

THE CONCEPT OF AN EXPERIMENT ON MEASURING THE LENGTH OF COHERENT SCATTERING OF NATURAL GADOLINIUM



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Motivation

Gadolinium is known for the fact that its natural isotope mixture possesses a **record-high neutron radiative capture cross-section, which is ~50 000 barns for thermal neutrons**. This makes it suitable to use as an absorber in diffractometers and polarizers, and as a reference layer in neutron reflectometry to determine the modulus and phase of the reflection coefficient of multilayer nanostructures. For the optimal use of this material, a **knowing of the scattering length is important**.

As the literature analysis shows, at the moment **there is no accurate data of this value**:

Authors/year	Method	Wavelength	Re(b), fm
Watanabe N. et al., 1975 [1]	Diffraction	Epithermal neutrons	9.5 ± 0.2
Korneev D. A. et al., 1982 [2]	Reflectometry	1 – 5 Å	18.53
Rauch H. et al., 1985 [3]	Interferometry	1.86 Å	5.1 ± 0.4
Frank A. I. et al., 2002 [4]	Reflectometry	3.5 – 8 Å	11.5 ± 0.7
Nikova E.S. et al., 2019 [5]	Transmission	0.6 – 9 Å	7.6

Measuring the scattering length for gadolinium is associated with significant difficulties. Natural gadolinium consists of a mixture of six stable isotopes, two of which – ¹⁵⁵Gd and ¹⁵⁷Gd – **have resonances of neutron capture cross-section in thermal region**.

Due to the presence of these resonances, its scattering length has strong dependence on energy of neutrons and is not a constant value. In such a case, it is necessary to **use the Breit-Wigner formula** for calculations:

$$b_{coh} = b_0 + \sum \frac{2\lambda_j \Gamma_{nj} (E - E_j)}{4(E - E_j)^2 + \Gamma_j^2} + i \sum \frac{\lambda_j \Gamma_{nj} \Gamma_j}{4(E - E_j)^2 + \Gamma_j^2},$$

where **b₀** is the constant part of the scattering length, λ is the reduced wavelength, Γ_j and Γ_{nj} are the total and neutron widths of the j -th resonance, and E_j is the energy at which the j -th resonance occurs.

