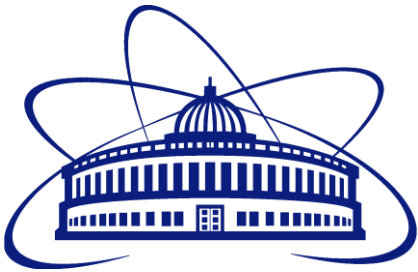


# Neutron and x-ray scattering for studies of biological systems

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Joint Institute for Nuclear Research*



# Outline

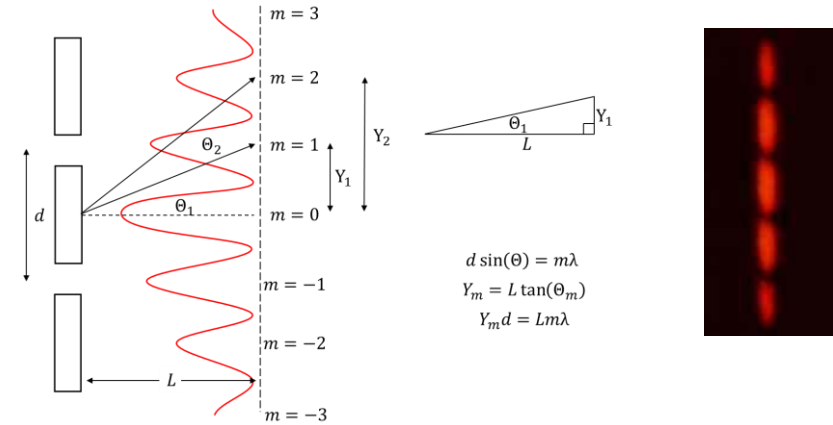
- Historical Overview: X-ray
- X-ray Sources
- Historical Overview: Neutrons
- Neutron Sources
- X-ray vs Neutron
- Theory of scattering from matter
- Imaging Techniques
- Protein crystallography
- Small angle scattering
- Other scattering methods

# The Wave Nature of Light

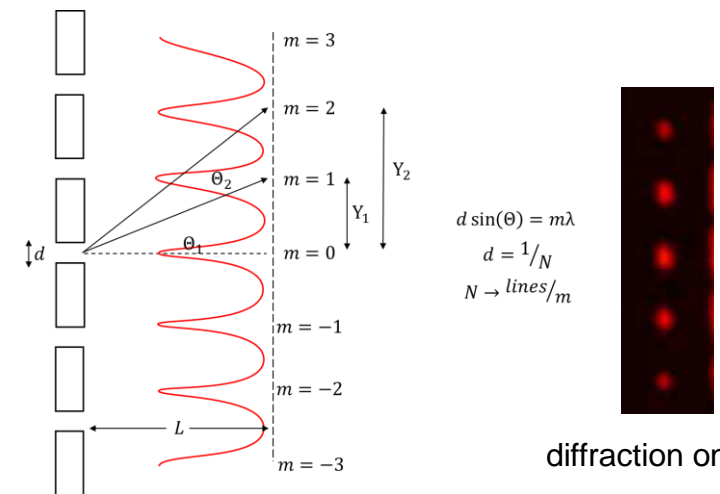
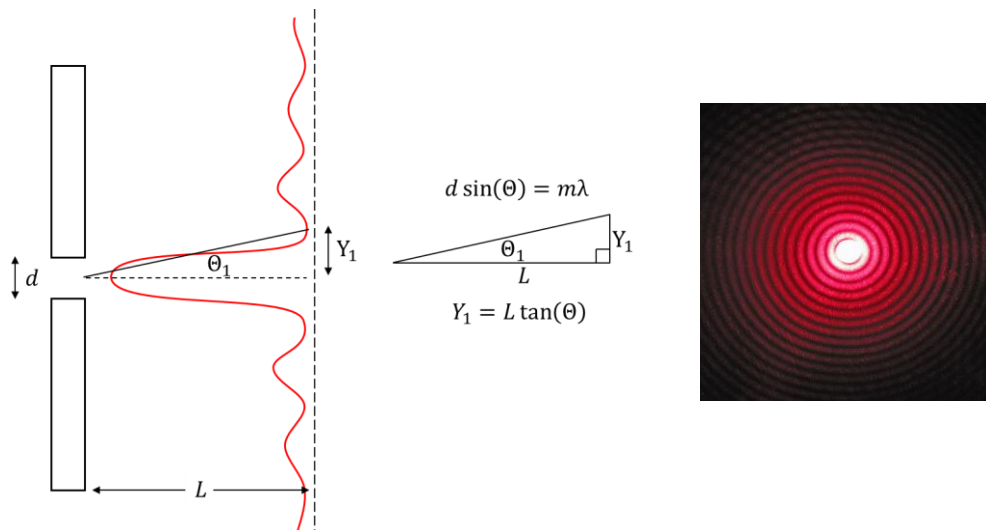
1678 - Christiaan Huygens published *Traité de la Lumière* (Treatise on light). Wave theory of light

1801 - Thomas Young presented a famous paper to the Royal Society entitled "On the Theory of Light and Colours"

1818 - Augustin-Jean Fresnel theory of the light diffraction

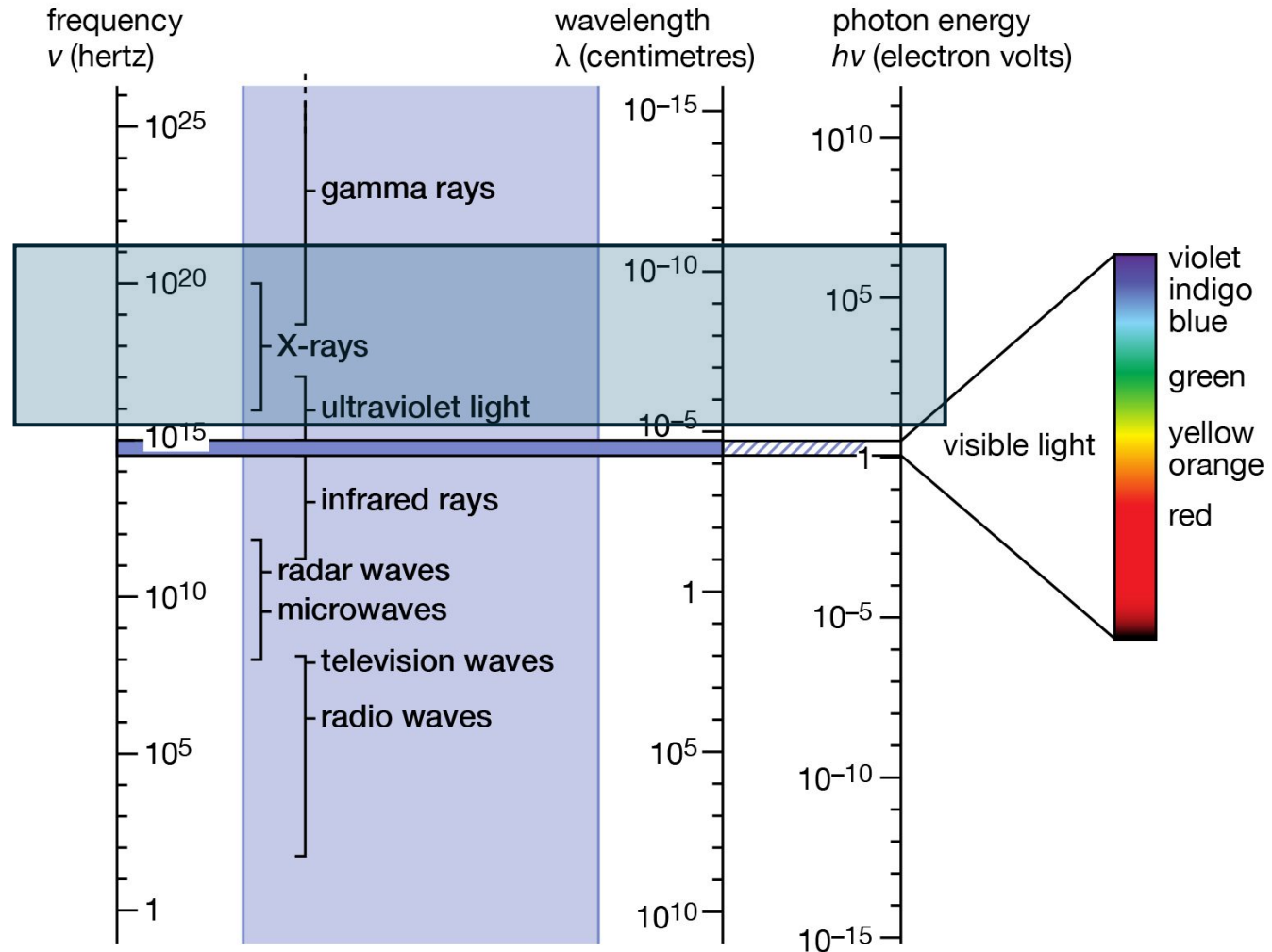


T. Young's double-slit experiment (1801)



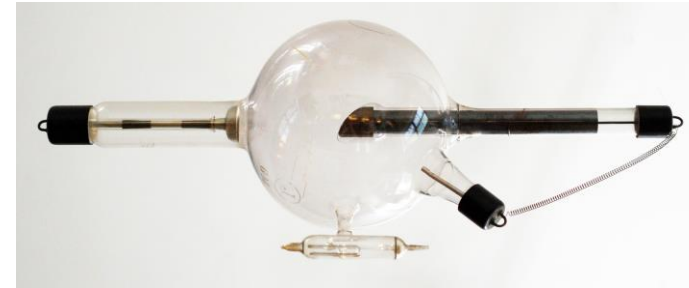
diffraction on the grating

# What are x-rays?



# Discovery and Utilization of X-rays

**1895** – Wilhelm Röntgen discovered X-rays. While experimenting with electric current flow in a partially evacuated glass tube, he noted that a radiation was emitted that affected photographic plates and caused a fluorescent substance across the room to emit light.



Crookes tube from early 1900s



Hand des Anatomischen Geheimraths von Kölliker in Würzburg.  
Im Physikalischen Institut der Universität Würzburg  
am 23. Januar 1896 mit X-Strahlen aufgenommen.  
von  
Professore Dr. W. C. Kötter.

**X-RAY FITTING**



**3. X-RAY FITTING TEST**



LEFT	RIGHT
<input type="checkbox"/>	<input type="checkbox"/>
<input type="checkbox"/>	<input type="checkbox"/>
<input type="checkbox"/>	<input type="checkbox"/>

**RIGHT WAY**      **GOOD**      **FAIR**      **POOR**      **WRONG WAY**

**CUSTOMERS**      **EXPECT IT!**



# Discovery and Utilization of X-rays

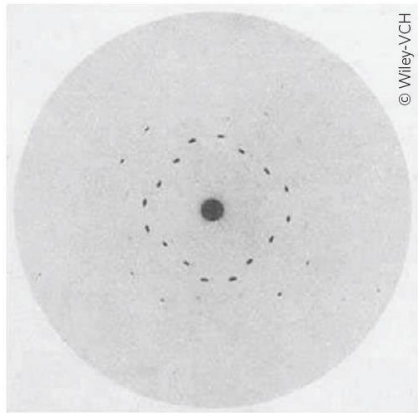
**1912** - the first observations of X-ray crystal diffraction by **W. Friedrich, P. Knipping** and **von Laue**.

**1912—1915 W. H. Bragg , W. L. Bragg, G. Wulff** interpreted diffraction in terms of reflection from crystal planes. They solved the crystal structures of NaCl and KCl and introduced Fourier analysis of the X-ray measurements.

**1920s** Diffraction at complex **organic crystals** (long-chain hydrocarbons, hexamethylbenzene, urea), **hairs, wool** fibers.

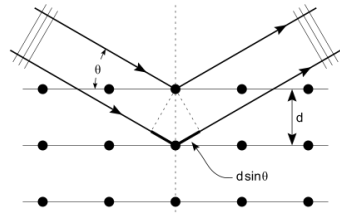
**1930** - Diffraction on **nerve fibers** at different humidities.

Late **1930s** - **Andre Guinier** developed his theory to show that X-ray scattering at small angles, around the direct beam direction, by non-crystalline solids and solutions contained information on particle size and shape.



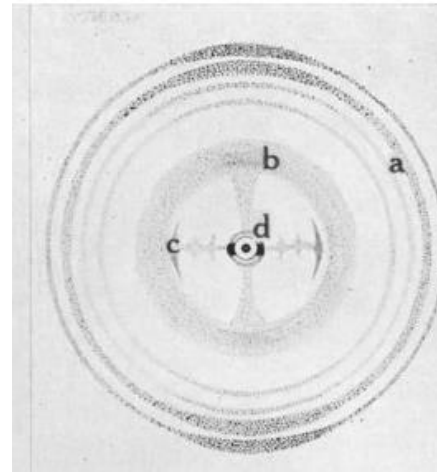
© Wiley-VCH

X-ray diffraction pattern from a zinc-blende (ZnS) crystal. Figure reprinted with permission from W. Friedrich et al. *Annalen der Physik* 346, 971-988 (1913).



Bragg-Wulff equation:

$$2 \cdot d \sin(\theta) = n\lambda$$



Schmitt, Francis O.; Bear, Richard S.; Clark, George L. (1935). X-ray Diffraction Studies on Nerve. *Radiology*, 25(2), 131-151.

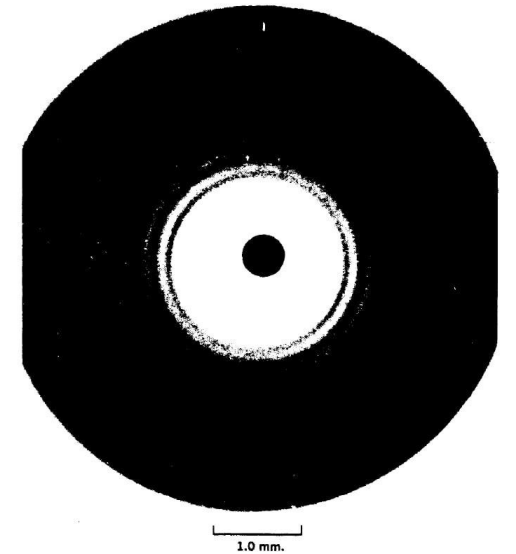


Fig. 41. Scattering pattern of uniform spherical particles (Dow Latex) obtained with a point-focusing monochromator (Fig. 32). The first visible ring is the fifth maximum (Fig. 6); on the original film, the rings are visible up to the seventeenth maximum. Sample-to-film distance: 66 cm. Cu K $\alpha$  radiation. Exposure time: 129 hours. (Danielson, Shenfi, and DuMond [25].)



**1953 - F. Crick, J. Watson, R. Franklin and M. Wilkins** published the double-helix structure of DNA calculated from X-ray fibre diffraction and chemical model building.

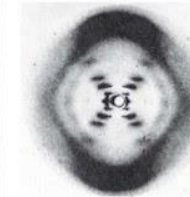


**Rosalind Franklin (1950's)**

- Worked with Maurice Wilkins
- X-ray crystallography = images of DNA
- Provided measurements on chemistry of DNA



(a) Rosalind Franklin



(b) Franklin's X-ray diffraction photograph of DNA

**James Watson & Francis Crick (1953)**

- Discovered the double helix by building models to conform to Franklin's X-ray data and Chargaff's Rules.



No. 4711 February 13, 1960 NATURE

**1960s** - Research groups led by **J. C. Kendrew** and **M. Perutz** published the first angstrom resolution structures of proteins (myoglobin and haemoglobin, respectively) from X-ray crystallography.

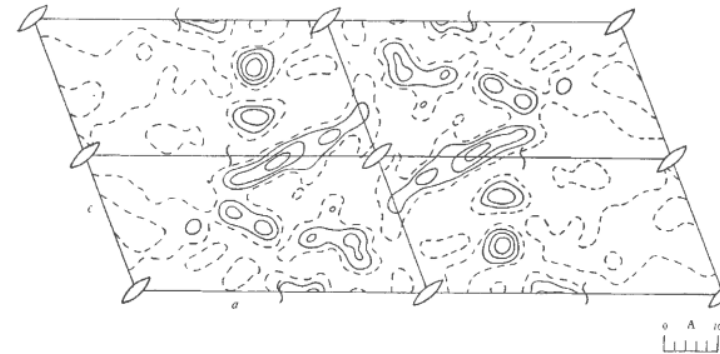


Fig. 1. Section at  $y = 1/32b$ . This cuts through the middle of the molecule on which the diagram is centred. 'Flat' areas indicating liquid appear on the left and right. Contours are drawn at intervals of 0.14 electron/Å<sup>3</sup>. The broken line marks 0.4 electron/Å<sup>3</sup>. Contours at lower levels are omitted

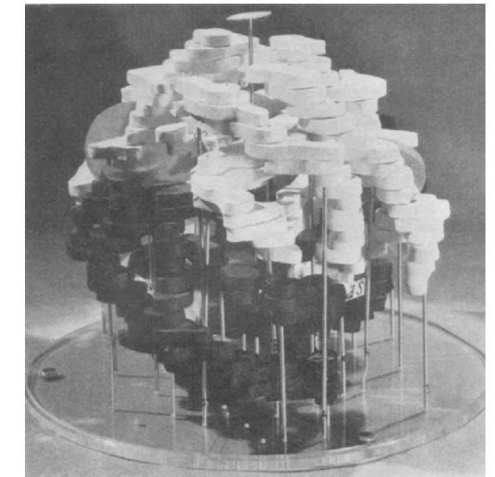
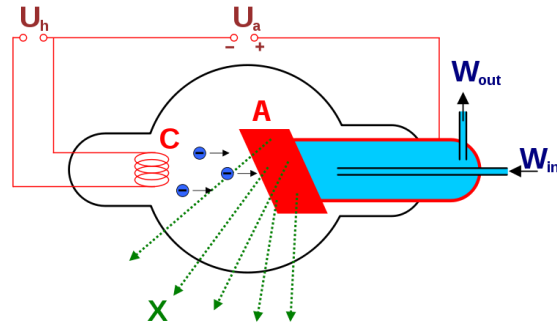


Fig. 9. Haemoglobin model viewed normal to c

**1980s** - The crystallization and first X-ray crystal structures of membrane proteins were obtained by using detergents. Because they are soluble only in complex solvents, the biochemical and structural study of membrane proteins lagged far behind that of water-soluble proteins.

