

**MaGiC: Matter And Gravitation In Collisions
of
Relativistic Heavy Ions and GR Neutron Star Mergers**

Probe the EoS of hot, dense matter by Flow + Gravitational Waves

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Matthias Hanauske, Elias Most, Jens Papenfort, Luciano Rezzolla, Horst Stöcker *

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Institut für Theoretische Physik, Johann Wolfgang Goethe Universität Frankfurt

GSI Helmholtzzentrum für Schwerionenforschung GmbH Darmstadt

***Walter Greiner Gesellschaft zur Förderung der physikalischen Grundlagenforschung e.V., Frankfurt**

Matter and Gravity

1679 **I. Newton** published his theory of gravitation. According to Newton, gravity manifests itself as an instantaneous **force between masses** proportional to their masses and inversely proportional distance squared. With this theory he could explain all of the astronomical observations of this time.



1915 **A. Einstein**, born in Ulm, published GR: Gravity governs the motion of masses and light by curving spacetime.

1915 **Karl Schwarzschild**, born 1873 in Frankfurt am Main, found the static solution of GR - died in WW I just after publishing his article.

Consequences of Schwarzschild's vision: **black holes, neutron stars**

Add Einstein's Gravitational Waves + we see a **whole new Universe**

Einstein equations - first solved by Karl Schwarzschild

Einstein tensor

stress-energy tensor

$$G_{\mu\nu} = 8\pi T_{\mu\nu}$$

spacetime
curvature

mass and energy
in the spacetime

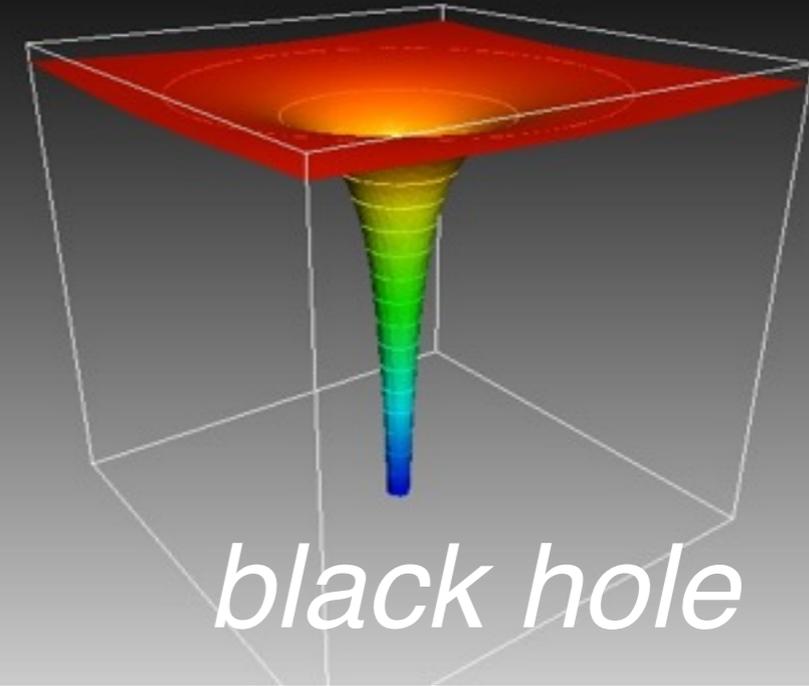
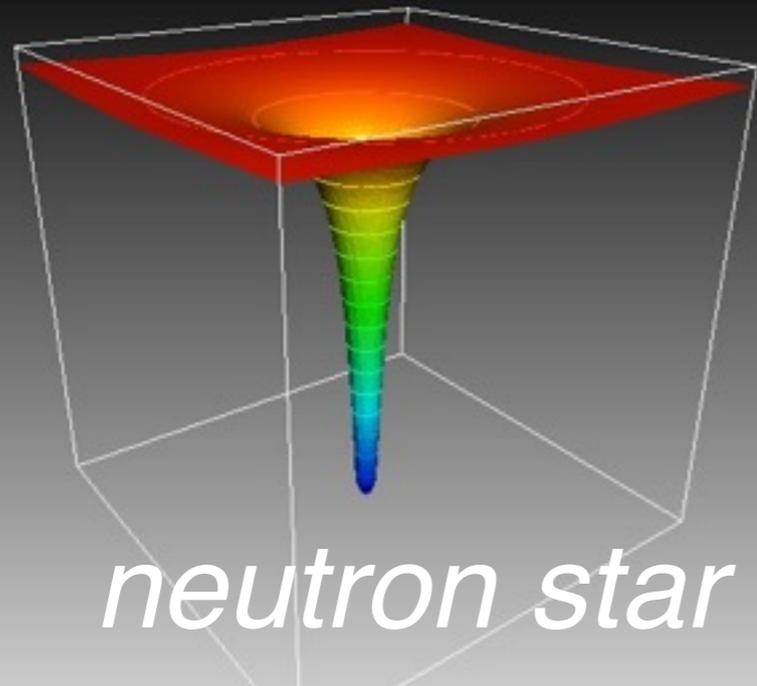


The importance of Einstein equations lies in setting a relation between the **curvature** and the **mass/energy**:

gravity becomes the manifestation of spacetime curvature

Neutron Star - or Schwarzschild's Black Hole ?

Narrow transition from a very compact star to a black hole
- many of the spacetime properties are similar.



Two aspects differ: Neutron Stars have a **hard surface**,
the curvature is large - but **finite** ;

Black Hole: **No Surface** - curvature is **infinite** at the centre
- but there is a SINGULARITY : NEVER divide by zero !

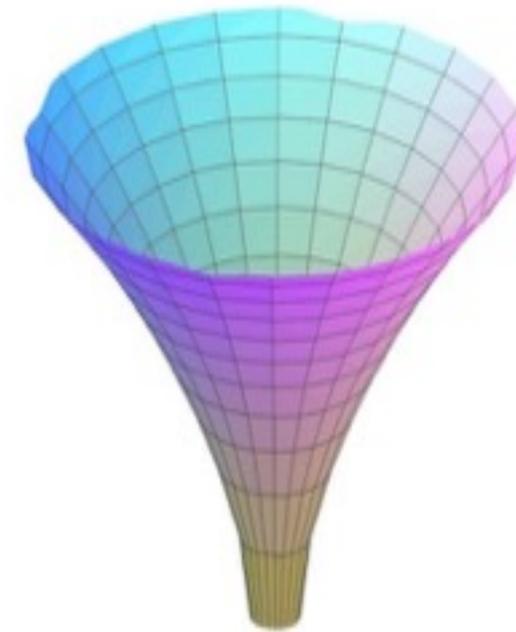
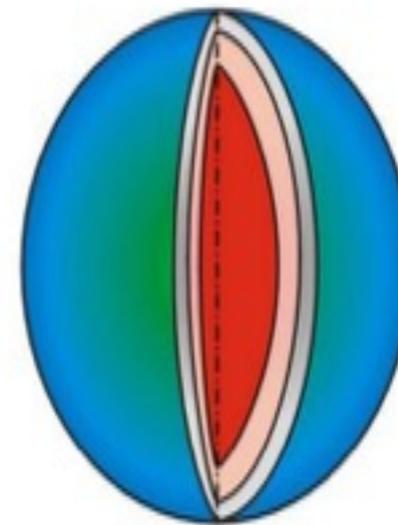
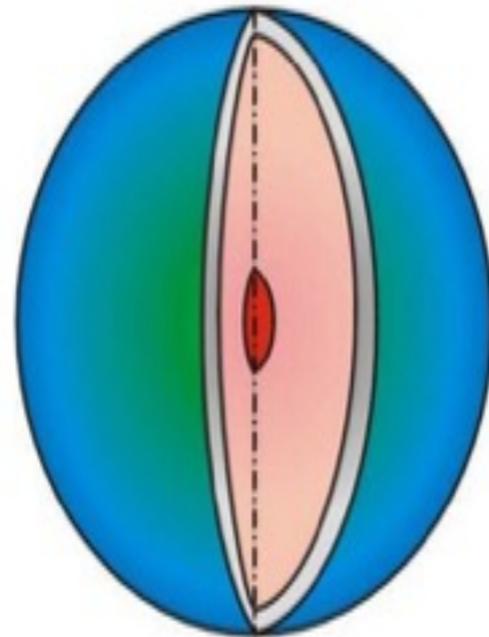
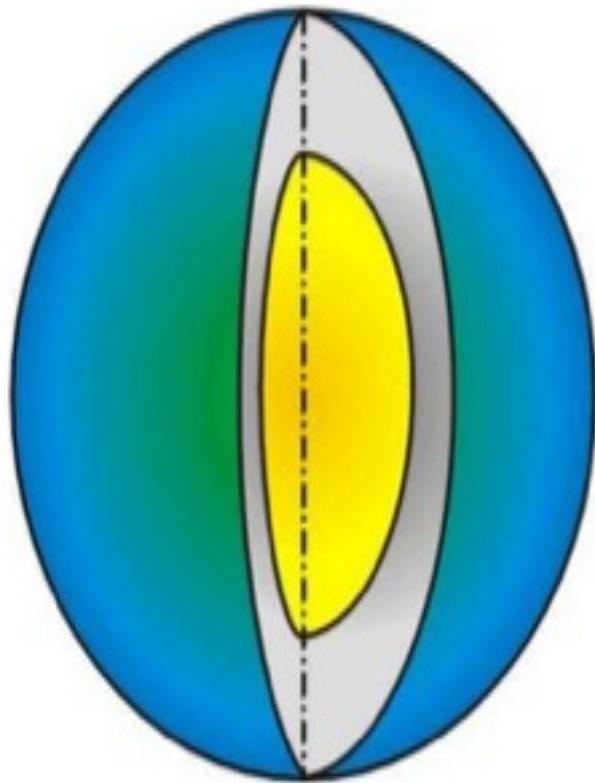
Neutronstars, Quarkstars, Black holes

Neutron Stars

Hybrid Stars

Quark Stars

Black Holes



$$\rho_c = \rho_0$$

$$\approx 2\rho_0$$

$$\approx 5\rho_0$$

... ∞

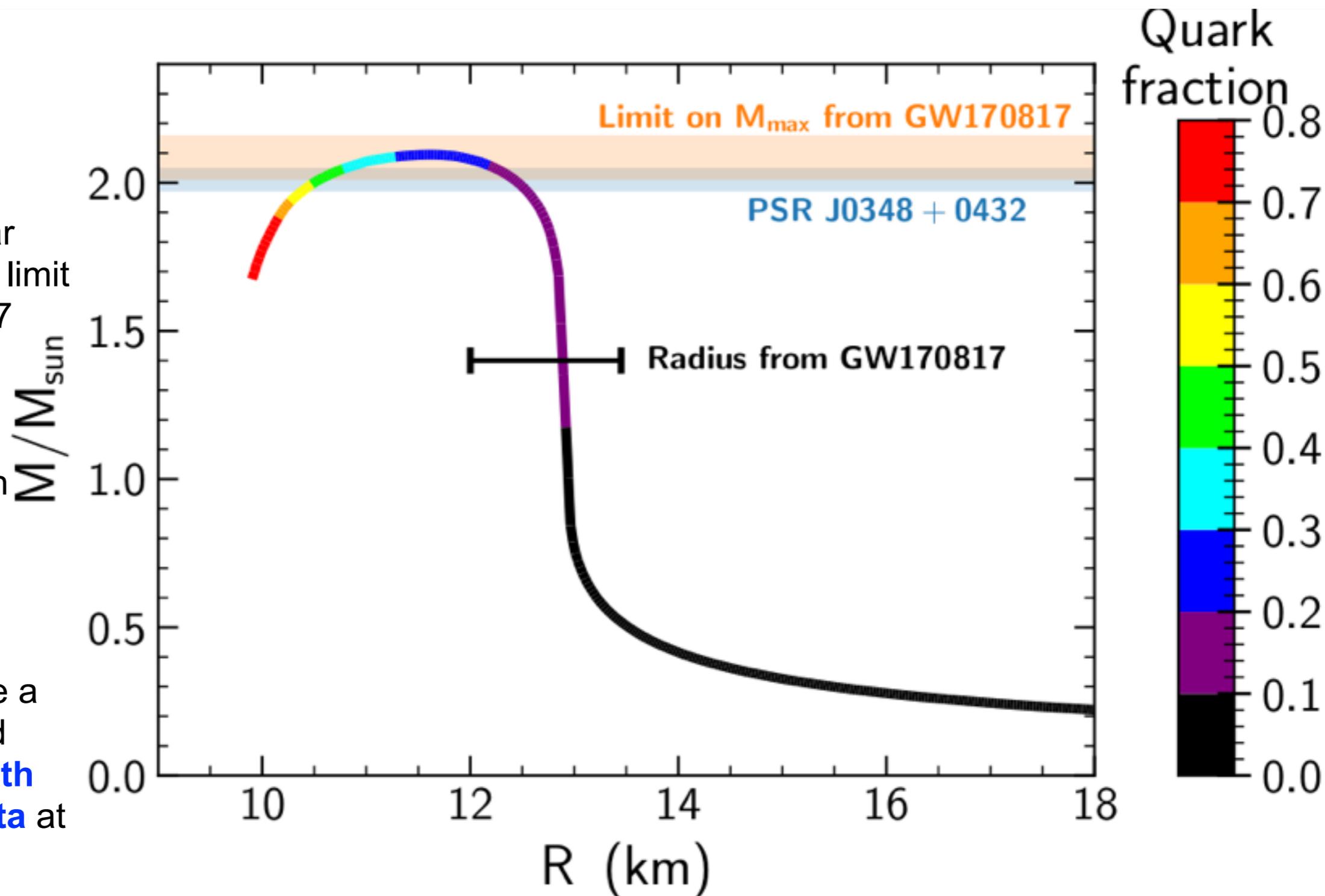
Central density ρ_c in the star

$$(\rho_0 := 0.15/\text{fm}^3)$$

Neutron Star Masses and Radius - Chiral quark-hadron MF EoS

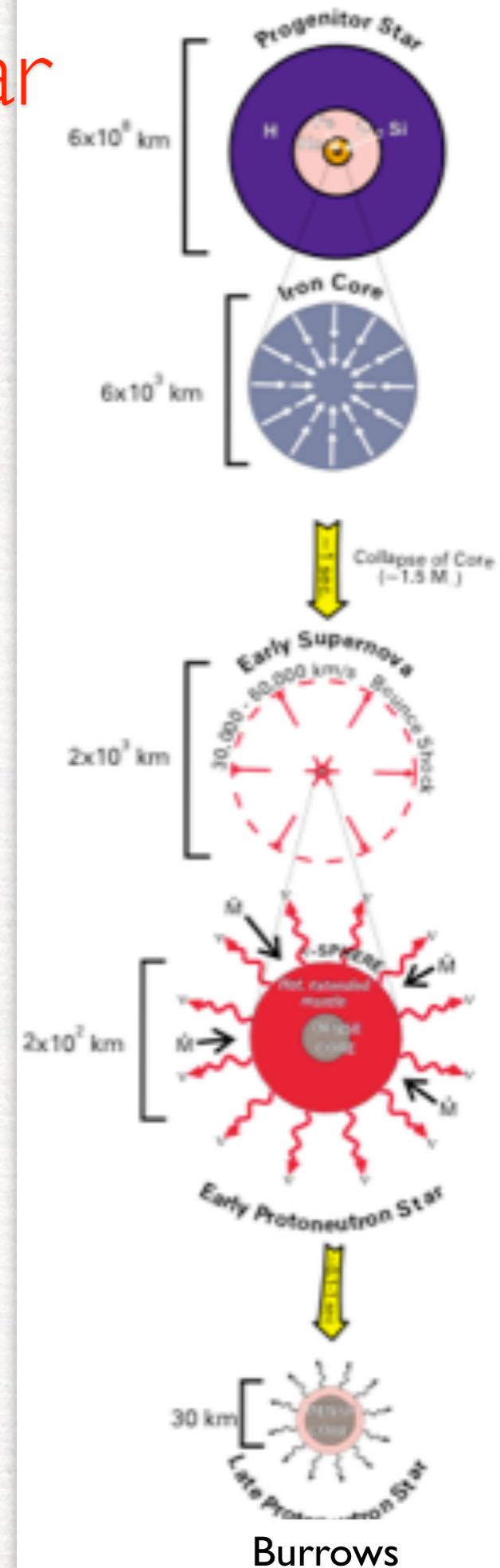
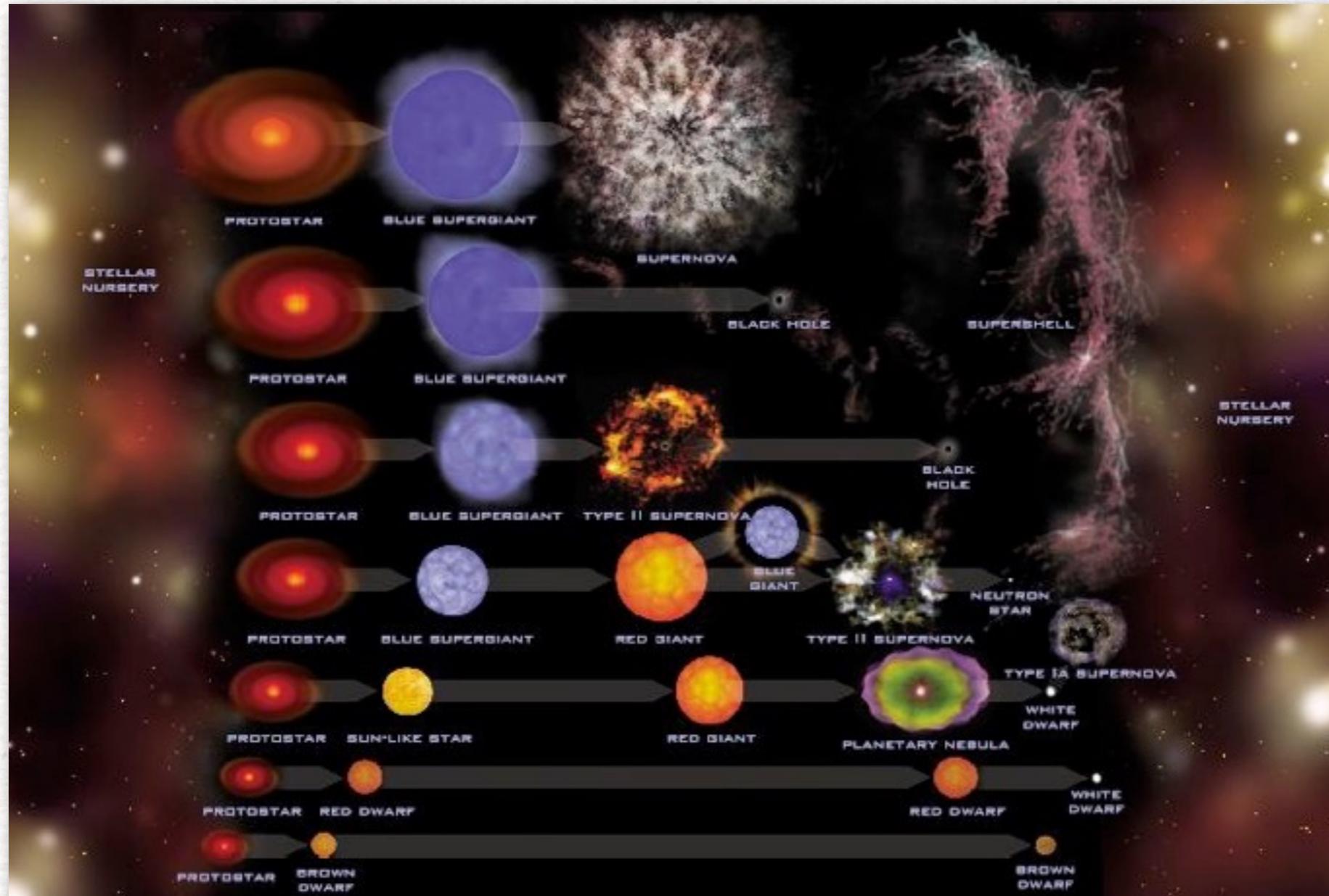
Features:

- Maximum mass agrees with observed 2 solar mass stars **and** limit from GW170817
- Radii are small ($\sim 13\text{km}$) in accordance with various experimental findings
- For the first time a model for hybrid stars **agrees with lattice QCD data** at low μ_B



A. **Motornenko**, Vovchenko, Steinheimer, Schramm, Stoecker 1809.02000

Death of a Star - Birth of a Neutron Star



Neutron Stars are most commonly born in the violent death of massive Stars, i.e. Stars with

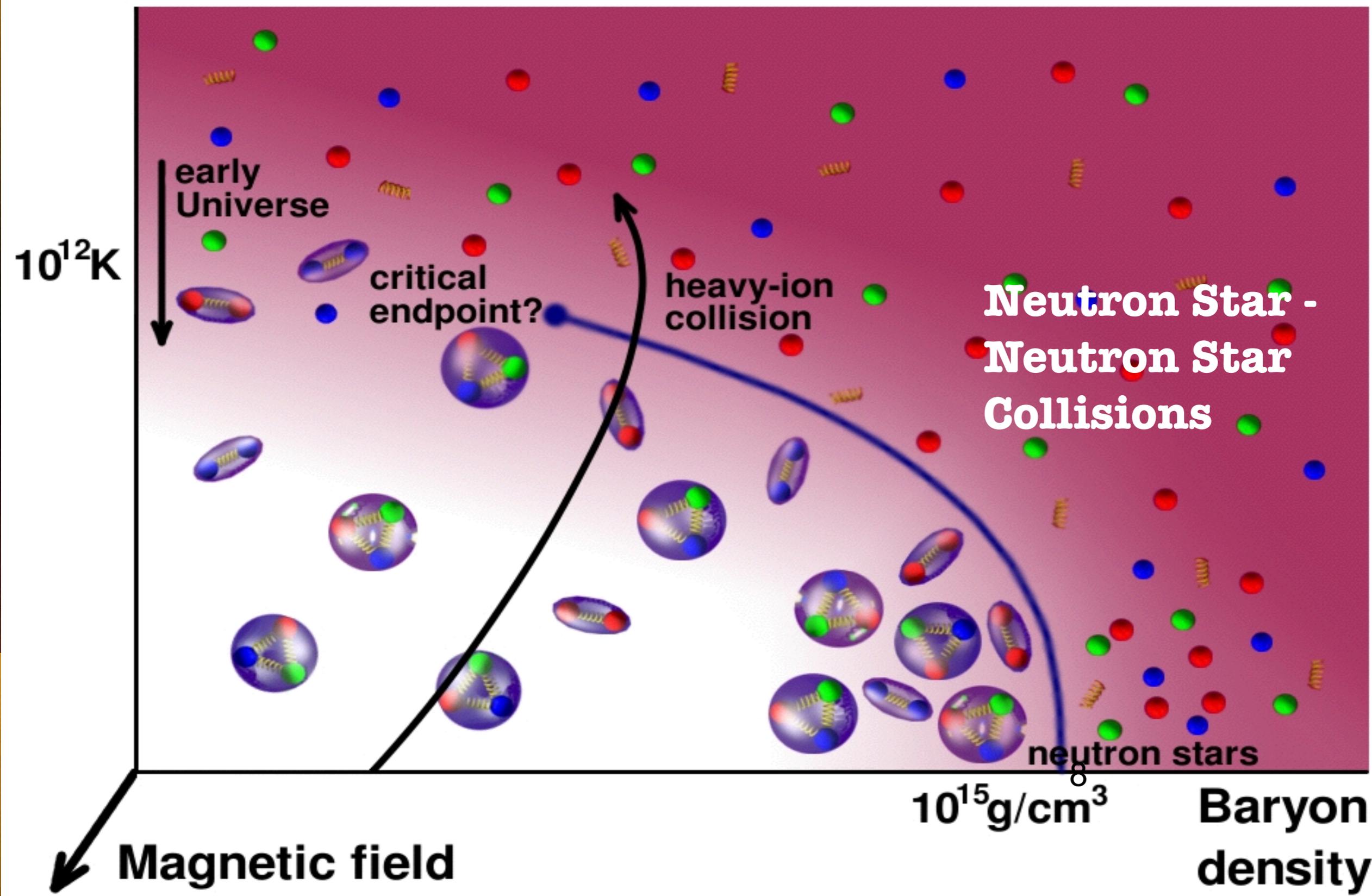
$$10M_{\odot} \lesssim M \lesssim 100M_{\odot}$$

ending their evolution as a **supernova collapse**

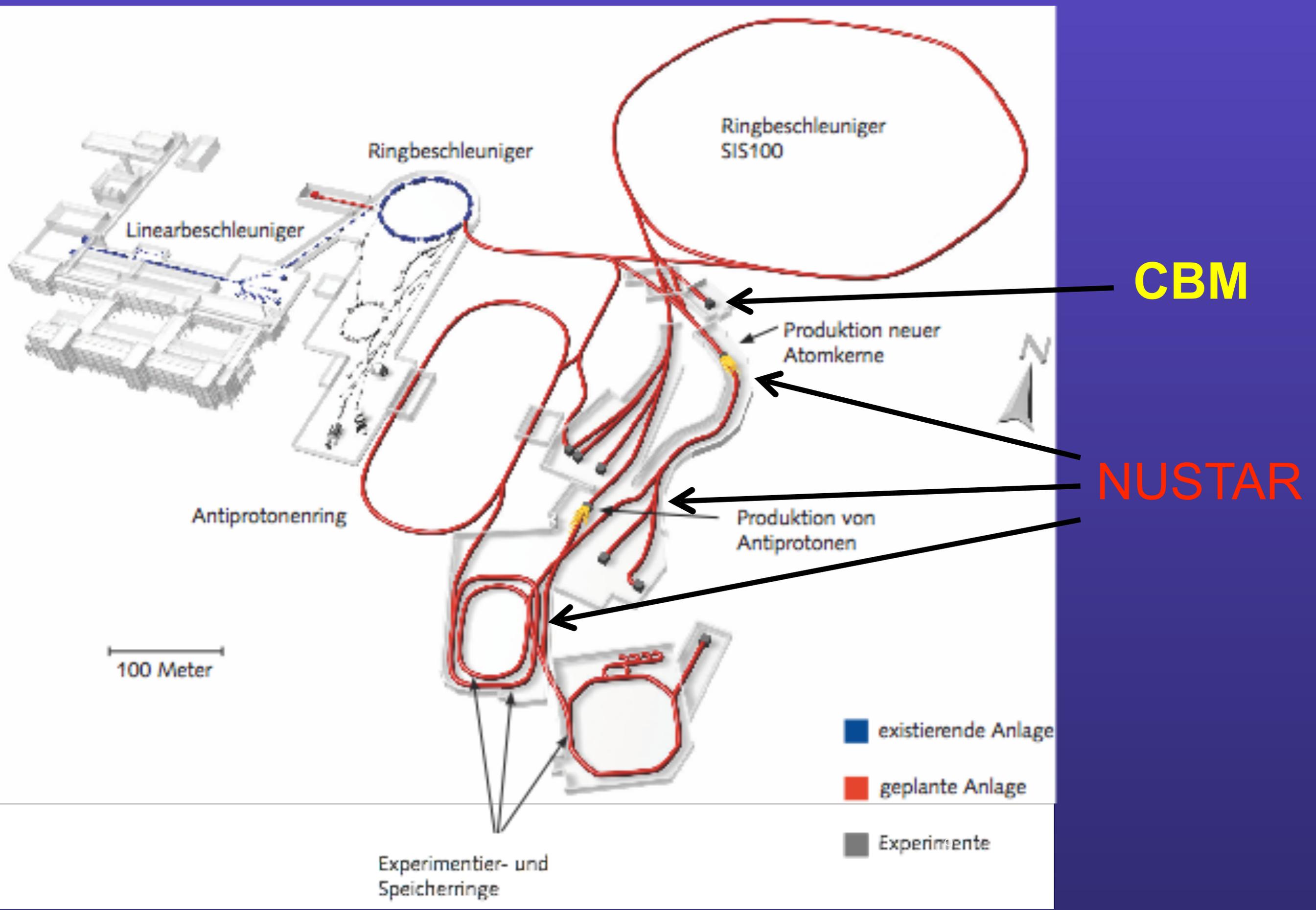
FAIR: Dense Matter, Strange Matter, Quark Matter, Quark Stars?