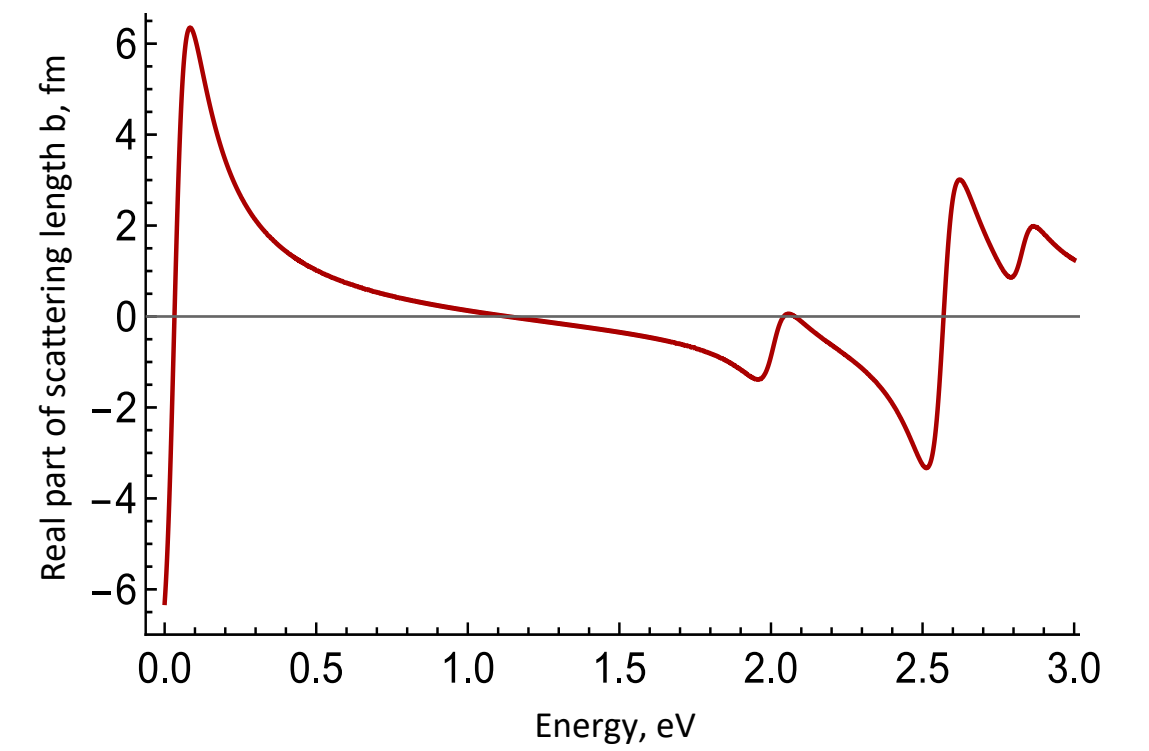


Fig. 1: Dependence of the real part of gadolinium scattering length on energy.

Systematic analysis of the previous experiment [4]

Since gadolinium is actively oxidized in air, it is necessary to use a protective coating. In the experiment [4], a thin layer of titanium was used as such a coating. Measurements were done at the TOF reflectometer REFLEX (FLNP JINR). Experimental reflection curves were compared by theoretical calculations in which the variable parameter was the constant part of the scattering length.

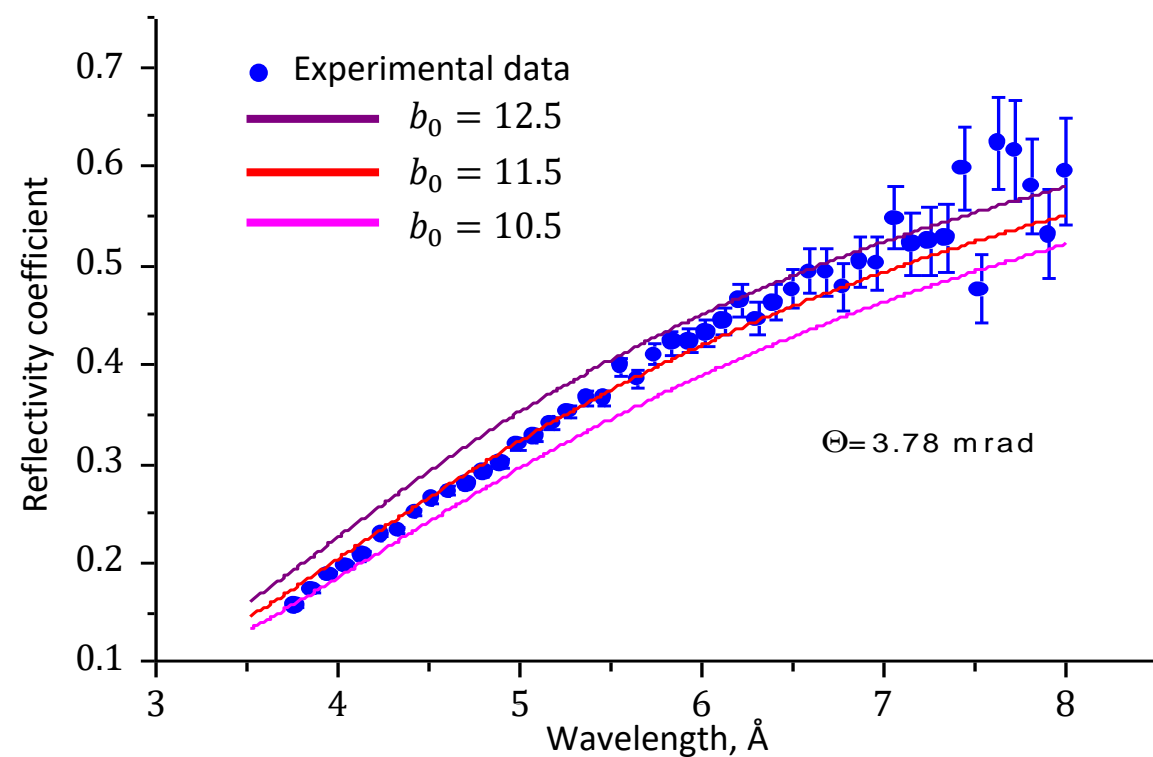


Fig. 2: Comparison of experimental and theoretical curves at three values of the constant part of the scattering length [4]

