

# Модифицированный бариогенезис и космические лучи сверхвысоких энергий

Елена Арбузова

Государственный Университет «Дубна»  
Новосибирский Государственный Университет  
*по работам с А.Д. Долговым, К. Дуттой, Р. Рангараджаном,  
А.А. Никитенко*

Поддержано грантом РФФ № 22-12-00103

Научная сессия секции ядерной физики ОФН РАН

1 – 5 апреля 2024, ОИЯИ, г. Дубна

# Baryogenesis

## Dominance of matter over antimatter in the universe

- The local universe is clearly matter dominated.
- On the other hand, matter and antimatter seem to have similar properties  $\implies$  we could expect a matter-antimatter symmetric universe.
- A satisfactory model of our universe should be able to explain the origin of the matter-antimatter asymmetry.

The term **baryogenesis** is used to indicate the **generation of the asymmetry** between baryons and antibaryons.

## Sakharov Principles (1967):

- 1 Non-conservation of baryonic number
- 2 Breaking of symmetry between particles and antiparticles
- 3 Deviation from thermal equilibrium (Th.Eq.)

SBG and GBG do not demand an explicit C and CP violation and can proceed in Th.Eq.

# Spontaneous Baryogenesis (SBG)

Cosmological baryon asymmetry can be created by SBG in thermal equilibrium:

- A. Cohen, D. Kaplan, Phys. Lett. B 199, 251 (1987); Nucl.Phys. B308 (1988) 913. A.Cohen, D.Kaplan, A. Nelson, Phys.Lett. B263 (1991) 86-92

Reviews:

- A.D.Dolgov, Phys. Repts 222 (1992) No. 6; V.A. Rubakov, M.E. Shaposhnikov, Usp. Fiz. Nauk, 166 (1996) 493; A.D. Dolgov, Surveys in High Energy Physics, 13 (1998) 83.

«spontaneous»  $\implies$  spontaneous breaking of underlying symmetry of the theory

- **Unbroken phase:** the theory is invariant with respect to the global  $U(1)$ -symmetry, which ensures conservation of total baryonic number.
- **Spontaneous symmetry breaking:** the Lagrangian density acquires the term

$$\mathcal{L}_{SB} = (\partial_\mu \theta) J_B^\mu$$

$\theta$  is the (pseudo) Goldstone field and  $J_B^\mu$  is the baryonic current of matter fields.

$$\text{SBG: } \mathcal{L}_{SB} = (\partial_\mu \theta) J_B^\mu$$

Spatially homogeneous field  $\theta = \theta(t)$ :

$$\mathcal{L}_{SB} = \dot{\theta} n_B, \quad n_B \equiv J_B^0$$

- $n_B$  is the baryonic number density, so it is tempting to identify  $\dot{\theta}$  with the chemical potential,  $\mu_B$ , of the corresponding system.

The identification of  $\dot{\theta}$  with chemical potential is questionable. It depends upon the representation chosen for the fermionic fields and is heavily based on the assumption  $\dot{\theta} \approx \text{const}$ :

- A.D. Dolgov, K. Freese, Phys.Rev. D **51** (1995) 2693-2702; A.D. Dolgov, K. Freese, R. Rangarajan, M. Srednicki, Phys.Rev. D **56** (1997) 6155
- E.V. Arbuzova, A.D. Dolgov, V.A. Novikov, Phys. Rev. D **94** (2016) 123501 – the assumption  $\dot{\theta} \approx \text{const}$  is relaxed.

Still the scenario is operative and presents a beautiful possibility to create an excess of particles over antiparticles in the Universe.

# Gravitational Baryogenesis (GBG)

The scenario of SBG was modified by the introduction of the coupling of the baryonic current to the derivative of the curvature scalar  $R$ :

$$\mathcal{L}_{GBG} = \frac{1}{M^2} (\partial_\mu R) J_B^\mu$$

- $M$  is a constant parameter with the dimension of mass.

GBG mechanism can successfully explain the magnitude of the cosmological baryon asymmetry of the universe.

