

**Scientific session of the nuclear physics section of  
the Division of Physical Sciences of  
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**Charged kaon femtoscopy with ALICE at the LHC**

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on behalf of the ALICE Collaboration

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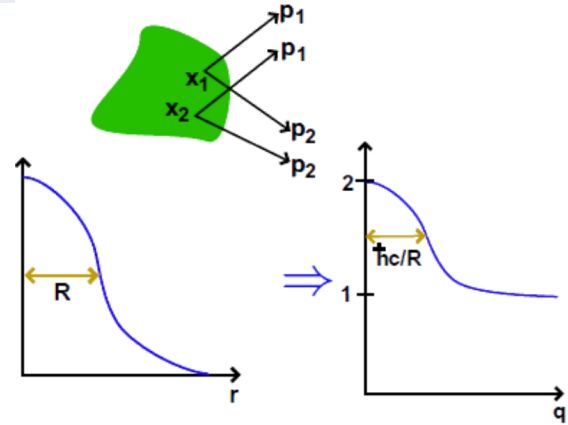
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# Outline

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- Femtoscopy
- ALICE setup
- Kaon and pion in pp 13 TeV
- Kaon in p–Pb 5.02 TeV
- Non-identical kaons in Pb–Pb 2.76 TeV
- Summary

# Femtoscscopy



## Correlation femtoscopy:

Measurement of space–time characteristics  $\mathbf{R}$ ,  $\mathbf{ct}$  of particle production using particle correlations due to the effects of quantum statistics ( QS ) and final–state interactions ( FSI )

## Two-particle correlation function:

theory: 
$$C(q) = \frac{N_2(p_1, p_2)}{N_1(p_1) \cdot N_2(p_1)}, C(\infty) = 1$$

experiment: 
$$C(q) = \frac{S(q)}{B(q)}, q = p_1 - p_2$$
  $S(q)$  – distribution of pair momentum difference from same event,  $B(q)$  – reference distribution built by mixing different events

## Parametrizations used:

1D CF:

$$C(q_{inv}) = 1 + \lambda e^{-R^2 q_{inv}^2}$$

$R$  – Gaussian radius in PRF,

$\lambda$  – correlation strength parameter

3D CF:

$$C(q_{out}, q_{side}, q_{long}) = 1 + \lambda e^{-R_{out}^2 q_{out}^2 - R_{side}^2 q_{side}^2 - R_{long}^2 q_{long}^2}$$

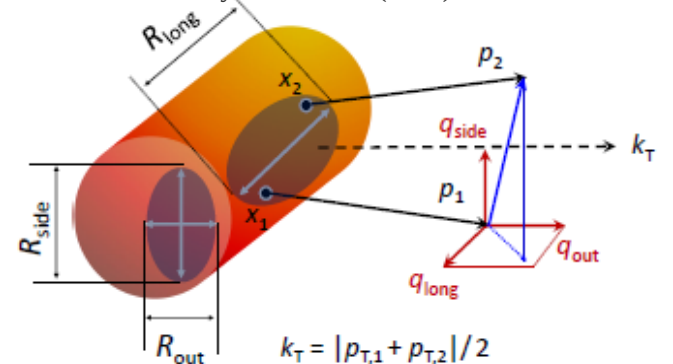
$R$  and  $q$  are in Longitudinally Co-Moving Frame (LCMS)

long  $\parallel$  beam; out  $\parallel$  transverse pair velocity  $\mathbf{v}_T$ ; side normal to out, long

