



# Superconducting magnetic system for gradient spin-flipper with a strong magnetic field

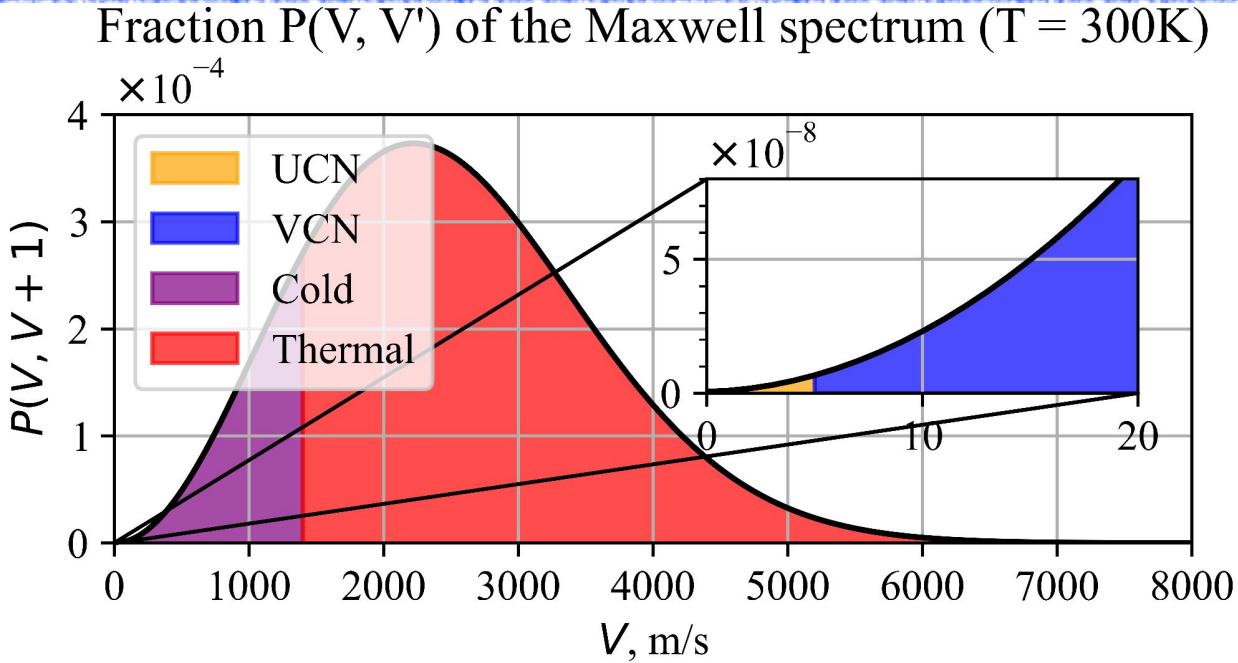
AYSS 2024

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1.11.2024  
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# Ultracold neutrons



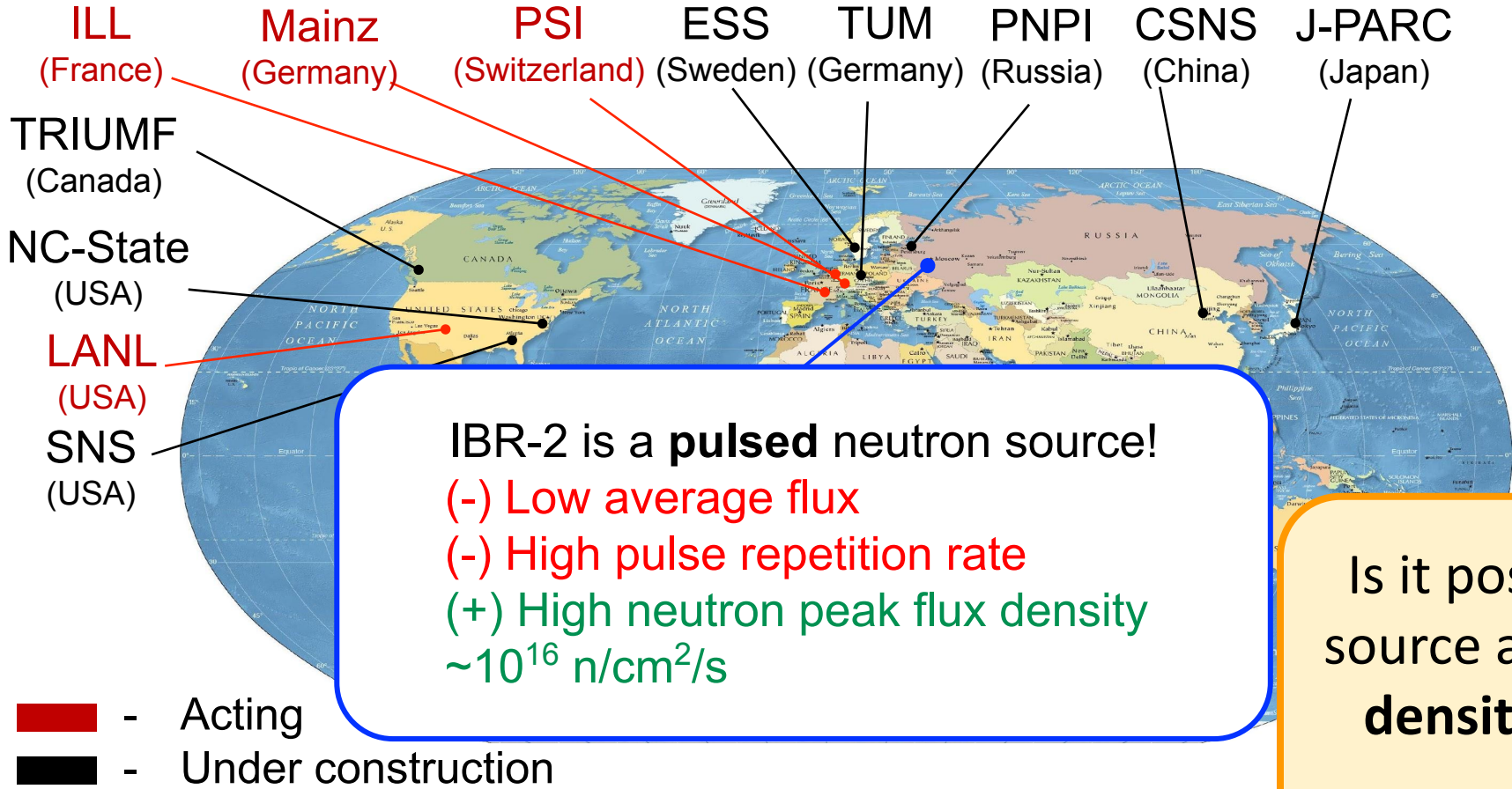
**Effective potential for neutron-matter interaction:**  
 $U = (2\pi\hbar^2/m)\rho b,$   
 $\rho$  - amount of nuclei per unit volume,  
 $b$  - coherent scattering length

| Neutrons               | Energy (eV)                      | fraction at the Maxwell spectrum (300 K) |
|------------------------|----------------------------------|--|
| <b>Ultracold (UCN)</b> | <b><math>&lt; 10^{-7}</math></b> | <b><math>\sim 10^{-8}</math></b>         |
| Very cold (VCN)        | $10^{-7} - 10^{-4}$              | $\sim 10^{-4}$                           |
| Cold                   | $10^{-4} - 10^{-2}$              | $\sim 0.14$                              |
| Thermal                | $> 10^{-2}$                      | $\sim 0.85$                              |