Relativistic collisions of NS-NS vs. Heavy Ions

Temperature



Neutron Star matter in CBM @FAiR-GSI Helmholtzcentre





FAIR - the Death Star machine! (The Times of India)

FAIR and NICA ideally equipped for precision studies
to compare relativistic collisions between
neutron stars and **heavy ions**

- **consistent theoretical treatment necessary:**

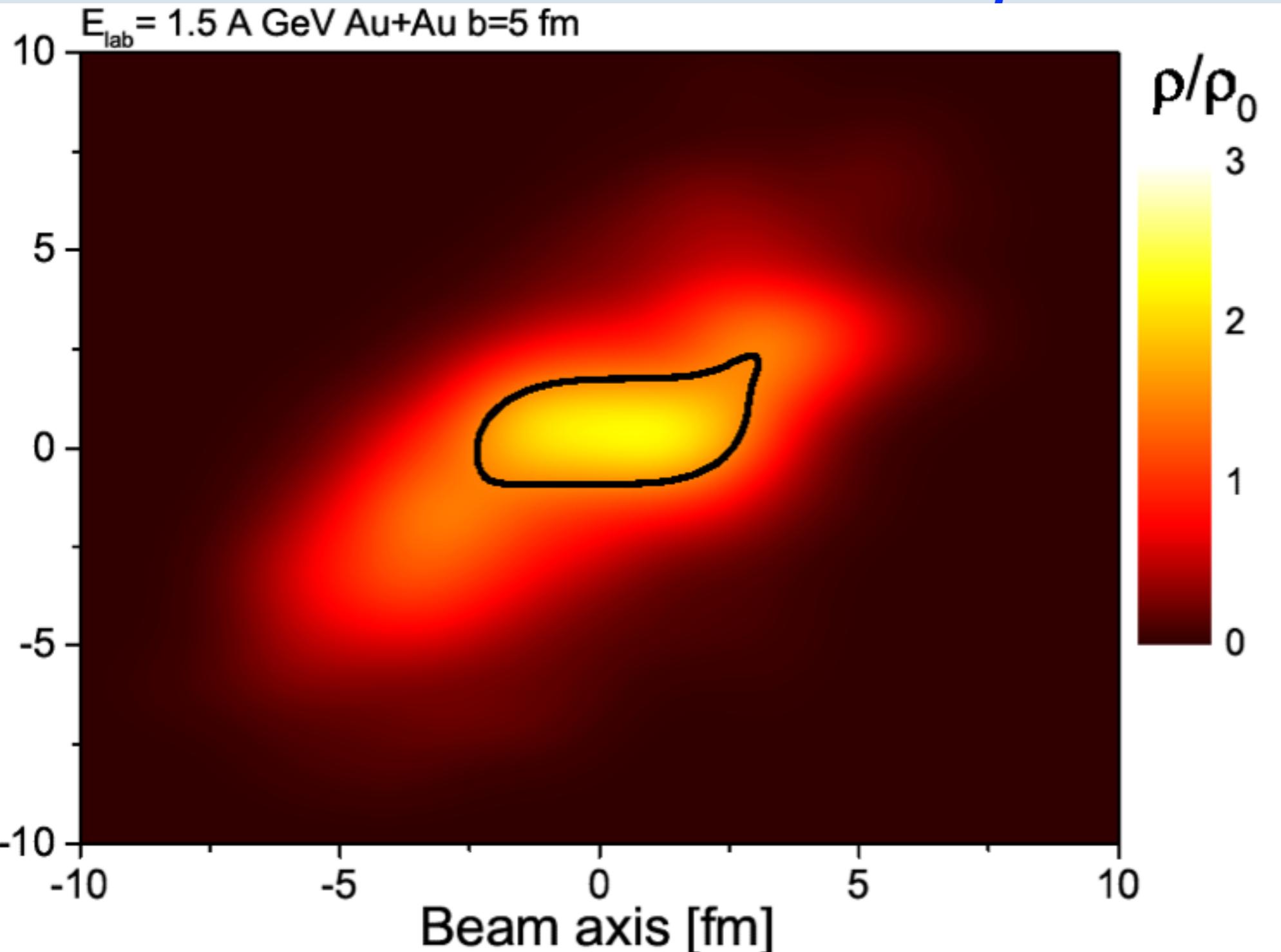
Relativistic EoS Equation of State of dense QCD Matter
input into

General **Relativistic** 3+1 Dim **Hydro**dynamical Transport

- **Predict and compare to observational data -**

Neutronstar merger vs. heavy ion collisions

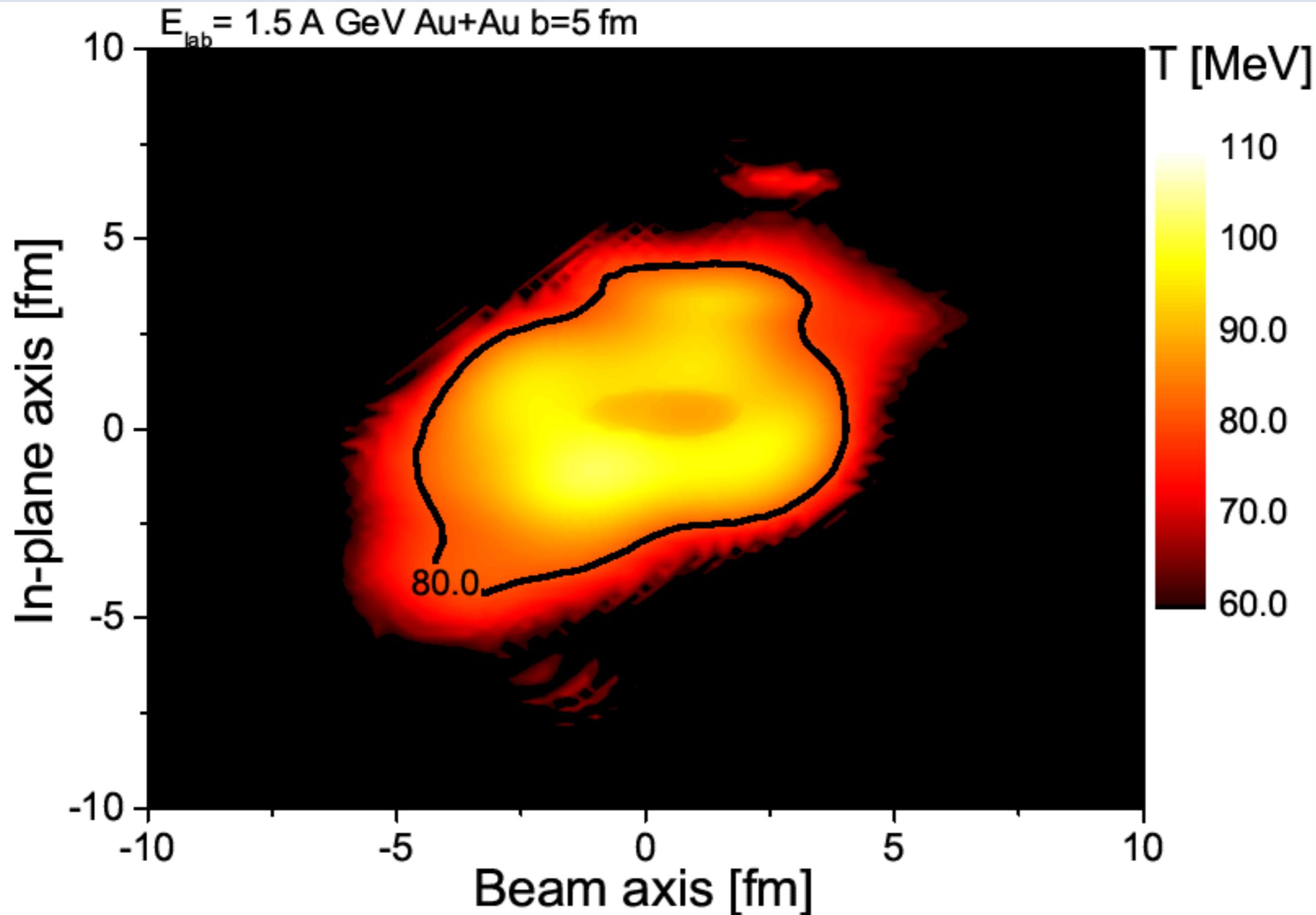
Which densities are expected ?



- Beam energy corresponds to GSI-SIS18.
- 3-5 times nuclear ground state density reached.
- Large inhomogeneity.
- Short lifetime $\sim 20 \text{ fm}/c$
- Small system size $\sim 10 \text{ fm}$

Neutronstar merger vs. heavy ion collisions

Which *temperatures* are expected?



Steinheimer et.al: Coarse-grained UrQMD-simulation input for hydrogen. evolution

- Beam energy corresponds to GSI-SIS18.
- Temperatures** up to $T=90 \text{ MeV}$ reached.
- Large inhomogeneity.
- Short lifetime $\sim 20 \text{ fm/c}$
- Small system size $\sim 10 \text{ fm}$

Numerical Relativity: probing the extreme with relativistic EoS and relativistic Hydro

$$R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R = 8\pi T_{\mu\nu} \quad (\text{field eqs : } 6 + 6 + 3 + 1)$$

$$\nabla_{\mu}T^{\mu\nu} = 0, \quad (\text{cons. en./mom. : } 3 + 1)$$

$$\nabla_{\mu}(\rho u^{\mu}) = 0, \quad (\text{cons. of baryon no : } 1)$$

$$p = p(\rho, \epsilon, \dots). \quad (\text{EoS : } 1 + \dots)$$

$$\nabla_{\nu}^*F^{\mu\nu} = 0, \quad (\text{Maxwell eqs. : induction, zero div.})$$

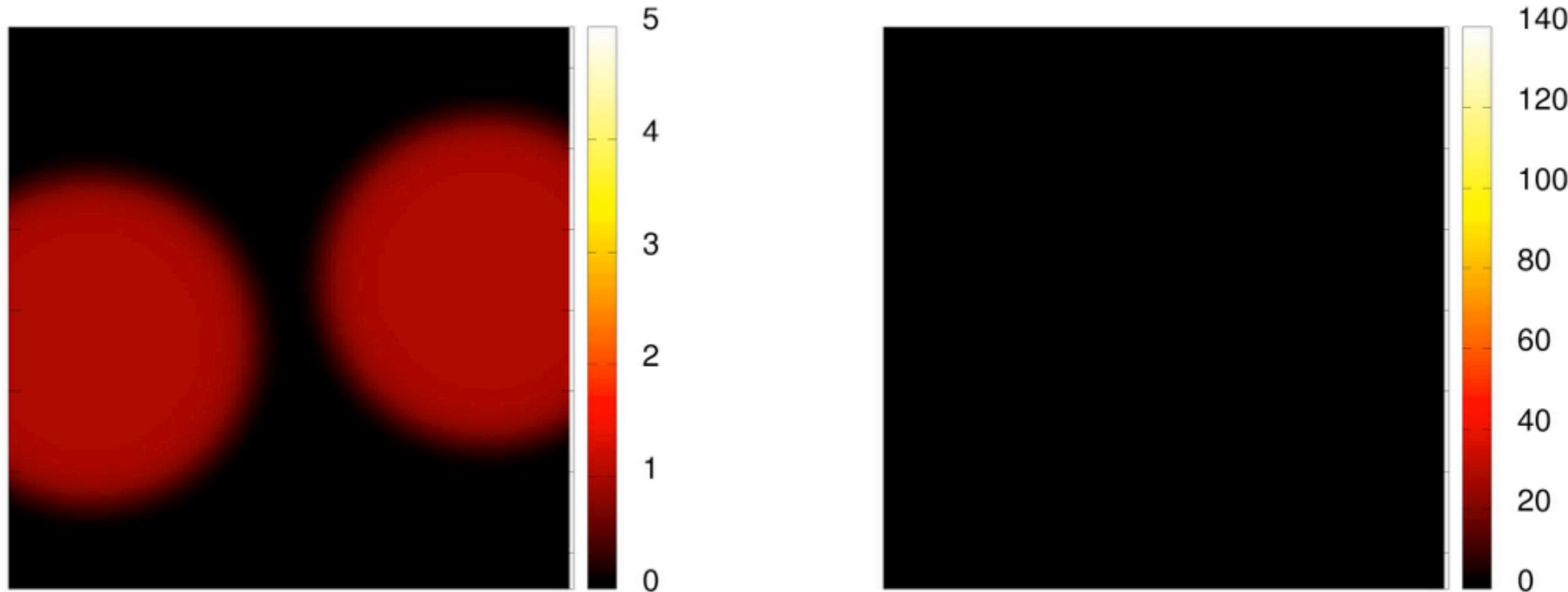
$$T_{\mu\nu} = T_{\mu\nu}^{\text{fluid}} + T_{\mu\nu}^{\text{em}} + \dots$$

These are the equations we normally solve: Einstein equations and those of relativistic hydrodynamics and MHD

The codes built are “**theoretical laboratories**”, representing our approximation to “*reality*”... they must and can be continuously improved: microphysics, magnetic fields, viscosity, radiation transport ,...

Relativistic 3+1 Dim Hydrodynamics for Heavy Ion Collisions@FAIR

Gold+Gold collisions at GSI: Helmholtz Zentrum für Schwerionenforschung.
At the FAIR facility: with high intensity beam



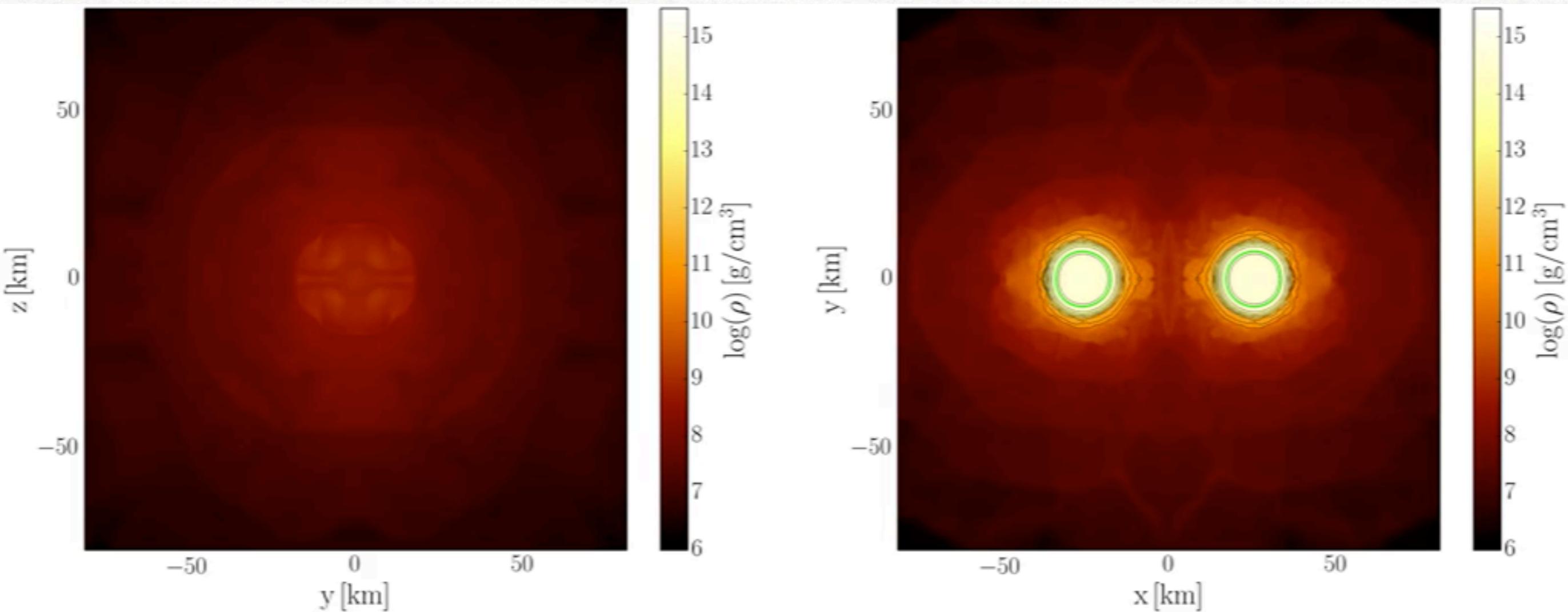
Density in units of nuclear ground state density

Temperature in MeV

time= 0.08 fm/c

Jan Steinheimer , FIAS, Flux-corrected Transport Code
Frankfurt Relativistic 3+1 Dim Hydrodynamics '80-/'90-ies
G.Graebner, D.Rischke et al., Goethe University

General Relativistic 3+1 Dim. Hydro-Dynamical Collision of 2 Neutron Stars





Neutron Star mergers vs. Heavy Ion collisions: No Difference in Hydro-Dynamics?

- Hydro-Dynamics is scale invariant !
- System Size: Kilometers vs. Femtometers - does not matter !
- Evolution time: Milliseconds vs. fm/c - does not matter !
- Chemical Equilibrium & Phase-Equilibrium vs. Non-Equilibrium ?
- Gravity is relevant ! Attraction** is enormous- Special Relativity vs. GR: BHs
- Relativistic Hydro-Dynamics works for both SR & GR!
- Importance of QCD-consistent **Relativistic nuclear EoS** equation of state
- input for both S-&G- Relativistic Hydrodynamics

SU(3) parity-doublet quark-hadron chiral mean field model

Mesonic fields:

$$\begin{aligned}
 L_{meson} = & -\frac{1}{2}(m_\omega^2\omega^2 + m_\phi^2\phi^2) \\
 & -g_4\left(\omega^4 + \frac{\phi^4}{4} + 3\omega^2\phi^2 + \frac{4\omega^3\phi}{\sqrt{2}} + \frac{2\omega\phi^3}{\sqrt{2}}\right) \\
 & +\frac{1}{2}k_0(\sigma^2 + \zeta^2) - k_1(\sigma^2 + \zeta^2)^2 \\
 & -k_2\left(\frac{\sigma^4}{2} + \zeta^4\right) - k_3\sigma^2\zeta + k_6(\sigma^6 + 4\zeta^6) \\
 & +m_\pi^2 f_\pi \sigma \\
 & +\left(\sqrt{2}m_k^2 f_k - \frac{1}{\sqrt{2}}m_\pi^2 f_\pi\right)\zeta,
 \end{aligned}$$

$$m_{i\pm}^* = \sqrt{\left[(g_{\sigma i}^{(1)}\sigma + g_{\zeta i}^{(1)}\zeta)^2 + (m_0 + n_s m_s)^2\right]}$$

Baryon octet + partners:

$$\begin{aligned}
 \mathcal{L}_B = & \sum_i (\bar{B}_i i \not{\partial} B_i) + \sum_i (\bar{B}_i m_i^* B_i) \\
 & + \sum_i (\bar{B}_i \gamma_\mu (g_{\omega i} \omega^\mu + g_{\rho i} \rho^\mu + g_{\phi i} \phi^\mu) B_i),
 \end{aligned}$$

$$\pm g_{\sigma i}^{(2)} \sigma \pm g_{\zeta i}^{(2)} \zeta, \quad B = \begin{pmatrix} \frac{\Sigma^0}{\sqrt{2}} + \frac{\Lambda}{\sqrt{6}} & \Sigma^+ & p \\ \Sigma^- & -\frac{\Sigma^0}{\sqrt{2}} + \frac{\Lambda}{\sqrt{6}} & n \\ \Xi^- & \Xi^0 & -2\frac{\Lambda}{\sqrt{6}} \end{pmatrix}$$

σ and ζ drive **chiral symmetry** breaking of non-strange and strange sector respectively.

Excluded volume corrections for hadrons:

$$\rho_i = \frac{\rho_i^{\text{id}}}{1 + \sum_j v_j \rho_j^{\text{id}}}$$

Quarks in PNJL-like approach:

$$\Omega_q = -T \sum_{i \in Q} \frac{\gamma_i}{(2\pi)^3} \int d^3k \ln \left(1 + \Phi \exp \frac{E_i^* - \mu_i}{T} \right)$$

$$m_q^* = g_{q\sigma} \sigma + \delta m_q + m_{0q}$$

$$m_s^* = g_{s\zeta} \zeta + \delta m_s + m_{0q},$$

where Polyakov loop Φ controls

deconfinement with the following potential:

$$U = -\frac{1}{2}a(T)\Phi\Phi^*$$

$$+ b(T) \log[1 - 6\Phi\Phi^* + 4(\Phi^3 + \Phi^{*3}) - 3(\Phi\Phi^*)^2],$$

$$a(T) = a_0 T^4 + a_1 T_0 T^3 + a_2 T_0^2 T^2, \quad b(T) = b_3 T_0^3 T$$

EoS by SU(3) Parity-doublet Quark-Hadron Chiral Mean Field CMF

Unified approach for QCD thermodynamics at wide range of scales.