## LCMS decomposition:

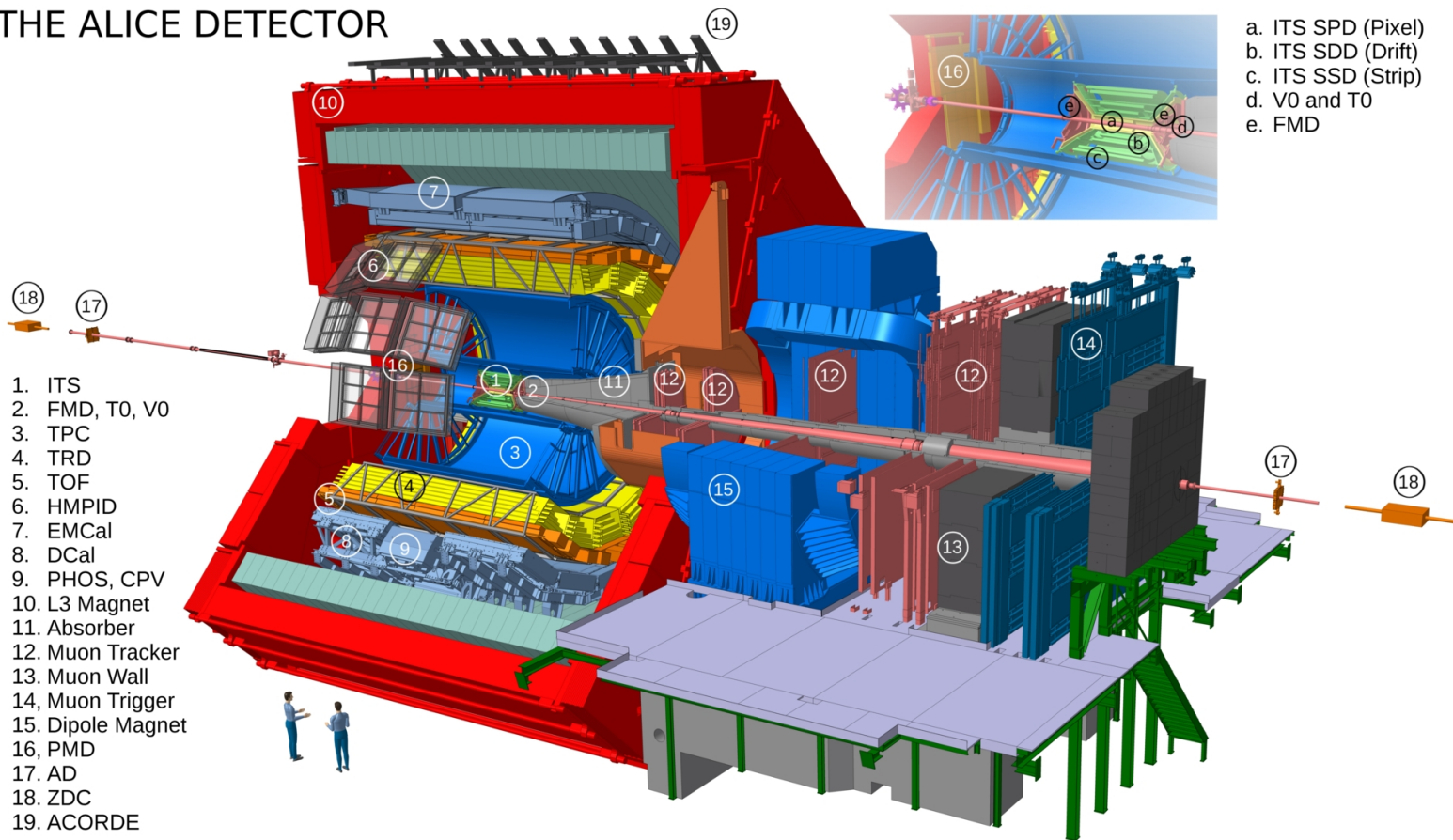
S. Pratt. Phys. Rev. D 33 (1986) 1314

G. Bertsch. Phys. Rev. C 37 (1988) 1896



# ALICE setup

## THE ALICE DETECTOR



### Tracking and vertexing

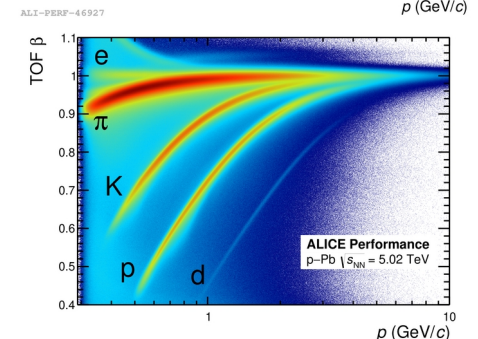
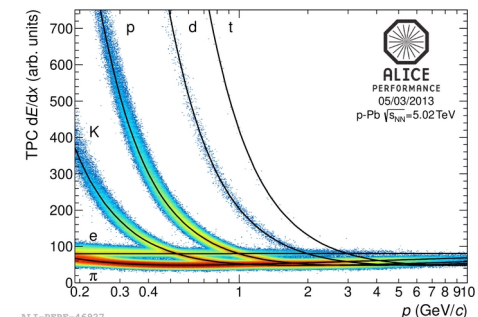
- Time Projection Chamber (TPC) & Inner Tracking System (ITS)

### Particle Identification

- TPC and Time of Flight (TOF)

### Centrality determination

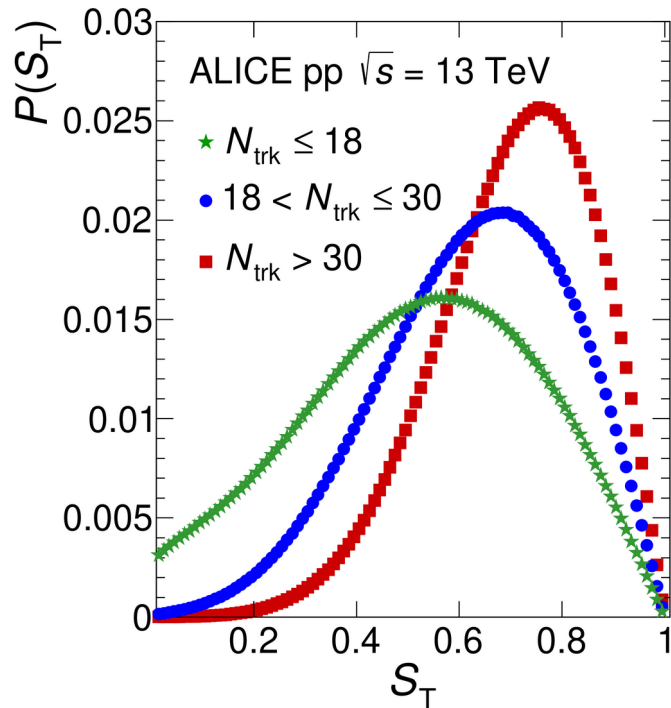
- V0



ALI-PERF-149520

# $\pi$ and $K$ femtoscopy with event-shape selection

Femtoscopic correlations of identical charged pions and kaons in pp collisions at  $\sqrt{s}=13$  TeV with event-shape selection ALICE Collaboration, arXiv:2310.07509



- Select jetty or spherical events

- $S_T$  transverse sphericity

$$S_T = \frac{2 \min(\lambda_1, \lambda_2)}{\lambda_1 + \lambda_2}$$

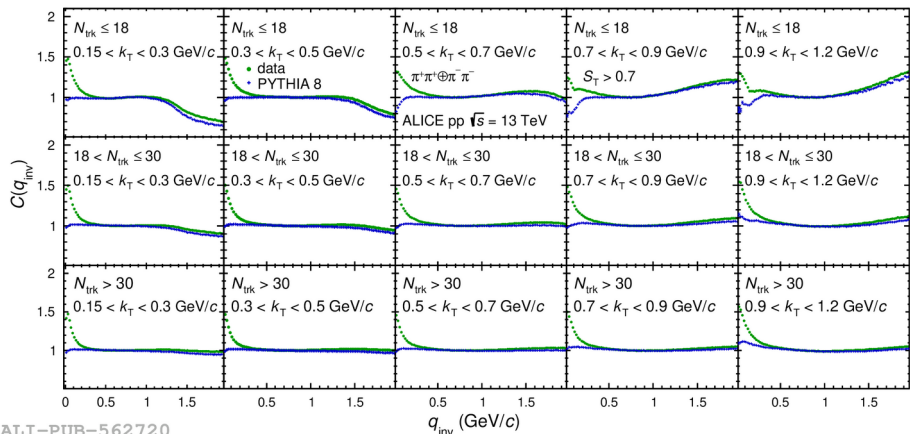
$\lambda_1$  and  $\lambda_2$  are the eigenvalues of the matrix of  $p_T$

$$S_T = \frac{1}{\sum_i p_T^i} \sum_i \frac{1}{p_T^i} \begin{pmatrix} (p_x^i)^2 & p_x^i p_y^i \\ p_x^i p_y^i & (p_y^i)^2 \end{pmatrix}$$

- $S_T \rightarrow 0$  : a strongly elongated ellipse
- $S_T \rightarrow 1$  : an isotropic source

