

Methods of the increasing the efficiency of registration the rare decay $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$ in the E391 experiment

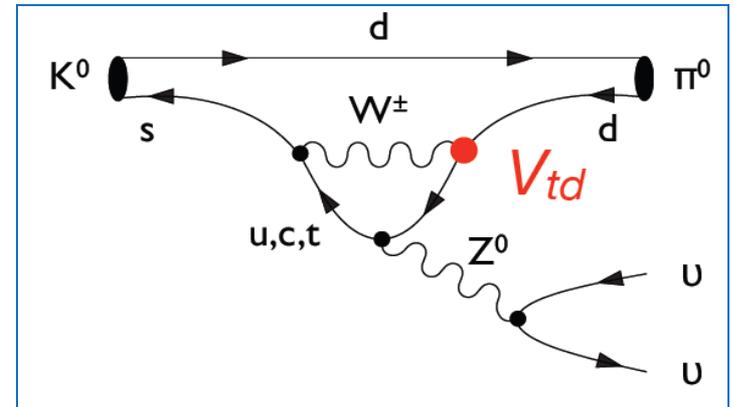
Yu. Yu. Stepanenko (DLNP, JINR)

Pub: Increase in the detection efficiency for the $K_0(L) \rightarrow \pi^0 \nu \bar{\nu}$ decay in the E391 experiment.
Yu.Yu. Stepanenko, A.S. Kurilin, S.V. Podolsky. *Physics of Particles and Nuclei Letters*, 2017, Vol. 14, No. 6, pp. 168–174.

$K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$ Decay

- “Direct” CP violating process
 - indirect contribution $\approx 10^{-3}$ (negligibly small)
- Measures η in CKM matrix

$$Br(K_L^0 \rightarrow \pi^0 \nu \bar{\nu}) \propto \eta^2$$

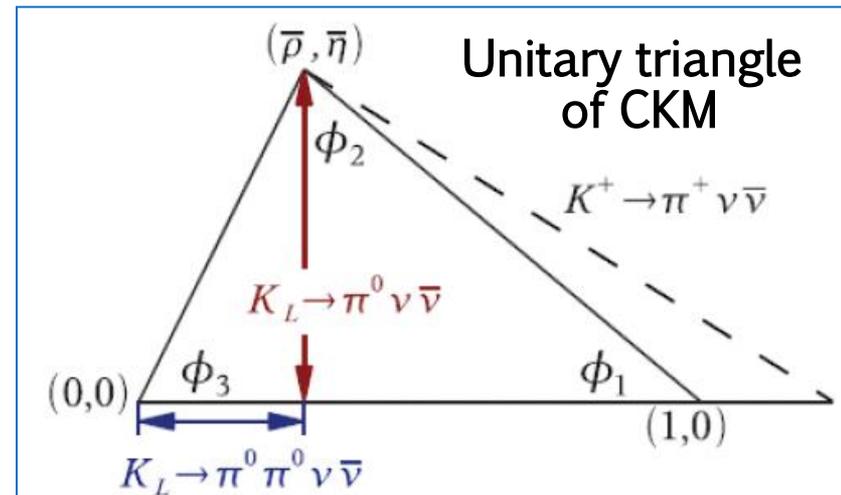


$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4)$$

- Small theoretical uncertainty ($\approx 2\%$)
 - Precise check of SM
- Rare decay in SM prediction

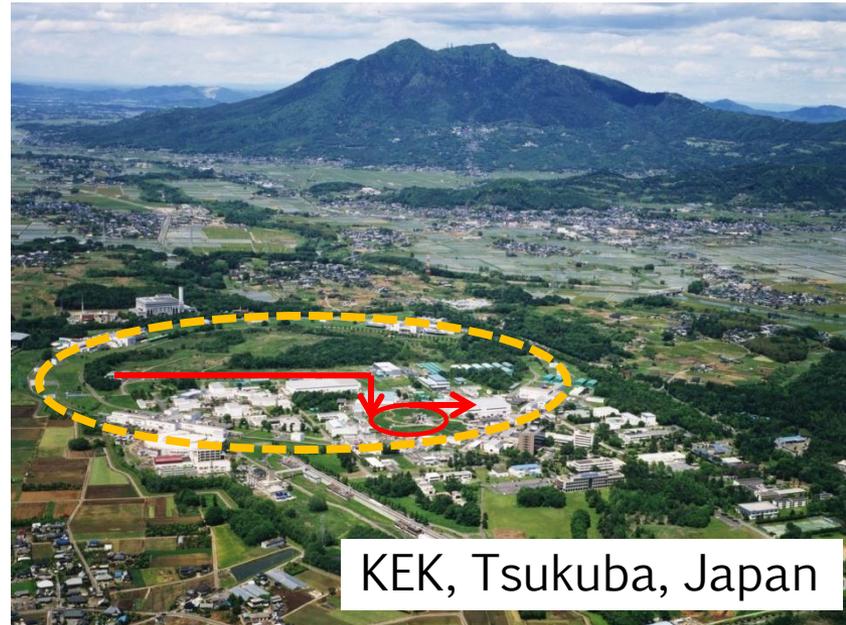
$$Br(K_L^0 \rightarrow \pi^0 \nu \bar{\nu}) = 3.0 \times 10^{-11}$$

- Probe to New Physics



The E391 Experiment

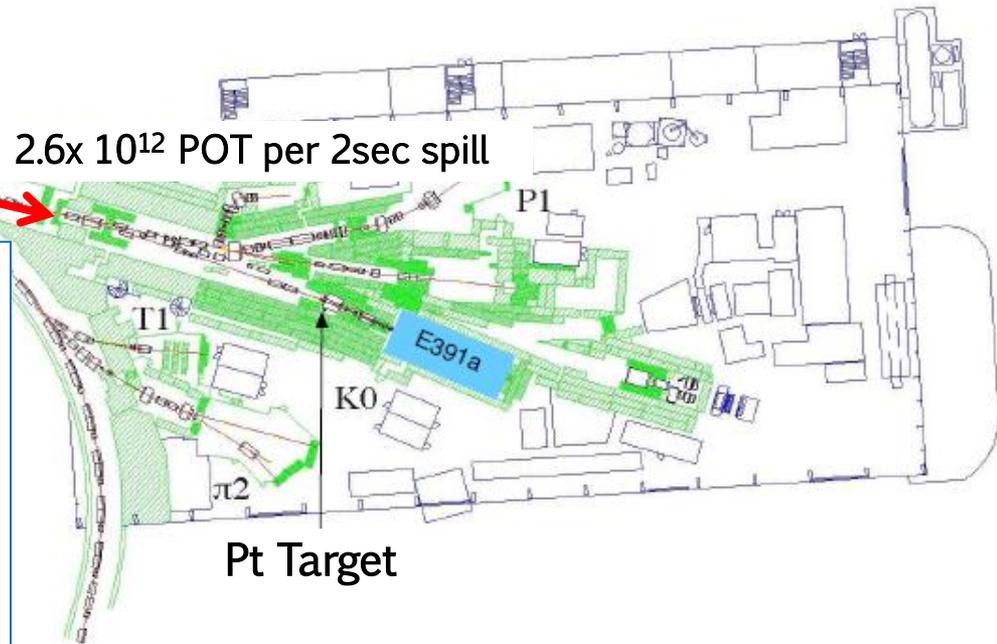
- Measures $Br(K_L^0 \rightarrow \pi^0 \nu \bar{\nu})$ @KEK 12GeV Proton Synchrotron
 - First dedicated experiment for this mode
 - Pilot experiment for KOTO (J-PARC E14)
 - Physics runs in 2004-2005
 - New Upper Limit:



$Br < 2.6 \times 10^{-8}$ @ 90% C.L.

2.6×10^{12} POT per 2sec spill

Run-I	Period	Feb. 2004 to June. 2004
	Total protons	2.1×10^{18}
	Remarks	Membrane problem
Run-II	Period	Feb. 2005 to Apr. 2005
	Total protons	1.4×10^{18}
	Remarks	Be absorber
Run-III	Period	Oct. 2005 to Dec. 2005
	Total protons	1.2×10^{18}
	Remarks	New BA, Additional photon counter