The addition of the curvature dependent term to the Hilbert-Einstein Lagrangian of GR leads to higher order gravitational equations of motion which are strongly unstable with respect to small perturbations.

- EA, A.D. Dolgov, *Intrinsic problems of the gravitational baryogenesis*, Phys.Lett. B769 (2017) 171-175, arXiv:1612.06206. *Instability of gravitational baryogenesis with fermions*, JCAP 1706 (2017) no.06, 001, arXiv:1702.07477.

## GBG with scalars

The action of the scalar model:

$$S = - \int d^4x \sqrt{-g} \left[ \frac{m_{Pl}^2}{16\pi} R + \frac{1}{M^2} (\partial_\mu R) J^\mu - g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi^* + U(\phi, \phi^*) \right] + S_m$$

- where  $m_{Pl} = 1.22 \cdot 10^{19}$  GeV is the Planck mass,  $S_m$  is the matter action.

The baryonic number is carried by scalar field  $\phi$  with potential  $U(\phi, \phi^*)$ .

If the potential  $U(\phi)$  is not invariant w.r.t. the  $U(1)$ -rotation  $\phi \rightarrow e^{i\beta} \phi \implies$  the baryonic current defined in the usual way is not conserved.

$$J_\mu = iq(\phi^* \partial_\mu \phi - \phi \partial_\mu \phi^*)$$

- Here  $q$  is the baryonic number of  $\phi$

The corresponding equation of motion for the curvature scalar:

$$\frac{m_{Pl}^2}{16\pi} R + \frac{1}{M^2} [(R + 3D^2) D_\alpha J^\alpha + J^\alpha D_\alpha R] - D_\alpha \phi D^\alpha \phi^* + 2U(\phi) = -\frac{1}{2} T_\mu^\mu$$

- $D_\mu$  is the covariant derivative,  $T_\mu^\mu$  is the trace of EM tensor of matter

EoM in FLRW background:  $ds^2 = dt^2 - a^2(t)dr^2$ ,  $H = \dot{a}/a$

In the homogeneous case the equation for the curvature scalar:

$$\frac{m_{Pl}^2}{16\pi} R + \frac{1}{M^2} \left[ (R + 3\partial_t^2 + 9H\partial_t) D_\alpha J^\alpha + \dot{R} J^0 \right] = -\frac{T^{(tot)}}{2}$$

- $T^{(tot)}$  is the trace of the energy-momentum tensor of matter including contribution from the  $\phi$ -field.

The covariant divergence of the baryonic current in homogeneous case:

$$D_\alpha J^\alpha = \frac{2q^2}{M^2} \left[ \dot{R} (\phi^* \dot{\phi} + \phi \dot{\phi}^*) + (\ddot{R} + 3H\dot{R}) \phi^* \phi \right] + iq \left( \phi \frac{\partial U}{\partial \phi} - \phi^* \frac{\partial U}{\partial \phi^*} \right)$$

The expectation values of the products of the quantum operators  $\phi$ ,  $\phi^*$ , and their derivatives after the thermal averaging:

$$\langle \phi^* \phi \rangle = \frac{T^2}{12}, \quad \langle \phi^* \dot{\phi} + \dot{\phi}^* \phi \rangle = 0$$

- $T$  is the plasma temperature

# Exponential instability of GBG with scalars

Equation of motion for the classical field  $R$  in the cosmological plasma:

$$\frac{m_{Pl}^2}{16\pi} R + \frac{q^2}{6M^4} (R + 3\partial_t^2 + 9H\partial_t) \left[ \left( \ddot{R} + 3H\dot{R} \right) T^2 \right] + \frac{1}{M^2} \dot{R} \langle J^0 \rangle = -\frac{T^{(tot)}}{2}$$

- $\langle J^0 \rangle$  is the thermal average value of the baryonic number density of  $\phi$ .
- This term can be neglected, since it is small initially and subdominant later.