The agreement of the theory with the experiment was not complete. The discrepancy between the empirical and calculated curves is clearly seen. One of the main hypotheses is the **unknown oxidation depth of the titanium protective layer**.

To analyze the role of titanium oxide the calculations from the article [4] were reproduced, considering three scenarios: a fully oxidized titanium layer, one oxidized to half of its thickness, and a non-oxidized layer.

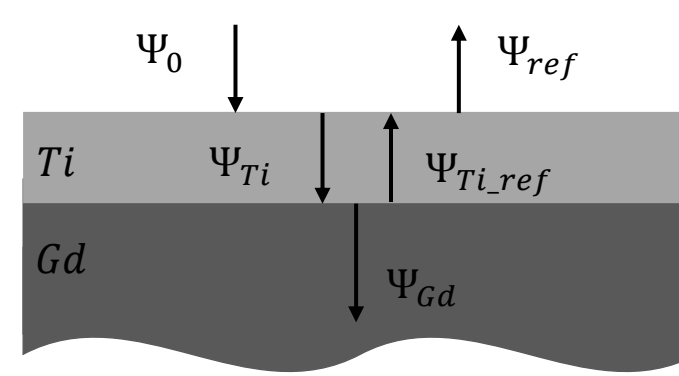


Fig. 3: Scheme of the Ti-Gd structure. The TiO₂-Gd structure appears the same.

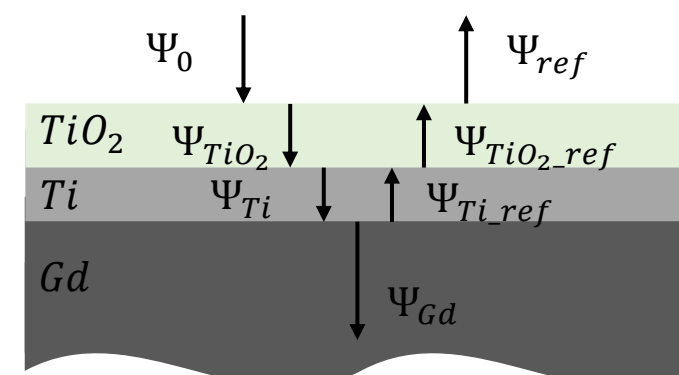


Fig. 4: Scheme of the TiO₂-Ti-Gd structure.