**Ultracold neutrons** reflect from material by any angle of incidence

**UCN** can be accumulated in material traps

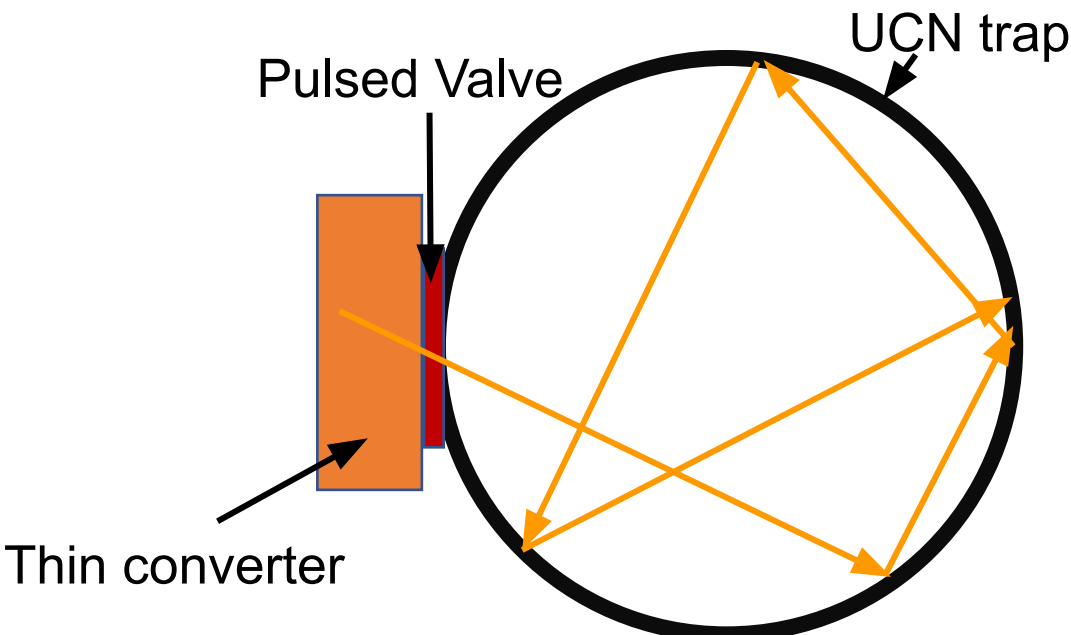
# UCN Sources



IBR-2 is a **pulsed** neutron source!  
(-) Low average flux  
(-) High pulse repetition rate  
(+) High neutron peak flux density  
 $\sim 10^{16}$  n/cm<sup>2</sup>/s

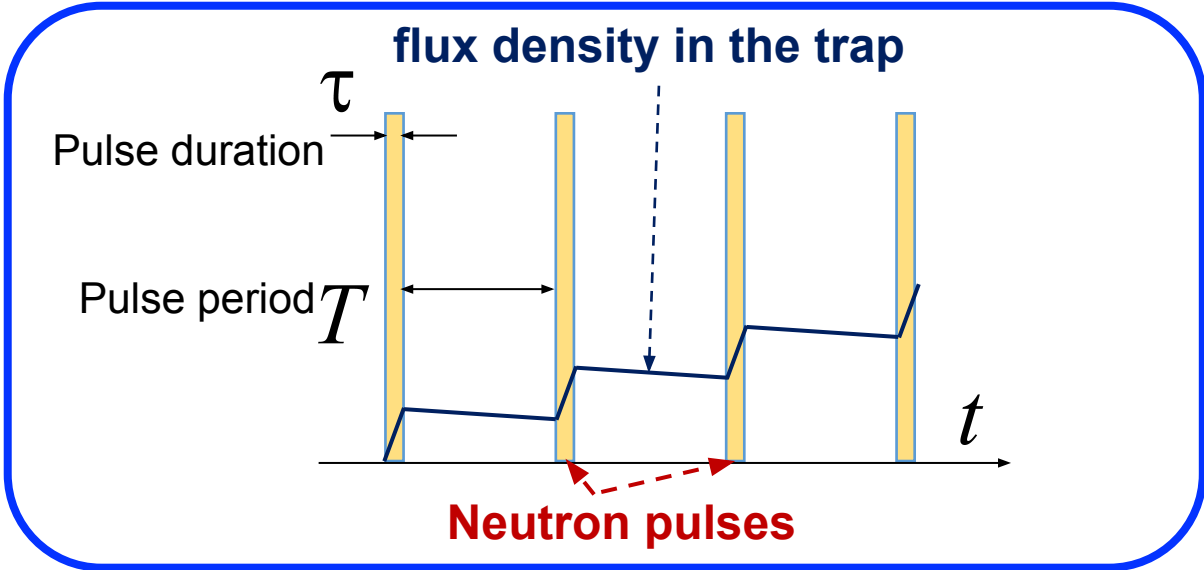
Is it possible to create the UCN source at IBR-2 using a **peak flux density** instead of an average flux density?

# The idea of UCN source at a pulsed reactor



$$0 < E_n < E_{trap} \approx 250 \text{ neV}$$

The main idea is effective **pulsed accumulation** of UCN in the trap



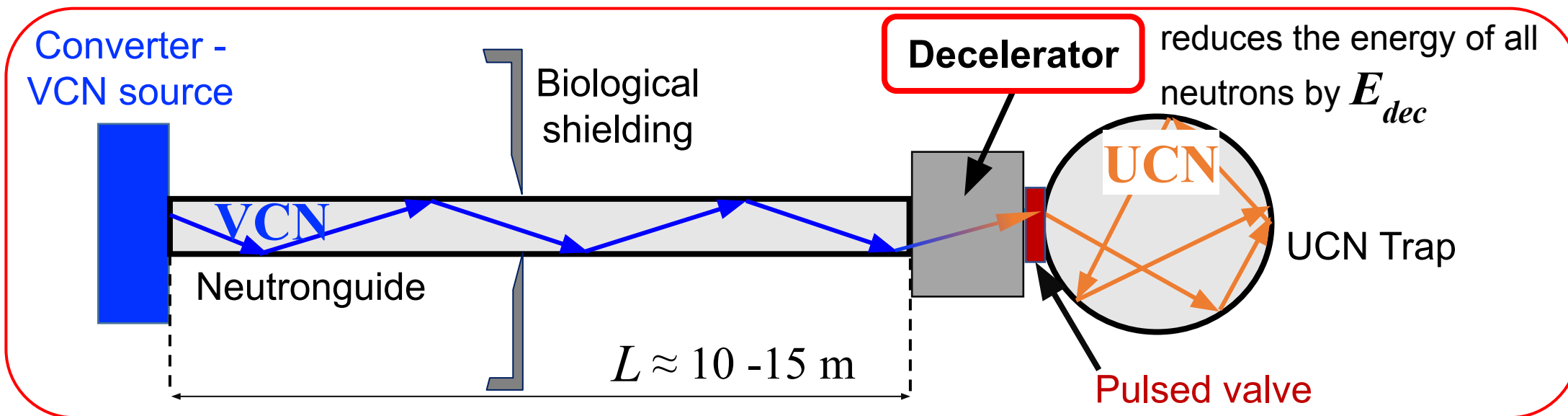
The increasing of the neutron flux in the trap due to pulsed filling of the trap

$$g = \frac{ST}{S\tau + \Sigma\mu T}$$

- S - area of the trap entrance
- $\Sigma$  - area of the UCN trap surface
- $\mu$  - probability of UCN lost
- $\tau$  - bunch duration at the trap entrance
- T - pulse period

$$g \rightarrow 10 \div 10^2$$

# Concept of the UCN source



Before the **decelerator**:

$$E_{dec} < E_n < E_{dec} + E_{trap}$$

At the **decelerator**:

$$E_n \rightarrow E_n - E_{dec}$$

After the **decelerator**:

$$0 < E_n < E_{trap}$$

$$\delta t/t = \delta V/V = \delta E/(2E) = E_{trap}/2E_{dec}$$

$$\delta E \ll E \Rightarrow \delta t \ll T$$

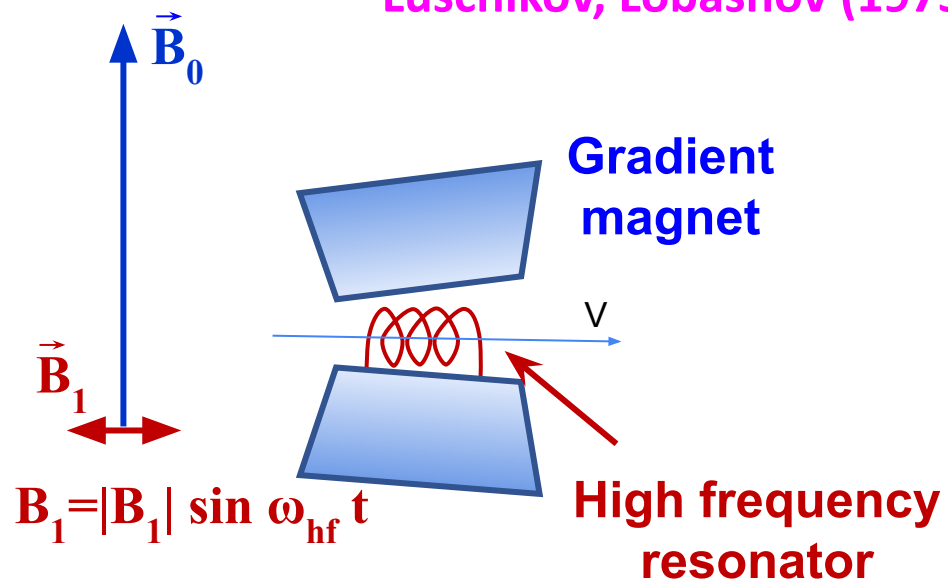
The flux of neutrons, which can be trapped after strong ( $E_{dec} \gg E_{trap}$ ) deceleration, has a **pulsed structure**