Keeping only the linear in  $R$  terms we obtain the **linear fourth order equation**:

$$\frac{d^4 R}{dt^4} + \mu^4 R = -\frac{1}{2} T^{(tot)}, \quad \mu^4 = \frac{m_{Pl}^2 M^4}{8\pi q^2 T^2}$$

The homogeneous part of this equation has exponential solutions:

$$R \sim e^{\lambda t}, \quad \lambda = |\mu| e^{i\pi/4 + i\pi n/2}, \quad n = 0, 1, 2, 3$$

- There are two solutions with positive real parts of  $\lambda$ .

Curvature scalar is exponentially unstable w.r.t. small perturbations, so  $R$  should rise exponentially fast with time and quickly oscillate around this rising function.



# GBG with fermions

We start from the action in the form:

$$S = - \int d^4x \sqrt{-g} \left[ \frac{m_{Pl}^2}{16\pi} R - \mathcal{L}[Q, L] \right] + S_{\text{matt}}$$

with

$$\begin{aligned} \mathcal{L}[Q, L] &= \frac{i}{2} (\bar{Q} \gamma^\mu \nabla_\mu Q - \nabla_\mu \bar{Q} \gamma^\mu Q) - m_Q \bar{Q} Q \\ &+ \frac{i}{2} (\bar{L} \gamma^\mu \nabla_\mu L - \nabla_\mu \bar{L} \gamma^\mu L) - m_L \bar{L} L \\ &+ \frac{g}{m_X^2} [(\bar{Q} Q^c)(\bar{Q} L) + (\bar{Q}^c Q)(\bar{L} Q)] + \frac{d}{M^2} (\partial_\mu R) J^\mu + \mathcal{L}_{\text{matt}} \end{aligned}$$

- $Q$  is the quark (or quark-like) field with non-zero baryonic number  $B_Q$ ,  
 $L$  is another fermionic field (lepton)
- $\nabla_\mu$  is the covariant derivative of Dirac fermion in tetrad formalism
- $J^\mu = B_Q \bar{Q} \gamma^\mu Q$  is the quark current with  $\gamma^\mu$  being the curved space gamma-matrices;  $d = \pm 1$  is dimensionless coupling constant.
- The four-fermion interaction between quarks and leptons is introduced to ensure the necessary non-conservation of the baryonic number

## Gravitational EoM for curvature scalar in fermionic case

Taking trace of gravitational EoM we obtain:

$$\begin{aligned} -\frac{m_{Pl}^2}{8\pi} R &= m_Q \bar{Q}Q + m_L \bar{L}L + \frac{2g}{m_X^2} [(\bar{Q} Q^c)(\bar{Q}L) + (\bar{Q}^c Q)(\bar{L}Q)] \\ &- \frac{2d}{M^2} (R + 3D^2) D_\alpha J^\alpha + T_{other} \end{aligned}$$

- $T_{other}$  is the trace of the energy momentum tensor of all other fields.
- At relativistic stage we can take  $T_{other} = 0$ .

To calculate the current divergence, we use kinetic equation, which leads to an explicit dependence of  $D_\alpha J^\alpha$  on  $\dot{R}$ , if the current is not conserved.

As a result we obtain high (fourth) order equation for  $R$ .

We study solutions in homogeneous and isotropic FRW background:

$$ds^2 = dt^2 - a^2(t) dr^2, \quad D_\alpha J^\alpha = (\partial_t + 3H) J^t \equiv (\partial_t + 3H) n_B$$

## Curvature Instability

The contribution of thermal matter into EoM for  $R$  can be neglected

$$\frac{m_{Pl}^2}{8\pi} R = \frac{2d}{M^2} (R + 3D^2) (\partial_t + 3H) n_B$$

From the kinetic equation we find the baryonic number density:

$$n_B \sim \frac{9d}{10} \frac{g_s B_Q \dot{R}}{M^2 T}$$

Neglecting the  $H$ -factor in comparison with time derivatives of  $R$ , we arrive to:

$$\frac{d^4 R}{dt^4} + \lambda^4 R = 0, \quad \lambda^4 = \frac{5m_{Pl}^2 M^4}{36\pi g_s B_Q^2 T^2}$$

- $g_s$  is the number of quark spin states.

