Axionlike particles search using diatomic molecules

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EDM predictions



*A. Boeschoten et al., arXiv:2303.06402 (2023) Compiled by D. DeMille

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Reinterpretation of BaF experiment

 $\mathcal{T}\text{,}\mathcal{P}\text{-violating energy shift}$

$$\delta E = d_{\rm e} \Omega W_d \approx 8 \ \mu {
m Hz}$$

where $E_{
m eff} = W_d |\Omega| pprox 1.565 \cdot 10^{24}$ Hz/(e·cm)

Reinterpretation in terms of ALPs

$$V_{eN}(\mathbf{r}) = +i\frac{g_N^s g_e^p}{4\pi} \frac{e^{-m_a |\mathbf{r} - \mathbf{R}|}}{|\mathbf{r} - \mathbf{R}|} \gamma_0 \gamma_5 \qquad V_{ee}(\mathbf{r}_1, \mathbf{r}_2) = +i\frac{g_e^s g_e^p}{4\pi} \frac{e^{-m_a |\mathbf{r}_1 - \mathbf{r}_2|}}{|\mathbf{r}_1 - \mathbf{r}_2|} \gamma_0 \gamma_5$$
$$W_{ax}^{(eN)}(m_a) = \frac{1}{\Omega} \frac{1}{g_N^s g_e^p} \langle \Psi | \sum_{i=1}^{N_e} V_{eN}(\mathbf{r}_i) | \Psi \rangle \qquad W_{ax}^{(ee)}(m_a) = \frac{1}{\Omega} \frac{1}{g_e^s g_e^p} \langle \Psi | \sum_{i,j=1}^{N_e} V_{ee}(\mathbf{r}_i, \mathbf{r}_j) | \Psi \rangle$$
$$\delta E = g_e^s g_e^p \Omega W_{ax}^{(eN)}(m_a) \qquad \delta E = g_e^s g_e^p \Omega W_{ax}^{(ee)}(m_a)$$

Stadnik, Y. V., Dzuba, V. A., Flambaum, V. V. (2018), Phys. rev. lett., 120(1), 013202.

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Integrals

Standard Coulumb interaction integrals

$$\langle ab|rac{1}{r_{12}}|cd
angle
ightarrow F_m(T) = \int_0^1 dt t^{2m} e^{-Tt^2}$$

a, b, c, d are primitive Gaussian-type basis functions $x^n y^m z^k e^{-\beta r^2}$

Yukawa interaction integrals

$$\langle ab|rac{e^{-m_a r_{12}}}{r_{12}}|cd
angle o G_m(T,U) = \int_0^1 dt t^{2m} e^{-Tt^2 + U(1-rac{1}{t^2})}$$

Implemented in LIBINT library!

Default approach

• $0 \leq \mathcal{T} \leq 2^{10}$ and $10^{-7} \leq \mathcal{U} \leq 10^3 \rightarrow$ Gaussian quadrature

precalculated values of the Chebyshev expansion coefficients of the positions and weights of the grid points are used

• $T>2^{10}$ or $U<10^{-7}$ ightarrow upward recursive relations

$$G_{-1} = \frac{e^{-T}}{4} \sqrt{\frac{\pi}{U}} \left[e^{k^2} \operatorname{erfc}(k) + e^{\lambda^2} \operatorname{erfc}(\lambda) \right],$$

$$G_0 = \frac{e^{-T}}{4} \sqrt{\frac{\pi}{T}} \left[e^{k^2} \operatorname{erfc}(k) - e^{\lambda^2} \operatorname{erfc}(\lambda) \right],$$

where $k = -\sqrt{T} + \sqrt{U}, \ \lambda = \sqrt{T} + \sqrt{U}.$

All the remaining G_m values are obtained using the recurrence relations

$$G_m = \frac{1}{2T}[(2m-1)G_{m-1} + 2UG_{m-2} - e^{-T}].$$

Modifications

• T=0 and $U<10^{-7}$

The first element of relations is

$$G_0 = 1 - e^U \sqrt{\pi U} \operatorname{erfc}(\sqrt{U}),$$

All the remaining G_m values are obtained using the recurrence relations

$$G_m(0, U) = \frac{1}{2m+1}[1-2UG_{m-1}(0, U)].$$

• T < 0.1 and $U < 10^{-7}$

$$G_m(T, U) = \sum_{k=0}^{\infty} \frac{(-T)^k}{k!} G_{m+k}(0, U),$$

Calculated $W^{(ee)}_{\rm ax}(m_a)$ and derived limits on $|g^s_e g^p_e|$ for BaF