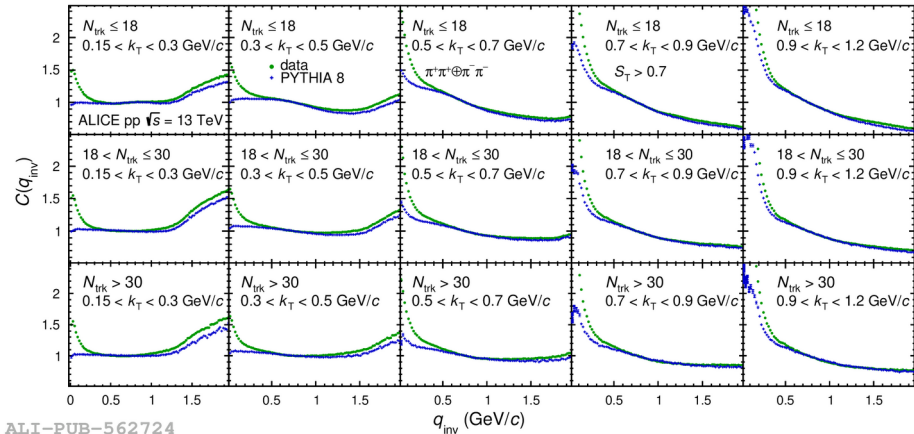
# $\pi$ and K correlation function

## Spherical events



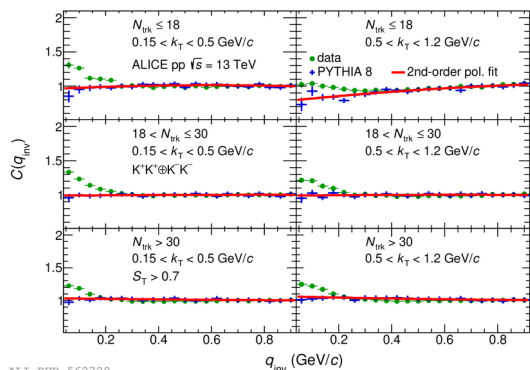
ALI-PUB-562720

## Jetty events



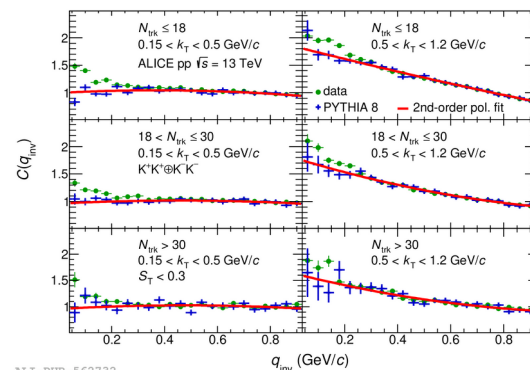
ALI-PUB-562724

$\pi\pi$



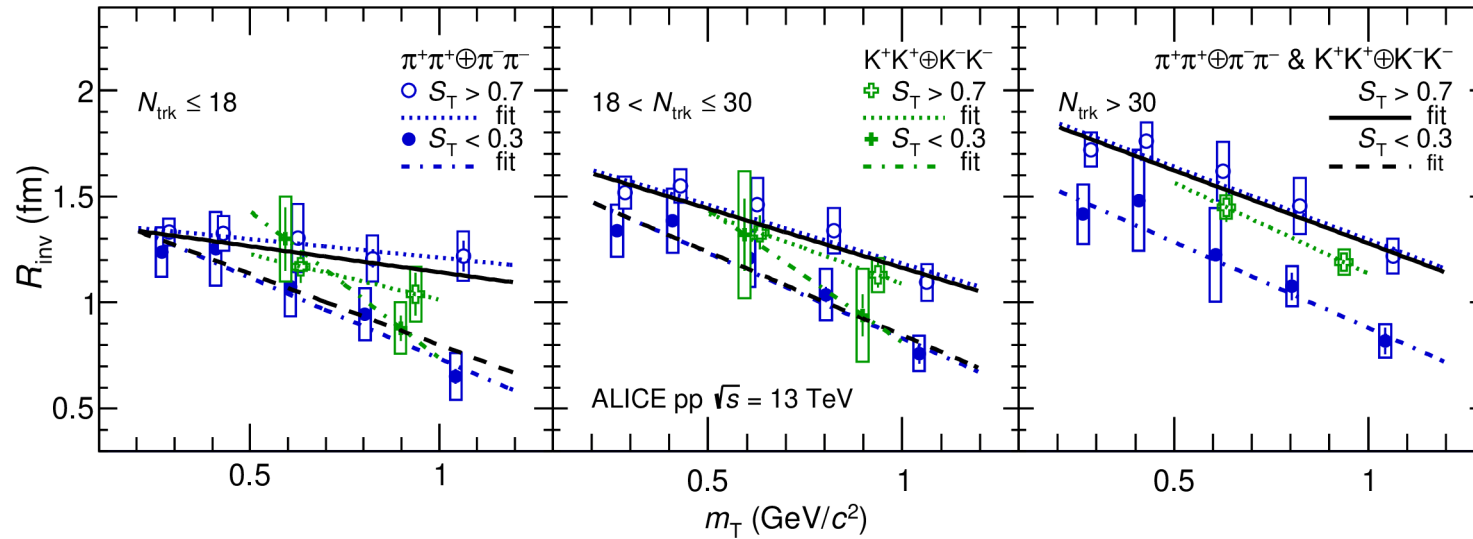
ALI-PUB-562728

$KK$



ALI-PUB-562732

# $\pi$ and $K$ spherical and jetty radii

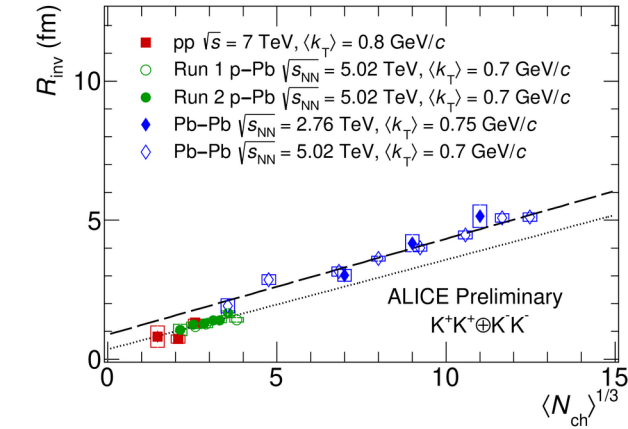
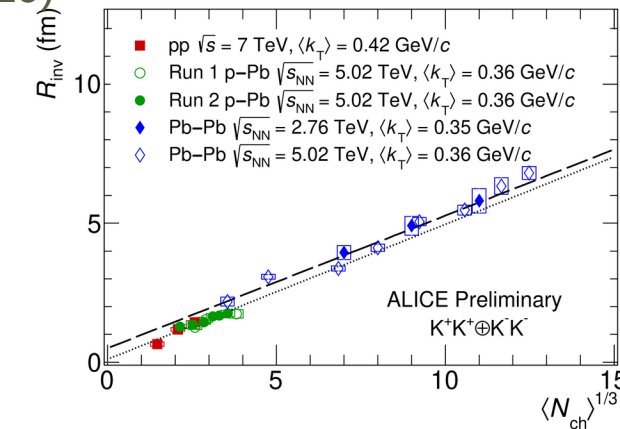
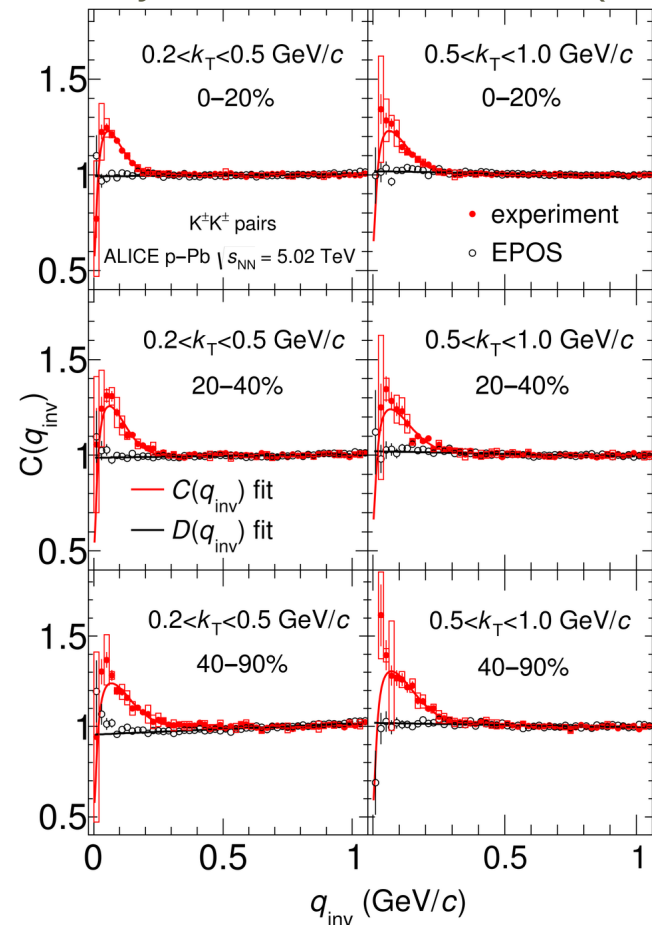