This equation has extremely unstable solution with instability time by far shorter than the cosmological time. This instability would lead to an explosive rise of  $R$

# Stabilization of GBG in $R^2$ -modified gravity

- EA, A.D. Dolgov, K. Dutta, and R. Rangarajan, *Gravitational Baryogenesis: Problems and Possible Resolution*, Symmetry 15 (2023) 2, 404.

Possible stabilization mechanism might be achieved in  $R^2$ -modified gravity:

$$S_{\text{Grav}} = -\frac{m_{\text{Pl}}^2}{16\pi} \int d^4x \sqrt{-g} \left( R - \frac{R^2}{6M_R^2} \right)$$

$R^2$ -term:

- In the early universe generates inflation (Starobinsky) and density perturbations.
- leads to excitation of the scalar degree of freedom: scalaron with the mass  $M_R$ .
- Amplitude of the observed density perturbations demands:  $M_R = 3 \cdot 10^{13} \text{ GeV}$ .

Bosonic case: baryonic number is carried by a complex scalar field  $\phi$ :

$$S_{\text{tot}}[\phi] = - \int d^4x \sqrt{-g} \left[ \frac{m_{\text{Pl}}^2}{16\pi} \left( R - \frac{R^2}{6M_R^2} \right) + \frac{1}{M^2} (\partial_\mu R) J^\mu_{(\phi)} \right] - \int d^4x \sqrt{-g} [g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi^* - U(\phi, \phi^*)] + S_{\text{matt}}$$

## Stabilization: Bosonic Case

The equation for the curvature evolution in spatially flat FLRW-metric:

$$\frac{m_{Pl}^2}{16\pi} \left[ R + \frac{1}{M_R^2} (\partial_t^2 + 3H\partial_t) R \right] + \frac{1}{M^2} \left[ (R + 3\partial_t^2 + 9H\partial_t) D_\alpha J_{(\phi)}^\alpha + \dot{R} J_{(\phi)}^0 \right] + 2U(\phi) - (D_\alpha \phi)(D^\alpha \phi^*) = -\frac{T_\mu^\mu(\phi)}{2}$$

With the divergence of the baryonic current:

$$D_\alpha J_{(\phi)}^\alpha = \frac{2q^2}{M^2} \left[ \dot{R} (\phi^* \dot{\phi} + \phi \dot{\phi}^*) + (\ddot{R} + 3H\dot{R}) \phi^* \phi \right] + iq \left( \phi \frac{\partial U}{\partial \phi} - \phi^* \frac{\partial U}{\partial \phi^*} \right)$$

we obtain the 4th order differential equation:

$$\frac{m_{Pl}^2}{16\pi} \left( R + \frac{1}{M_R^2} D^2 R \right) + \frac{q^2}{6M^4} (R + 3\partial_t^2 + 9H\partial_t) \left[ (\ddot{R} + 3H\dot{R}) T^2 \right] = -\frac{T_\mu^\mu(\phi)}{2}$$

Keeping only the dominant terms we simplify the above equation to:

$$\frac{d^4 R}{dt^4} + \frac{\kappa^4}{M_R^2} \frac{d^2 R}{dt^2} + \kappa^4 R = -\frac{1}{2} T_\mu^\mu(\phi), \quad \kappa^4 = \frac{m_{Pl}^2 M^4}{8\pi q^2 T^2}$$

## Stabilization: Fermionic Case

$$S_{tot}[Q, L] = - \int d^4x \sqrt{-g} \left[ \frac{m_{Pl}^2}{16\pi} \left( R - \frac{R^2}{6M_R^2} \right) + \frac{d}{M^2} (\partial_\mu R) J_Q^\mu - \mathcal{L}[Q, L] \right]$$

The equation for the curvature evolution:

$$\begin{aligned} - \frac{m_{Pl}^2}{8\pi} \left( R + \frac{1}{M_R^2} D^2 R \right) &= m_Q \bar{Q} Q + m_L \bar{L} L + \\ + \frac{2g}{m_X^2} [(\bar{Q} Q^c)(\bar{Q} L) + (\bar{Q}^c Q)(\bar{L} Q)] &- \frac{2d}{M^2} (R + 3D^2) D_\alpha J_Q^\alpha + T_{matt} \end{aligned}$$

- In the early universe, when various species are relativistic  $T_{matt} = 0$ .
- Higher order equation for  $R$  originates after we substitute the current divergence  $D_\alpha J^\alpha$  calculated from kinetic equation in external field  $R$ .