Includes:

- **PDG** vacuum hadrons - plus **quarks and gluons**
- Proper description of nuclei, hypernuclei, single particle states, SHE
- **nuclear and neutron star matter, cold and hot**
- Chiral crossover: Parity partners' masses become equal
- **Deconfinement: comes separate at higher energy densities**

Main aspects of QCD phenomenology are consistently included

**A realistic and relativistic EOS for HI-Coll. at FAIR/NICA
and for NS ($T=0$) and binary NS mergers ($T\sim 70$ MeV)**

P. Papazoglou, S. Schramm et al., Phys. Rev. C 57, 2576 (1998).

P. Papazoglou, D. Zschiesche S. Schramm et al., Phys. Rev. C 59, 411 (1999).

J. Steinheimer, S. Schramm, H. Stoecker, Phys.Rev. C84 045208 (2011)

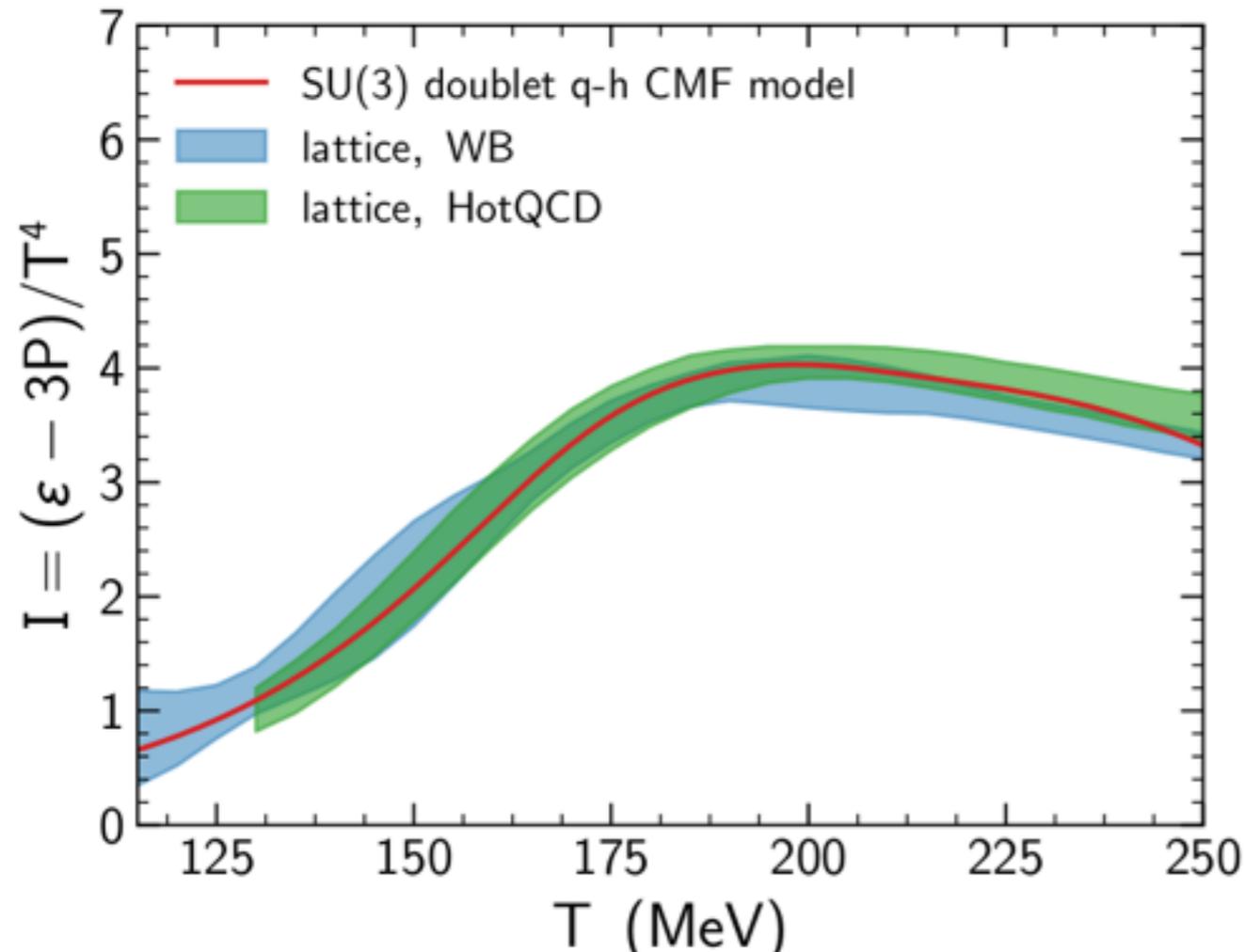
P. Rau, J. Steinheimer, S. Schramm, H. Stoecker, Phys.Lett. B733 (2014) 176-182

A. Mukherjee, J. Steinheimer, S. Schramm, Phys.Rev. C96 (2017) no.2, 025205

A. Motornenko, V. Vovchenko, J. Steinheimer, S. Schramm, H. Stoecker, 1809.02000

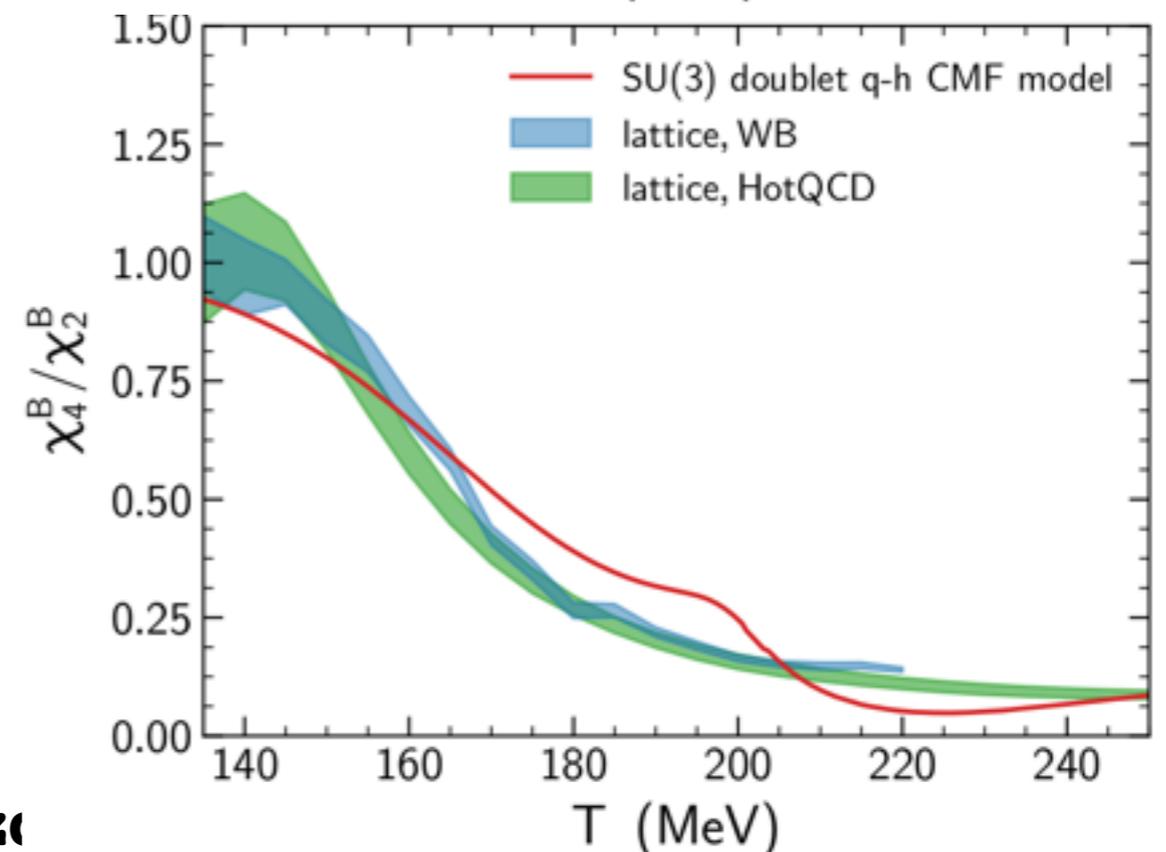
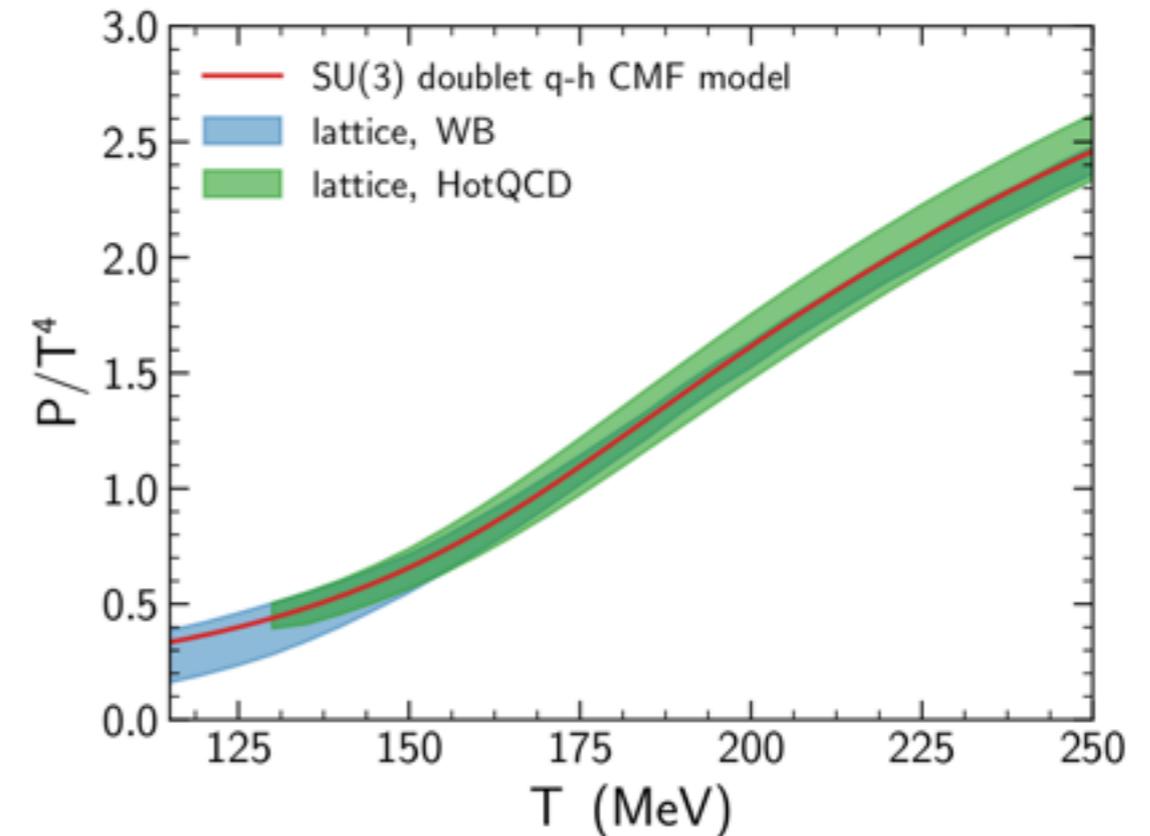
Quark-Hadron-EoS of CMF -fits to Lattice QCD data

A, Motornenko et al., 1809.02000



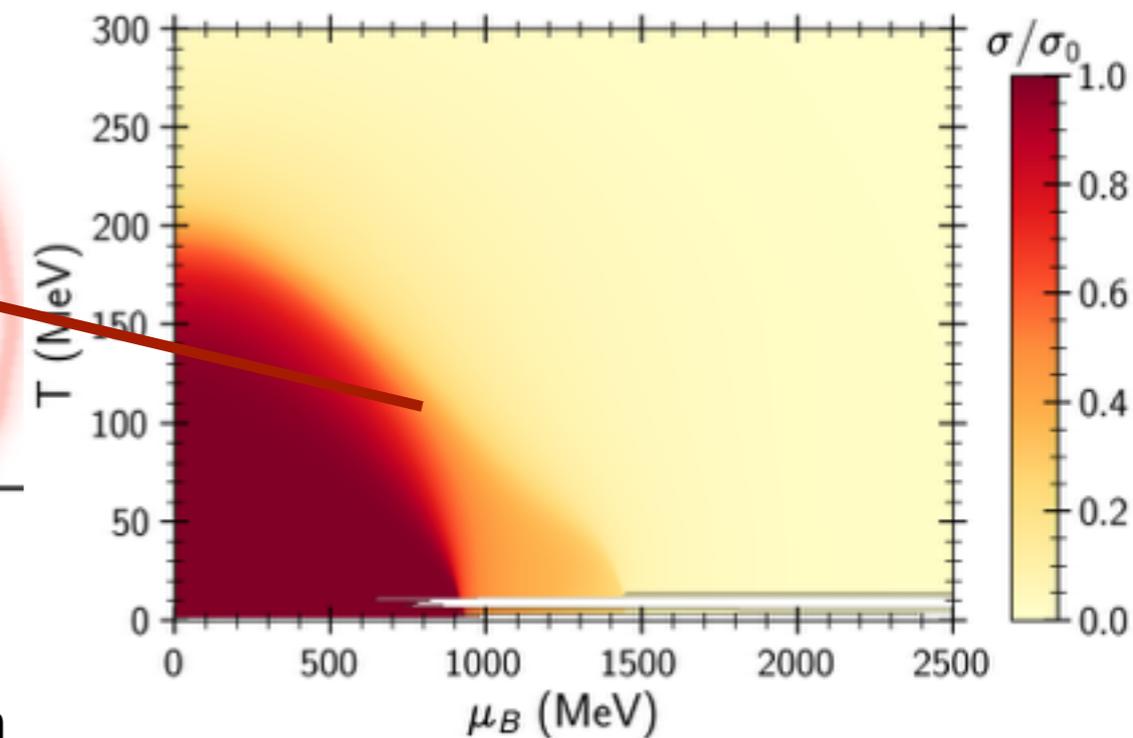
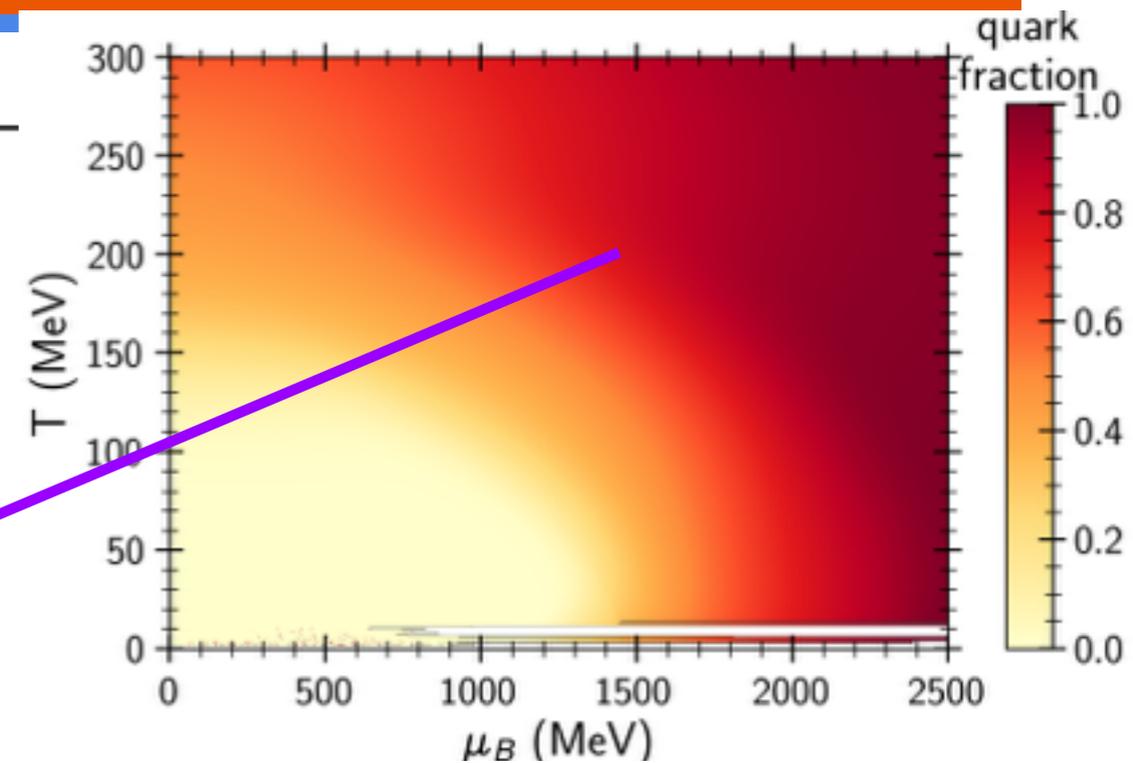
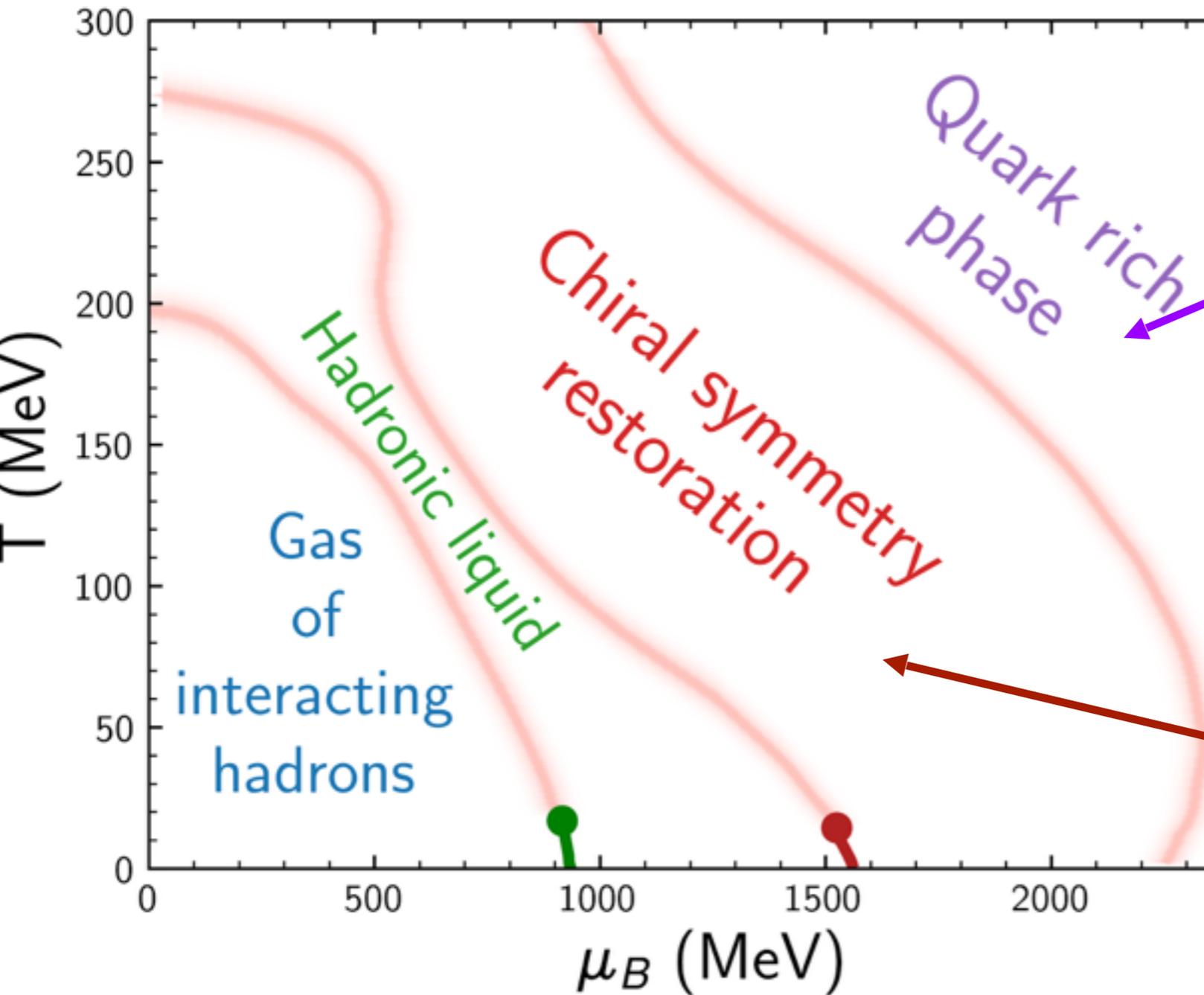
Wuppertal-Budapest collaboration, 1112.4416, 1309.5258, 1507.04627
HotQCD collaboration, 1203.0784, 1407.6387, 1701.04325

**Model successfully
reproduces lattice QCD data**



Phase diagram from relativistic Chiral Mean Field CMF

NO Phase transition at $T > 20$ MeV!

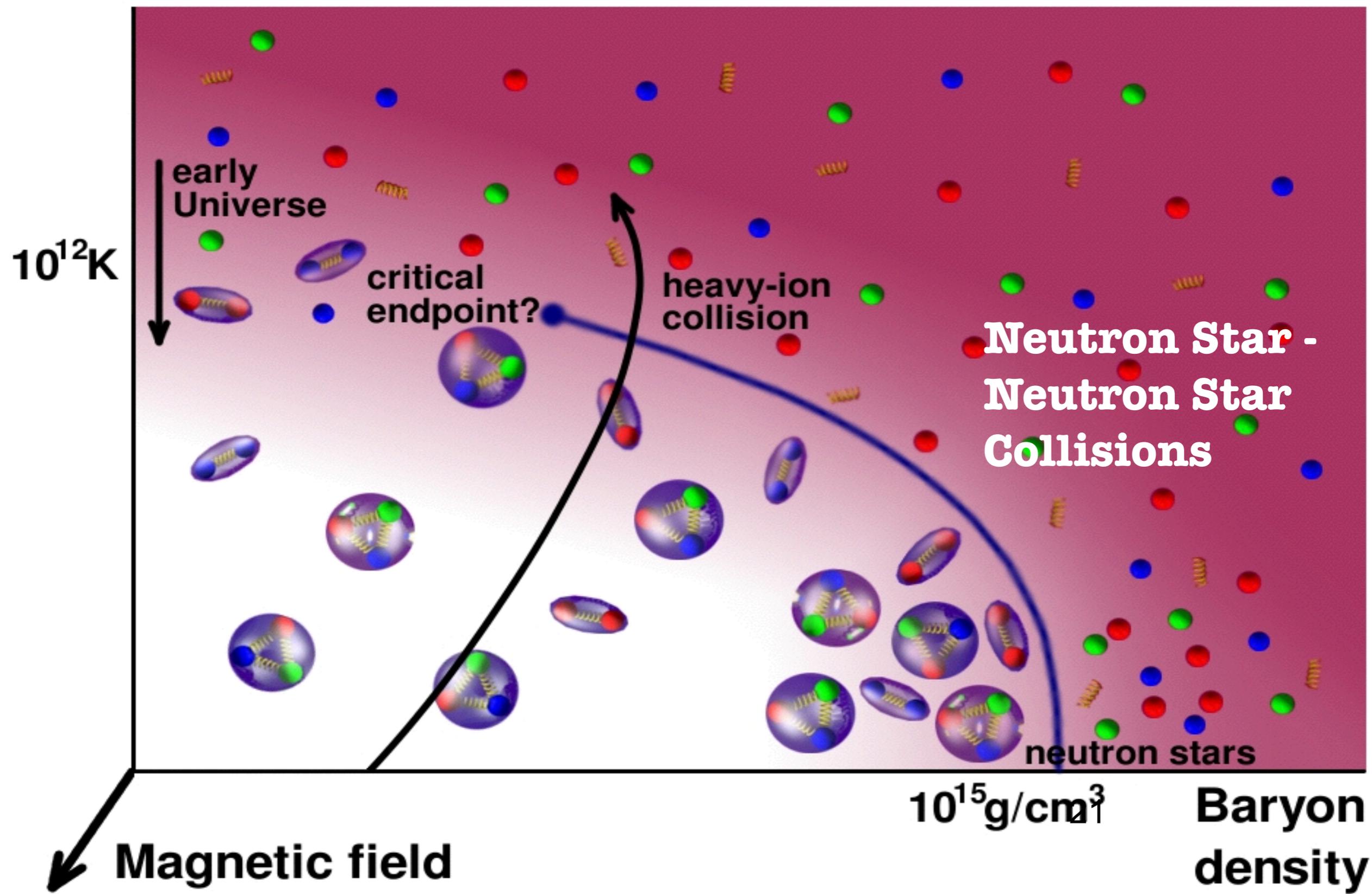


A. Motornenko et al., submitted for publication

FAIR: Dense Matter, Strange Matter, Quark Matter, Quark Stars?

