

Decoding the nature of Dark Matter

Alexander Belyaev



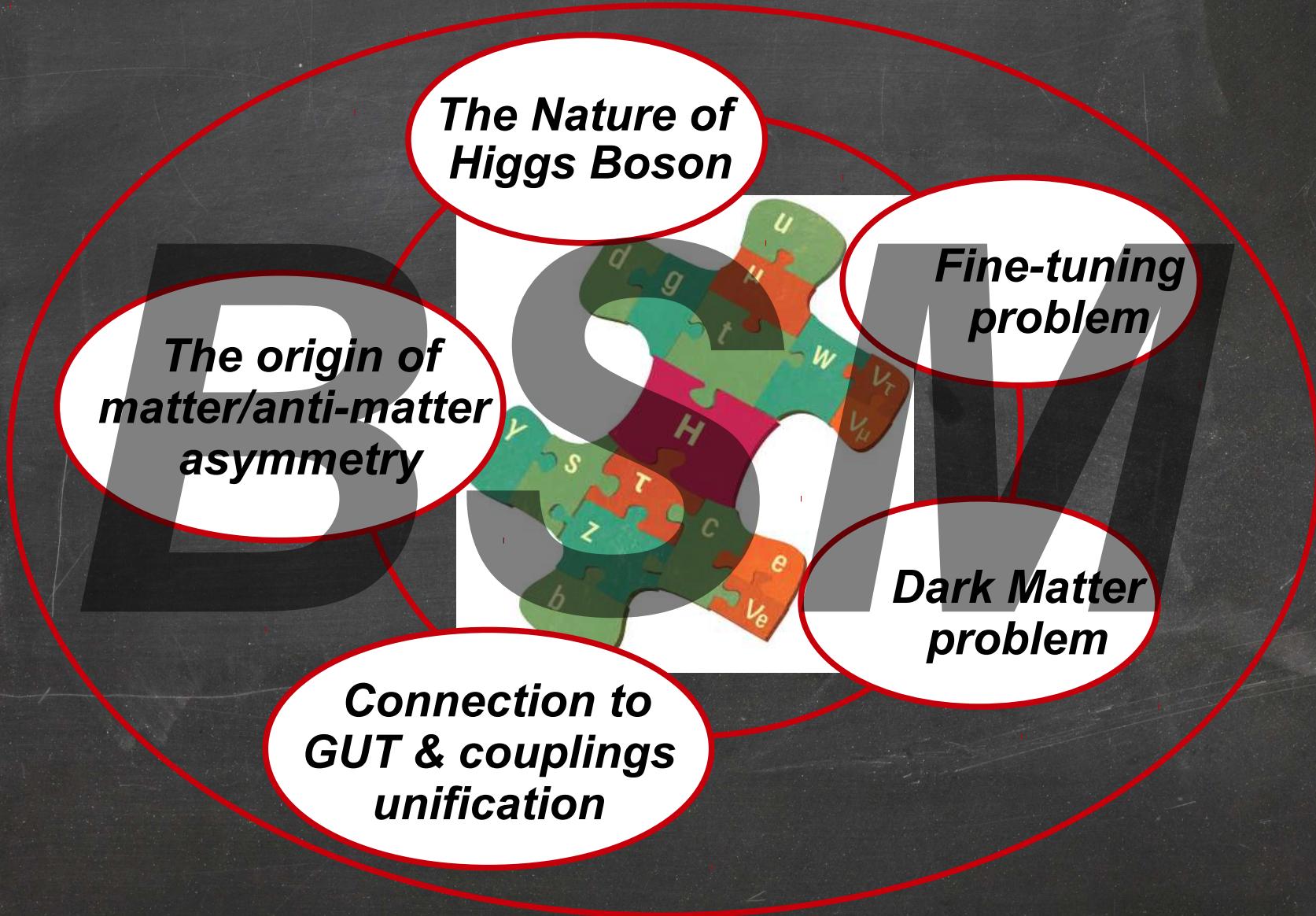
Southampton University & Rutherford Appleton Laboratory

Helmholtz International School
"Modern Colliders - Theory and Experiment 2018" and Workshop
"Calculations for Modern and Future Colliders (CALC2018)"

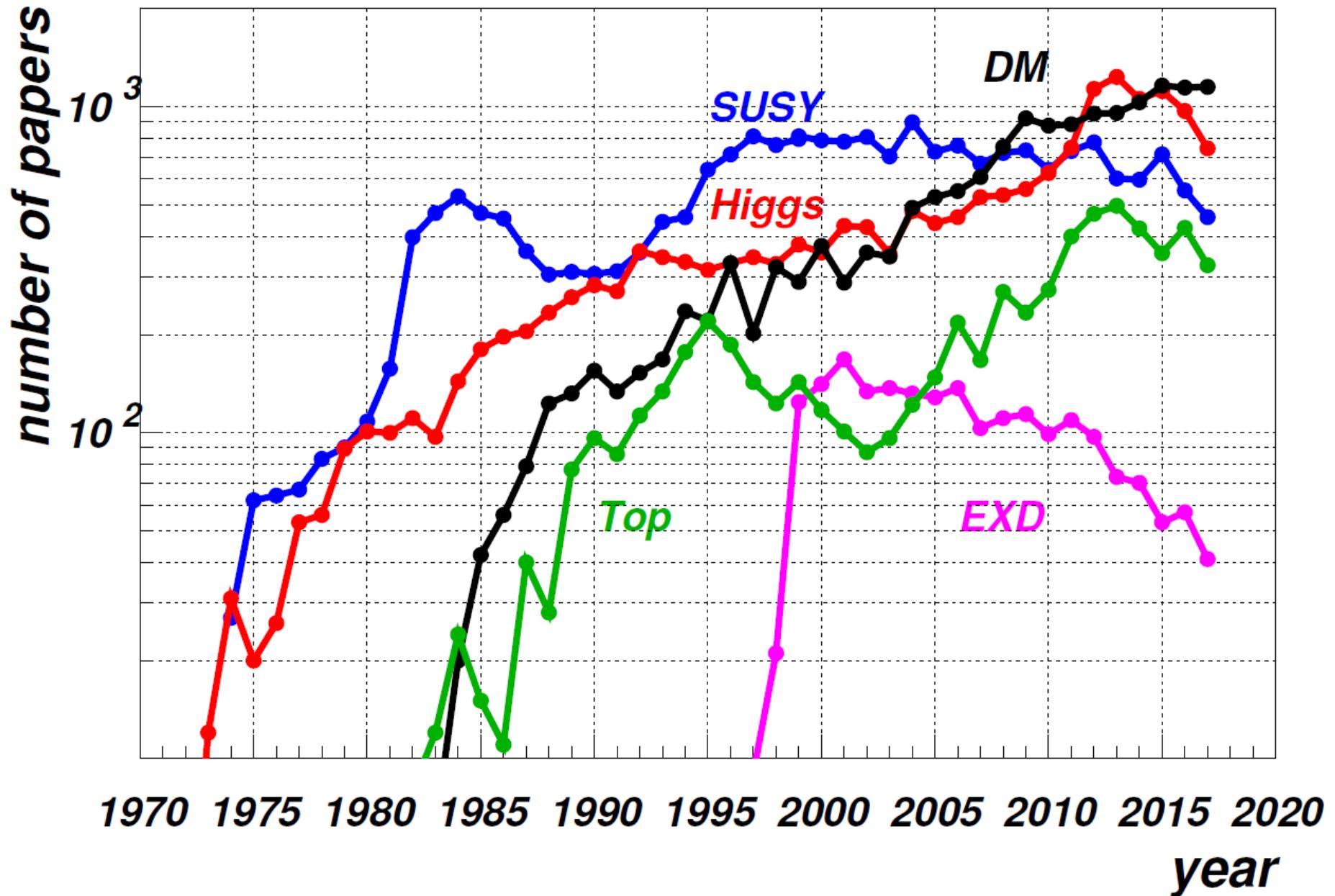
Higgs Boson Discovery has finished the SM puzzle



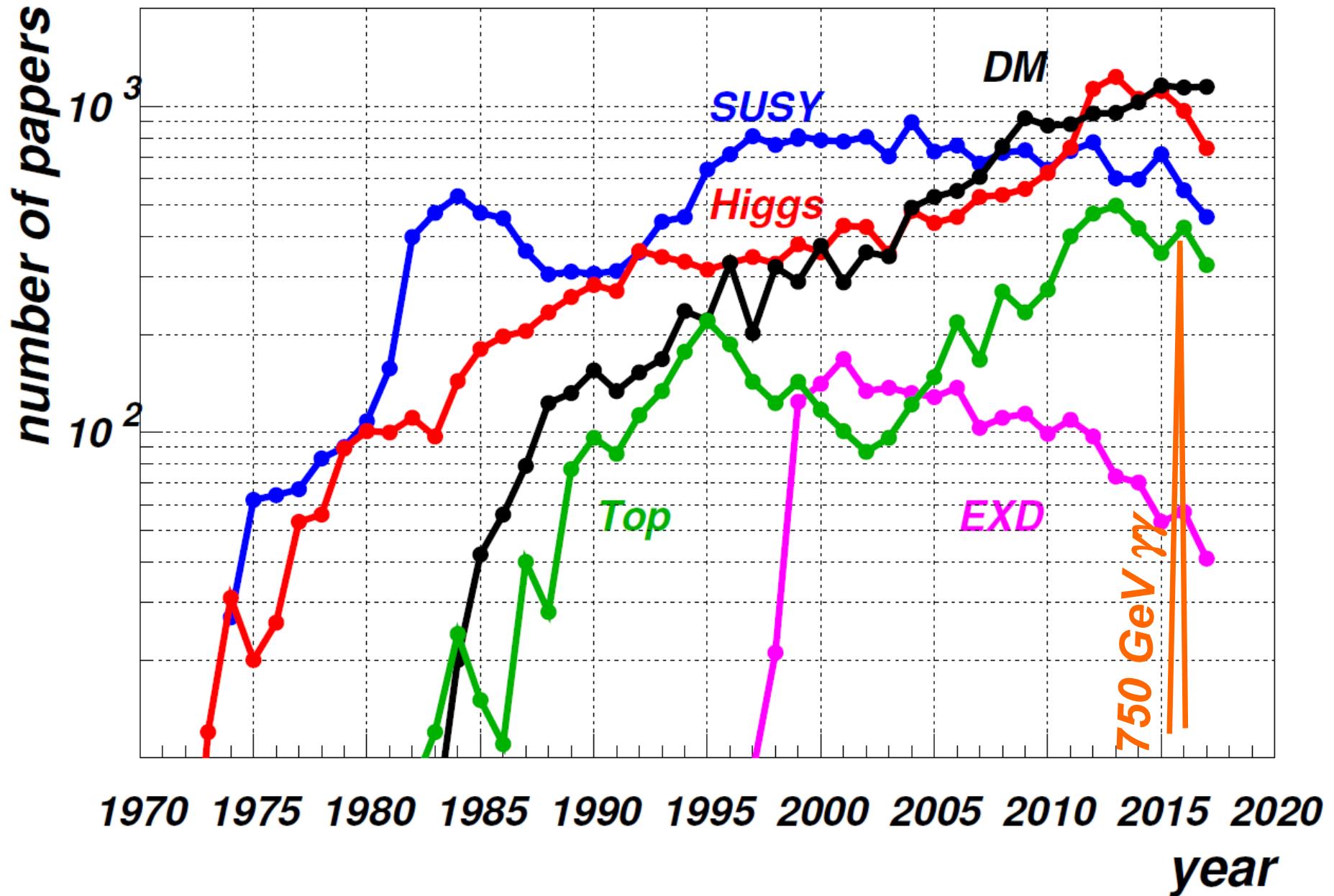
Higgs Boson Discovery has finished the SM puzzle, but it is just a piece of some (more) complete and consistent one!



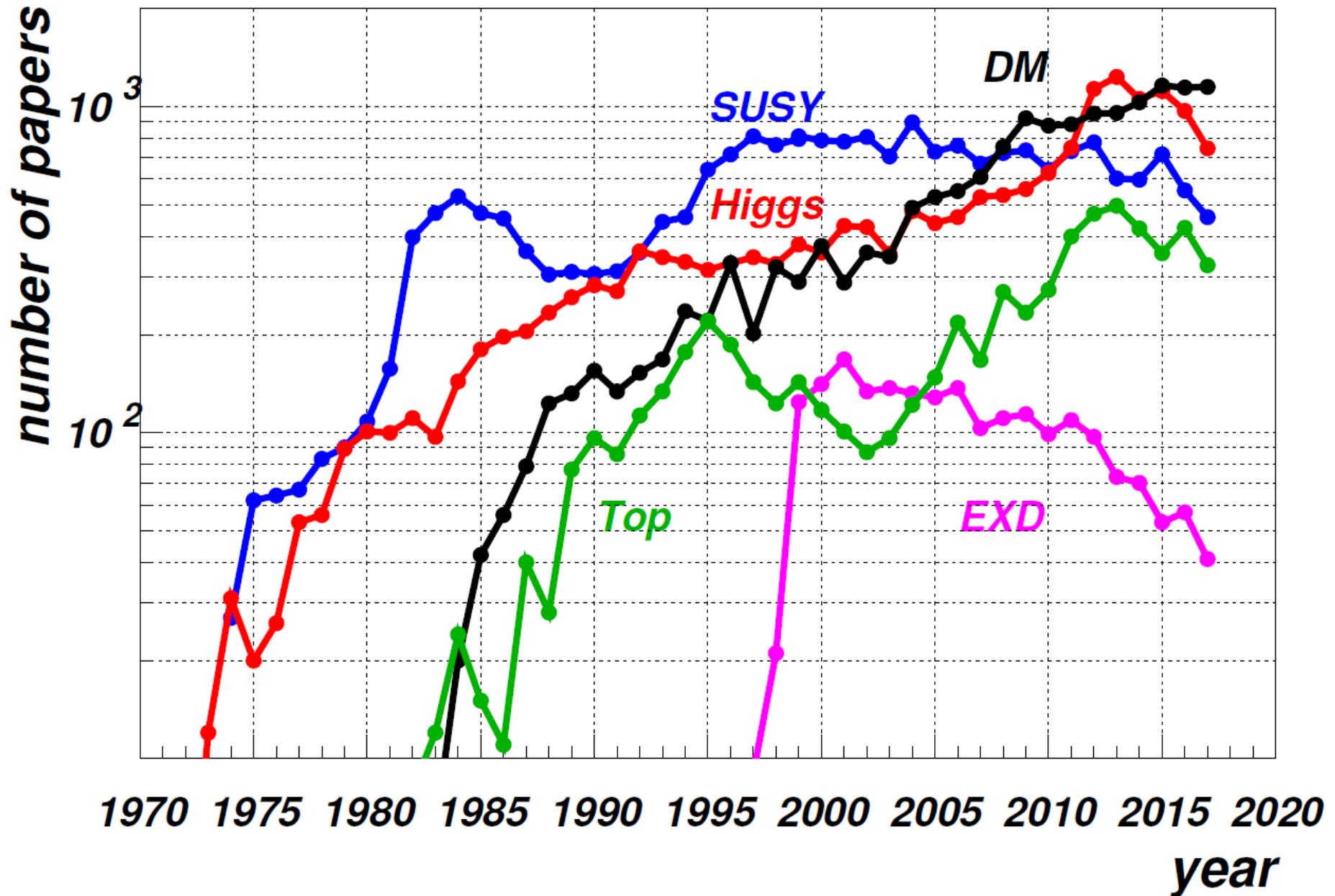
Why we are so keen to study DM?



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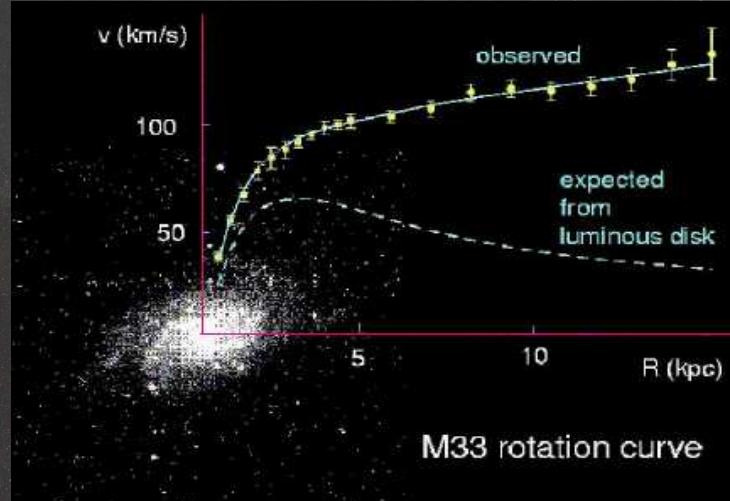


Why we are so keen to study DM?

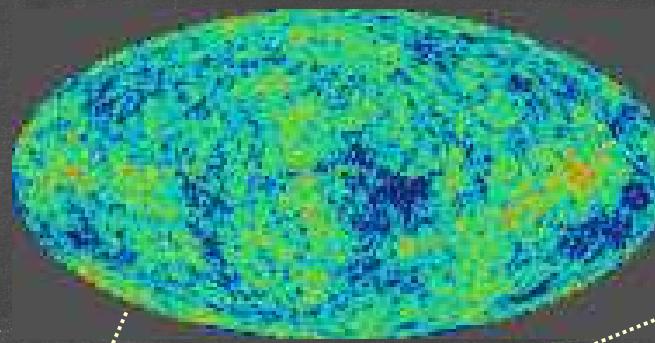


Because the existence of DM is the strongest evidence for BSM!

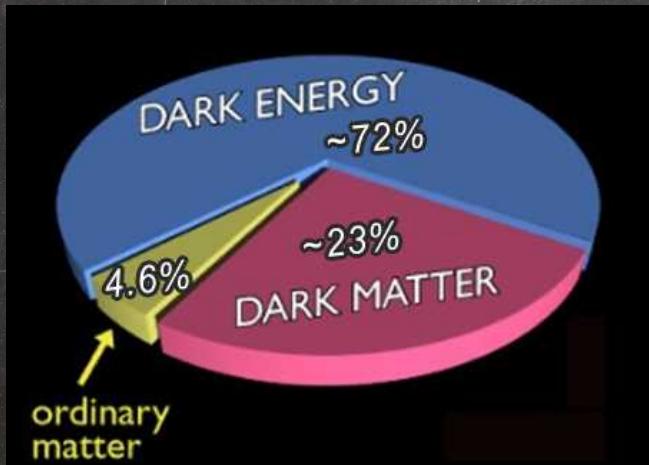
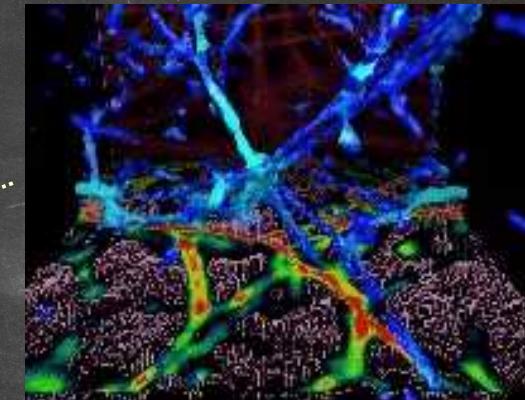
Galactic rotation curves



CMB: WMAP and PLANCK



Large Scale Structures



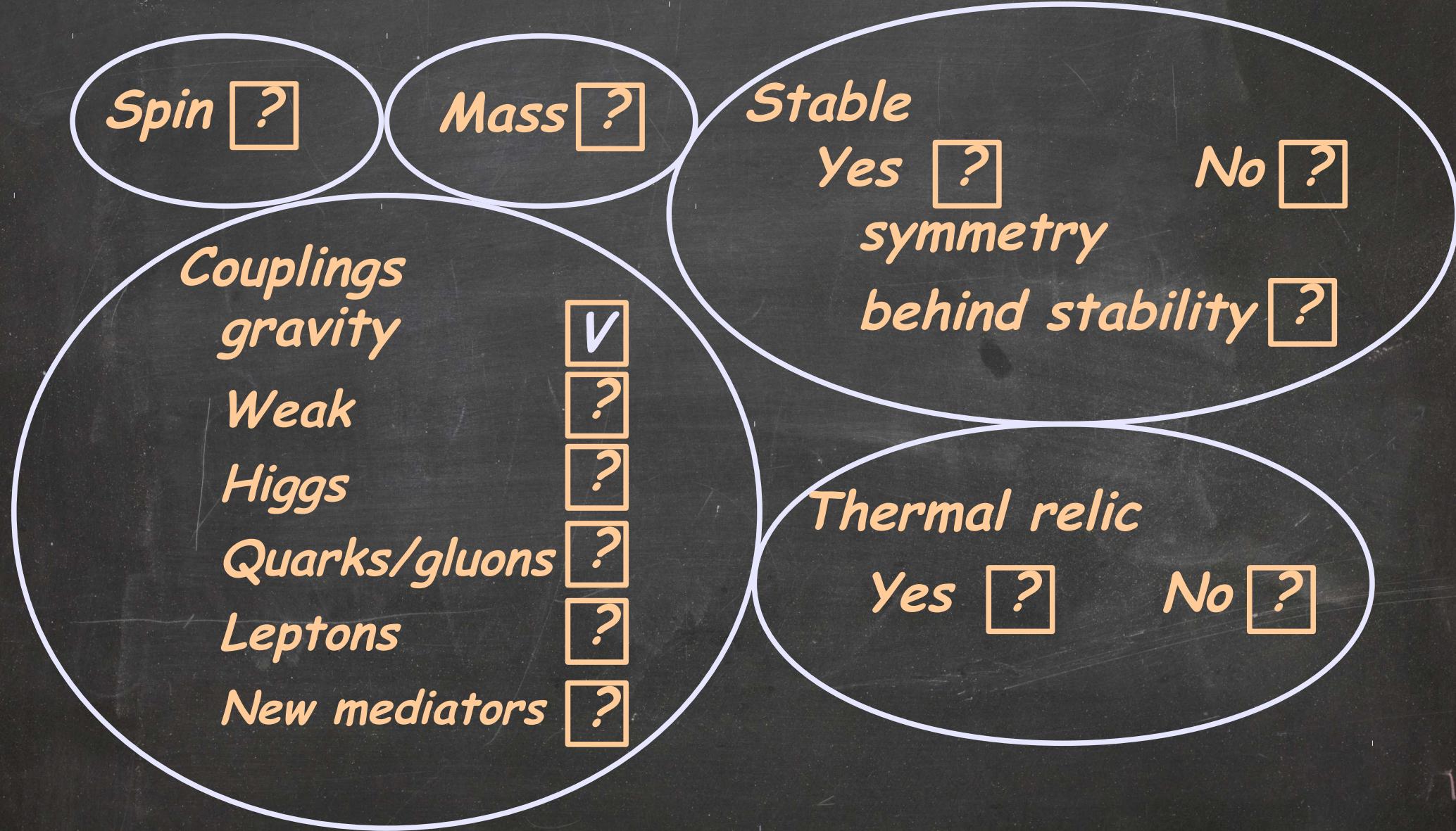
Gravitational lensing



Bullet cluster



Even though we know almost nothing about it!



How we can decode the fundamental nature of Dark Matter?

How we can decode
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We need a DM signal first!

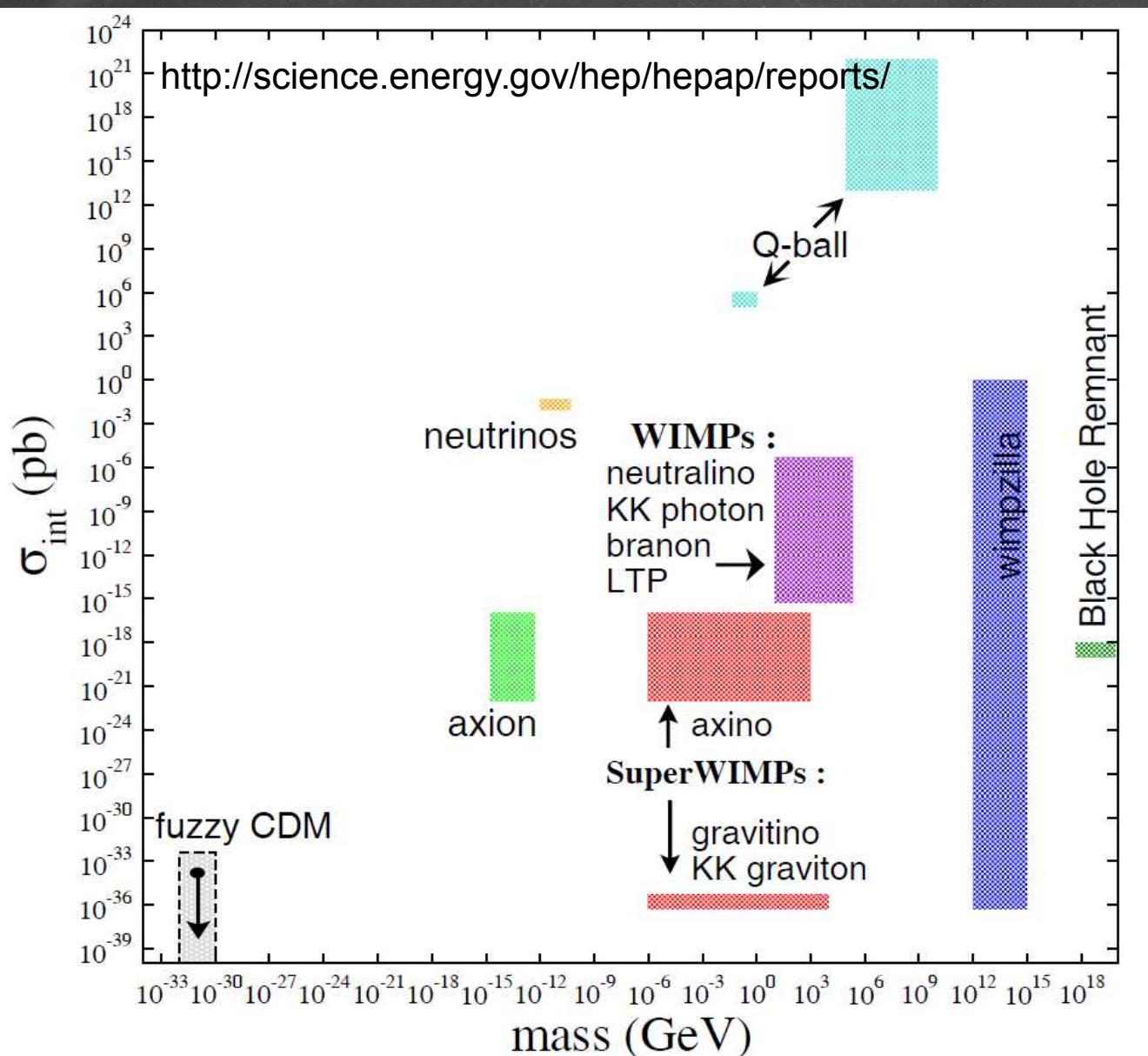
How we can decode the fundamental nature of Dark Matter?

We need a DM signal first!