In complete analogy with the previous cases we obtain:

$$(*) \quad \frac{d^4 R}{dt^4} + \frac{\kappa_f^4}{M_R^2} \frac{d^2 R}{dt^2} + \kappa_f^4 R = 0, \quad \kappa_f^4 = \frac{5m_{Pl}^2 M^4}{36\pi g_s B_Q^2 T^2}$$

## Stability condition

The characteristic equation for the solution  $R \sim \exp(\lambda t)$ :

$$\lambda^4 + \frac{\kappa^4}{M_R^2} \lambda^2 + \kappa^4 = 0 \quad \Rightarrow \quad \lambda^2 = -\frac{\kappa^4}{2M_R^2} \pm \kappa^2 \sqrt{\frac{\kappa^4}{4M_R^4} - 1}$$

No instability, if  $\lambda^2 < 0$  and Eq. (\*) has only oscillating solutions.

Stability condition (boson case):

$$\kappa^4 = \frac{m_{Pl}^2 M^4}{8\pi q^2 T^2} > 4M_R^4 \quad \Rightarrow \quad M > 3 \cdot 10^4 \text{ GeV} \left( \frac{q T}{\text{GeV}} \right)^{1/2}$$

The value of  $\lambda$  depends upon the relation between  $\kappa$  and  $M_R$ :

- $\kappa \sim M_R \Rightarrow$  the frequency of oscillations is of the order of  $M_R$ ,  $|\lambda| \sim M_R$ .
- $\kappa \gg M_R \Rightarrow$  2 possible solutions:  $|\lambda| \sim M_R$  and  $|\lambda| \sim M_R(\kappa/M_R)^2 \gg M_R$ .

High frequency oscillations of  $R$  would lead to **efficient gravitational particle production** and, as a result, to damping of the oscillations.

# Production of dark matter particles by oscillating curvature

Heavy DM particles have been created in the model of the Starobinsky inflation:

$$S(R^2) = -\frac{M_{Pl}^2}{16\pi} \int d^4x \sqrt{-g} \left[ R - \frac{R^2}{6M_R^2} \right]$$

The width of the scalaron decay into a pair of fermions with mass  $m_f$ :

$$\Gamma_f = \frac{m_f^2 M_R}{6M_{Pl}^2}$$

- This result is obtained for particles with masses  $m_f \ll M_R$ .
- $X$ -particles created by the scalaron decay into heavier fermions could form DM, if  $m_f \sim 10^7$  GeV,  $M_X \sim 10^6$  GeV (EA, A. Dolgov, R.Singh, *R<sup>2</sup>-cosmology and New Windows for Superheavy Dark Matter*, Symmetry 13 (2021) 5, 877)

We are interested in the case when the scalaron decays create particles with mass about  $10^{20}$  eV, that is the energy of UHECR.

- EA, A.D. Dolgov, A.A. Nikitenko, *Cosmic rays from heavy particle decays*, Physics of Atomic Nuclei, 2024, Vol. 87, No. 1, pp. 49–55, ArXiv: 2305.03313 [hep-ph]



## The problem of the origin of the ultra high energy cosmic rays (UHECR)

Particles with energies close to the Greisen-Zatsepin-Kuzmin (GZK, 1966) limit  $E \gtrsim 10^{20}$  eV: Extremely High Energy Cosmic Rays (EHECR).