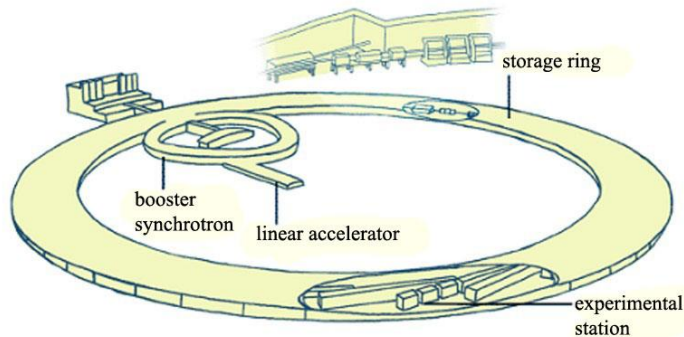


# X-ray Sources

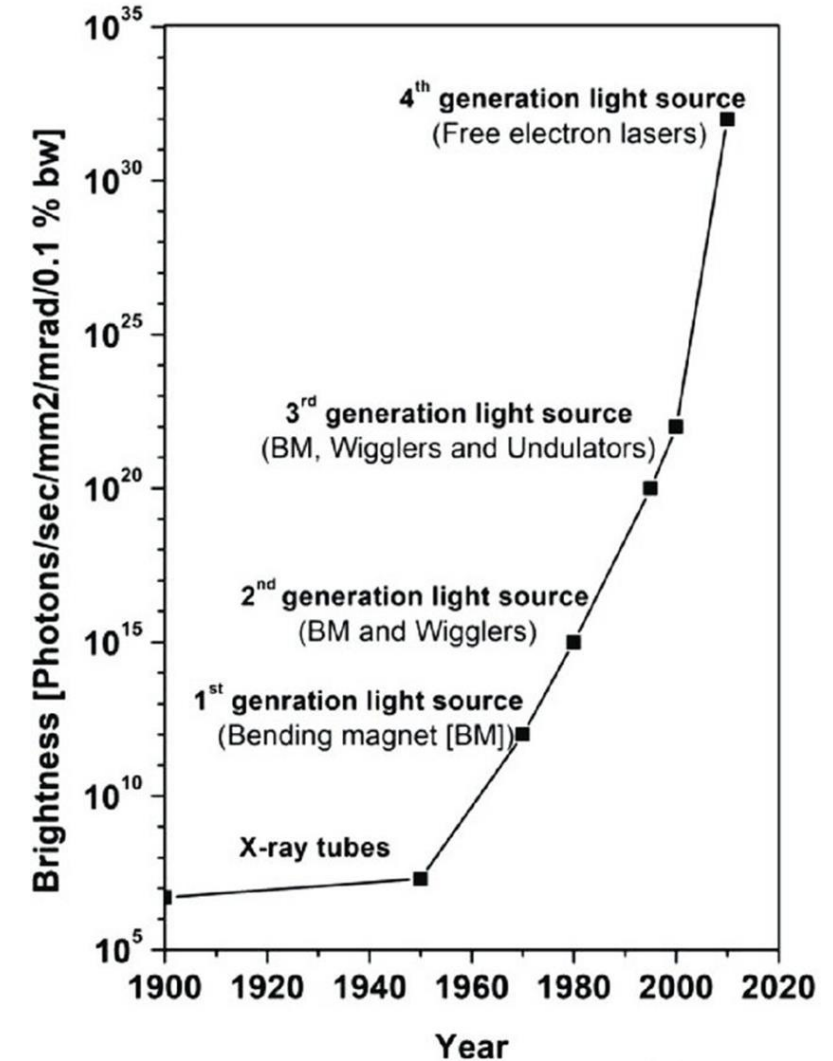


**X-RAY TUBE**  
Decelerating electron

1895- Wilhelm Conrad Röntgen investigated the external effects from the newly developed types of vacuum Crookes tube equipment



**SYNCHROTRON**  
Accelerating electron



1947 – Elder, Gurewitsch, Langmuir and Pollock – observation of synchrotron radiation

1961 – Synchrotron Ultraviolet Radiation Facility at NIST – the first generation synchrotron





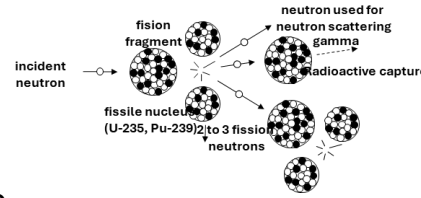
X-ray scattering station at FLNP JINR, Dubna

# Discovery and Utilization of Neutrons

1932 – James Chadwick - discovery of neutron



1936 - W. M. Elsasser, H. v. Halban & P. Preiswerk and D. P. Mitchell & P. N. Powers demonstrated diffraction of neutrons from a radium--beryllium source, and thus their **wave nature**.

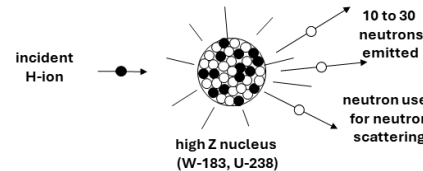


1933 – Leó Szilárd – the idea of nuclear chain reaction

1937 – Glenn T. Seaborg – concept of nuclear spallation

1942 – Enrico Fermi – the first artificial nuclear reactor Chicago Pile-1

1950-1954 – Ernest O. Lawrence – the first spallation source Materials Testing Accelerator



1945 and the following years

Neutron beams became available for diffraction experiments and crystallography.

C. Shull - the first **neutron diffraction** experiments

In the early 1950s, B. N. Brockhouse - the triple-axis spectrometer and measured **vibrations** in solids by neutron scattering.

1960s and 1970s

Neutron sources with neutron beams for the study of matter and biological membranes and macromolecules



C.G. Shull

Neutrons show where atoms are



B.N. Brockhouse

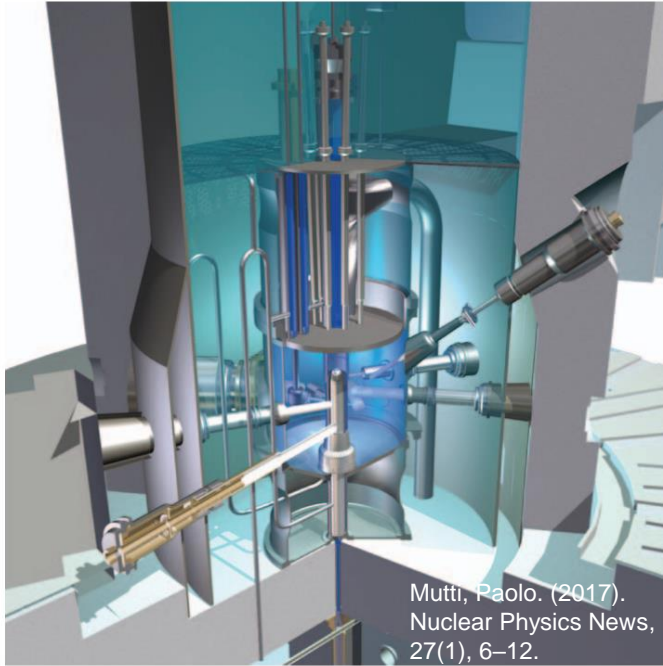
Neutrons show what atoms do



1994 - "for pioneering contributions to the development of neutron scattering techniques for studies of condensed matter"

# Neutron Sources

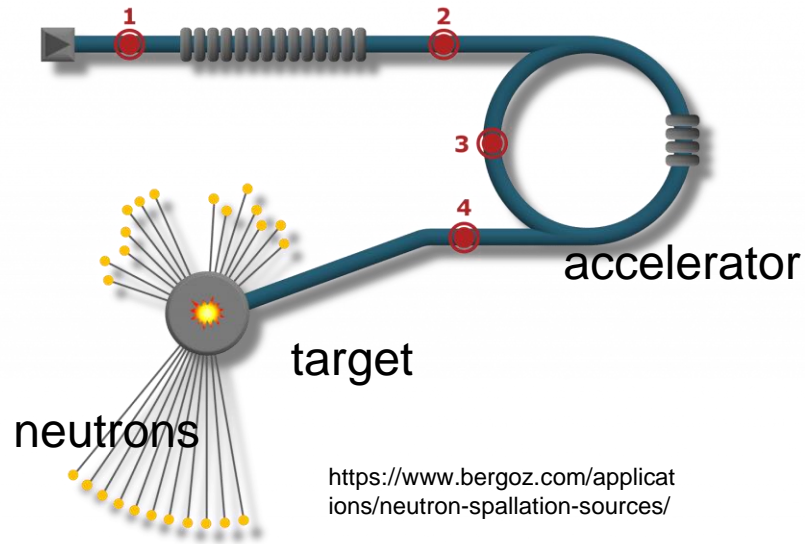
## 1. Continuous Reactors



ILL High-flux Reactor, Grenoble, France

Mutti, Paolo. (2017). Nuclear Physics News, 27(1), 6–12.

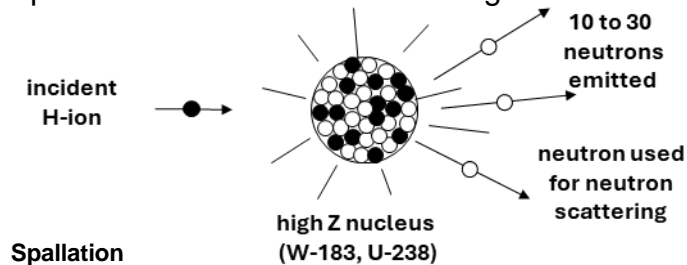
## 2. Spallation sources



<https://www.bergoz.com/applications/neutron-spallation-sources/>

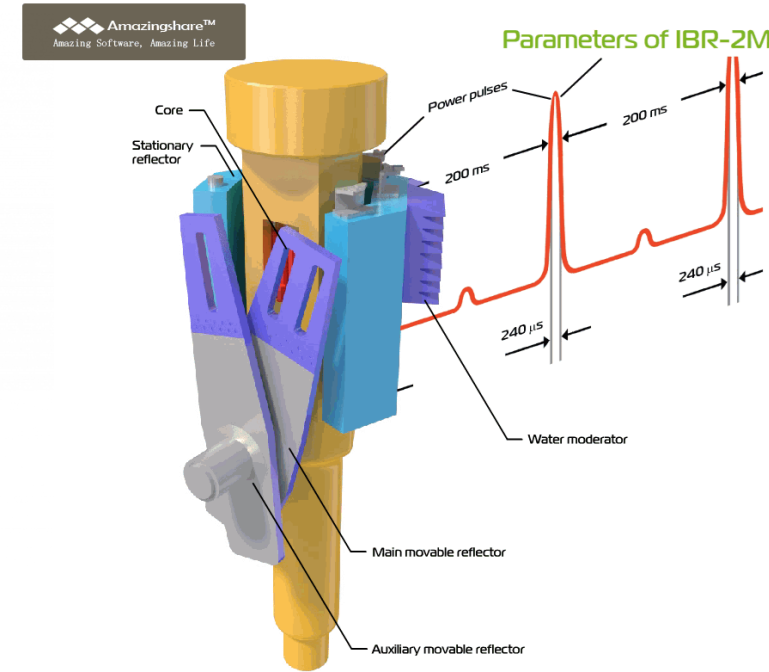
1937 – Glenn T. Seaborg – concept of nuclear spallation

1950-1954 – Ernest O. Lawrence – the first spallation source Materials Testing Accelerator



Spallation

## 3. Pulsed Reactors



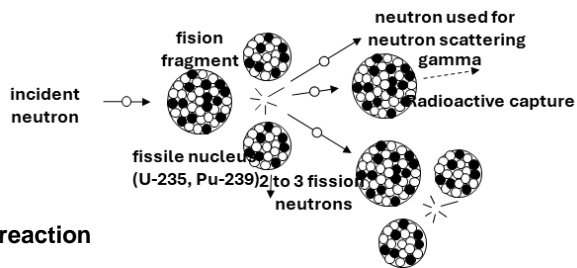
IBR-2 fast neutron pulse reactor (with a periodic operation), Dubna, Russia

1955 – Dimitry I. Blokhintsev – the idea of pulsed reactor

1960 – Ilya M. Frank & Fyodor L. Shapiro – the pulsed reactor IBR

1933 – Leó Szilárd – the idea of nuclear chain reaction

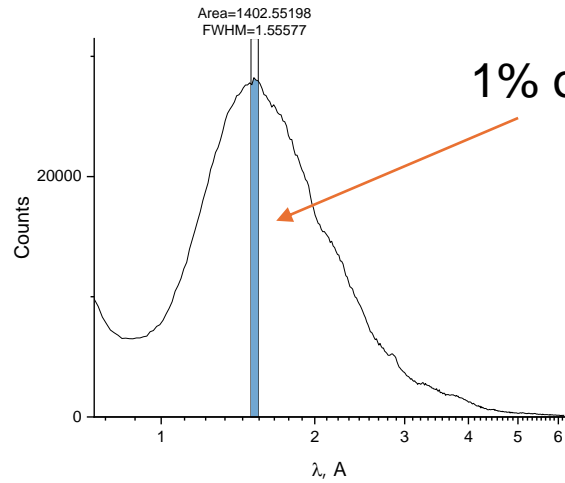
1947-1993 & 1957 – National Research eXperimental & National Research Universal reactors



nuclear chain reaction

# Continuous Reactors

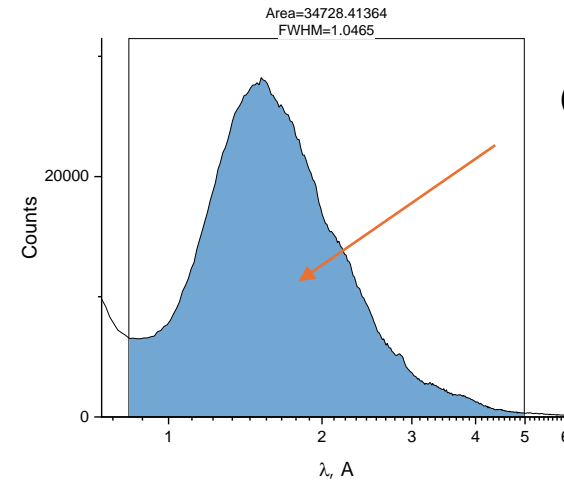
$$\lambda = const$$



# Pulsed sources

Time of flight technique (TOF)

$$\lambda = \frac{h}{mv} = \frac{t \cdot h}{m \cdot L}$$



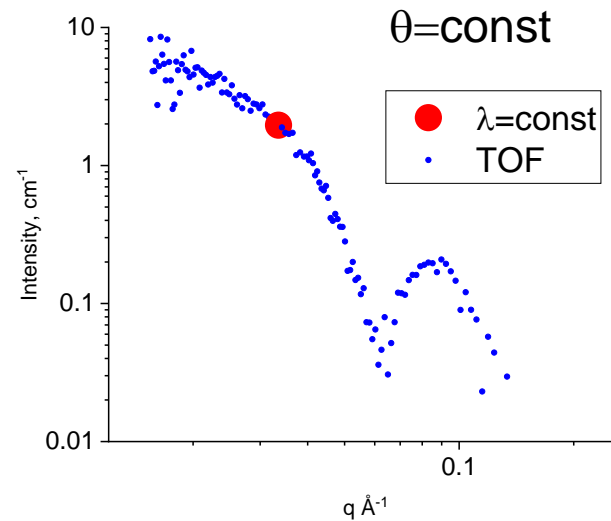
## Dynamic range

$$\frac{q_{max}}{q_{min}} = \frac{\theta_{max}}{\theta_{min}}$$

$$\frac{q_{max}}{q_{min}} = \frac{\theta_{max}}{\theta_{min}} \cdot \frac{\lambda_{max}}{\lambda_{min}}$$


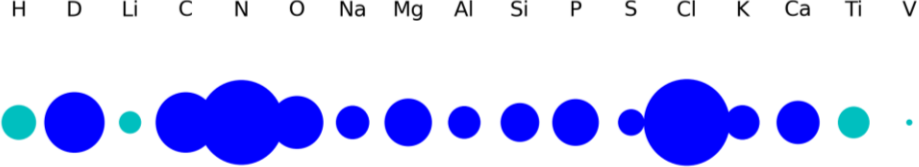

Scattering vector

$$q = \frac{4\pi \sin \vartheta}{\lambda}$$



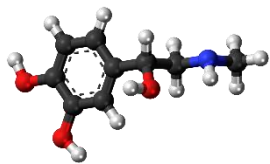
Factor = 10

# X-ray and neutron characteristics

X-ray	Neutron
Scatters at the <b>electrons</b> of the atomic shell	Scattered by the <b>atomic nucleus</b>
<p><b>Scattering length</b> (“scattering power”) of an atom increases with its <b>number of electrons</b>.</p>  <p>H D Li C N O Na Mg Al Si P S Cl K Ca Ti V</p>	<p><b>Scattering length</b> shows a <b>random</b> way of nucleus dependence</p>  <p>H D Li C N O Na Mg Al Si P S Cl K Ca Ti V</p>
<p><b>No isotope effect</b> Heavy atoms dominate the diffraction pattern</p>	<p>Different <b>isotopes</b> of the same element <b>can be very different</b>; hydrogen (1H) and deuterium (2H or D) is of particular interest in structural biology</p>
$\lambda \sim 1\text{\AA}$	$\lambda \sim 0.5\text{-}10\text{\AA}$
<p>E of electrons <math>\sim 10\,000\text{ eV}</math> far from movements in the matter More challenge task</p>	<p>Energy of movements in the matter: <math>10^{-9}\text{ eV} - 1\text{ eV}</math> Average E of neutrons <math>\sim 0.08\text{ eV}</math> - <b>Ideal tool for dynamical investigations</b></p>
<p>Researching properties of magnetic materials is more <b>challenge</b></p>	<p>Spin = <math>\frac{1}{2}</math> (magnetic dipole moment) <b>The smallest magnetometer</b></p> 
<p>Hight absorption by heavy elements</p>	<p>Deep penetration into matter</p>
<p>Simpler construction of sources Hight intensity</p>	<p>Creating neutron sources is a more difficult task</p>