But at the moment we can:

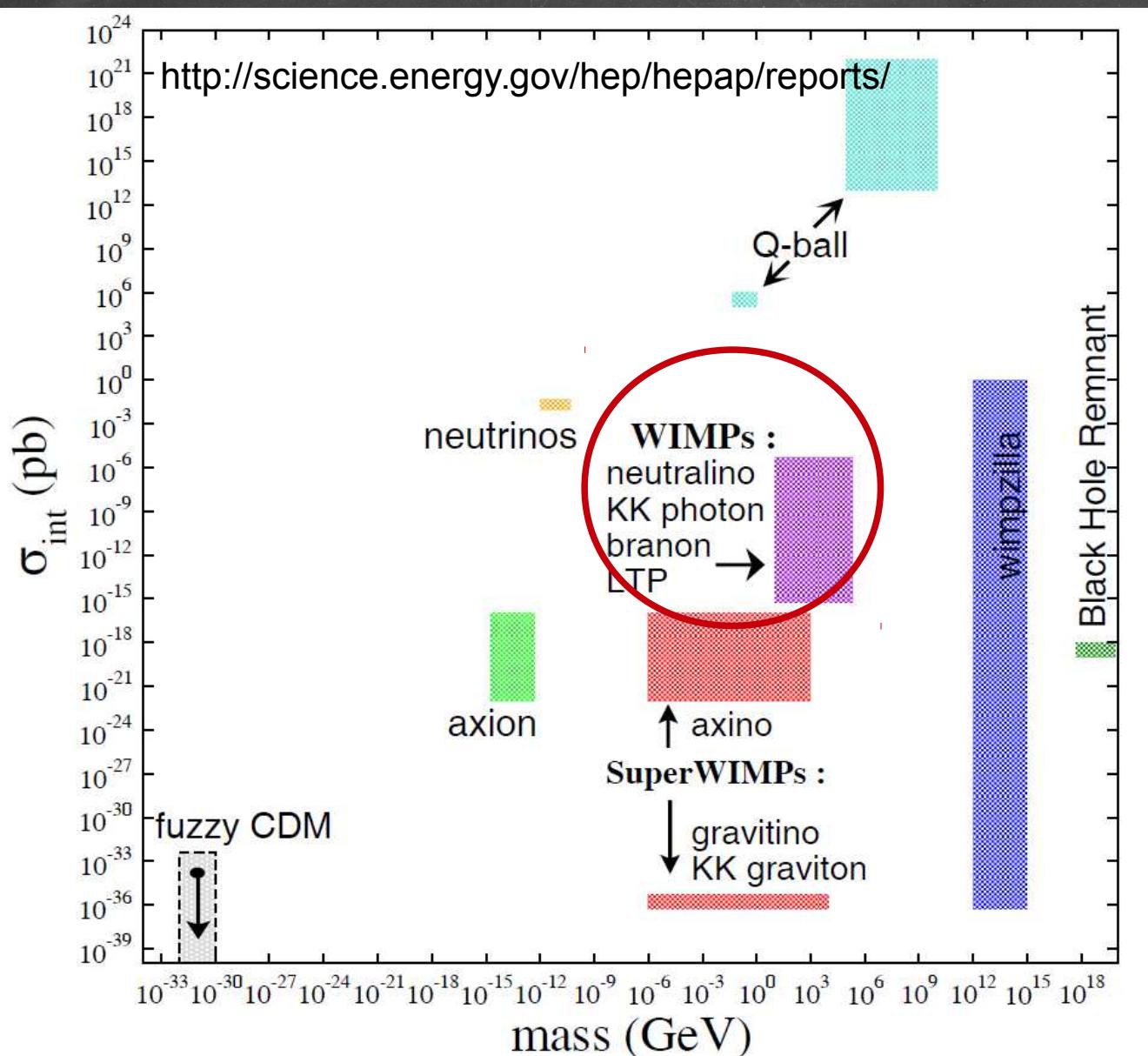
- ⇒ understand what kind of DM is already excluded
- ⇒ explore theory space and prepare ourselves to discovery and decoding of DM

DM candidates: interaction vs mass



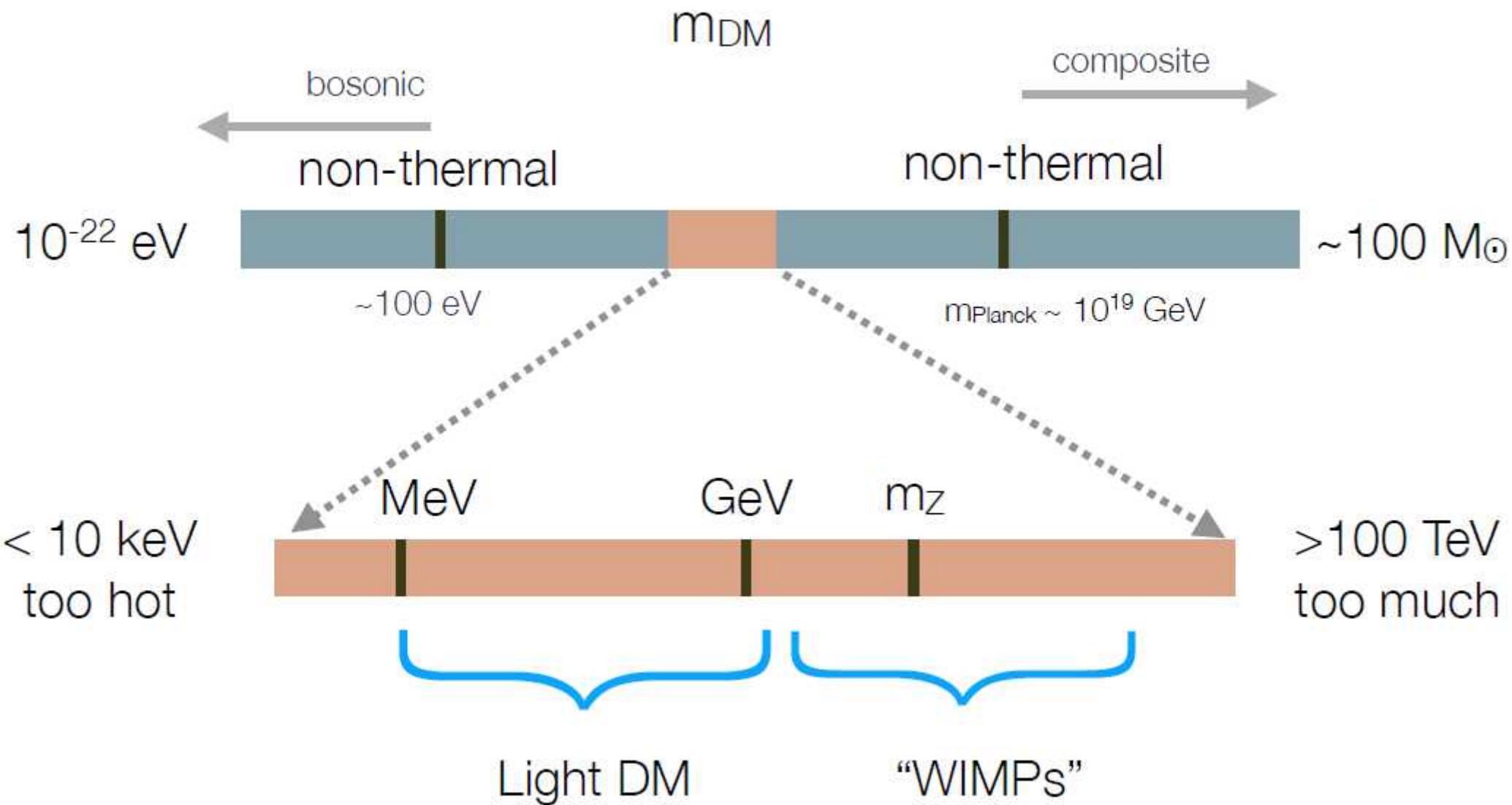
- Planck mass BH remnants: tiny black holes protected by gravity effects [Chen '04] from decay via Hawking radiation
- Wimpzillas: very massive non-thermal WIMPs [Kolb, Chung, Riotto '98]
- Q-balls: topological solitons that occur in QFT [Coleman '86]
- EW scale WIMPs, protected by parity – LSP, LKP, LTP particles
- SuperWIMPs: electrically and color neutral DM interacting with much smaller strength (perhaps only gravitationally)
- Neutrinos: usual neutrinos are too light- HDM, subdominant component only (to be consistent with large scale structures); but heavier gauge singlet neutrinos can be CDM
- Axions:
$$\frac{\theta_{QCD}}{32\pi i^2} F^{\mu\nu} \tilde{F}^{\mu\nu}$$
 θ_{QCD} is replaced by a quantum field, the potential energy allows the field to relax to near zero strength, axion as a consequence

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Mass range for thermal DM



Spectrum of Theory Space

Less Complete



Simplified Models



Models



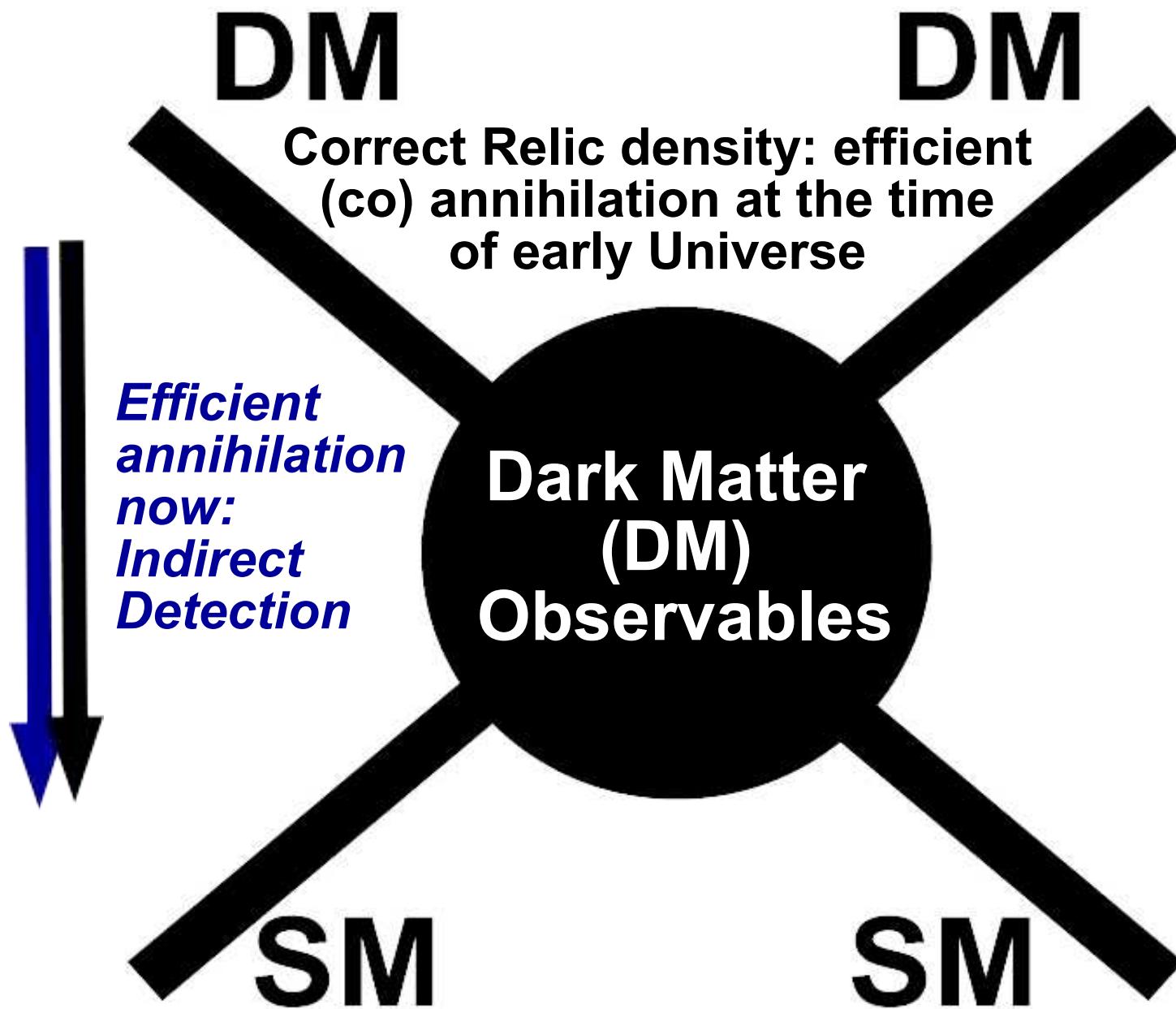
MSSM

More Complete

Sketches of Models

T.Tait



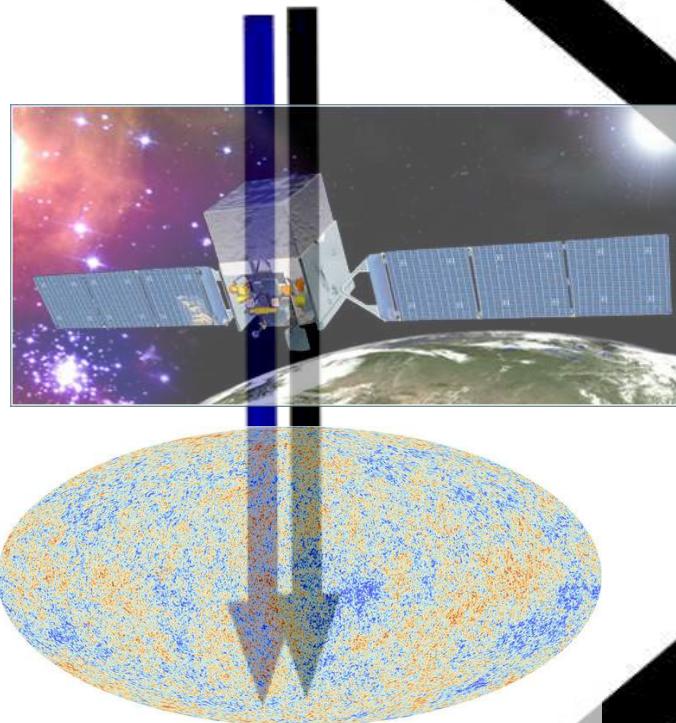


DM

DM

**Correct Relic density: efficient
(co) annihilation at the time
of early Universe**

**Dark Matter
(DM)
Observables**



SM

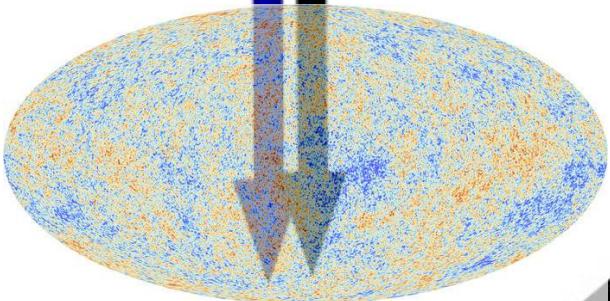
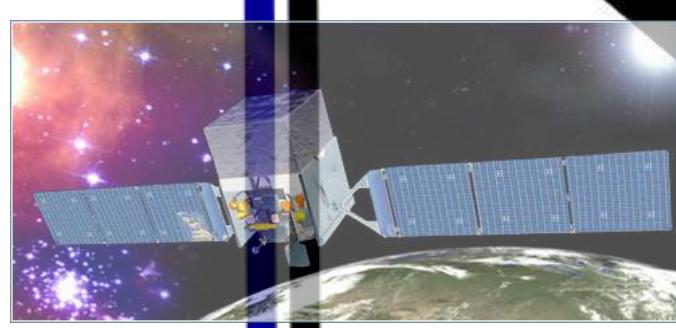
SM

DM

DM

Correct Relic density: efficient
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Dark Matter
(DM)
Observables



SM

SM

*Efficient scattering
off nuclei: Direct
Detection*

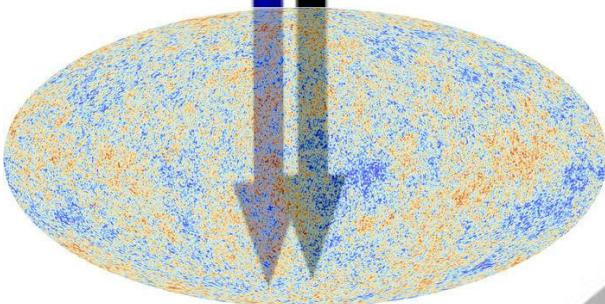
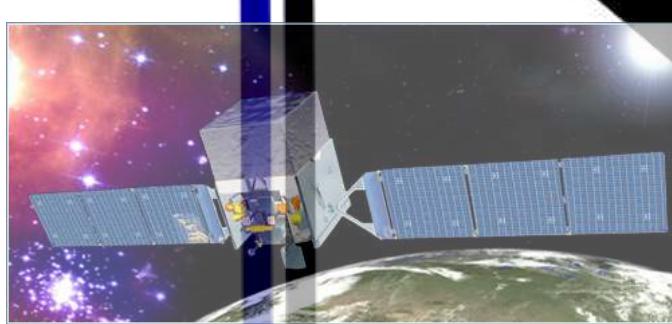


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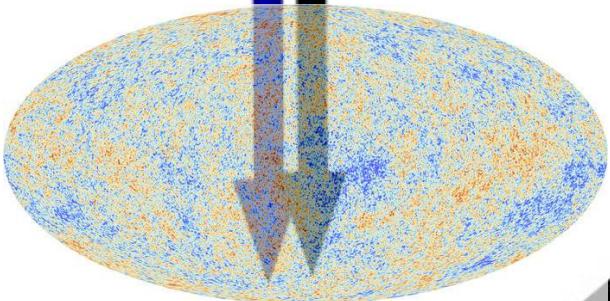
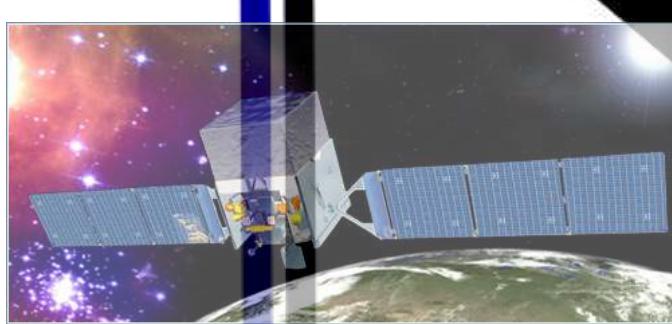
DM

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Dark Matter
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Observables

*Efficient
production
at colliders*



SM

SM

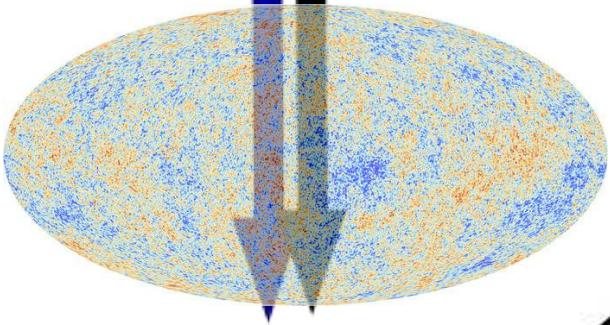
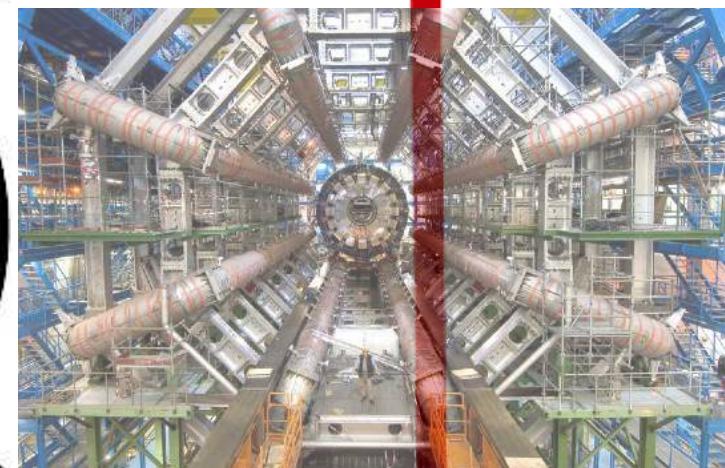


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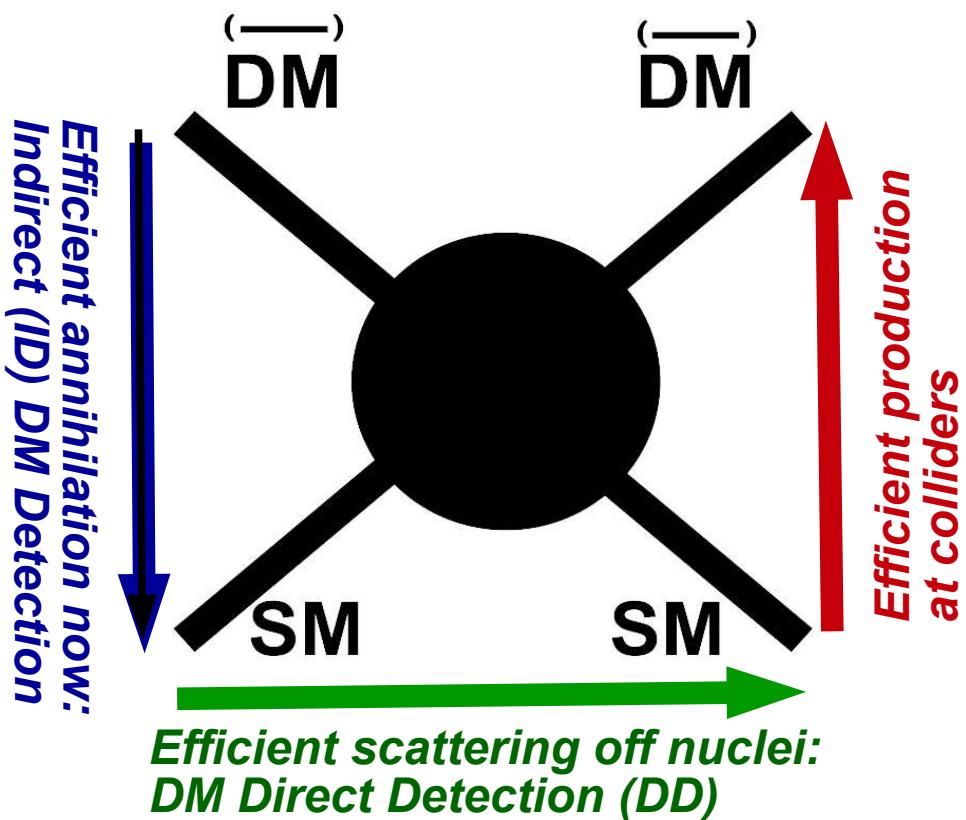
Dark Matter
(DM)
Observables



SM

SM

Complementarity of DM searches

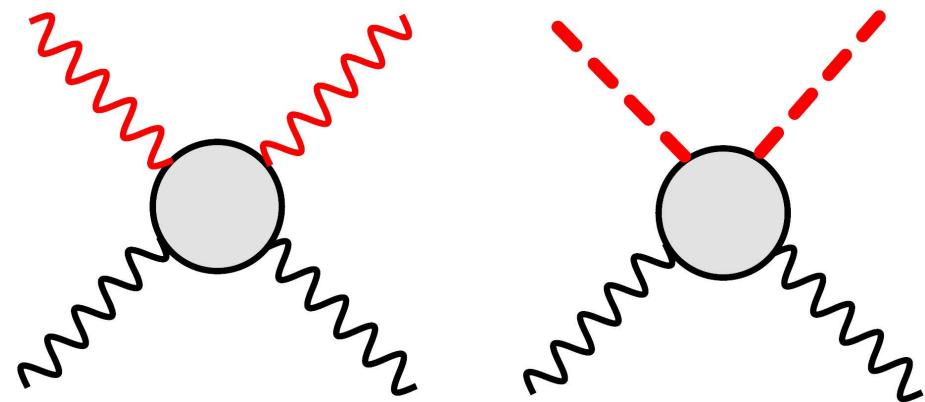
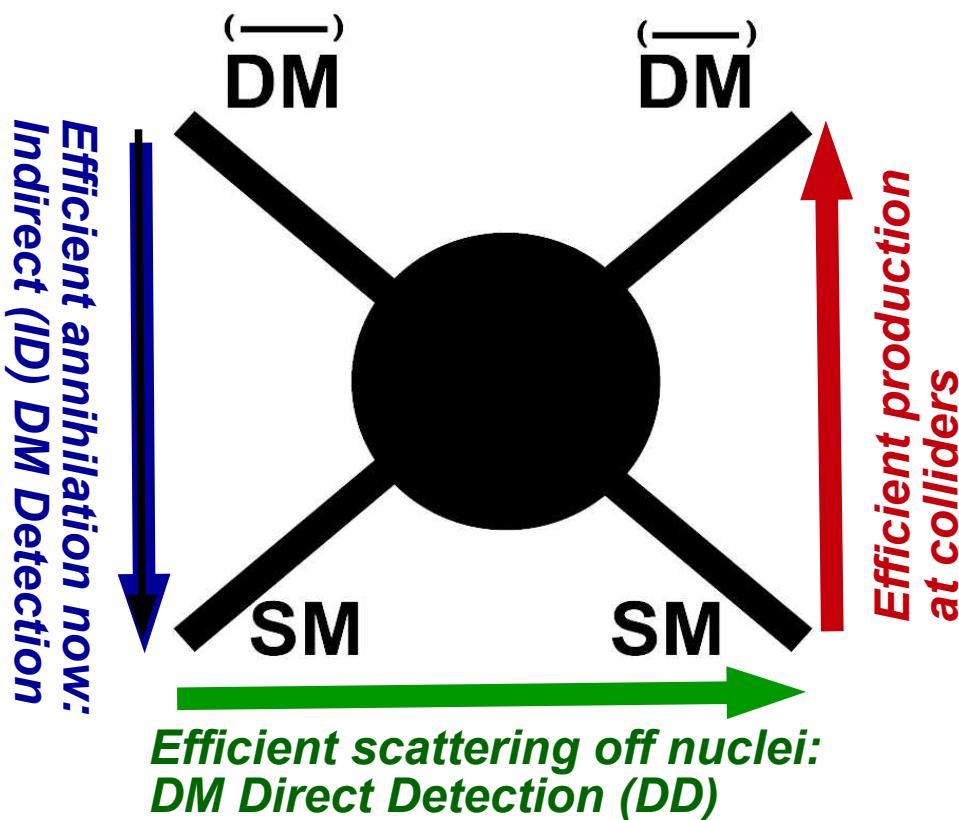


Important: there is no 100% correlation between signatures above. E.g. the high rate of annihilation does not always guarantee high rate for DD!