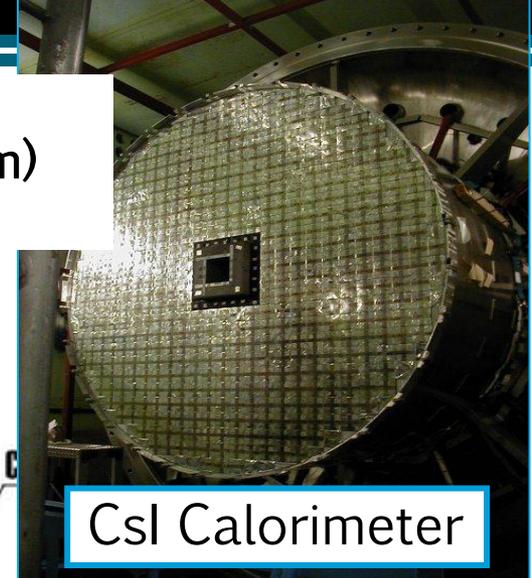




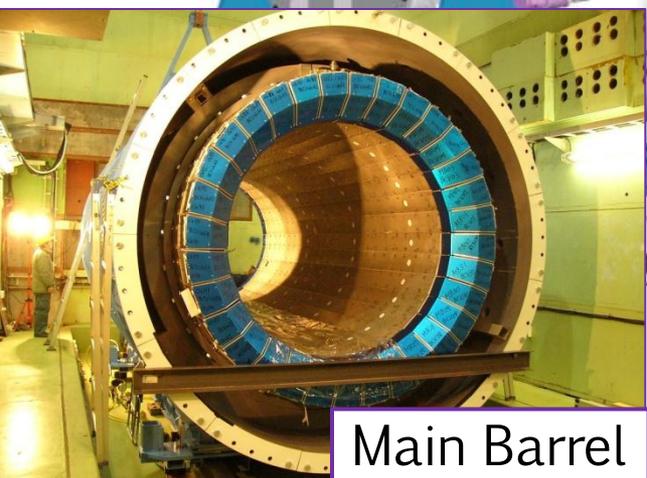
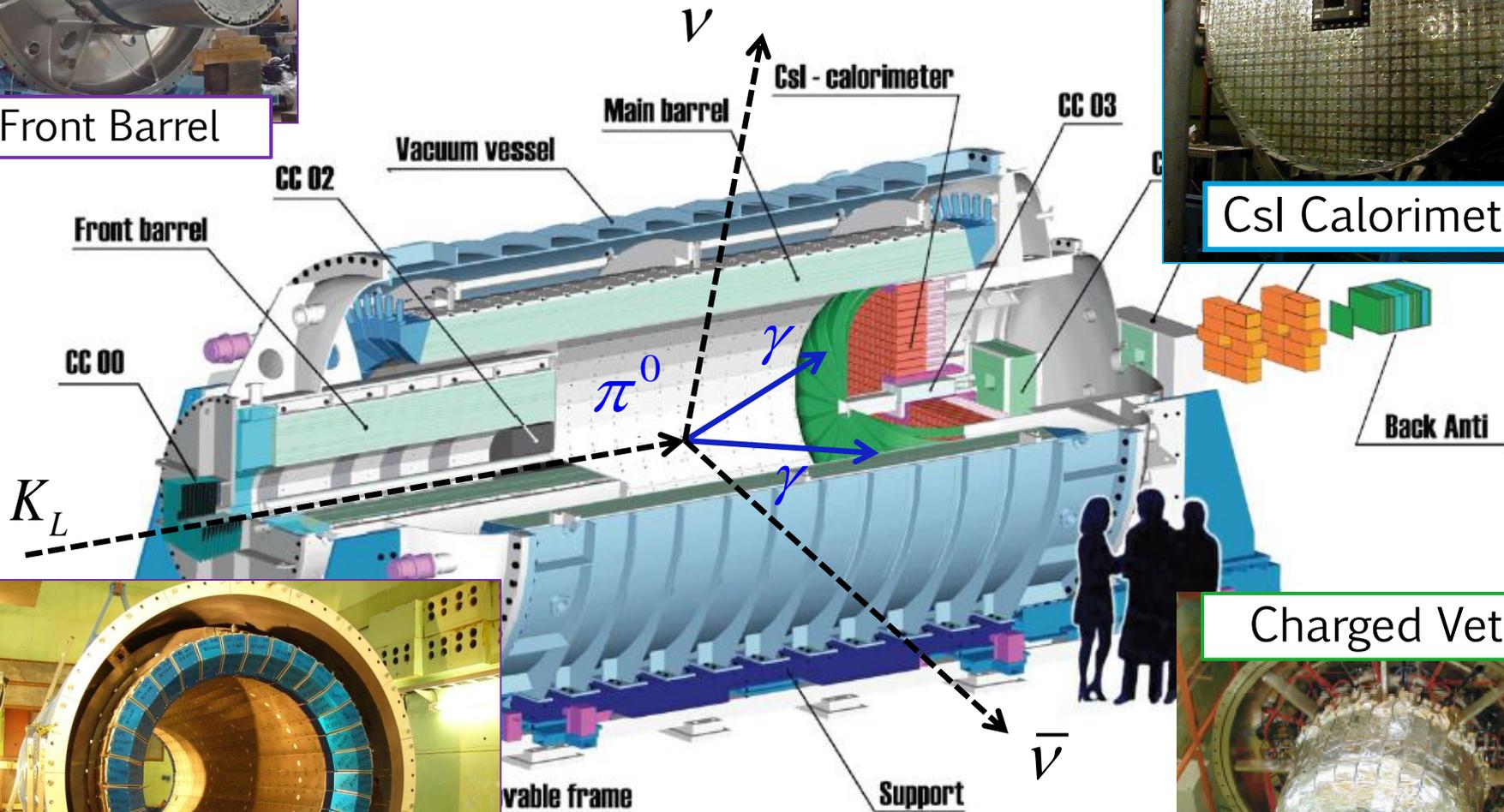
Front Barrel

E391 Setup

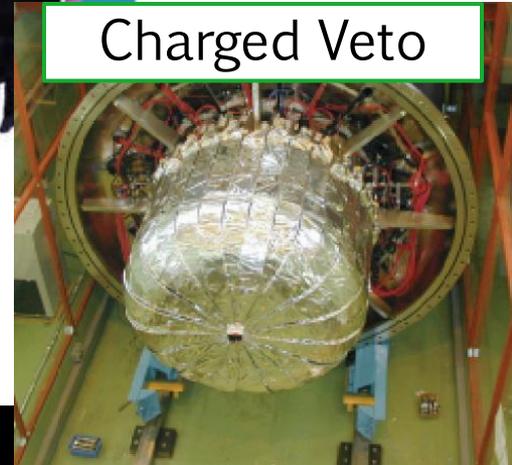
Pure CsI crystal
7x7x30cm (5x5x50cm)
576 channels



CsI Calorimeter



Main Barrel



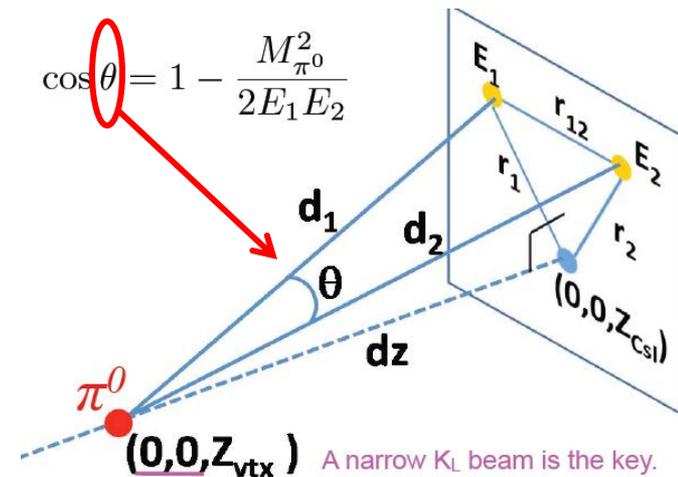
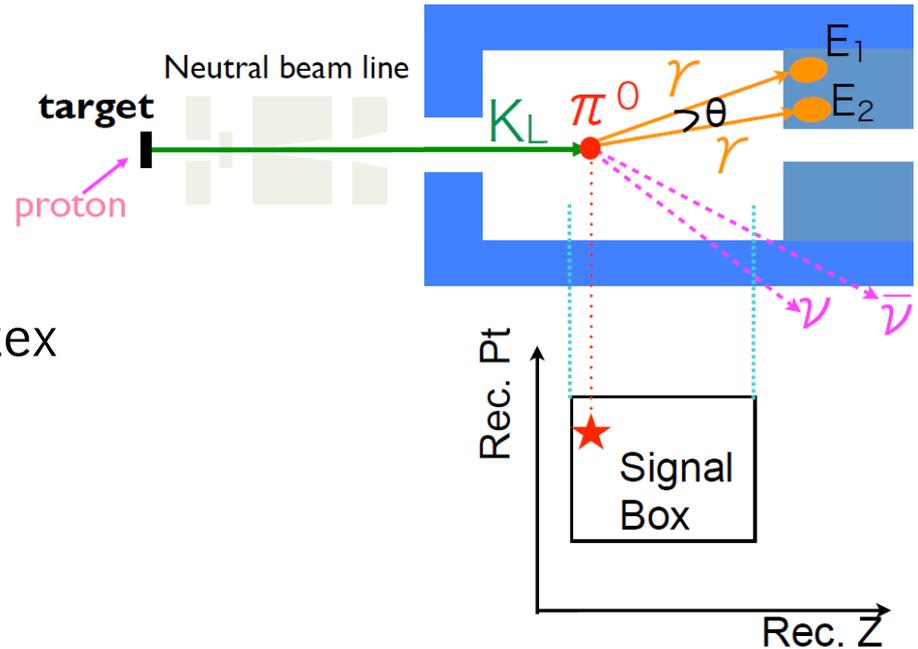
Charged Veto

Experimental Principle

- “ 2γ + nothing”
 - 2γ – CsI calorimeter (E, x, y)
 - “nothing” – hermetic veto system
- Reconstruct the π^0 decay Z-vertex
 - on the beam line (Xvtx=Yvtx=0)
 - with $M(\pi^0)$ assumption
 - “pencil” beam to improve Pt resolution