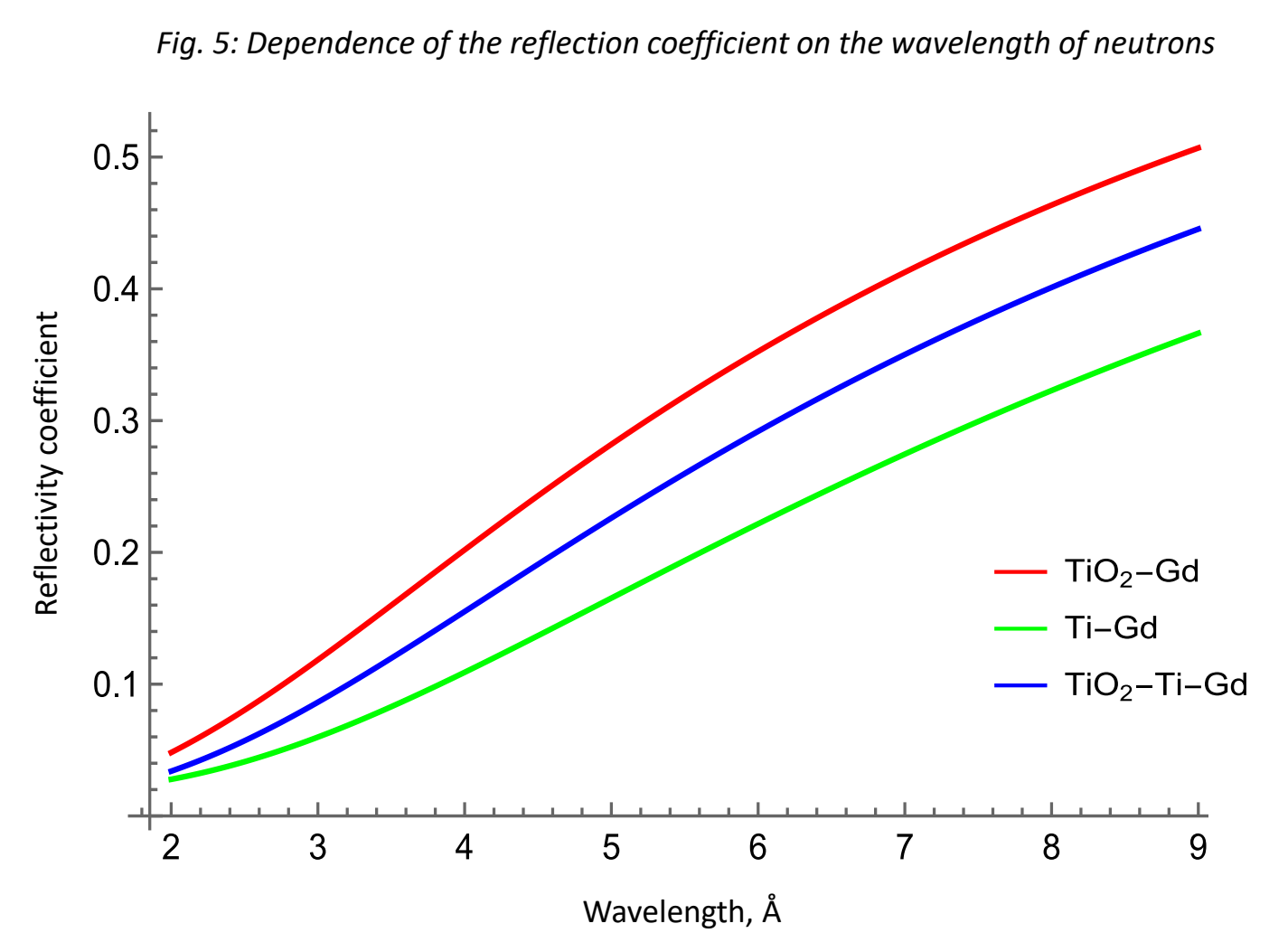


Fig. 5: Dependence of the reflection coefficient on the wavelength of neutrons

Presence of the oxide in the surface layer significantly affects the value of the reflection coefficient!