Actually there is a great complementarity in this:

- In case of NO DM Signal – we can efficiently exclude DM models
- In case of DM signal – we can efficiently determine the nature of DM

Complementarity of DM searches



Example of DM interactions with negligible/suppressed DD rates

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Direct Dark Matter Detection

- Search for the recoil energy of a nucleus in an underground detector after collision with a WIMP

- Elastic recoil energy

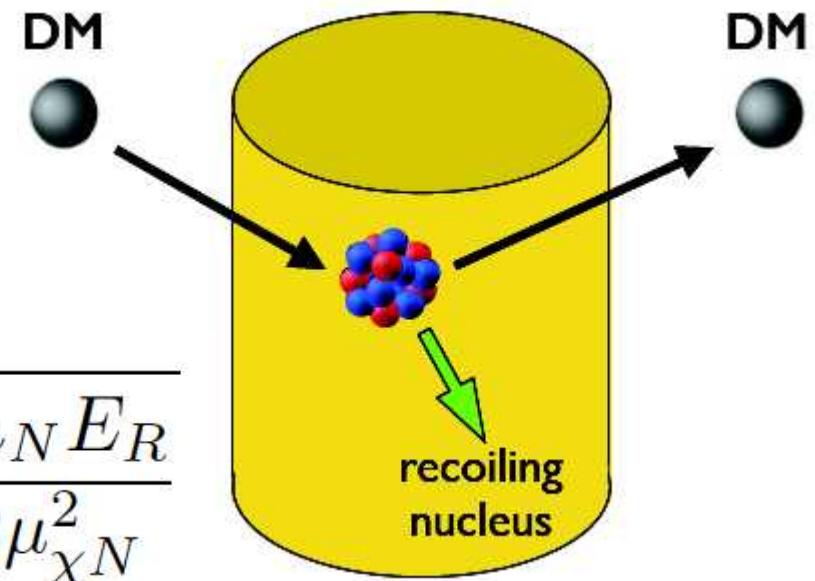
$$E_R = \frac{2\mu_{\chi N}^2 v^2}{m_N} \cos^2 \theta$$

- Minimum WIMP speed required to produce a recoil energy

$$v_{\min} = \sqrt{\frac{m_N E_R}{2\mu_{\chi N}^2}}$$

- The differential event rate (per unit detector mass):

$$\frac{dR}{dE_R} = \frac{\rho_\chi}{m_\chi m_N} \int_{v > v_{\min}} d^3 v \frac{d\sigma_{\chi N}}{dE_R} v f_{\text{det}}(\mathbf{v}, t)$$



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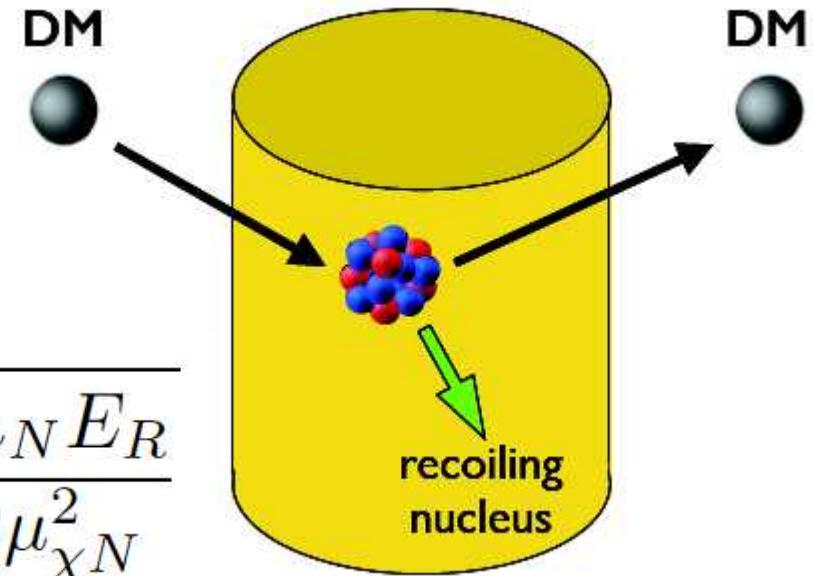
$$\frac{dR}{dE_R} = \frac{\sigma_0 F^2(E_R)}{2m_\chi \mu_{\chi N}^2}$$

astrophysics

$$\rho_\chi \eta(v_{\min}, t)$$

particle physics

halo integral

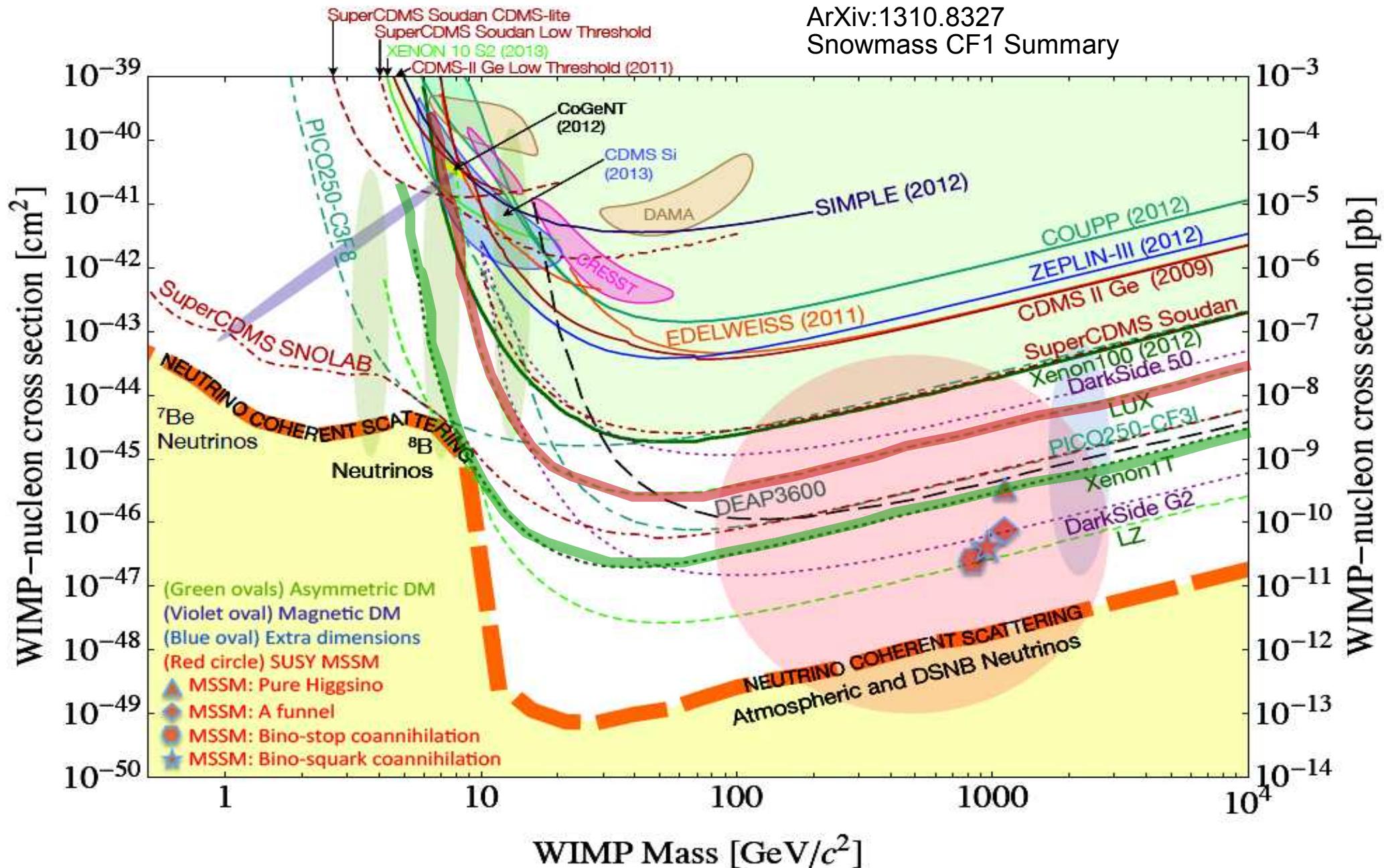


DM DD experiments



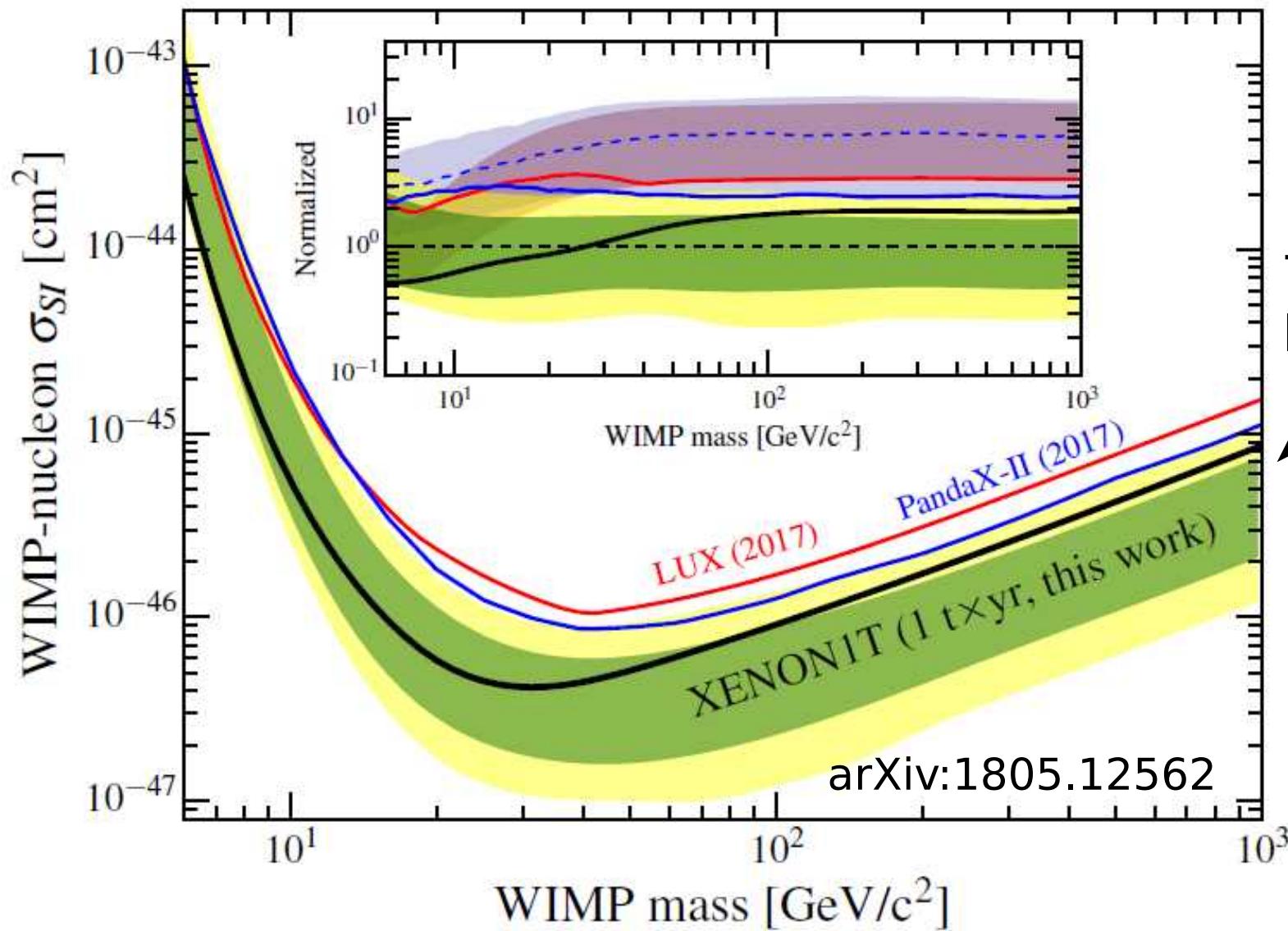
Power of DM DD to rule out theory space

ArXiv:1310.8327
Snowmass CF1 Summary



Latest XENON 1T results

$$10^{-46} \text{ cm}^2 = 10^{-10} \text{ pb}$$

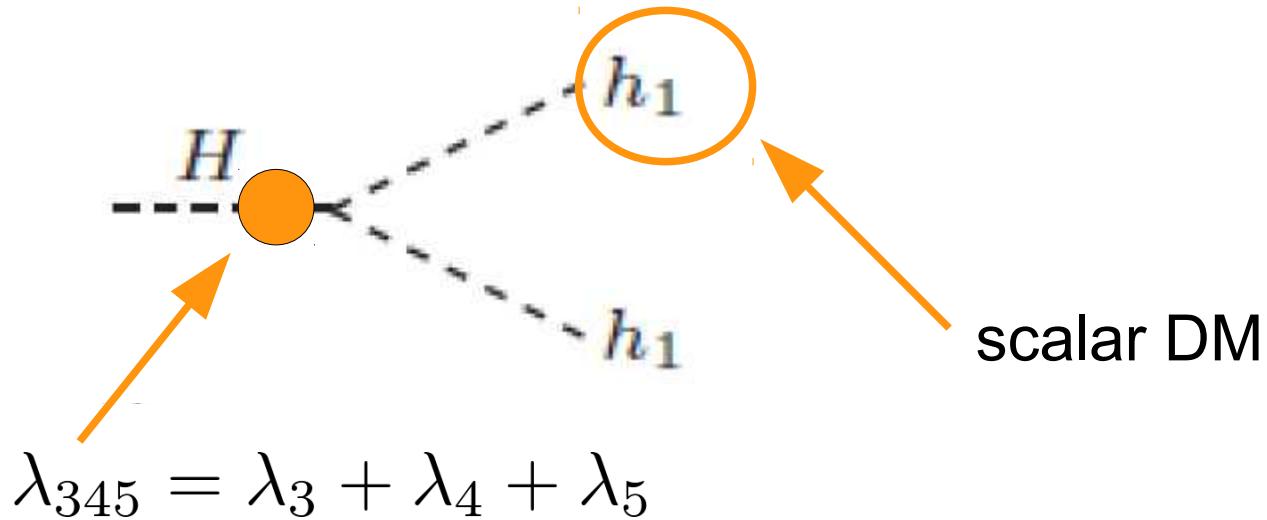


Power of DM DD to rule out theory space

Inert 2 Higgs Doublet Model

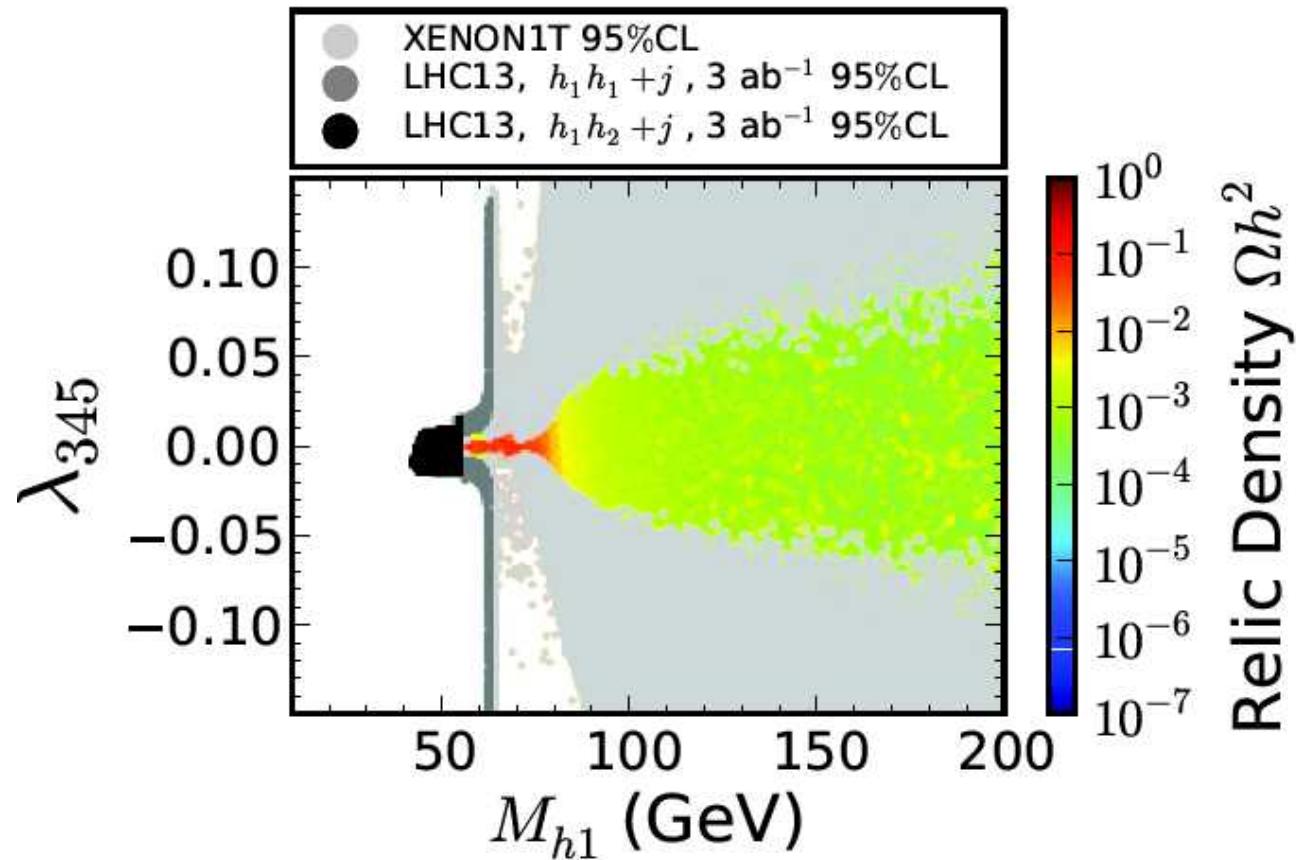
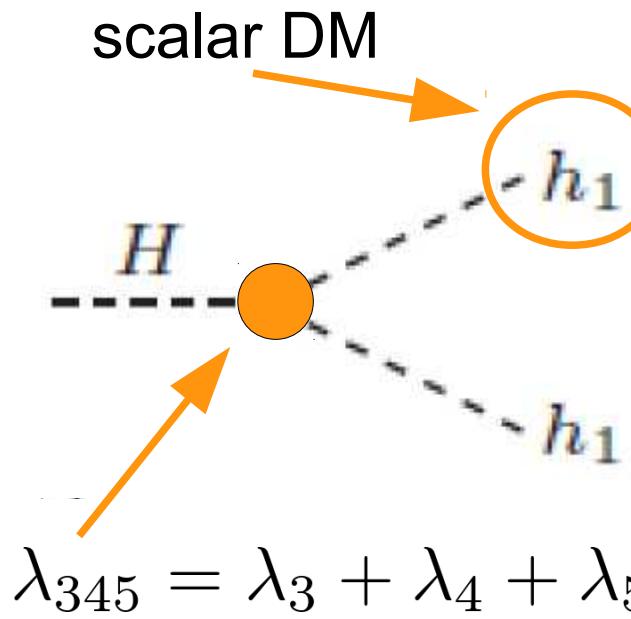
$$\phi_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + H \end{pmatrix} \quad \phi_2 = \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2}h^+ \\ h_1 + ih_2 \end{pmatrix}$$

$$V = -m_1^2(\phi_1^\dagger \phi_1) - m_2^2(\phi_2^\dagger \phi_2) + \lambda_1(\phi_1^\dagger \phi_1)^2 + \lambda_2(\phi_2^\dagger \phi_2)^2 + \lambda_3(\phi_1^\dagger \phi_1)(\phi_2^\dagger \phi_2) + \lambda_4(\phi_2^\dagger \phi_1)(\phi_1^\dagger \phi_2) + \frac{\lambda_5}{2} \left[(\phi_1^\dagger \phi_2)^2 + (\phi_2^\dagger \phi_1)^2 \right]$$



Power of DM DD to rule out theory space

Inert 2 Higgs Doublet Model



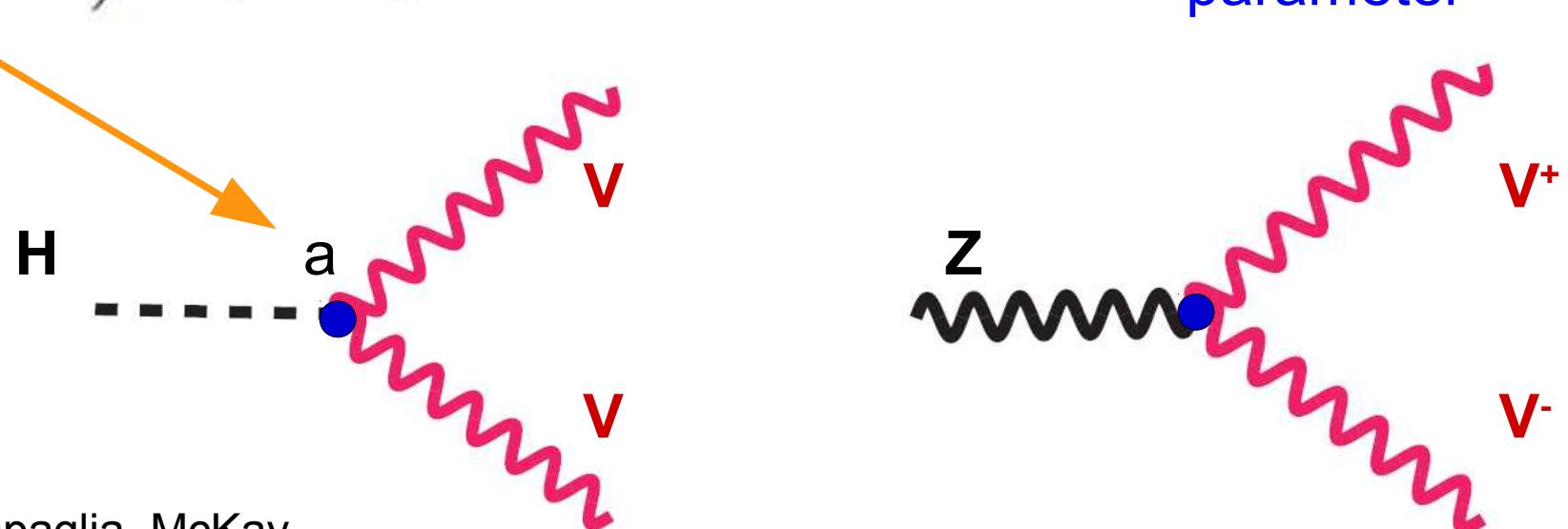
AB, G. Cacciapaglia, I. Ivanov, F. Rojas,
M. Thomas, 2017

Power of DM DD to rule out theory space

Vector DM Model

$$\begin{aligned}\mathcal{L} = & \mathcal{L}_{SM} - Tr \{ D_\mu V_\nu D^\mu V^\nu \} + Tr \{ D_\mu V_\nu D^\nu V^\mu \} \\ & - \frac{g^2}{2} Tr \{ [V_\mu, V_\nu] [V^\mu, V^\nu] \} \\ & - ig Tr \{ W_{\mu\nu} [V^\mu, V^\nu] \} + \tilde{M}^2 Tr \{ V_\nu V^\nu \} \\ & + a (\Phi^\dagger \Phi) Tr \{ V_\nu V^\nu \}\end{aligned}$$

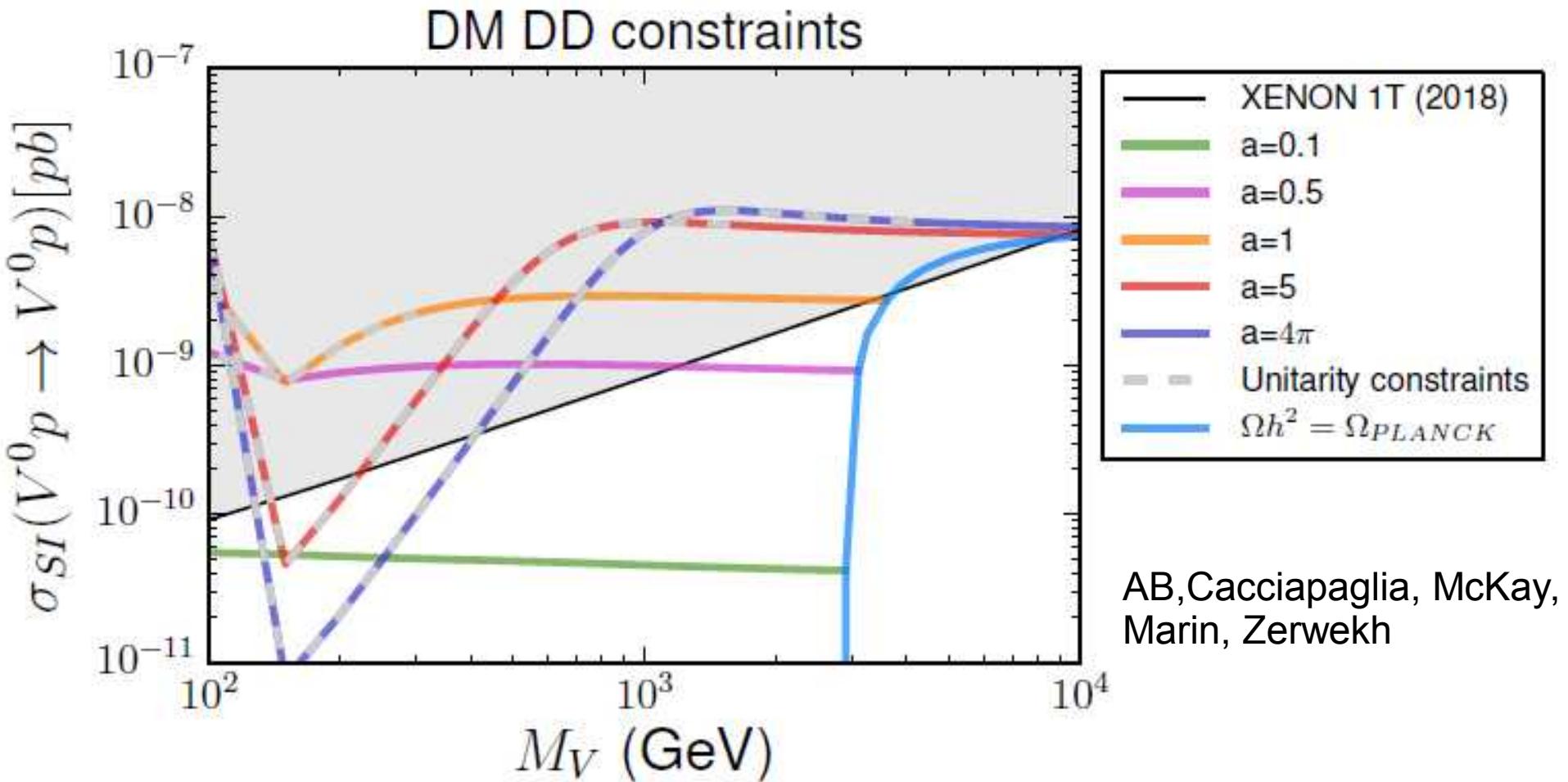
- DM from vector triplet
- SM gauge coupling
- $V_{DM} V_{DM} H$ coupling is the only free parameter



AB,Cacciapaglia, McKay,
Marin, Zerwekh

Power of DM DD to rule out theory space

Vector DM Model

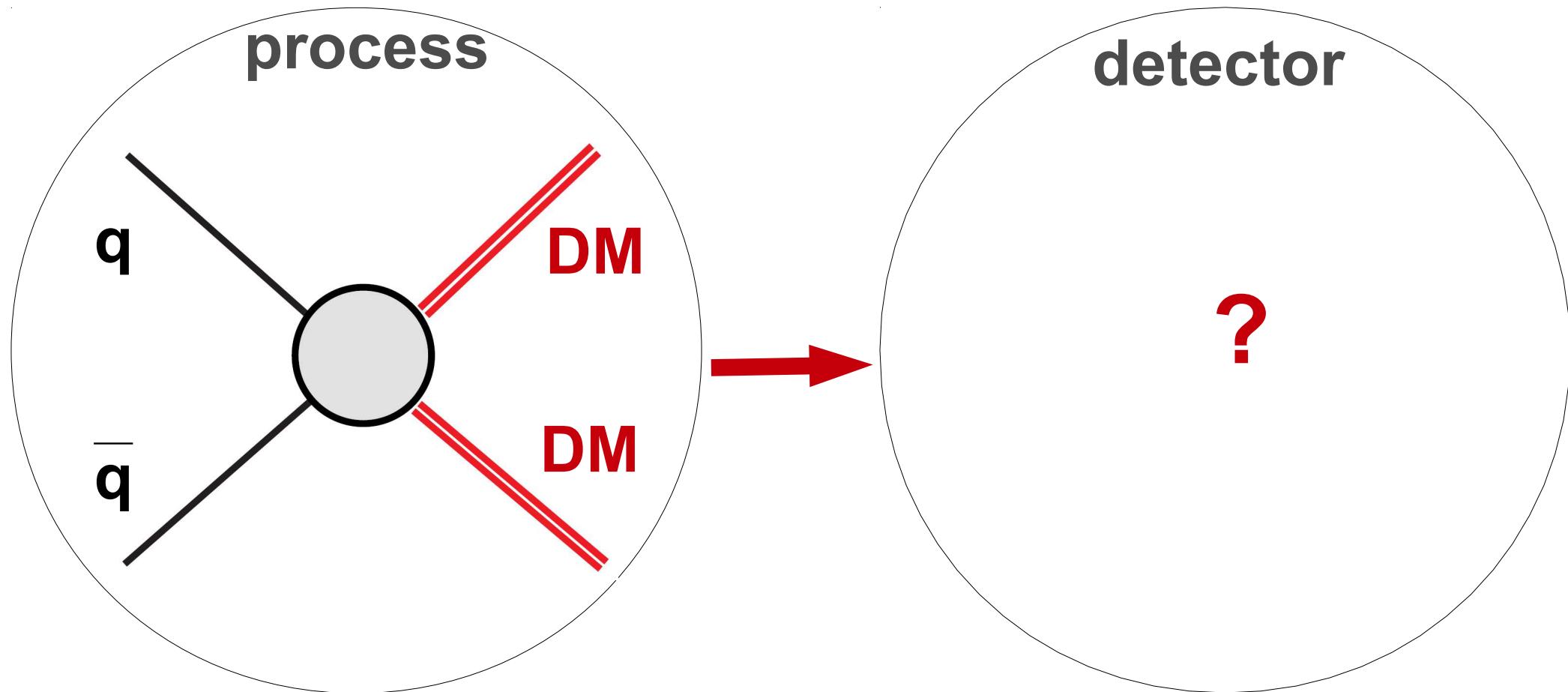


- ZENON 1T excludes **both** large HV_{DM}V_{DM} couplings and large M_{DM}
- The **rest** of the parameter space can be covered at future colliders