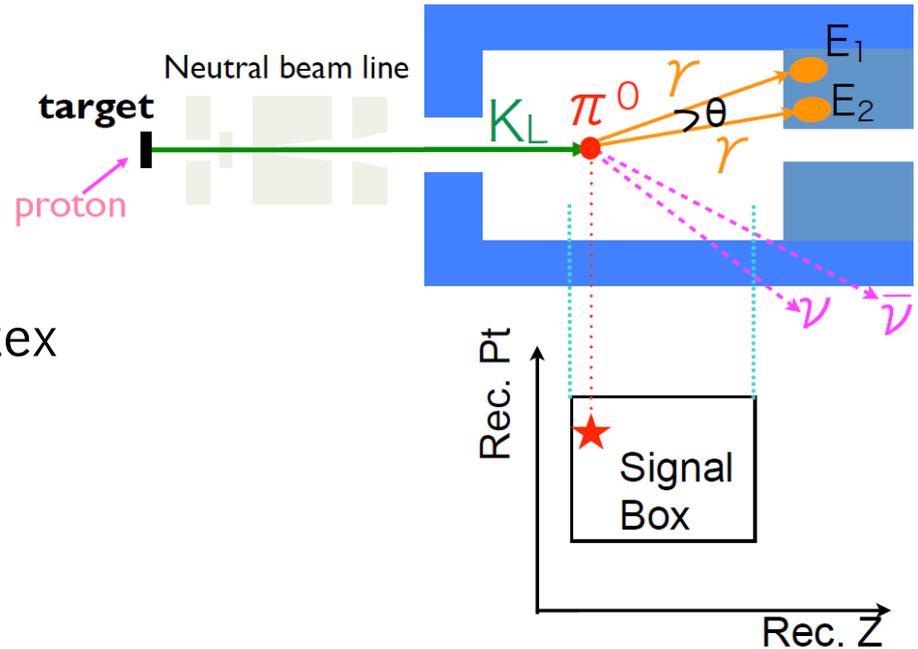
$$\cos \theta = 1 - \frac{M_{\pi^0}^2}{2E_1 E_2}$$

- Select signal events using reconstructed decay vertex and reconstructed transverse momentum
 - Required Pt and Z vertex in the signal box



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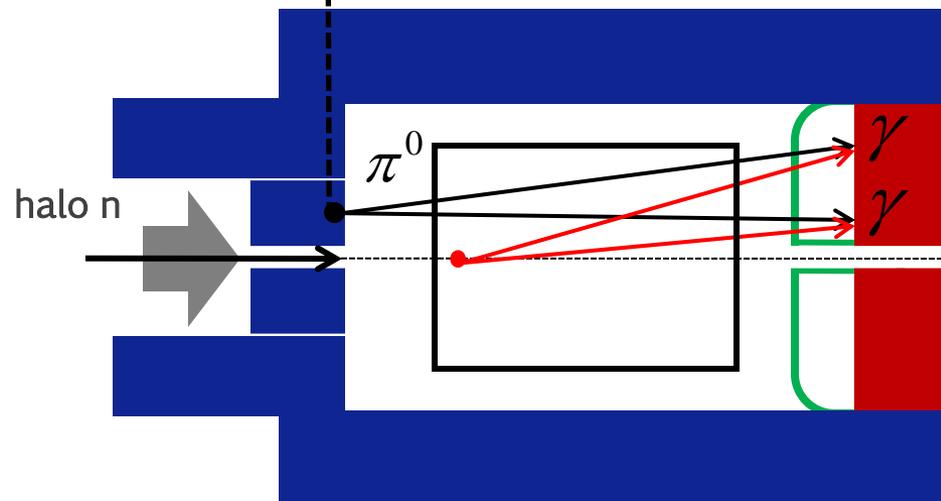
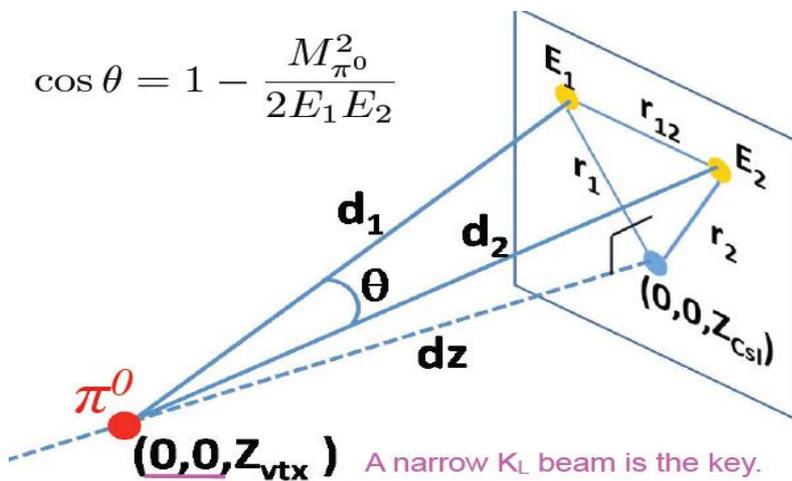
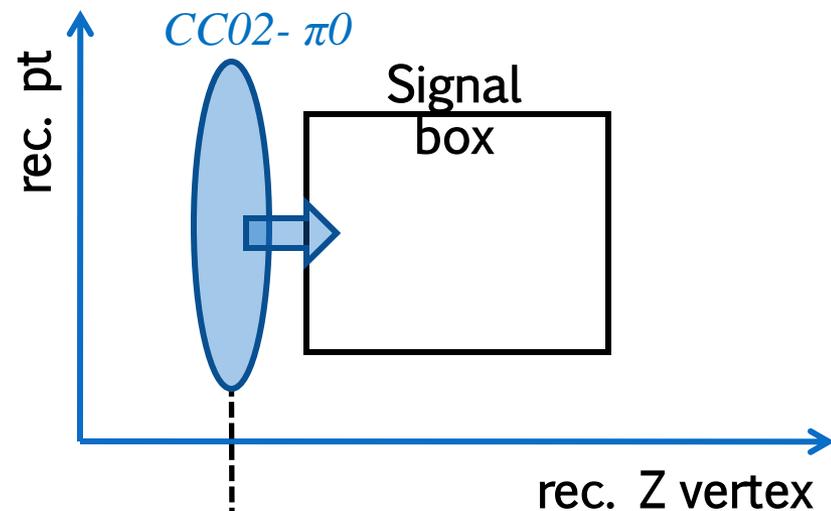
$$\cos \theta = 1 - \frac{M_{\pi^0}^2}{2E_1 E_2}$$

During of analysis, it was found that these approaches for event reconstruction don't provide effective suppression of background events

$(0,0,Z_{vtx})$ A narrow K_L beam is the key.

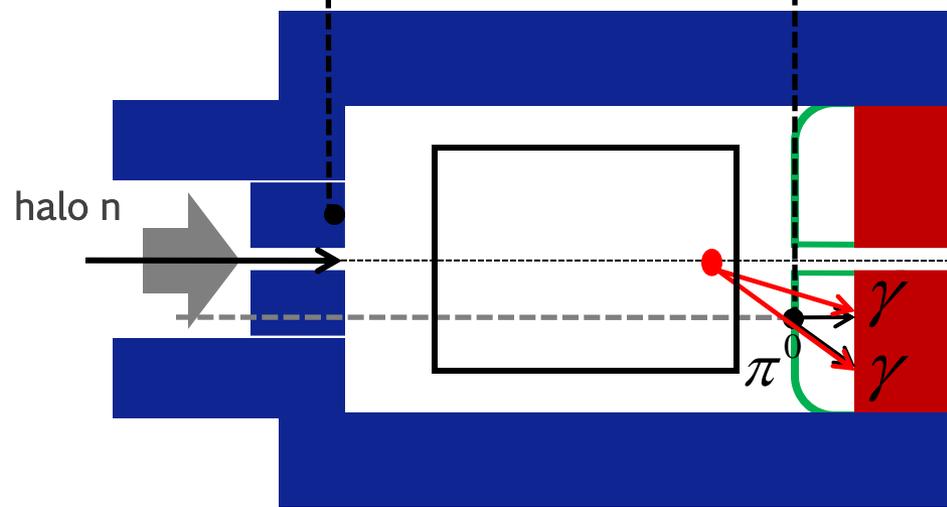
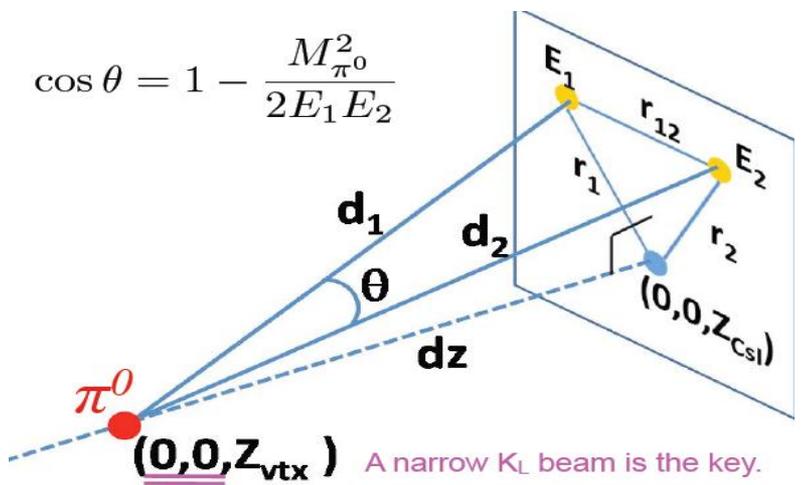
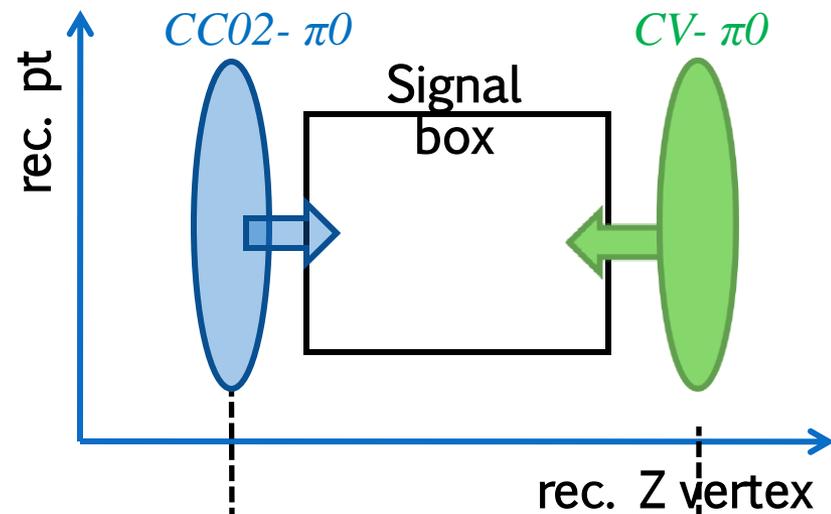
Background Sources from miss-reconstruction