<i>m</i> _a , eV	$m{W}_{ m ax}^{(ee)}(m{m_a})$, $m{m_e}m{c}/\hbar$			$ g_e^s g_e^p $
	DHF	CCSD	CCSD(T) (Final)	Limit, $\hbar c$
1	$+6.3\cdot10^{-6}$	$+8.1\cdot10^{-6}$	$+8.0 \cdot 10^{-6}$	$+1.6 \cdot 10^{-20}$
10	$+6.3 \cdot 10^{-6}$	$+8.1 \cdot 10^{-6}$	$+8.0\cdot 10^{-6}$	$+1.6 \cdot 10^{-20}$
10 ²	$+6.3 \cdot 10^{-6}$	$+8.1 \cdot 10^{-6}$	$+8.0 \cdot 10^{-6}$	$+1.6 \cdot 10^{-20}$
10 ³	$+4.8 \cdot 10^{-6}$	$+6.6\cdot10^{-6}$	$+6.5 \cdot 10^{-6}$	$+1.9 \cdot 10^{-20}$
104	$+1.2 \cdot 10^{-6}$	$+2.0 \cdot 10^{-6}$	$+2.0 \cdot 10^{-6}$	$+6.5 \cdot 10^{-20}$
10 ⁵	$+9.3\cdot10^{-8}$	$+1.4 \cdot 10^{-7}$	$+1.4 \cdot 10^{-7}$	$+9.2 \cdot 10^{-19}$
10 ⁶	$-3.3\cdot10^{-9}$	$-5.2\cdot10^{-9}$	$-5.1\cdot10^{-9}$	$+2.5 \cdot 10^{-17}$
107	$-5.1\cdot10^{-11}$	$-8.0\cdot10^{-11}$	$-7.8 \cdot 10^{-11}$	$+1.6 \cdot 10^{-15}$
10 ⁸	$-5.1\cdot10^{-13}$	$-8.0\cdot10^{-13}$	$-7.9 \cdot 10^{-13}$	$+1.6 \cdot 10^{-13}$
10 ⁹	$-5.1\cdot10^{-15}$	$-8.0\cdot10^{-15}$	$-7.9\cdot10^{-15}$	$+1.6 \cdot 10^{-11}$
10 ¹⁰	$-5.1\cdot10^{-17}$	$-8.1\cdot10^{-17}$	$-7.9 \cdot 10^{-17}$	$+1.6\cdot10^{-9}$

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Calculated $W^{(eN)}_{\rm ax}(m_a)$ and derived limits on $|\bar{g}^s_N g^p_e|$ for BaF

m _a , eV	$W^{(eN)}_{ m ax}(m_a)$, m_ec/\hbar		$W^{(eN)}_{ m ax}(m_a)$, m_ec/\hbar	$ ar{m{g}}^s_Nm{g}^p_e $
	Point	Correction, %	Finite	Limit, $\hbar c$
1	$+1.74 \cdot 10^{-5}$	0.0	$+1.74 \cdot 10^{-5}$	$+7.29 \cdot 10^{-21}$
10	$+1.74 \cdot 10^{-5}$	0.0	$+1.74 \cdot 10^{-5}$	$+7.29 \cdot 10^{-21}$
10 ²	$+1.73 \cdot 10^{-5}$	0.0	$+1.73 \cdot 10^{-5}$	$+7.31 \cdot 10^{-21}$
10 ³	$+1.45 \cdot 10^{-5}$	0.0	$+1.45 \cdot 10^{-5}$	$+8.71 \cdot 10^{-21}$
104	$+1.86 \cdot 10^{-6}$	0.0	$+1.86 \cdot 10^{-6}$	$+6.81\cdot 10^{-21}$
10 ⁵	$-1.07 \cdot 10^{-5}$	0.0	$-1.07 \cdot 10^{-5}$	$+1.18\cdot 10^{-20}$
10 ⁶	$-4.70 \cdot 10^{-6}$	0.0	$-4.70 \cdot 10^{-6}$	$+2.69 \cdot 10^{-20}$
10 ⁷	$-1.36 \cdot 10^{-7}$	-0.4	$-1.36 \cdot 10^{-7}$	$+9.34\cdot 10^{-19}$
10 ⁸	$-1.99\cdot10^{-9}$	-4.0	$-1.91\cdot10^{-9}$	$+6.65\cdot10^{-17}$
10 ⁹	$-2.09\cdot10^{-11}$	-5.6	$-1.97\cdot10^{-11}$	$+6.43 \cdot 10^{-15}$
10 ¹⁰	$-2.09 \cdot 10^{-13}$	-5.6	$-1.97 \cdot 10^{-13}$	$+6.43 \cdot 10^{-13}$