$T$  - pulse period,  $t$  - flight time,  $\delta t$  - variance of the flight time at the trap entrance,  
 $E_n$  - energies of neutrons, which can be trapped after strong deceleration

# Decelerator – gradient (adiabatic) spin-flipper

## Scheme of the first adiabatic spin-flipper

Luschikov, Lobashov (1973)



A spin flip in a combination of stationary and nonstationary magnetic fields **leads to a change in energy**

Drabkin, Zhitnikov (1960)

$$\Delta E = \hbar \omega_{hf} = 2\mu B_0$$

$$\omega_{hf} = \omega_L = \gamma B_0 - \text{resonance condition}$$

$\omega_L$  - angular velocity of Larmor precession at  $B_0$  field

$\mu = 60.31 \text{ neV/Tl}$  - the magnetic moment of a neutron

$\gamma = 1.83 \cdot 10^8 \text{ rad Tl}^{-1} \text{ sec}^{-1}$  - the gyromagnetic ratio of a neutron

# Spinflip probability at adiabatic spin-flippers

Adiabaticity parameter  $k$ :

$$k = \omega_L / \omega_B = \frac{\gamma B_1^2}{(\partial |B_0| / \partial z) V}$$

$p > 0.99$ , when  $k > 4$

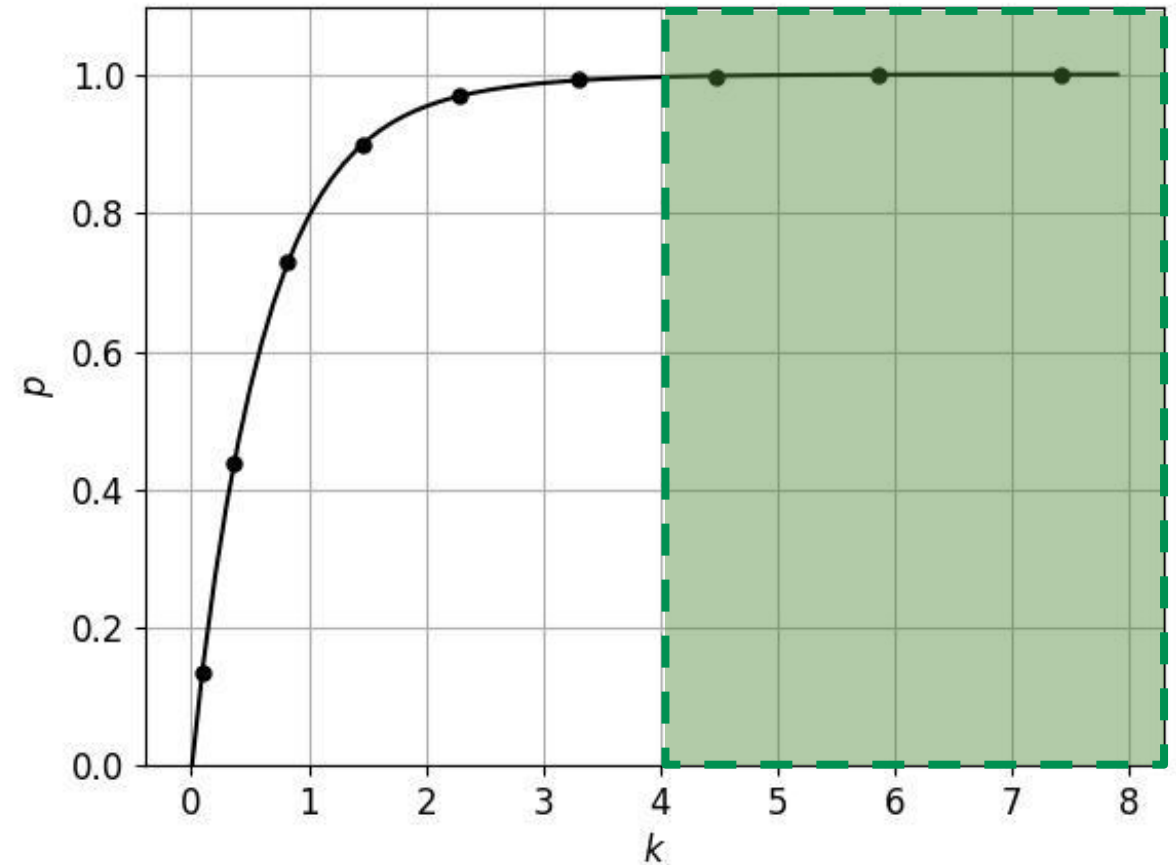
$\omega_B$  - angular velocity of field B in neutron coordinate system