- CC02 π^0 BG
 - energy γ was miss-measured



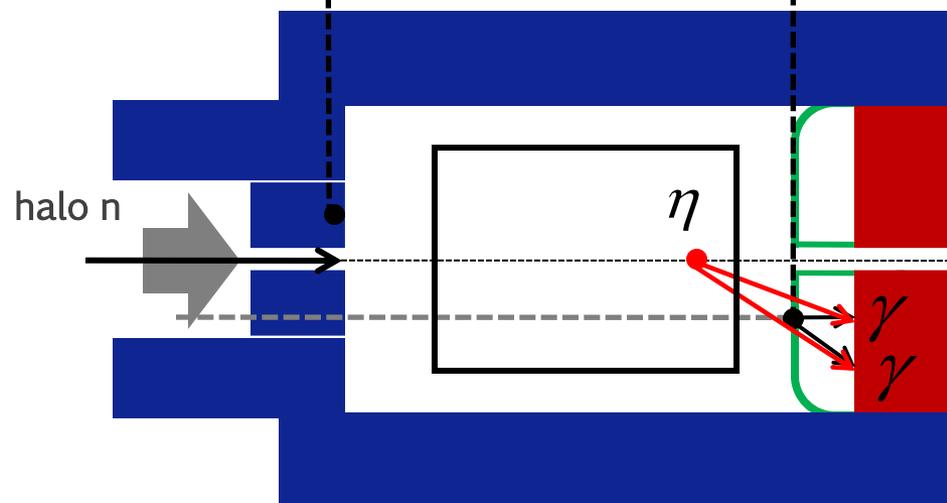
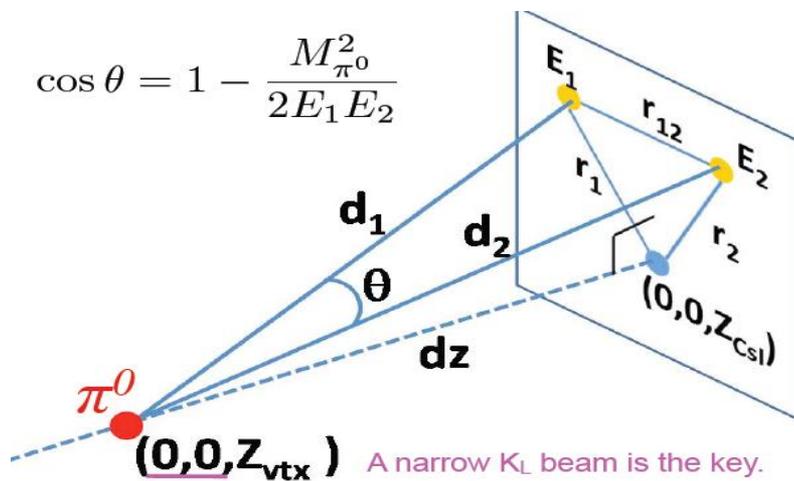
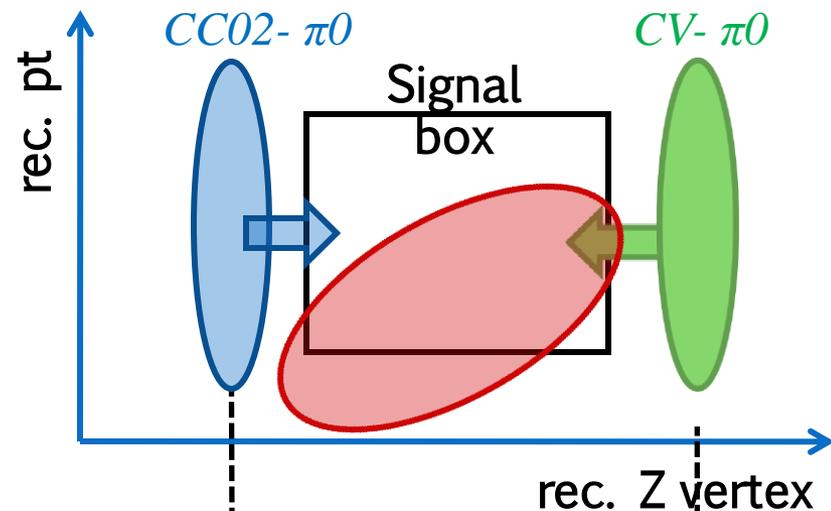
Background Sources from miss-reconstruction

- CC02 π^0 BG
 - energy γ was miss-measured
- CV π^0 BG
 - fusion γ cluster

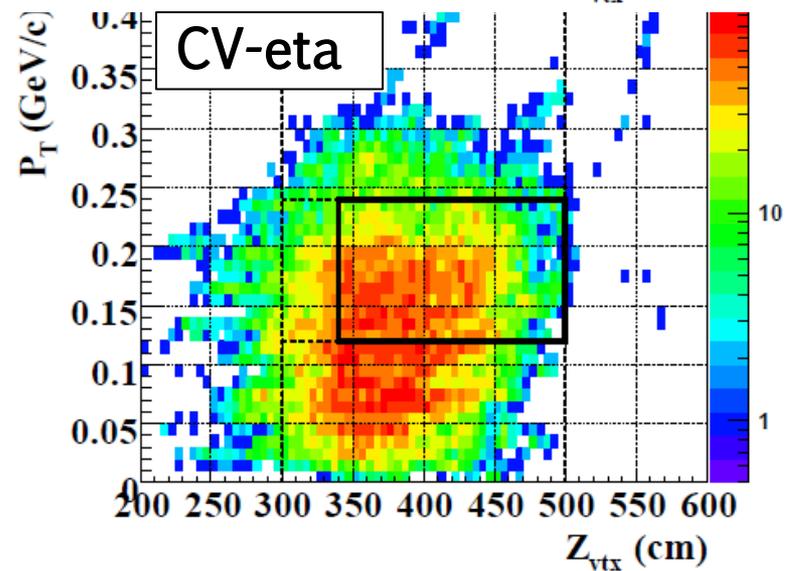
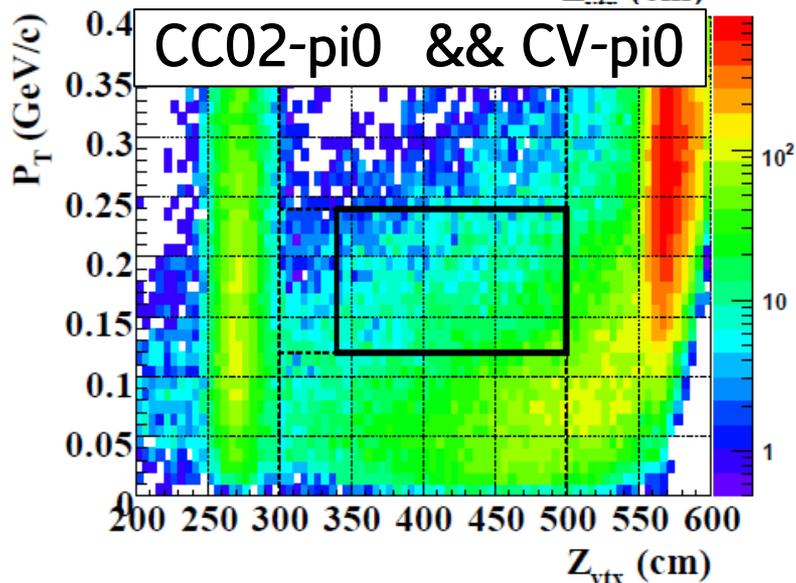
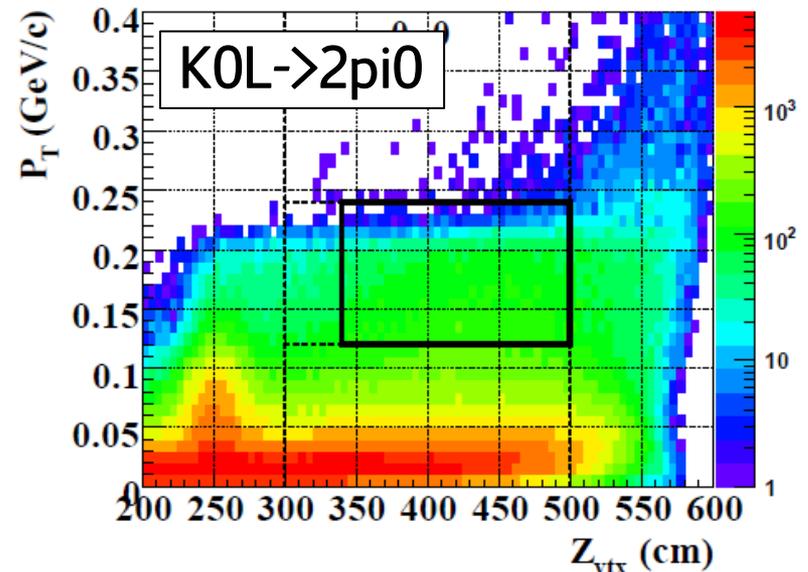
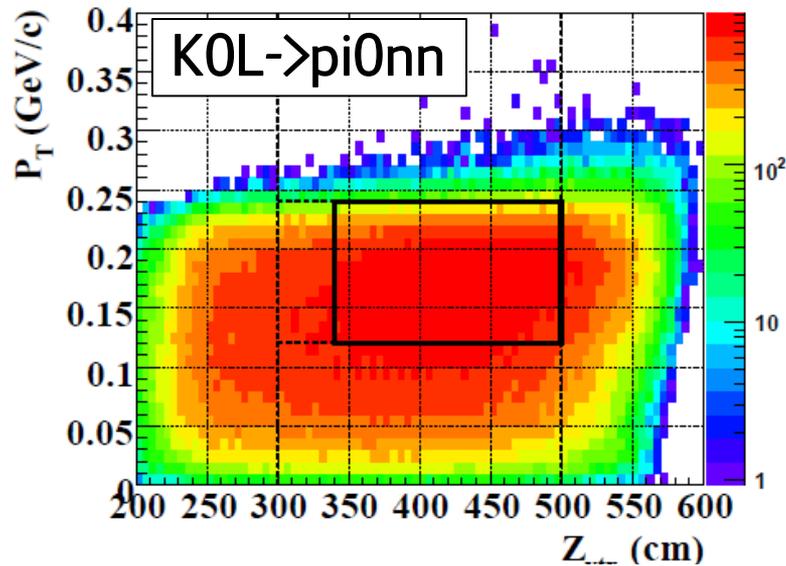