ALI-PUB-562752

- $\pi$  radii extracted for spherical events  $>$  those for jet-like events
- Both  $\pi$  and  $K$   $R_{inv}$  demonstrate a decreasing trend with increasing  $m_T$
- Spherical and jetty events  $m_T$  dependence is different

# p-Pb $\sqrt{s_{NN}}=5.02$ TeV: 1D KK results

Phys. Rev. C 100, 024002 (2019)



- E.g. of 1D CF fit by Bowler-Sinyukov (B-S) equation:

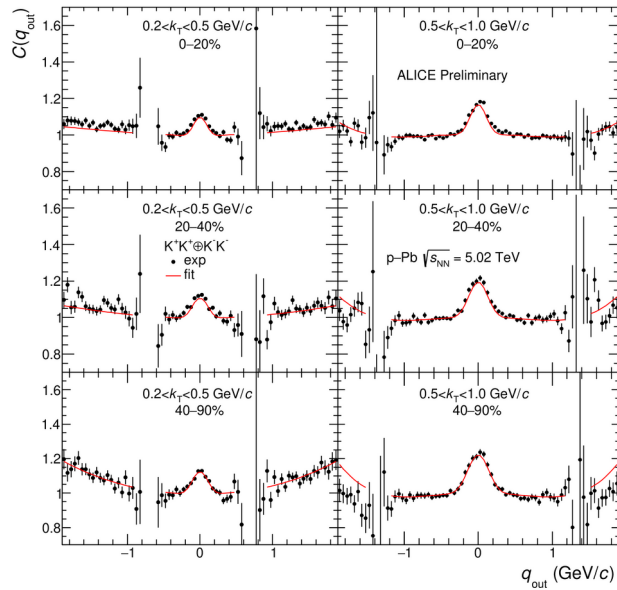
$$C(q_{inv}) = N \cdot [1 - \lambda + \lambda K(q_{inv}, R_{inv}) e^{-R_{inv}^2 q_{inv}^2}] \cdot D(q_{inv})$$

- $R_{inv}$  vs  $\langle N_{ch} \rangle^{1/3}$  at low  $k_T$
- $R_{inv}$  vs  $\langle N_{ch} \rangle^{1/3}$  at high  $k_T$
- Gap between Pb-Pb and pp+p-Pb
- Value of gap increases with increasing  $k_T$



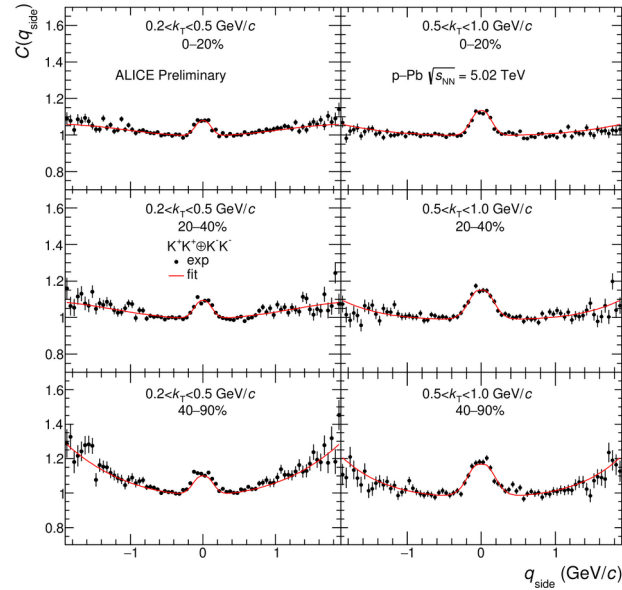
# p-Pb $\sqrt{s_{NN}}=5.02$ TeV: 3D KK CF projections

out



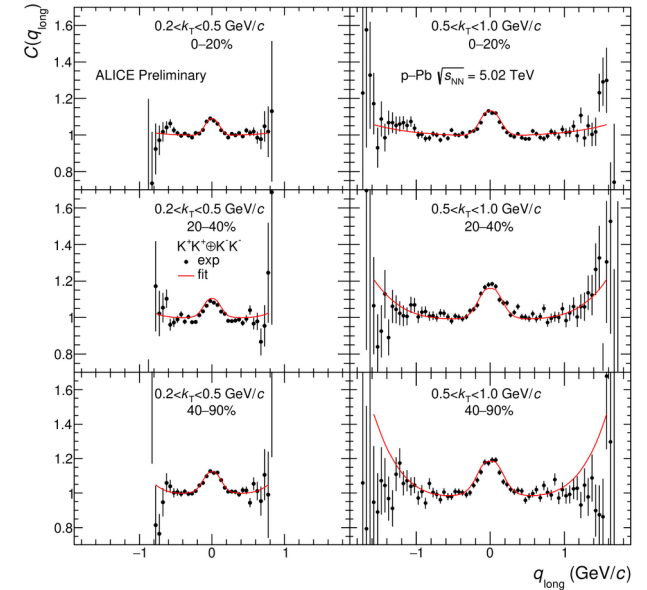
ALI-PREL-540481

side



ALI-PREL-540161

long



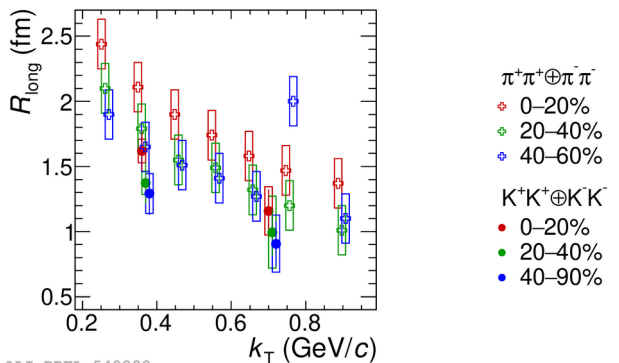
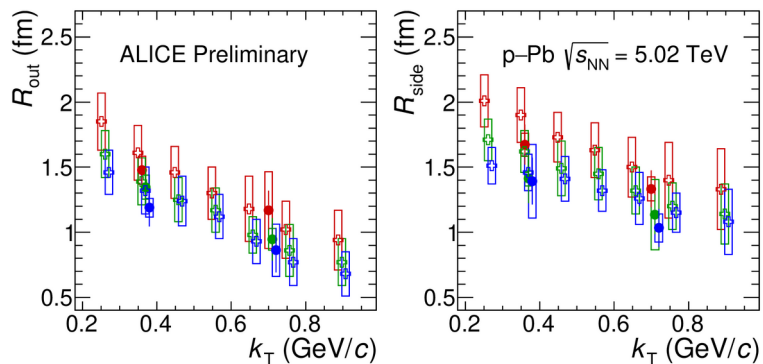
ALI-PREL-540155