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Calculated $W^{(eN)}_{\rm ax}(m_a)$ and derived limits on $|\bar{g}^s_N g^p_e|$ for HfF⁺

m _a , eV	$W^{(eN)}_{ m ax}(m_a)$, m_ec/\hbar		$W^{(eN)}_{ m ax}(m_a)$, m_ec/\hbar	$ ar{m{g}}^s_Nm{g}^p_e $
	Point	Correction, %	Finite	Limit, $\hbar c$
1	$+1.67 \cdot 10^{-5}$	0	$+1.67 \cdot 10^{-5}$	$1.11\cdot10^{-20}$
10	$+1.67 \cdot 10^{-5}$	0	$+1.67 \cdot 10^{-5}$	$1.11\cdot 10^{-20}$
10 ²	$+1.66 \cdot 10^{-5}$	0	$+1.66 \cdot 10^{-5}$	$1.11\cdot 10^{-20}$
10 ³	$+1.54 \cdot 10^{-5}$	0	$+1.54 \cdot 10^{-5}$	$1.19\cdot 10^{-20}$
104	$+3.30 \cdot 10^{-6}$	0	$+3.31 \cdot 10^{-6}$	$5.24\cdot10^{-20}$
10 ⁵	$-1.15\cdot10^{-5}$	0	$-1.15\cdot10^{-5}$	$1.67\cdot 10^{-20}$
10 ⁶	$-6.41 \cdot 10^{-6}$	0	$-6.41 \cdot 10^{-6}$	$2.97\cdot 10^{-20}$
10 ⁷	$-2.85 \cdot 10^{-7}$	-1	$-2.82 \cdot 10^{-7}$	$6.74\cdot10^{-19}$
10 ⁸	$-5.30\cdot10^{-9}$	-9	$-4.81 \cdot 10^{-9}$	$3.95\cdot10^{-17}$
10 ⁹	$-5.85\cdot10^{-11}$	-13	$-5.09\cdot10^{-11}$	$3.73\cdot10^{-15}$
10 ¹⁰	$-5.87 \cdot 10^{-13}$	-13	$-5.10 \cdot 10^{-13}$	$3.73\cdot 10^{-13}$

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Radius of Yukawa-type interaction

 $R_{
m Yu} = 1/m_a ({
m relativistic units}) = \hbar/m_a c$

Low-mass limit

1 Bohr $\longleftrightarrow m_a \approx 4$ keV $\Rightarrow \frac{e^{-m_a r}}{4\pi r} \approx \frac{1}{4\pi r} \Rightarrow W_{ax}(m_a) \approx constant$

• High-mass limit

1 Fermi $\longleftrightarrow m_a \approx 0.2 \text{ GeV} \quad \Rightarrow \quad \frac{e^{-m_a r}}{4\pi r} \approx \frac{1}{m_a^2} \delta(\mathbf{r}) \quad \Rightarrow \quad W_{ax}(m_a) \approx \widetilde{W}_{ax}m_a^{-2}.$

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EDM limitation



https://en.wikipedia.org/wiki/Electron electric dipole moment

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Image: A math a math

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Limit	BaF*	HfF+ **	ThO***
$ ar{g}^s_N g^p_e /(\hbar c),\;m_a\ll 1\;{ m keV}$	$7.3 imes10^{-21}$	$1.1 imes 10^{-20}$	$9.0 imes10^{-20}$
$ g_e^s g_e^p /(\hbar c),\;m_a\ll 1\;{ m keV}$	$1.6 imes10^{-20}$	$2.2 imes 10^{-20}$	$2.4 imes10^{-19}$
$ ar{g}^s_N g^p_e /(\hbar c m_a^2)$, $m_a \geq 1~{ m GeV}$	$6.4 \times 10^{-15} ~{\rm GeV}^{-2}$	$3.7\times 10^{-15}~{\rm GeV}^{-2}$	$6.0\times 10^{-15}~{\rm GeV}^{-2}$
$ g_e^s g_e^p /(\hbar c m_a^2), \; m_a \geq 1 \; { m GeV}$	$1.6 \times 10^{-11} \ {\rm GeV}^{-2}$	$1.7 \times 10^{-11} \ {\rm GeV}^{-2}$	$5.6\times 10^{-11}~{\rm GeV}^{-2}$

* Prosnyak, S. D., Skripnikov, L. V. (2024), Phys. Rev. A 109, 042821
** Prosnyak, S. D., Maison, D. E., Skripnikov, L. V. (2023), Symmetry, 15(5), 1043.
***Combining theoretical data from [Stadnik, Y. V., Dzuba, V. A., & Flambaum, V. V. (2018), Phys. rev. lett., 120(1), 013202; arXiv:1708.00486] and experimental data from [ACME Collaboration (2018), Nature, 562(7727), 355-360.]

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Current limitations



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Thank you for attention!

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Astrophysical experiments

QUAX-g_pg_s experiment

Torsion pendulum Eöt–Wash experiment

Magnetometry experiment

for $m_a < 10^{-14}$ eV about 17 order of magnitude better, but can be spoiled by some mechanisms

 $g_N^s g_e^p < 4.3 \times 10^{-30} \hbar c$ for the range of ALP masses $7 \times 10^{-7} \div 4 \times 10^{-6}$ eV, but for heavy axions many orders less stringent

better only for $m_a < 10^{-7}$ eV, but not for heavy axions

better only for $m_a < 10^{-6}$ eV, but not for heavy axions

EDM predictions



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