Background Sources from miss-reconstruction

- **CC02 pi0 BG**
 - energy γ was miss-measured
- **CV pi0 BG**
 - fusion γ cluster
- **CV eta BG**
 - difference in $M(\pi^0)$ and $M(\eta)$



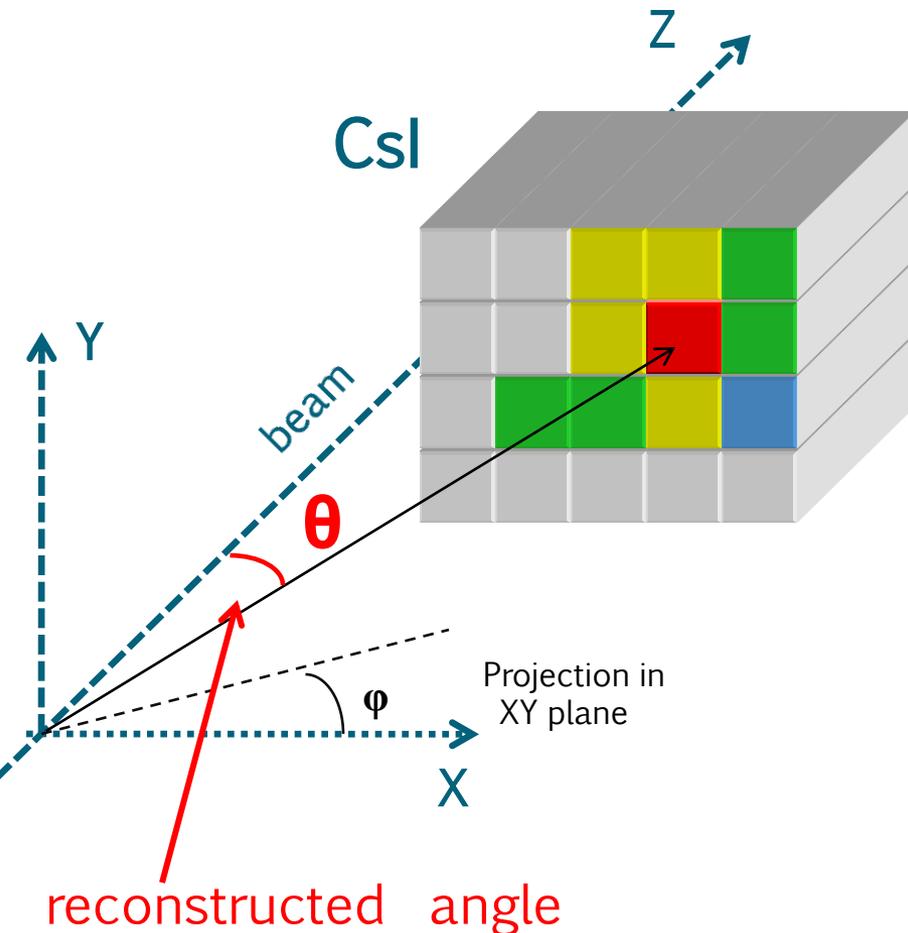
Main Background Sources (MC simulation)



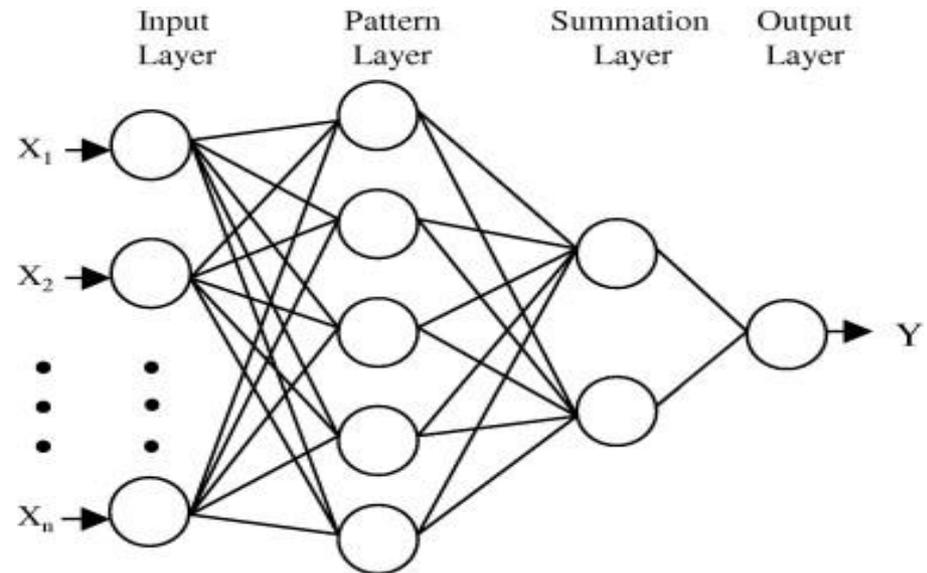
Motivation 1

- For more deep BG suppression and signal selection it will be very helpful to obtain angle information of each photon
 - We can reconstruct Z_{vtx} without π^0 mass assumption

Method for the Photon Angle Reconstruction



Generalized Regression Neural Network with Radial Basis Function



Inputs:

- E gamma
- E of each crystal in cluster

Outputs:
Angle θ

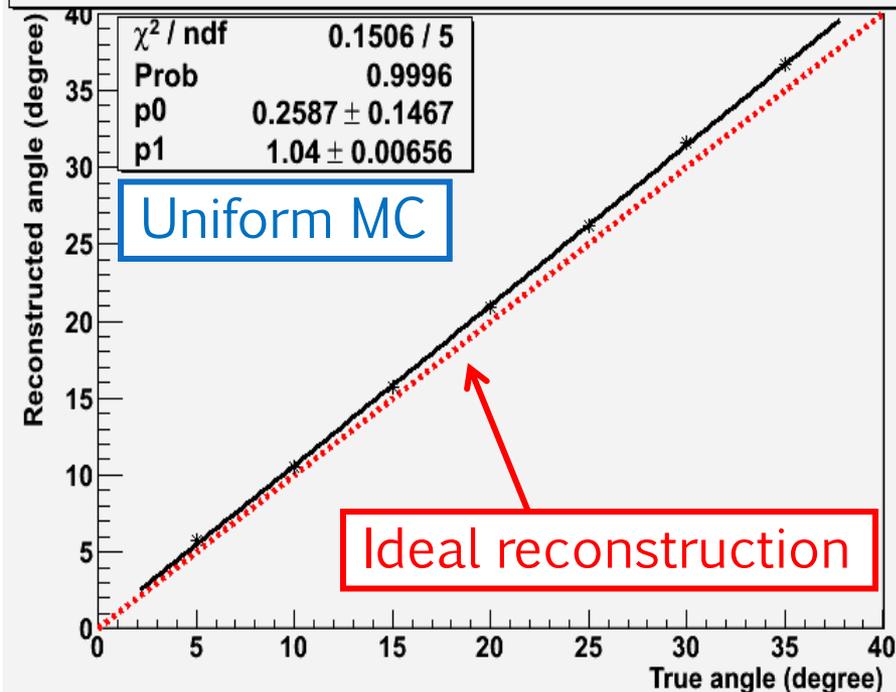
Training samples:

- 7x7 matrix of 7.0x7.0cm crystals
- $x, y = [-3.5; 3.5]$ cm step=0.35cm
- $E = [200; 2500]$ MeV step=50MeV
- $\Phi = [0; 45]$ deg. step=3 deg.
- $\Theta = [0; 50]$ deg. step=0.5 deg