Possible new experiment

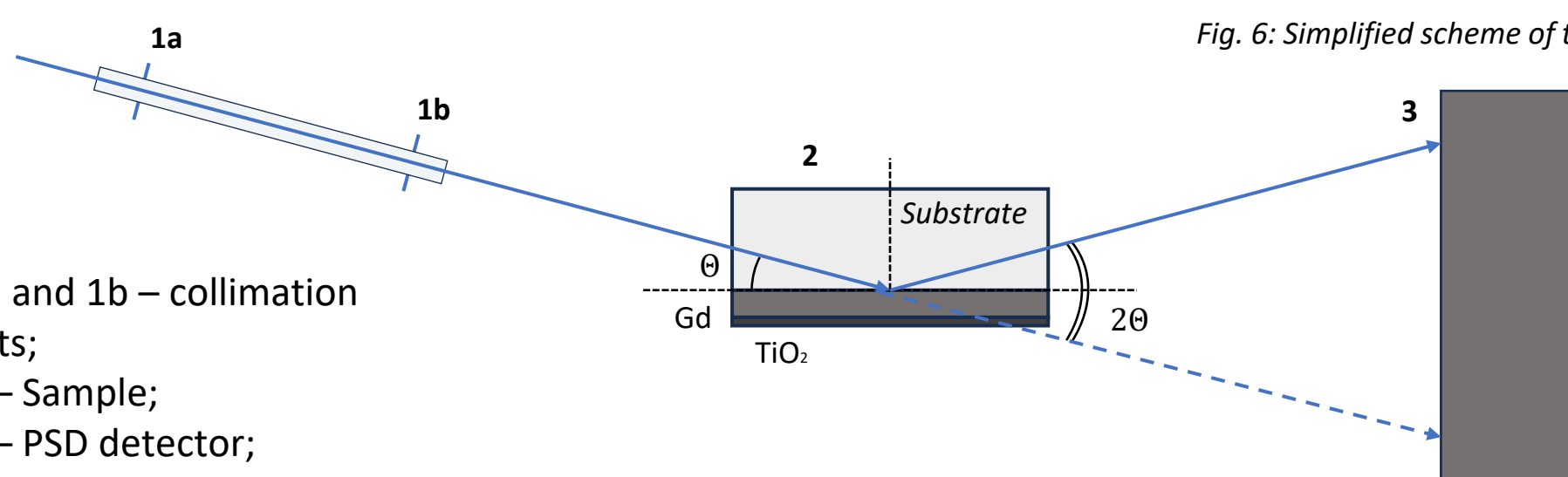


Fig. 6: Simplified scheme of the experiment.

1a and 1b – collimation slits;
2 – Sample;
3 – PSD detector;

The main difference between the planned experiment and the previous one is the use of the so-called **"inverse" geometry**: neutrons will fall on gadolinium through a glass substrate.

This approach has several advantages:

- neutron beam is directed to the Gd through a glass substrate, which is weakly interacts with thermal neutrons, and therefore can be considered transparent;
- such a structure has only one glass-gadolinium interface, which greatly simplifies the calculations.

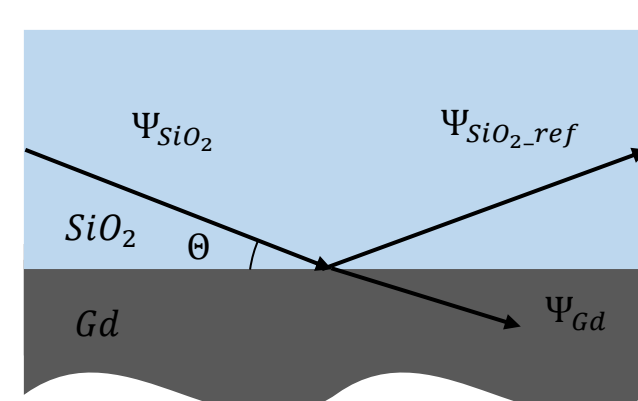


Fig. 7: Scheme of the SiO₂-Gd structure.

The experiment is planned to be carried out at one of the **reflectometers of the IBR-2 reactor of the FLNP JINR**.

Parameters in Breit-Wigner formula, with the exception of b_0 , were taken from the ENDF nuclear data library [6]. The constant part of the scattering length b_0 is a **variable parameter**.

The **number of resonances** in the radiation capture cross-section of gadolinium is **~200 for ¹⁵⁵Gd and ~90 for ¹⁵⁷Gd**. However, not all of these resonances significantly affect. After sorting, the number of resonances taking into account was significantly **reduced to ~80 for ¹⁵⁵Gd and ~20 for ¹⁵⁷Gd**. The contribution from other resonances will simply be an addition to the constant part of the scattering length b_0 .