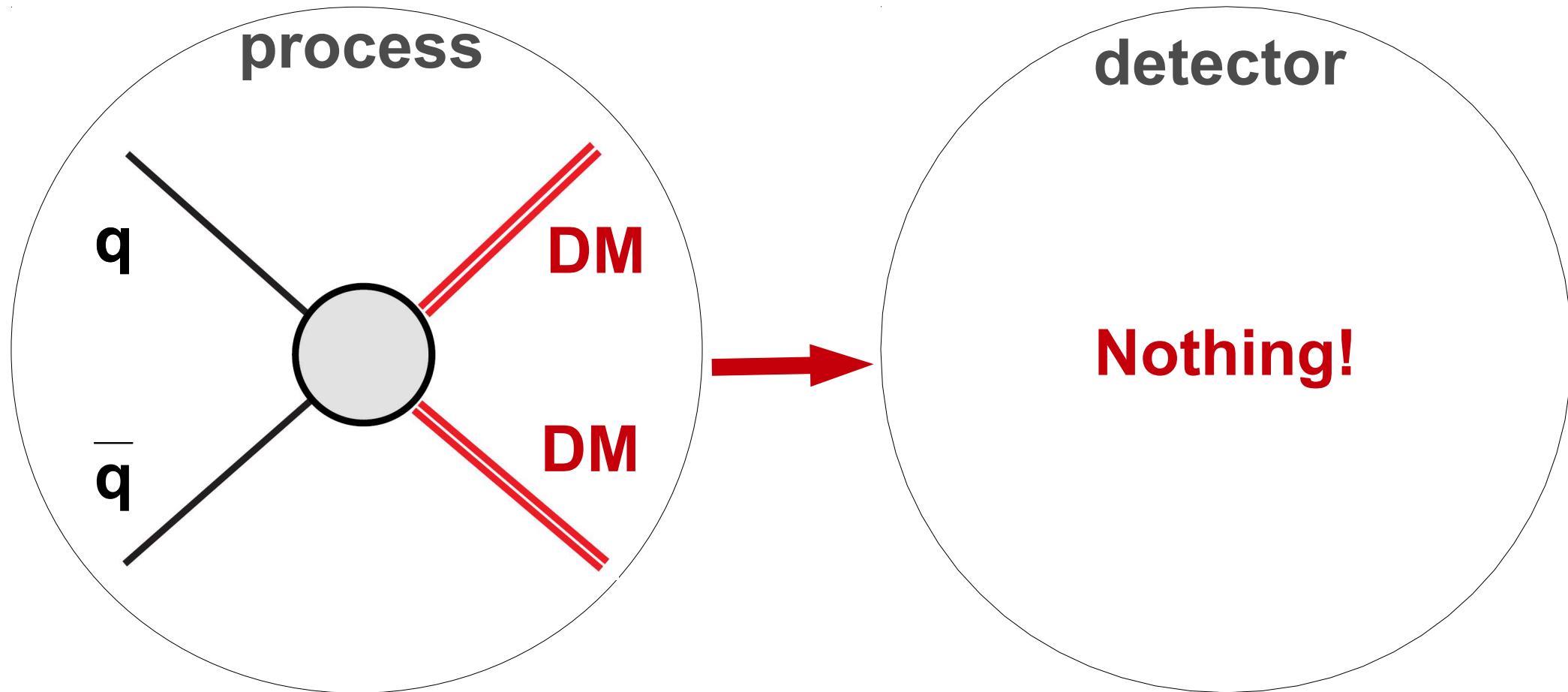
Power of DM DD to rule out theory space

- DM Interaction with SM particles is very limited
- E.g. coupling of Dirac Fermion DM interaction with Z-boson is excluded above **10⁻³** level with DM DD searches
- Majorana Fermion DM does not have this problem, the limit comes from Higgs interactions, the coupling above **0.1** is excluded

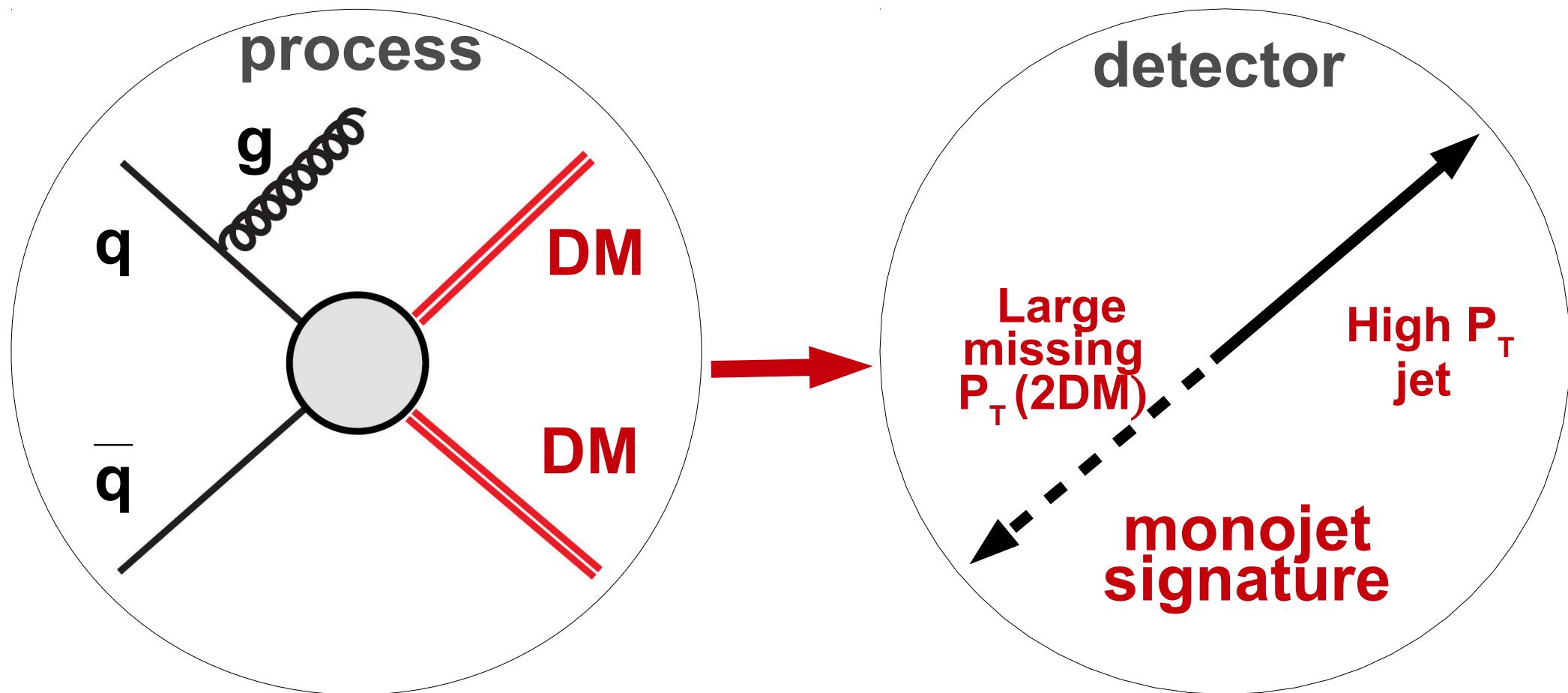
DM DD interplay with Collider Searches



Hunting for DM at Colliders



Hunting for DM at Colliders



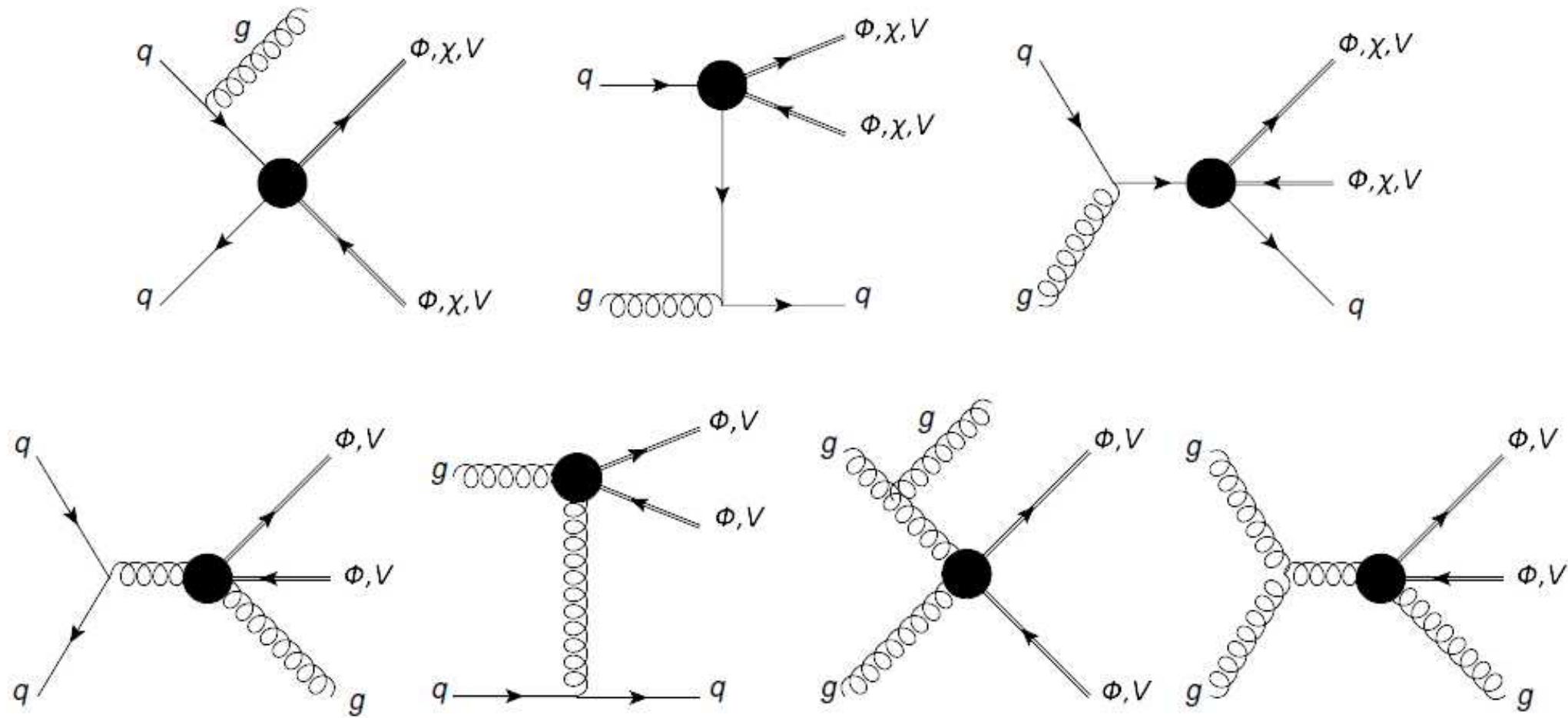
Can we test DM properties at the LHC?

Let us check the effects of DM spin on Missing transverse momentum (**MET**) distributions at the LHC:

- we use the EFT approach: simplicity and model independence
- explore the complete set of DIM5/DIM6 operators involving two SM quarks (gluons) and two DM particles
- consider DM with spin=0, 1/2, 1
- use mono-jet signature at the LHC

The aim: to find LHC discovery potential for scenarios with different DM spins and potential to distinguish these scenarios

Mono-jet diagrams from EFT operators



DIM5/6 operators (spin 0,1/2,1)

Complex scalar DM [†]	
$\frac{\tilde{m}}{\Lambda^2} \phi^\dagger \phi \bar{q} q$	[C1]*
$\frac{\tilde{m}}{\Lambda^2} \phi^\dagger \phi \bar{q} i\gamma^5 q$	[C2]*
$\frac{1}{\Lambda^2} \phi^\dagger i \overleftrightarrow{\partial}_\mu \phi \bar{q} \gamma^\mu q$	[C3]
$\frac{1}{\Lambda^2} \phi^\dagger i \overleftrightarrow{\partial}_\mu \phi \bar{q} \gamma^\mu \gamma^5 q$	[C4]
$\frac{1}{\Lambda^2} \phi^\dagger \phi G^{\mu\nu} G_{\mu\nu}$	[C5]*
$\frac{1}{\Lambda^2} \phi^\dagger \phi \tilde{G}^{\mu\nu} G_{\mu\nu}$	[C6]*

Dirac fermion DM [†]	
$\frac{1}{\Lambda^2} \bar{\chi} \chi \bar{q} q$	[D1]*
$\frac{1}{\Lambda^2} \bar{\chi} i\gamma^5 \chi \bar{q} q$	[D2]*
$\frac{1}{\Lambda^2} \bar{\chi} \chi \bar{q} i\gamma^5 q$	[D3]*
$\frac{1}{\Lambda^2} \bar{\chi} \gamma^5 \chi \bar{q} \gamma^5 q$	[D4]*
$\frac{1}{\Lambda^2} \bar{\chi} \gamma^\mu \chi \bar{q} \gamma_\mu q$	[D5]
$\frac{1}{\Lambda^2} \bar{\chi} \gamma^\mu \gamma^5 \chi \bar{q} \gamma_\mu q$	[D6]
$\frac{1}{\Lambda^2} \bar{\chi} \gamma^\mu \chi \bar{q} \gamma_\mu \gamma^5 q$	[D7]
$\frac{1}{\Lambda^2} \bar{\chi} \gamma^\mu \gamma^5 \chi \bar{q} \gamma_\mu \gamma^5 q$	[D8]
$\frac{1}{\Lambda^2} \bar{\chi} \sigma^{\mu\nu} \chi \bar{q} \sigma_{\mu\nu} q$	[D9]*
$\frac{1}{\Lambda^2} \bar{\chi} \sigma^{\mu\nu} i\gamma^5 \chi \bar{q} \sigma_{\mu\nu} q$	[D10]*

Complex vector DM [‡]	
$\frac{\tilde{m}}{\Lambda^2} V_\mu^\dagger V^\mu \bar{q} q$	[V1]*
$\frac{\tilde{m}}{\Lambda^2} V_\mu^\dagger V^\mu \bar{q} i\gamma^5 q$	[V2]*
$\frac{1}{2\Lambda^2} (V_\nu^\dagger \partial_\mu V^\nu - V^\nu \partial_\mu V_\nu^\dagger) \bar{q} \gamma^\mu q$	[V3]
$\frac{1}{2\Lambda^2} (V_\nu^\dagger \partial_\mu V^\nu - V^\nu \partial_\mu V_\nu^\dagger) \bar{q} i\gamma^\mu \gamma^5 q$	[V4]
$\frac{\tilde{m}}{\Lambda^2} V_\mu^\dagger V_\nu \bar{q} i\sigma^{\mu\nu} q$	[V5]
$\frac{\tilde{m}}{\Lambda^2} V_\mu^\dagger V_\nu \bar{q} \sigma^{\mu\nu} \gamma^5 q$	[V6]
$\frac{1}{2\Lambda^2} (V_\nu^\dagger \partial^\nu V_\mu + V^\nu \partial^\nu V_\mu^\dagger) \bar{q} \gamma^\mu q$	[V7P]
$\frac{1}{2\Lambda^2} (V_\nu^\dagger \partial^\nu V_\mu - V^\nu \partial^\nu V_\mu^\dagger) \bar{q} i\gamma^\mu q$	[V7M]
$\frac{1}{2\Lambda^2} (V_\nu^\dagger \partial^\nu V_\mu + V^\nu \partial^\nu V_\mu^\dagger) \bar{q} \gamma^\mu \gamma^5 q$	[V8P]
$\frac{1}{2\Lambda^2} (V_\nu^\dagger \partial^\nu V_\mu - V^\nu \partial^\nu V_\mu^\dagger) \bar{q} i\gamma^\mu \gamma^5 q$	[V8M]
$\frac{1}{2\Lambda^2} \epsilon^{\mu\nu\rho\sigma} (V_\nu^\dagger \partial_\rho V_\sigma + V_\nu \partial_\rho V_\sigma^\dagger) \bar{q} \gamma_\mu q$	[V9P]
$\frac{1}{2\Lambda^2} \epsilon^{\mu\nu\rho\sigma} (V_\nu^\dagger \partial^\nu V_\mu - V^\nu \partial^\nu V_\mu^\dagger) \bar{q} i\gamma_\mu q$	[V9M]
$\frac{1}{2\Lambda^2} \epsilon^{\mu\nu\rho\sigma} (V_\nu^\dagger \partial_\rho V_\sigma + V_\nu \partial_\rho V_\sigma^\dagger) \bar{q} \gamma_\mu \gamma^5 q$	[V10P]
$\frac{1}{2\Lambda^2} \epsilon^{\mu\nu\rho\sigma} (V_\nu^\dagger \partial^\nu V_\mu - V^\nu \partial^\nu V_\mu^\dagger) \bar{q} i\gamma_\mu \gamma^5 q$	[V10M]
$\frac{1}{\Lambda^2} V_\mu^\dagger V^\mu G^{\rho\sigma} G_{\rho\sigma}$	[V11]*
$\frac{1}{\Lambda^2} V_\mu^\dagger V^\mu \tilde{G}^{\rho\sigma} G_{\rho\sigma}$	[V12]*

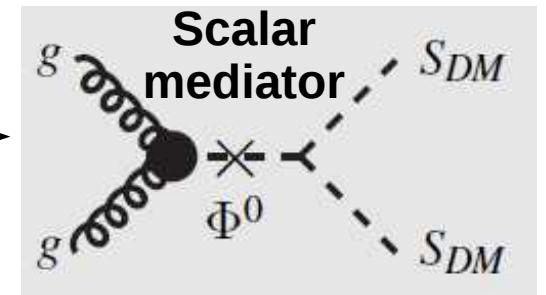
* operators applicable to real DM fields, modulo a factor 1/2

† Listed in J. Goodman *et al.*, *Constraints on Dark Matter from Colliders*, Phys. Rev. D82 (2010) 116010, [arXiv:1008.1783]

‡ All but V11 and V12 listed in Kumar *et al.*, *Vector dark matter at the LHC*, Phys. Rev. D92 (2015) 095027, [arXiv:1508.04466]

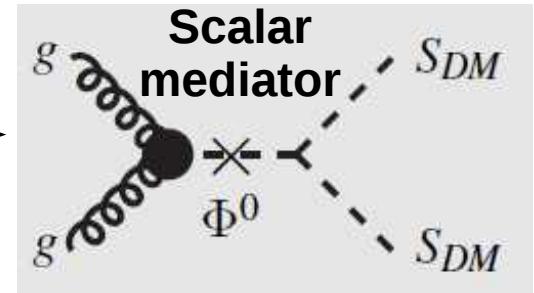
Mapping EFT operators to simplified models

C5,C5A $\frac{1}{\Lambda^2} \phi^* \phi G^{\mu\nu} G^{\mu\nu}, \quad \frac{1}{\Lambda^2} \phi^* \phi \tilde{G}^{\mu\nu} G^{\mu\nu}$ →



Mapping EFT operators to simplified models

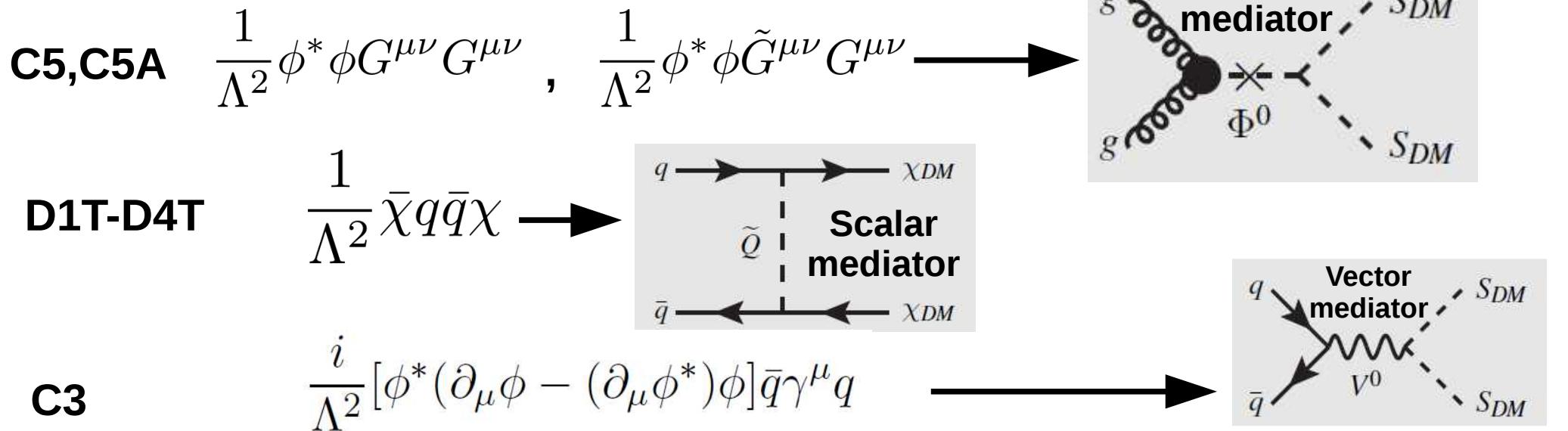
C5,C5A $\frac{1}{\Lambda^2} \phi^* \phi G^{\mu\nu} G^{\mu\nu}, \quad \frac{1}{\Lambda^2} \phi^* \phi \tilde{G}^{\mu\nu} G^{\mu\nu}$ →



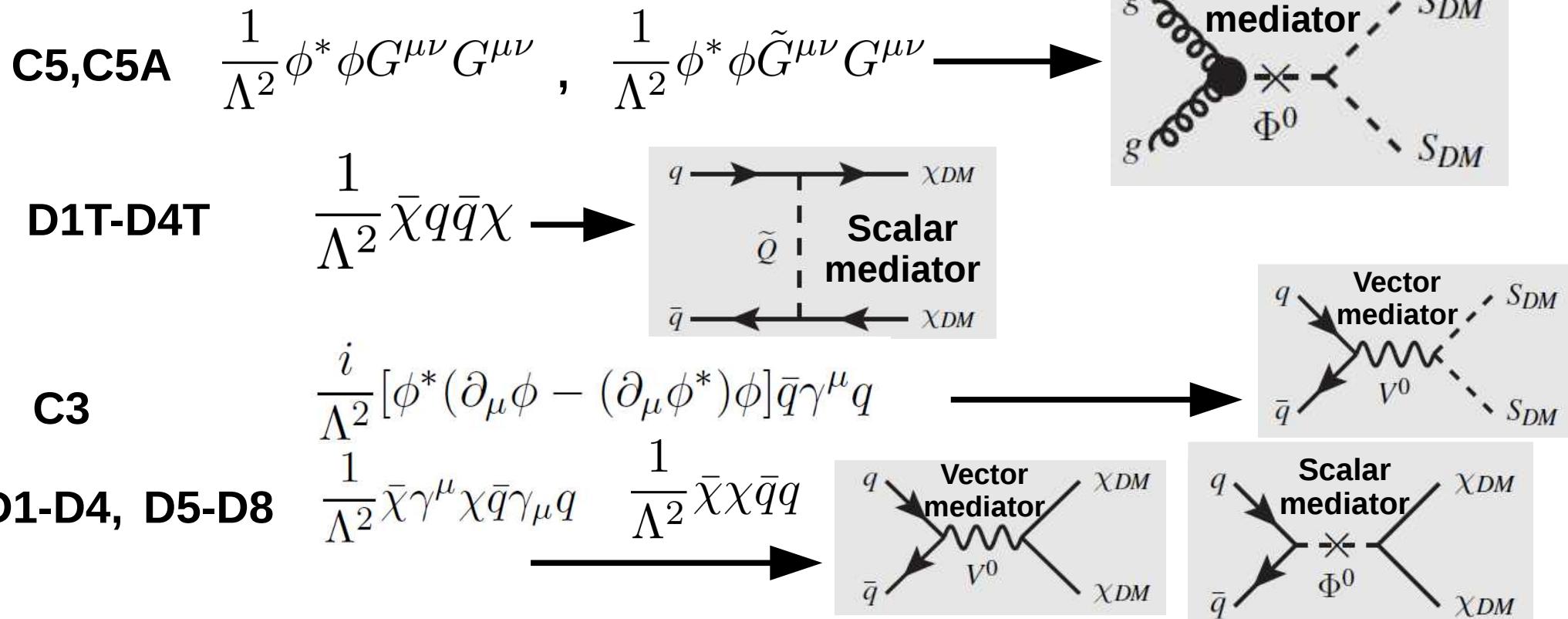
D1T-D4T $\frac{1}{\Lambda^2} \bar{\chi} q \bar{q} \chi$ →

Feynman diagram showing a quark q (solid line) and an antiquark \bar{q} (dashed line) interacting via a "Scalar mediator" (dashed line) to produce a scalar dark matter particle χ_{DM} (solid line). The label "Scalar mediator" is placed below the dashed line.

Mapping EFT operators to simplified models



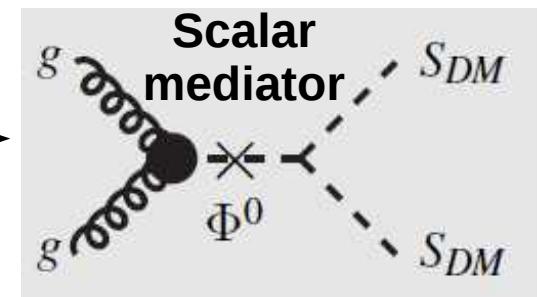
Mapping EFT operators to simplified models



Mapping EFT operators to simplified models

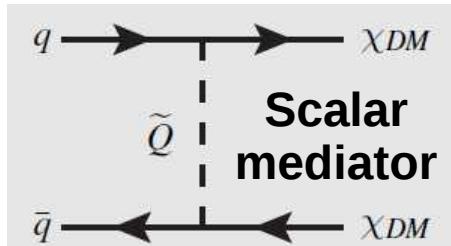
C5,C5A $\frac{1}{\Lambda^2} \phi^* \phi G^{\mu\nu} G^{\mu\nu}$

$$\frac{1}{\Lambda^2} \phi^* \phi \tilde{G}^{\mu\nu} G^{\mu\nu} \longrightarrow$$



D1T-D4T

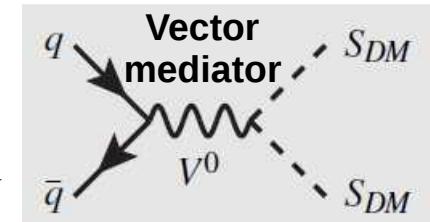
$$\frac{1}{\Lambda^2} \bar{\chi} q \bar{q} \chi \longrightarrow$$



C3

$$\frac{i}{\Lambda^2} [\phi^* (\partial_\mu \phi - (\partial_\mu \phi^*) \phi] \bar{q} \gamma^\mu q$$

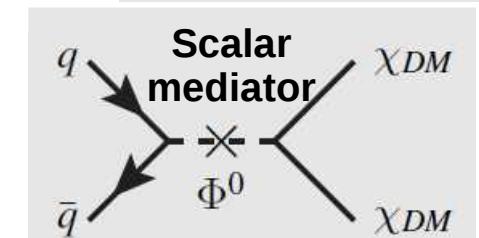
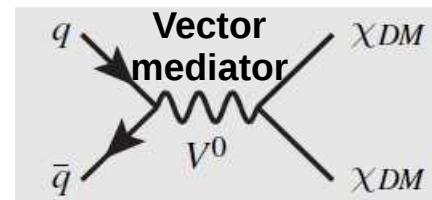
$$\longrightarrow$$



D1-D4, D5-D8

$$\frac{1}{\Lambda^2} \bar{\chi} \gamma^\mu \chi \bar{q} \gamma_\mu q \quad \frac{1}{\Lambda^2} \bar{\chi} \chi \bar{q} q$$

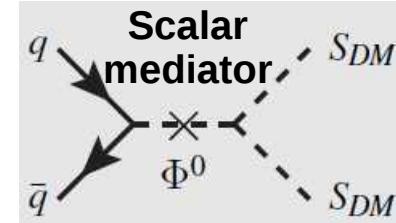
$$\longrightarrow$$



C1

$$\frac{1}{\Lambda^2} \phi^* \phi \bar{q} q \Phi \implies \frac{v}{\Lambda^2} \phi^* \phi \bar{q} q$$

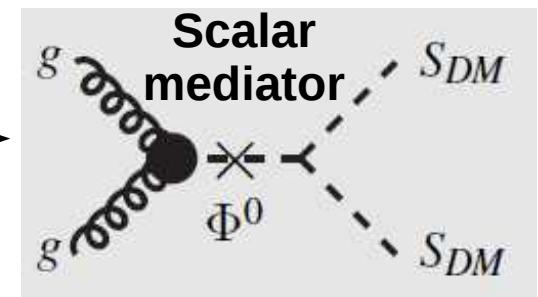
$$\longrightarrow$$



Mapping EFT operators to simplified models

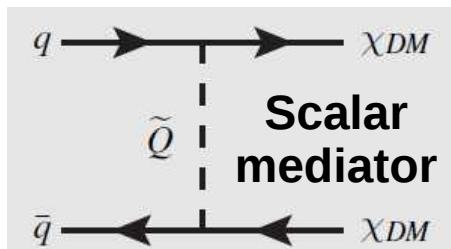
C5,C5A $\frac{1}{\Lambda^2} \phi^* \phi G^{\mu\nu} G^{\mu\nu}$

$$\frac{1}{\Lambda^2} \phi^* \phi \tilde{G}^{\mu\nu} G^{\mu\nu} \longrightarrow$$



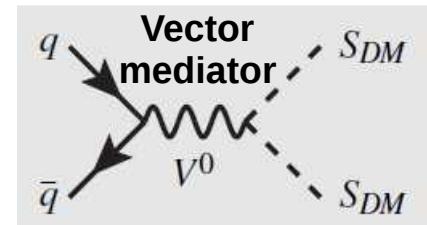
D1T-D4T

$$\frac{1}{\Lambda^2} \bar{\chi} q \bar{q} \chi \longrightarrow$$



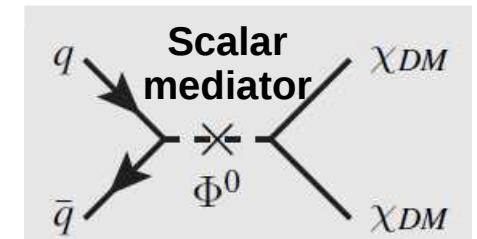
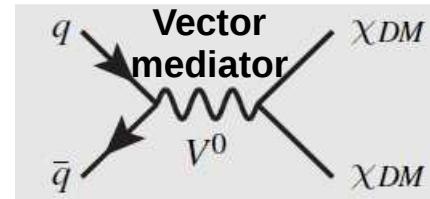
C3

$$\frac{i}{\Lambda^2} [\phi^* (\partial_\mu \phi - (\partial_\mu \phi^*) \phi] \bar{q} \gamma^\mu q$$