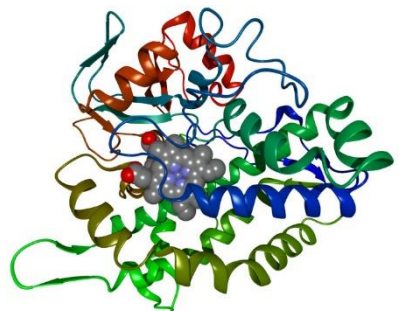


# Space range of investigated objects



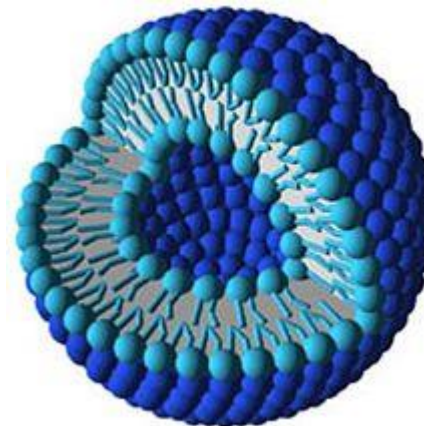
## Molecules

(water, bioactive molecules, peptides, sugars etc)



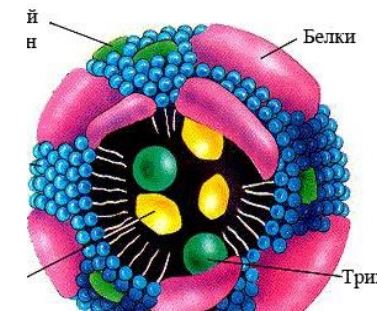
## Biopolymers

(proteins, RNA, DNA, polysaccharides)



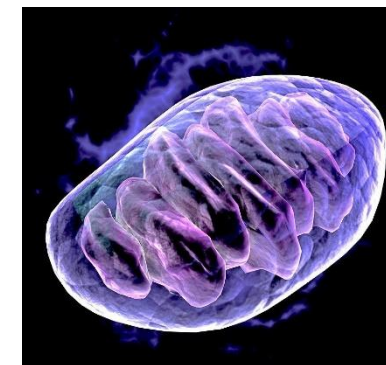
## Aggregates

(micelles, model lipid and biological membranes)



## Multicomponent complex

(multi-subunit proteins, membranes, lipoproteins, fibrills, protein-DNA/RNA complexes, chromatin)

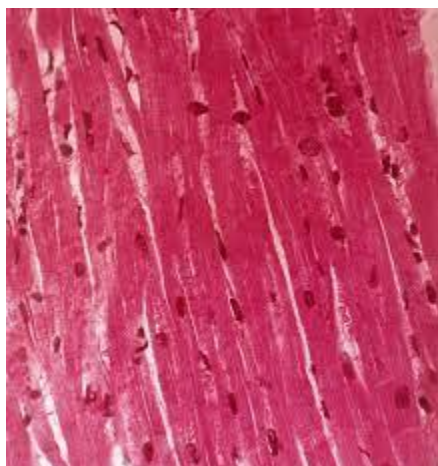


## Organelles

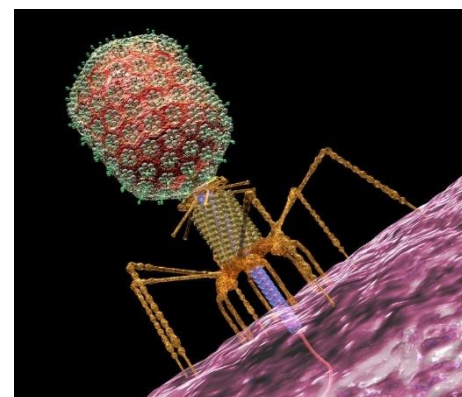
14



## Multicellular organisms



## Tissues



## Unicellular organisms

(bacteria, viruses)



# Time range (spectroscopy) Dynamical properties

psec – 100 nsec

- Autocorrelation vibrations of atoms
- Substrate binding to the catalytic center, conformational changes
- Conformational mobility of subunits in protein and other macromolecular complexes (*spin-echo NSE*, ps-100ns)
- Diffusion and rotation of lipid molecules in membranes, lipid raft formation
- Membrane Undulation: physical and mechanical properties of the membrane (flexural modulus)
- Protein folding
- Dynamics of the hydration shell of macromolecules.
- Movement of water in cells (*QENS*, *NSE*)

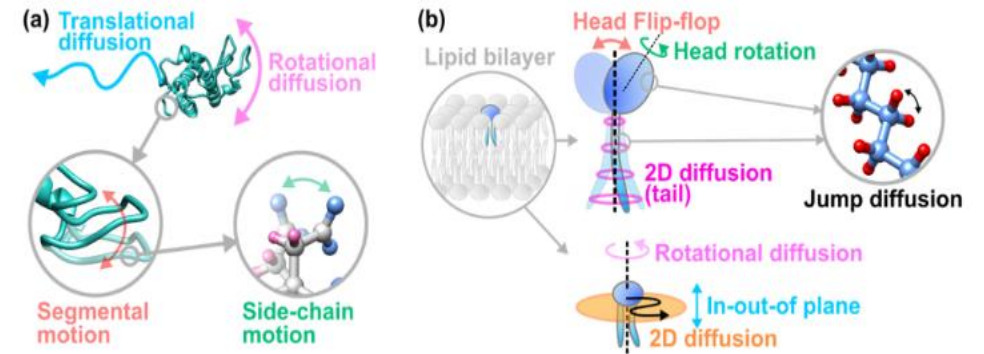
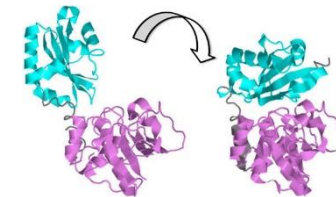
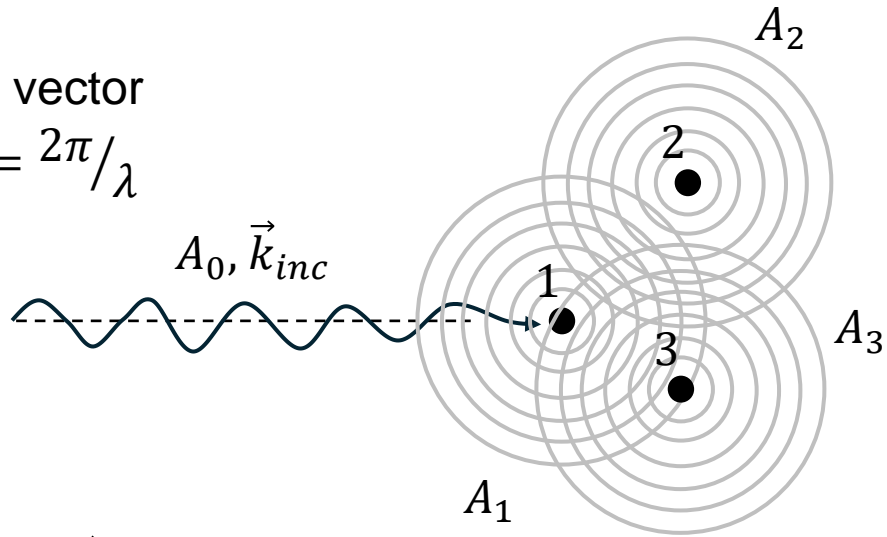


Figure 1. Hierarchical intramolecular motions observed by iNS for proteins (a) and lipid molecules (b). Classification of the motions of lipid molecules is based on the latest theoretical dynamical model called the Matryoshka model [15]. This figure is adapted from Ref. [16] with permission.



wave vector

$$k_{inc} = 2\pi/\lambda$$



$$A_0 = e^{i\vec{k}_{inc}\vec{r}}$$

$$A_1 = A_0 b_1 \frac{e^{i\vec{k}_{sc}\vec{R}}}{|\vec{R}|}$$

$$A_2 = A_0 b_2 \frac{e^{i\vec{k}_{sc}\vec{R}}}{|\vec{R}|}$$

$$A_3 = A_0 b_3 \frac{e^{i\vec{k}_{sc}\vec{R}}}{|\vec{R}|}$$

1, 2, 3, ... etc = j

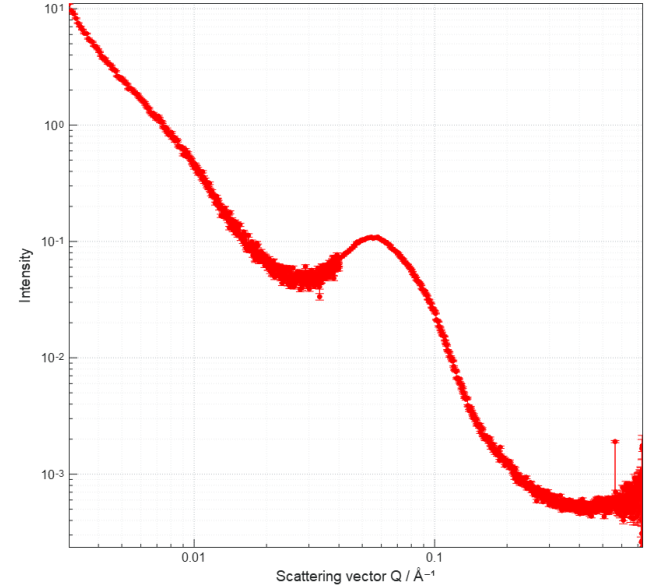
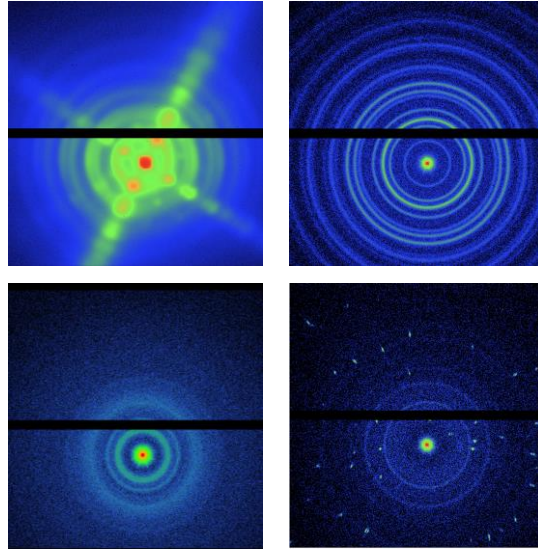
$$A = A_0 e^{i\vec{k}_{inc}\vec{r}} \cdot \sum_{j=1}^N A_j$$

**Scattering intensity**

$$I(q) = \langle A_s(\vec{R}) \cdot A_s^*(\vec{R}) \rangle = \frac{A_0^2}{R^2} \sum_{j,k=1}^N b_j b_k e^{i\vec{q}(\vec{r}_j - \vec{r}_k)}$$

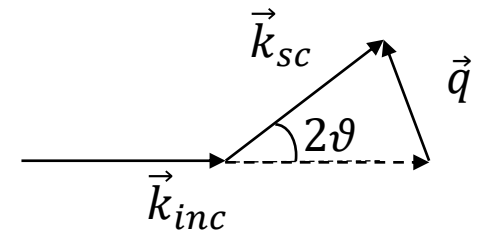
**For continuous medium**

$$I(q) = \left\langle \left| \int_V \rho(\vec{r}) e^{i\vec{q}\cdot\vec{r}} d\vec{r} \right|^2 \right\rangle$$



$A$  – Scattering amplitude  
 $\vec{k} = 4\pi/\lambda$  – wave vector  
 $b$  – scattering length  
 $\rho$  – scattering density  
 $\vec{q}$  – scattering vector

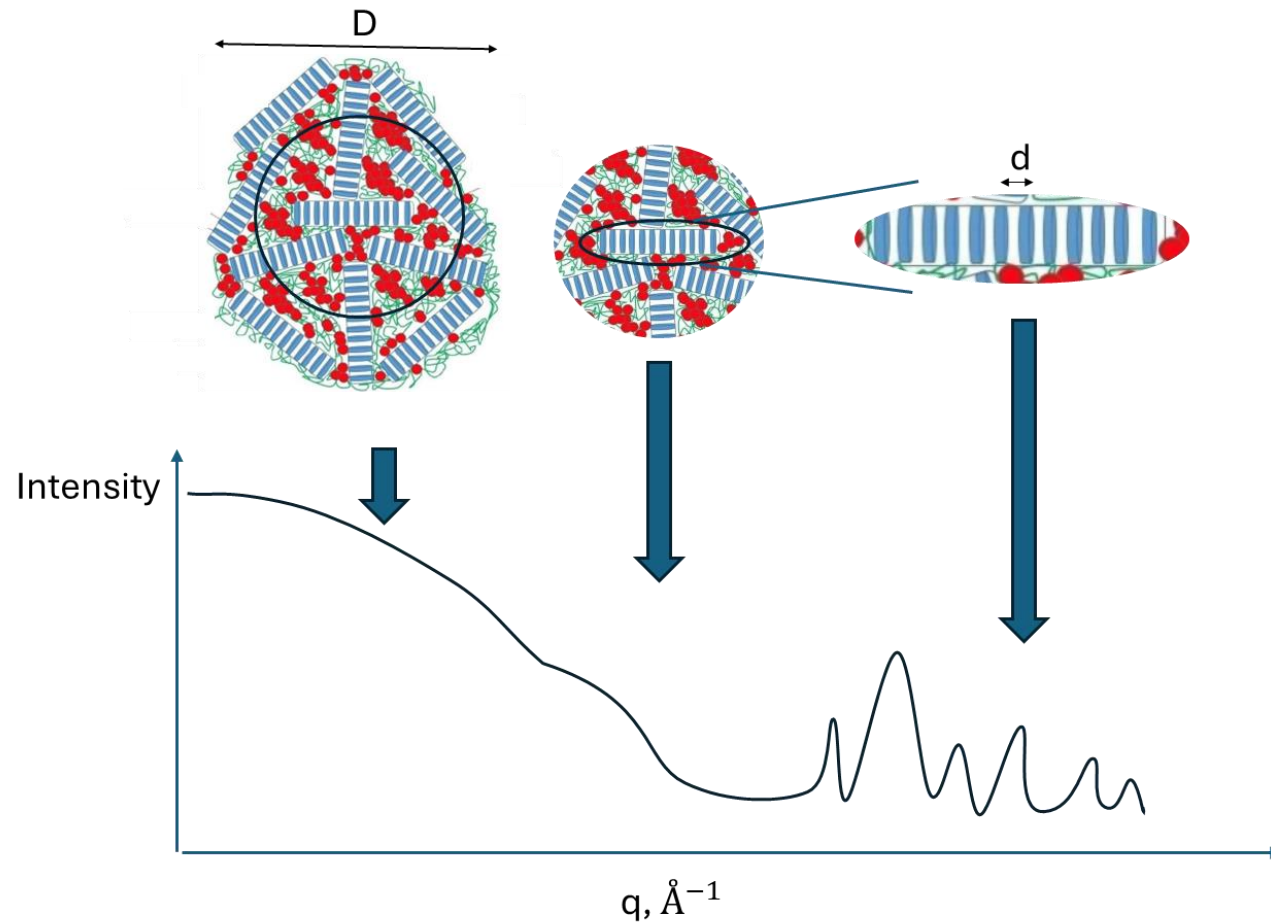
Scattering vector



$$\rho = \frac{\sum b_i}{V}$$

$$q = \frac{4\pi \sin \vartheta}{\lambda}$$

# Real space vs Reciprocal space



**Real space**

$$[D] = \frac{2\pi}{q} [\text{\AA}]$$

**Reciprocal space**

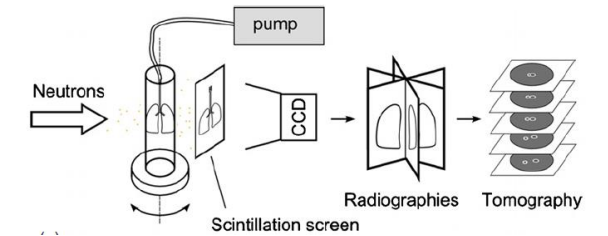
$$[q] = \frac{4\pi}{\lambda} \sin \vartheta [\text{\AA}^{-1}]$$



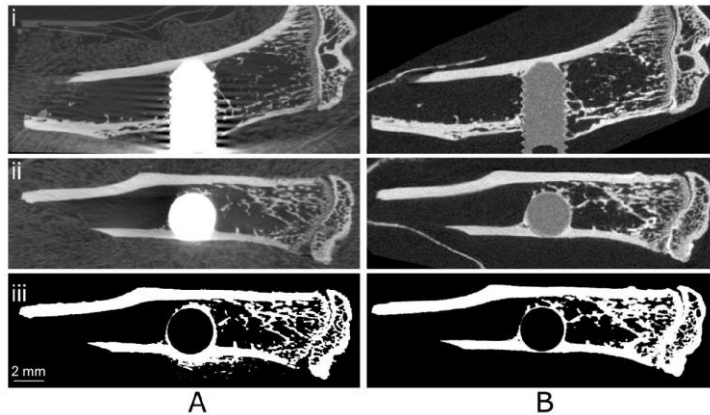
# X-ray and neutron Imaging Techniques

**X-ray** – beam attenuation depends on density

**Neutron** - no density dependence;  
 - good penetration;  
 - direct visualization of the hydrogen distribution

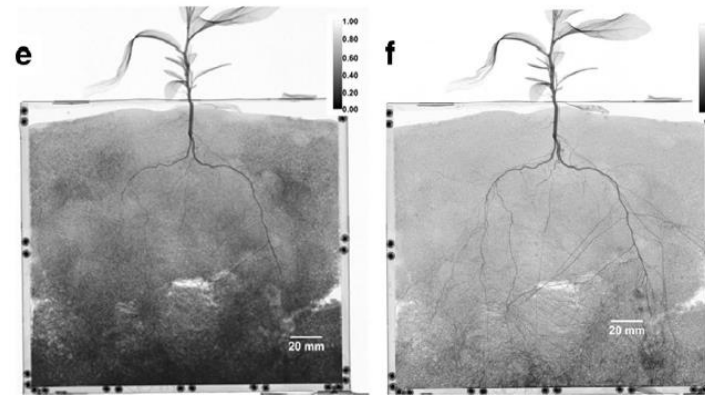


X-Ray      Neutron



Comparison of images obtained with (A) X-ray tomography (Zeiss-XRM520 laboratory tomograph, 26 μm voxel size) and (B) neutron tomography (13.5 μm voxel size)

Remodeling of bone tissue at the border with a metal implant



Neutron imaging.

Water distribution in newer root system: water absorption; root growth; influence of extreme drought and soil pollution. (e) initial radiograph prior to drying cycle, (f) final radiograph after 2-day drying cycle

Dhiman, I., et al. Quantifying root water extraction after drought recovery using sub-mm in situ empirical data. *Plant Soil* **424**, 73–89 (2018).