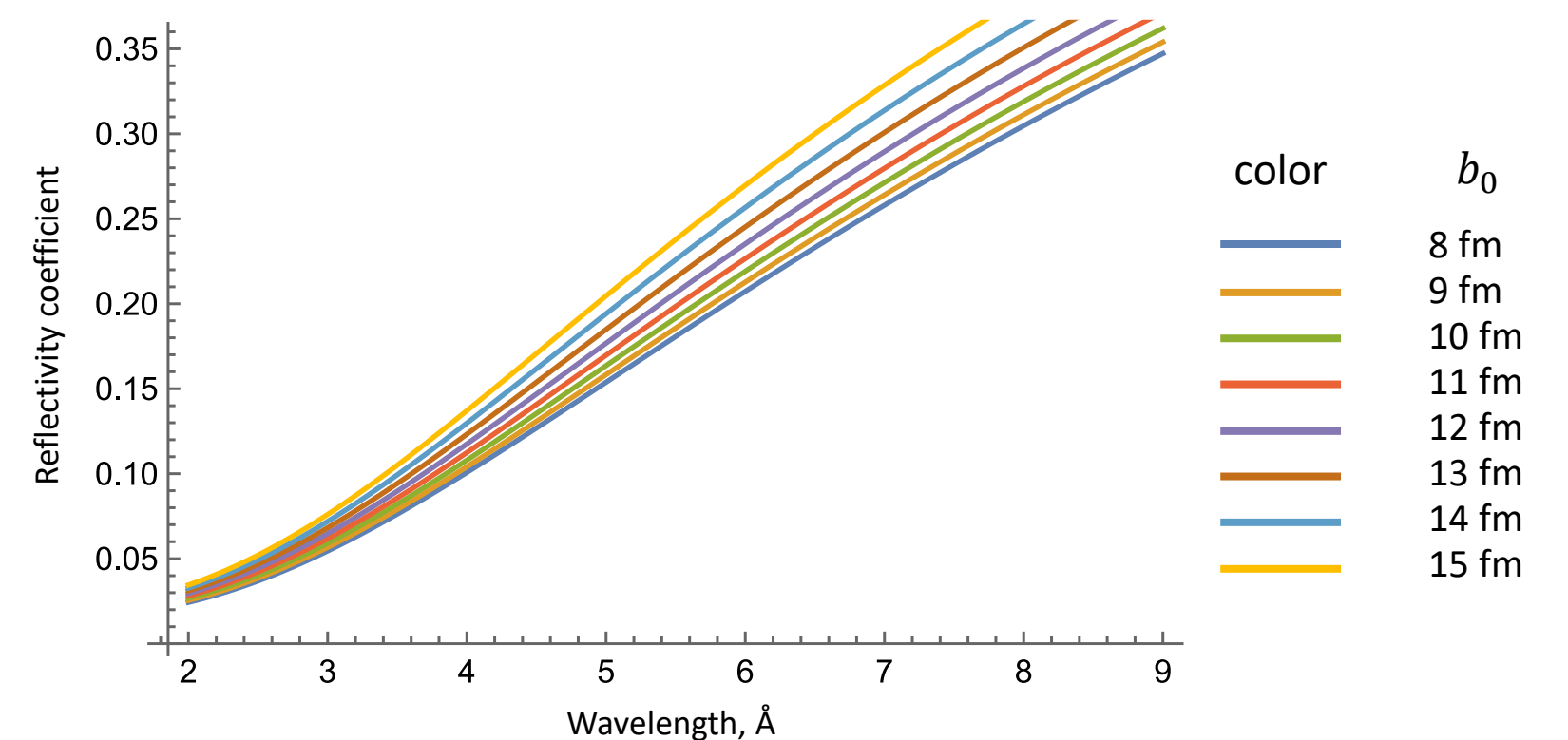


Fig. 8: Dependence of the reflection coefficient on the wavelength.

- [1] Watanabe N., Ishikawa Y., Takei K., Suzuki H. Kakuriken Kenkyu Hokoku, Vol. 8, №2 (1975) p. 302-308
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 [6] Koning A.J., Rochman D., Sublet J.-Ch. et al. Nuclear Data Sheets, Vol. 155 (2019) p. 1-55