$V$  - neutron velocity

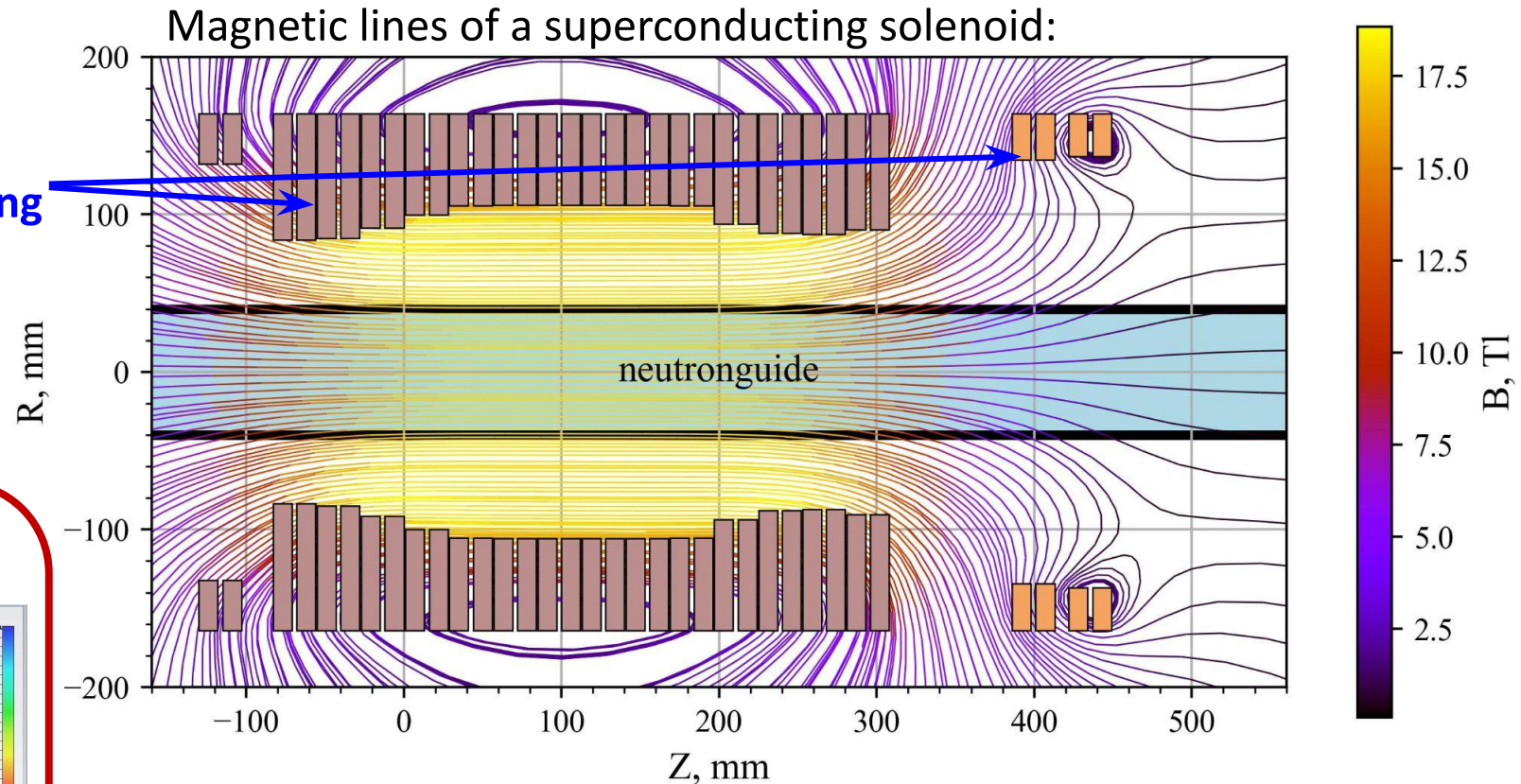
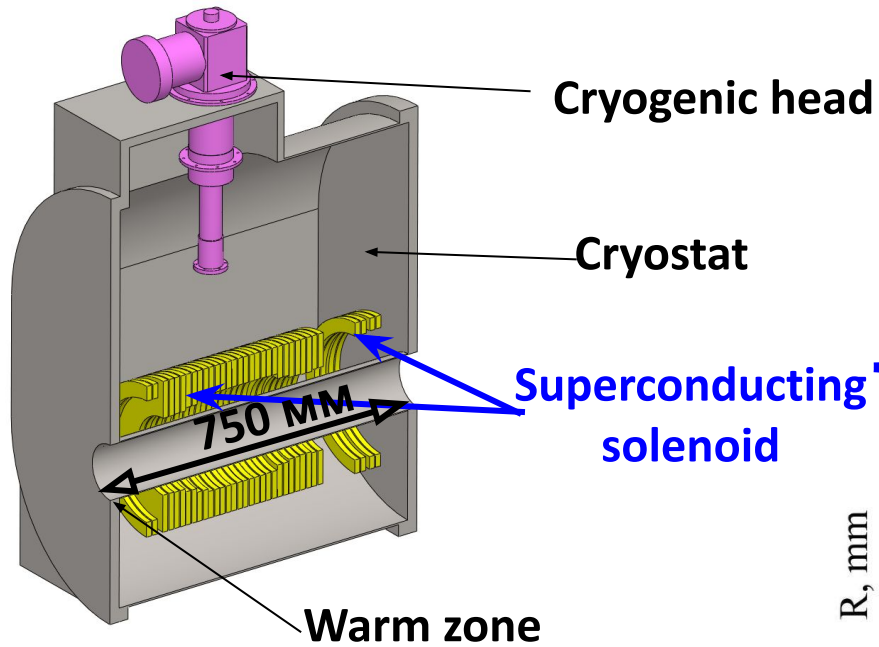
$B_0$  - stationary gradient field

$B_1$  - rotating HF field

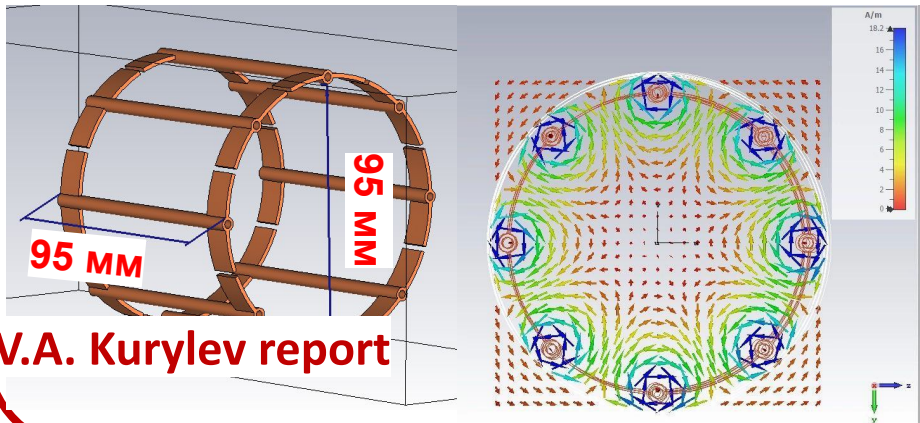
Spinflip probability  $p$  in dependence of adiabaticity parameter  $k$