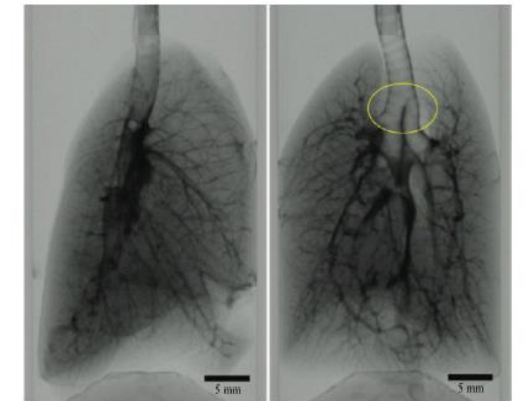


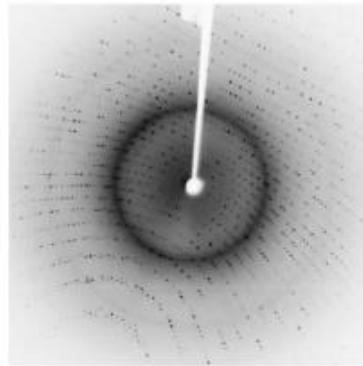
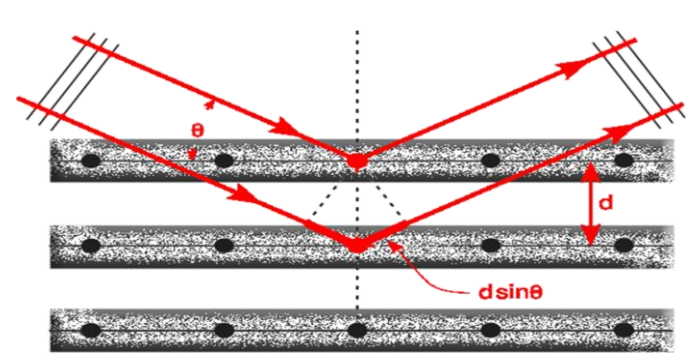
Figure 17 Left: photograph of a rat lung at the neutron beamline. Right: lateral and frontal neutron radiographs of the lung showing the lung physiology such as the trachea, lobes and airways (Metzke et al., 2011). The spatial resolution was approximately 50–60 μm. The yellow ellipse indicates the first bifurcation. Videos of the nCT data are available at <http://iopscience.iop.org/article/10.1088/0031-9155/56/1/N01/data#>.

Good contrast between air and tissue, distribution of air in the lungs. Without contrast media.

Metzke RW, et al. Neutron computed tomography of rat lungs. *Phys Med Biol.* 2011 Jan 7;56(1):N1-N10.



# X-ray/neutron protein crystallography



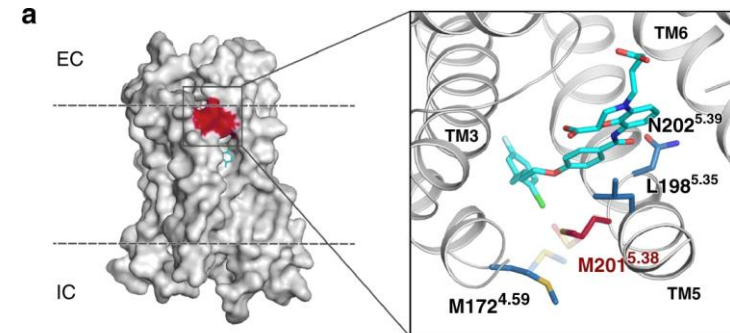
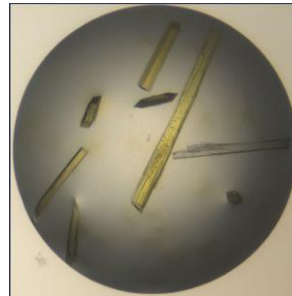
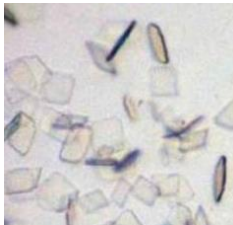
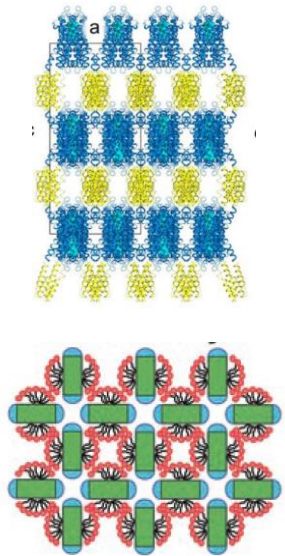
## The Bragg's Law

The two planes will scatter in phase if the path difference '2 d sin(q)' is a whole number of wavelengths 'n λ':

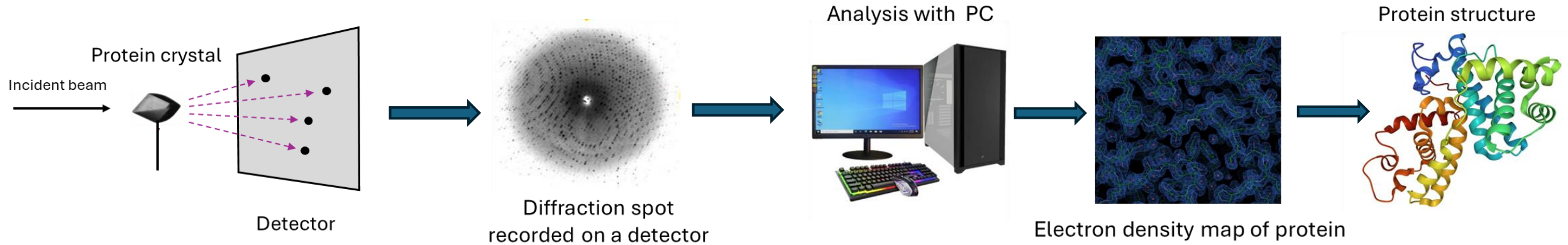
$$2 \cdot d \sin(\theta) = n\lambda$$

## Why do we need protein crystals?

1. Understanding the mechanisms of functioning of living systems at the atomic level
2. Developing drugs (Rational design)
3. Proteins – the main target for drug design



# Principle of protein crystallography



Sample preparation

Overexpression

Purification

Crystallization

Diffraction experiment

Diffraction data collection

Structural analysis

Calculating of electron density

Model building

# Advantages of neutron protein crystallography

## Limits for x-ray

- **Hydrogen are invisible** by x-ray -> position of H are extrapolated from chemical knowledge
- **Radiation damage** -> artefacts. Essential for proteins contained Metals and redox –cofactors
- **Cryo-temperatures** - frozen crystals at -170 -180 oC

## Advantages of neutrons

- Can see Hydrogen and Water
- Non- destructive
- Physiologically relevant temperatures

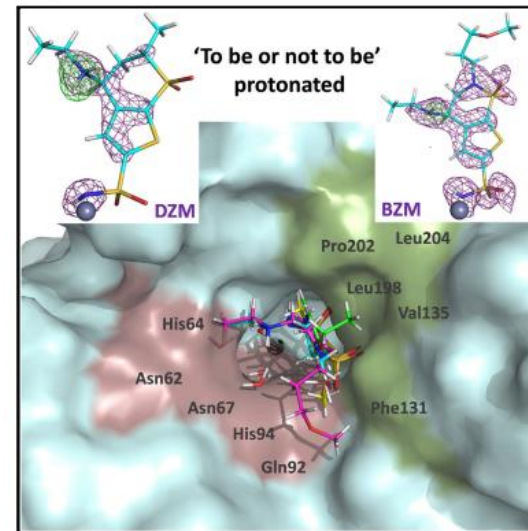
## Special tasks for neutrons

- Investigation of enzyme catalytic mechanisms,
- Direct experimental insight into chemical reactions
- Mechanism of redox enzymes (no radiation damage)
- Location of hydrogen bond network governing ligand binding (e.g. pharmaceutical drugs)
- Proton transfer pathways

## Problems in neutron experiments

- Growing large crystals
- Deuterating crystals (for decreasing noise)
- Long time of measuring

**50% total atoms in biomolecules are HYDROGENS**



## Human Carbonic Anhydrase hCA II (15 isomers)

Catalyzes the reversible hydration of CO<sub>2</sub>.

- Glaucoma
- Epilepsy
- Altitude sickness
- Some types of cancer

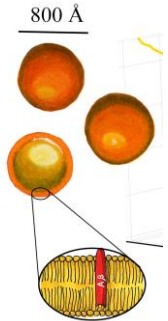
The **position of hydrogen atoms** has been determined. The network of hydrogen bonds has been found; that gives the idea of introducing an additional hydrogen into drug's structure to enhance its binding with active site.

**X-ray** – the tail of brinzolamide is located in a hydrophobic pocket (low temperatures)

**Neutrons** – in a hydrophilic pocket (room temperatures)

--> It is necessary to pay attention to hydrophilic pockets in other isomers hCA

# Small angle scattering

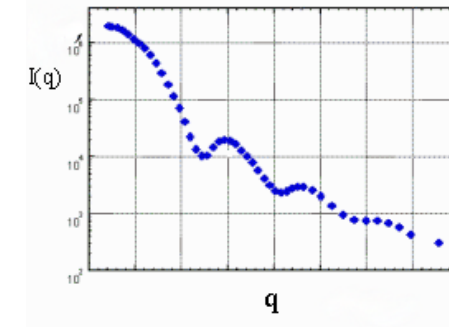


## Fields

- Biology
- Colloid chemistry
- Materials Science
- Solid State
- Polymer physics

## Type of objects

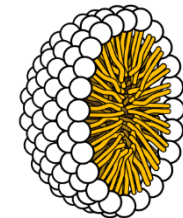
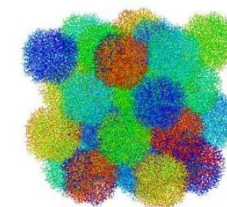
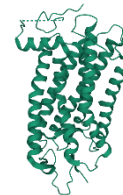
- Solutions of macromolecules and their complexes
- Alloys
- Films
- Powders



## Structural information:

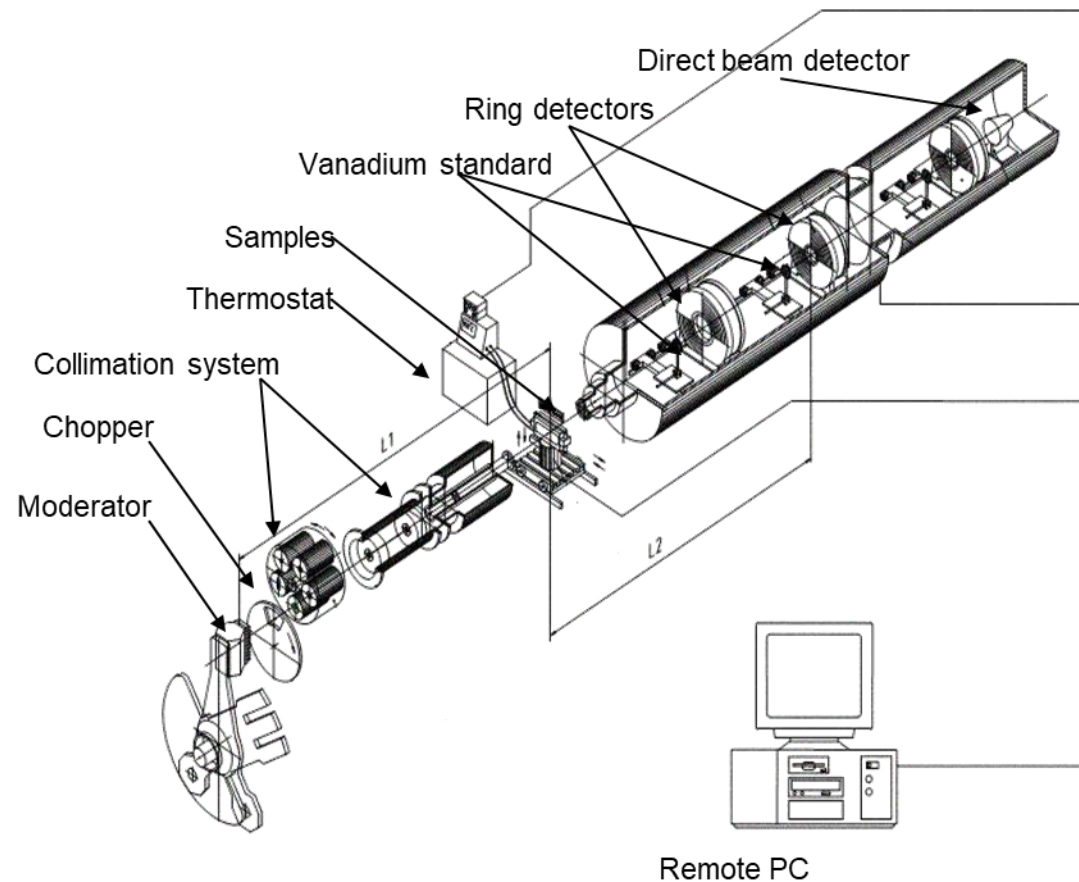
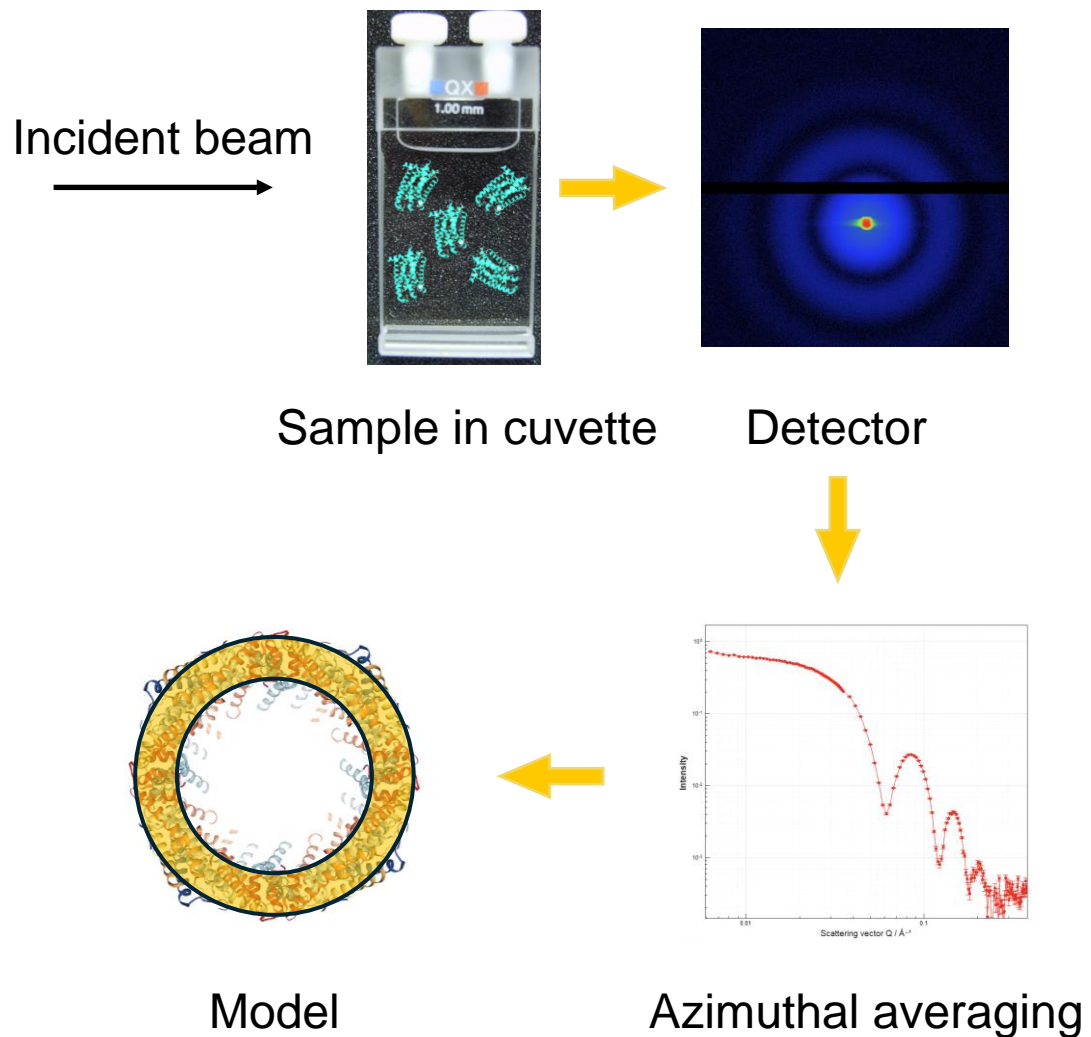
10-1000 Å

- Size, volume, molecular weight
- Form
- Conformation
- Oligomeric state
- 3D structures with  $\sim 10$  Å resolution