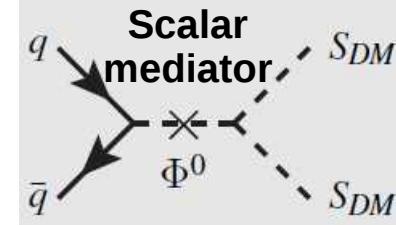
D1-D4, D5-D8

$$\frac{1}{\Lambda^2} \bar{\chi} \gamma^\mu \chi \bar{q} \gamma_\mu q \quad \frac{1}{\Lambda^2} \bar{\chi} \chi \bar{q} q$$



C1

$$\frac{1}{\Lambda^2} \phi^* \phi \bar{q} q \Phi \implies \frac{v}{\Lambda^2} \phi^* \phi \bar{q} q$$



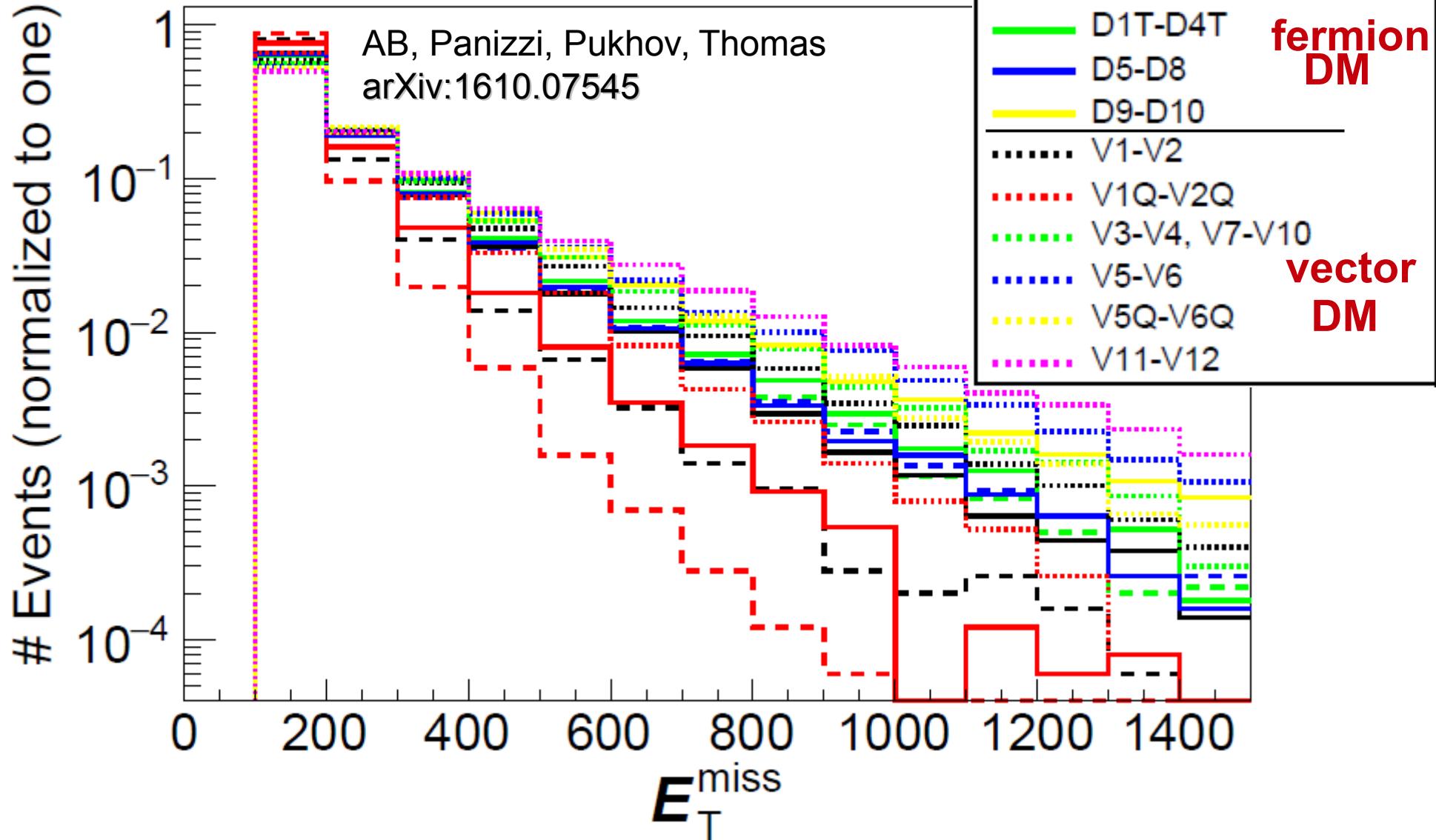
D9,D10

$$\frac{1}{\Lambda^2} \bar{\chi} \sigma^{\mu\nu} \chi \bar{q} \sigma_{\mu\nu} q \longrightarrow$$

$$\frac{8}{\Lambda^2} [\bar{\chi} q \bar{q} \chi - \frac{1}{4} (\bar{\chi} \chi \bar{q} q + \bar{\chi} \gamma^5 \chi \bar{q} \gamma^5 q + \bar{\chi} \gamma^\mu \chi \bar{q} \gamma_\mu q - \bar{\chi} \gamma^\mu \gamma^5 \chi \bar{q} \gamma_\mu \gamma^5 q)]$$

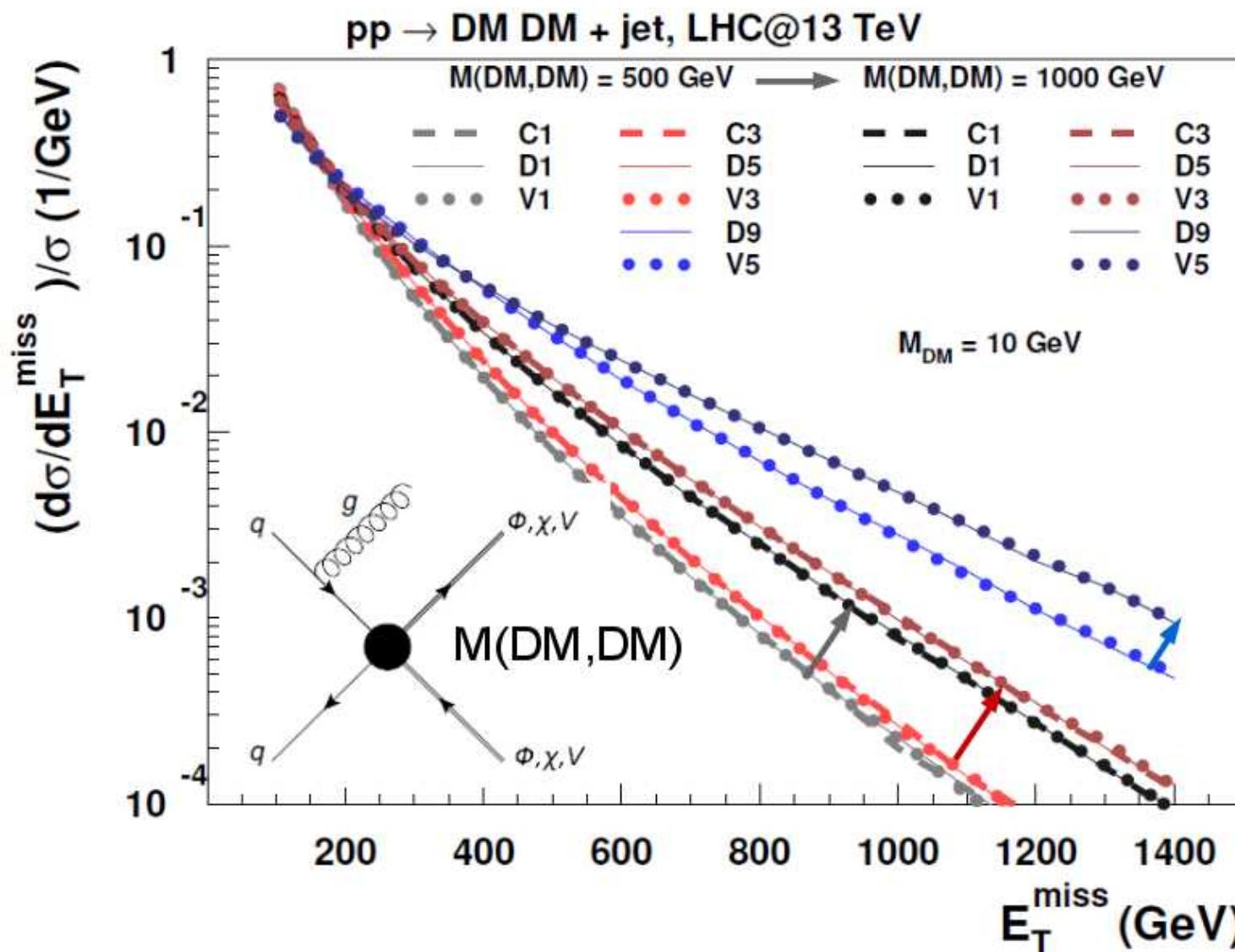
Missing E_T (MET) distributions: the large range of slopes

$M_{DM} = 10 \text{ GeV}$, $\sqrt{s} = 13 \text{ TeV}$



Properties of MET distributions:

- MET distributions are **the same** for the fixed mass of DM pair [$M(DM,DM)$] & **fixed SM operator**
- With the **increase of $M(DM,DM)$** , MET slope decreases (PDF effect)



$$\frac{\tilde{m}}{\Lambda^2} \phi^* \phi \bar{q} q \quad [\text{C1}]$$

$$\frac{1}{\Lambda^2} \bar{\chi} \chi \bar{q} q \quad [\text{D1}]$$

$$\frac{\tilde{m}}{\Lambda^2} V^\dagger \mu V_\mu \bar{q} q \quad [\text{V1}]$$

$$\frac{1}{\Lambda^2} \phi^\dagger i \overleftrightarrow{\partial}_\mu \phi \bar{q} \gamma^\mu q \quad [\text{C3}]$$

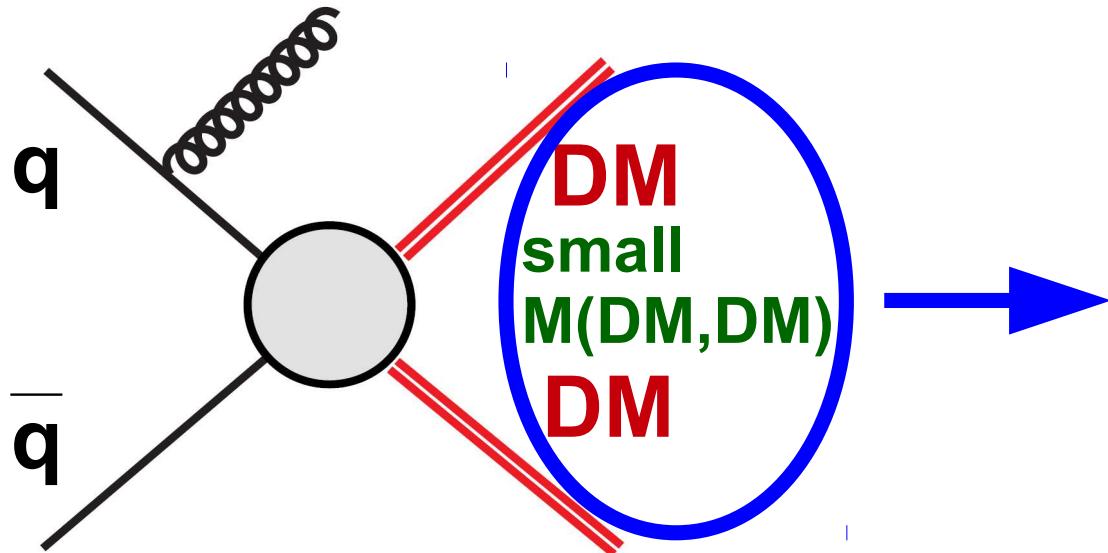
$$\frac{1}{\Lambda^2} \bar{\chi} \gamma^\mu \chi \bar{q} \gamma_\mu q \quad [\text{D5}]$$

$$\frac{1}{\Lambda^2} \bar{\chi} \sigma^{\mu\nu} \chi \bar{q} \sigma_{\mu\nu} q \quad [\text{D9}]$$

$$\frac{\tilde{m}}{\Lambda^2} V_\mu^\dagger V_\nu \bar{q} i \sigma^{\mu\nu} q \quad [\text{V5}]$$

Properties of MET distributions for small and large M(DM,DM)

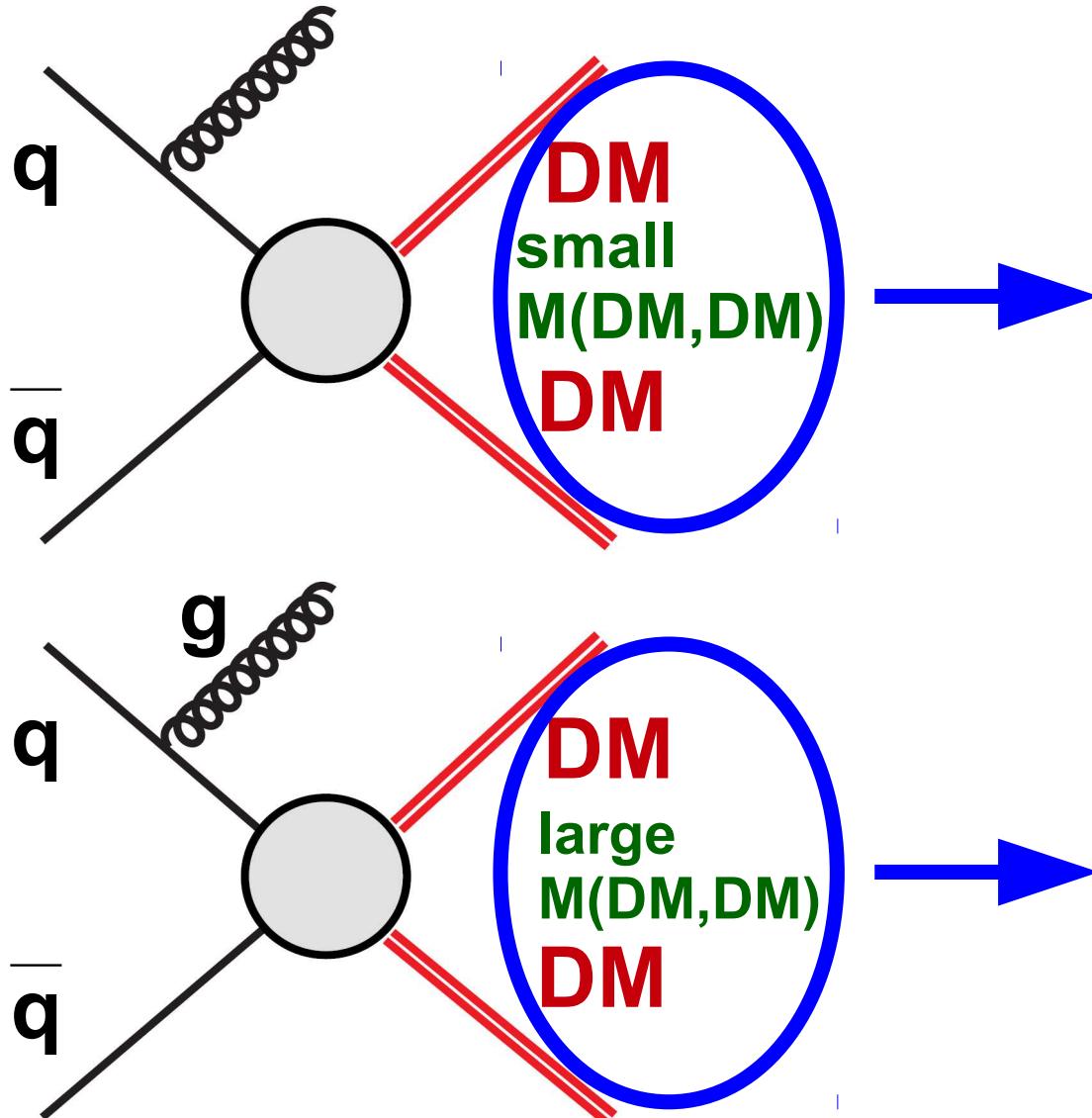
- MET distributions are **the same** for the **fixed mass** of DM pair [M(DM,DM)] & **fixed SM operator**
- With the **increase** of M(DM,DM), MET slope decreases (PDF effect)



for $p_T(g)$ increase
 $\Delta (x_1 x_2)/(x_1 x_2)$ is large
and MET slope is steep

Properties of MET distributions for small and large M(DM,DM)

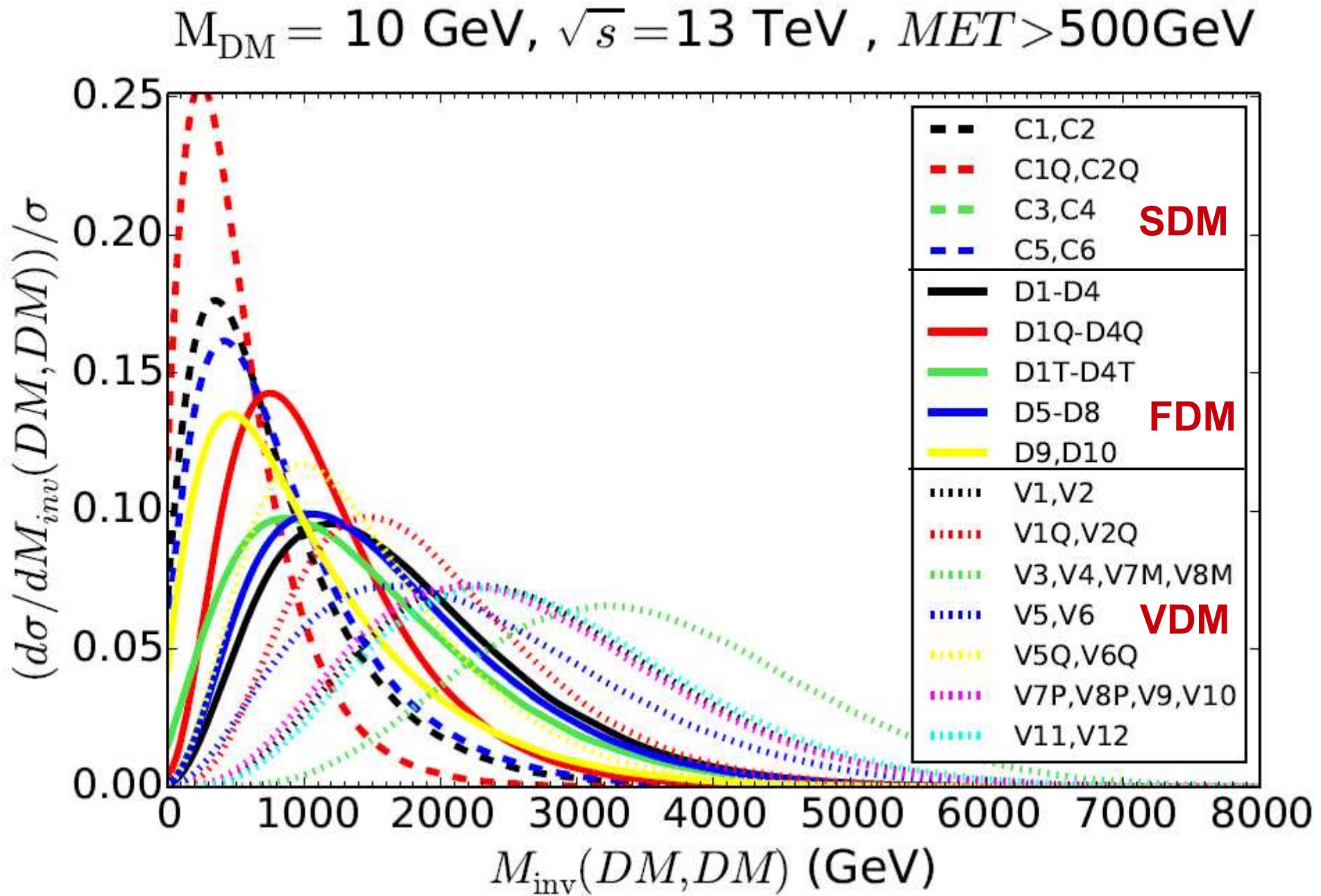
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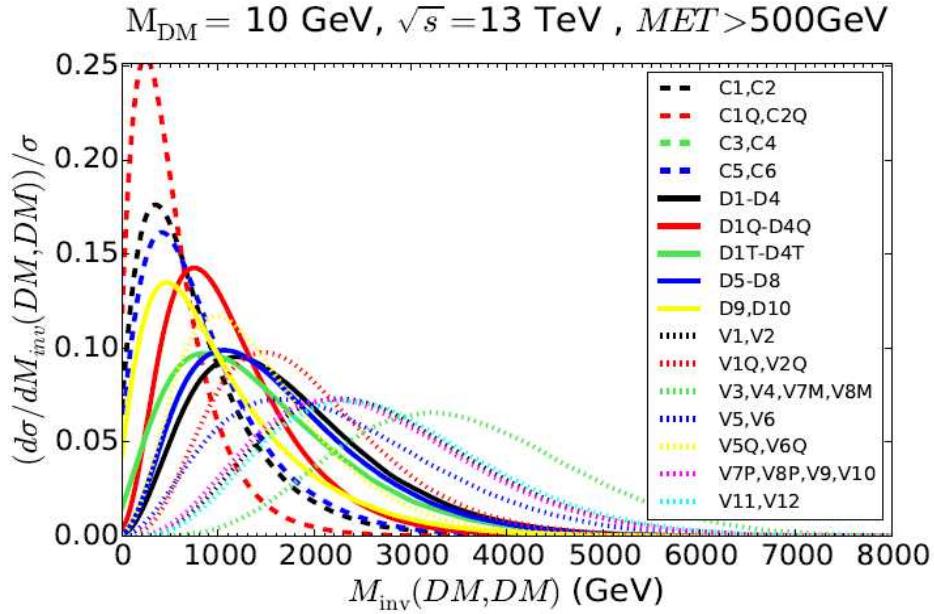
for $p_T(g)$ increase
 $\Delta (x_1 x_2)/(x_1 x_2)$ is small
and MET slope is gradual

On the other hand, $M(DM,DM)$ distributions, defined by the EFT operators are different!

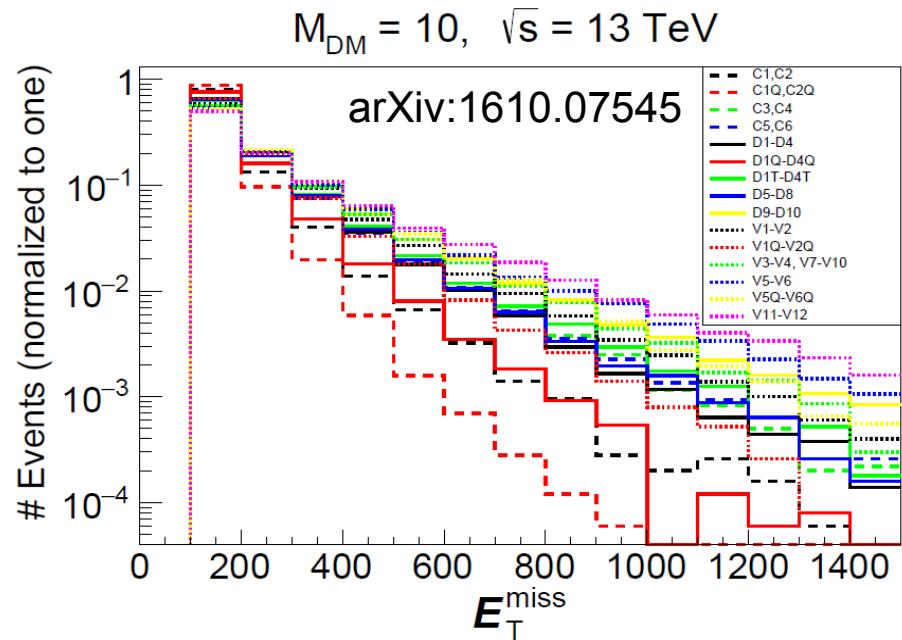


Distinguishing DM operators/theories

The harder M(DM,DM) distributions



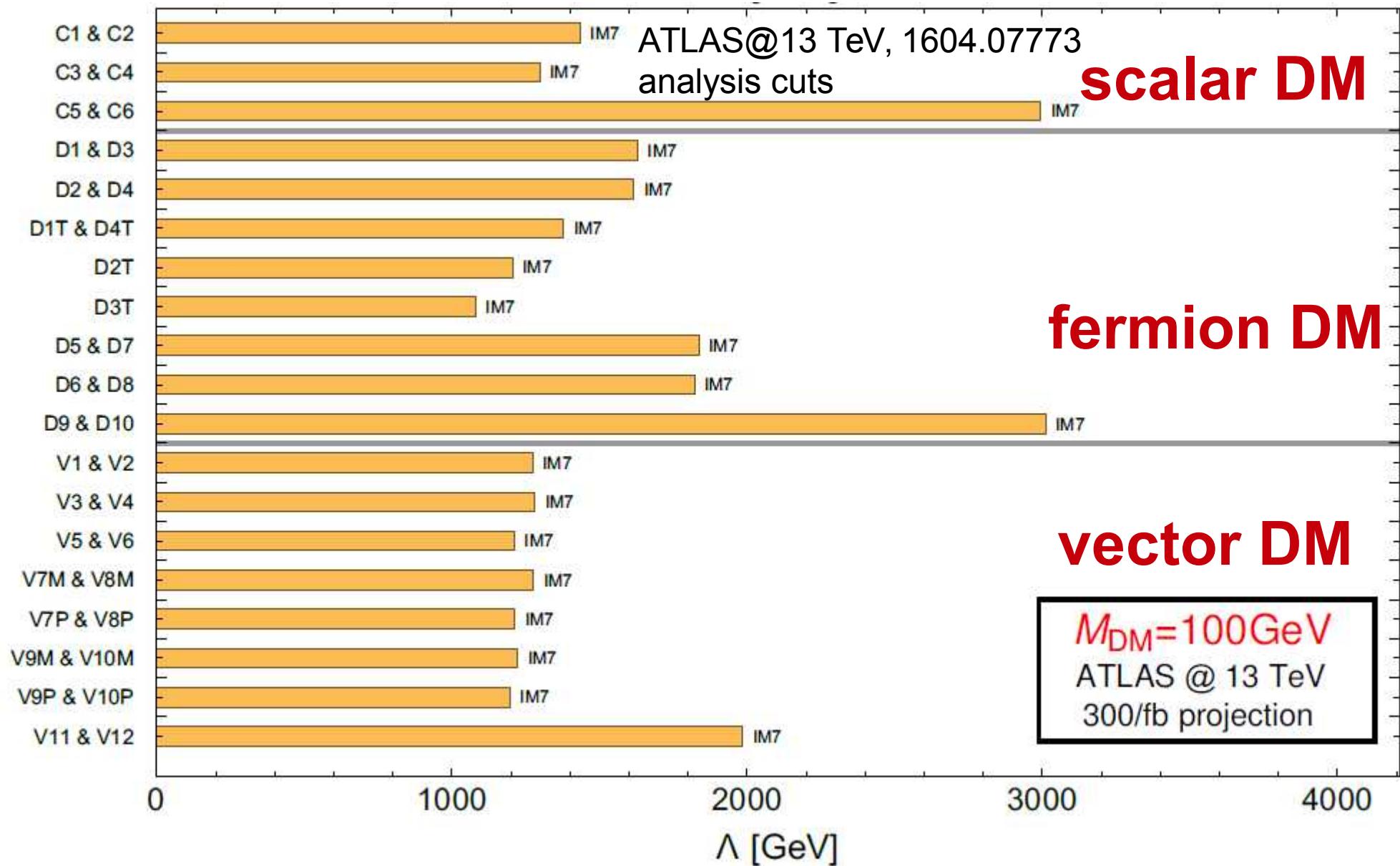
The flatter MET shapes



- ⇒ energy dependence of the DM operator → $M_{\text{DM}\text{DM}}$ distributions → slopes of MET
- ⇒ projection for 300 fb^{-1} : some operators C1-C2,C5-C6,D9-D10,V1-V2,V3-V4,V5-V6 and V11-12 can be distinguished from each other
- ⇒ Application beyond EFT: when the DM mediator is not produced on-the-mass-shell and $M_{\text{DM}\text{DM}}$ is not fixed: t-channel mediator or mediators with mass below $2M_{\text{DM}}$