- E.g. of CF projection onto out-side-long axis in LCMS with fit B-S:

$$C(q_{out}, q_{side}, q_{long}) = N [\lambda - 1 + \lambda K(R, q_{inv}) e^{-R_{out}^2 q_{out}^2 - R_{side}^2 q_{side}^2 - R_{long}^2 q_{long}^2}] D(q_{out}, q_{side}, q_{long})$$

- Fit function gives a good description for centrality (top to bottom) and  $k_T$  (left to right) bins

# p-Pb $\sqrt{s_{NN}}=5.02$ TeV: 3D KK CF results



ALI-PREL-540899

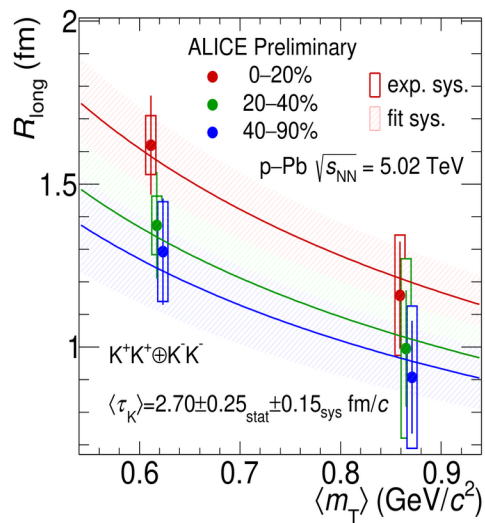
$\pi$  results from ALICE Collaboration, PRC 91 (2015) 034906

$\pi$  and K results agree well

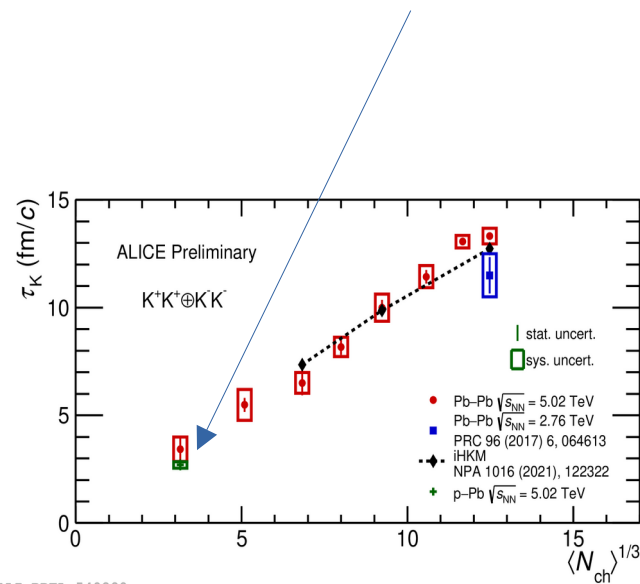
- Extract time of maximal emission  $\tau$
- $m_T$  dependence of  $R_{long}^2$  as NPA 1016(2021)122322

$$R_{long}^2 = \tau^2 \lambda^2 \left(1 + \frac{3}{2} \lambda^2\right), \quad \lambda^2 = T/m_T \sqrt{1 - \bar{v}_T^2}$$

- p-Pb and very peripheral Pb-Pb results for  $\tau$  are similar



ALI-PREL-540893



ALI-PREL-540890

# $K^+K^-$ theoretical correlation function (formalism)

[R.Lednicky, V.Lyuboshitz Sov. J. Nucl. Phys. 35, 770 (1982), R.Lednicky Phys. Part. Nucl.40, pp.307(2009)]

The  $K^+K^-$  correlation function(CF) at given  $\mathbf{k}^*$  and 3-momentum  $\mathbf{P}$ :

$$C_{sFSI}(\mathbf{k}^*, \mathbf{P}) = \int d^3\mathbf{r}^* S^\alpha(\mathbf{r}^*, \mathbf{P}) \sum_{\alpha'} \left| \psi_{-\mathbf{k}^*}^{\alpha'\alpha}(\mathbf{r}^*) \right|^2 \quad (1) \quad \text{Spatial separation: } S(\mathbf{r}^*) \sim \exp(-\mathbf{r}^{*2}/4R^2)$$

The s-wave scattering amplitude  $f(k^*)$ :

$$f_0(k^*) = \frac{\gamma_{f_0 \rightarrow K+K^-}}{m_{f_0}^2 - s - i(\gamma_{f_0 \rightarrow K+K^-} k^* + \gamma_{f_0 \rightarrow \pi\pi} k_{\pi\pi})} \quad \text{and} \quad f_1(k^*) = \frac{\gamma_{a_0 \rightarrow K+K^-}}{m_{a_0}^2 - s - i(\gamma_{a_0 \rightarrow K+K^-} k^* + \gamma_{a_0 \rightarrow \pi\eta} k_{\pi\eta})} \quad (2)$$

The p-wave strong interaction through  $\phi$  meson resonance [R.Lednicky Part. Nucl. Letters 8(2011)965]:

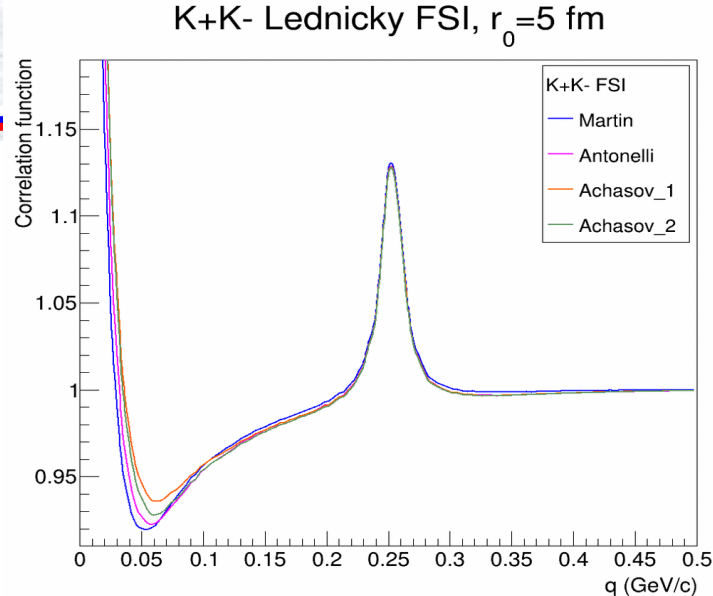
$$C_\phi(p_1, p_2) = N^{-1}(p_1, p_2) \int d^3\mathbf{r} W_P(\mathbf{r}, \mathbf{k}) \sum_{\alpha' m'} \left| \psi_{-\mathbf{k}}^{\alpha' m'; \alpha}(\mathbf{r}) \right|^2 \quad (3)$$

The total correlation function :  $C_{FSI}(p_1, p_2) = 1 + C_{sFSI}(p_1, p_2) + N_1 C_{\phi\text{-direct}}(p_1, p_2) + N_2 C_\phi(p_1, p_2)$  (4)

$C_{\phi\text{-direct}}(p_1, p_2)$  is a non-relativistic Breit-Wigner function.