# The design of the flipper-decelerator



## HF-resonator "Birdcage"



V.A. Kurylev report

$$B_1 > 0.7 \text{ mT}$$

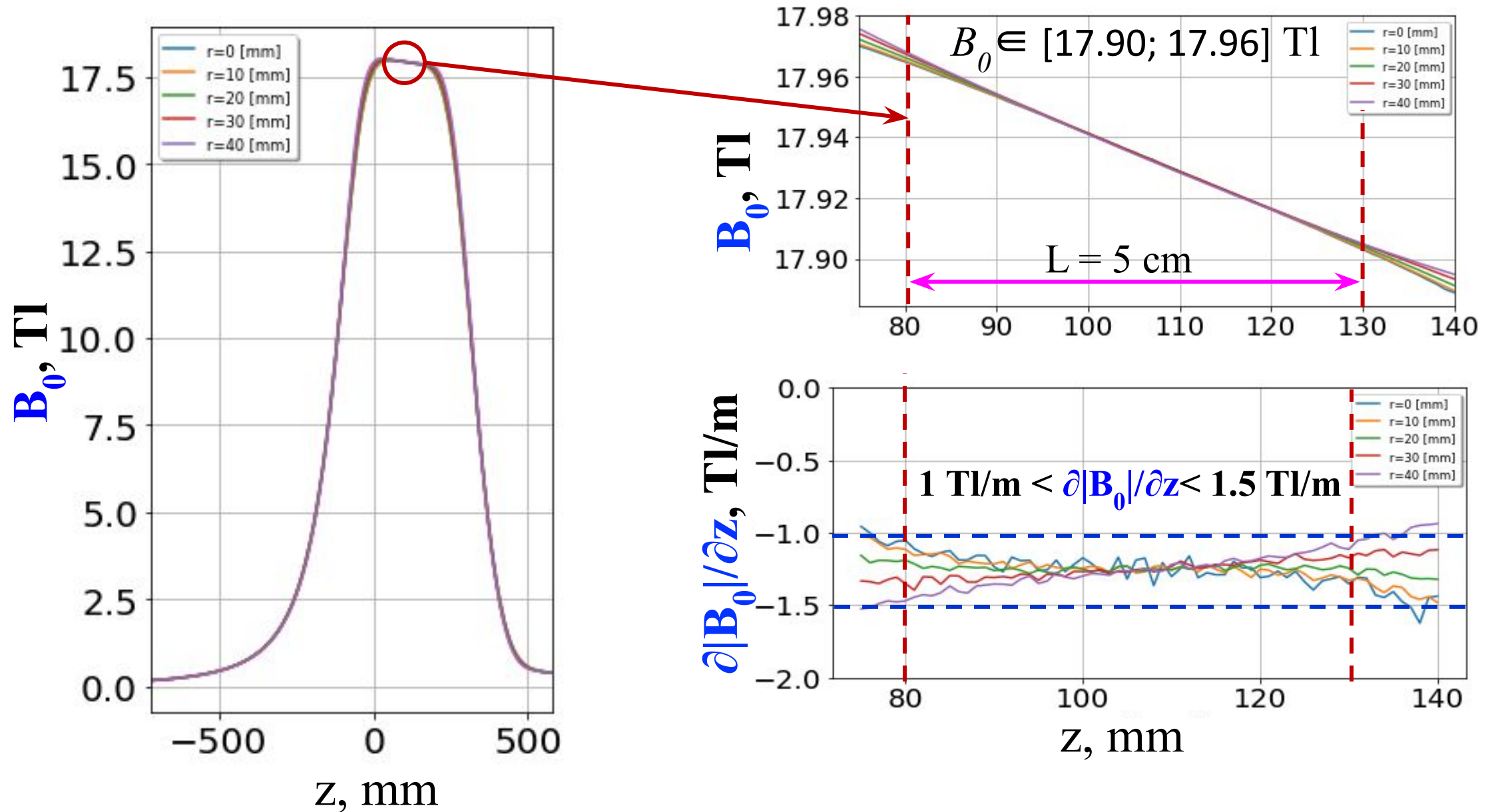
$$f = \omega/2\pi = 524 \text{ MHz}$$

$$B_0 = 18 \text{ T}, \Delta E = 2.2 \mu\text{eV}$$

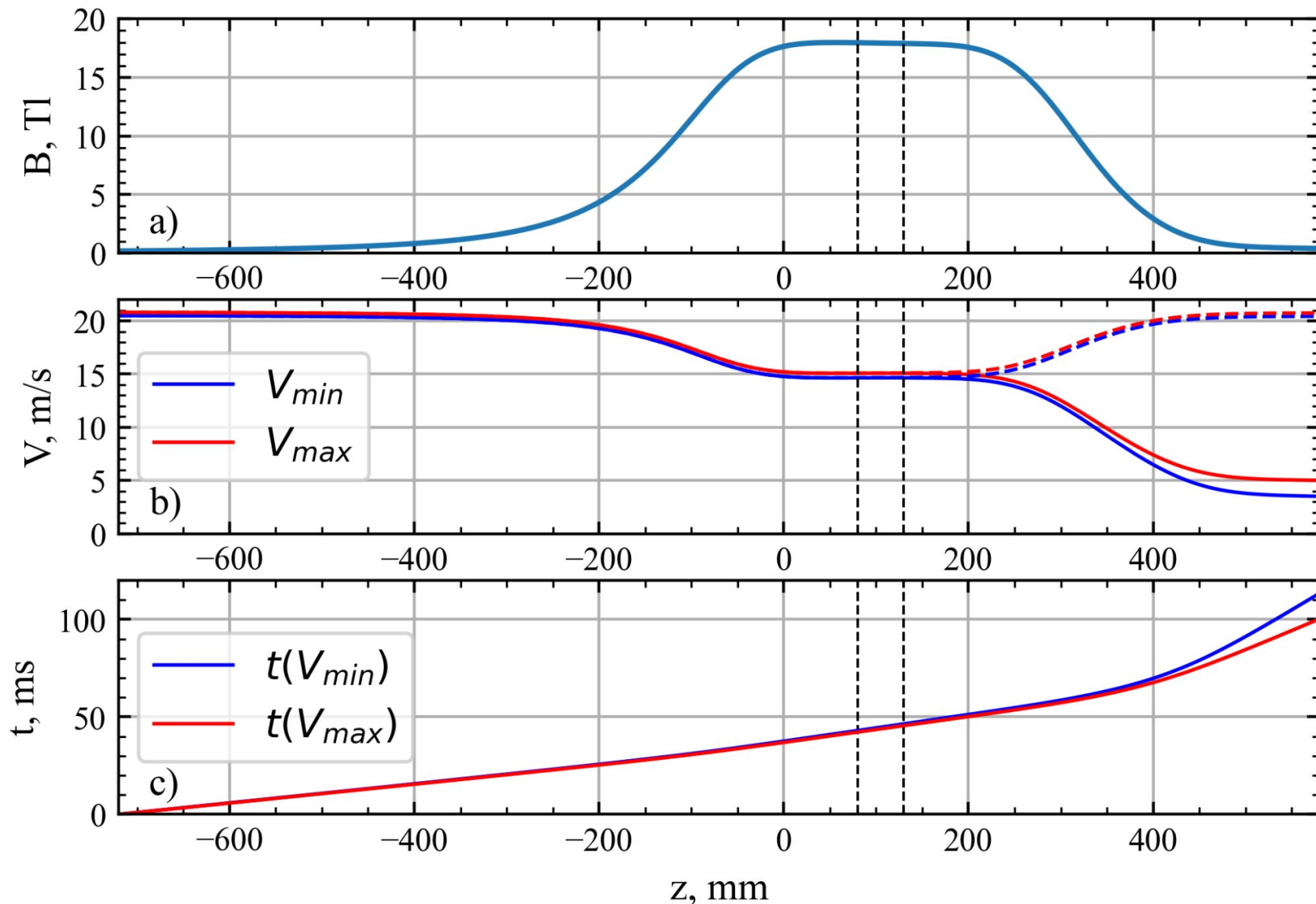
$$1 \text{ T/m} < \partial|B_0|/\partial z < 1.5 \text{ T/m}$$



# Magnetic fields of the superconducting magnet



# Neutrons in a strong magnetic field



- a) Field  $B_0$  distribution along z-axis
- b) Neutron velocity evolution in field  $B_0$  along z-axis
- c) Neutron deceleration time evolution along z-axis

The full energy change occurs only over a small area, but **the velocity change occurs throughout the entire path inside the magnetic field**

# The results of the MC-analysis of the magnetic system\*

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## *Bunch depolarisation*

$$< \mathbf{0.1\%}, \omega_L/\omega_B > 10^4$$

## *Flipper efficiency*

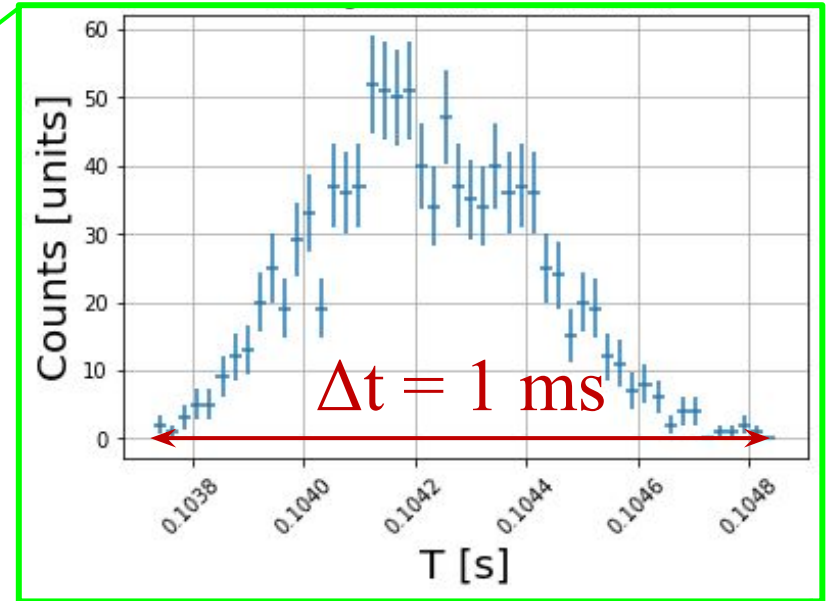
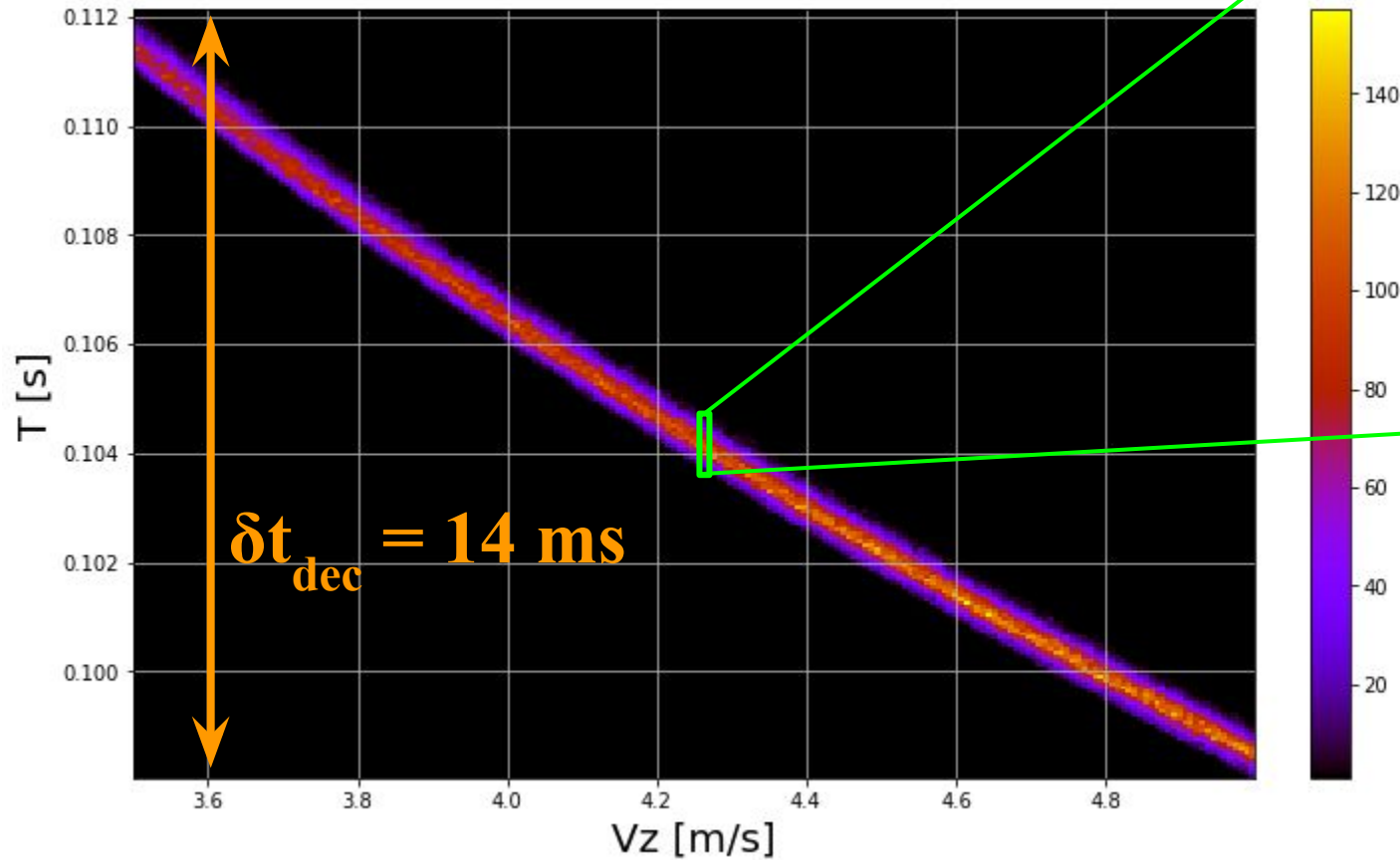
Spinflip probability  $> 0.99$