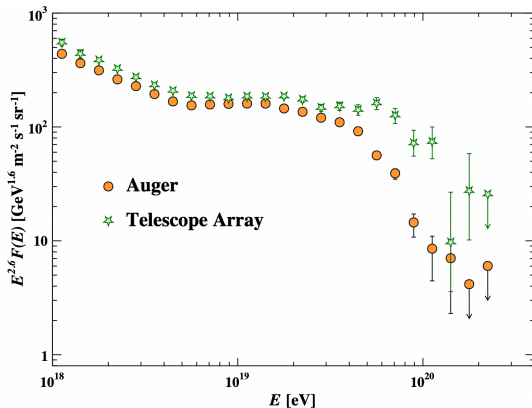


Рис.: The UHECR fluxes measured by Auger and Telescope Array (PDG, 2023)

# Origin of UHECR – ???

No single opinion on the origin of UHECR

- **Traditional approach:** astrophysical sources such as active galactic nuclei, Seyfert galaxies, or possibly hypernovae.
- **Alternative approaches:** cosmic ray emission by topological defects, superheavy particle decays in SUSY due to instanton and wormholes effects, Binary Neutron Star Mergers, ...

Two distinct ranges in energy of UHECR:

- **Cosmic rays with  $E \lesssim 10^{20}$  eV** may be created by stellar processes by acceleration of stellar material in catastrophic processes.
- **Cosmic rays with higher energies,  $E \gtrsim 10^{20}$  eV**, called **EHECR**, cannot be explained by stellar processes.

We suggest new possible source of EHECR at energies  $E \gtrsim 10^{20}$  eV:

- Decays of superheavy dark matter particles via virtual black hole.

## Scaloron decay into extremely heavy DM

The width of the scalaron decay into superheavy fermions with mass  $M_F \sim M_R/2$ :

$$\Gamma_F = \frac{M_F^2 M_R}{6M_{Pl}^2} \sqrt{1 - \frac{4M_F^2}{M_R^2}}$$

- The phase space factor  $(1 - 4M_F^2/M_R^2)^{1/2}$  makes it possible to arrange the density of presumably DM particles  $F$  equal to the observed density of DM.

However, with the canonical energy scale of gravitational interaction with  $M_{Pl} = 1.22 \cdot 10^{19}$  GeV, the life-time of such DM-particles turns out to be too long to allow for any observable consequences of their decays.

A possible way out could be opened by diminishing the fundamental gravity scale at small distances down to a lower value  $M_* < M_{Pl}$ . This could lead to a considerable increase of decay probability of DM-particles.

# Decays through virtual Black Holes

- Usually dark matter particles are supposed to be absolutely stable.
- **Zeldovich mechanism (1976)**: decay of any presumably stable particles is possible through creation of virtual black holes.
- **The rate of the proton decay calculated in the canonical gravity**, with the energy scale equal to  $M_{Pl}$ , **is extremely tiny** and the corresponding life-time is by far longer than the universe age.

However, **the smaller scale of gravity** and **huge mass of DM particles** both lead to a **strong amplification of the Zeldovich effect**.

Superheavy DM particles with  $M_X \sim 10^{12}$  GeV may decay through the virtual BH with life-time **only a few orders of magnitude longer** than the universe age.

**Decays of such particles could make essential contribution to the UHECR.**

# Multidimensional Modification of Gravity

**Model:** the observable universe with the SM particles is confined to a 4-dim brane embedded in a  $(4+d)$ -dim bulk, while gravity propagates throughout the bulk.

- N. Arkani-Hamed, S. Dimopoulos, G. Dvali, Phys. Lett. B **429**, 263 (1998);  
I. Antoniadis, N. Arkani-Hamed, S. Dimopoulos, G. Dvali, Phys. Lett. B **436**, 257 (1998).

The Planck mass  $M_{Pl}$  becomes a long-distance 4-dimensional parameter and the relation with the effective gravity scale at small distances,  $M_*$ , is given by:

$$M_{Pl}^2 \sim M_*^{2+d} R_*^d, \quad R_* \sim \frac{1}{M_*} \left( \frac{M_{Pl}}{M_*} \right)^{2/d},$$

- $R_*$  is the size of the extra dimensions.

We choose  $M_* \approx 3 \times 10^{17}$  GeV, so  $R_* \sim 10^{(4/d)}/M_* > 1/M_*$ .