# Pb-Pb $\sqrt{s_{NN}}=2.76$ TeV: K+K- fit

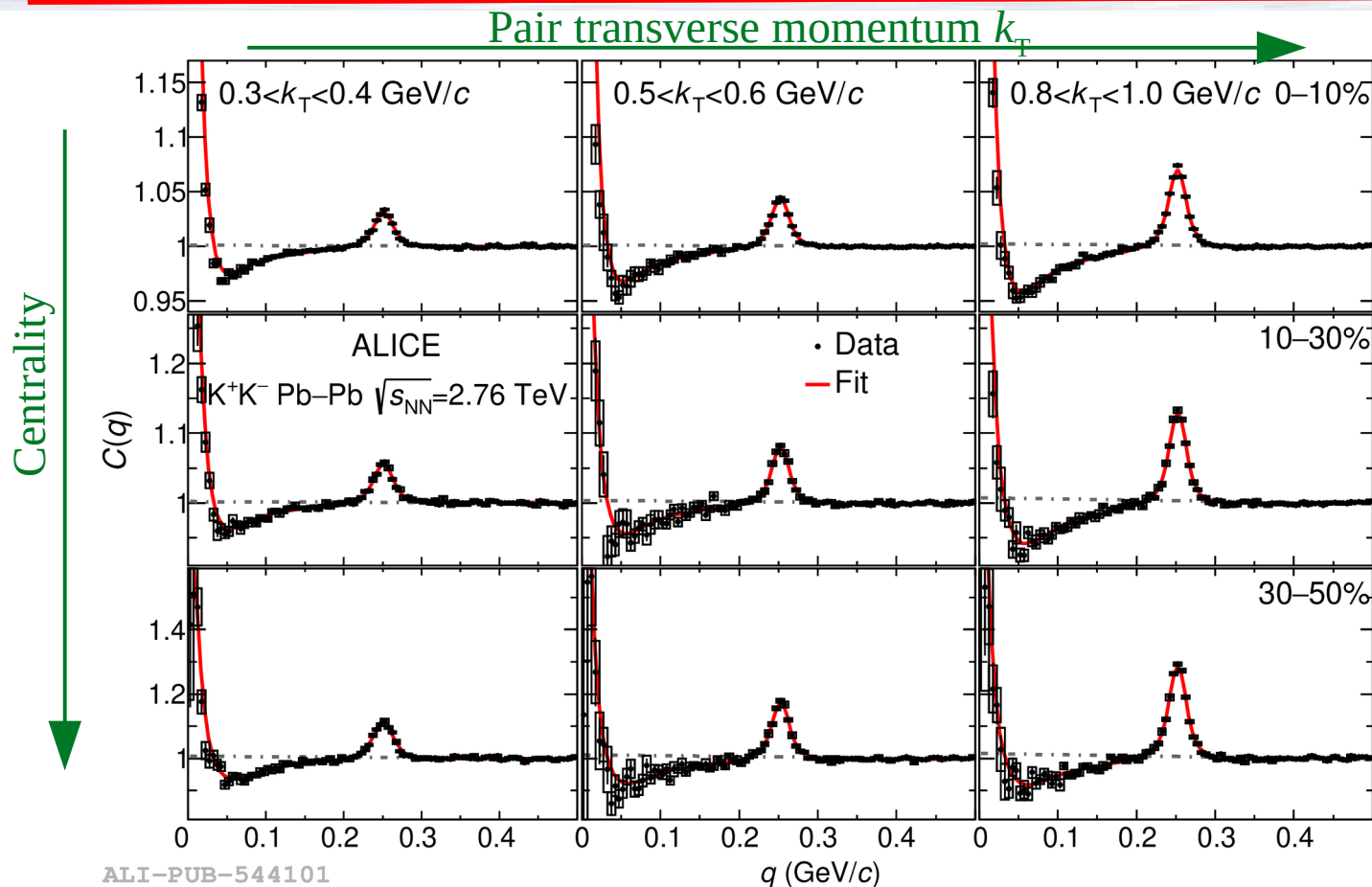
- $C(q) = \text{Norm} \cdot [1 + \lambda \cdot C_{\text{sFSI}}(q, R) + \lambda_\phi \cdot C_\phi(q, M, \sigma)]$   
 $C_{\text{sFSI}}(q, R)$  - Lednicky model  
 $C_\phi(q, M, \sigma)$  - Breit-Wigner  $\Gamma_\phi=4.25\text{MeV}$
- $a_0$  parameters fixed from [Achasov<sup>2</sup>](#) [ALICE PLB774 (2017) 64, PLB 790 (2019) 22]
- $f_0$  mass and coupling parameters are [free](#)



The masses ( $a_0$  and  $f_0$ ) and coupling parameters

Model	$m_{f_0}^2$	$m_{a_0}^2$	$\gamma_{f_0 \rightarrow K+K-}$	$\gamma_{f_0 \rightarrow \pi\pi}$	$\gamma_{a_0 \rightarrow K+K-}$	$\gamma_{a_0 \rightarrow \pi\eta}$	
<a href="#">Martin</a>	.9565	.9487	.792	.199	.333	.222	NPB 121 (1977) 514
<a href="#">Antonelli</a>	.9467	.9698	2.763	.5283	.4038	.3711	hep-ex/0209069
<a href="#">Achasov<sup>1</sup></a>	.9920	.9841	1.305	.2684	.5555	.4401	PRD 63(2001) 094007
<a href="#">Achasov<sup>2</sup></a>	.9920	<b>1.0060</b>	1.305	.2684	<b>.8365</b>	<b>.4580</b>	<b>PRD 68(2003) 014006</b>

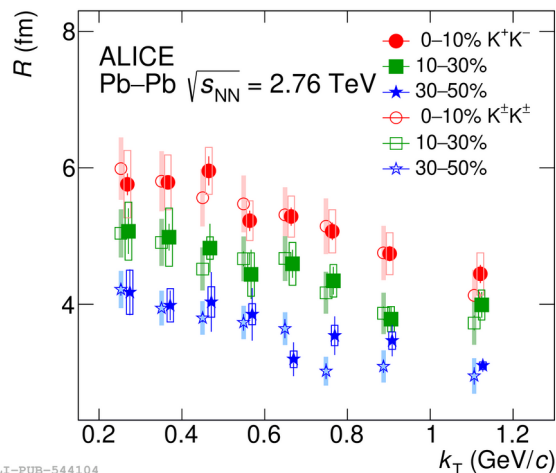
# Pb-Pb $\sqrt{s_{NN}}=2.76$ TeV: K+K- CF



ALICE Collaboration,  
Phys. Rev. C107 (2023) 054904

Fit function gives a good description for centrality (top to bottom) and  $k_T$  (left to right) bins