\*only for useful neutrons!  $V \in [20.9; 21.2]$  m/s

# The results of the MC-analysis of the magnetic system\*

## Deceleration time

Neutron distribution by deceleration time  $T$  and final longitudinal velocity  $V_z$

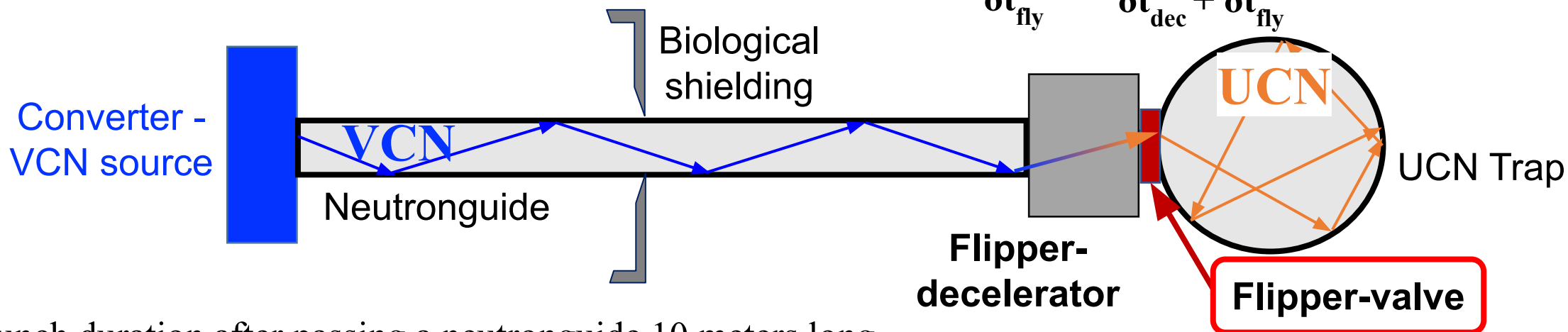
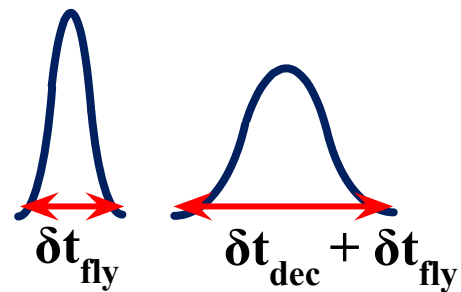


\*only for useful neutrons!  $V \in [20.9; 21.2] \text{ m/s}$

# The possibility of a pulsed accumulation

$$\begin{aligned}\delta t_{\text{fly}} &\approx 15 \text{ ms} \\ \delta t_{\text{dec}} &\approx 14 \text{ ms} \\ \delta t &\approx \delta t_{\text{dec}} + \delta t_{\text{fly}} \approx 30 \text{ ms}\end{aligned}$$

$$\begin{aligned}\delta t &\ll T = 200 \text{ ms} \\ \delta t/T &\approx 1/7\end{aligned}$$



Pulsed accumulation is possible!

$\delta t_{\text{fly}}$  - VCN bunch duration after passing a neutronguide 10 meters long  
 $\delta t_{\text{dec}}$  - VCN bunch duration after passing flipper-decelerator,  
 $\delta t$  - full VCN bunch duration,  
 $T$  - pulse period.