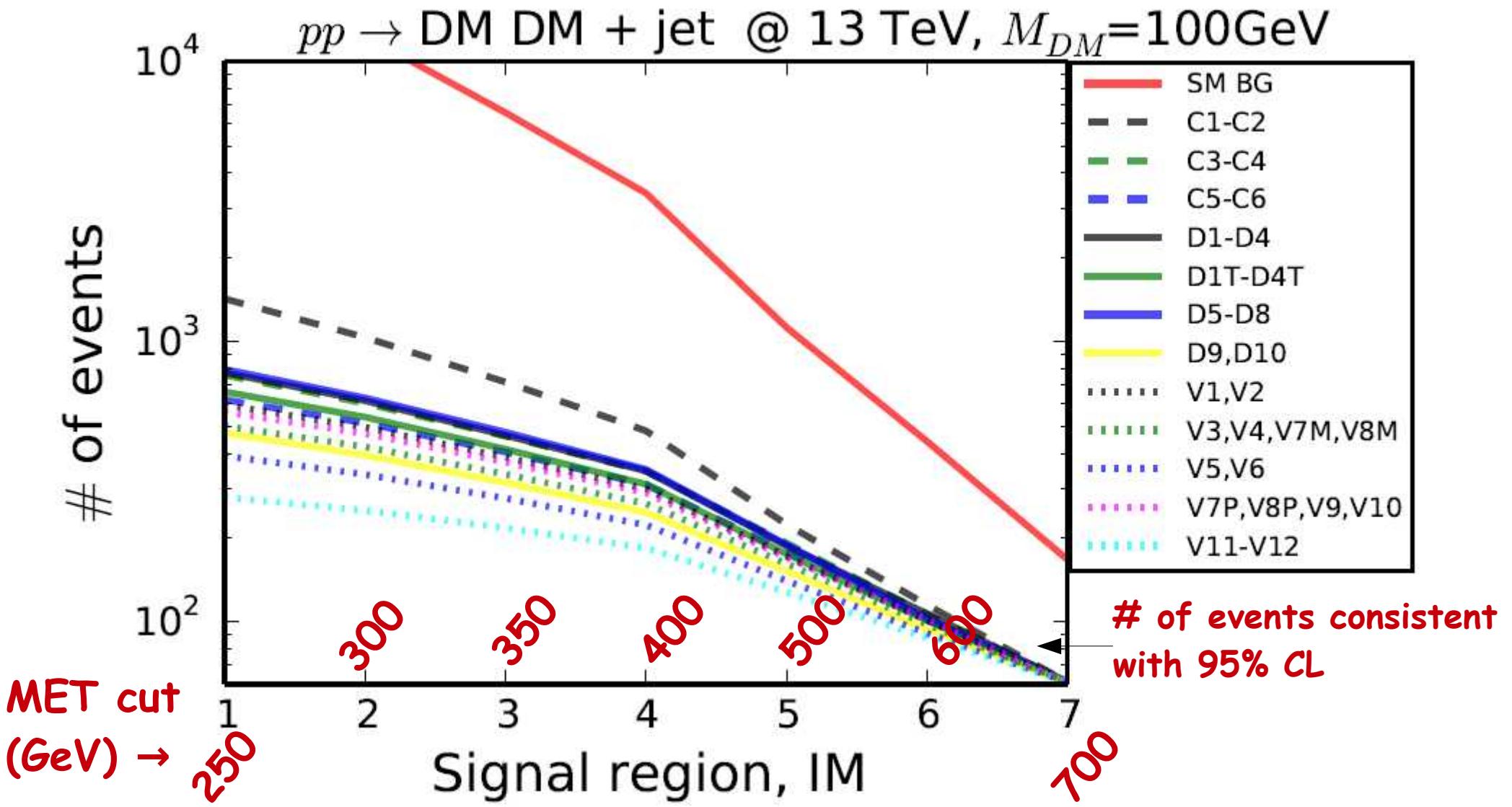
LHC@13TeV reach projected 100 fb^{-1}

LanHEP → CalcHEP/ Madgraph → LHE → CheckMATE 2 chain



Distinguishing DM operators

energy dependence of the operator → $M_{DM\bar{D}M}$ shape → MET shape



Distinguishing the DM operators: χ^2 for pairs of DM operators

$$\chi^2_{k,l} = \min_{\kappa} \sum_{i=3}^7 [(\frac{1}{2}N_i^k - \kappa \cdot N_i^l)/(10^{-2}BG_i)]^2$$

: if $\chi^2 > 9.48$ (95%CL for 4 DOF) – operators can be distinguished!

			Complex Scalar DM				Dirac Fermion DM			
			100 GeV		1000 GeV		100 GeV		1000 GeV	
			C1	C5	C1	C5	D1	D9	D1	D9
Complex Scalar	100	C1	0.0	19.7	25.54	74.63	11.73	41.79	25.78	52.58
	GeV	C5	15.74	0.0	0.37	16.25	1.11	3.93	0.74	7.35
DM	1000	C1	19.89	0.36	0.0	11.82	2.33	2.09	0.27	4.58
	GeV	C5	50.86	13.86	10.34	0.0	21.03	3.7	11.18	1.53
Dirac Fermion	100	D1	9.88	1.17	2.52	25.99	0.0	9.23	2.4	14.17
	GeV	D9	30.49	3.59	1.96	3.96	7.99	0.0	2.71	0.52
DM	1000	D1	20.31	0.73	0.27	12.92	2.25	2.93	0.0	5.42
	GeV	D9	37.38	6.54	4.18	1.6	11.96	0.5	4.89	0.0

Distinguishing the DM operators: χ^2 for pairs of DM operators

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		Complex Scalar DM				Dirac Fermion DM				Complex Vector DM								
		100 GeV		1000 GeV		100 GeV		1000 GeV		100 GeV		1000 GeV		1000 GeV		1000 GeV		
		C1	C5	C1	C5	D1	D9	D1	D9	V1	V3	V5	V11	V1	V3	V5	V11	
Complex Scalar DM	100 GeV	C1	0.0	19.7	25.54	74.63	11.73	41.79	25.78	52.58	22.97	32.89	54.35	73.34	25.18	34.61	52.34	80.85
		C5	15.74	0.0	0.37	16.25	1.11	3.93	0.74	7.35	0.18	1.53	8.2	15.73	0.44	1.9	7.24	19.13
	1000 GeV	C1	19.89	0.36	0.0	11.82	2.33	2.09	0.27	4.58	0.06	0.45	5.29	11.41	0.06	0.68	4.42	14.36
		C5	50.86	13.86	10.34	0.0	21.03	3.7	11.18	1.53	11.57	6.82	1.26	0.01	10.84	6.1	1.61	0.14
Dirac Fermion DM	100 GeV	D1	9.88	1.17	2.52	25.99	0.0	9.23	2.4	14.17	1.85	5.09	15.34	25.37	2.29	5.85	13.85	29.81
		D9	30.49	3.59	1.96	3.96	7.99	0.0	2.71	0.52	2.49	0.62	0.73	3.69	2.31	0.39	0.56	5.36
	1000 GeV	D1	20.31	0.73	0.27	12.92	2.25	2.93	0.0	5.42	0.32	0.82	6.33	12.58	0.08	1.18	5.08	15.7
		D9	37.38	6.54	4.18	1.6	11.96	0.5	4.89	0.0	4.98	2.02	0.06	1.44	4.56	1.61	0.04	2.55
Complex Vector DM		V1	18.06	0.17	0.06	13.34	1.72	2.68	0.32	5.5	0.0	0.77	6.25	12.9	0.1	1.06	5.34	16.03
	100 GeV	V3	24.86	1.45	0.44	7.57	4.57	0.65	0.79	2.14	0.74	0.0	2.68	7.25	0.57	0.03	2.04	9.59
		V5	38.36	7.24	4.79	1.3	12.86	0.7	5.67	0.06	5.61	2.5	0.0	1.14	5.24	2.04	0.13	2.13
		V11	50.03	13.43	10.0	0.01	20.55	3.45	10.89	1.39	11.2	6.54	1.11	0.0	10.52	5.83	1.49	0.16
	1000 GeV	V1	19.73	0.43	0.06	12.46	2.13	2.48	0.08	5.02	0.1	0.59	5.83	12.09	0.0	0.89	4.78	15.14
		V3	25.96	1.78	0.65	6.72	5.21	0.4	1.12	1.7	1.01	0.03	2.17	6.41	0.85	0.0	1.65	8.6
		V5	37.33	6.47	4.04	1.68	11.72	0.55	4.59	0.04	4.84	1.93	0.14	1.55	4.34	1.57	0.0	2.72
		V11	54.48	16.14	12.42	0.13	23.85	4.95	13.43	2.41	13.74	8.55	2.03	0.16	13.01	7.73	2.57	0.0

Importance of the operator running in the DM DD \leftrightarrow Collider interplay

- In case of axial operators, e.g

$$c_A^{(q)} c_\chi \bar{\chi} \gamma^\mu \chi \bar{q} \gamma_\mu \gamma_5 q \quad (D7) \quad \text{or} \quad c_A^{(q)} c_\phi \phi^\dagger \overleftrightarrow{\partial}_\mu \phi \bar{q} \gamma^\mu \gamma_5 q \quad (C4)$$

couplings $c_v^{(q)}$ arise due to the running of the wilson coefficient $c_A^{(q)}$
leading to sizable constraints on the DM DD constraints

Importance of the operator running in the DM DD \leftrightarrow Collider interplay

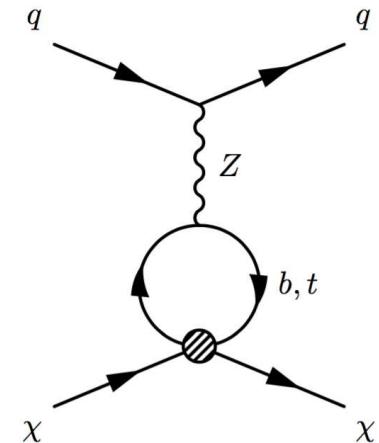
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- One can use **runDM** program (github.com/bradkav/runDM) by
F. D'Eramo, B. J. Kavanagh & P. Panci

$$c_A^{(u)}, c_A^{(d)}, c_v^{(u)}, c_v^{(d)} = (1, 1, 0, 0)[5\text{TeV}] \rightarrow (1.1, 1.1, 0.04, -0.07)[1\text{GeV}]$$



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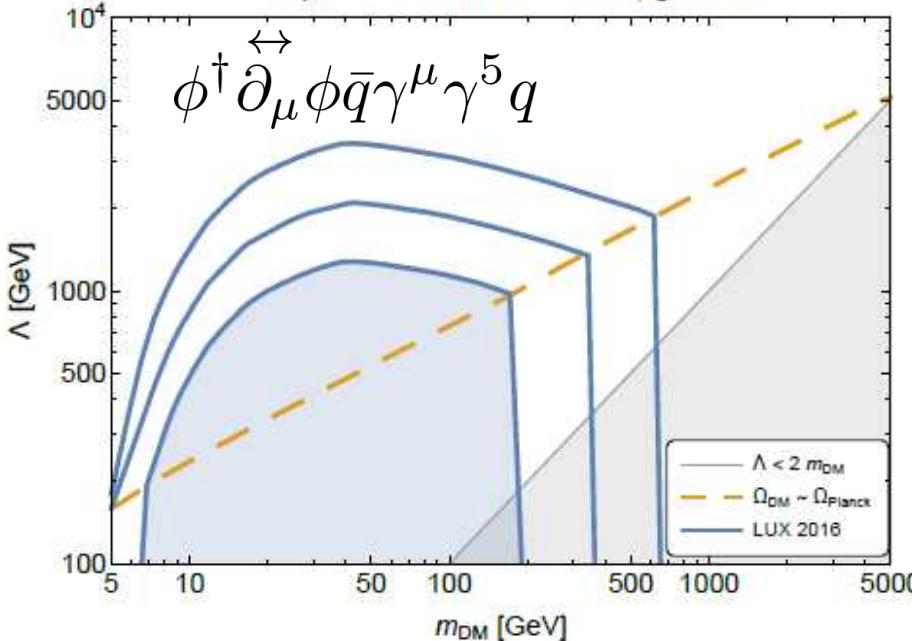
or $c_A^{(q)} c_\phi \phi^\dagger \not{\partial}_\mu \phi \bar{q} \gamma^\mu \gamma_5 q \quad (C4)$

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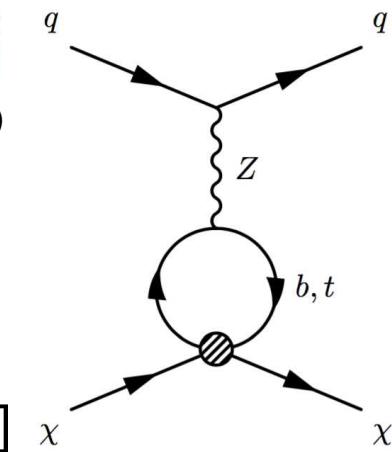
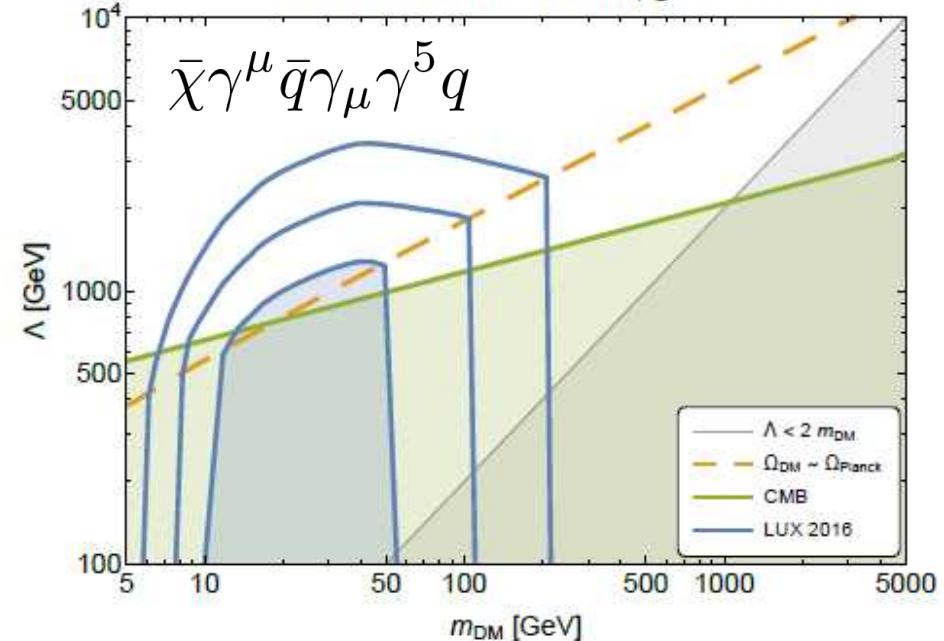
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Complex scalar dark matter, $g_{C4} = 1$



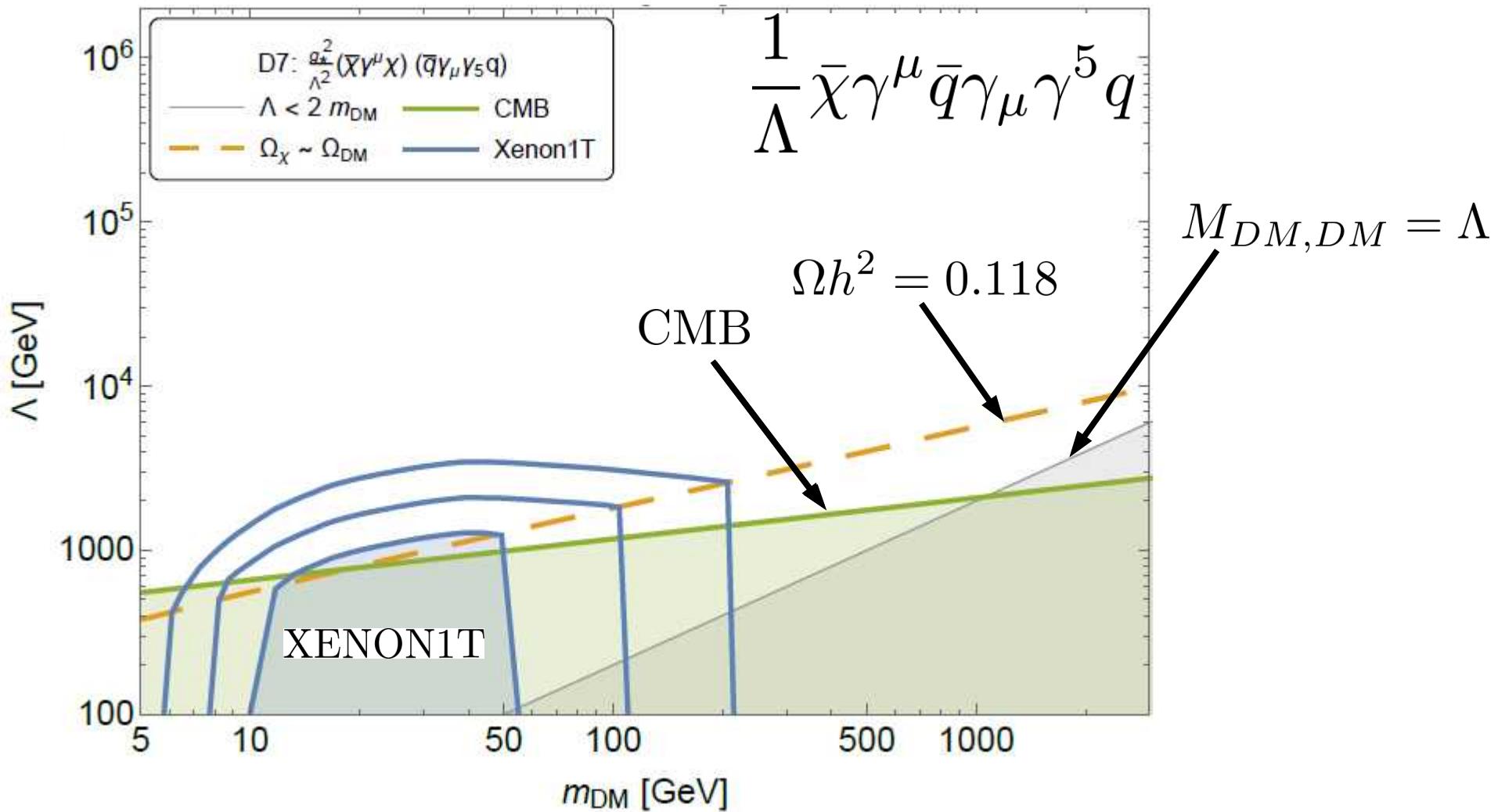
Dirac fermion dark matter, $g_{D7} = 1$



AB, Bertuzzo, Caniu, di Cortona, Eboli, Pukhov 2018

DM DD \leftrightarrow Collider interplay

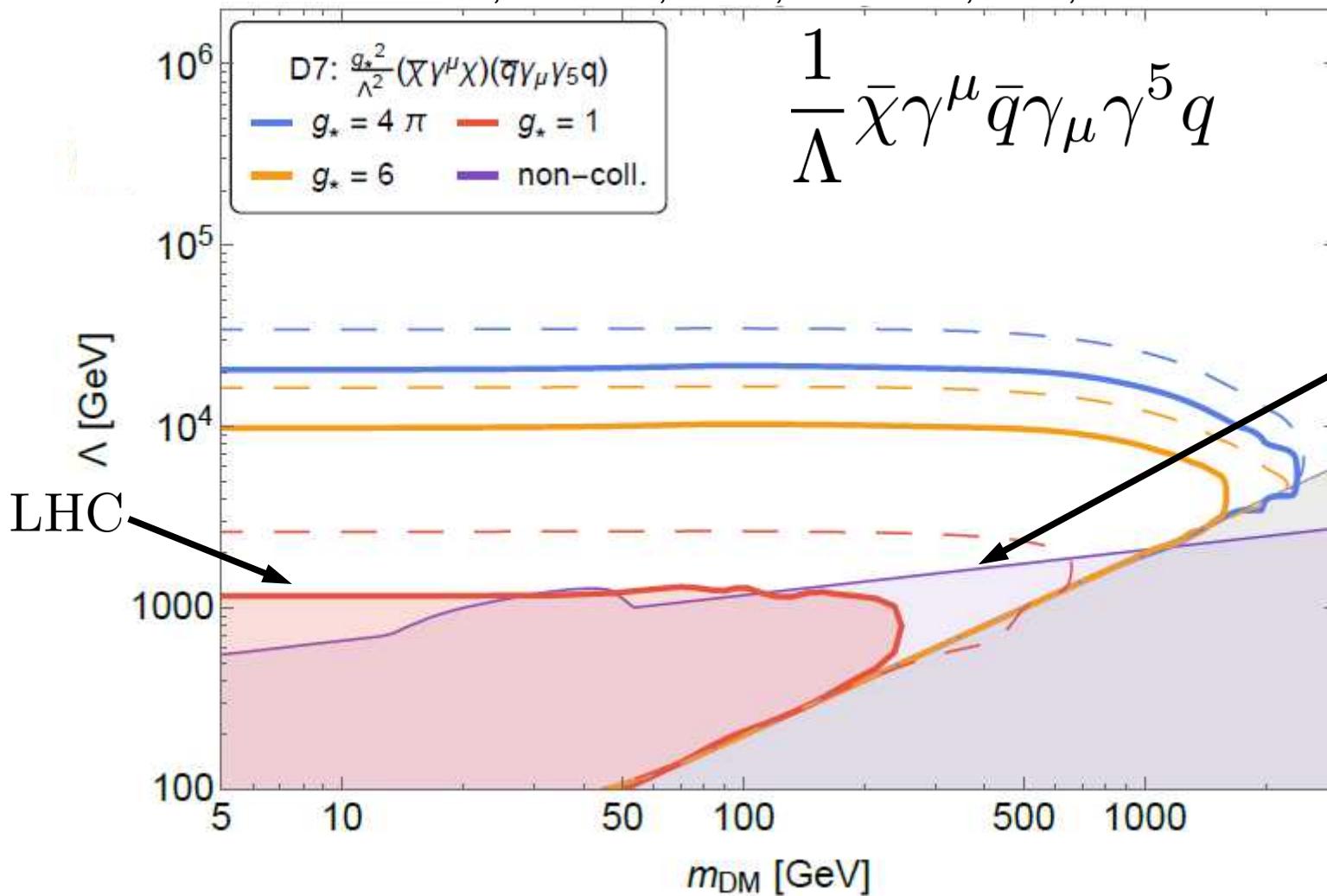
AB, Bertuzzo, Caniu, di Cortona, Eboli, Pukhov 2018



CMB: $p_{\text{ann}} < 4.1 \times 10^{-28} \frac{\text{cm}^3}{\text{s GeV}}$ at 95% C.L. , where $p_{\text{ann}} = \sum_j f_j(600, m_{\text{DM}}) \frac{\langle \sigma v \rangle_j(600)}{m_{\text{DM}}}$

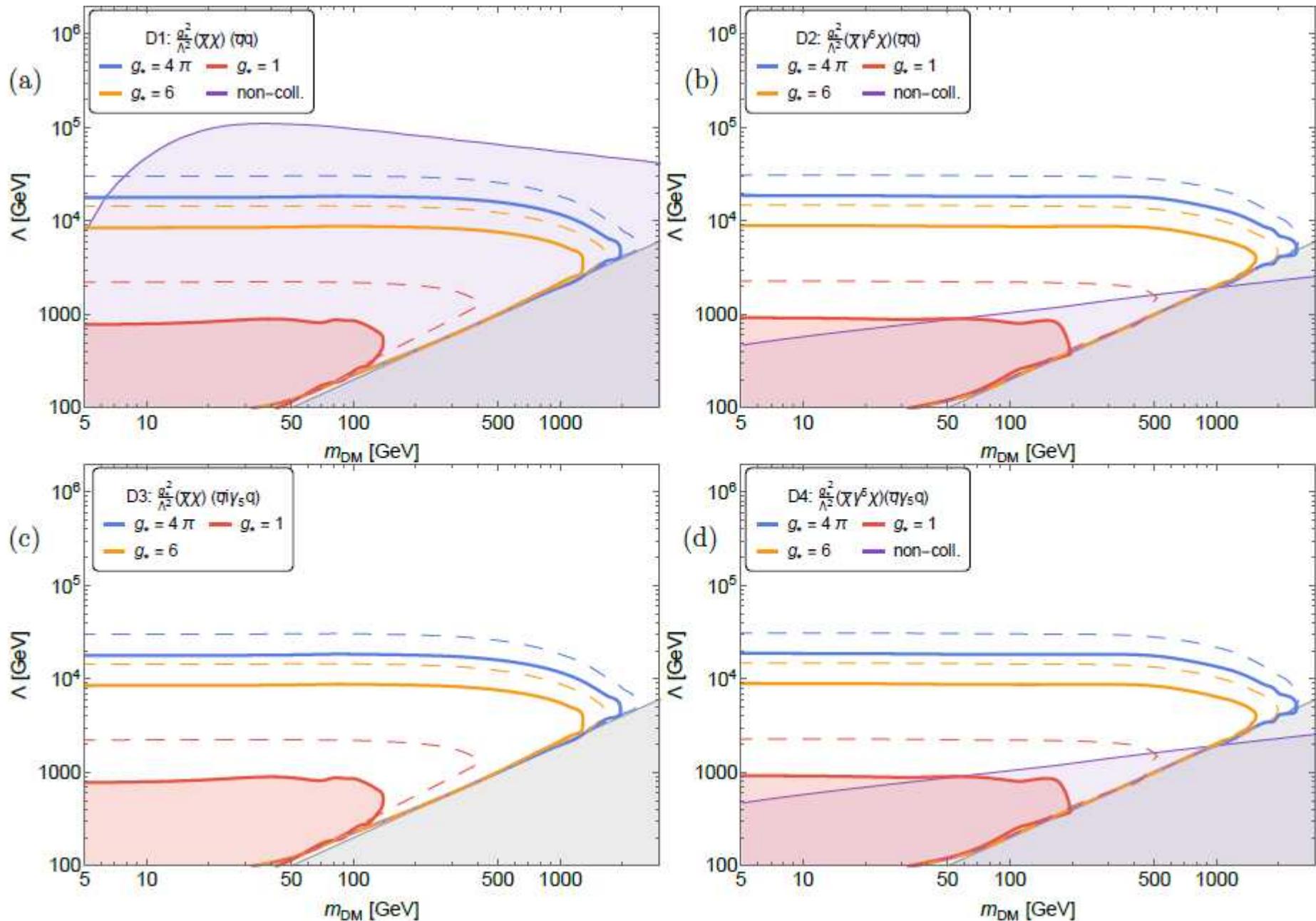
DM DD \leftrightarrow Collider interplay