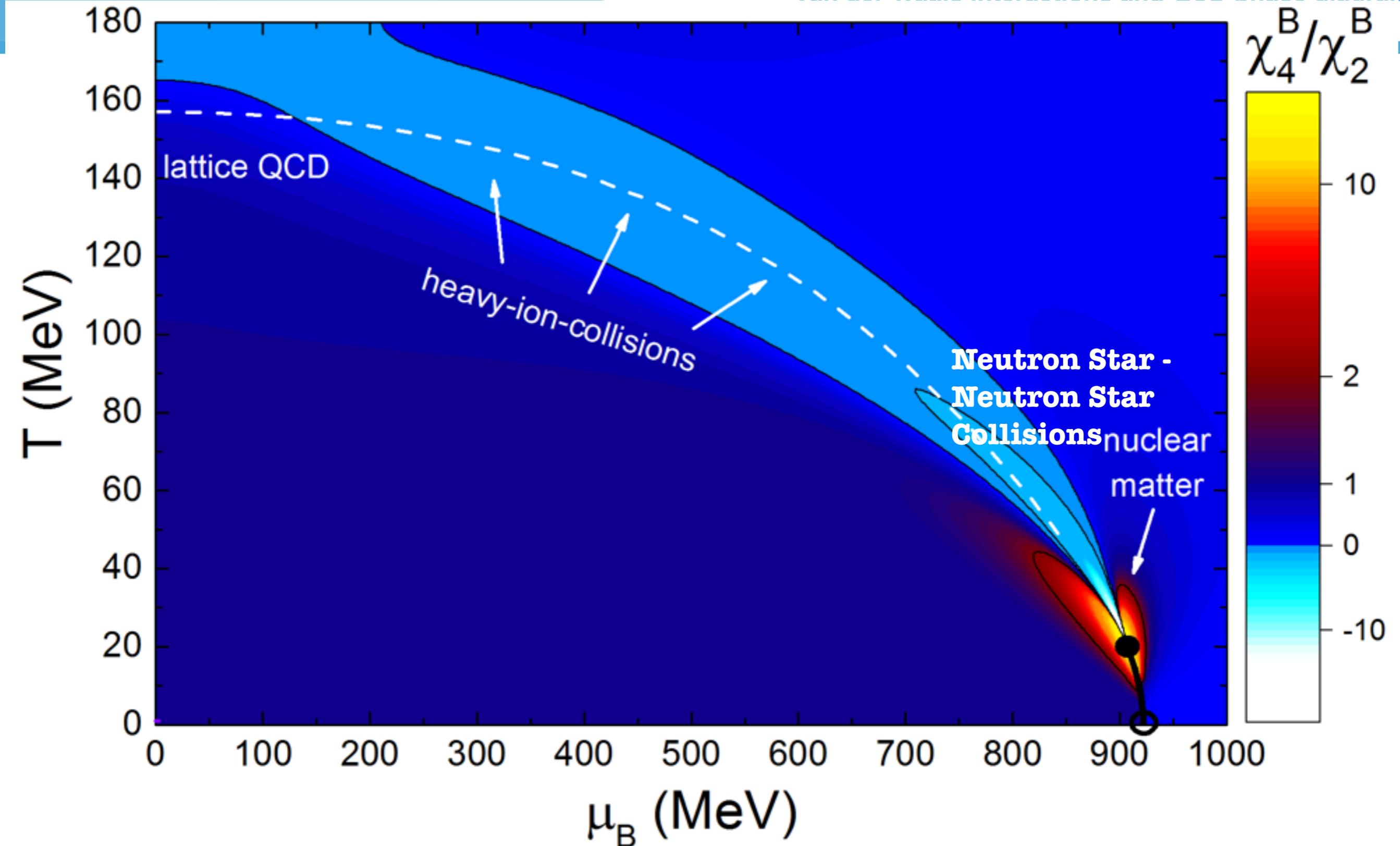
Relativistic collisions of NS-NS vs. Heavy Ions

Temperature



Unlike lattice QCD, QvdW approach is not restricted to zero net-baryon density

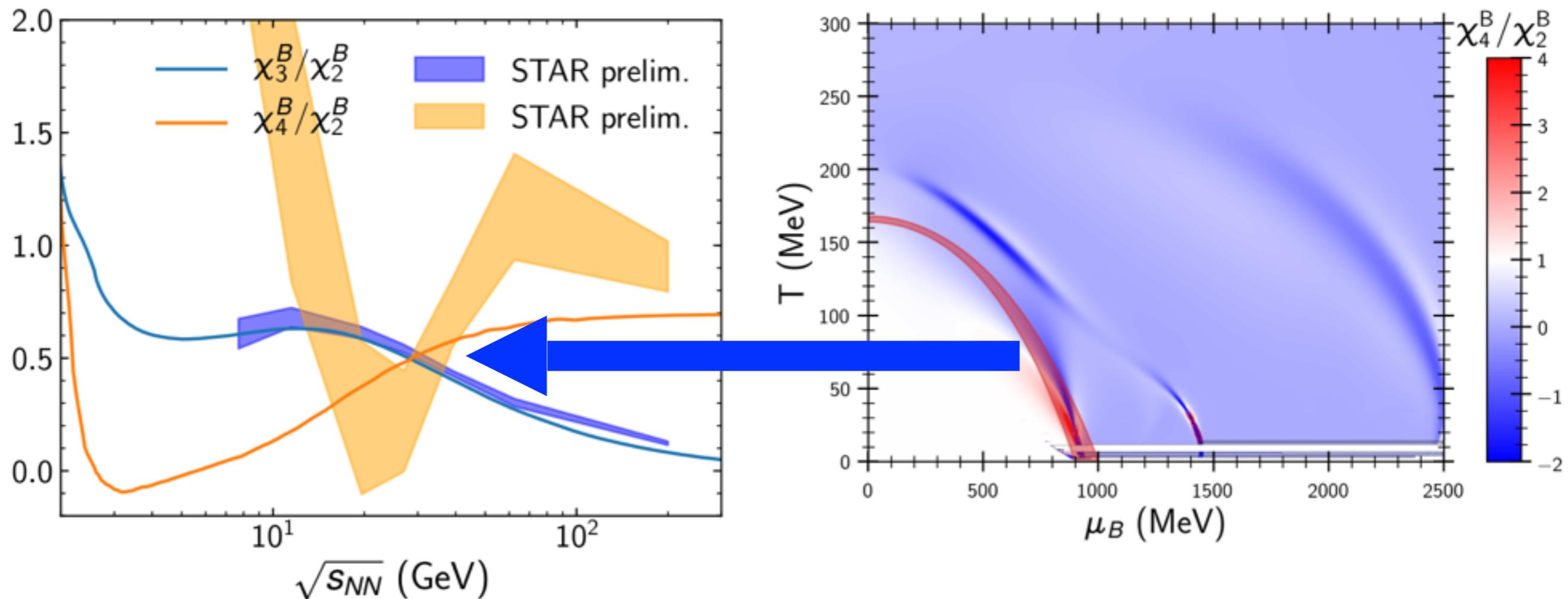
van der Waals interactions and QCD phase diagram



Nuclear matter **shines brightly** across **whole phase diagram** probed in HIC & NsNs

Probing phase diagram by heavy ions collisions

If one take “freeze-out” curve seriously, higher order susceptibilities may be presented as function of $\sqrt{s_{NN}}$ and compared with preliminary STAR data for proton cumulants.



Freeze-out curve: Cleymans, Oeschler, Redlich, Wheaton, [hep-ph/0511094]

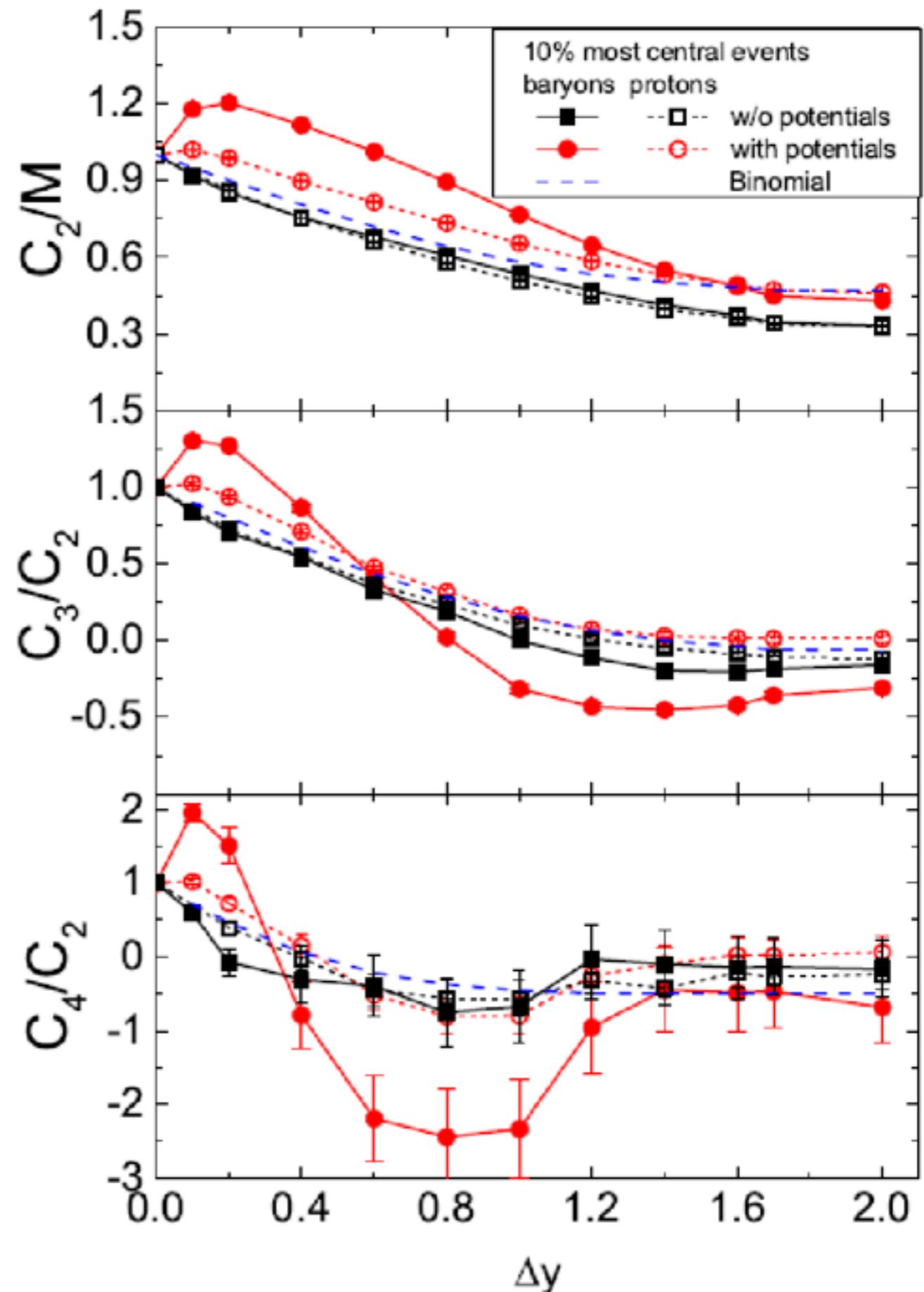
STAR data: X. Luo [STAR Collaboration], 1503.02558

Baryon number fluctuations reveal the attr.-rep. nuclear interactions

- Simulations of central Au+Au collisions with UrQMD at HADES/GSI SIS18 beam energy.
- Either use cascade mode or include Skyrme potentials.
- Calculations with potentials see an significant increase of all cumulant ratios, at small rapidity windows
- Can we find effects of the nuclear L-G critical point?
- Work in progress.

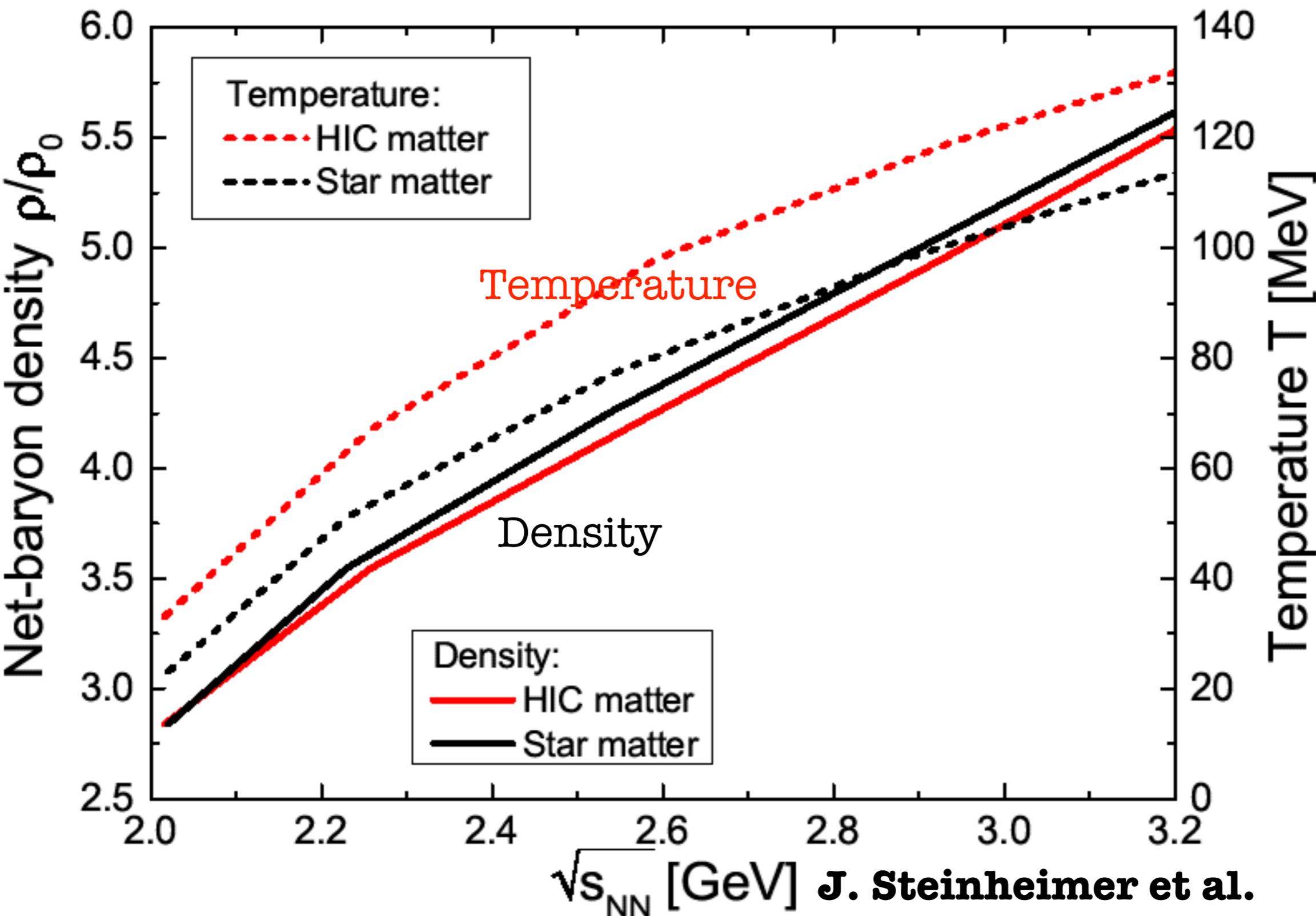
J. Steinheimer, Y. Wang, A. Mukherjee, Y. Ye, C. Guo, Q. Li and H. Stoecker, Phys. Lett. B 785, 40 (2018)

Y. Ye, et al., arXiv:1808.06342 [nucl-th].



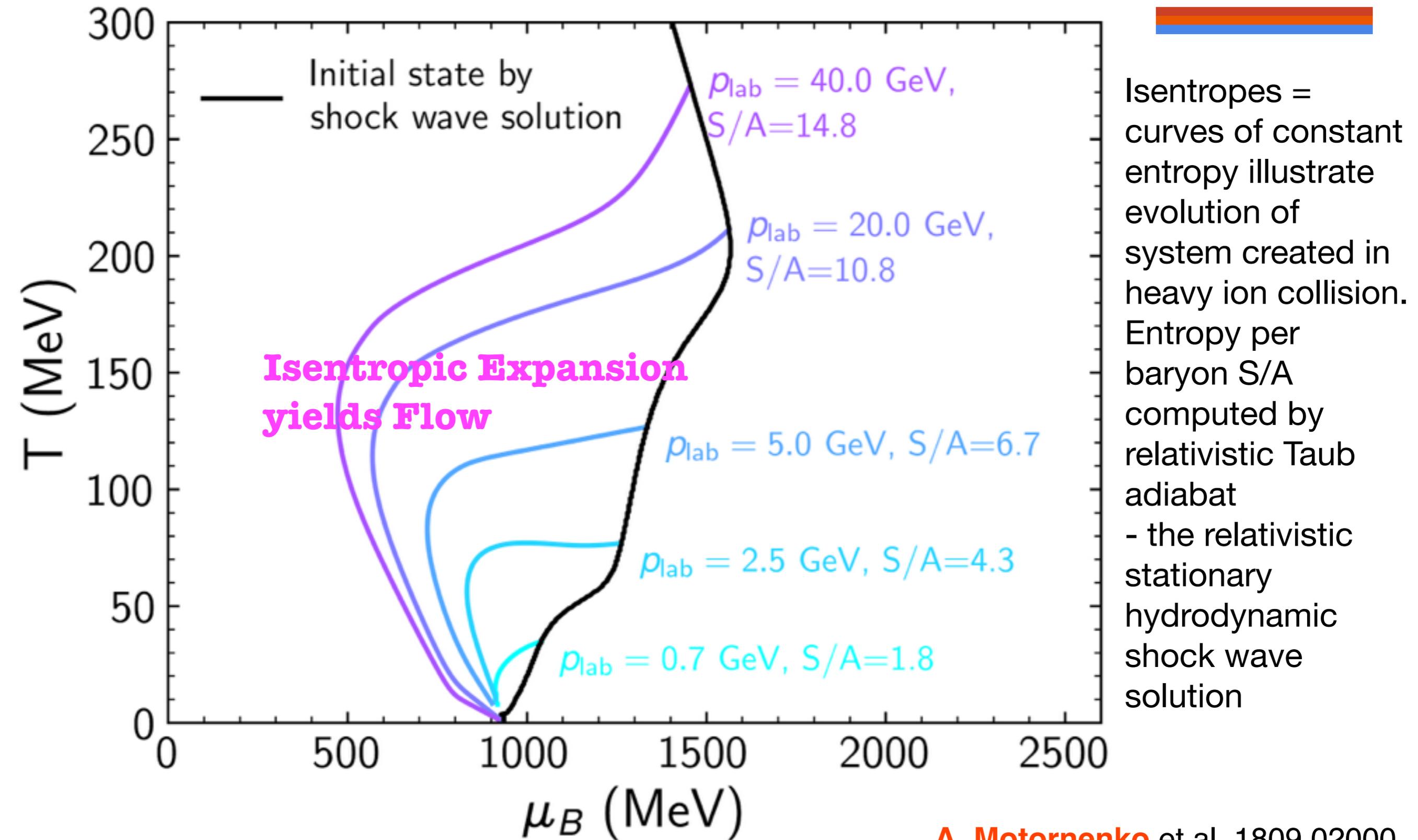
Neutron Star merger vs. heavy ion collisions: Which initial Densities and Temperatures are reached?

+ initialize by Relativistic Rankine Hugoniot Taub Adiabats with Relativistic CMF- EoS



Compare central heavy ion collisions with head-on neutron star collisions:
Rankine Hugoniot Taub Adiabate
conserve baryon number and energy momentum current densities across shock front yields 1-Dim, stationary hydrodynamical equation for n, p vs $E_{cm}=E$:
 $E^2 - E_0^2 = (p-p_0)(E/n - E_0/n_0)$

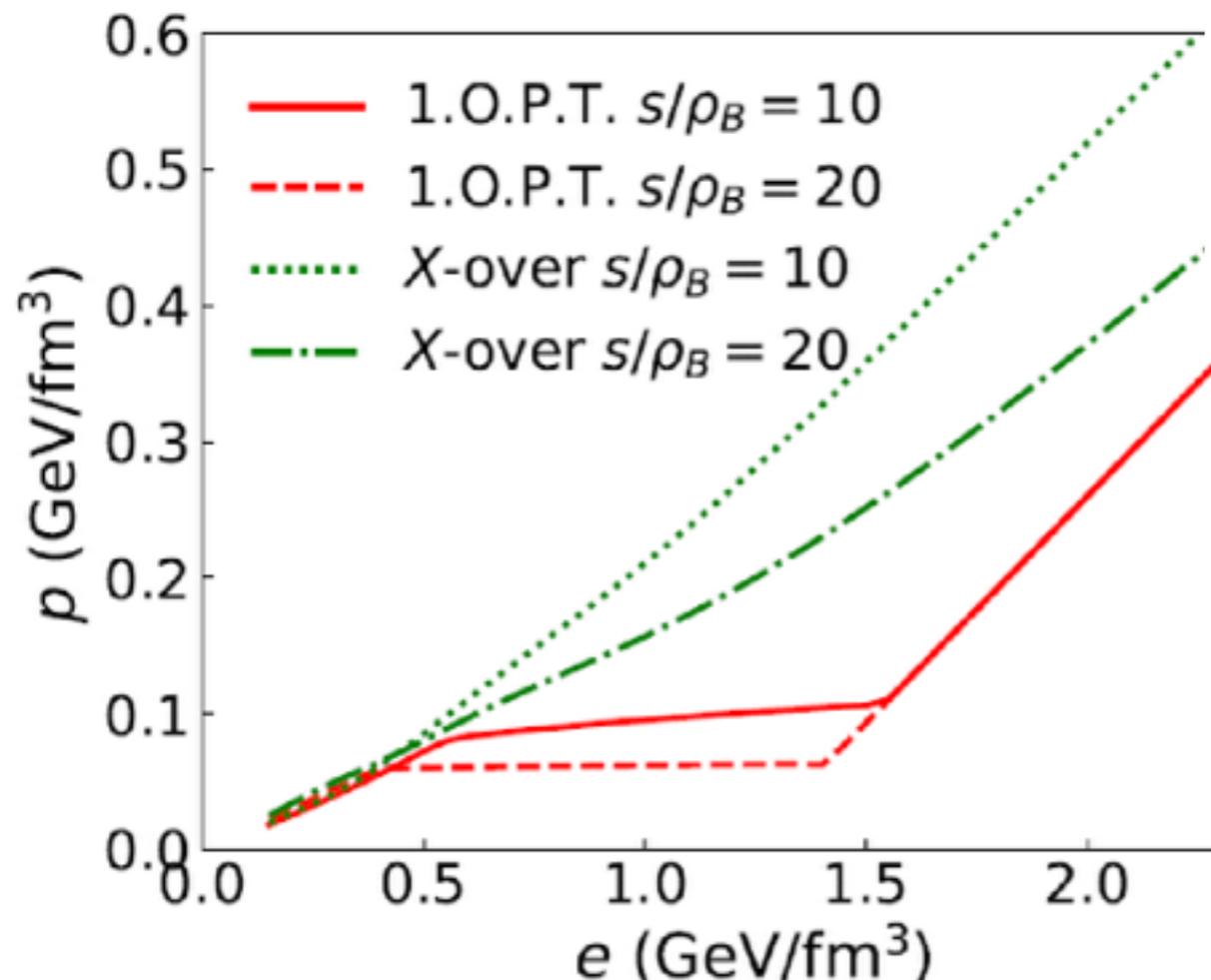
Probing phase diagram by relativistic heavy ions collisions: Collective Flow from High Pressure initial state by isentropic expansion



A. Motornenko et al., 1809.02000

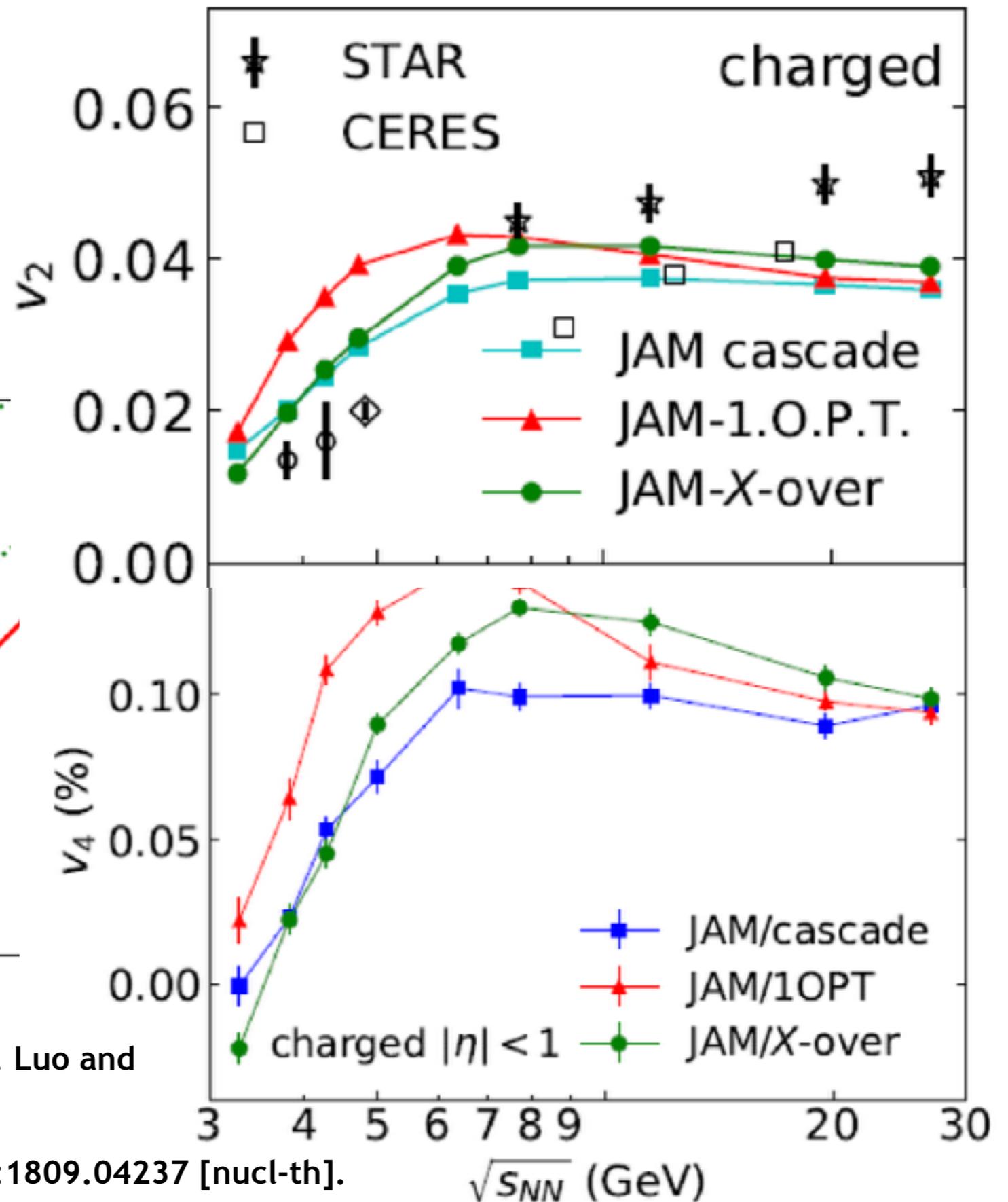
2.nd and 4.th order coefficient of FLOW will signal a 1. order phase transition

- Calculation relativistic
- JAM transport model
- EoS introduced via azimuthal scattering angle
- Clear peak in v_2 and v_4 for first order phase transition.