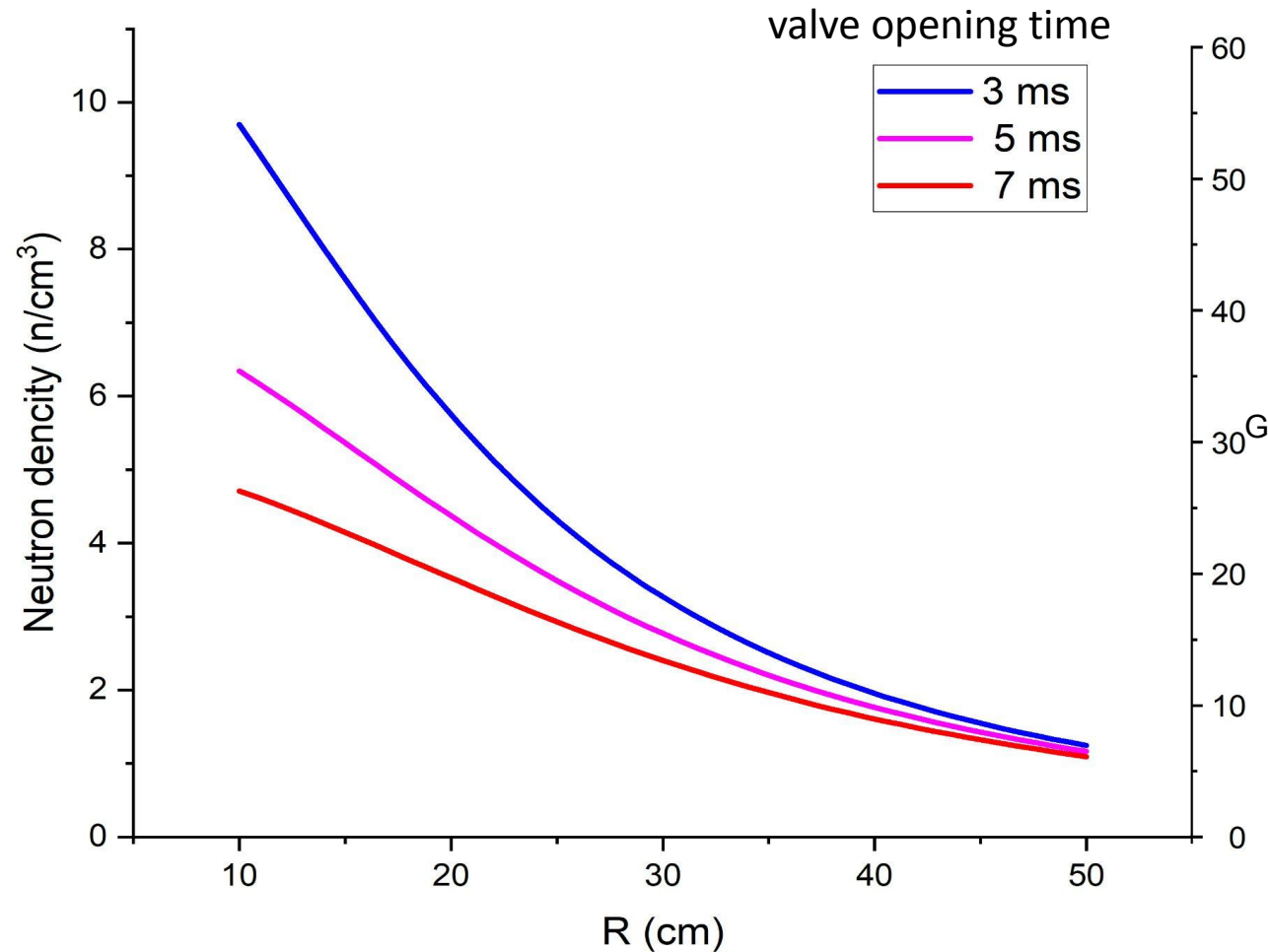
# Summary

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- A primary design of the superconducting gradient solenoid for a UCN source has been developed
- It was shown:
  - The flipper efficiency is better than 99 %
  - The variance of the deceleration time  $\delta t_{\text{dec}} = 14$  ms.
  - **Using flipper-decelerators allows one to implement the idea of effective pulsed accumulation.**

# Additional materials

# Neutron density in a spherical UCN trap (liquid H<sub>2</sub> converter)



G is the ratio of the flux in the trap to the average flux at the trap entrance

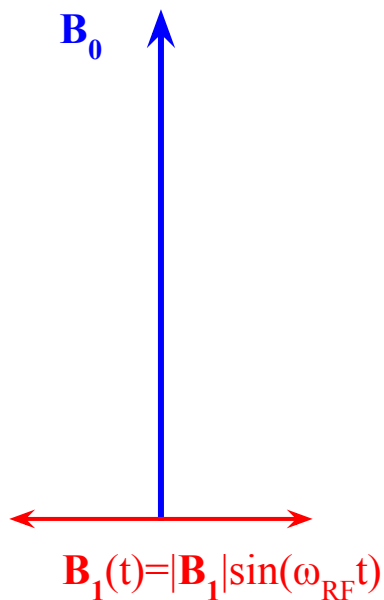
Neutron density depending on the UCN trap radius

For more effective converter, like **solid D<sub>2</sub>**, the neutron density can be increased by **30** times

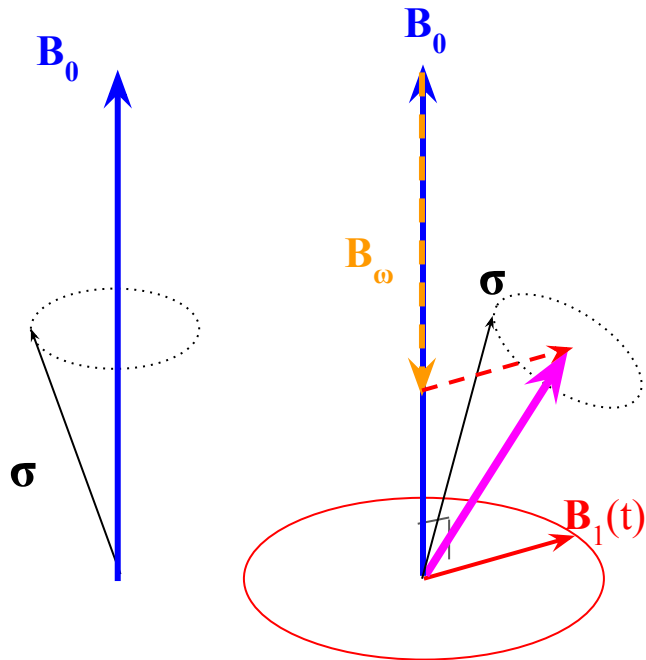


# Polarization evolution in magnetic resonance system

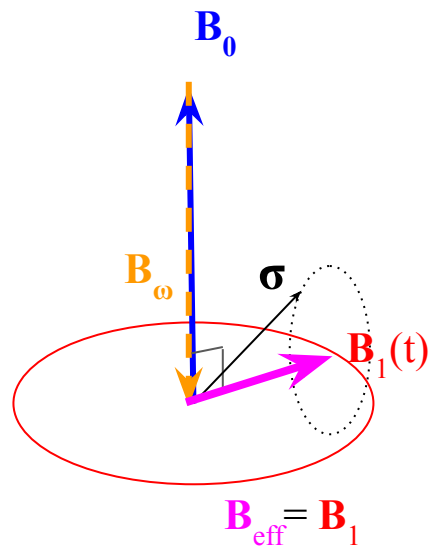
$\mathbf{B}_0 = \mathbf{B}_0(z)$  - gradient static field  
 $\mathbf{B}_1 = \mathbf{B}_1(t)$  - oscillating time-dependent RF field  
 $\mathbf{B}_\omega = -\omega_{\text{RF}}/\gamma$  - fictive field  
 $\mathbf{B}_{\text{eff}} = \mathbf{B}_0 + \mathbf{B}_\omega + \mathbf{B}_1$  - effective field