AB, Bertuzzo, Caniu, di Cortona, Eboli, Pukhov 2018



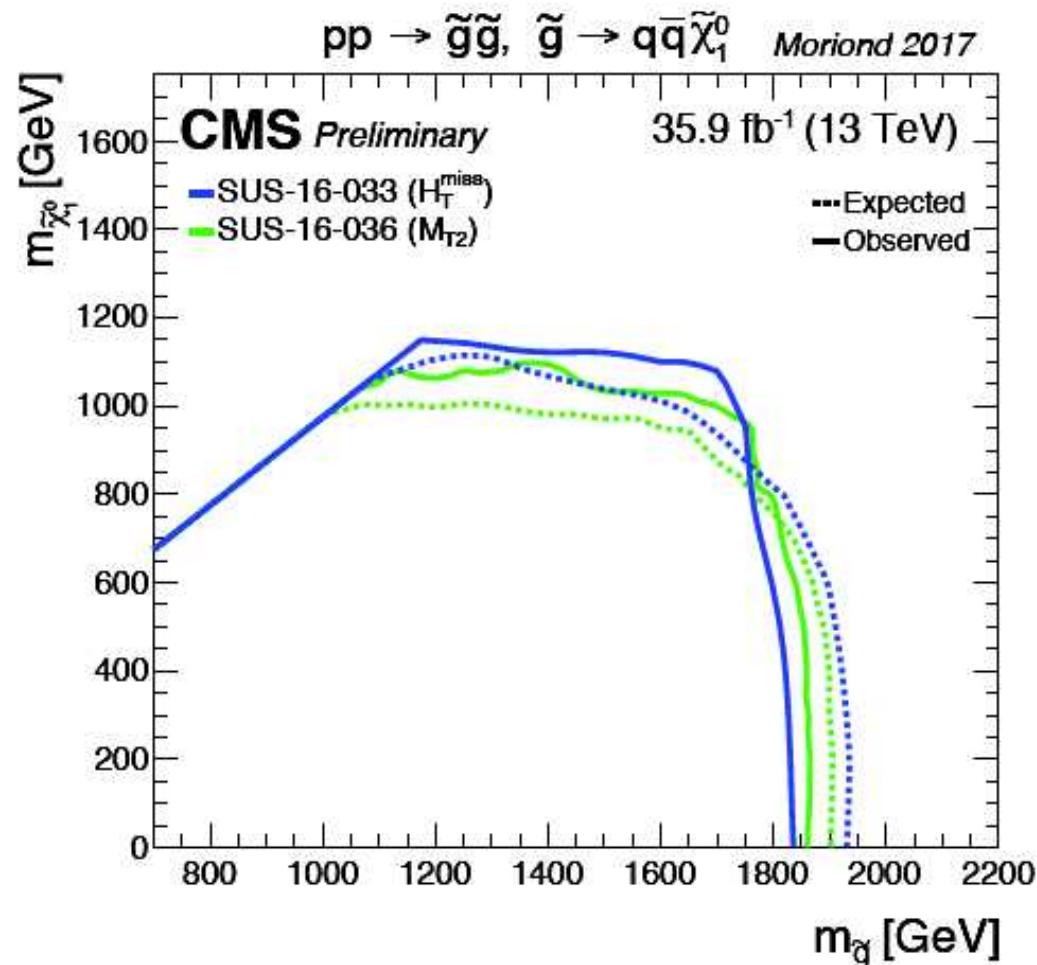
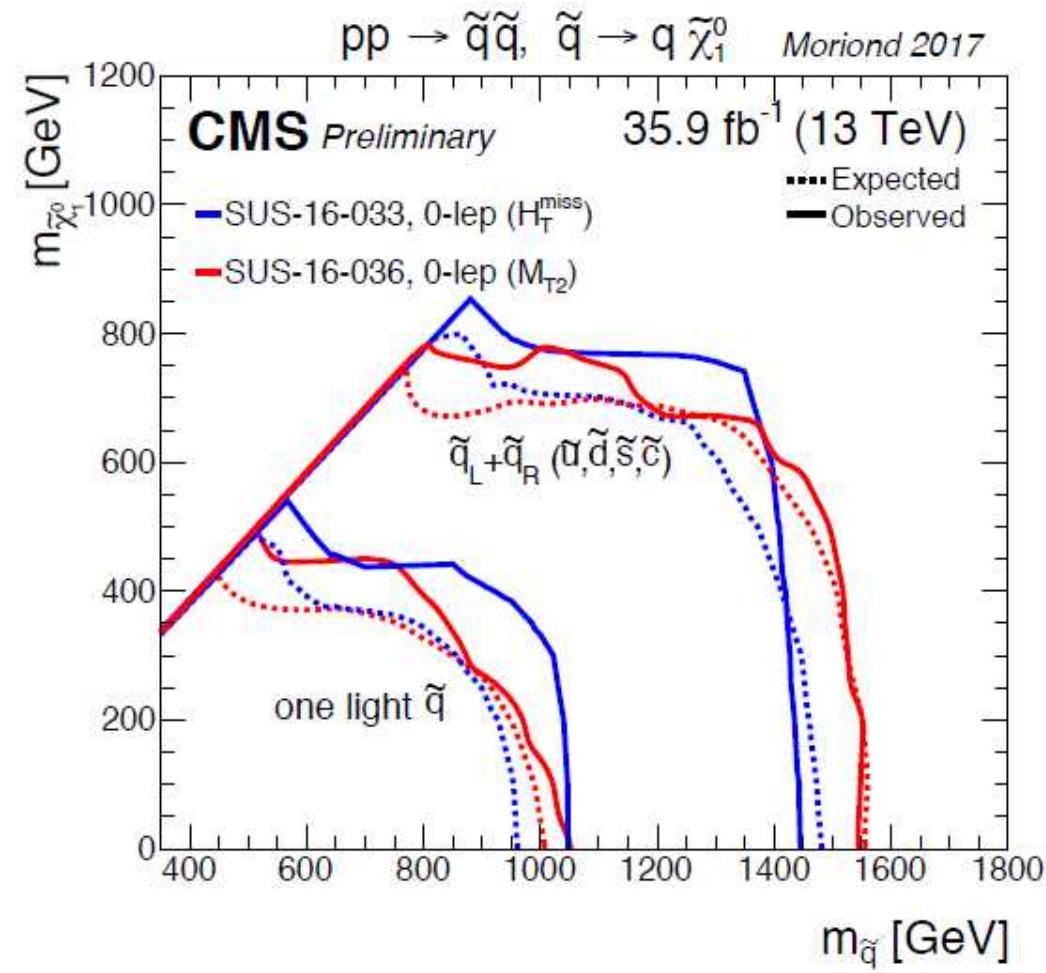
non-collider
constraints

DM DD \leftrightarrow Collider interplay



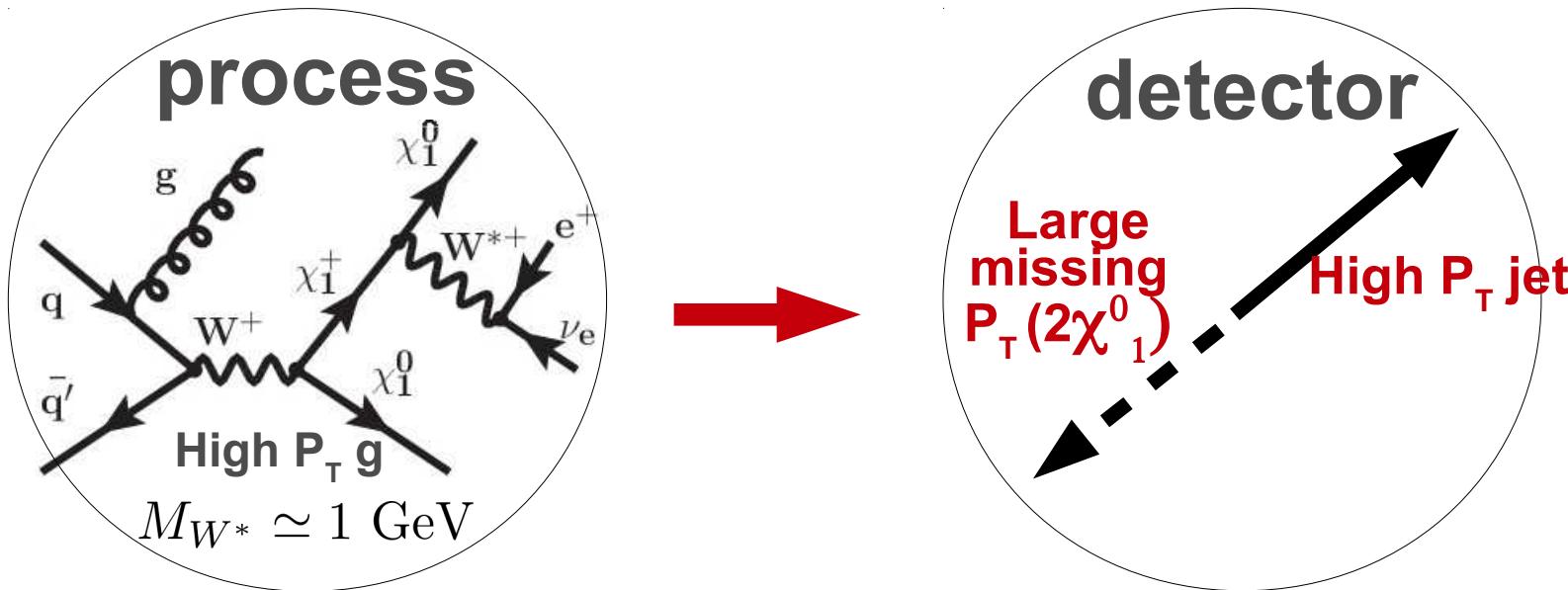
Application beyond the EFT: SUSY

There is no limit on the LSP mass if the mass of strongly interacting SUSY particles above ~ 1.9 TeV



SUSY Compressed Mass Spectrum scenario

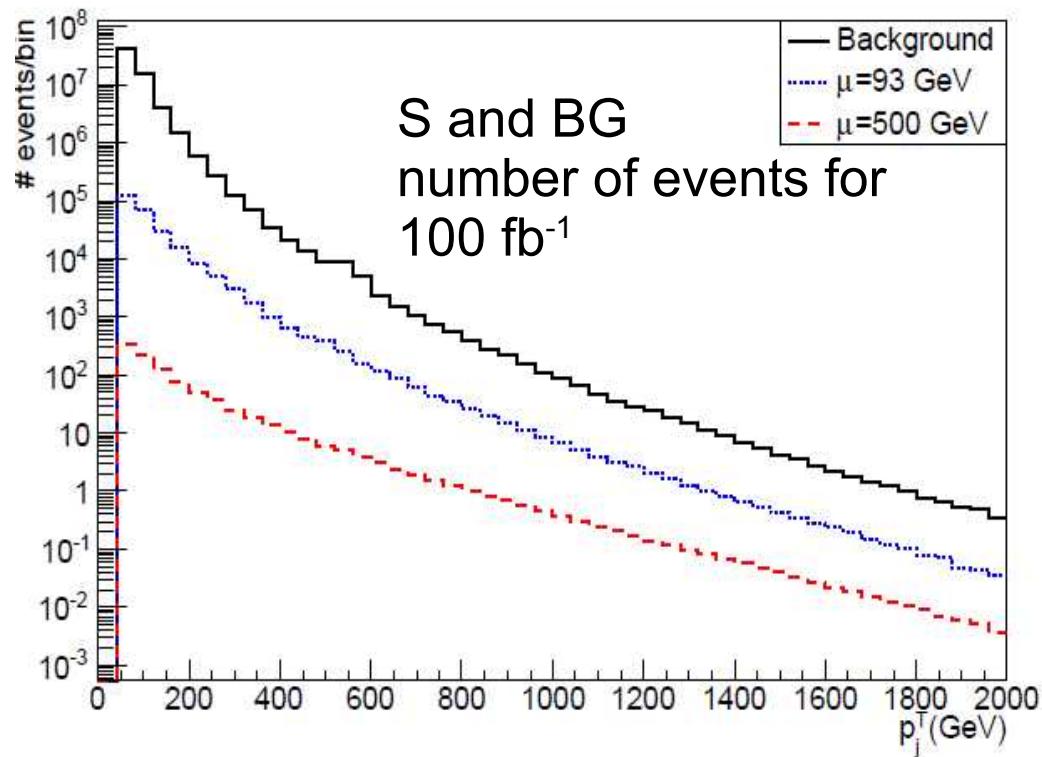
- The most challenging case takes place when only $\chi_{1,2}^0$ and χ_1^\pm are accessible at the LHC, and the mass gap between them is not enough for leptonic signatures
- The only way to probe CHS is a mono-jet signature
[“Where the Sidewalk Ends? ...” Alves, Izaguirre,Wacker '11] , which has been used in studies on compressed SUSY spectra, e.g. Dreiner,Kramer,Tattersall '12; Han,Kobakhidze,Liu,Saavedra,Wu'13; Han,Kribs,Martin,Menon '14



Signal vs Background

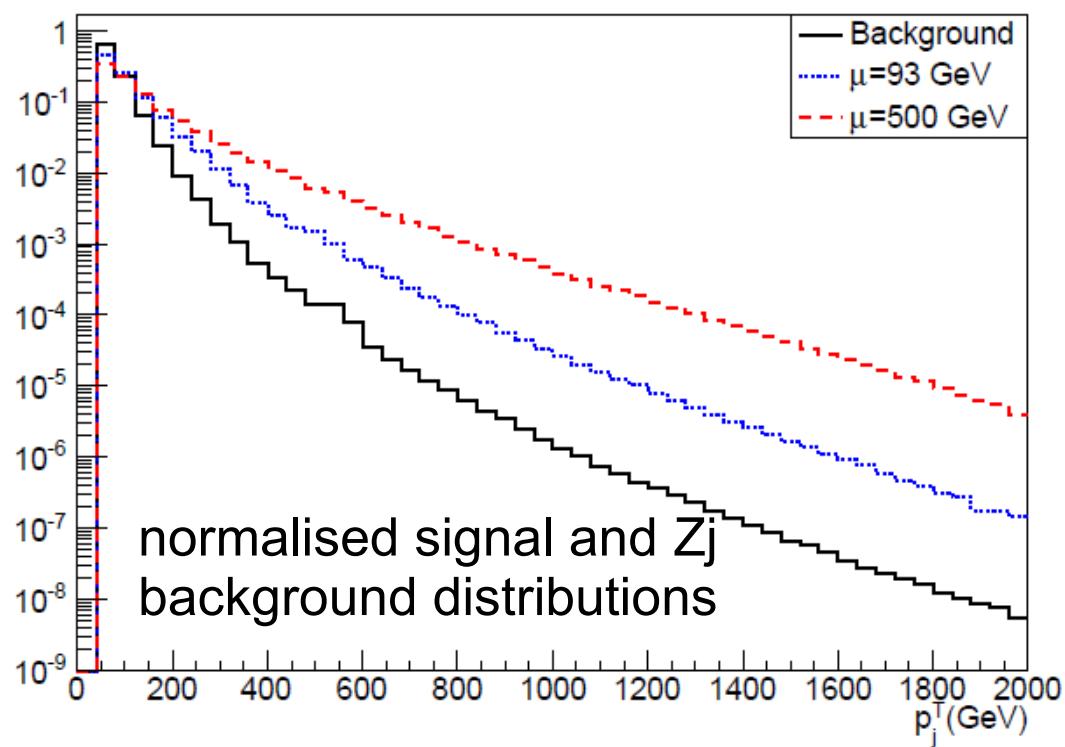
- difference in rates is pessimistic ...

$pp \rightarrow vvj$ vs. $pp \rightarrow \chi\chi j$



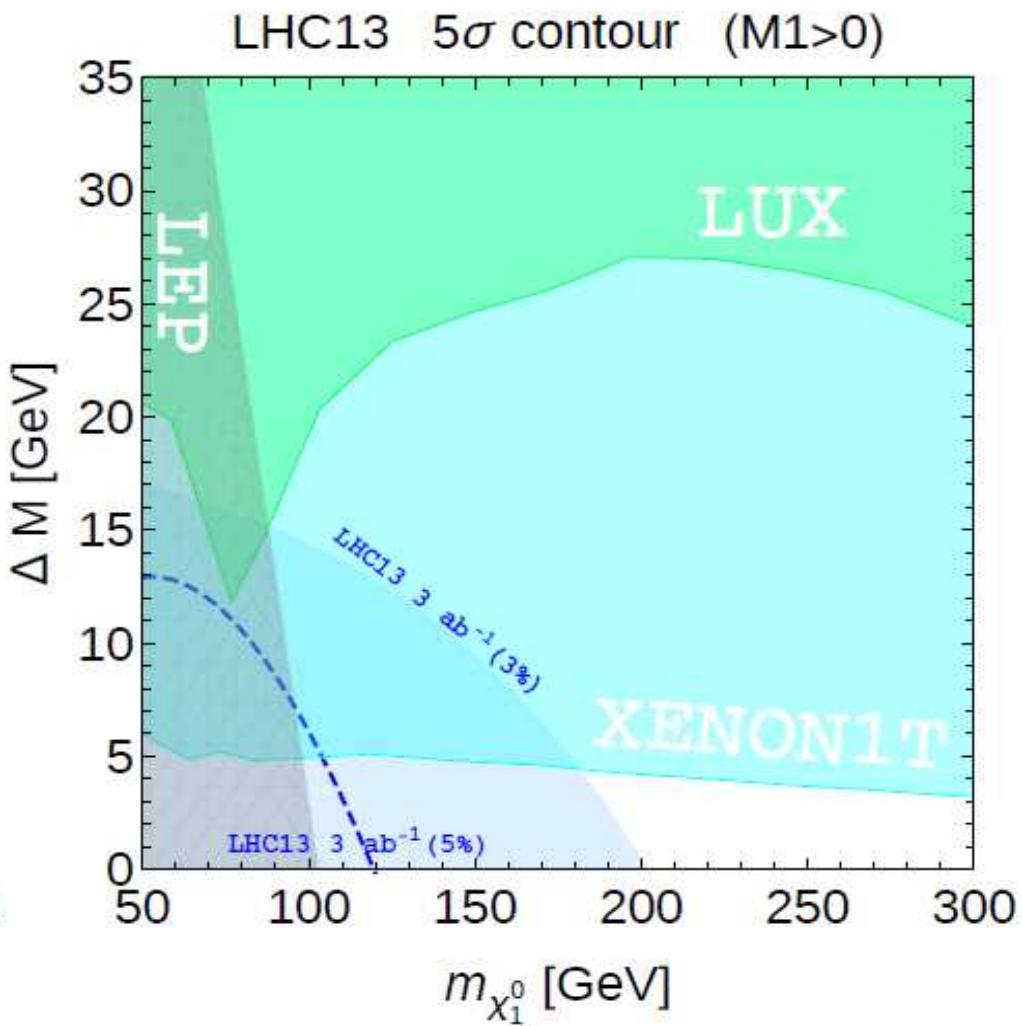
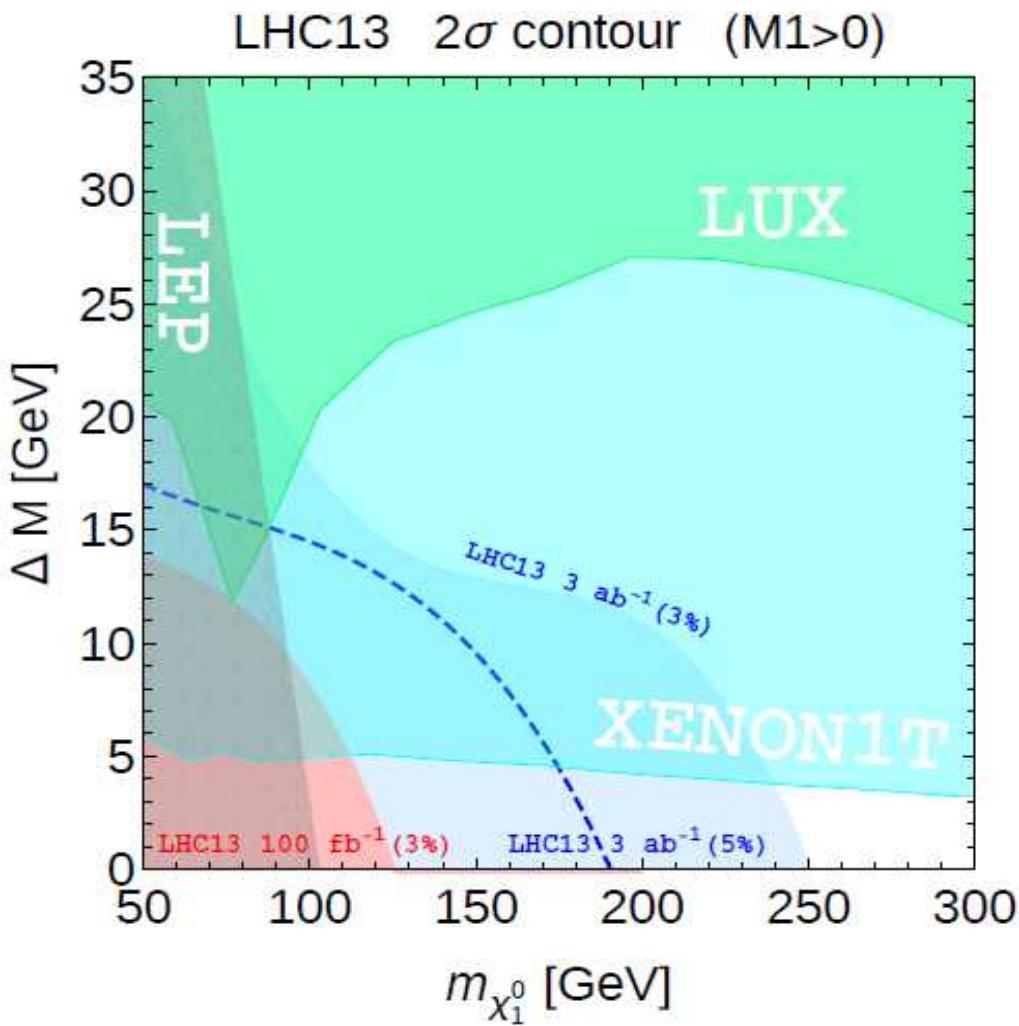
- but the difference in shapes is encouraging, especially for large DM mass \rightarrow bigger $M(DM, DM)$ \rightarrow flatter MET

$pp \rightarrow vvj$ vs. $pp \rightarrow \chi\chi j$



Signal and Z_j background p_T^j distributions for the 13 TeV LHC

LHC/DM direct detection sensitivity

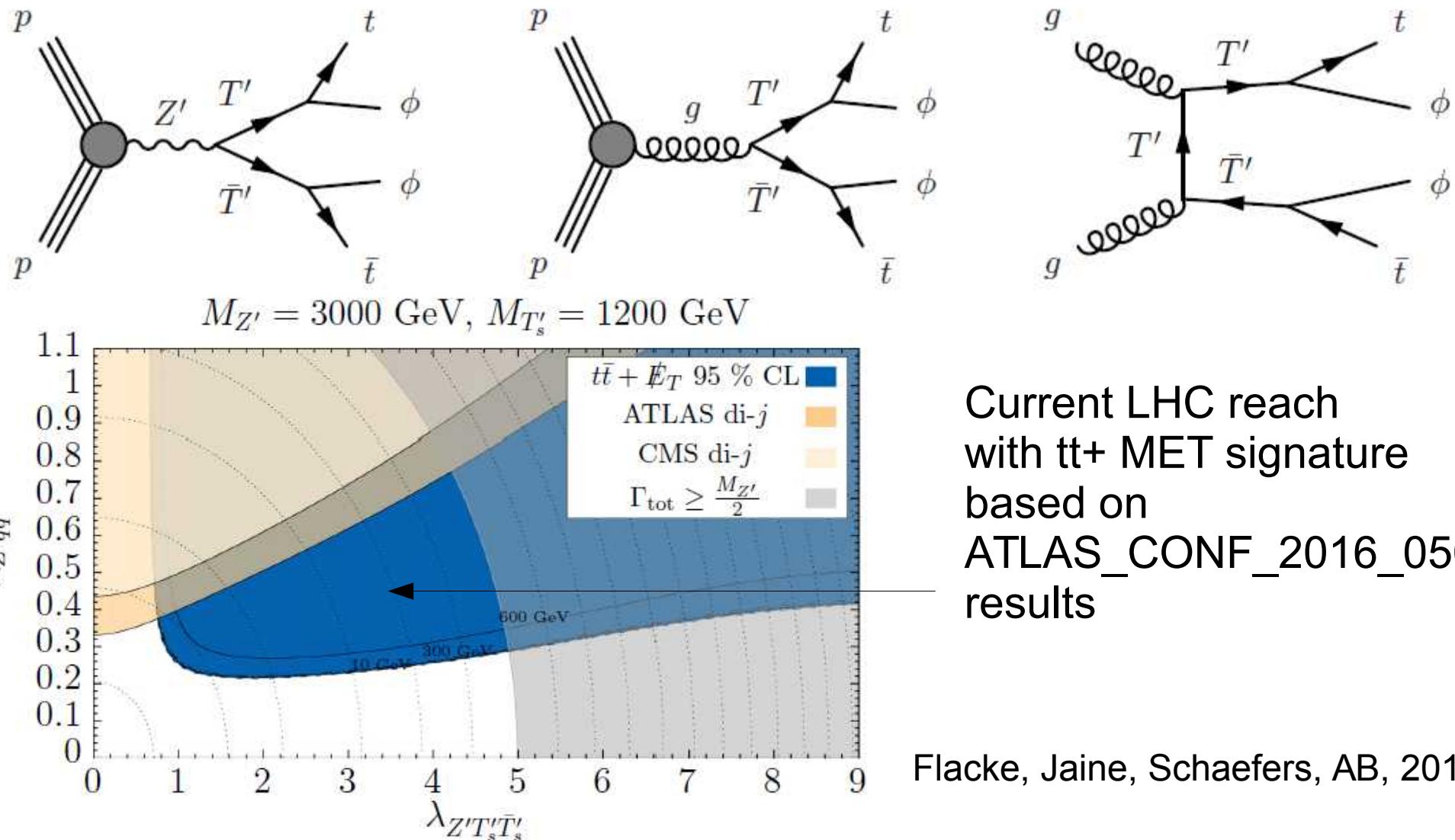


AB, Barducci,Bharucha,Porod,Sanz JHEP, 1504.02472

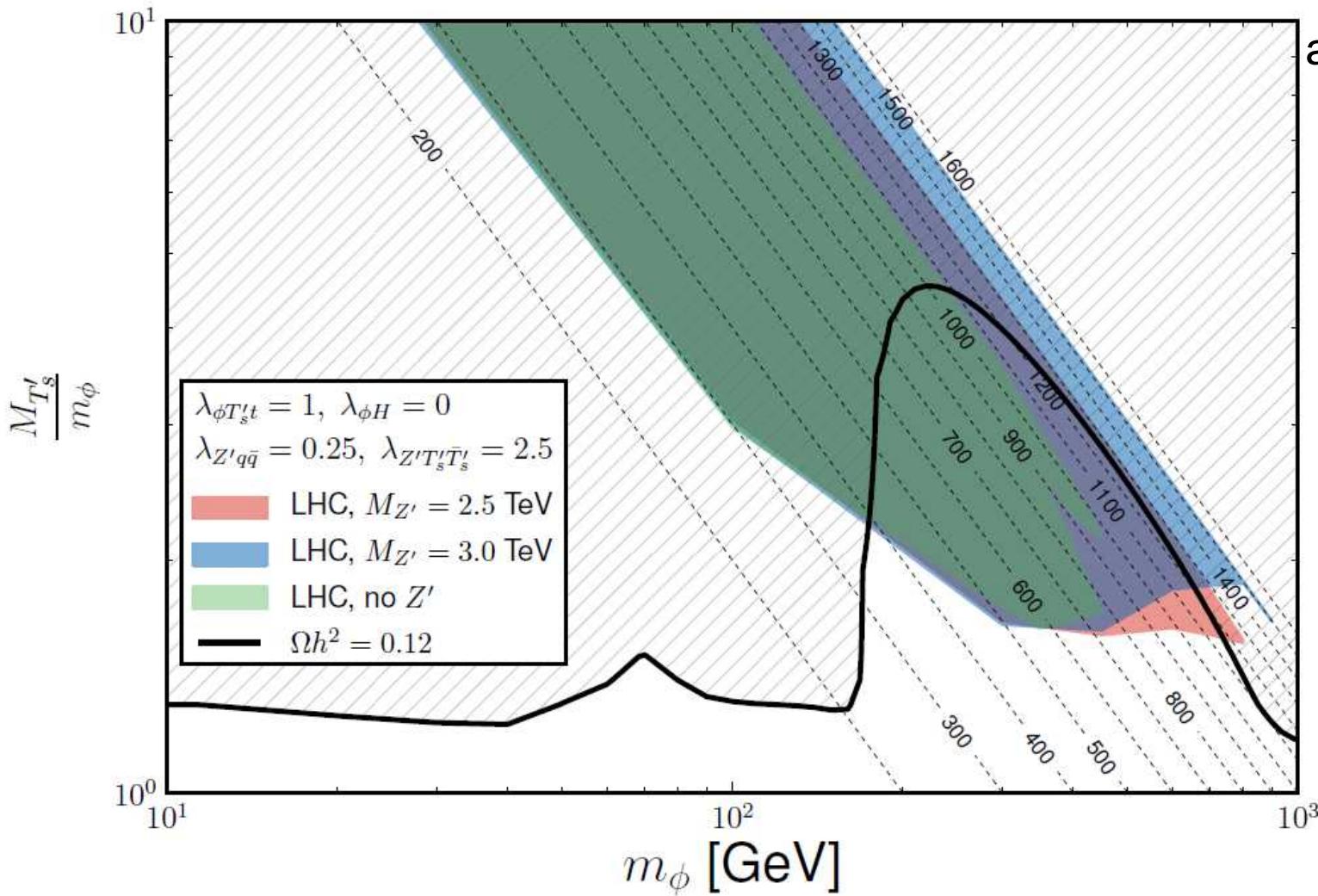
- SUSY DM, can be around the corner (~ 100 GeV), but it is hard to detect it!
- Great complementarity of DD and LHC for small DM (NSUSY) region

Beyond the mono-jet signature

Example of the vector resonance in the Composite Higgs model:
 $Z' \rightarrow T\bar{T} \rightarrow t\bar{t} DM DM$ signature