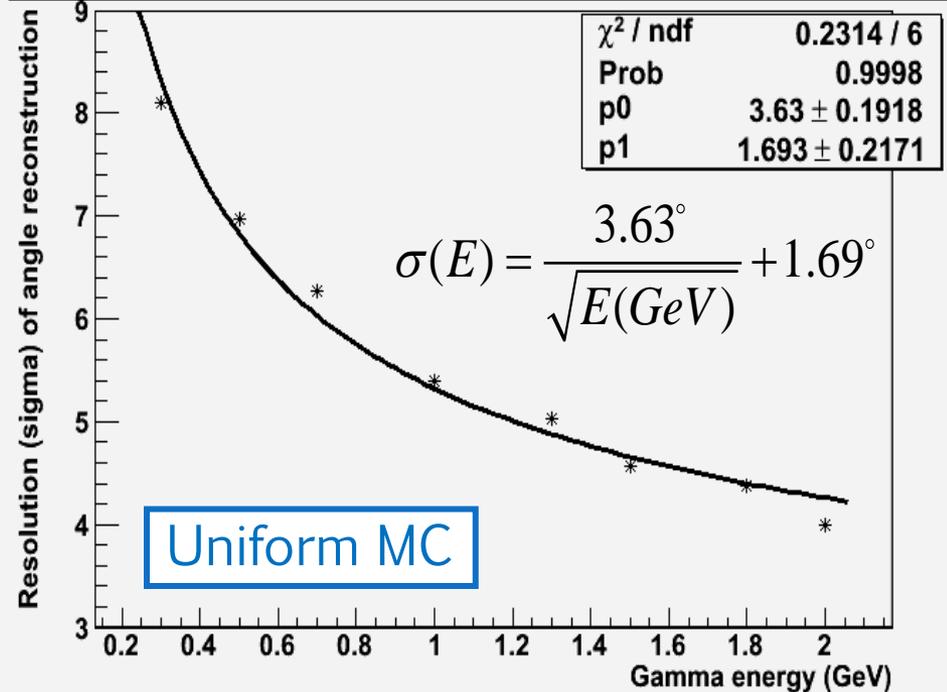
Photon Angle Reconstruction: Performance of NN

Linearity of reconstructed angle vs. true angle(left) and direction reconstruction precision vs. gamma energy (right). These distributions were obtained from special uniform MC

Reconstructed angle vs. true angle dependency

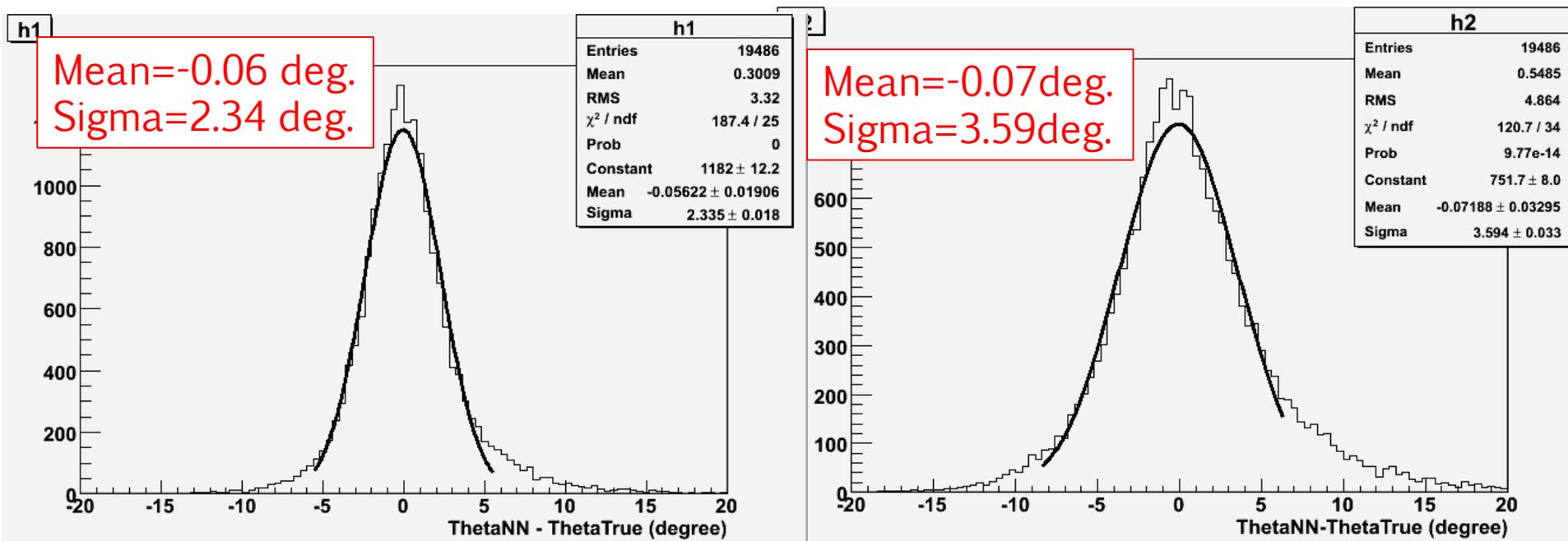


Angle reconstruction precision on the gamma energy dependency



Photon Angle Reconstruction: Performance of NN

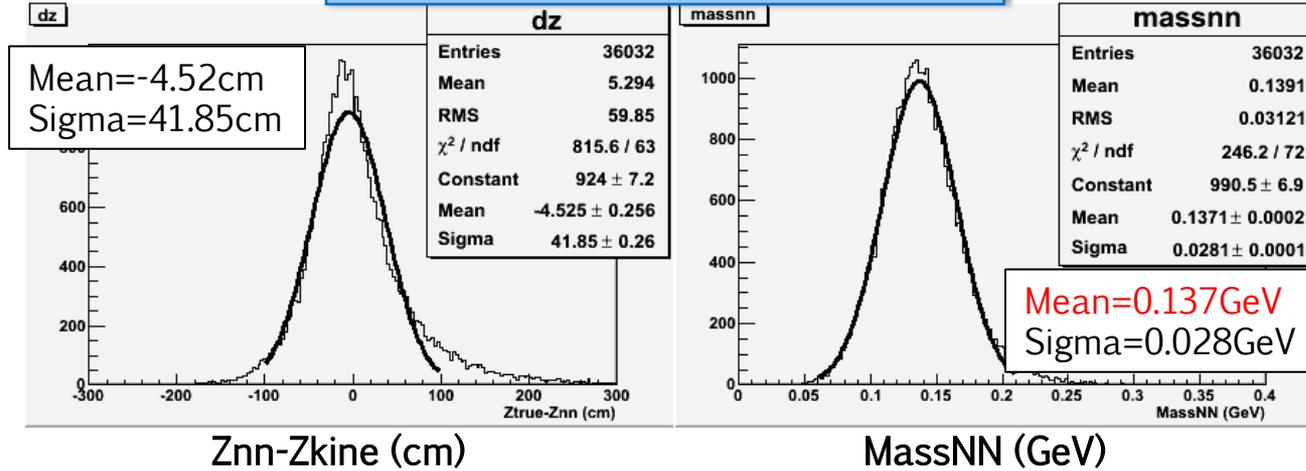
Differences between angle obtained from NN and angle obtained from kinematic(left for higher energy gamma, right for lower energy gamma). This distributions were obtained from MC $K^0_L \rightarrow \pi^0 n \nu \bar{\nu}$



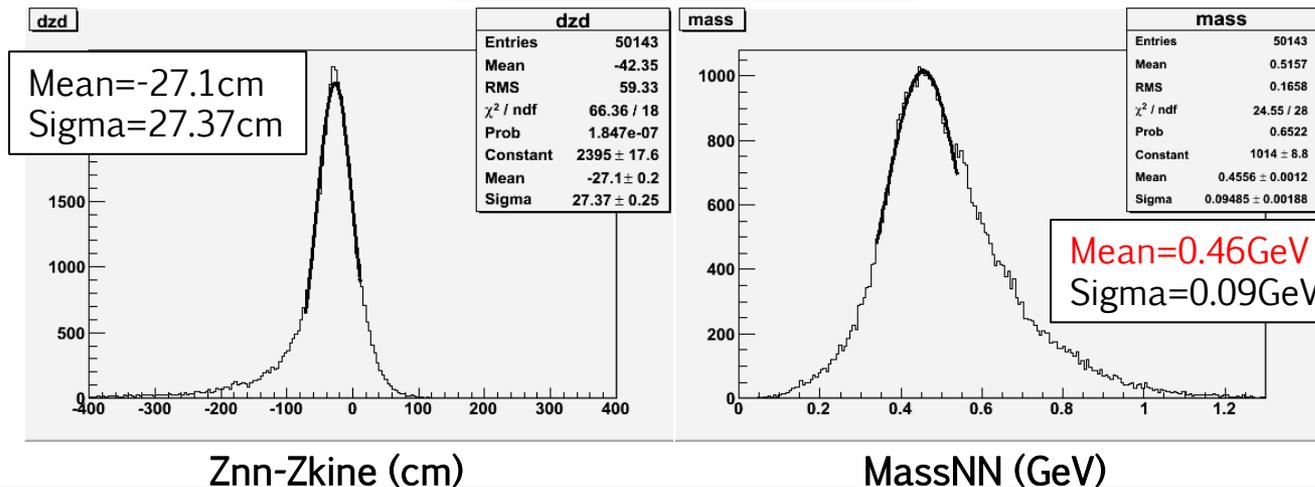
$K^0_L \rightarrow \pi^0 n \nu \bar{\nu}$ MC sample

Photon Angle Reconstruction: Mass & Zvtx reconstruction

K→piOnunubar sample (MC)



K→gg sample (MC)



On reconstruction we use kinematic fitting (with assumption of single vertex of reconstructed gamma)

Main condition:

$$z_{g1} - z_{g2} = \frac{\sqrt{x_1^2 + y_1^2}}{\text{tg}(\theta_1)} - \frac{\sqrt{x_2^2 + y_2^2}}{\text{tg}(\theta_2)} \equiv 0$$