Y. Nara, H. Niemi, A. Ohnishi, J. Steinheimer, X. Luo and H. Stöcker, Eur. Phys. J. A 54, no. 2, 18 (2018)

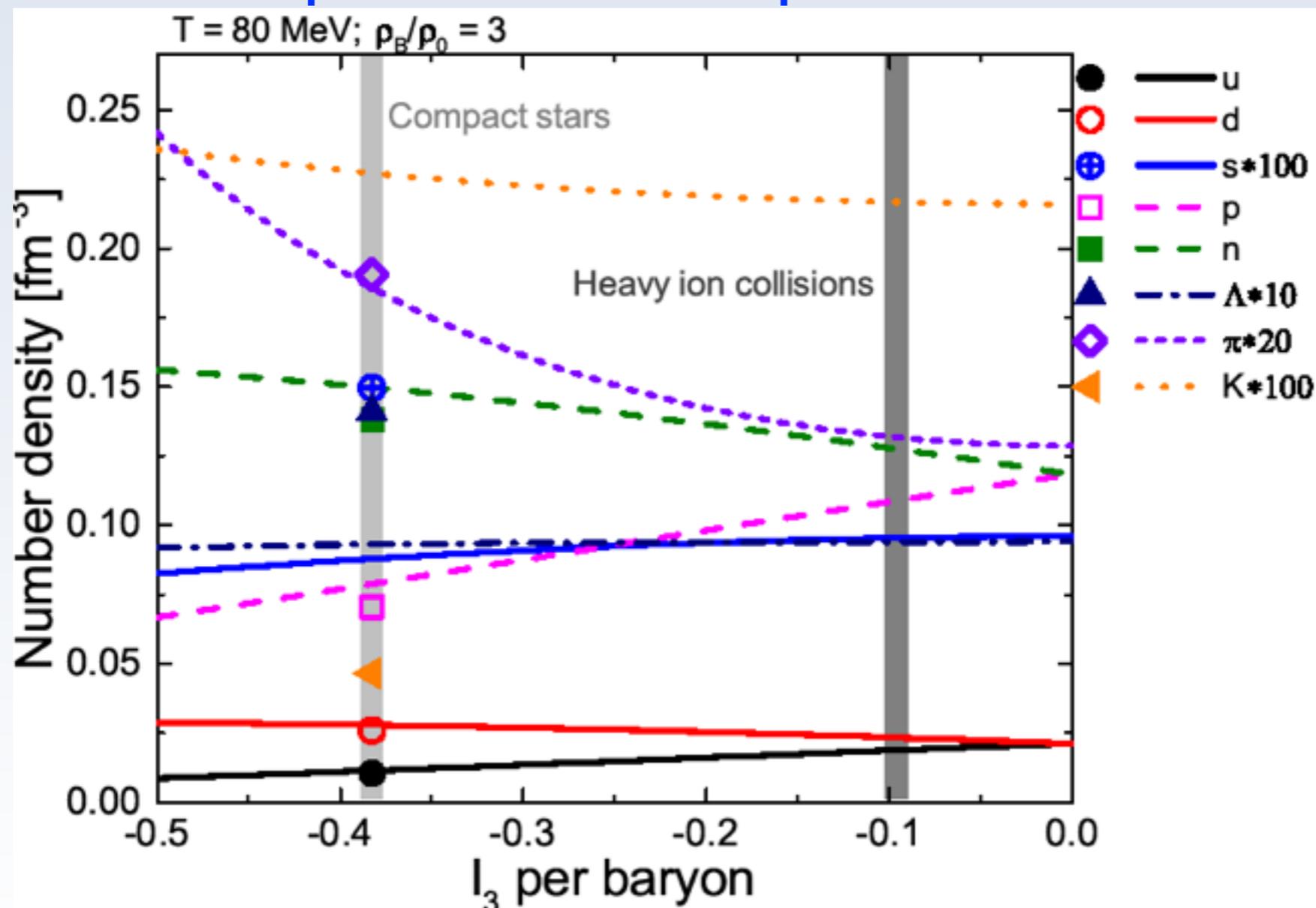
Y. Nara, J. Steinheimer and H. Stoecker, arXiv:1809.04237 [nucl-th].



Neutronstar merger vs. heavy ion collisions

Differences in chemical composition

- ❑ The EOS for heavy ion collisions: conserved strangeness and NO beta-equilibrium
- ❑ The EOS for compact stars: in beta-equilibrium



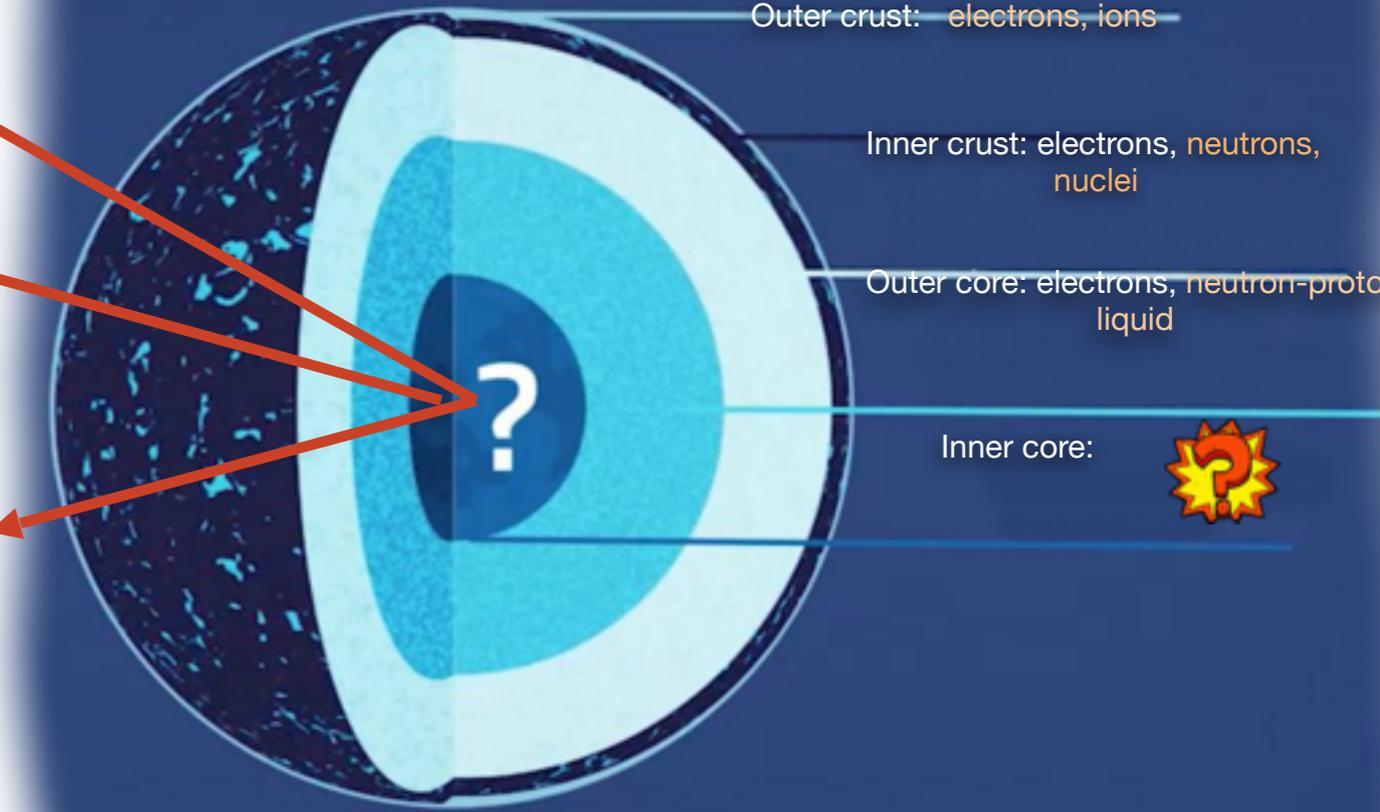
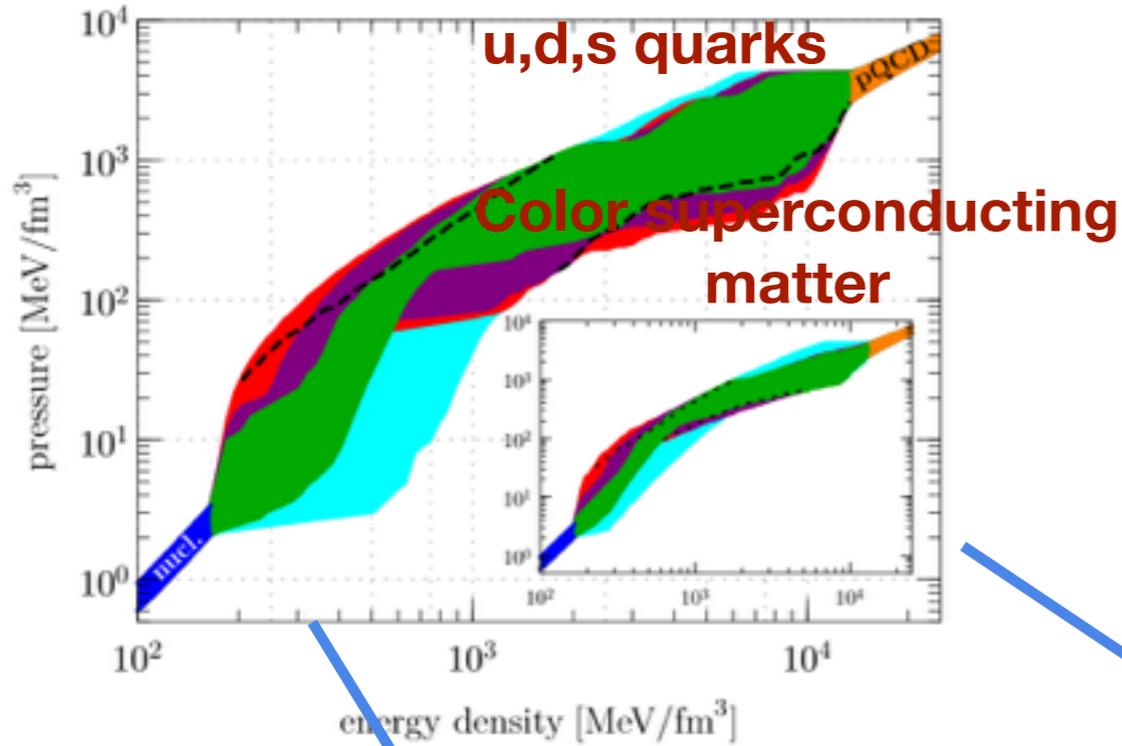
- ❑ $T = 80 \text{ MeV}$
- ❑ 3 times nuclear ground state density
- ❑ Large difference in strangeness content and iso-spin

Neutron stars put constraints on properties of T=0 QCD matter!

SU(3) parity-doublet quark-hadron chiral mean field model

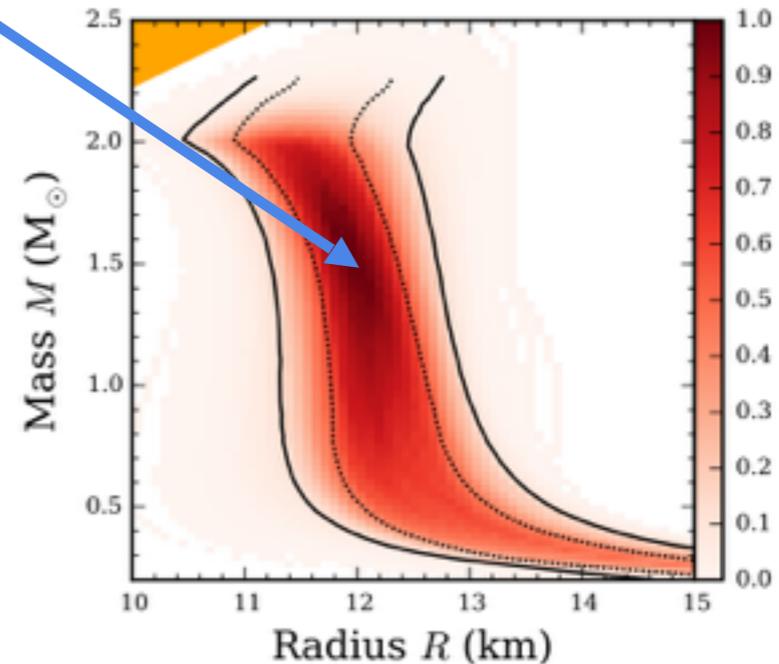
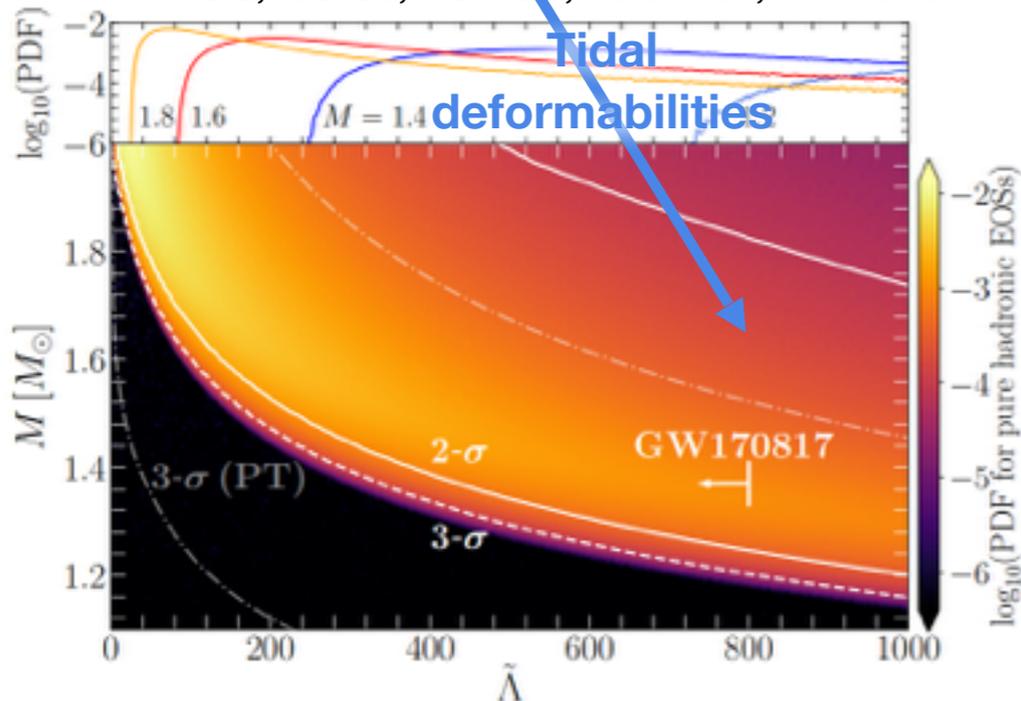
Hyperons

Equation of state at T=0:



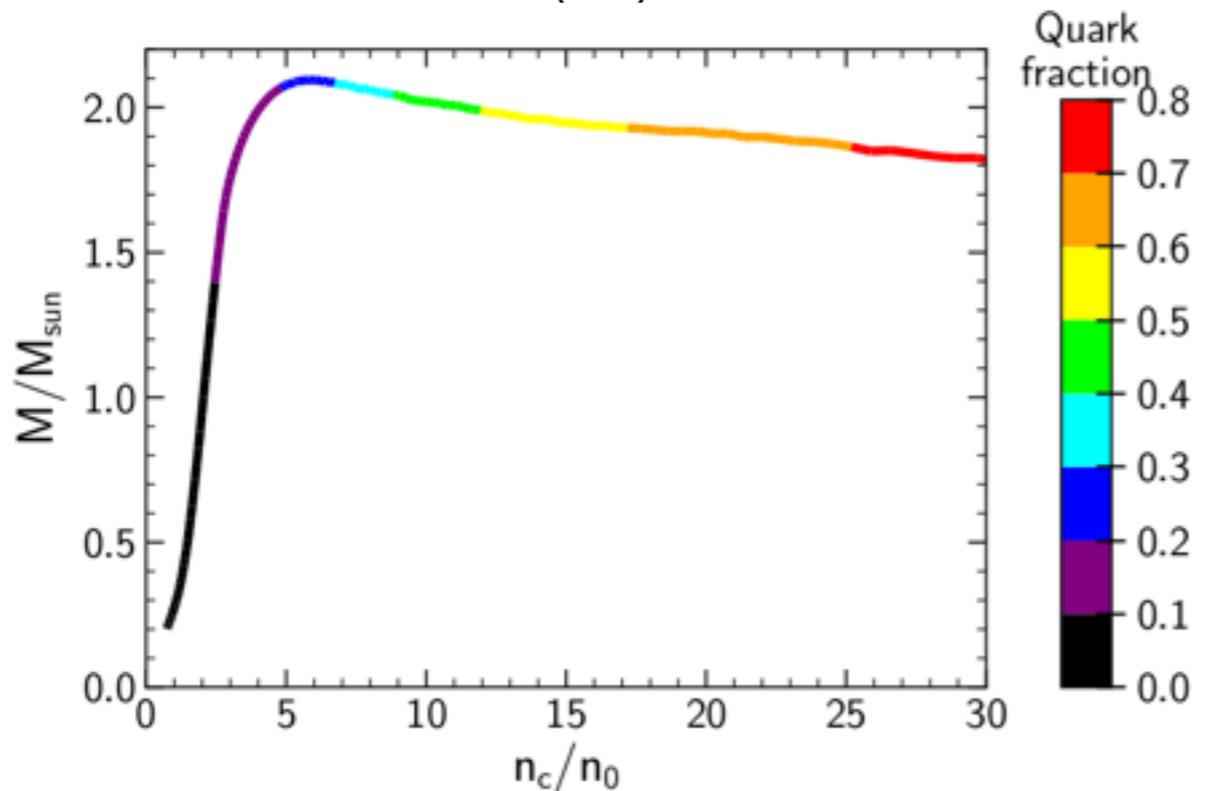
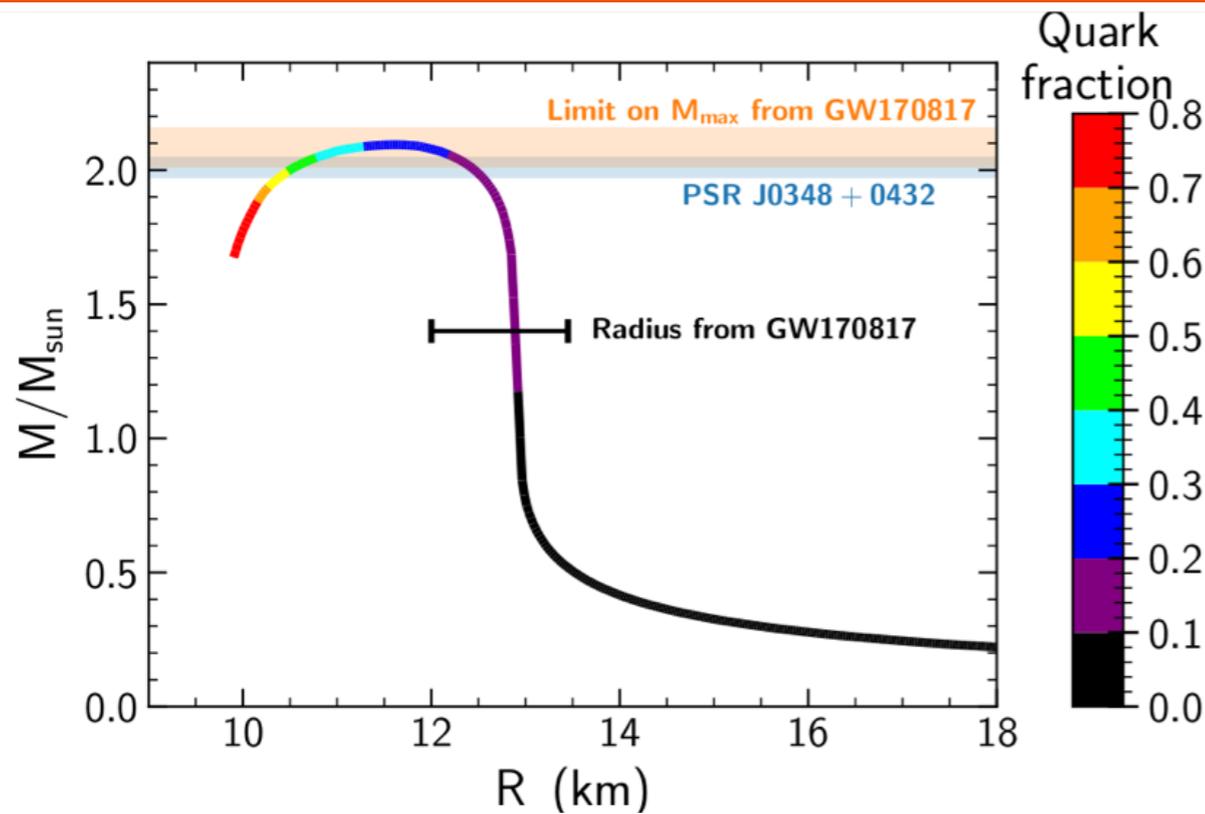
Mass-radius relations

Annala, Gorda, Kurkela, Vuorinen, 1711.02644

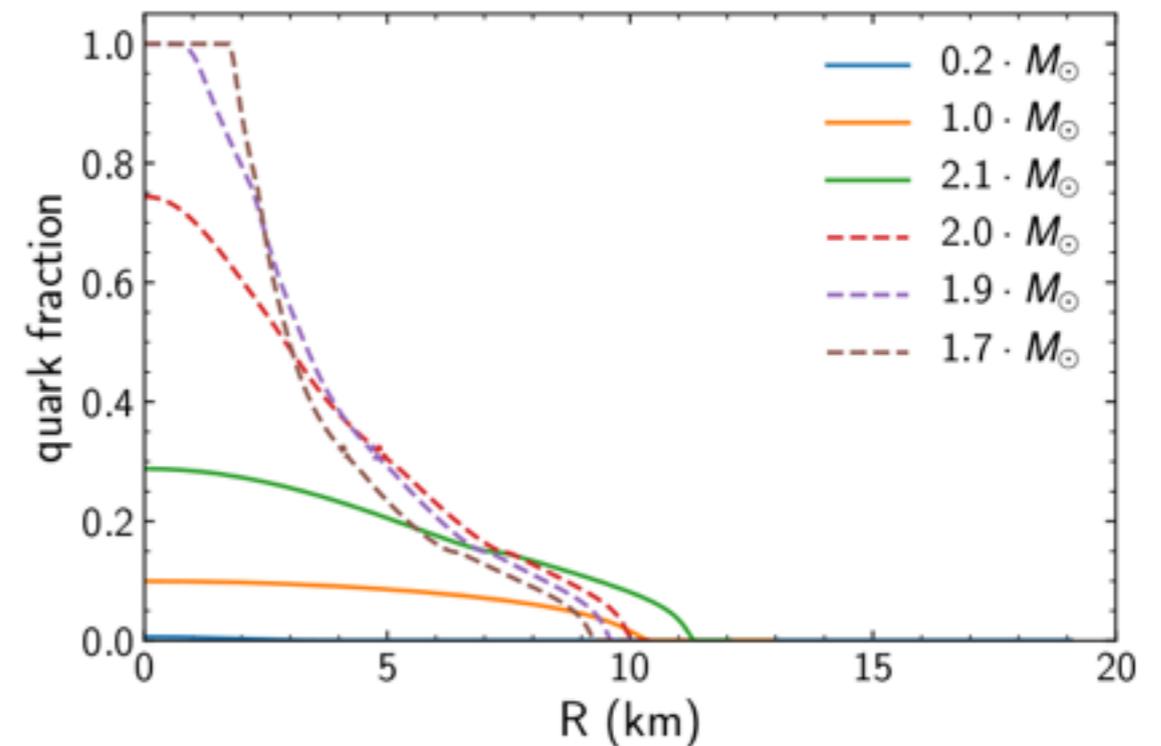


Nättilä et al., 1509.06561

Mass-radius relations



Local quark fraction
(dashed — unstable stars):



Maximal mass is in agreement with recent constraints from GW170817:

