from 2023-05-24 15:00:00 UTC (1368975618.0)
Network duty factor
[1368975618-1389456018]
Triple interferometer [0.0%]
Double interferometer [53.4%]
Single interferometer [29.7%]
No interferometer [16.9%]

O4a Summary (cont.)

O4a (more than 1/2 year) — 81 significant candidates

Significant alerts:

- False alarm rate less than ~1/month
- ~ 1 BBH per 3 days **actual**
- ~ 1 BNS per 3-6 months **predicted**

Other alerts:

- Not significant and false alarm rate less than few per day.

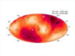
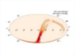
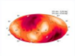
O4 Significant Detection Candidates: **81** (92 Total - 11 Retracted)

O4 Low Significance Detection Candidates: **1610** (Total)

Show All Public Events

Page 1 of 7. next last »

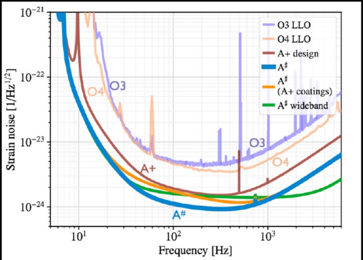
SORT: EVENT ID (A-Z)

Event ID	Possible Source (Probability)	Significant	UTC	GCN	Location	FAR
S240109a	BBH (99%)	Yes	Jan. 9, 2024 05:04:31 UTC	GCN Circular Query Notices | VOE		1 per 4.3136 years
S240107b	BBH (97%), Terrestrial (3%)	Yes	Jan. 7, 2024 01:32:15 UTC	GCN Circular Query Notices | VOE		1.8411 per year
S240104bl	BBH (>99%)	Yes	Jan. 4, 2024 16:49:32 UTC	GCN Circular Query Notices | VOE		1 per 8.9137e+08 years

BBH — 81 events. BNS — 0 events.

A+ Status and Plans

- The LSC “Post-O5” report recommends pursuing a series of upgrades for the LIGO detectors collectively known as A#



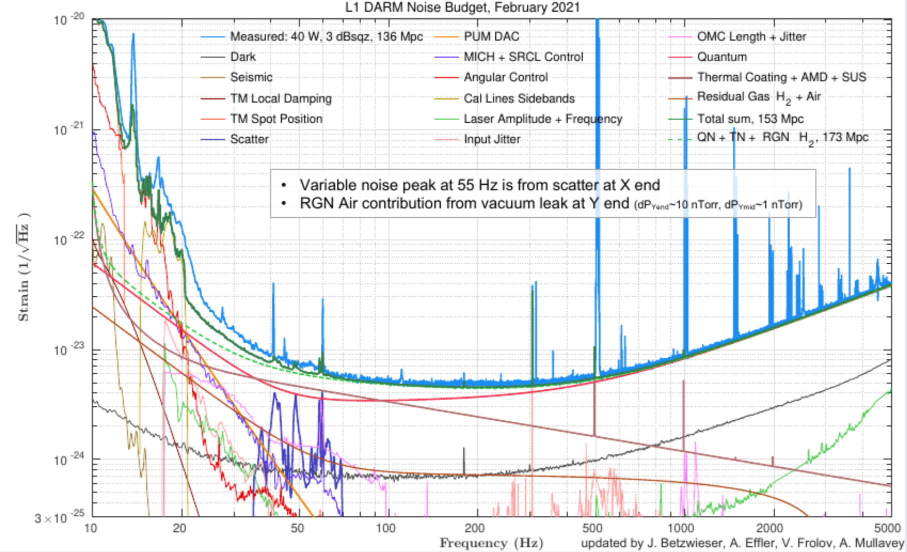
Design parameter	A+	A♯	CE
Arm length	4 km	4 km	20 km, 40 km
Arm power	750 kW	1.5 MW	1.5 MW
Squeezing level	6 dB	10 dB	10 dB
Mass of test-mass	40 kg	100 kg	320 kg
Test-mass coatings	A+	A+/2	A+
Suspension length	1.6 m	1.6 m	4 m
Newtonian suppression	0 db	6 db	20 db

- We are aiming to have a mature conceptual design and costing to be able to submit a proposal by mid-2025 frame.

See Monday afternoon SUS/SEI session talk by Edgard Bonilla

Noise budget: L1GO Louisiana, 2021

Sensitivity is close to SQL. What is it?