The constraint is imposed using the Lagrange multiplier method:

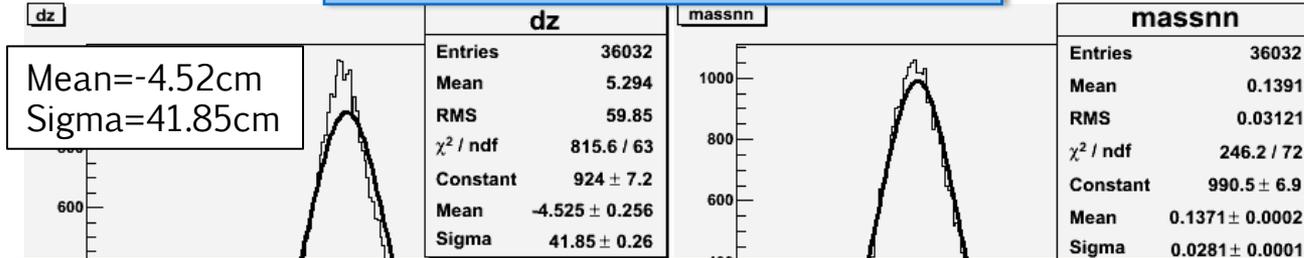
$$\chi^2 = \frac{(\theta_1 - \theta_1^0)^2}{\sigma_{\theta_1}^2} + \frac{(\theta_2 - \theta_2^0)^2}{\sigma_{\theta_2}^2} + 2\lambda \left(\frac{\sqrt{x_1^2 + y_1^2}}{\text{tg}(\theta_1)} - \frac{\sqrt{x_2^2 + y_2^2}}{\text{tg}(\theta_2)} \right)$$

Where θ_1^0, θ_2^0 are the initial measurements of

θ_1, θ_2

Photon Angle Reconstruction: Mass & Zvtx reconstruction

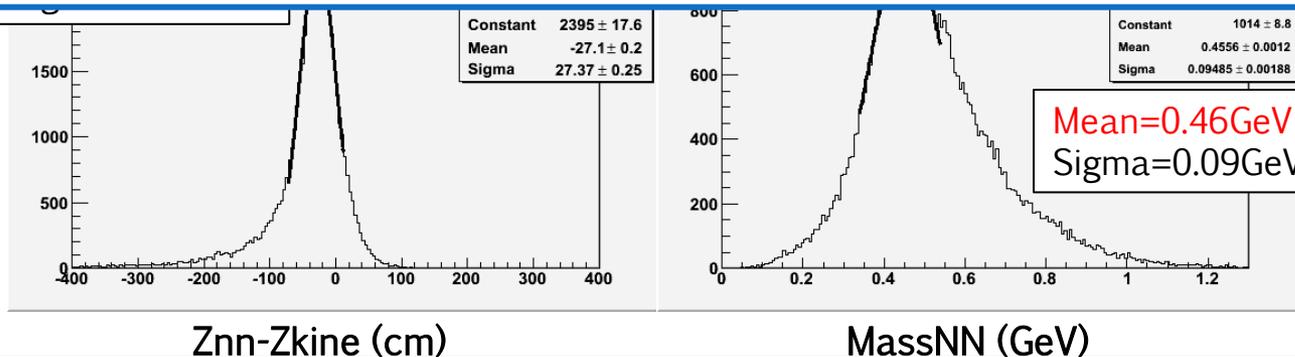
K→pi0nubar sample (MC)



On reconstruction we use kinematic fitting (with assumption of single vertex of reconstructed gamma)

Main condition:

- Using angle information we reconstruct mass of X→2gamma (**first time in experiment!**)
- New variables for events selection: $M(\pi^0)$, $\theta_{\text{rec}} - \theta_{\text{true}}$
- Involving new variables into analysis allowed to **increase sensitivity on 35%** (Run2 statistics)



$$+2\lambda \left(\frac{\sqrt{x_1^2 + y_1^2}}{\text{tg}(\theta_1)} - \frac{\sqrt{x_2^2 + y_2^2}}{\text{tg}(\theta_2)} \right)$$

Where θ_1^0, θ_2^0 are the initial measurements of

θ_1, θ_2

Motivation 2: Brief Scheme of Event Selection in E391

Detect 2γ clusters
in CsI calorimeter



Hermetic Photon
Veto System



“No signal”
*[deposited energy < threshold
for each detector]*



About 20
variables



Reconstruct kinematics of
decay



Kinematic selection for
separation between signal &
backgrounds



About 20
variables

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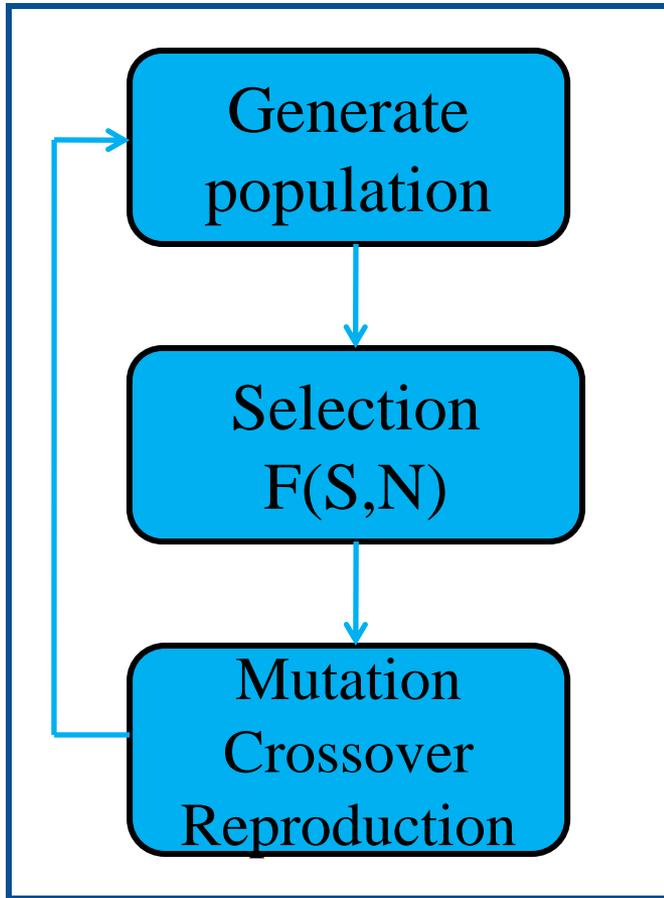


About 20
variables

Cuts thresholds
tuning making
“by hands”

Cuts tuning require a lot of time

Automatic cuts optimization with Genetic Algorithms



- **Main goal:** Fully automatic cuts optimization with complete BG estimation and acceptance calculation

- **Different ways for optimization:** by introducing different kinds of fitness functions we could change direction of searching – significantly increasing acceptance (S-signal) or suppressing background (N-noise) or keeping S/N ratio.

- **Optimization principle:**

- 1) Generate initial population of cuts
- 2) For each “individual” (set of cuts) :
 - evaluate acceptance
 - evaluate background
 - calculate **fitness function** $F(S,N)$
- 3) Select better individuals in population
- 4) Generate new population -> go to step 2

Free source code: <http://garage.cse.msu.edu/software/lil-gp/>

Automatic cuts optimization with Genetic Algorithms

- Main goal: Fully automatic cuts optimization with complete BG estimation and acceptance calculation
- Different ways for optimization: by introducing

Result of test optimization: sensitivity the E391a setup increased on 42 %, and the contribution of background events decreased by 29 % (Run2 result)