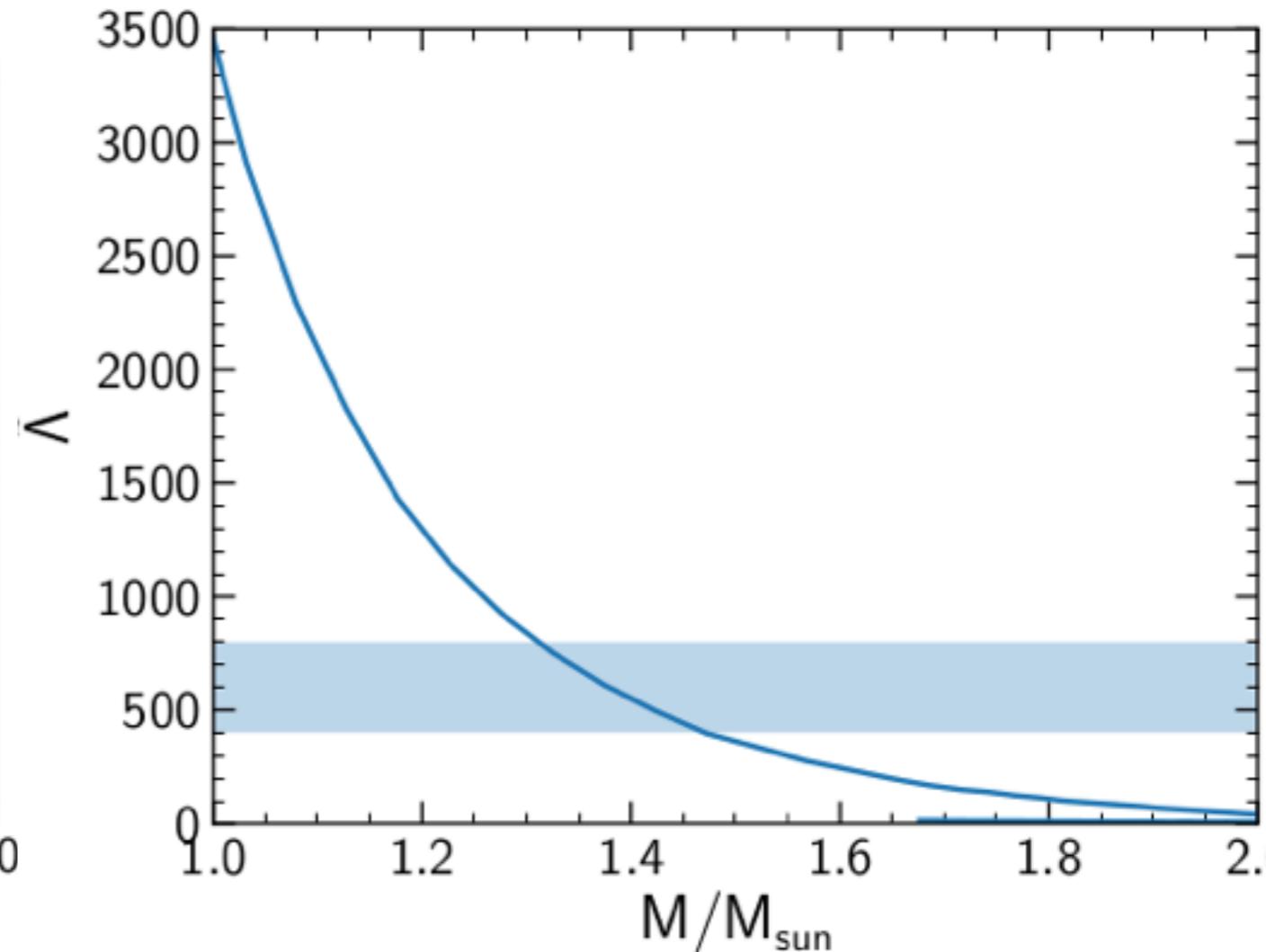
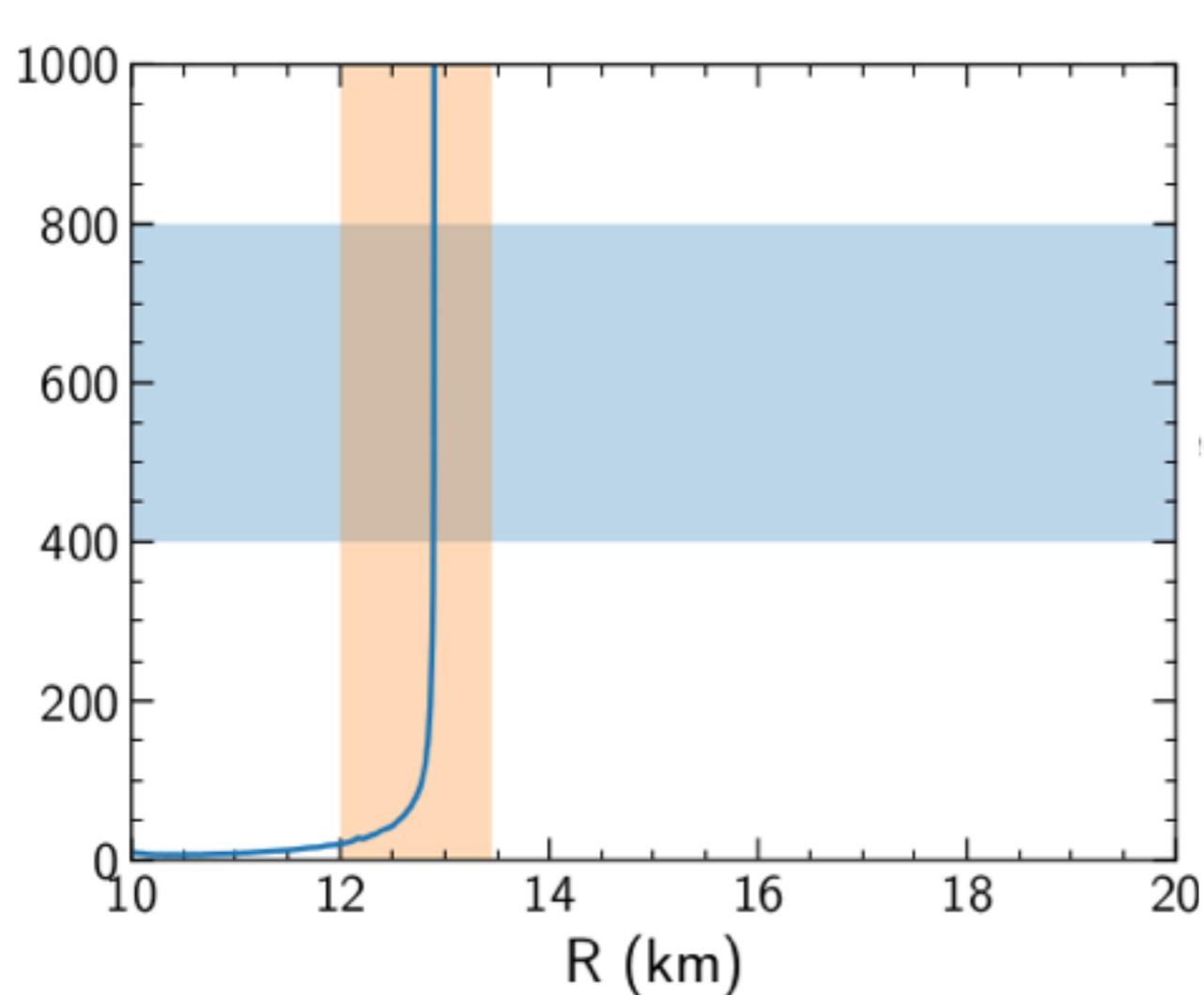
$$2.01^{+0.04}_{-0.04} \leq M_{\text{TOV}}/M_{\odot} \lesssim 2.16^{+0.17}_{-0.15}$$

Rezzolla, Most, Weih, *Astrophys.J.* 852 (2018) no.2, L25

Neutron star tidal deformabilities

Tidal deformability $Q_{ij} = -\Lambda \epsilon_{ij}$ how does star's gravit. field react to external quadrupol field:

- important EoS- dependent quantity for inspiral phase of binary neutron star system.



A. Motornenko, et al., in preparation

Bands — recent constraints for radius and tidal deformability of $1.4M_{\text{sun}}$ star.

Most, Weih, Rezzolla, Schaffner-Bielich., 1803.00549

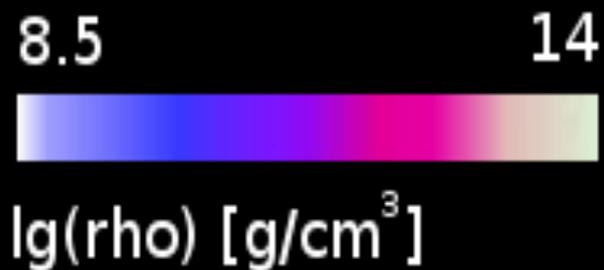
Lines — results on Λ using CMF-EoS

The Death Star will be revived only once she is attracted to her Partner !

Credits: Cosima Breu, David Radice und Luciano Rezzolla

Density of
NeutronStar Matter

Temperature of
NeutronStar Matter



Über Gravitationswellen.

Von A. EINSTEIN.

(Vorgelegt am 31. Januar 1918 [s. oben S. 79].)

Die wichtige Frage, wie die Ausbreitung der Gravitationsfelder erfolgt, ist schon vor anderthalb Jahren in einer Akademiearbeit von mir behandelt worden¹. Da aber meine damalige Darstellung des Gegenstandes nicht genügend durchsichtig und außerdem durch einen bedauerlichen Rechenfehler verunstaltet ist, muß ich hier nochmals auf die Angelegenheit zurückkommen.

Sitzungsberichte der Königlich-Preußischen Akademie der Wissenschaften
Einstein's First work on Gravitational Waves, Juni 1916, was ...**wrong**...

100 years later - LIGO:

LIGO: Laser Interferometer Gravitational-Wave Observatory

PRL 116, 061102 (2016)

Selected for a Viewpoint in *Physics*
PHYSICAL REVIEW LETTERS

week ending
12 FEBRUARY 2016



Observation of Gravitational Waves from a Binary Black Hole Merger

B. P. Abbott *et al.**

(LIGO Scientific Collaboration and Virgo Collaboration)

(Received 21 January 2016; published 11 February 2016)

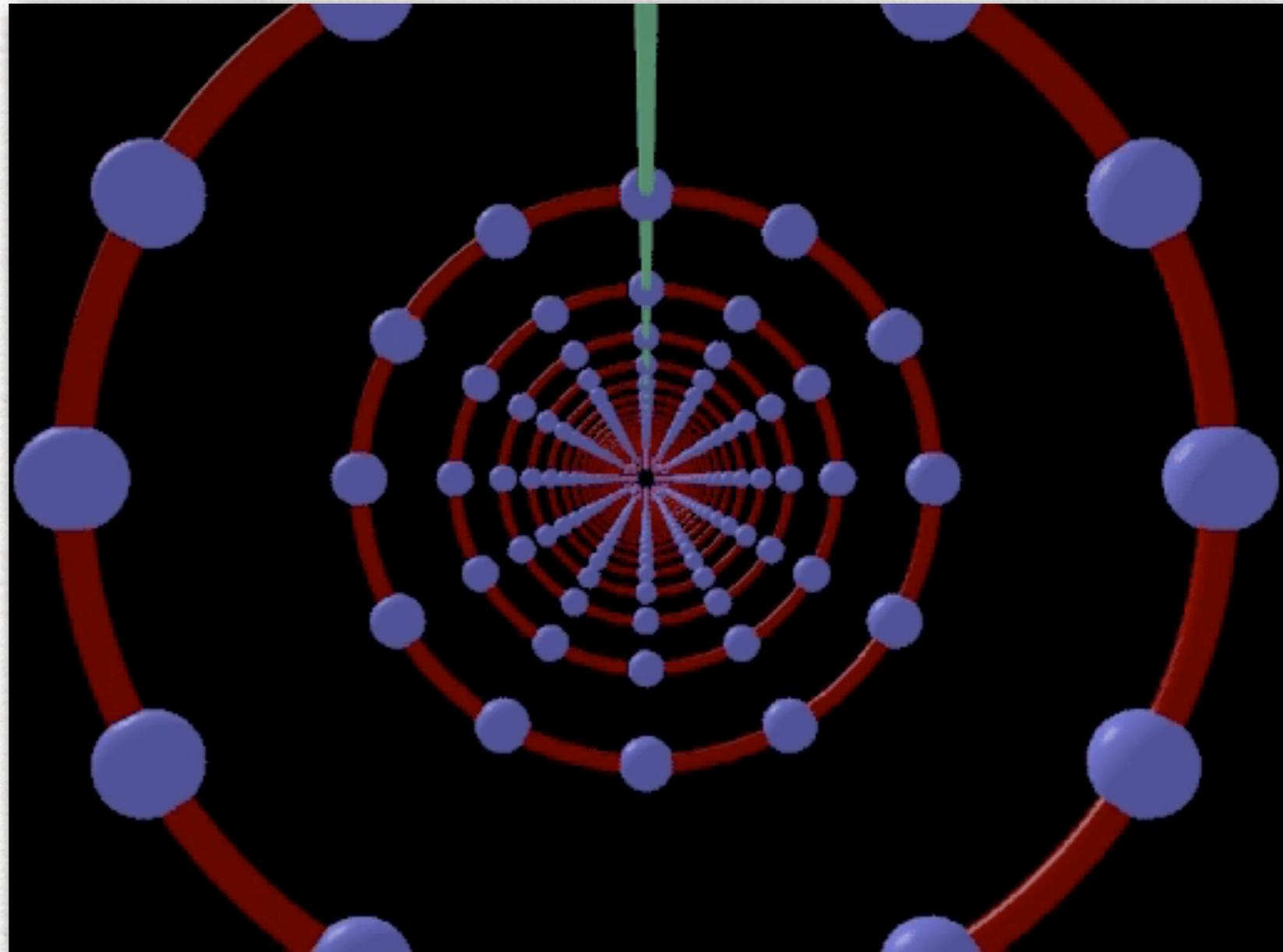
On September 14, 2015 at 09:50:45 UTC the two detectors of the Laser Interferometer Gravitational-Wave Observatory simultaneously observed a transient gravitational-wave signal. The signal sweeps upwards in frequency from 35 to 250 Hz with a peak gravitational-wave strain of 1.0×10^{-21} . It matches the waveform predicted by general relativity for the inspiral and merger of a pair of black holes and the ringdown of the resulting single black hole. The signal was observed with a matched-filter signal-to-noise ratio of 24 and a false alarm rate estimated to be less than 1 event per 203 000 years, equivalent to a significance greater than 5.1σ . The source lies at a luminosity distance of 410_{-180}^{+160} Mpc corresponding to a redshift $z = 0.09_{-0.04}^{+0.03}$. In the source frame, the initial black hole masses are $36_{-4}^{+5} M_{\odot}$ and $29_{-4}^{+4} M_{\odot}$, and the final black hole mass is $62_{-4}^{+4} M_{\odot}$, with $3.0_{-0.5}^{+0.5} M_{\odot} c^2$ radiated in gravitational waves. All uncertainties define 90% credible intervals. These observations demonstrate the existence of binary stellar-mass black hole systems. This is the first direct detection of gravitational waves and the first observation of a binary black hole merger.

First Direct Discovery of Gravitational Waves
Signalform: **melting** of two Black Holes

Gravitational waves: ripples in spacetime

The mechanical analogy is very close: general relativity predicts that if masses are accelerated, they produce *gravitational waves (GWs)*

- GWs are **transverse** waves moving at the speed of light, i.e. they produce changes in the direction orthogonal to the propagation one
- GWs effect is distorting space and time, producing **quadrupole distortions: squeeze** in one direction and **stretch** in the orthogonal one



Gravitational Waves discovered ??!!!

Collision of 2 BHs GW150914

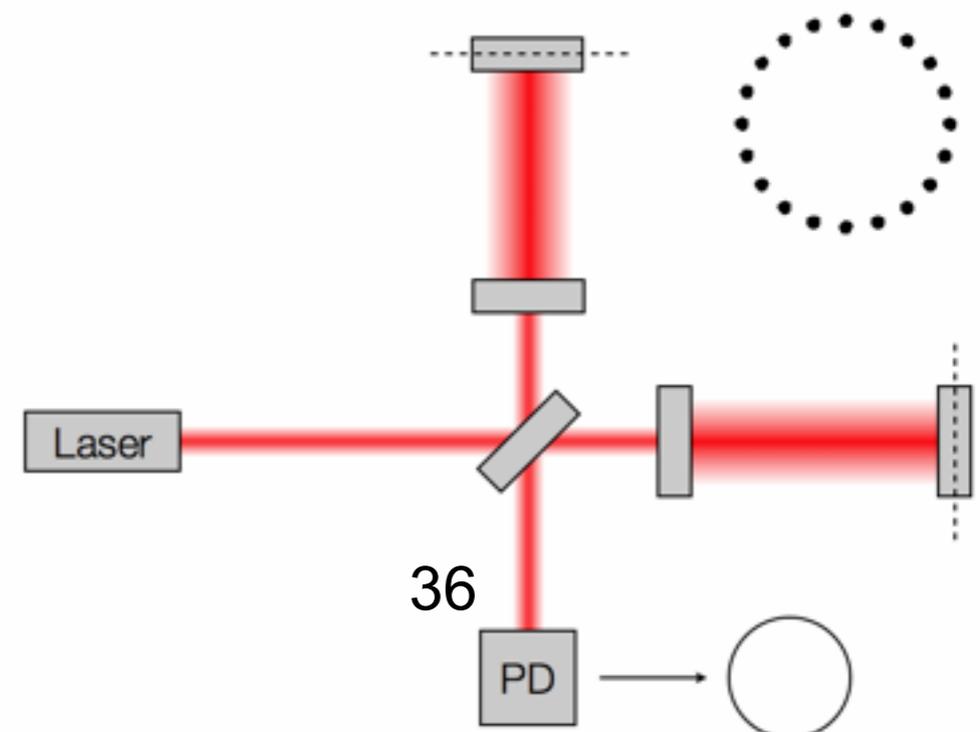
Masses of BHs: 36 & 29 Solar Masses

**Distance to Earth 410 Mpc
(1340 Million Lightyears)**

Length Difference 10^{-21} m

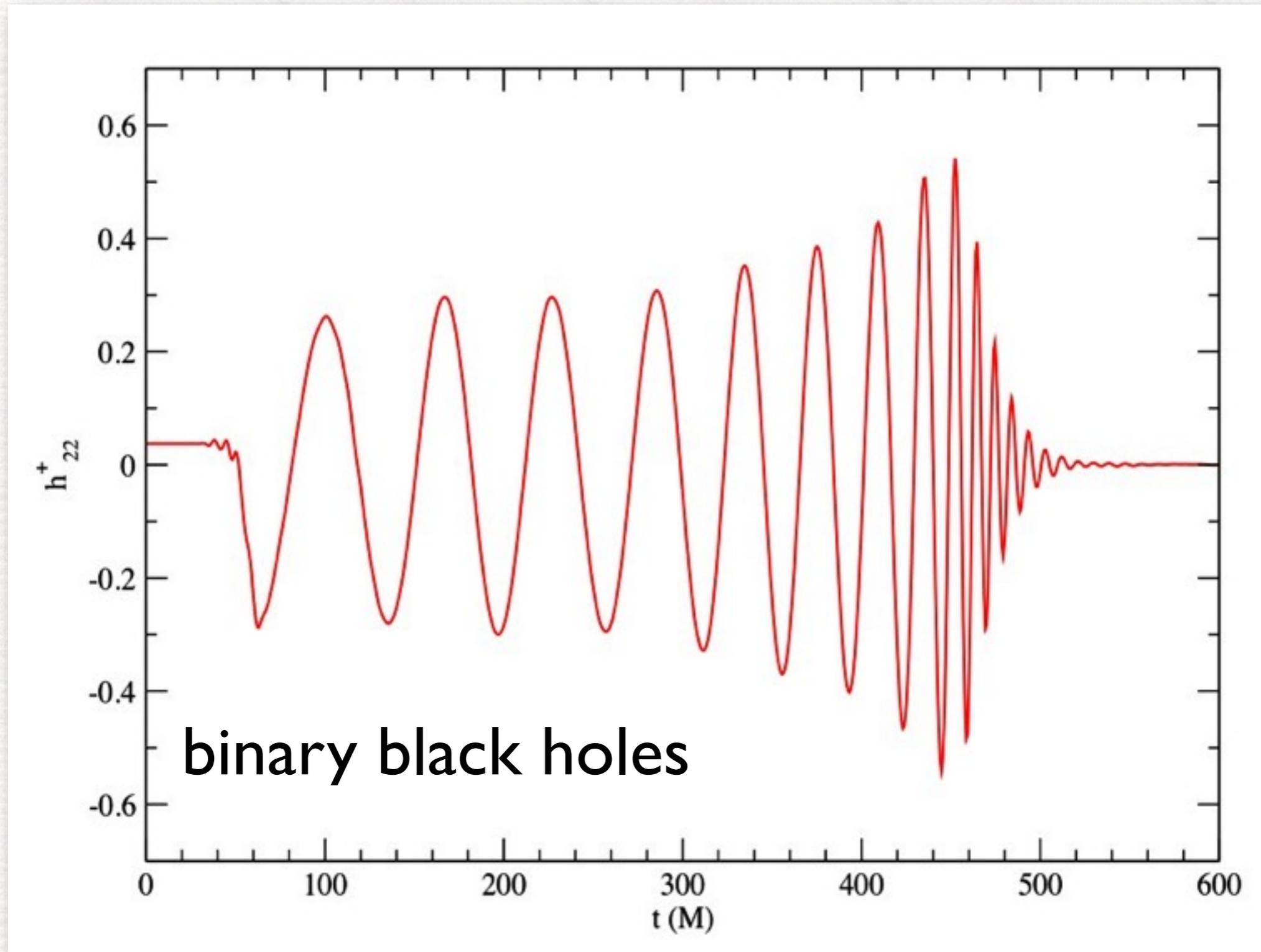


LIGO, NSF, Illustration: A. Simonnet (SSU)

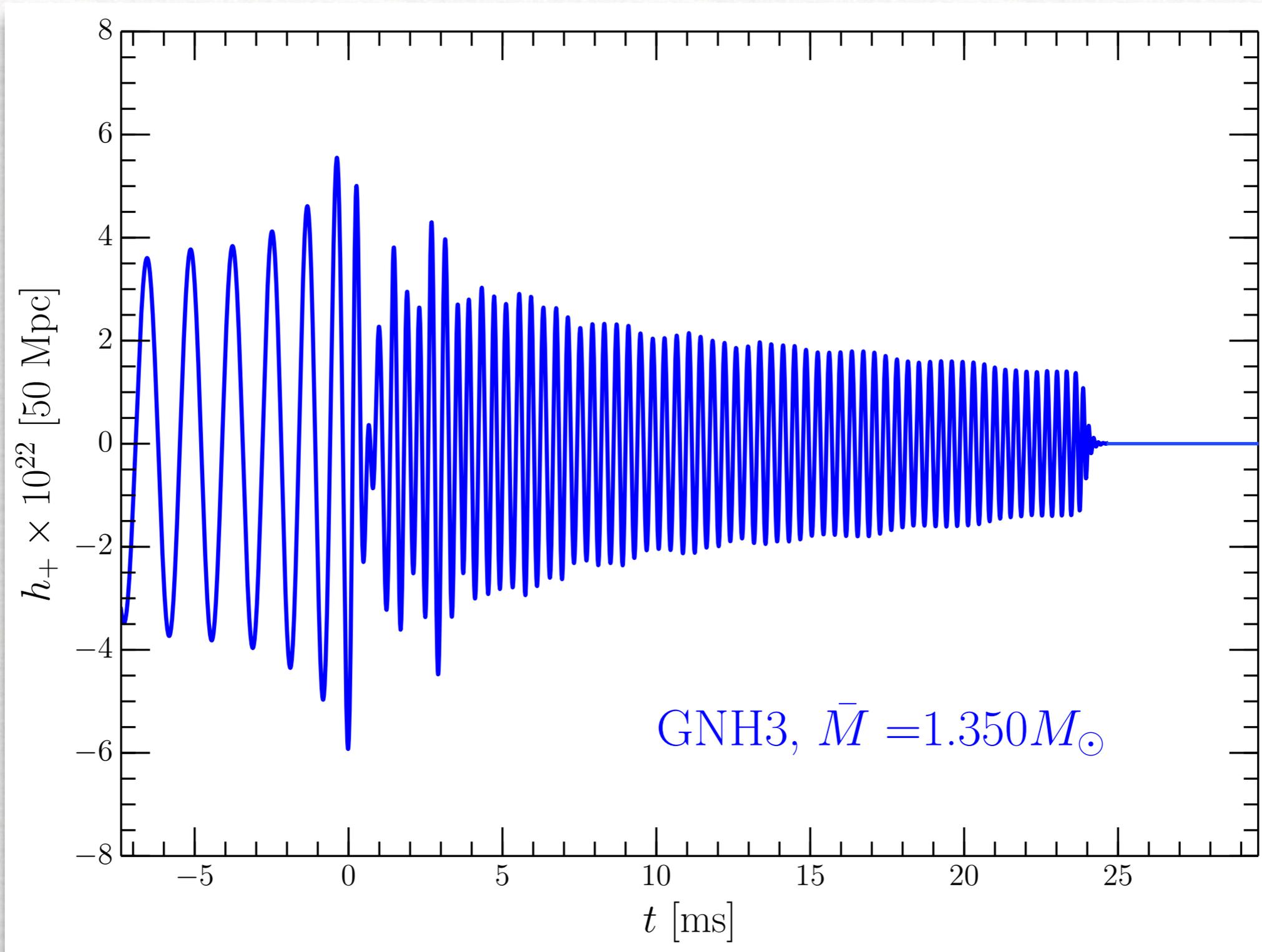


Credit: Les Wade from Kenyon College.