Coherent state of quantum oscillator

Zero state $|0\rangle$

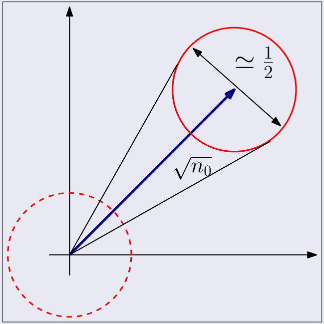
$$\sqrt{\langle \Delta x^2\rangle} = \sqrt{\frac{\hbar}{2m\omega}},\quad \sqrt{\langle \Delta p^2\rangle} = \sqrt{\frac{\hbar m\omega}{2}} \quad \Rightarrow \quad \langle \mathcal{E}\rangle = \frac{\hbar\omega}{2}$$

Cohherent state $\alpha\rangle$

α — mean amplitude,
$n_0 = \alpha^2$ — mean qaunta number

$$\langle \mathcal{E}\rangle = \hbar\omega_0\alpha^2 + \frac{\hbar\omega}{2},$$

$$\Delta n = \sqrt{n_0},\quad \Delta\phi = \frac{1}{2\sqrt{n_0}}$$



Standard Quantum Limit (SQL)

Coherent state of light

Uncertainty of phase ϕ и quanta number n in laser pulse (N — mean quanta number):

$$\Delta n = \sqrt{N}, \quad \Delta\phi = \frac{1}{2\sqrt{N}}$$

SQL — V.B. Braginsky idea (1968)

Reason of SQL[a]:
continious measurement and Heisenberg principle:

$$\Delta X_{\text{meas}}\, \Delta P_{\text{BA}} \geq \hbar/2\,.$$

[a] V.B. Braginsky, Sov. Phys. JETP, **26**, 831, 1968.
V.B. Braginsky and F.Ya. Khalili, Quantum measurement, 1992.

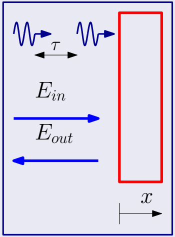
Simple optic meter

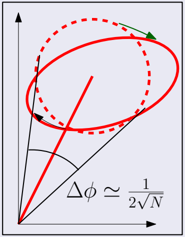
Measurement error — phase fluctuations

$$2k\delta X_{\text{meas}} = \Delta\phi, \qquad k = \frac{\omega_0}{c}$$

$$\Delta\phi = \frac{1}{2\sqrt{N}}$$

$$\Rightarrow \quad \delta X_{\text{meas}} = \frac{1}{4k\sqrt{N}}.$$





Back action

Back action: amplitude fluctuations (fluctuations of light pressure force)

$$\delta P_{\text{BA}} = 2\hbar k\sqrt{N}\,, \quad \delta X_{\text{BA}} = \frac{\delta P_{\text{BA}}\tau}{m},$$

SQL

Total error of coordinate

$$\Delta x_{\text{total}} = \sqrt{\delta X_{\text{meas}}^2 + \delta X_{\text{BA}}^2} = \sqrt{\left[\frac{1}{4k\sqrt{N}}\right]^2 + \left[\frac{2\hbar k\sqrt{N}\cdot\tau}{m}\right]^2}$$

$$\Delta x_{\text{total}}\big|_{\text{min}} = \Delta X_{SQL} = \sqrt{\frac{\hbar\tau}{m}}, \quad N_{\text{opt}} = \frac{m}{8\hbar k^2\tau}$$

How to surpass SQL

Quantum Non-Demolition Measurement (QND)

To measure integral of movement — back action cancellation[a].

For example, invariant for free mass — speed (momentum).
But it should be *direct* measurement — difficulty.

[a] V.B. Braginsky and F.Ya. Khalili, Quantum measurement, Cambridge Univ. Press, 1992

Not QND measurement

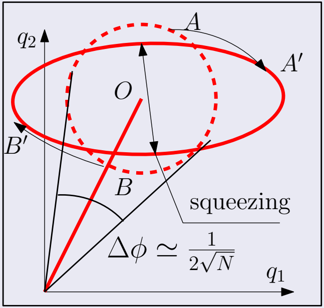
- Quantum variational measurement
- Squeezed input
- Optical rigidity

Realization — more easy.

Quantum variational measurement

What will be at $N > N_{opt}$?

SQL — at $N = N_{opt}$.
At $N > N_{opt}$ quasi-classically:
LP force is larger in point A, it transforms to A'
In B LP force is smaller, it it transforms to B'
Phase disturbance.
It means — *squeezing*
$\Rightarrow$ we have to measure squeezed quadrature
SQL can be surpassed[a]



[a] S.P. Vyatchanin, ZhETF, **109**, 1873, 1996

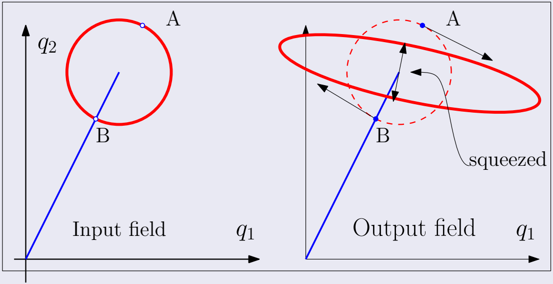
Quantum variational measurement (cont.)