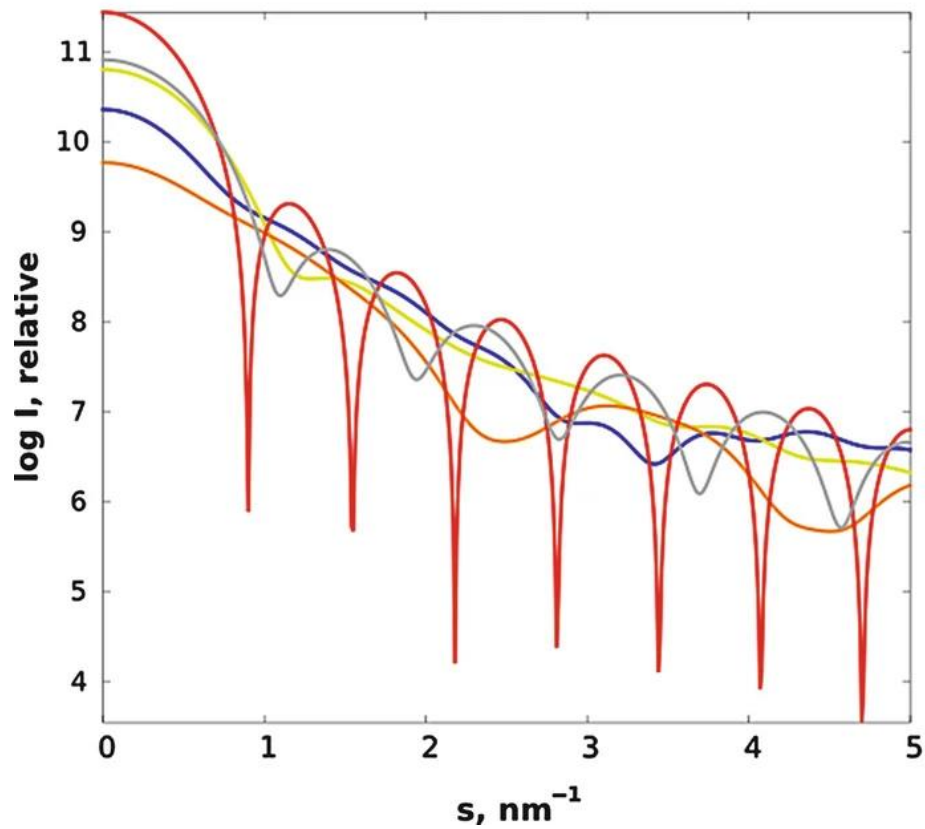


# Small angle scattering experiment



YuMO SANS-spectrometer at IBR-2 reactor, Dubna. Russia

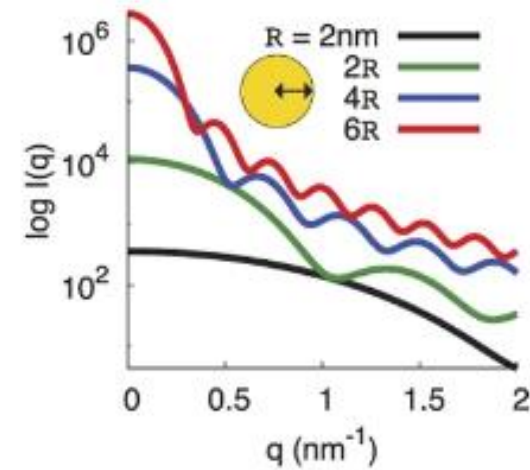
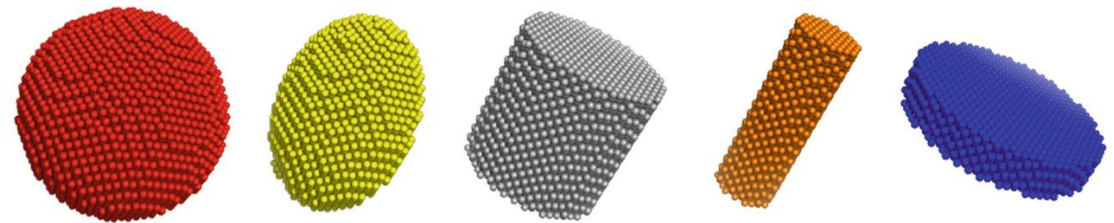




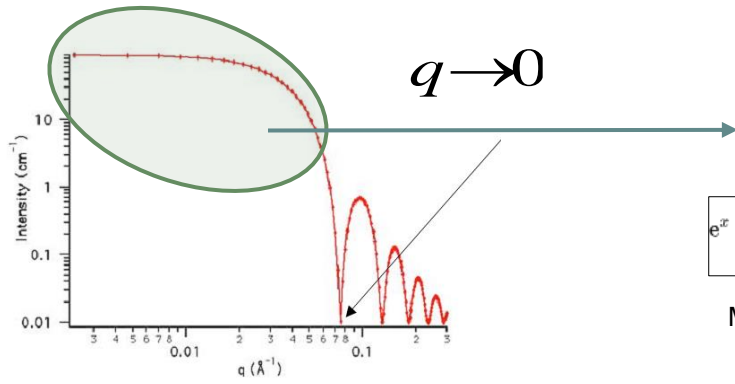
Size

Shape

Surface



# Guinier Regime



$$e^x = 1 + \frac{x}{1!} + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$$

Maclaurin series

$$I(q) = \left| \int_V \rho(\vec{r}) e^{i\vec{q}\vec{r}} d\vec{r} \right|^2$$

$\downarrow q \rightarrow 0 \rightarrow$

$$I(q) \sim V^2 \left[ 1 - \frac{q^2 R_g^2}{3!} + \dots \right]^2 \approx V^2 e^{-\frac{q^2 R_g^2}{3}}$$



$$I(q) = \text{const} \cdot e^{-\frac{1}{3} R_g^2 q^2}$$



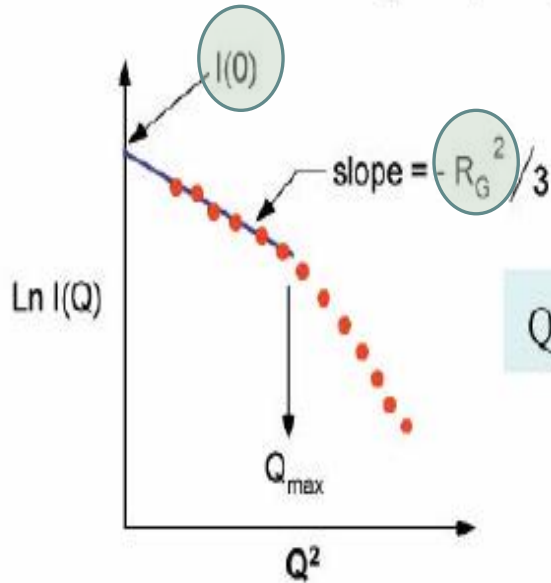
$$qI(q) = \text{const} \cdot e^{-\frac{1}{2} R_g^2 q^2}$$



$$q^2 I(q) = \text{const} \cdot e^{-R_g^2 q^2}$$

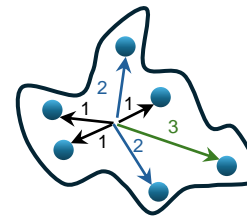
Guinier Plot

$$\ln[I(Q)] = \ln[I(0)] - Q^2 R_G^2 / 3$$



**Radius of gyration**

$R_g^2$  is the average squared distance of the scatterers from the centre of the object



$$R_g^2 = (1^2 + 1^2 + 1^2 + 2^2 + 2^2 + 3^2) / 6 = 20/6$$

$$R_g^2 = \sqrt{3.333} = 1.82$$

**Radius of gyration depends on particle shape**

Objects	$\langle R_G^2 \rangle^{1/2}$
Sphere with a radius $R$	$\sqrt{\frac{3}{5}} R$
Spherical shell with an outer and inner radius of $R_o$ and $R_i$ , respectively	$\sqrt{\frac{3(R_o^5 - R_i^5)}{5(R_o^3 - R_i^3)}}$
Cylinder with a radius $R$ and a length $t$ ; therefore:	$\sqrt{\frac{R^2}{2} + \frac{t^2}{12}}$
Long rod: $R \rightarrow 0$ and $t \gg R$	$\frac{t}{\sqrt{12}}$
Thin disk: $t \rightarrow 0$ and $R \gg t$	$\frac{R}{\sqrt{2}}$

# Molecular mass estimation

$$I(0) = \left| \int_V \rho(\vec{r}) d\vec{r} \right|^2 \xrightarrow{\rho = \text{const}} (\rho V)^2$$

Molecular weight:

$$MW = \frac{I(0) N_A}{c(\bar{\rho} - \rho_{buffer})^2 v^2}$$

$N_A$  - Avogadro's number

$c$  - concentration

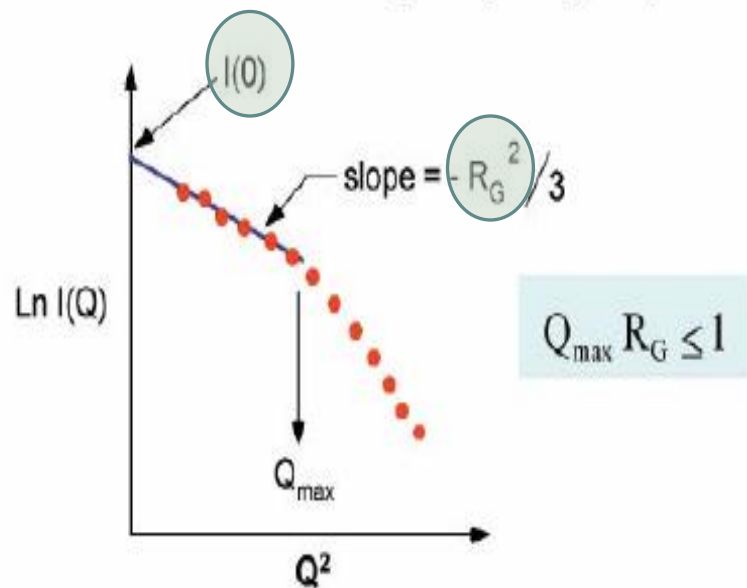
$\rho_{buffer}$  - scattering density of a buffer

$\bar{\rho}$  - scattering density of a studied molecule

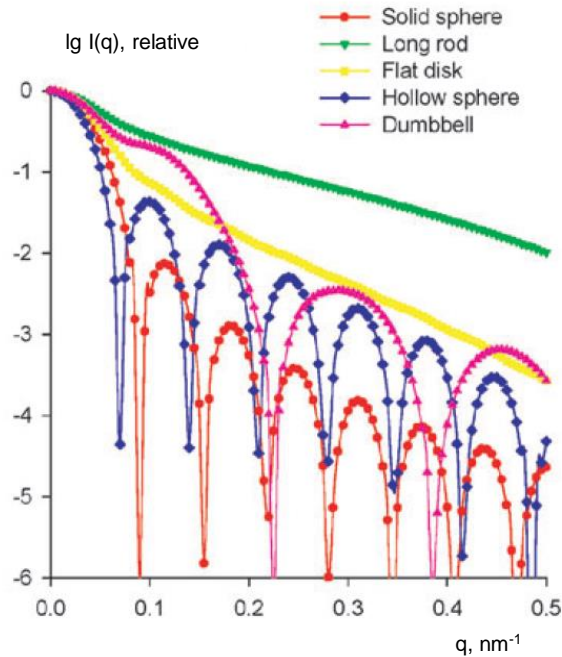
$v$  - partial specific volume, cm<sup>3</sup>/g

Guinier Plot

$$\ln[I(Q)] = \ln[I(0)] - Q^2 R_G^2 / 3$$

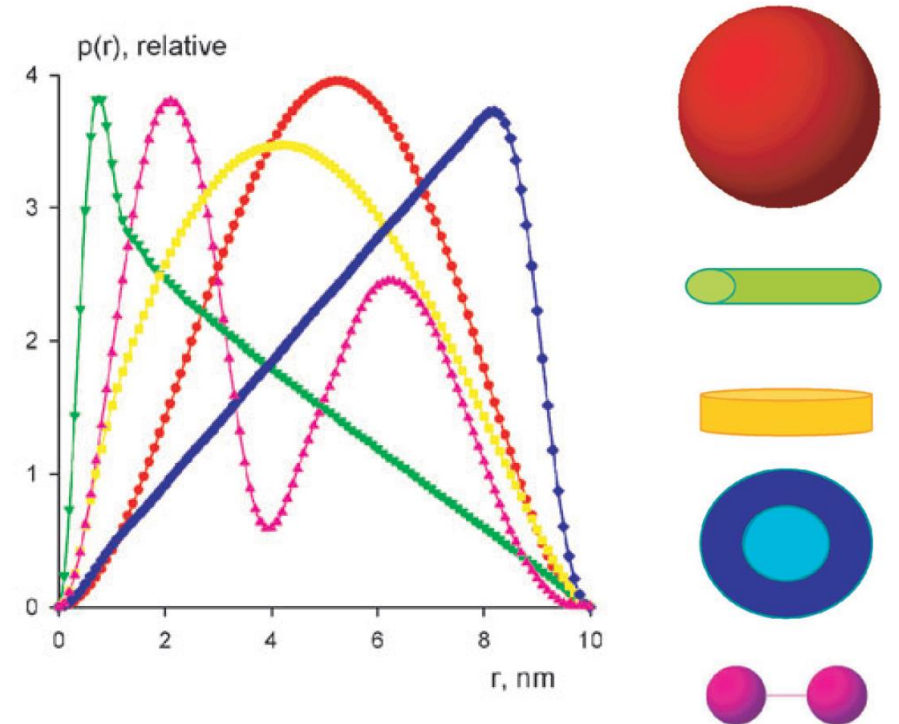


# Pair distance distribution function



$$P(r) = \frac{r^2}{2\pi} \int_0^\infty q^2 I(q) \frac{\sin(qr)}{qr} dr$$

Fourier Transform



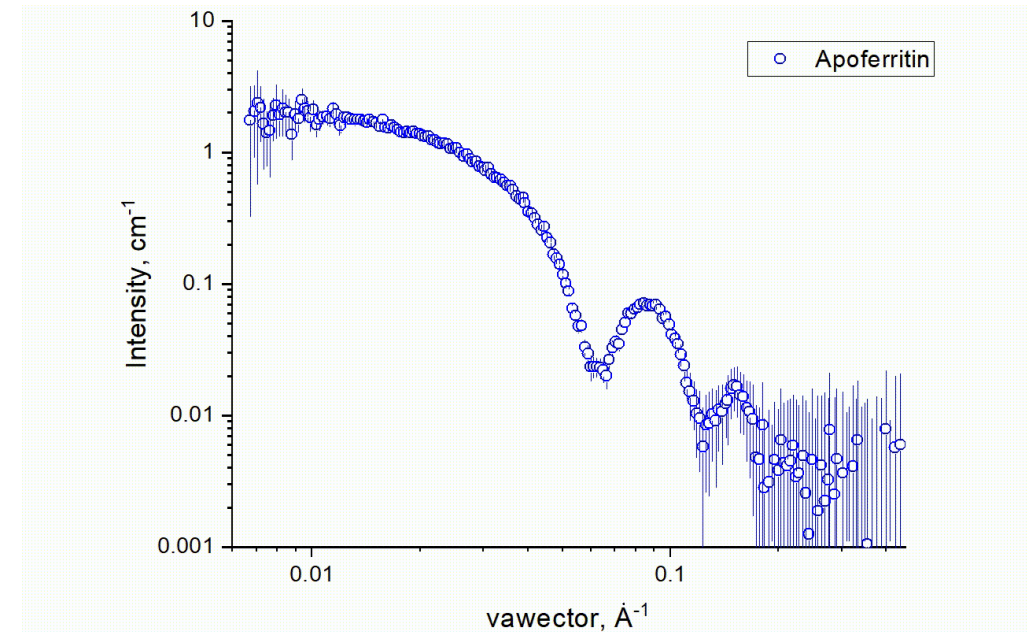
Scattering intensities of geometrical bodies with the same maximum size

distance distribution functions of geometrical bodies with the same maximum size

# Analytical functions (Form factors)

## Common form factors of particulate systems

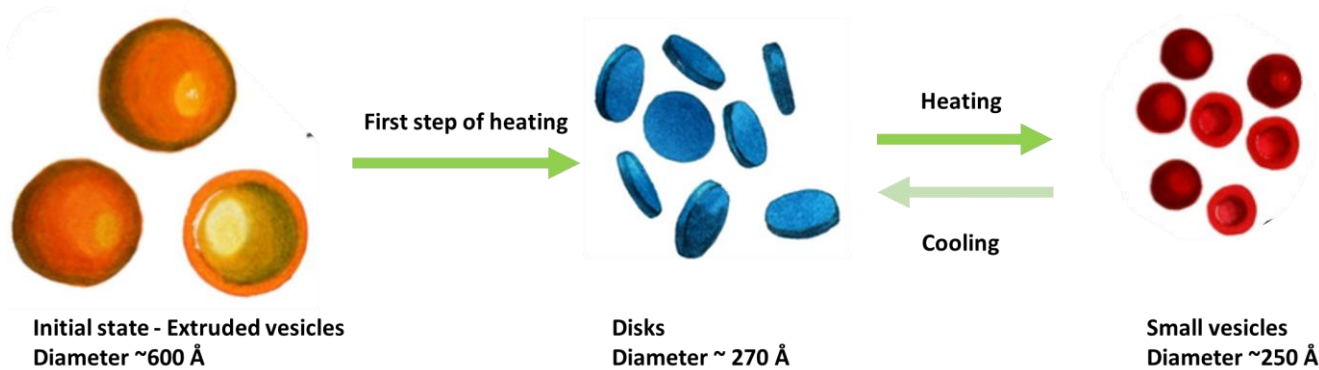
Morphologies	P(q)	Remarks
<b>Spheres</b> (radius :R)	$\frac{9}{(qR)^6} [\sin(qR) - qR \cdot \cos(qR)]^2 = A_{\text{sph}}^2(qR)$	
<b>Spherical shells</b> (outer radius: R <sub>1</sub> inner radius: R <sub>2</sub> )	$\frac{[R_1^3 \cdot A_{\text{sph}}(qR_1) - R_2^3 \cdot A_{\text{sph}}(qR_2)]^2}{(R_1^3 - R_2^3)^2}$	
<b>Triaxial ellipsoids</b> (semiaxes: a,b,c)	$\int_0^1 \int_0^1 A_{\text{sph}}^2 [q \sqrt{a^2 \cos^2(\pi x/2) + b^2 \sin^2(\pi x/2)(1-y^2) + c^2 y^2}] dx dy$	<ul style="list-style-type: none"> <li>• Integration of x and y are for orientational average.</li> <li>• J<sub>1</sub>(x) is the first kind Bessel function of order 1</li> </ul>
<b>Cylinders</b> (radius: R length: L)	$4 \int_0^1 \frac{J_1^2[qR\sqrt{1-x^2}]}{[qR\sqrt{1-x^2}]^2} \frac{\sin^2(qLx/2)}{(qLx/2)^2} dx$	
<b>Disk</b> (radius: R infinitely thin)	By setting L = 0 $\frac{2 - J_1(2qR)/qR}{q^2 R^2}$	
<b>Rod</b> (length: L infinitely thin)	By setting R = 0 $\frac{2}{qL} \int_0^{qL} \frac{\sin(t)}{t} dt - \frac{\sin^2(qL/2)}{(qL/2)^2}$	



by A. Ivankov



# Amyloid Beta Peptide changes the morphology of lipid membrane

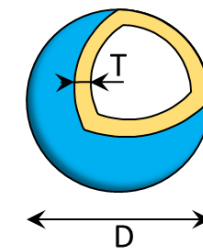
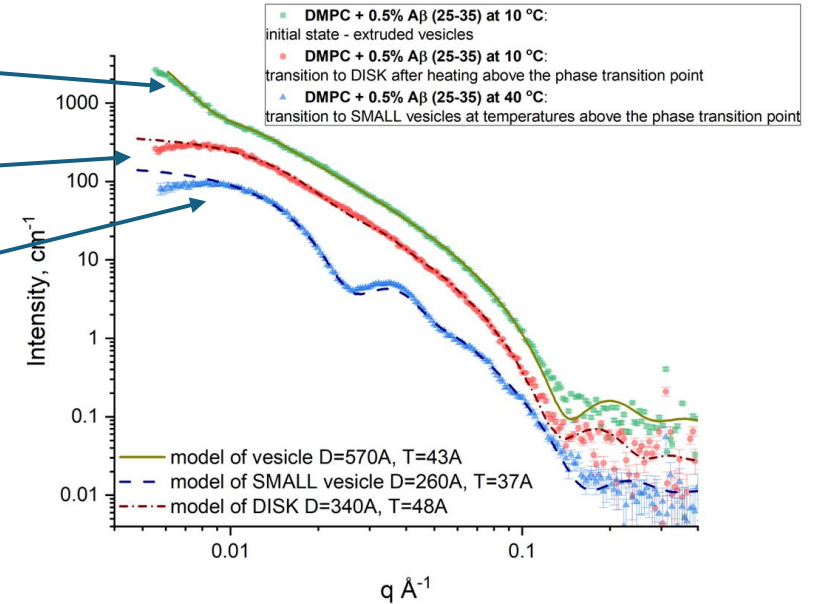


Changes in the membrane self-organization happen during the thermodynamic phase transitions of lipids and are interpreted as the peptide driven membrane breakage.