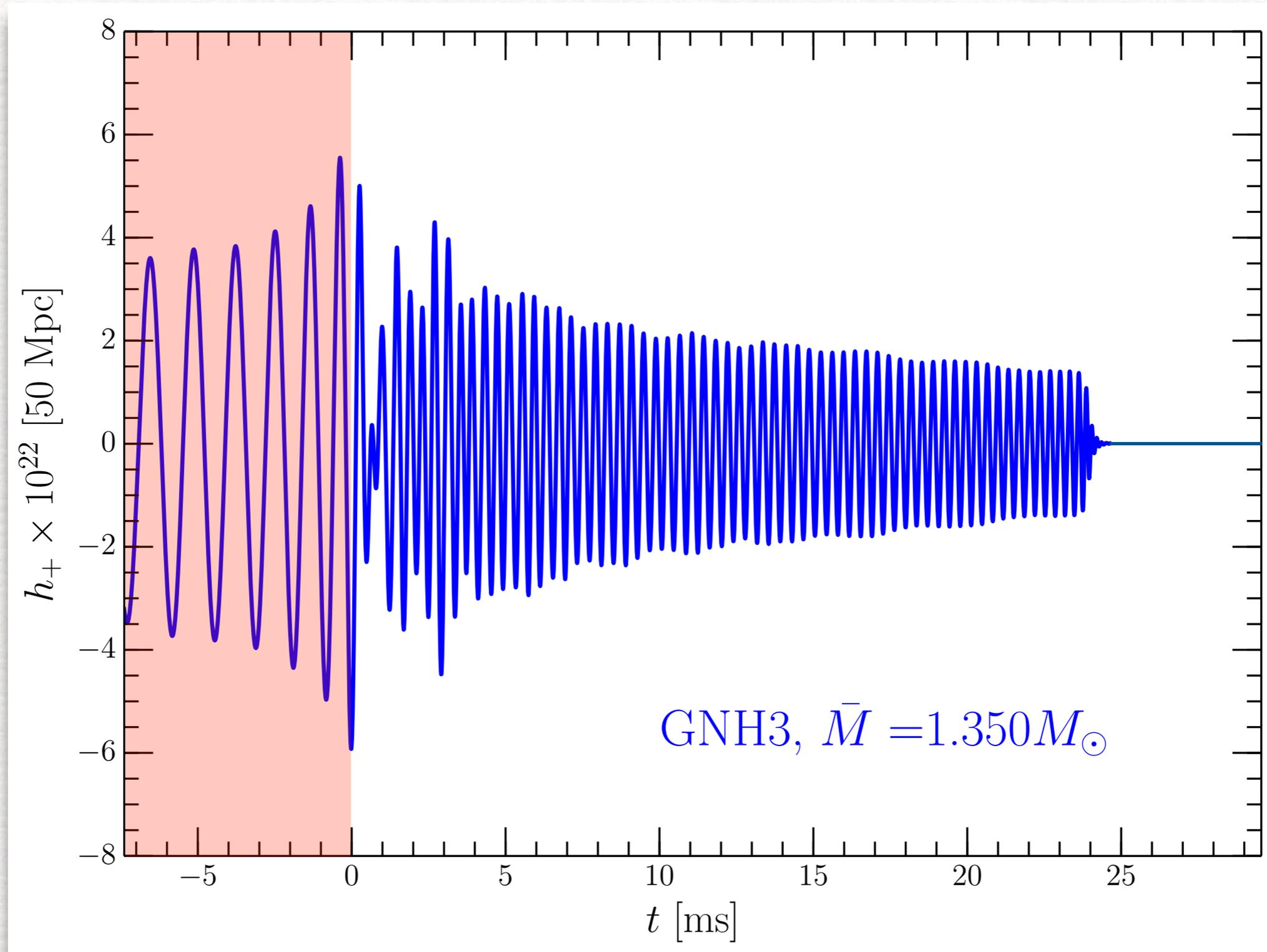
Anatomy of the GW signal for binary **Black Holes**



Anatomy of the GW signal for **binary NS Meger**

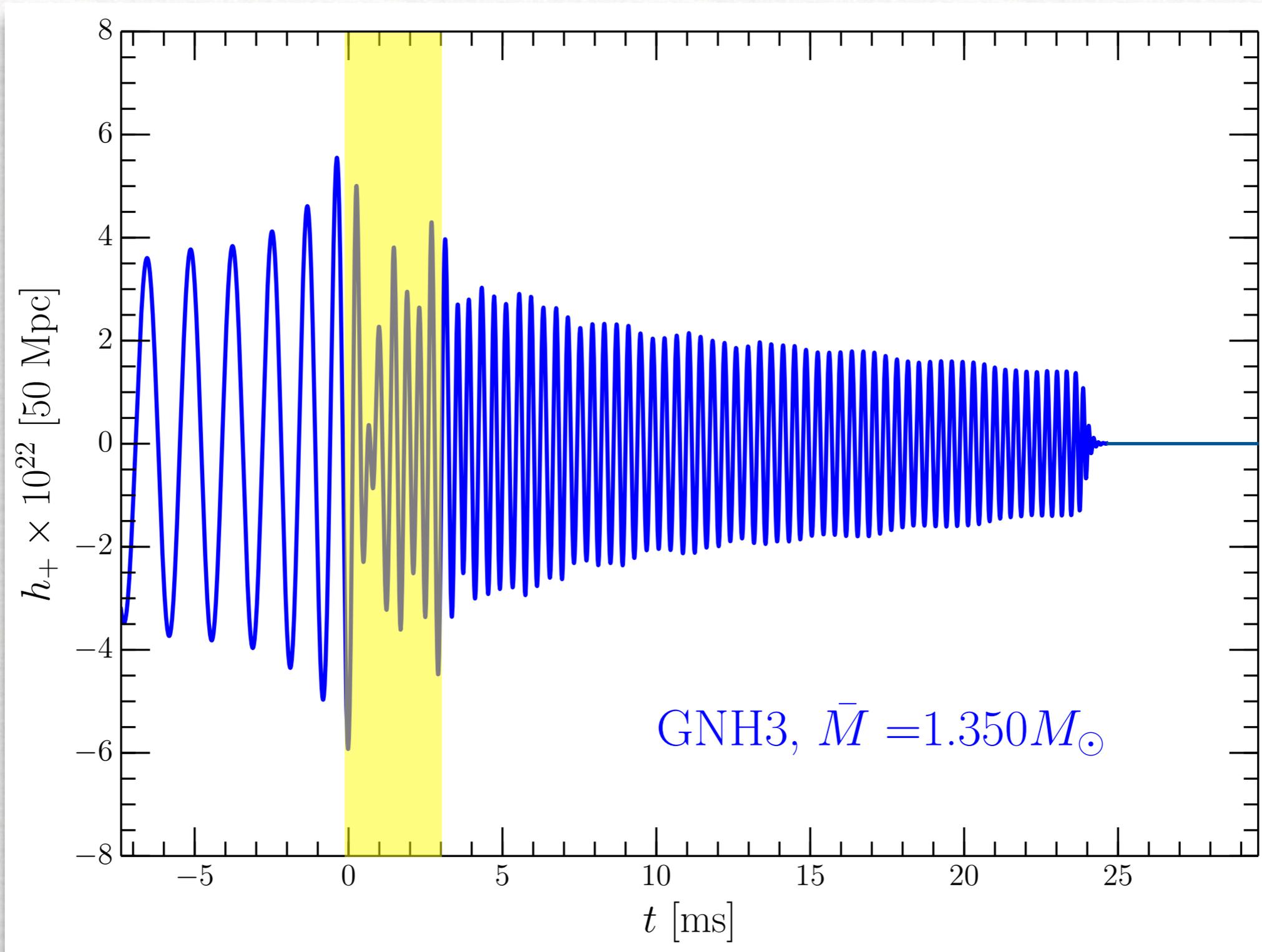


Anatomy of the GW signal **inspiring** BNSM



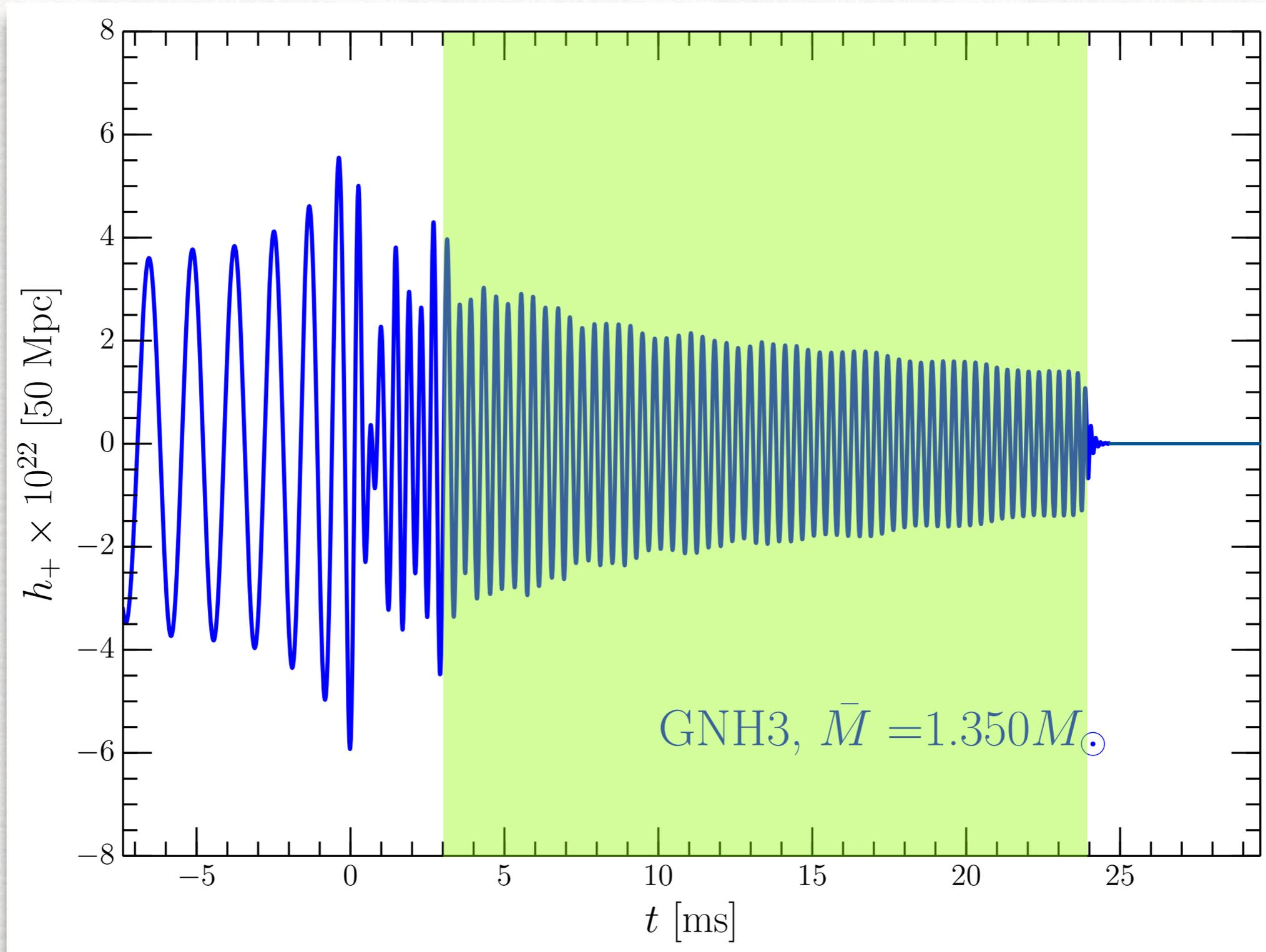
Inspiral: well approximated by PN/EOB; tidal effects important

Anatomy of the GW signal - **Merger**



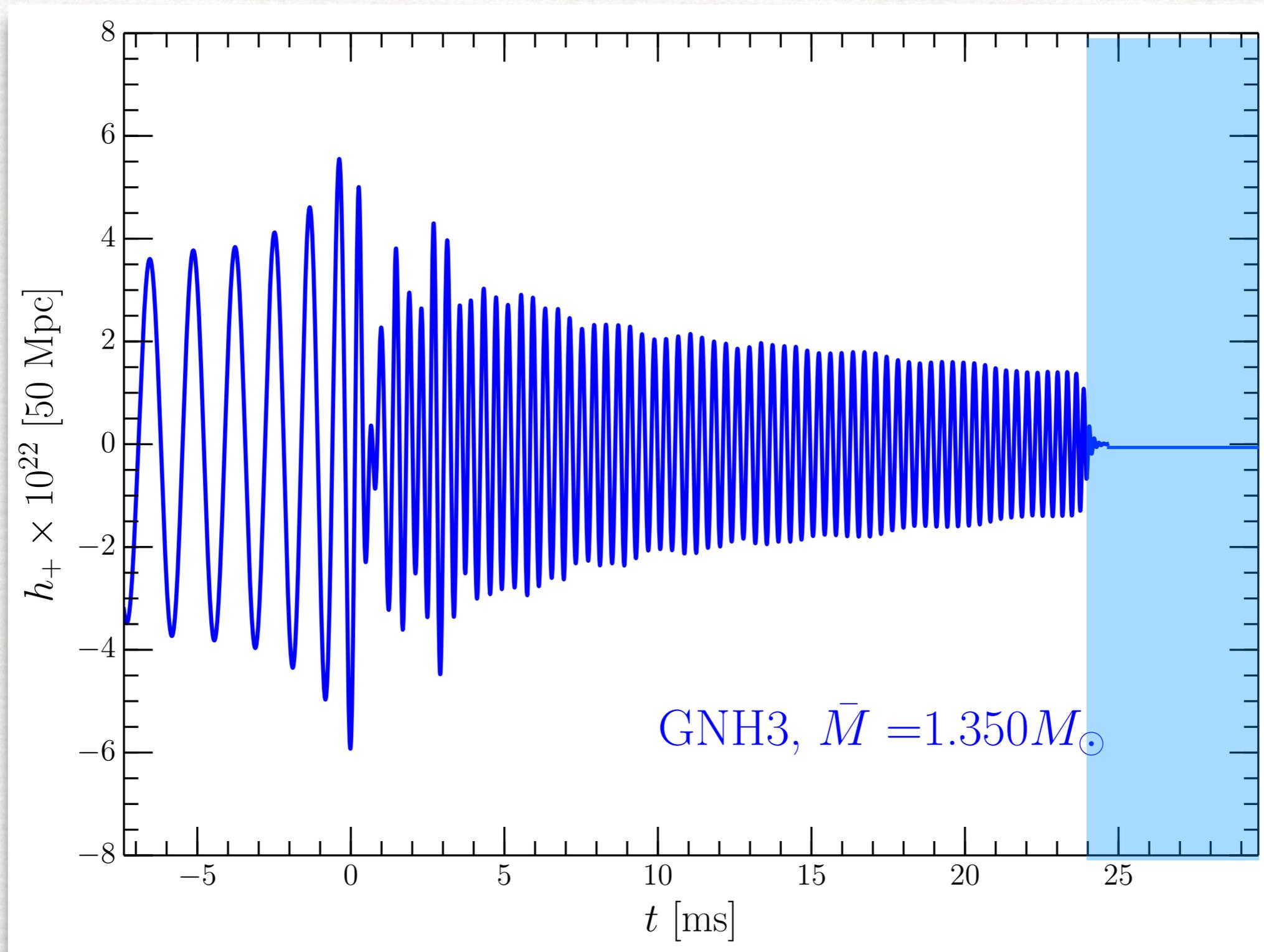
Merger: highly nonlinear but analytic description possible

Anatomy of the GW signal - **post merger**



post-merger: quasi-periodic emission of bar-deformed HMNS

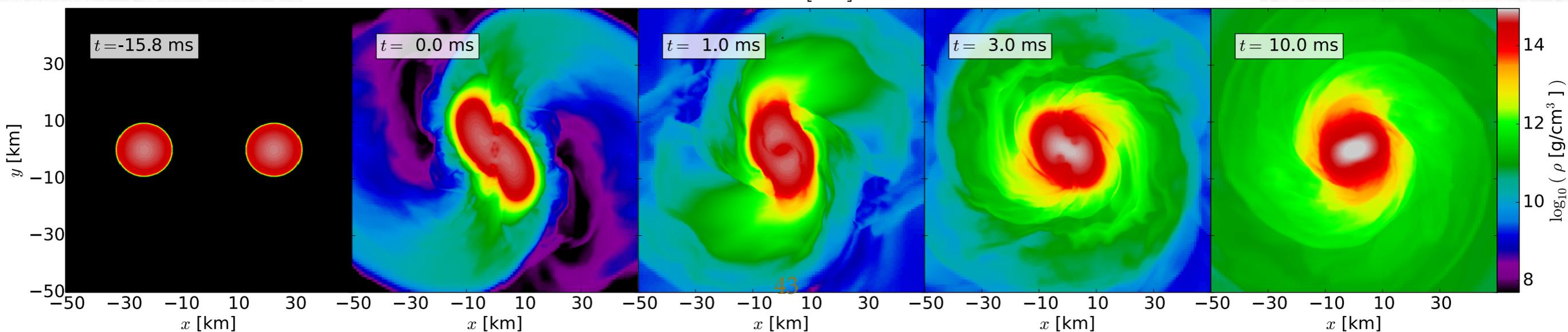
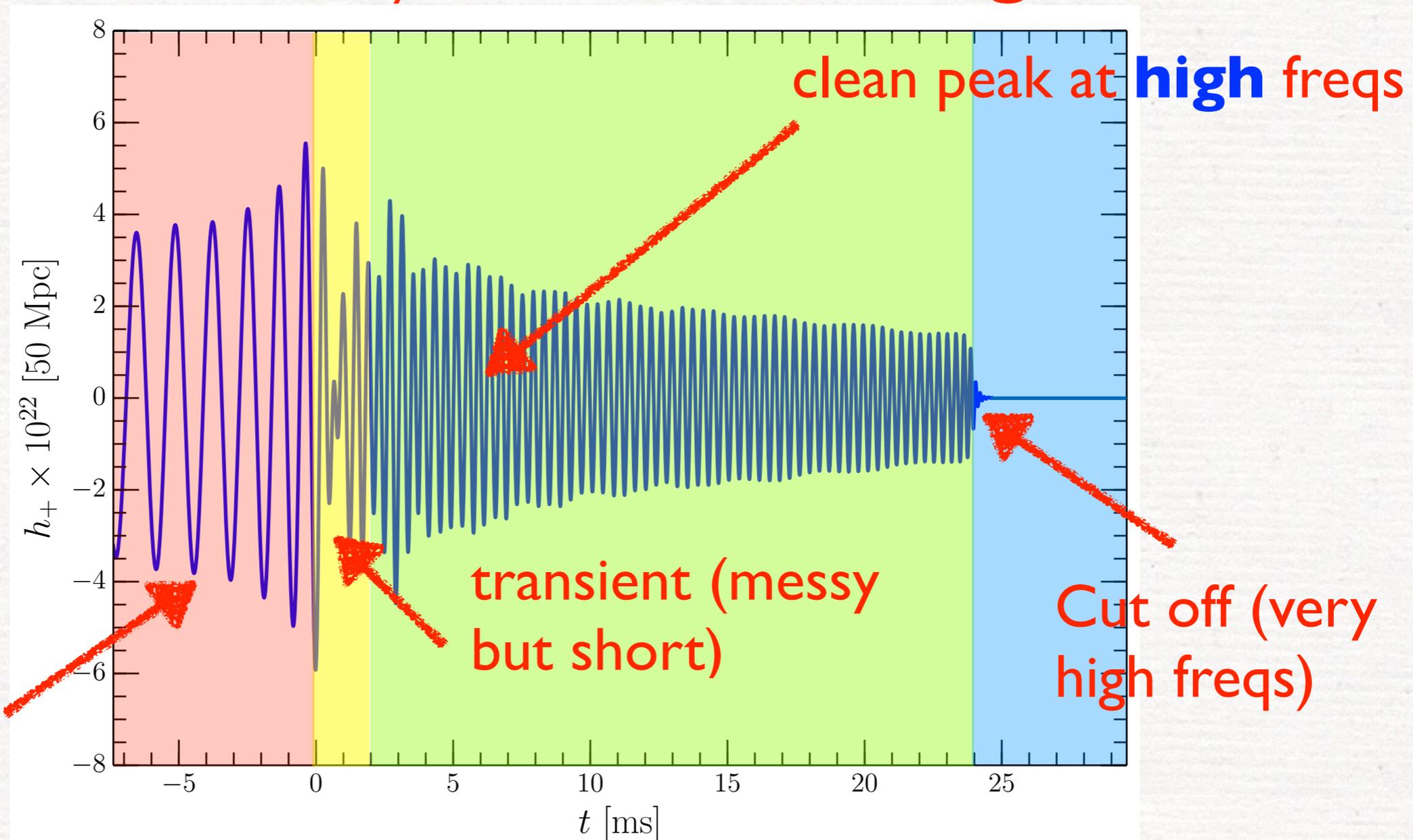
Anatomy of the GW signal > *collapse* > *ringdown* > **BH**



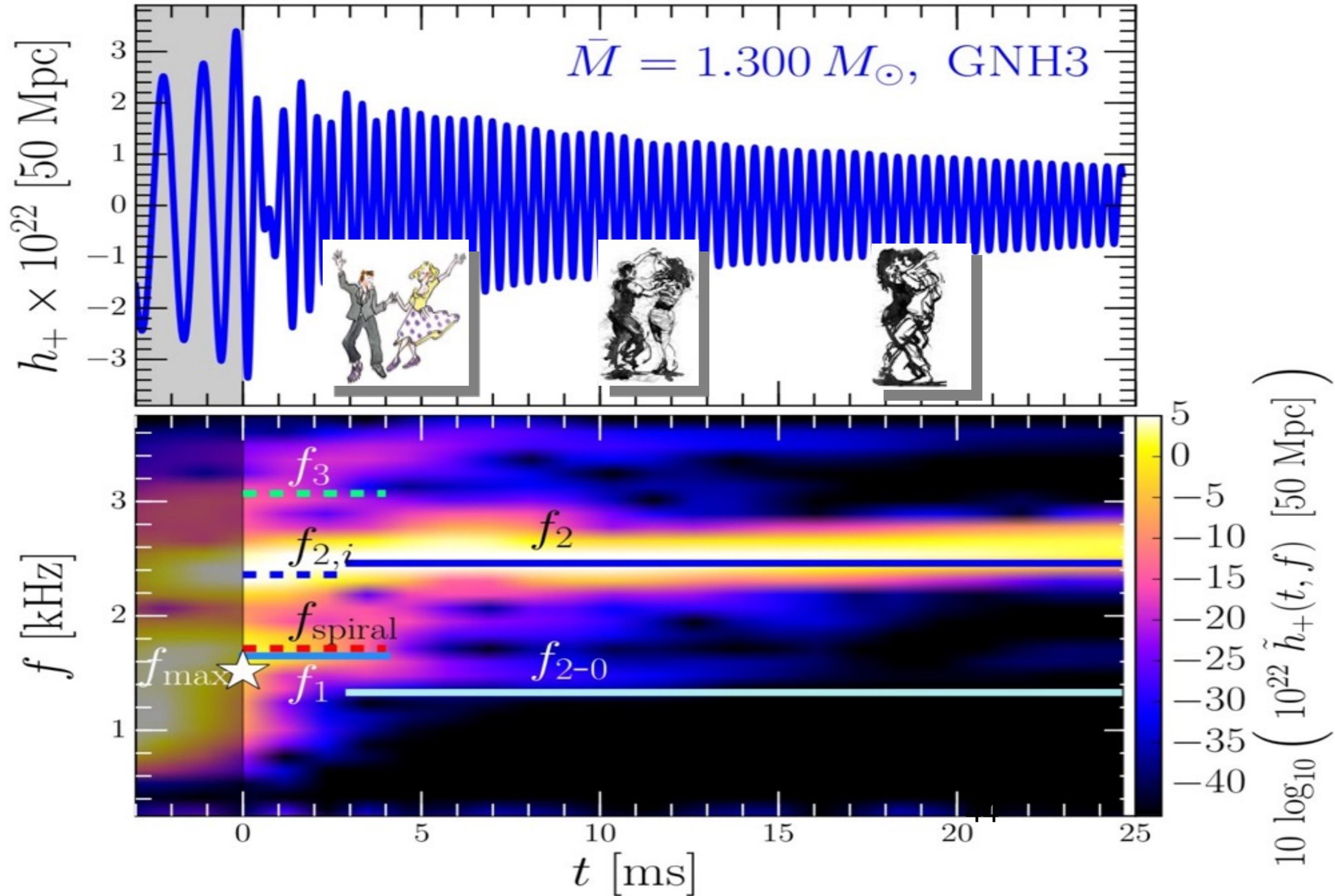
Collapse-ringdown: signal essentially shuts off.