The role of Z' vs QCD for $pp \rightarrow TT \rightarrow t\bar{t} DM DM$



arXiv: 1707.07000

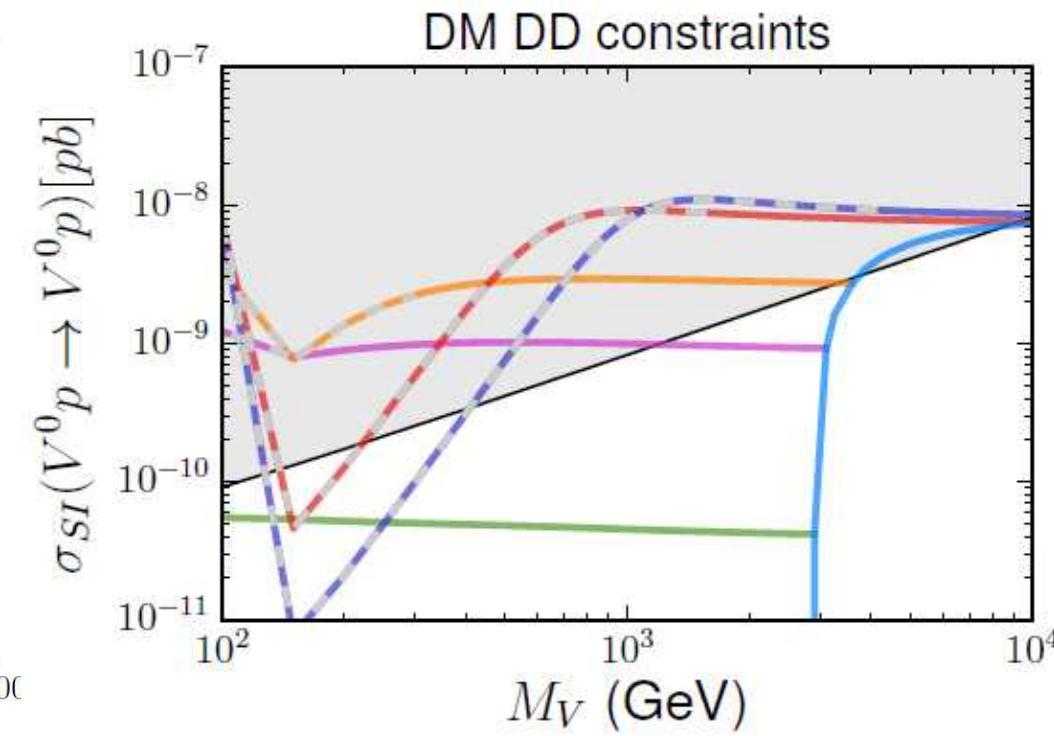
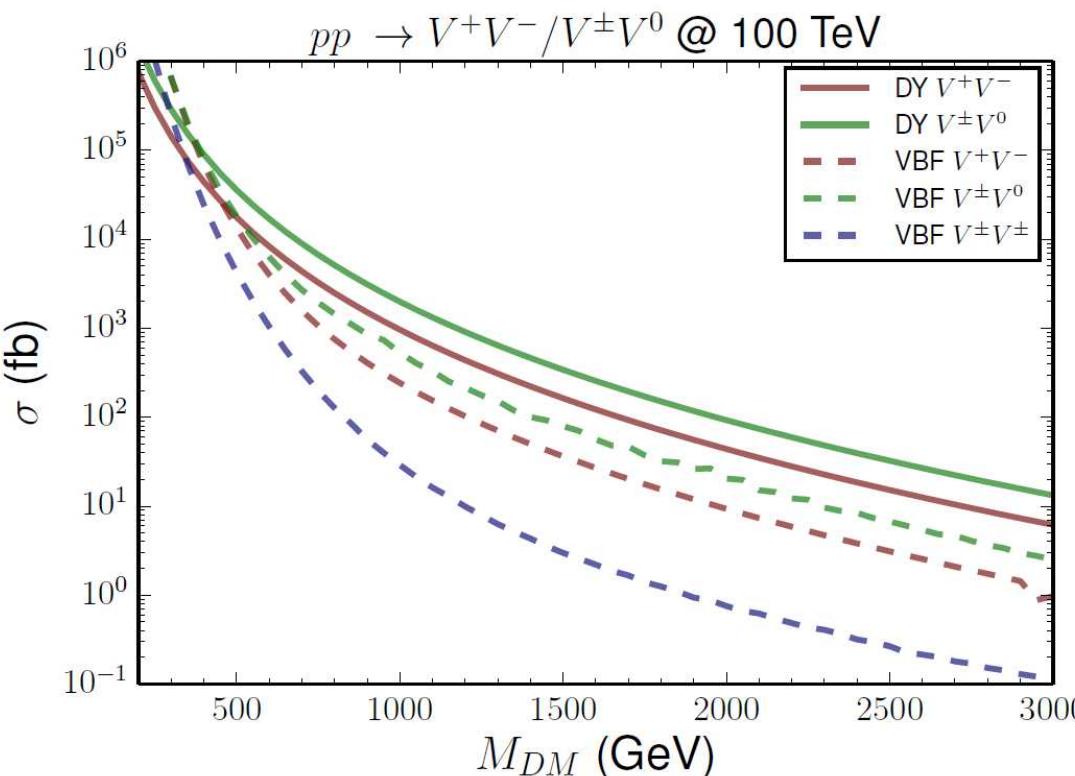
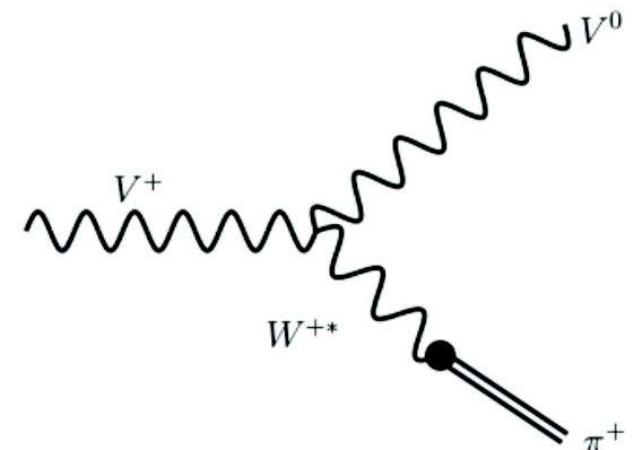
Z' + QCD TT
production

- ⇒ LHC is probing now DM and top partner masses up to about 0.9 and 1.5 TeV respectively: above bounds from QCD production alone by ~ factor of two
- ⇒ DM DD rates are loop-suppressed

Disappearing Charged Tracks from DM

The small mass gap between (\sim pion mass) DM and its charged partner will lead to the **disappearing charge tracks** signatures

The life-time should be properly evaluated using
W-pion mixing
(otherwise overestimated by factor of 10)

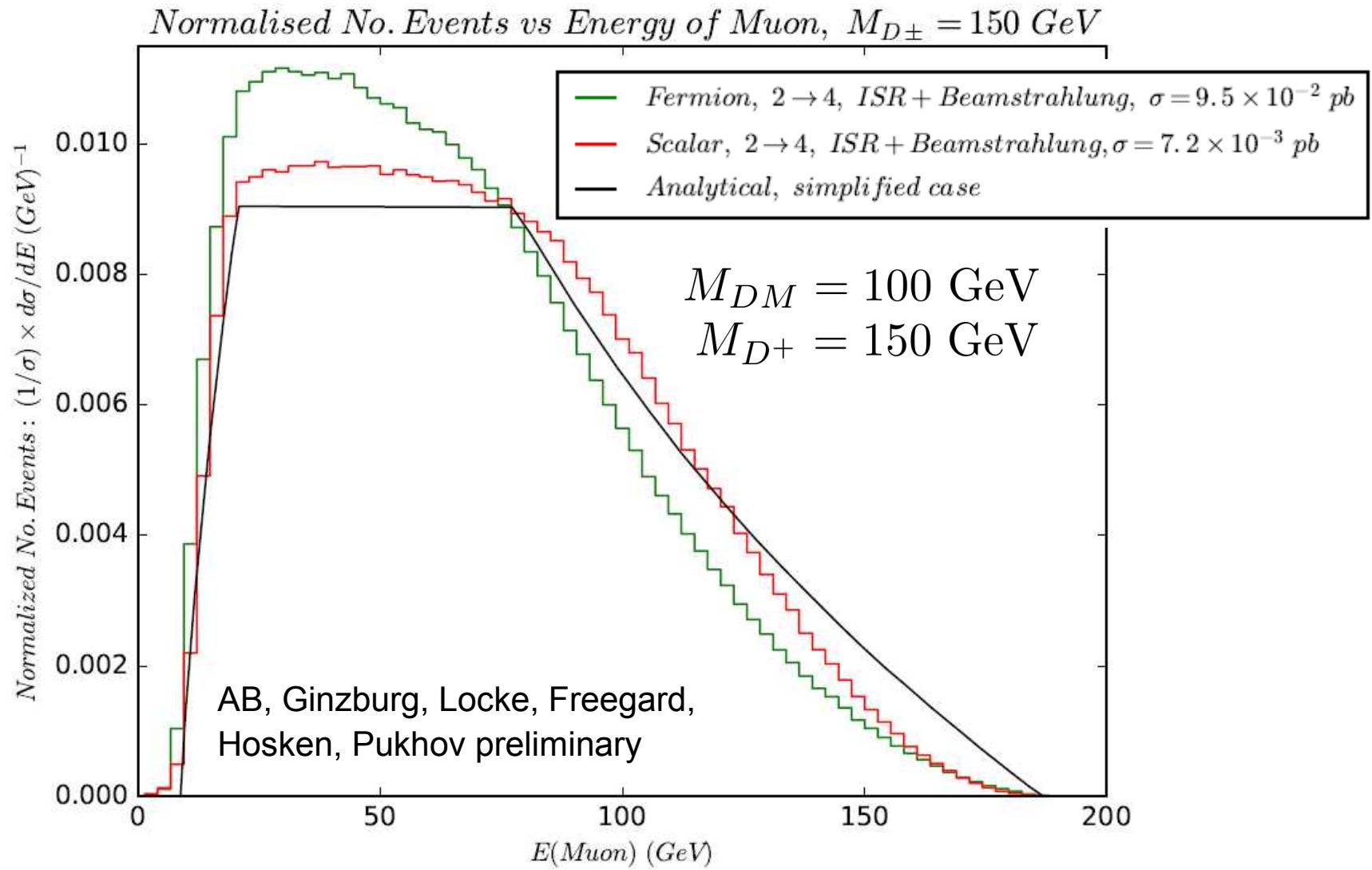


AB, Cacciapaglia, McKay, Marin, Zerwekh

Decoding the nature of DM at the ILC

muon spectrum from the models with scalar and fermion DM

$e^+e^- \rightarrow D^+ D^- \rightarrow DM\ DM\ W^+\ W^- \rightarrow DM\ DM\ jj\ \mu\ \nu$



Decoding Problem: Data → Theory link

- probably the most challenging problem to solve – **the inverse problem of decoding of the underlying theory from signal**
 - requires database of models, database of signatures
 - requires smart procedure based on machine learning of matching signal from data with the pattern of the signal from data

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- **HEPMDB (High Energy Physics Model Database)** was created in 2011
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 - convenient centralized storage environment for HEP models
 - it allows to evaluate the LHC predictions and perform event generation using CalcHEP, Madgraph for any model stored in the database
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- As a HEPMDB spin-off the **PhenoData** project was created
hepmdb.soton.ac.uk/phenodata
 - stores data (digitized curves from figures, tables etc) from those HEP papers which did not provide data in arXiv or HEPData
 - has an easy search interface and paper identification via arXiv, DOI or preprint numbers

Summary

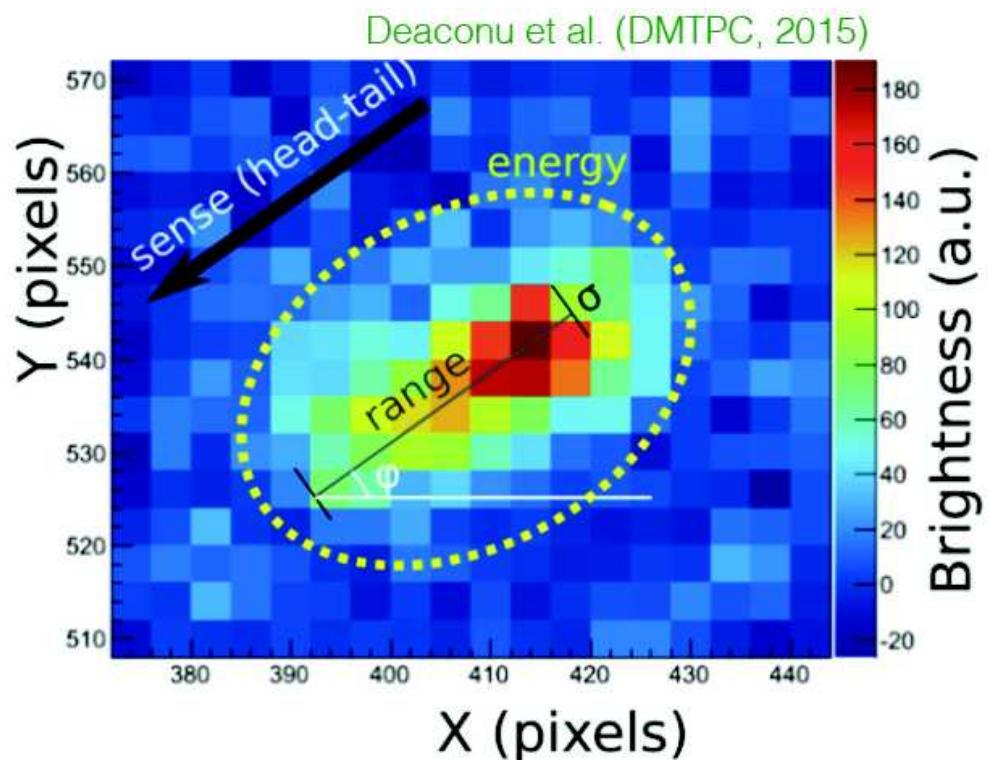
- ⇒ DM DD detection provides a very powerful probe of DM theory space – in general provides DM mass probe beyond the collider reach
- ⇒ Colliders – provide DM detection power in the region “blind” for DM DD, typically below 1 TeV
- ⇒ Several ways to decode DM nature from the signal which we hope to observe soon (slopes of MET, cross sections, signatures, ...)
- ⇒ New prospects: new DD experiments, new ideas, prospects for directional DM detection, new signatures at colliders (VFB, long lived ...), new colliders (great potential of ILC and FCC)
- ⇒ Great synergy of collider and non-collider experiments (DD, CMB, relic density)

Thank you!

Backup Slides

DM DD: directional detection – going beyond the neutrino floor

- The idea is to measure both the energy and the direction of the recoil
- Most mature technology is the gaseous Time Projection Chamber (TPC) : DRIFT, MIMAC, DMTPC, NEWAGE, D3



- Detecting recoil tracks in nuclear emulsion (e.g. NEWS experiment)
Aleksandrov et al. [1604.04199]
- Directional detection is HARD, But it is also very POWERFUL.

Relation of the actual dimension (D) and the naive one (d) for VDM operators

V_{DM} Operator	Λ_d	d	Λ_D	D	$\Delta_\sigma (\sigma_{2 \rightarrow 2} \propto E^{\Delta_\sigma})$	Amplitude Enhancement
V1,V2,V5,V6	$\frac{1}{\Lambda}$	5	$\frac{M_{DM}^2}{\Lambda^3}$	7	4	$(E/M_{DM})^2$
V3,V4,V7M,V8M,V11,V12	$\frac{1}{\Lambda^2}$	6	$\frac{M_{DM}^2}{\Lambda^4}$	8	6	$(E/M_{DM})^2$
V7P,V8P,V9,V10	$\frac{1}{\Lambda^2}$	6	$\frac{M_{DM}}{\Lambda^3}$	7	4	E/M_{DM}

- we suggest a **new parametrisation** of VDM operators: since the energy E and the collider limit on L are of the same order, it is natural to use an additional M_{DM}/Λ factor for each power of E/M_{DM} enhancement, so collider limits are **not artificially enhanced**
[~100 TeV !!! for MDM = 1 GeV, see Kumar, Marfatia, Yaylali 1508.04466] and will be of the same order as limits for other operators
- Dictionary between limits on Λ in different parametrisations:

$$\Lambda_D = (\Lambda_d^{d-4} M_{DM}^{D-d})^{\frac{1}{D-4}} \quad \text{and} \quad \Lambda_d = (\Lambda^{D-4} M_{DM}^{d-D})^{\frac{1}{d-4}}$$

On the BG uncertainty

- The BG is statistically driven, e.g. $\text{pp} \rightarrow Zj \rightarrow nnj$ BG is defined from the $\text{pp} \rightarrow Zj \rightarrow l^+l^-j$ one

CMS-PAS-EXO-16-013

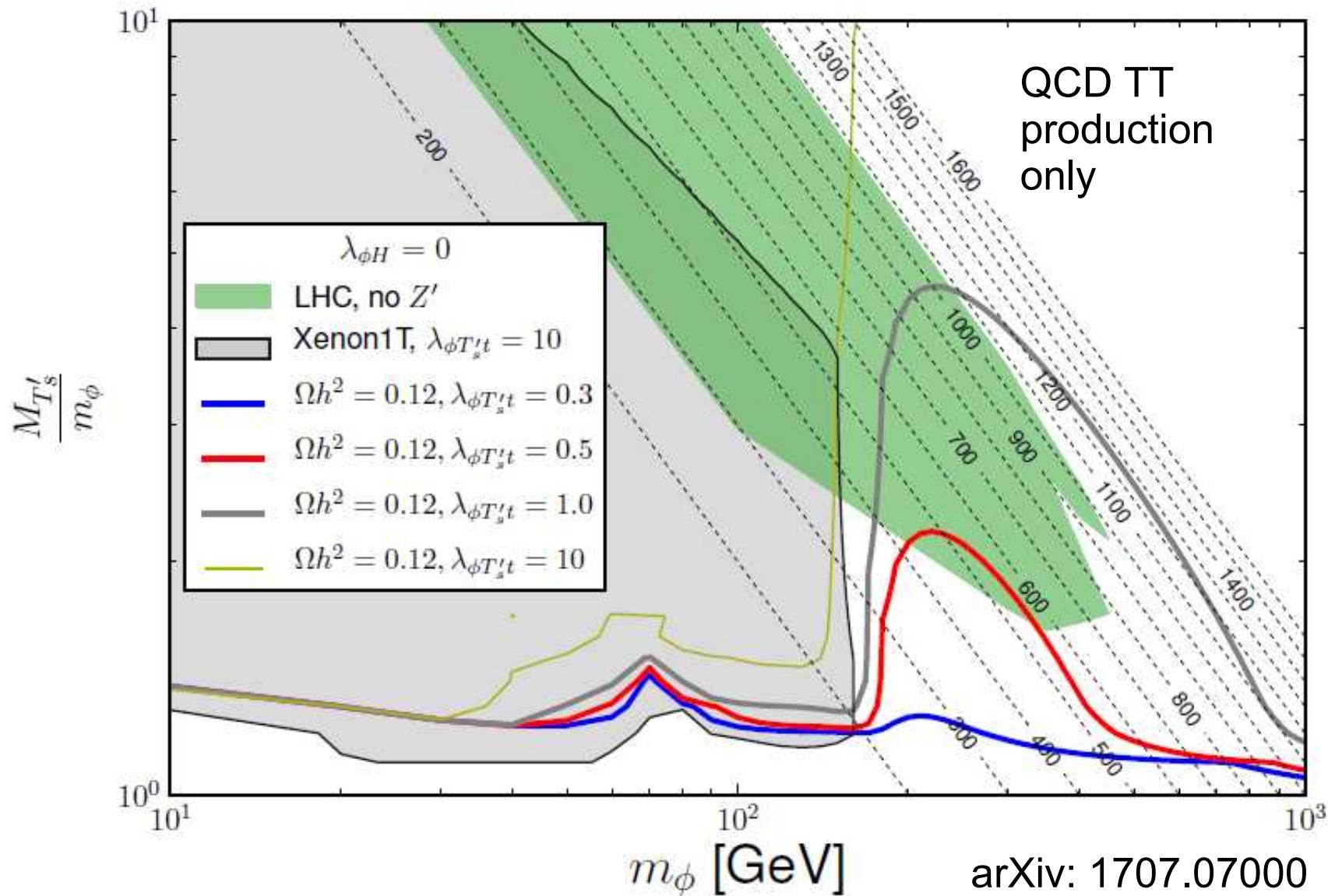
E_T^{miss} Range (GeV)	Z($\nu\nu$)+jets	W($\ell\nu$)+jets	Z($\ell\ell$)+jets	γ +jets	Top	Diboson	QCD	Total (Pre-fit)	Total (Post-fit)	Data
200 – 230	14919 ± 221	11976 ± 196	207 ± 13	230 ± 14	564 ± 55	251 ± 41	508 ± 171	27761 ± 1464	28654 ± 171	28601
230 – 260	7974 ± 116	5776 ± 101	92.9 ± 5.7	101 ± 6	267 ± 26	157 ± 26	308 ± 104	14114 ± 757	14675 ± 97	14756
260 – 290	4467 ± 70	2867 ± 50	37.9 ± 2.3	63.7 ± 3.9	116 ± 11	77.3 ± 12.7	38.3 ± 21.0	7193 ± 351	7666 ± 68	7770
290 – 320	2518 ± 46	1520 ± 34	18.4 ± 1.1	29.6 ± 1.8	56.7 ± 5.6	42.9 ± 7.1	29.8 ± 10.5	4083 ± 204	4215 ± 48	4195
320 – 350	1496 ± 35	818 ± 20	10.0 ± 0.6	19.7 ± 1.2	33.6 ± 3.3	25.4 ± 4.2	9.0 ± 5.4	2385 ± 118	2407 ± 37	2364
350 – 390	1204 ± 31	555 ± 15	3.9 ± 0.2	12.7 ± 0.8	24.5 ± 2.4	22.1 ± 3.6	6.0 ± 3.5	1817 ± 87	1826 ± 32	1875
390 – 430	684 ± 20	275 ± 9	2.1 ± 0.1	8.3 ± 0.5	9.8 ± 1.0	13.9 ± 2.3	3.0 ± 1.6	978 ± 45	998 ± 23	1006
430 – 470	382 ± 14	155 ± 6	0.96 ± 0.06	4.9 ± 0.3	9.4 ± 0.9	6.6 ± 1.1	1.0 ± 0.8	589 ± 30	574 ± 17	543
470 – 510	248 ± 11	87.3 ± 3.8	0.47 ± 0.03	3.7 ± 0.2	0.22 ± 0.02	5.1 ± 0.8	0.65 ± 0.44	337 ± 15	344 ± 12	349
510 – 550	160 ± 8	52.2 ± 2.7	0.23 ± 0.01	2.0 ± 0.1	2.7 ± 0.3	2.2 ± 0.4	0.28 ± 0.19	211 ± 9	219 ± 9	216
550 – 590	99.5 ± 6.0	29.2 ± 1.9	0.12 ± 0.01	1.8 ± 0.1	0.94 ± 0.09	2.0 ± 0.3	0.19 ± 0.14	134 ± 6	134 ± 7	142
590 – 640	77.3 ± 4.9	18.9 ± 1.4	0.09 ± 0.01	0.46 ± 0.03	< 0.13	1.7 ± 0.3	0.11 ± 0.08	100 ± 4	98.5 ± 5.8	111
640 – 690	44.8 ± 3.5	11.2 ± 0.9	0.017 ± 0.001	0.19 ± 0.01	< 0.13	1.5 ± 0.2	0.06 ± 0.05	59.6 ± 2.6	58.0 ± 4.1	61
690 – 740	27.8 ± 2.5	6.1 ± 0.6	0.013 ± 0.0008	0.57 ± 0.04	< 0.13	0.69 ± 0.11	0.02 ± 0.02	36.6 ± 1.5	35.2 ± 2.9	32
740 – 790	21.8 ± 2.3	5.3 ± 0.6	< 0.005	0.28 ± 0.02	0.23 ± 0.02	0.11 ± 0.02	0.02 ± 0.02	23.8 ± 1.0	27.7 ± 2.7	28
790 – 840	13.5 ± 1.9	2.8 ± 0.4	< 0.005	0.18 ± 0.01	0.27 ± 0.03	0.010 ± 0.001	0.008 ± 0.007	15.3 ± 0.7	16.8 ± 2.2	14
840 – 900	9.5 ± 1.4	2.0 ± 0.3	< 0.005	0.28 ± 0.02	< 0.13	0.25 ± 0.04	< 0.008	12.2 ± 0.6	12.0 ± 1.6	13
900 – 960	5.4 ± 1.0	1.1 ± 0.2	< 0.005	< 0.08	< 0.13	0.37 ± 0.06	< 0.008	7.6 ± 0.3	6.9 ± 1.2	7
960 – 1020	3.3 ± 0.8	0.77 ± 0.21	< 0.005	0.12 ± 0.01	< 0.13	0.23 ± 0.04	< 0.008	5.2 ± 0.3	4.5 ± 1.0	3
1020 – 1160	2.5 ± 0.8	0.52 ± 0.16	< 0.005	< 0.08	< 0.13	0.16 ± 0.03	< 0.008	3.6 ± 0.2	3.2 ± 0.9	1
1160 – 1250	1.7 ± 0.6	0.3 ± 0.11	< 0.005	< 0.08	< 0.13	0.16 ± 0.03	< 0.008	2.3 ± 0.1	2.2 ± 0.7	2
> 1250	1.4 ± 0.5	0.19 ± 0.08	< 0.005	< 0.08	< 0.13	0.06 ± 0.01	< 0.008	1.6 ± 0.1	1.6 ± 0.6	3

<http://cms-results.web.cern.ch/cms-results/public-results/preliminary-results/EXO-16-013/#AddFig>

Complementarity of LHC and non-LHC DM searches

for the model with Vector Resonances, Top Partners and Scalar DM

$T\bar{T} \rightarrow t\bar{t} DM DM$



LHC@13TeV Reach for spin 0 and $\frac{1}{2}$ DM

Operators	Coefficient	Excluded Λ (GeV) at 3.2 fb^{-1}			Excluded Λ (GeV) at 100 fb^{-1}			
		DM Mass			DM Mass			
		10 GeV	100 GeV	1000 GeV	10 GeV	100 GeV	1000 GeV	
Complex Scalar DM	C1 & C2	$1/\Lambda$	456	424	98	1168	1115	267
	C3 & C4	$1/\Lambda^2$	750	746	400	1134	1131	662
	C5 & C6	$1/\Lambda^2$	1621	1576	850	2656	2611	1398
Dirac Fermion DM	D1 & D3	$1/\Lambda^2$	931	940	522	1386	1405	861
	D2 & D4	$1/\Lambda^2$	952	936	620	1426	1399	1022
	D1T & D4T	$1/\Lambda^2$	735	729	476	1217	1199	780
	D2T	$1/\Lambda^2$	637	638	407	1053	1052	670
	D3T	$1/\Lambda^2$	586	625	391	969	938	644
	D5 & D7	$1/\Lambda^2$	1058	967	721	1580	1591	1190
	D6 & D8	$1/\Lambda^2$	978	1050	579	1608	1585	955
	D9 & D10	$1/\Lambda^2$	1587	1592	958	2613	2619	1580

LHC@13TeV Reach for spin 1 DM

Complex Vector DM

Operators	Coefficient	Excluded Λ (GeV) at 3.2 fb^{-1}			Excluded Λ (GeV) at 100 fb^{-1}			
		DM Mass			DM Mass			
		10 GeV	100 GeV	1000 GeV	10 GeV	100 GeV	1000 GeV	
Complex Vector DM	V1 & V2	M_{DM}^2/Λ_D^3	831	833	714	1162	1161	997
	V3 & V4	M_{DM}^2/Λ_D^4	930	931	833	1196	1193	1070
	V5 & V6	M_{DM}^2/Λ_D^3	784	791	711	1095	1104	993
	V7M & V8M	M_{DM}^2/Λ_D^4	930	926	882	1195	1193	1130
	V7P & V8P	M_{DM}/Λ_D^3	796	791	652	1112	1102	911
	V9M & V10M	M_{DM}/Λ_D^3	796	799	737	1109	1114	1027
	V9P & V10P	M_{DM}/Λ_D^3	794	782	609	1110	1089	850
	V11 & V11A	M_{DM}^2/Λ_D^4	1435	1442	1309	1844	1850	1683

Disappearing Charged Tracks from DM

The small mass gap between (\sim pion mass) DM and its charged partner will lead to the disappearing charge tracks

The life-time should be properly evaluated using
W-pion mixing

$$\mathcal{L}_{\pi^- V^+ V^0} = \frac{g^2 f_\pi}{2\sqrt{2} M_W^2} [g_{\beta\gamma} (p_{V^+} - p_{V^0})_\alpha + g_{\alpha\gamma} (p_{V^+} - p_{V^0})_\beta] p_{\pi^-}^\alpha \pi^- V^{+\beta} V^{0\gamma}$$