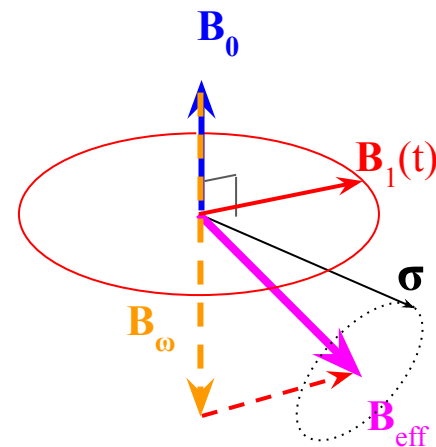
Before RF field



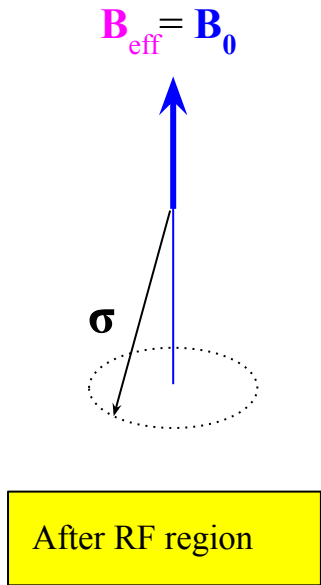
Beginning of RF region



spin-flipping area of RF region



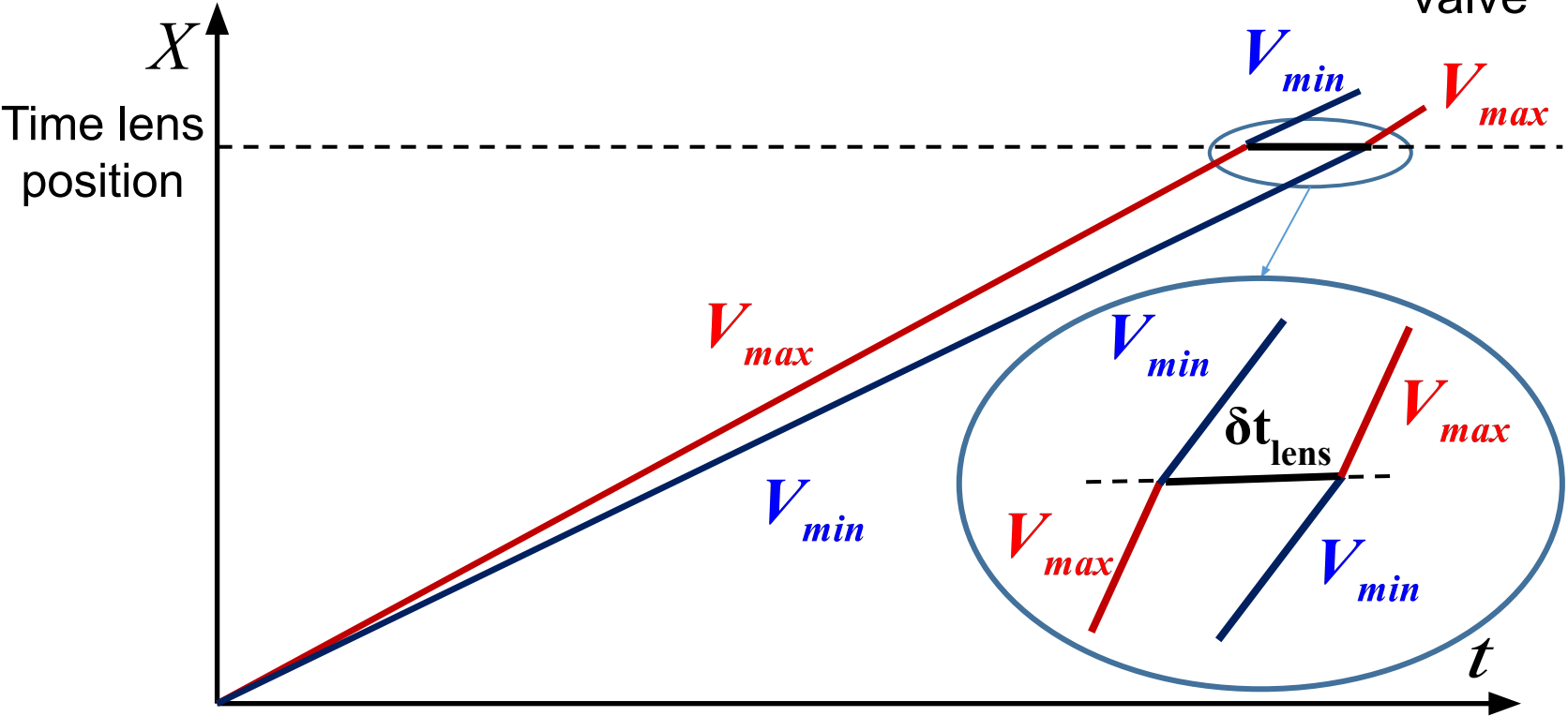
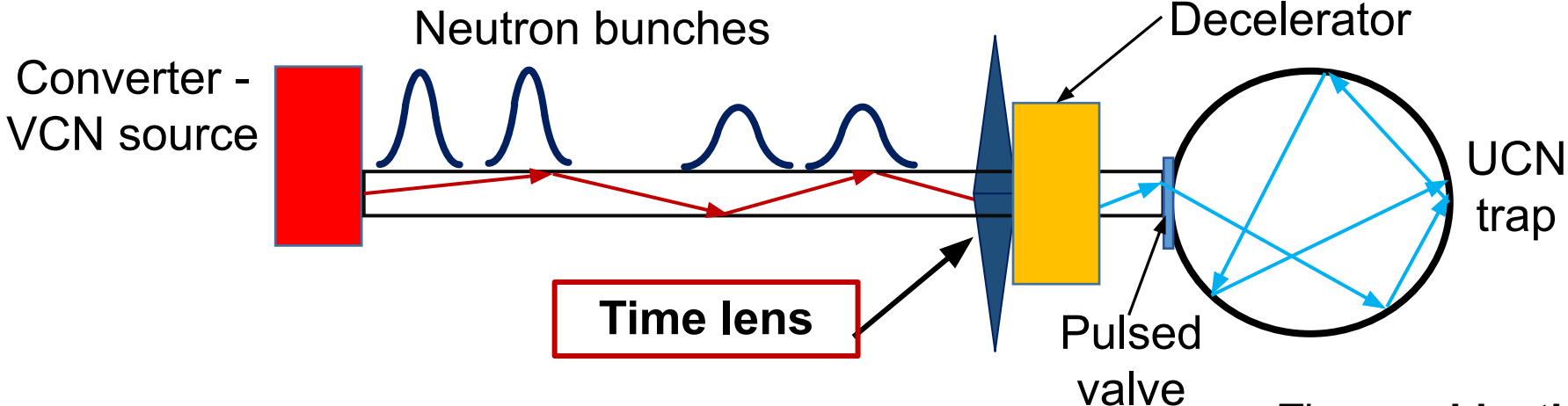
Ending of RF region



After RF region

# Time lens

Work in progress



The **combination** of the *time lens* and the *decelerator* allows to minimize **bunch duration**

$$\delta t \approx \delta t_{\text{dec}} - \delta t_{\text{lens}}$$

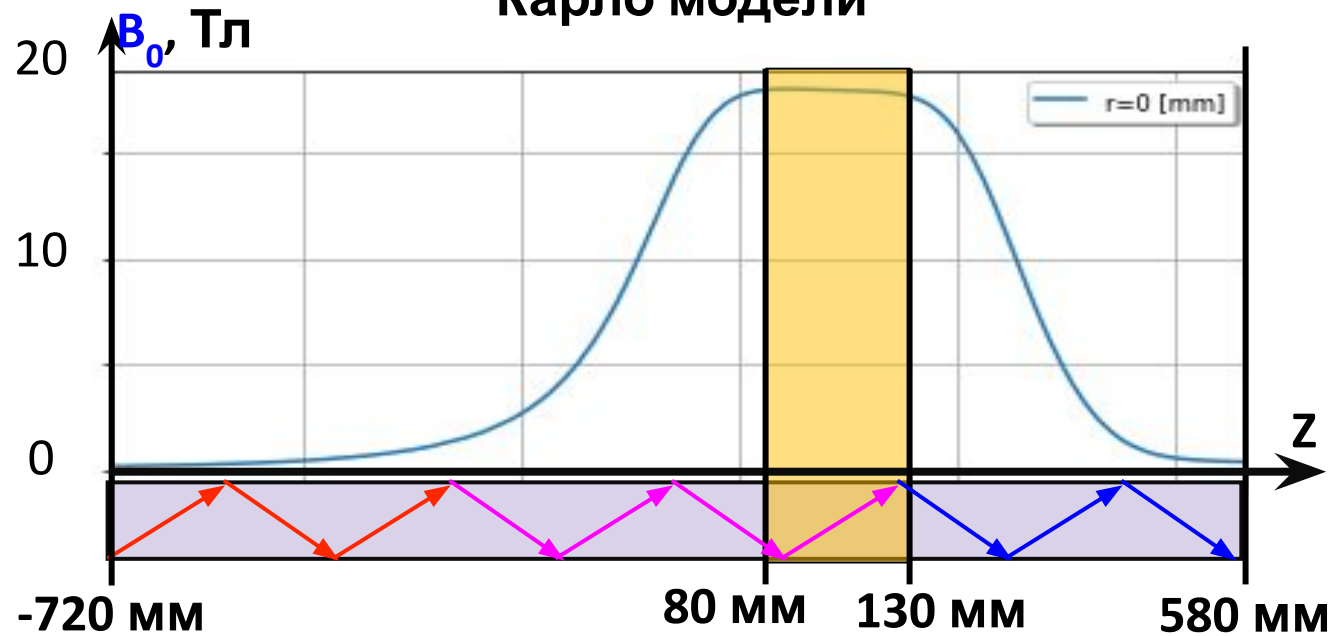
$$\delta t \ll \delta t_{\text{dec}} \approx \delta t_{\text{lens}}$$

$\delta t_{\text{lens}}$  - flight time dispersion

$\delta t_{\text{dec}}$  - deceleration time dispersion

# Монте-Карло модель движения нейтрона в магнитной резонансной системе

Рис.: Схема области расчета Монте-Карло модели



Основные положения модели:

- 1) Магнитное поле в модели задается **трехмерной сеткой** с известной напряженностью магнитного поля в узлах. **Шаг сетки - 1 мм.**
- 2) Градиент магнитного поля определяется внутри модели.
- 3) Движение осуществляется через ячейки с постоянным градиентом магнитного поля.
- 4) **Отражение** от стенок нейтроновода считается зеркальным.

$$\mathbf{F} = \nabla(\boldsymbol{\mu}, \mathbf{B}) - \text{уравнение движения нейтрона}$$
$$d\boldsymbol{\mu}/dt = \gamma[\boldsymbol{\mu}, \mathbf{B}] - \text{уравнение прецессии спина}$$

- Сечение нейтроновода 6 см x 6 см
- Длина области 1.3 м