Anatomy of the GW signal

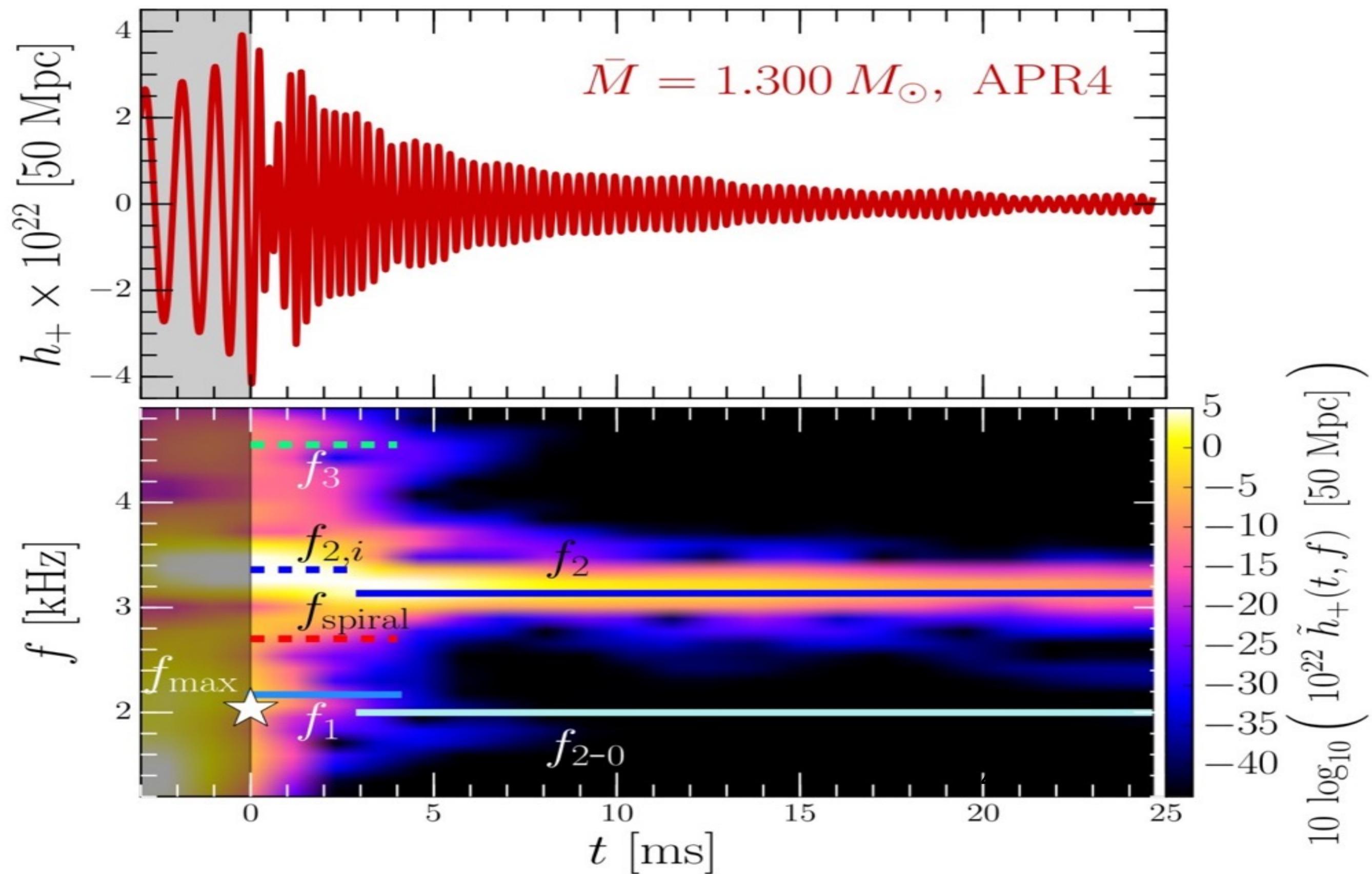
Chirp signal
(track from
low to high
frequencies)



The Gravitational Wave Spectrum for a **HARD** nuclear EoS



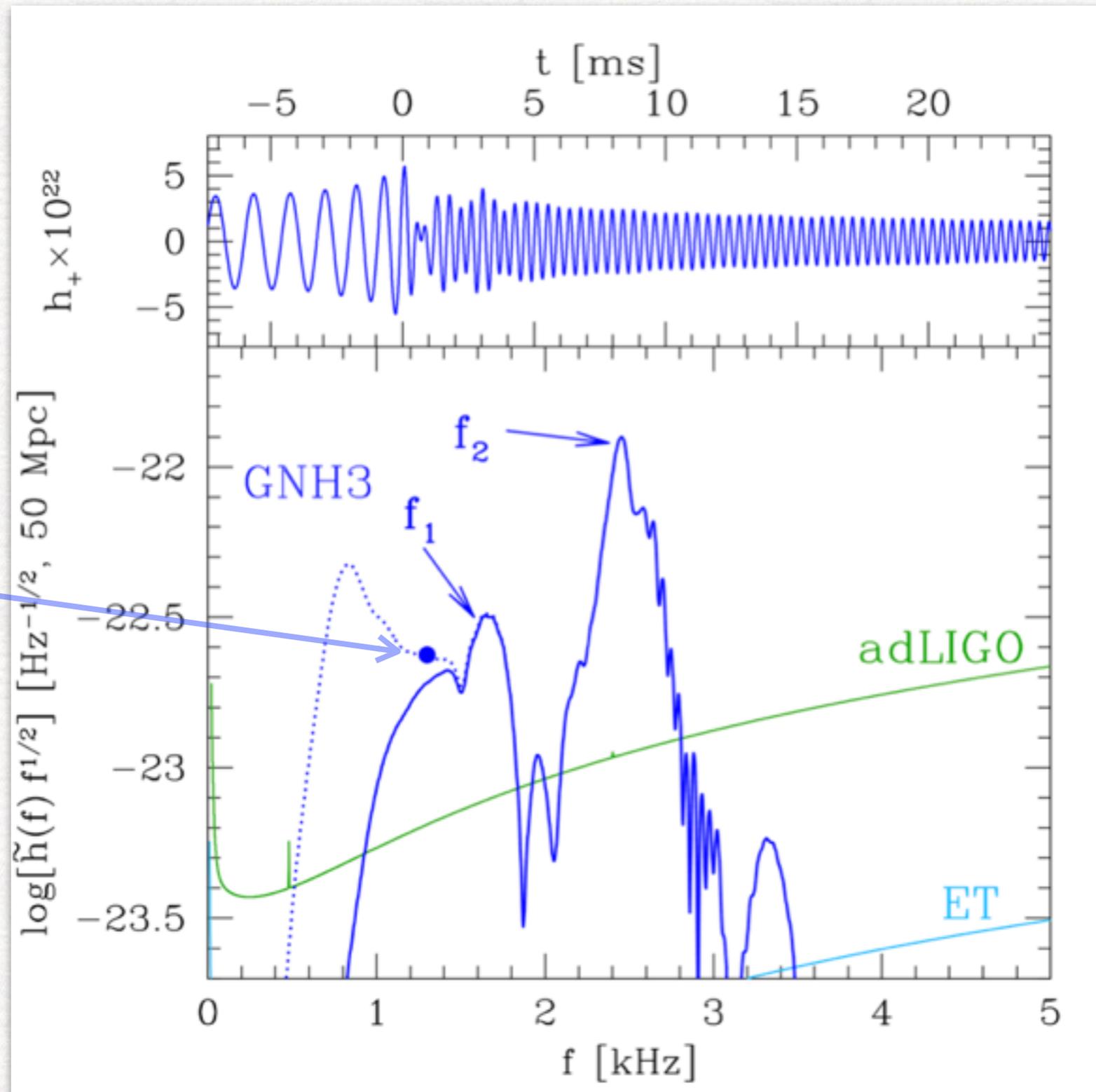
Gravitational Wave Frequency Spectrum: **soft** nuclear matter EoS



A new approach to constrain the EOS

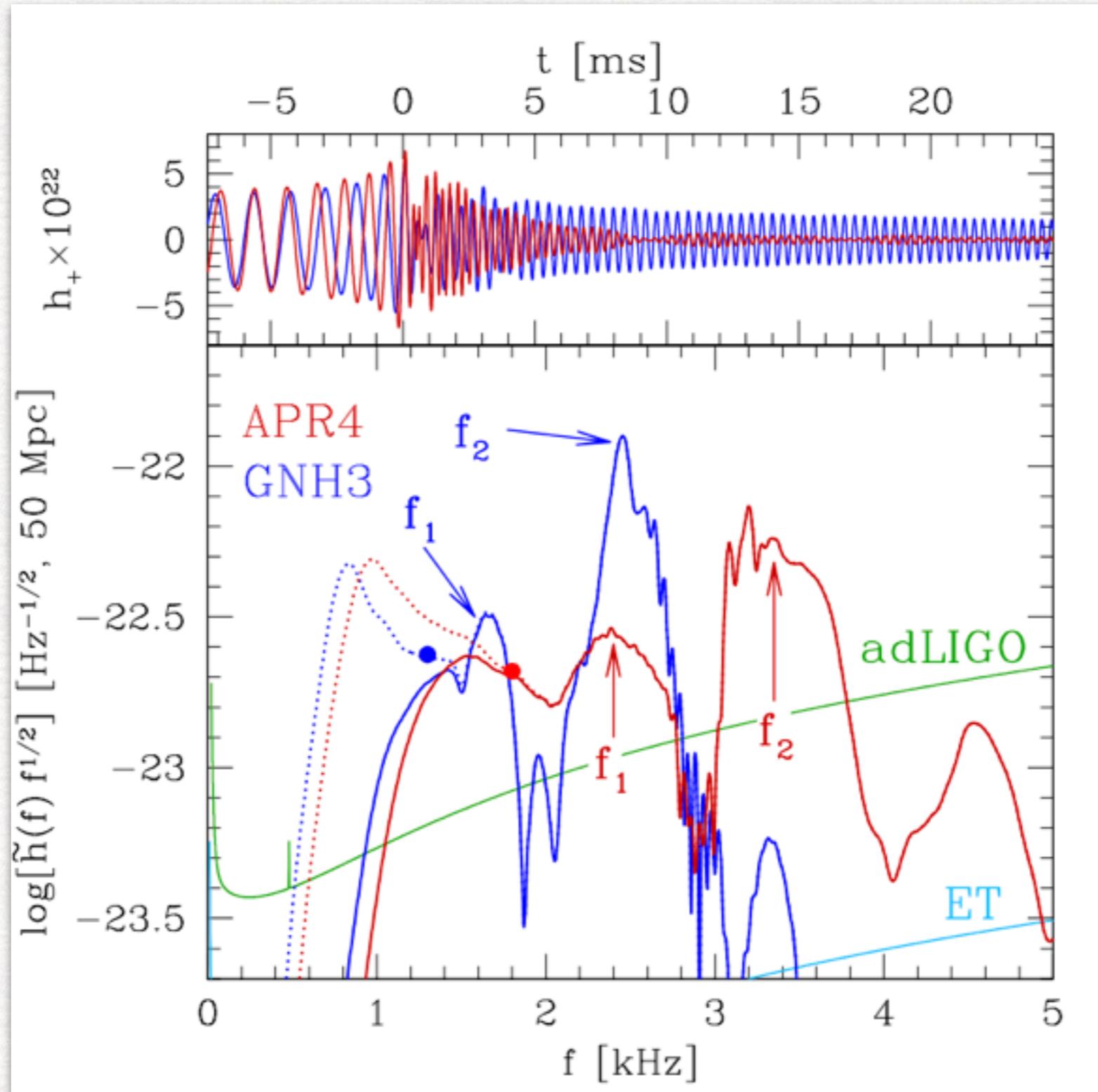
Oechslin+2007, Baiotti+2008, Bauswein+ 2011, 2012, Stergioulas+ 2011, Hotokezaka+ 2013, Takami 2014, 2015, Bernuzzi 2014, 2015, Bauswein+ 2015, LR+2016...

merger
frequency



A new approach to constrain the EOS

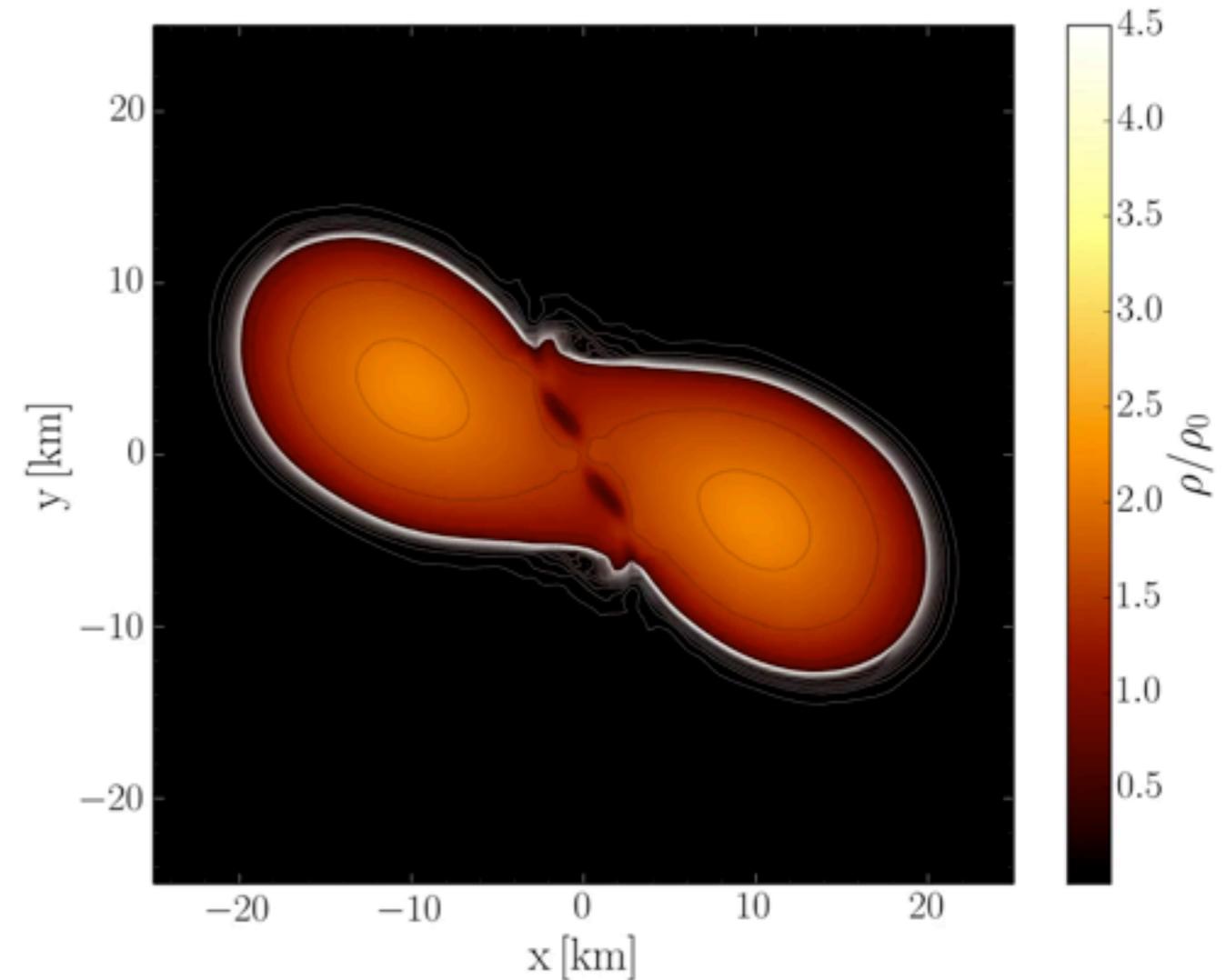
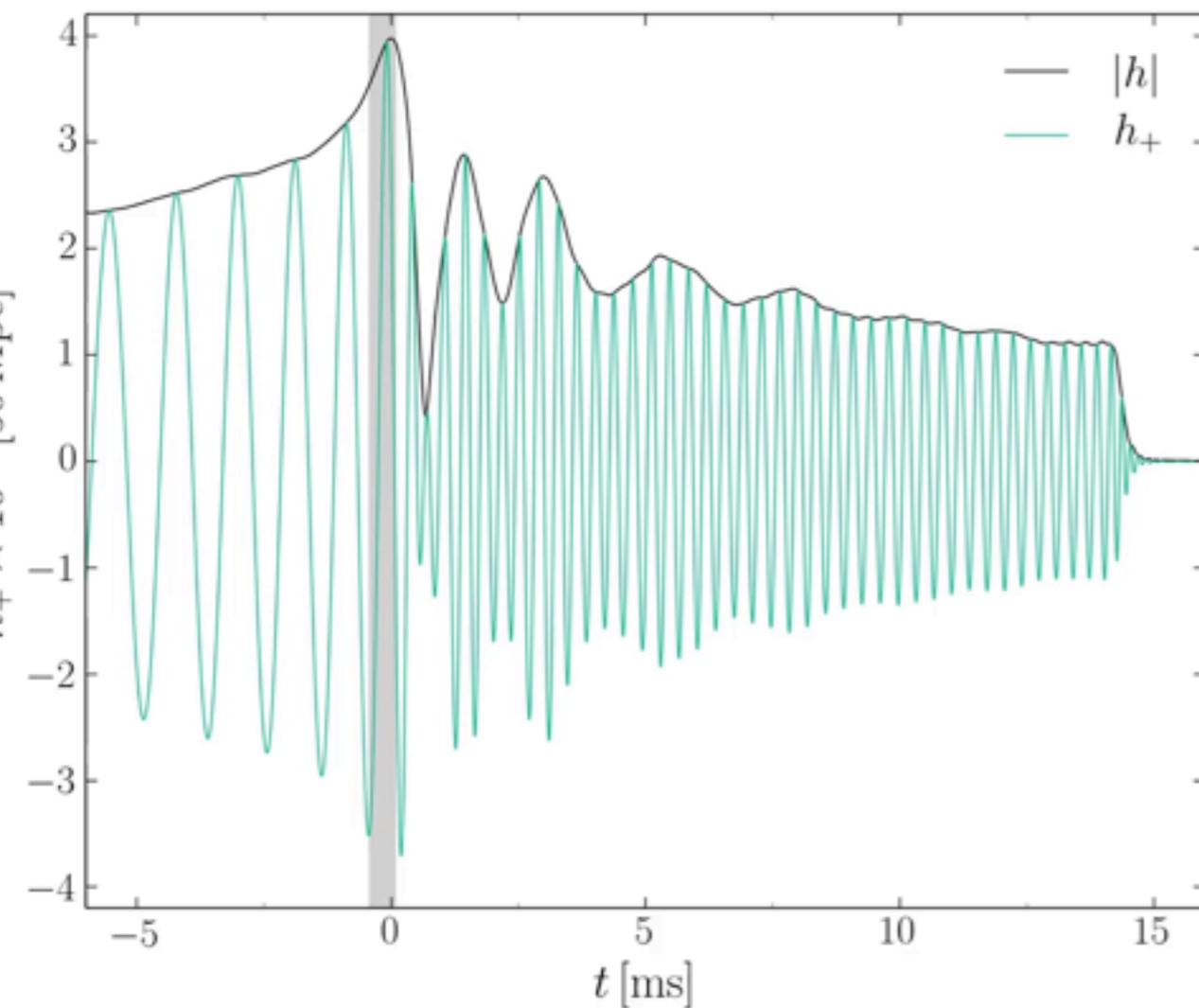
Oechslin+2007, Baiotti+2008, Bauswein+ 2011, 2012, Stergioulas+ 2011, Hotokezaka+ 2013, Takami 2014, 2015, Bernuzzi 2014, 2015, Bauswein+ 2015, LR+2016...



Hypermassive Neutronstar GR Hydro Simulation makes **Quarkmatter**

EoS Contains Neutrons, Protons, Electrons, Hyperons, Muons

Quarkmatter at high net baryon density ($3\rho_0$) ! Each NS: $M = 1.35$ Solar Mass



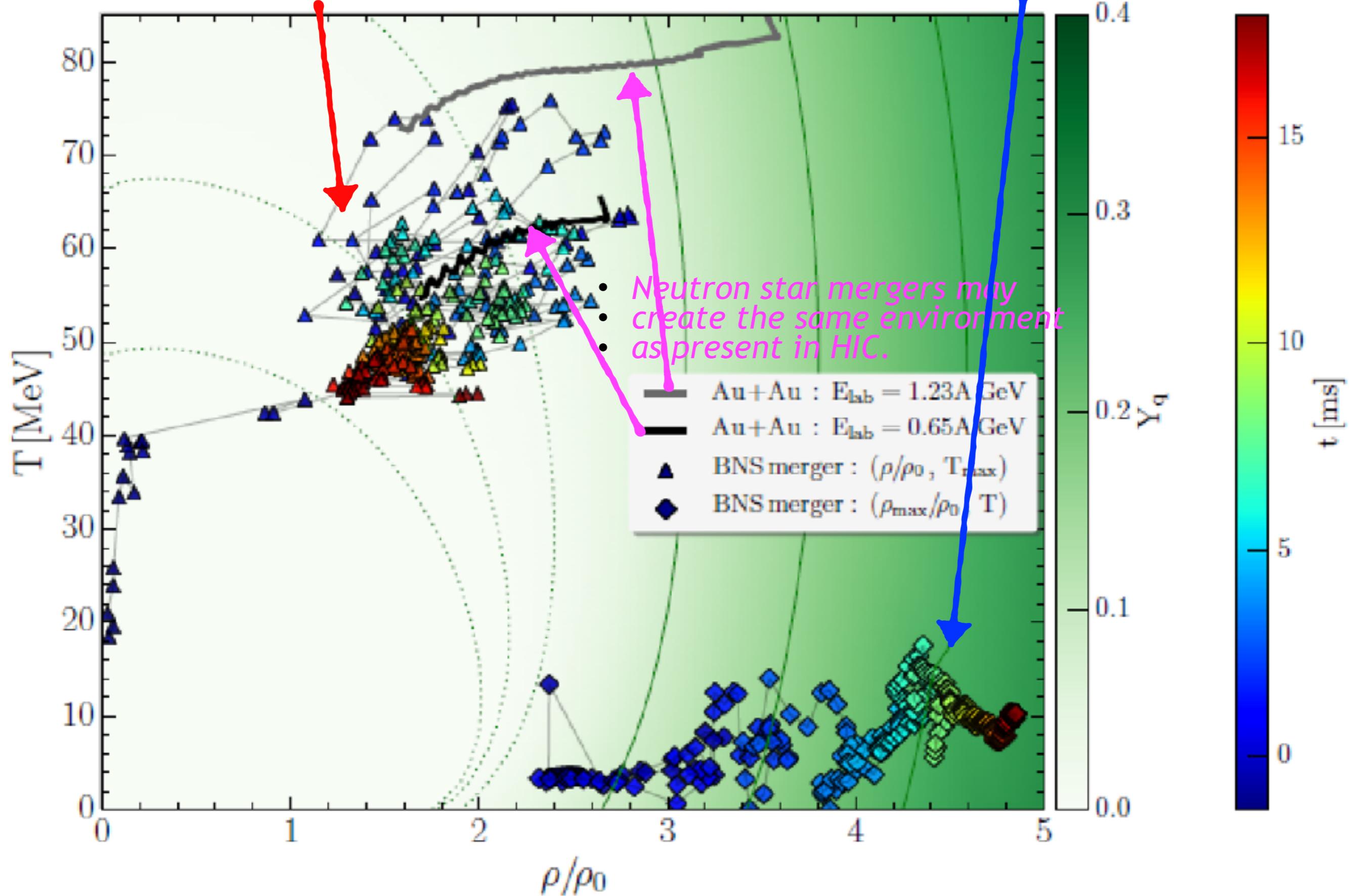
Amplitude der emittierten Gravitationswelle
im Abstand von 50 Mpc

Die Teilchendichte $\rho(x,y)$
in der äquatorialen Ebene in Einheiten der
normalen nuklearen Dichte ρ_0

48

Application of CMF EoS to neutron star mergers

- Separation of **hot hadronic corona** and **dense and cold quark matter core**.



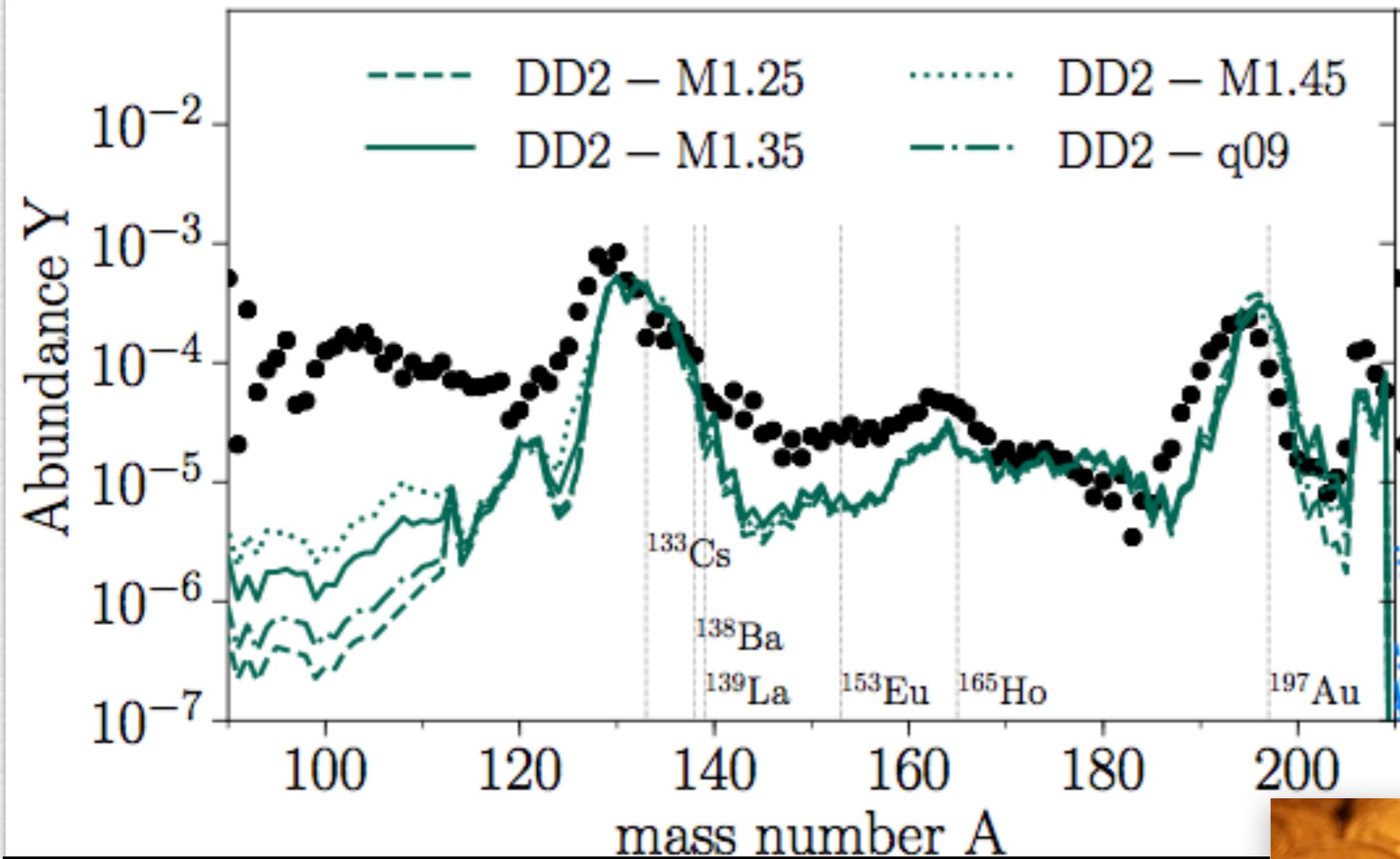
Conclusions

GSFC/NASA



It has happened over and over in the history of astronomy: as a new “window” has been opened, a “new”, universe has been revealed.

GWs will reveal Einstein’s universe⁵⁰ of black holes and neutron stars



Relative Abundance of cosmic elements - Simulation vs. Observation

GW170817 produced lots of **Gold, Platin:** 10x **M_earth!**

Tell our politicians!



The "Death-Star- Machines" FAIR and NICA: Neutron-Star matter by Nuclear Collisions in the Lab

!

Charm and Beauty of International Collaboration



Observers

-
-
-
-



2/27/2018

Austria Czech Hungary

China

Finland

France

Germany

India

Italy

Poland

Slovenia

Spain

Sweden

Romania

Russia

Rosatom

UK