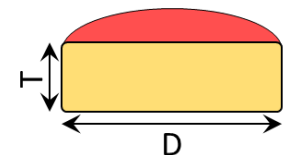
Small Spherical Hollow Shells

Bilayered Disks

Large Spherical Hollow Shells

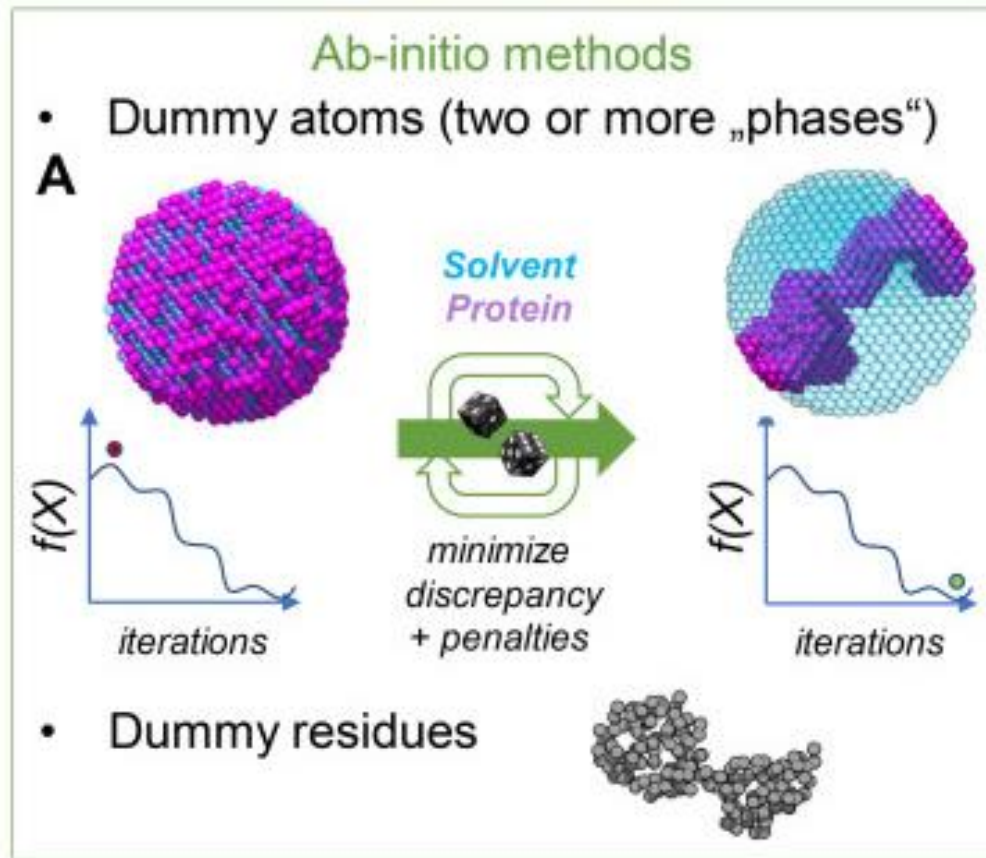


Vesicle  
(Spherical Hollow Shells)



Disk

# Ab initio modelling



## Debye`s formula

$$I(q) = \sum_{i=1}^K \sum_{j=1}^K f_i(q) f_j(q) \frac{\sin(qr_{ij})}{qr_{ij}}$$

K - number of beads,

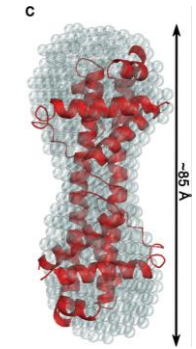
$f_i(q)$ - scattering amplitude from the  $i$ th dummy atom  
 $r_{ij}$  - is the distance between a pair of dummy atoms.

**C** ↓ *Fit quality*

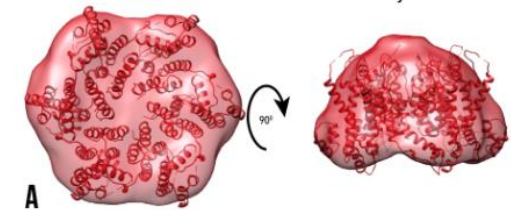
$$\chi^2 = \frac{1}{n-1} \sum_{i=1}^n \left( \frac{l_{exp}(s_i) - l_{calc}(s_i)}{\sigma_i} \right)^2 \text{ and } \chi_{free}^2$$

*Cormap* -  $p$

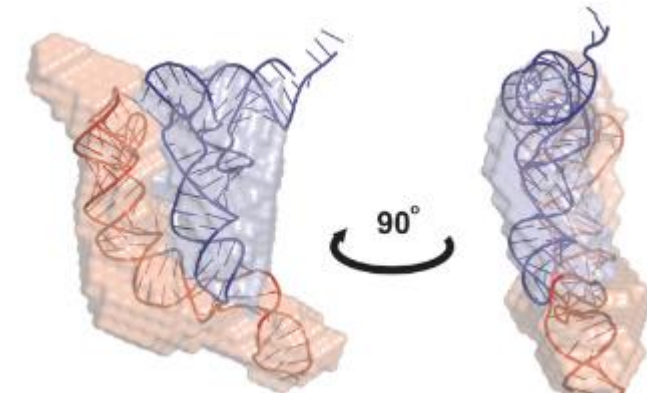
$V_r$



apoptosis-regulating protein



*Ab initio reconstruction of HIV-1 CA hexamer overlaid with PDB ID 3H47<sup>1</sup>*



186-tRNA complex model

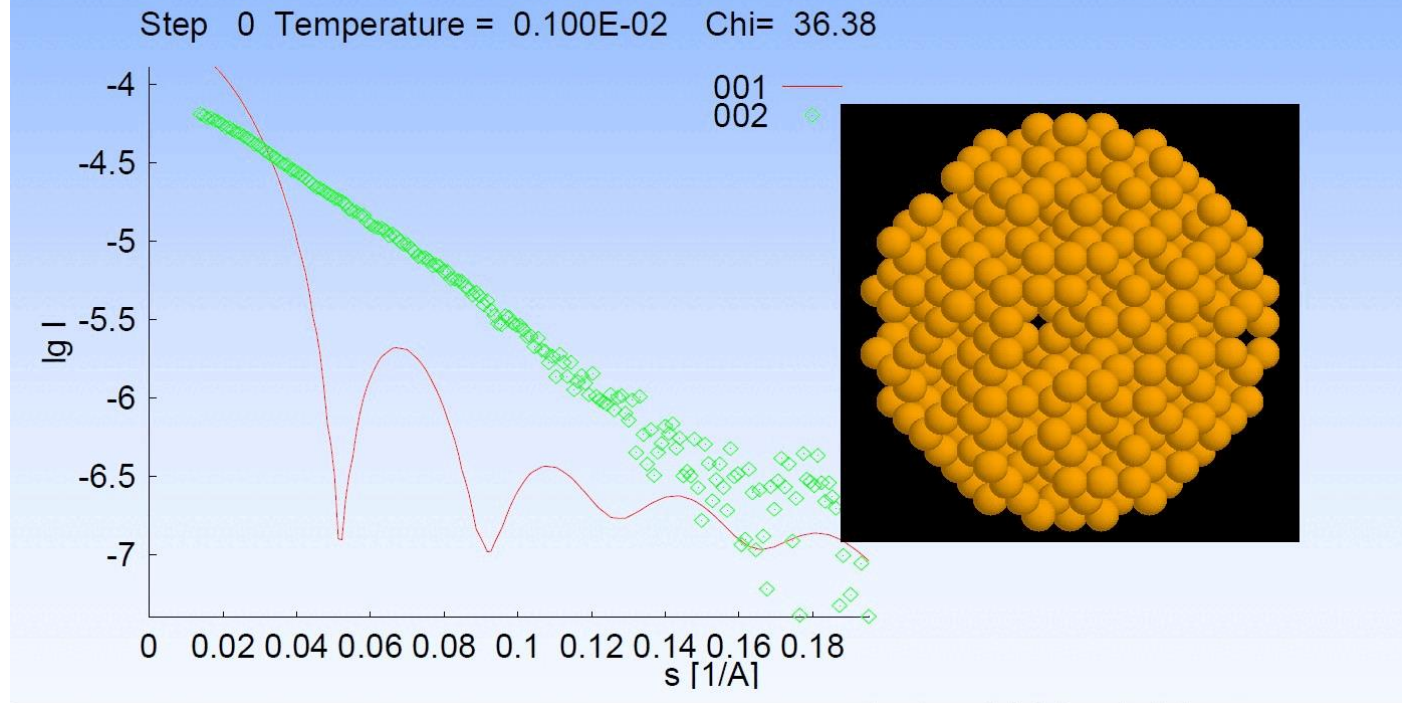
Da Vela S, Svergun DI. Methods, development and applications of small-angle X-ray scattering to characterize biological macromolecules in solution. *Curr Res Struct Biol.* 2020 Aug 27;2:164-170. doi: 10.1016/j.crstbi.2020.08.004.

**Data analysis software ATSAS 3.2.1**

<https://capsidconstructors.github.io/lab-book/saxs.html>  
 S. Rajan et al. *Sci. Rep.* 5, 10609 (2015),

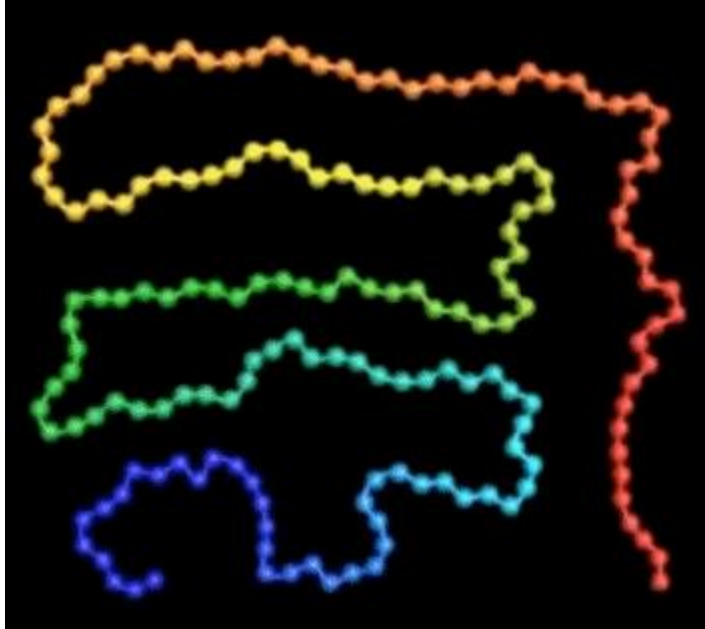
Chen Y, Pollack L. s. *Wiley Interdiscip Rev RNA.* 2016 Jul;7(4):512-526.  
 Fornillos, O., et al. (2009). *Capsid.Cell*, 137(7), pp.1282-1292.

## Case study: determination of structure of the myosin head S1

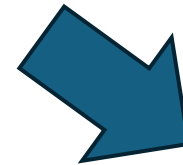


From presentation of V.V. Volkov , FSRC Crystallography & Photonics RAS, Moscow

# Molecular dynamics simulations + SAS



Simulation by Dina Badreeva, JINR



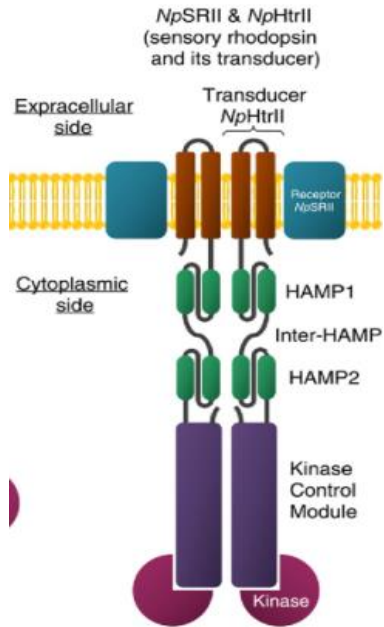
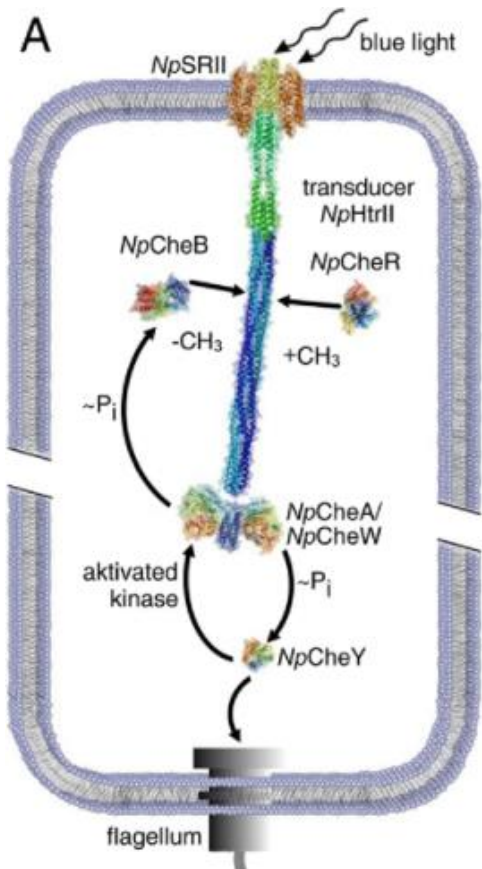
- The trajectories of atoms and molecules are determined by numerically solving Newton's equations of motion for a system
- Calculations use interatomic potentials or molecular mechanical force fields

## Programs for $I(q)$ calculation:

- Data analysis software ATSAS
- FoxS



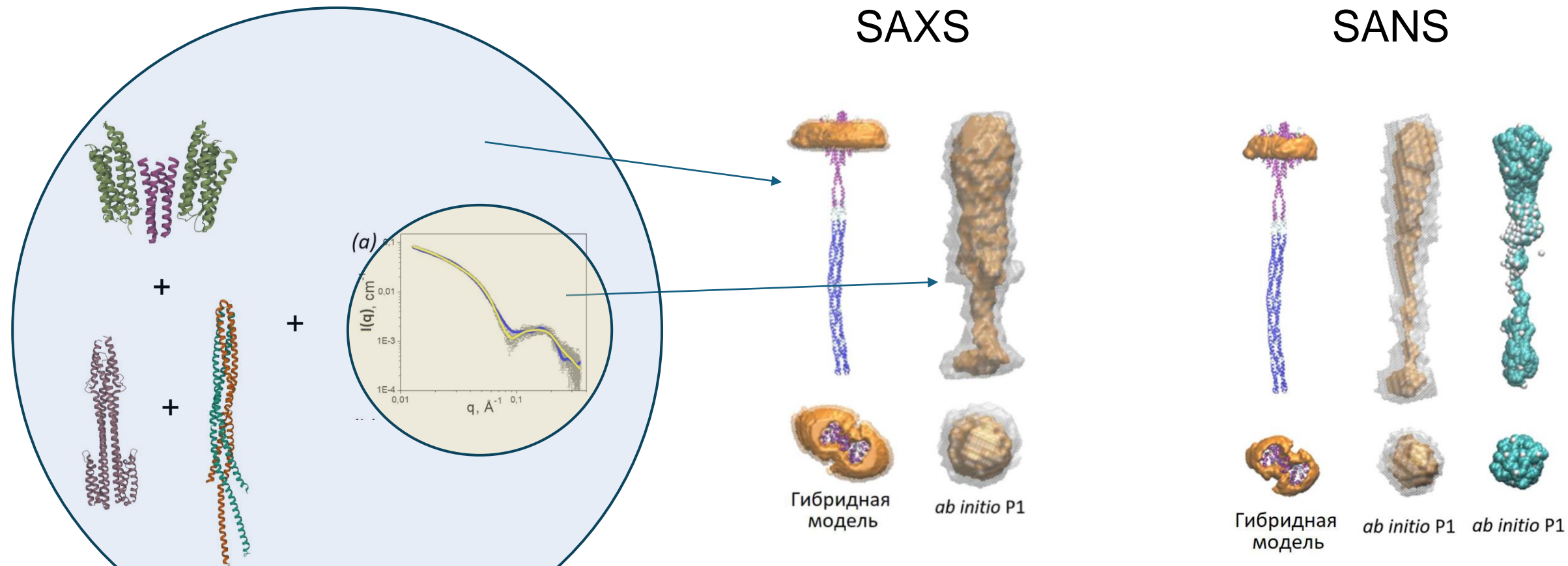
# Molecular model of a sensor of two-component signaling system: photoreceptor from *N. pharaonis*



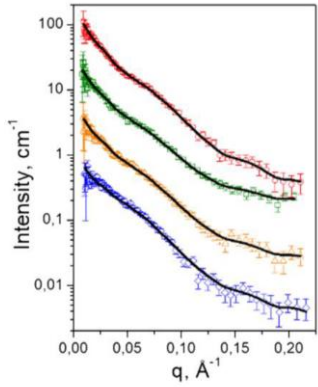
Soda Lake Zug from Wadi Natrun, Sahara Desert, Egypt

Grows optimally in 3.5 M NaCl and at pH 8.5.