Example: Squeezing in nonlinear media

Refraction index n depends on intensity P:

$$n = n_0(1 - \alpha P) \qquad (2)$$

Input field is in coherent state,
output one — squeezed.



Quasi-classical explanation:
point A moves slightly faster, point B — slower.

Idea of squeezed input

Phase diagrams

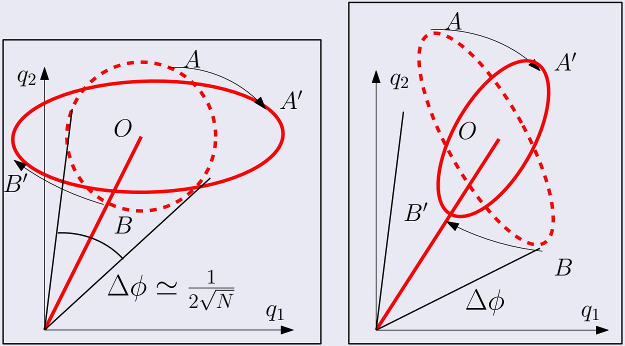


Figure: *Left:* input wave is in coherent state (dashed), phase of output wave is disturbed due to LP pressure ($A \to A'$, $B \to B/$). *Right:* input wave is in squeezed state (dashed), initial squeezing is chosen in optimal way so that after reflection — phase squeezing.

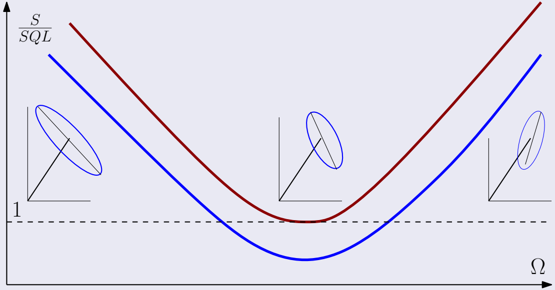
Squeezing should depends on spectral frequency

Recall

$$q_\phi(\Omega) = \beta \left\{ d_\phi(\Omega) - \mathcal{K}\, d_a \right\} - \sqrt{2\beta\mathcal{K}}\, \frac{F_s(\Omega)}{\sqrt{2\hbar m \Omega^2}}\,,$$

$$q_a(\Omega) = \beta\, d_a(\Omega), \quad \boxed{\mathcal{K} \equiv \frac{2\hbar\kappa_0\omega_0^2 A^2}{mL^2\Omega^2 \left|\frac{\kappa_0}{2} - i\Omega\right|^2}, \quad \beta \equiv \frac{\frac{\kappa_0}{2} + i\Omega}{\frac{\kappa_0}{2} - i\Omega}}\,.$$

Power parameter $\mathcal{K}$ defines the value of ponderomotive squeezing. It depends on frequency ($\mathcal{K} \sim 1/\Omega^2$).



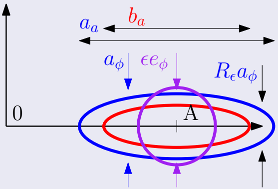
Frequency dependent squeezing

Experimental difficulties

- Relatively easy to obtain squeezing on high frequencies in range 100 kHz and larger. For GW detectors we need squeezing in band 10 Hz – 1 kHz.
- Frequency dependent squeezing on low frequencies — difficult task.
- Loss factor: squeezing is very vulnerable to optical losses ("problem of waist").

$$b_a = R_\epsilon\, a_a + \epsilon\, e_a = R_\epsilon\, e^r a_{a\,\mathrm{vac}} + \epsilon\, e_a,$$

$$b_\phi = R_\epsilon\, a_\phi + \epsilon\, e_\phi = R_\epsilon\, e^{-r} a_{\phi\,\mathrm{vac}} + \epsilon\, e_\phi,$$



Plan and reality

A+ LIGO plan: to inject 12 dB squeezing.
Now — 5.4 dB frequency dependent squeezing is realized (!)
5 dB $\Rightarrow$ $\Delta q_{vac}/\Delta q_{sq} \simeq 1.8$, 10 dB $\Rightarrow$ $\Delta q_{vac}/\Delta q_{sq} \simeq 3.1$

Conclusion

- Accuracy of GW detectors are about 160 Mp.
- During O4a about 81 BBH (binary black holes) coalescences are detected.
- No BNS (binary neutron stars) coalescences are detected.
- Accuracy of GW detectors are close to SQL
  $\Rightarrow$ surpassing SQL is an actual problem.
- Practical methods to overcome SQL for free mass
  - Quantum variational measurement
  - Squeezing input

Long Live Gravitational Waves!
Long Live Quantum measurements!

Thank you for attention!