# Pb-Pb $\sqrt{s_{NN}}=2.76$ TeV: results



$f_0(980)$  [j]

$$I^G(J^{PC}) = 0^+(0^{++})$$

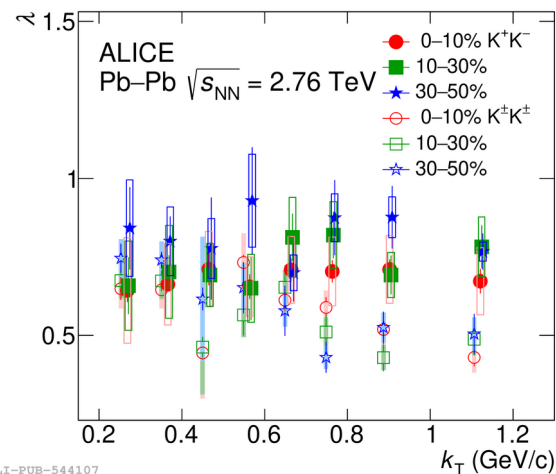
Mass  $m = 990 \pm 20$  MeV

Full width  $\Gamma = 10$  to  $100$  MeV

Particle Data Group

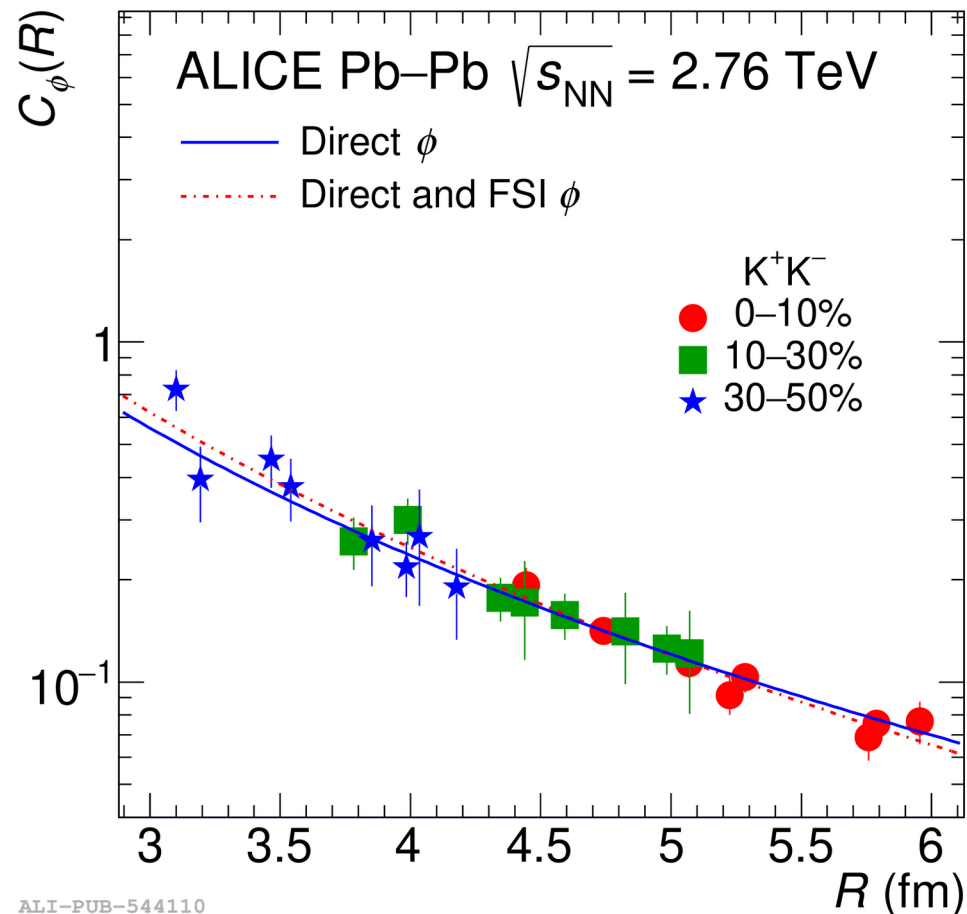
$f_0(980)$ DECAY MODES	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$\pi\pi$	dominant	476
$K\bar{K}$	seen	36
$\gamma\gamma$	seen	495

- Radii are in agreement within errors
- $\lambda$  of  $K^+K^-$  tend to be larger than for  $\lambda$  of  $K^\pm K^\pm$   
ALICE Collaboration, Phys. Rev. C107 (2023) 054904
- $f_0(980)$  mass, width and couplings parameters:
- $M_{f_0} = 967 \pm 3 \pm 7$  MeV/c<sup>2</sup>
- $\Gamma_{f_0} = 43.81 \pm 8.76 \pm 6.90$  MeV/c<sup>2</sup>
- $Y_{f_0 \rightarrow \pi\pi} = 0.089 \pm 0.0178 \pm 0.026$  GeV
- $Y_{f_0 \rightarrow K+K^-} = 0.34 \pm 0.068 \pm 0.101$  GeV



# Pb–Pb $\sqrt{s_{NN}}=2.76$ TeV: $\phi$ peak value

ALICE Collaboration, Phys. Rev. C107 (2023) 054904



- $\phi$  peak height (corrected for  $\lambda$  and MR):

$$C_\phi = CF(q = \sqrt{M_\phi^2 - 4m_K^2}) - 1$$

- $\phi$  peak: direct production and FSI  $K^+K^-$
- Direct =  $\text{const}/R^3$
- FSI =  $\text{const} \cdot \exp(-\mathbf{b}^2 k_0^2 R^2) / R^3$ ,  $k_0 = 126$  MeV/c
- $C_\phi = a_{\text{dir}} \cdot C_{\text{dir}} + a_{\text{FSI}} \cdot C_{\text{FSI}}$
- Red curve fit  $\rightarrow a_{\text{dir}} = 0.75$ ,  $a_{\text{FSI}} = 0.25$
- FSI fraction could be estimated
- Lack of statistic  $\rightarrow$  difficult to distinguish between direct and FSI contribution

# Summary

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- CF  $\pi^+\pi^+$  and  $K^+K^+$  in pp at  $\sqrt{s} = 13$  TeV were measured;
  - CF classified via global event-shape variable,  $S_T$ ;
  - Spherical CF cleared of mini-jets; Jet CF shows significant mini-jet effects;
  - The  $\pi^+\pi^+$  radii for spherical events are larger than for jet events;
- CF  $K^+K^+$  1D+3D in p–Pb at  $\sqrt{s_{NN}}=5.02$  TeV were measured;
  - 1D R vs  $N_{ch}$  for p–Pb and pp are in agreement and different from Pb–Pb;
  - 3D out-side-long  $K^+K^+$  and  $\pi^+\pi^+$  radii coincide within errors;
  - maximal emission time  $\tau_K$  was extracted and is close to one at very peripheral Pb–Pb;
- CF  $K^+K^-$  Pb–Pb at  $\sqrt{s_{NN}}=2.76$  TeV were measured;
  - For the first time the  $K^+K^-$  correlation functions were fitted with free  $f_0(980)$  mass, width with restriction on radii to be close to the corresponding identical  $K^+K^+$ ;
  - The measured width of the  $f_0(980)$  is  $43.81 \pm 8.76(\text{stat}) \pm 6.90(\text{sys})$  MeV/ $c^2$  and mass is  $967 \pm 3(\text{stat}) \pm 7(\text{sys})$  MeV/ $c^2$  which do not contradict the PDG data.

Thank you for your attention!