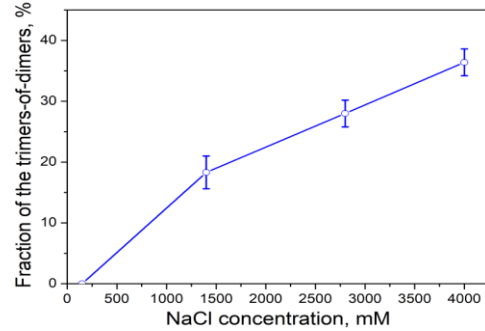
- Signaling system
- Mediate phototaxis
- Extremely haloalkaliphilic archaeon



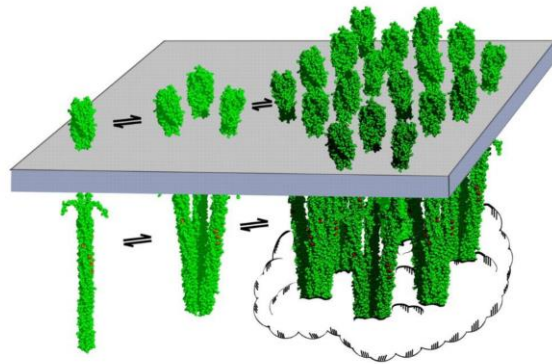
*Ab initio* models of *NpSRII/NpNtrII* complex at low ionic strength 150 mM NaCl  
 ATSAS program; MEMPROT



SANS experimental data obtained with the protein *NpSRII/NpHtrII* complex in  $D_2O$  solutions with 0.15, 1.4, 2.8 and 4.0 M NaCl



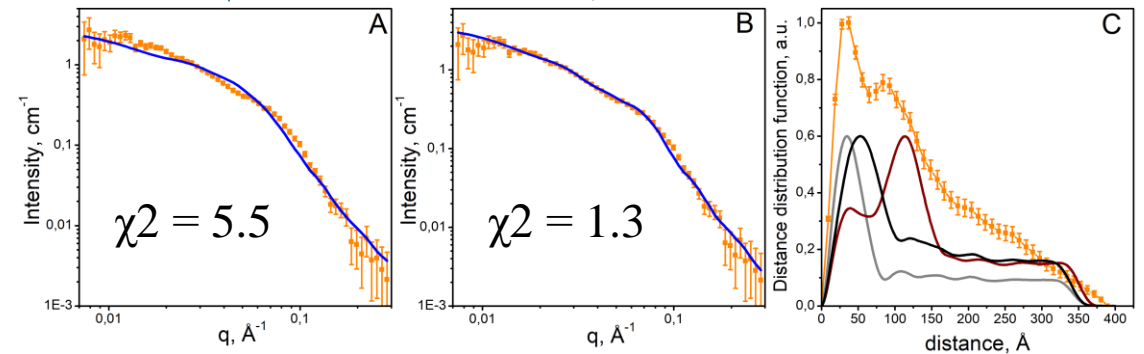
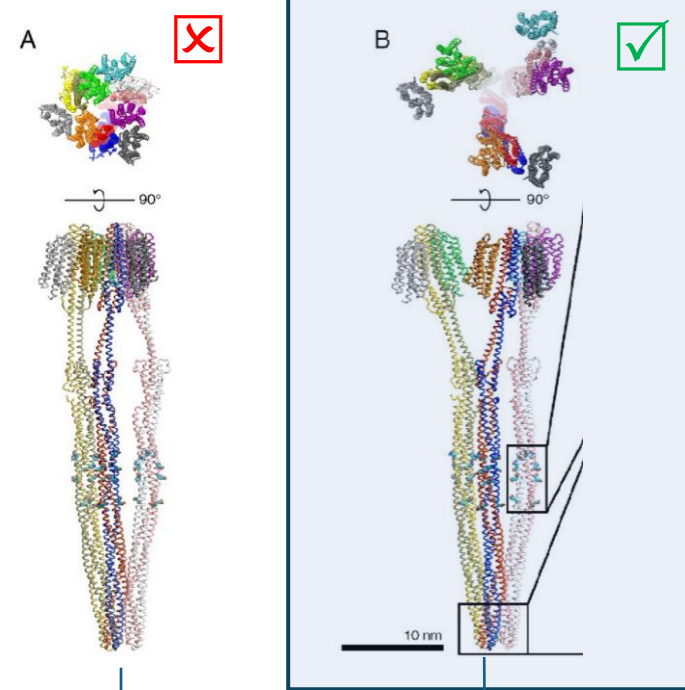
Weight fraction of the trimers of dimers of the full-length *NpSRII/NpHtrII* complex versus NaCl molarity. OLIGOMER program from ATSAS software suite. Fraction of the trimers-of-dimers at 150 mM NaCl assumed to be zero.



Oligomerization of dimers of chemoreceptors

### Transmembrane-bound

### Tripod-shaped



# Contrast variation technique

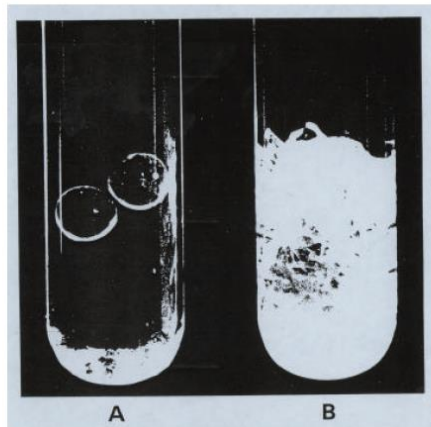
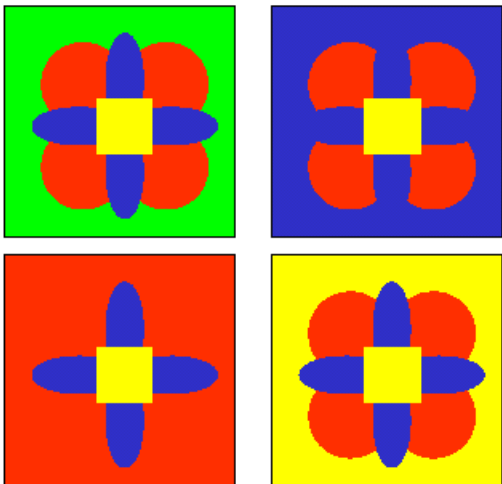
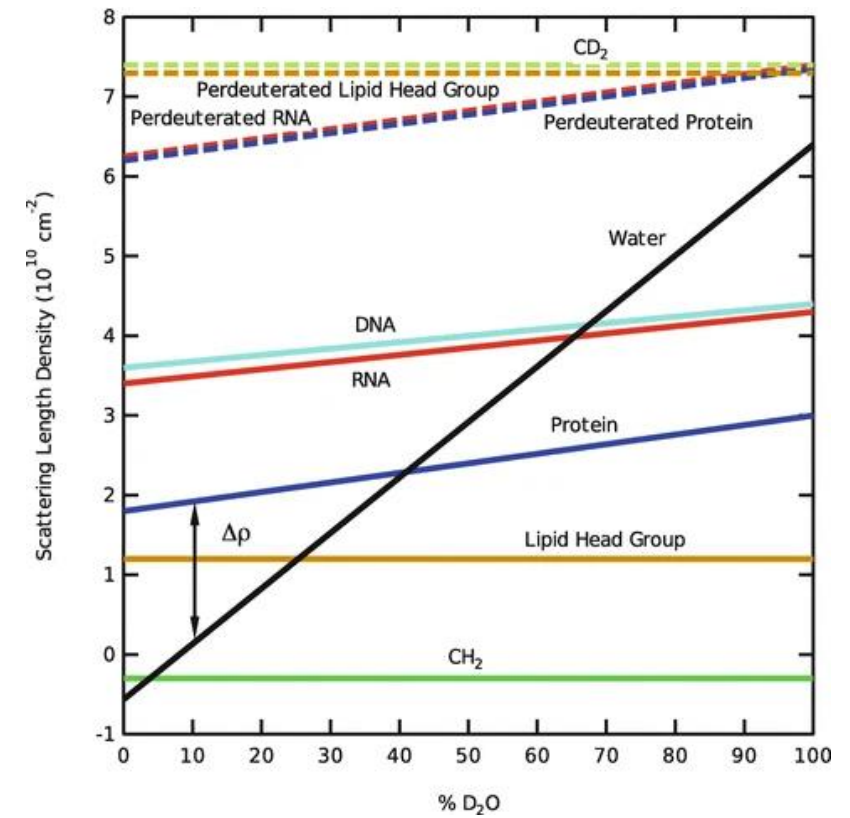
$$I(q) = N(\Delta\rho V)^2 F(q)$$

$$\Delta\rho = (\bar{\rho} - \bar{\rho}_{buffer})$$

$$\rho = \sum_i b/V$$

## Coherent scattering length for x-ray and neutron for main biological elements

Element/isotope	$b_{x\text{-ray}}$ (fm)	$b_{\text{neutron}}$ (fm)
Hydrogen ( $^1\text{H}$ )	2.82	-3.74
Deuterium ( $^2\text{D}$ )	2.82	6.67
Carbon ( $^{12}\text{C}$ )	16.9	6.65
Nitrogen ( $^{14}\text{N}$ )	19.7	9.36
Oxygen ( $^{16}\text{O}$ )	22.5	5.80
Phosphorous ( $^{31}\text{P}$ )	42.3	5.13



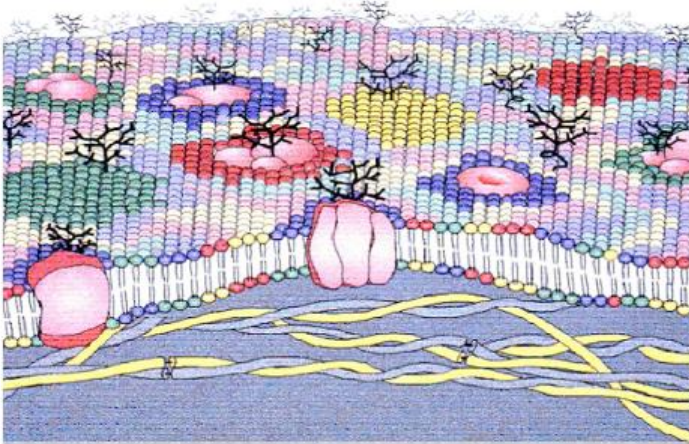
Tubes is borosilicate beads+pyrex fibers+solvent  
 A- refractive index matched to pyrex  
 B - solvent index different from beads and fibers

## X-ray and neutron SLD for typical components of biological samples

Molecule	$\rho_{x\text{-ray}}$ e/Å <sup>3</sup>	$\rho_{\text{neutron}}$ 10 <sup>-6</sup> Å <sup>-2</sup>
H <sub>2</sub> O	0.334	-0.56
D <sub>2</sub> O	0.334	6.4
Protein	0.42	2.1
D-protein	0.42	6.6
Nucleic acid	0.55	3.7
D-Nucleic acid	0.55	6.6
Phospholipid	0.3	0.3
Phospholipid head (PC)		1.8
Phospholipid d-head (d-PC)		5.7
Phospholipid chain		-0.3
Phospholipid d-chain		7.0
Head phosphatidylglycerol (PG)		2.47
Head phosphatidylethanolamine (PE)		2.55
Hydrophobic region of DDM	0.275	-0.4
Hydrophilic region DDM group of DDM	0.515	3.9

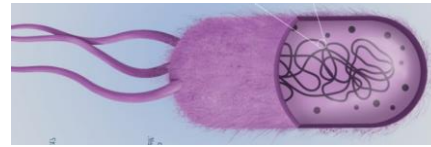
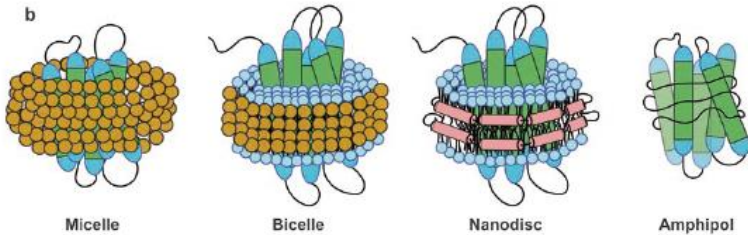


# Objects for contrast variation technique

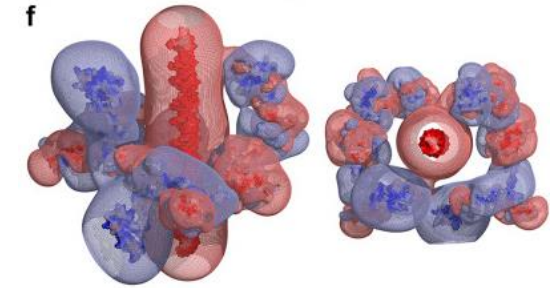


Biological membranes

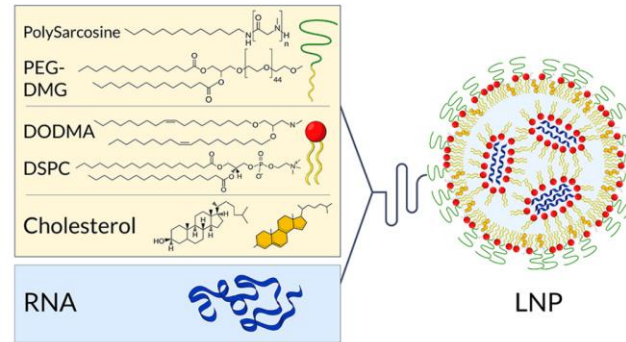
Escribá et al., JCM (2008)



bacteria



DNA+protein complex

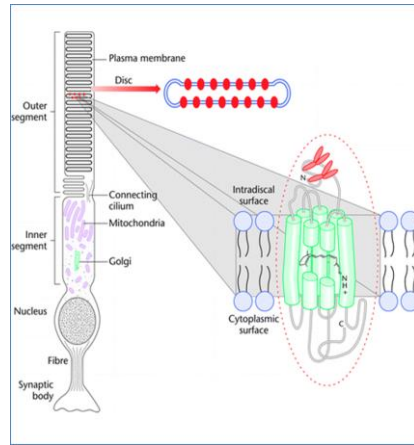
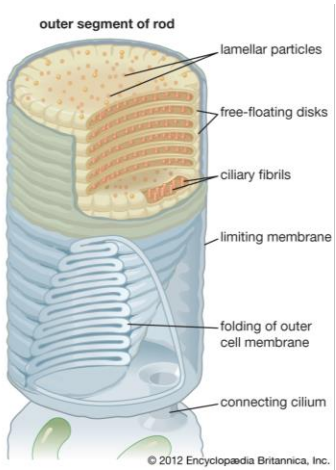


vaccine

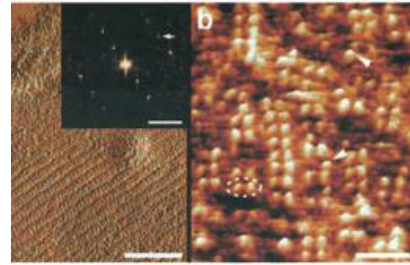


Cellular organelles

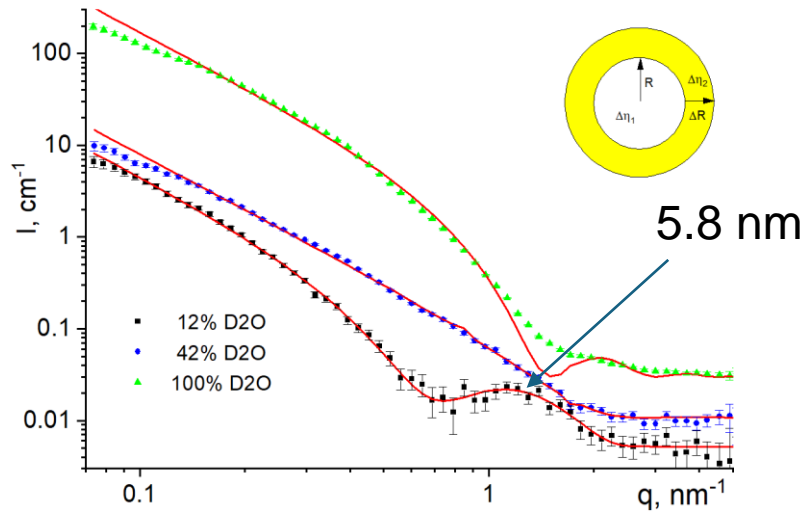
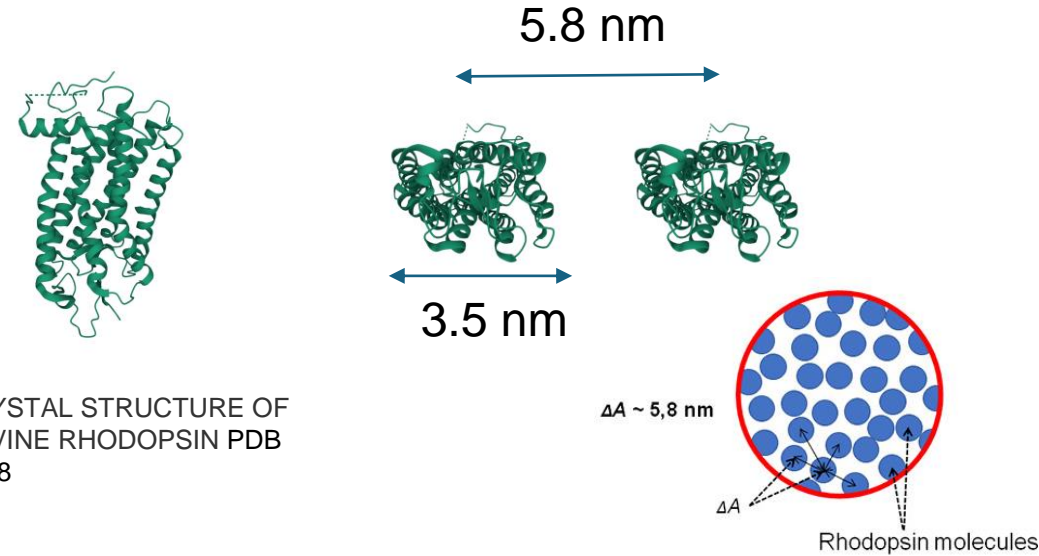
# Supramolecular organization of the visual pigment rhodopsin



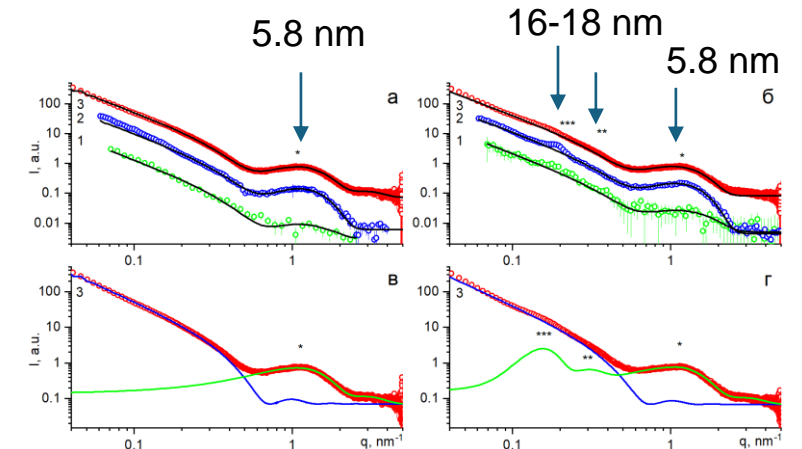
AFM of outer shape of disc with the rhodopsin protein from rod cell



Distance between rhodopsin centers 38 Å.  
Rhodopsin molecule size is 35 Å.