## Heavy proton type dark matter: $X \rightarrow L^+ \bar{q}_* q_*$

The width of the proton decay  $p \rightarrow l^+ \bar{q} q$  via virtual BH:

- C. Bambi, A. D. Dolgov and K. Freese, Nucl. Phys. B **763** (2007), 91-114

$$\Gamma_p = \frac{m_p \alpha^2}{2^{12} \pi^{13}} \left( \ln \frac{M_{Pl}^2}{m_q^2} \right)^2 \left( \frac{\Lambda}{M_{Pl}} \right)^6 \left( \frac{m_p}{M_{Pl}} \right)^{4 + \frac{10}{d+1}} \int_0^{1/2} dx x^2 (1 - 2x)^{1 + \frac{5}{d+1}}$$

Decay  $X \rightarrow L^+ \bar{q}_* q_*$ :  $m_p \Rightarrow M_X \sim 10^{12} \text{ GeV}$ ,  $m_{q_*} \sim M_X$ ,  $M_{Pl} \Rightarrow M_*$ .

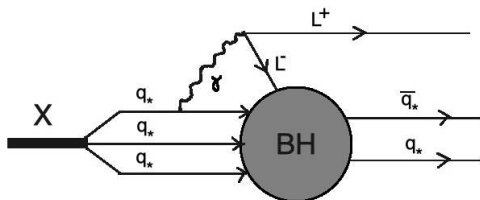


Рис.: Diagram illustrated  $X$ -particle decay into  $L^+ \bar{q}_* q_*$  through virtual BH.

**NB.** We assume, that BH has vacuum quantum numbers to avoid naked singularity.

# Superheavy DM particle decay

The life-time of X-particles:

$$\tau_X \approx 10^{-24} \text{ s} \cdot \frac{2^{11} \pi^{13}}{3\alpha_*^2} \left(\frac{\text{GeV}}{M_X}\right) \left(\frac{M_*}{\Lambda_*}\right)^6 \left(\frac{M_*}{M_X}\right)^{4+10/(d+1)} \left(\ln \frac{M_*}{m_{q_*}}\right)^{-2} I(d)^{-1},$$

where we took  $1/\text{GeV} = (2/3) \times 10^{-24} \text{ s}$  and

$$I(d) = \int_0^{1/2} dx x^2 (1-2x)^{1+\frac{5}{d+1}}, \quad I(7) \approx 0.0057.$$

Now all the parameters, except for  $\Lambda_*$ , are fixed:

- $M_* = 3 \times 10^{17} \text{ GeV}$ ,  $M_X = 10^{12} \text{ GeV}$ ,  $m_{q_*} \sim M_X$ , and  $\alpha_* = 1/50$

The life-time of X-particles can be estimated as:

$$\tau_X \approx 7 \times 10^{12} \text{ years} (10^{15} \text{ GeV}/\Lambda_*)^6 \quad \text{vs} \quad t_U \approx 1.5 \times 10^{10} \text{ years}$$

A slight variation of  $\Lambda_*$  near  $10^{15} \text{ GeV}$  allows to fix the life-time of DM particles in the interesting range. **They would be stable enough to behave as the cosmological DM and their decay could make considerable contribution into cosmic rays at ultra high energies.**

# Conclusions

- The derivative coupling of baryonic current to the curvature scalar in GBG scenarios leads to higher (4th) order equations for gravitational field.
- These equations are unstable with respect to small perturbations of the FRW background and such instability leads to an exponential rise of the curvature.
- For a large range of cosmological temperatures the development of the instability is much faster than the universe expansion rate.
- The problem of stability can be solved by adding to the Hilbert-Einstein action the  $R^2$ -term that leads to oscillations of curvature and to efficient particle production.
- In the model of high dimensional gravity modification may exist superheavy DM particles stable with respect to the conventional particle interactions. However, such DM particles should decay though the virtual BH formation.
- With a proper choice of the parameters the life-time of such quasi-stable particles may be larger than the universe age **only by 3-4 orders** of magnitude.
- This permits X-particles to make an essential contribution to the flux of high energy cosmic rays.
- The considered mechanism may lead to efficient creation of cosmic ray neutrinos of very high energies observed at IceCube and Baikal detectors.