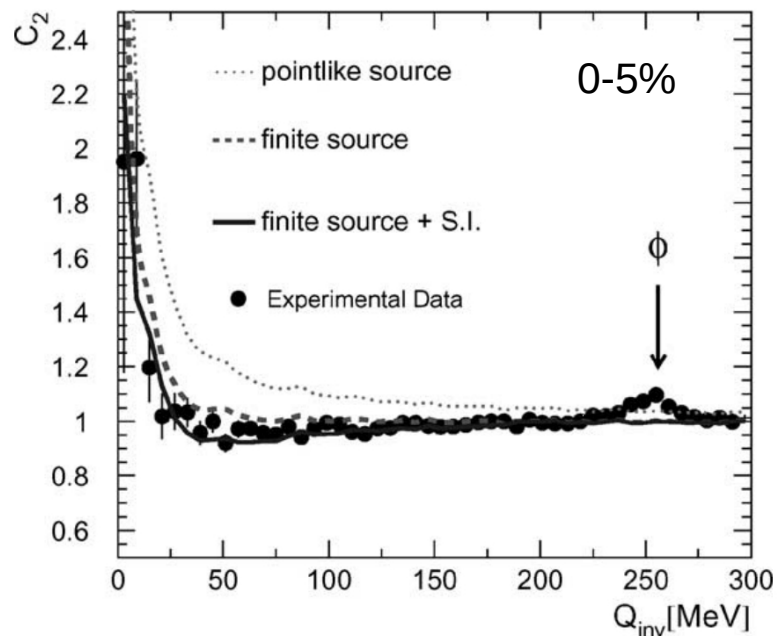


# Slides in trunk



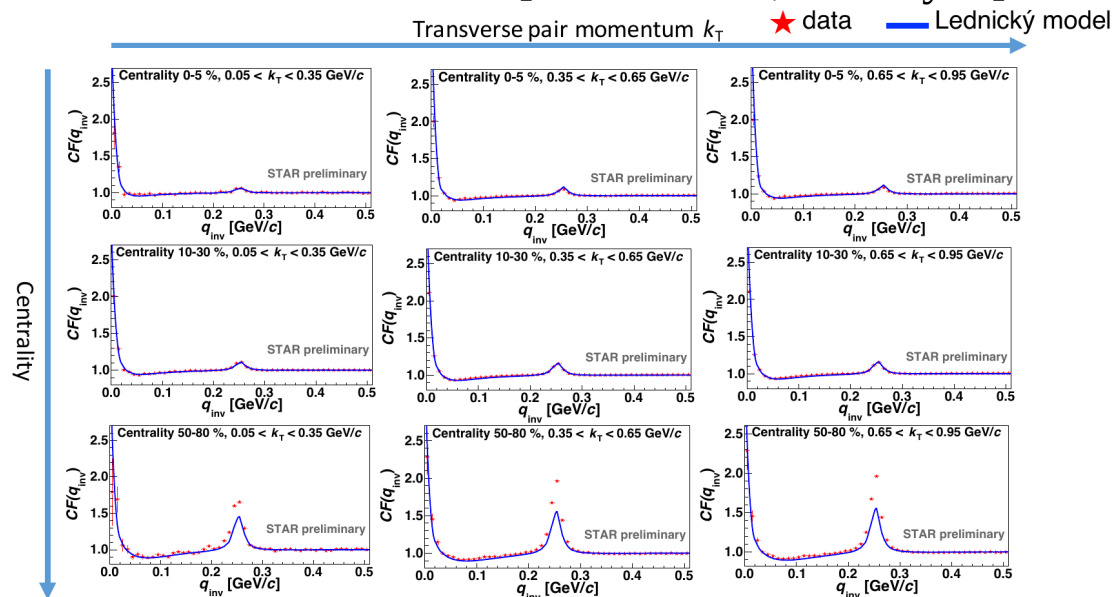
# $K^+K^-$ existing results

NA49 Pb-Pb 158 GeV [PLB 557(2003)157]



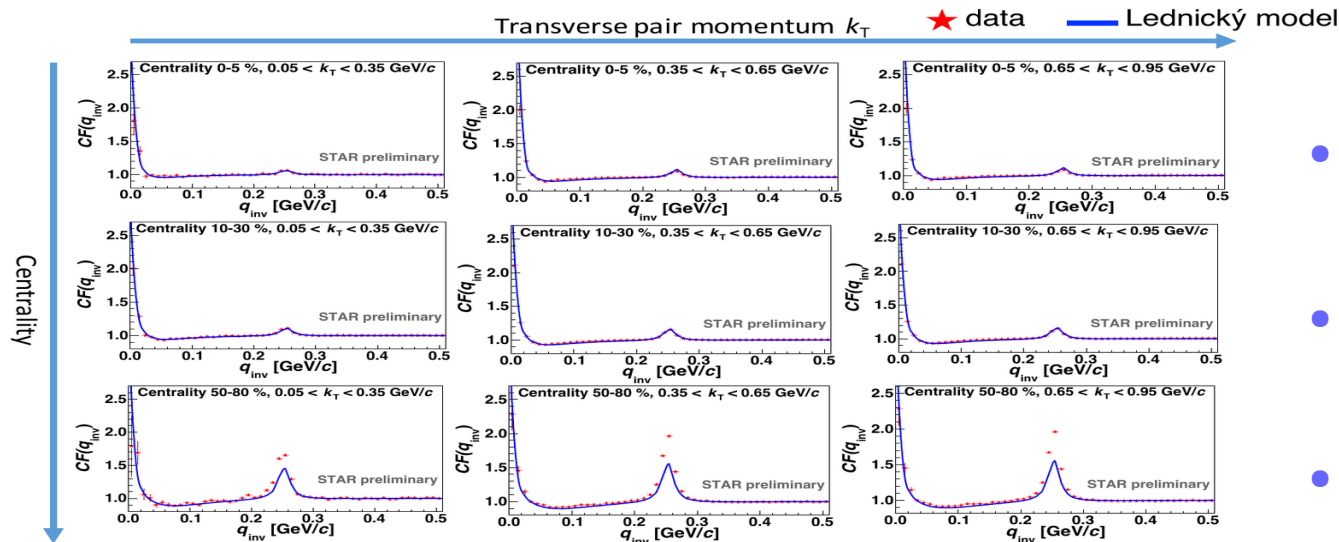
- Coulomb stays above data
- Dip at  $Q_{inv} \sim 50-150$  due to strong interaction
- Strong and Coulomb FSI does good job

STAR AuAu 200 GeV [WPCF 2017, J. Lidrych]



- No fit, comparison with Lednický model
- Data is described qualitatively for large source
- Phi production mechanism is not taken into account

# K<sup>+</sup>K<sup>-</sup> existing results: STAR



- K<sup>+</sup>K<sup>-</sup> in AuAu at  $\sqrt{s_{NN}}=200$  GeV  
[WPCF 2017, Jindřich Lidrych]
- $CF=(CF^{\text{theor}}-1)\cdot\lambda+1$  (no fit)  
 $CF^{\text{theor}} \rightarrow$  Lednický model
- Data is described qualitatively for large source

## Observations:

- The model underpredicts the strength of the correlation functions in the region of resonance with decreasing  $R_{\text{inv}}$
- Model *fails* for smaller system ( $\sim 3$ fm and smaller)
- Does not take into account  $\phi$  production mechanism