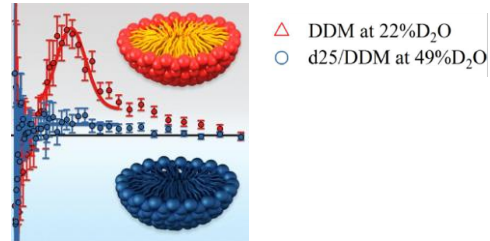
Photoreceptor disk Rot outer segment



# Membrane proteins: How to deal with the detergent belt - Masking out

1. Mix D2O / H2O in a buffer

2. Mix of h-detergent / d-detergent  
+ deuterated proteins



R. C. Oliver et. al. // *The Journal of Physical Chemistry Letters* **2017** 8 (20), 5041-5046

3. The synthesis of isotope-substituted detergents to have match-out at 100% D2O

**Table 1.** Deuteration levels needed and obtained for *n*-octyl  $\beta$ -D-glucopyranoside (OG) and *n*-dodecyl- $\beta$ -D-maltopyranoside (DDM).

	OG		DDM	
	Head group	Tail group	Head group	Tail group
Chemical composition of the detergent component	C <sub>2</sub> H <sub>11</sub> O <sub>6</sub>	C <sub>8</sub> H <sub>17</sub>	C <sub>12</sub> H <sub>21</sub> O <sub>11</sub>	C <sub>12</sub> H <sub>25</sub>
Exchangeable hydrogens	4	0	7	0
Theoretical level of deuteration needed for match-out at 100% D <sub>2</sub> O	C <sub>6</sub> D <sub>7.6</sub> H <sub>3.4</sub> O <sub>6</sub>	C <sub>8</sub> D <sub>15.9</sub> H <sub>1.1</sub>	C <sub>12</sub> D <sub>15.2</sub> H <sub>5.8</sub> O <sub>11</sub>	C <sub>12</sub> D <sub>22.4</sub> H <sub>2.6</sub>
Experimentally obtained level of deuteration in 100% D <sub>2</sub> O	C <sub>6</sub> D <sub>7.64</sub> H <sub>3.36</sub> O <sub>6</sub>	C <sub>8</sub> D <sub>15.98</sub> H <sub>1.12</sub>	C <sub>12</sub> D <sub>14.98</sub> H <sub>6.02</sub> O <sub>11</sub>	C <sub>12</sub> D <sub>22.25</sub> H <sub>2.75</sub>

Midtgaard, S.R., et al. // (2018), *FEBS J*, 285: 357-371

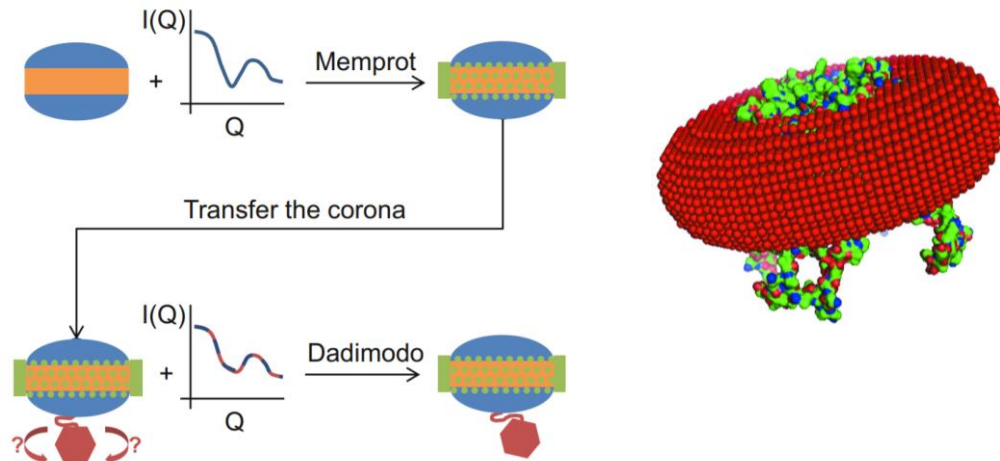
4. Production of lipids and scaffold proteins in a host organism in D2O-media to have match-out at 100% D2O

**Difficulties:**

- Limited availability of d-detergents
- Difficulties in the expression and purification of d-proteins
- High cost

# How to deal with the detergent belt: Hybrid approach

PDB protein-structure + coarse-grained detergent belt structure



Geometrical representation nano-disc  
+ coarse-grained protein shape



Top and side view of one particular result of an *ab initio* analysis of the scattering data. The phospholipid head and tail groups of the nanodisc are represented by the blue and yellow discs, respectively. The belt protein is not shown.

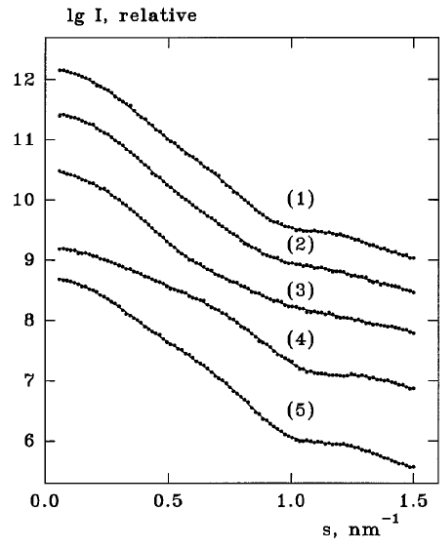
Baranowski M., Pérez J. (2020) In: Biophysics of Membrane Proteins. Methods in Molecular Biology, vol 2168. Humana, New York, NY.

Pérez J, Koutsioubas A. Memprot: a program to model the detergent corona around a membrane protein based on SEC-SAXS data. *Acta Crystallogr D Biol Crystallogr.* (2015) 1;71(Pt 1):86-93.

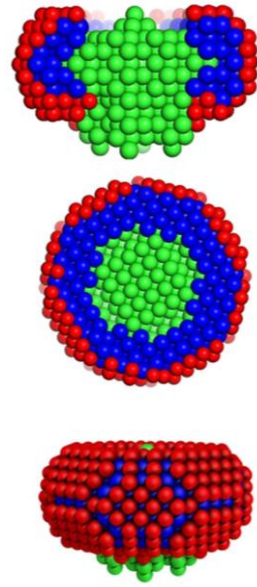
Skar-Gislinge N, Kynde SA, Denisov IG, et al. *Acta Crystallogr D Biol Crystallogr.* 2015;71(Pt 12):2412-2421. doi:10.1107/S1399004715018702



# Ab initio models from contrast variation



% of D2O



MONSA (multi-phase *ab initio*, the model was built from precalculated searching volume; fourfold symmetry around z-axis is imposed)

MD structure



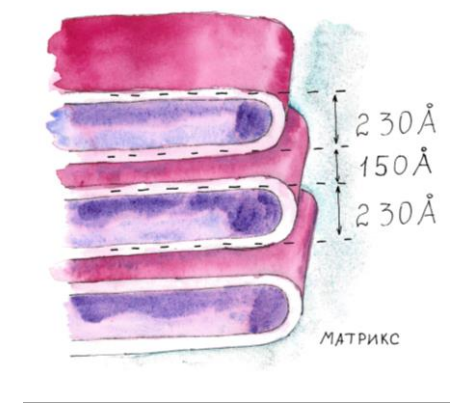
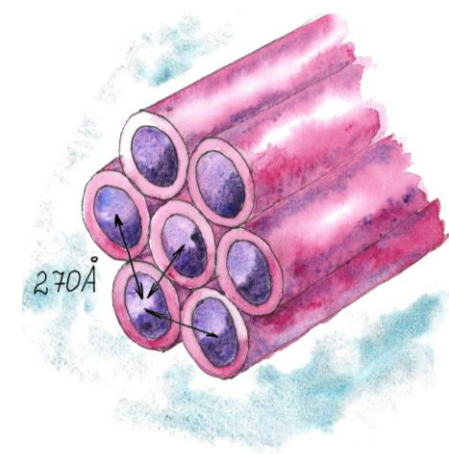
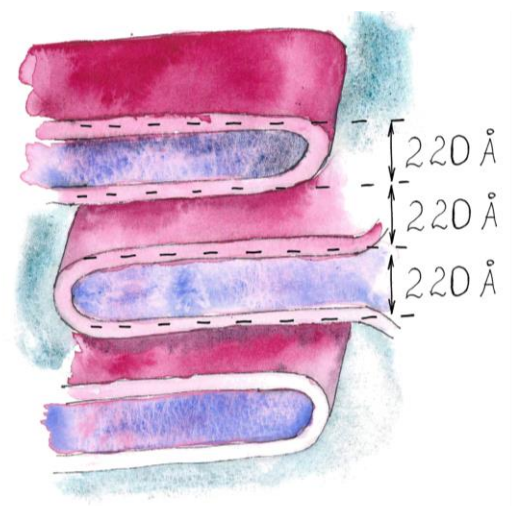
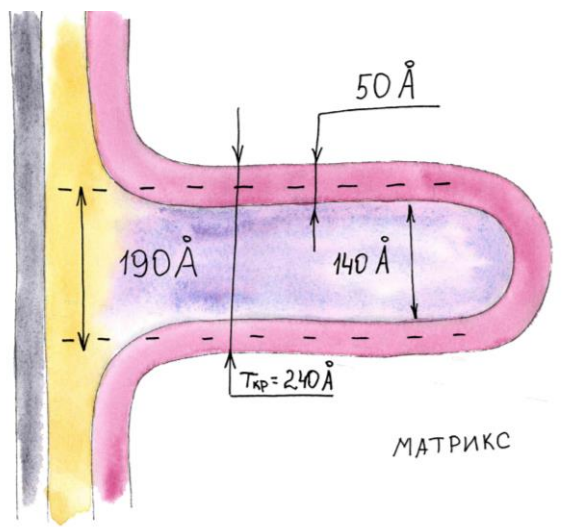
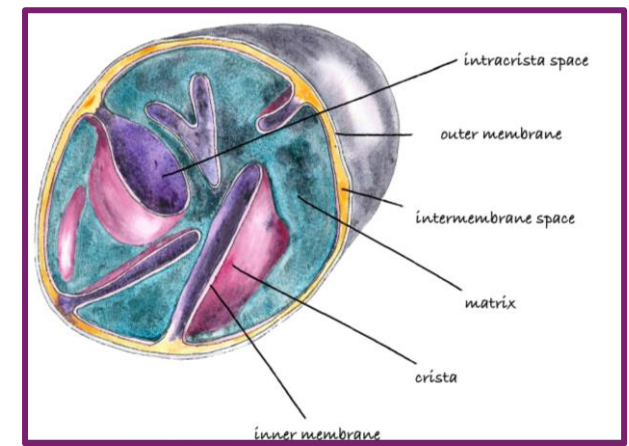
SANS curves with imposed fourfold axial symmetry



Ab initio shape reconstructions of the 270 dDM/AQ0 tetramer. The bead colors correspond to *green*, protein; *cyan*, detergent hydrophilic heads; and *magenta*, detergent hydrophobic tails.



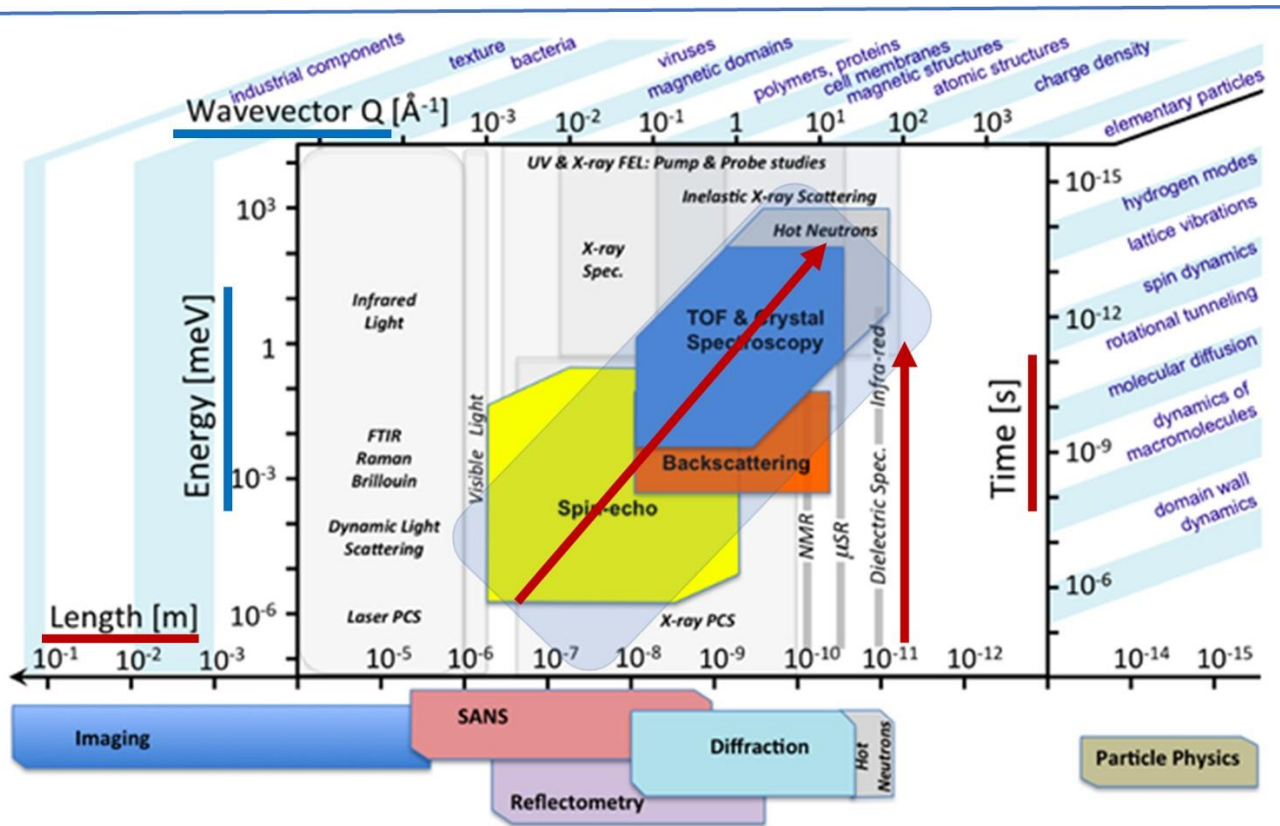
# Study of the structure of live functioning mitochondria (SANS experiments)



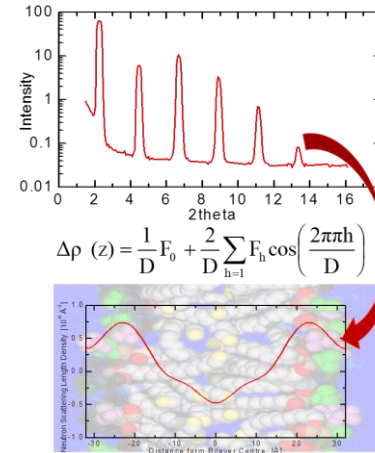
Structure of a liver mitochondrial crista under conditions of matrix swelling (hypotonic conditions), and heart mitochondrial cristae in normal (isotonic) conditions

Structure of rat heart mitochondrial cristae in hypotonic conditions.

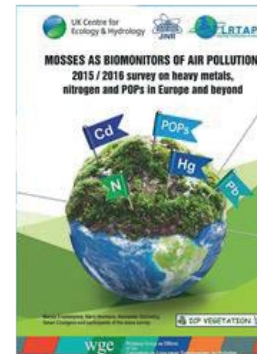
# Other scattering methods



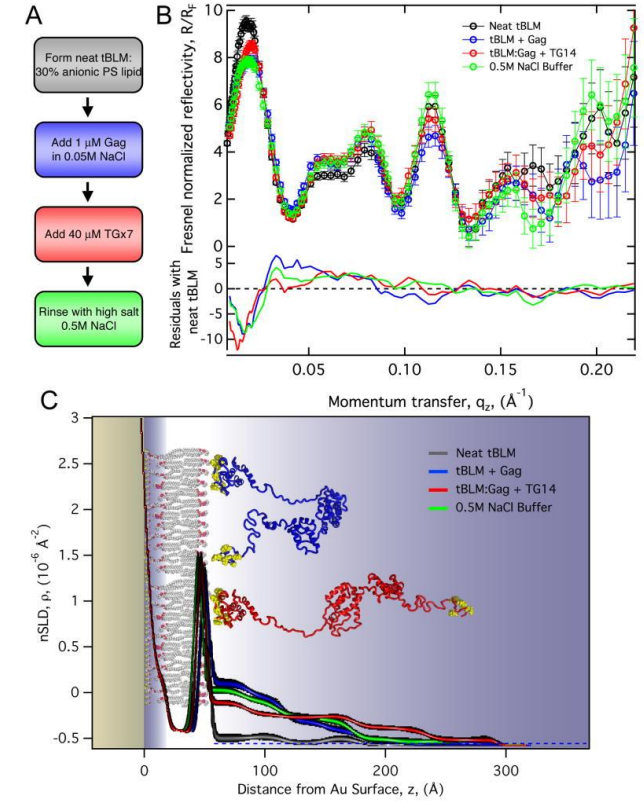
spectroscopy



Diffraction



Neutron activation analysis



Reflectometry

Datta SA, et al. HIV-1 Gag extension: conformational changes require simultaneous interaction with membrane and nucleic acid. *J Mol Biol.* 2011 Feb 18;406(2):205-14.

# Thank you for your attention!

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