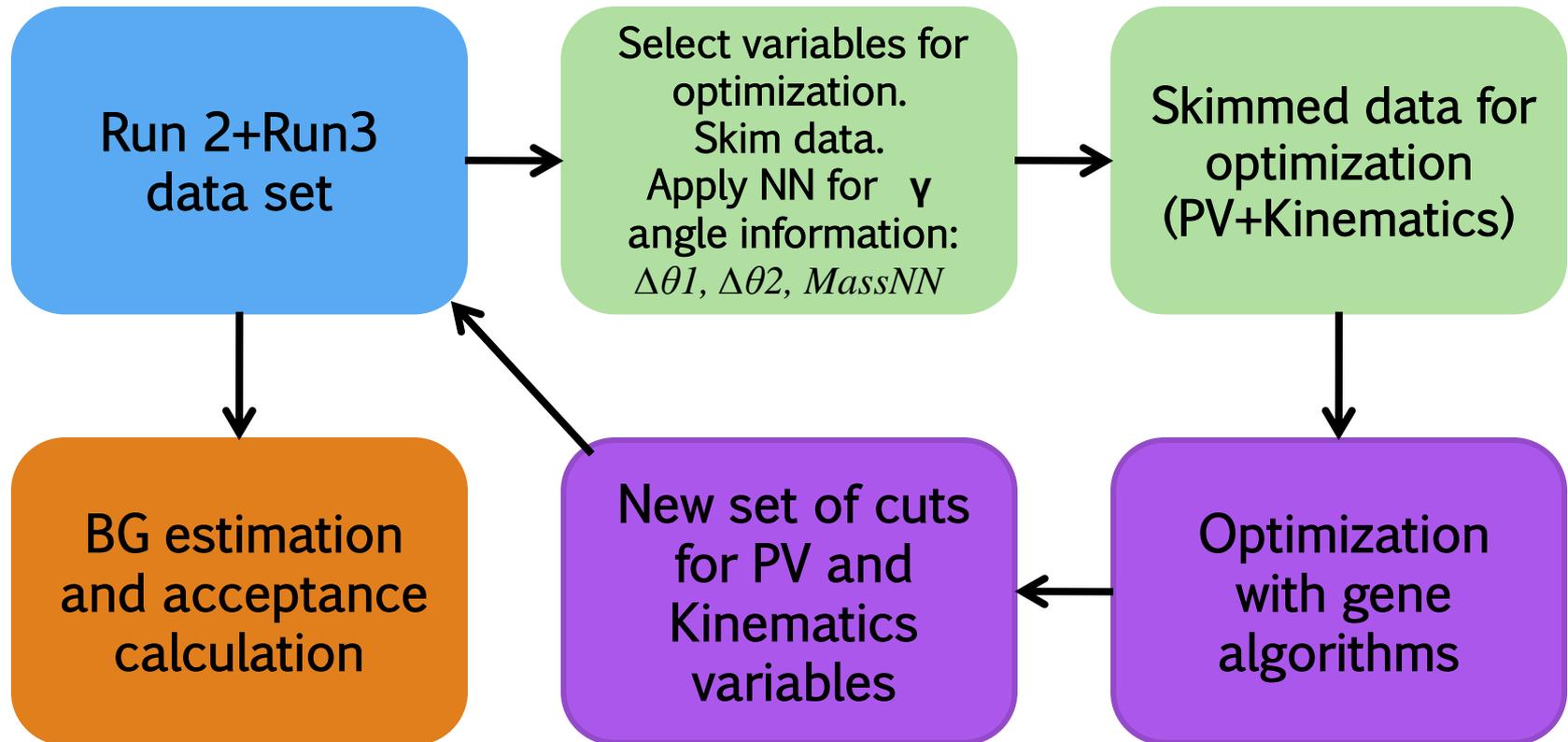
Generate population

Mutation
Crossover
Reproduction

- 2) For each “individual” (set of cuts) :
 - evaluate acceptance
 - evaluate background
 - calculate fitness function $F(S,N)$
- 3) Select better individuals in population
- 4) Generate new population -> go to step 2

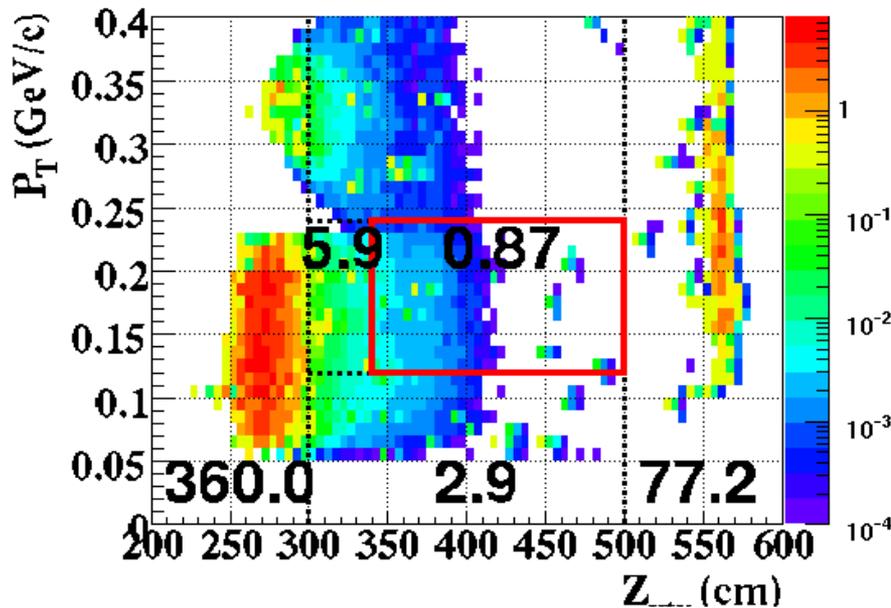
Free source code: <http://garage.cse.msu.edu/software/lil-gp/>

Motivation 3: E391 Data Reanalysis with 2 methods

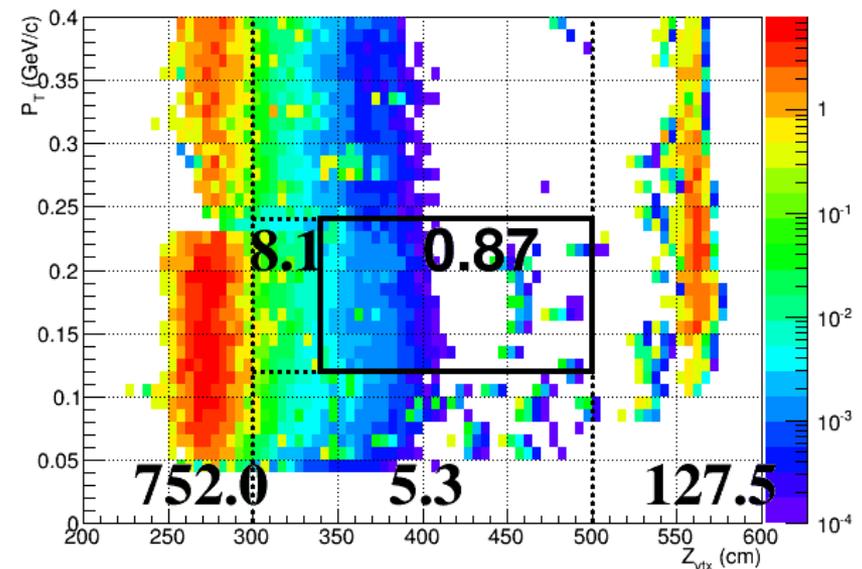


Results: Summary BG (Run2+Run3)

E391 analysis



E391 reanalysis



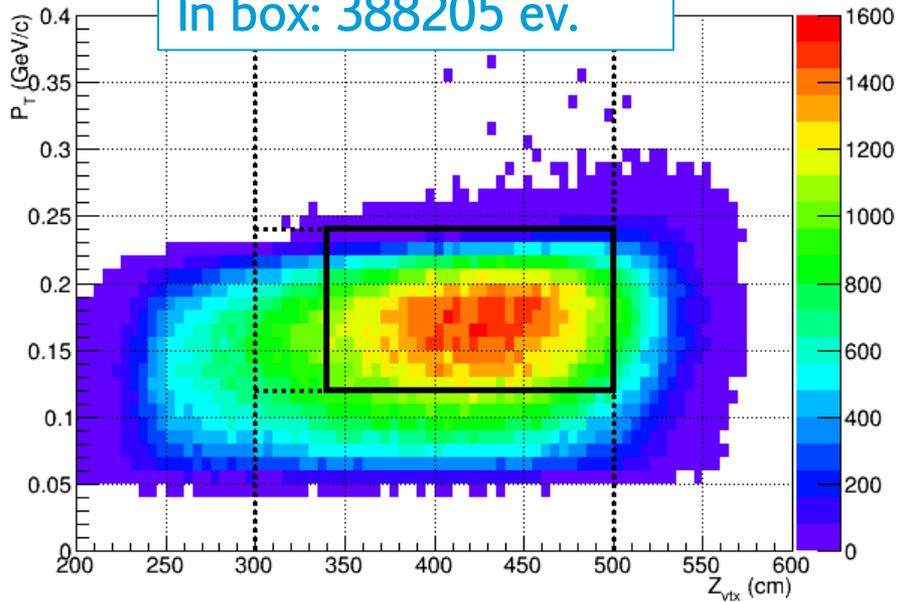
	K->2pi0	CC02-pi0	CV-pi0	CV-eta	Signal Box
E391 analysis	0.02	0.66	negligible	0.19	0.87
New analysis	0.03	0.29	0.34	0.25	0.87

Total BG: the same level
(In comparison with E391 final result)

Results: Acceptance (Run2+Run3)

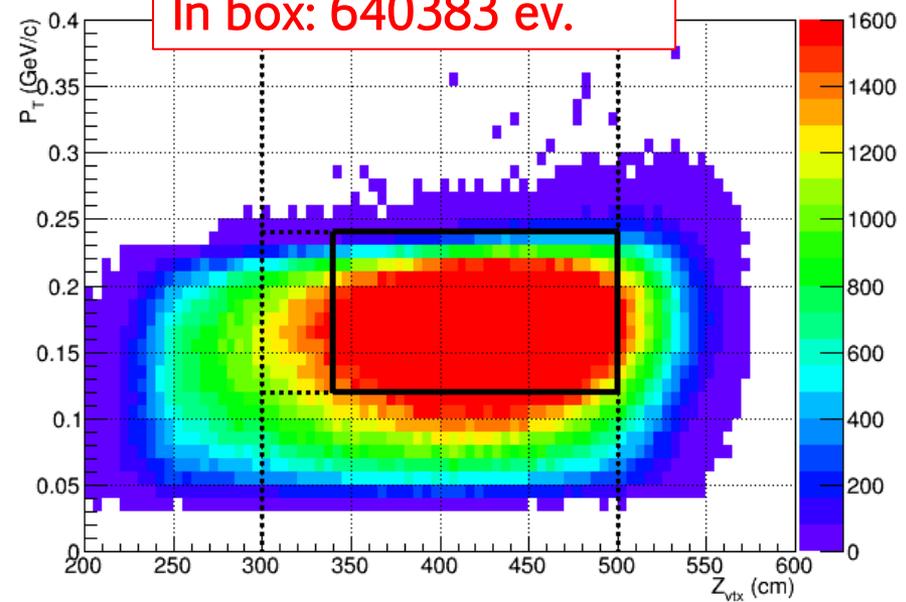
E391 analysis

In box: 388205 ev.



E391 reanalysis

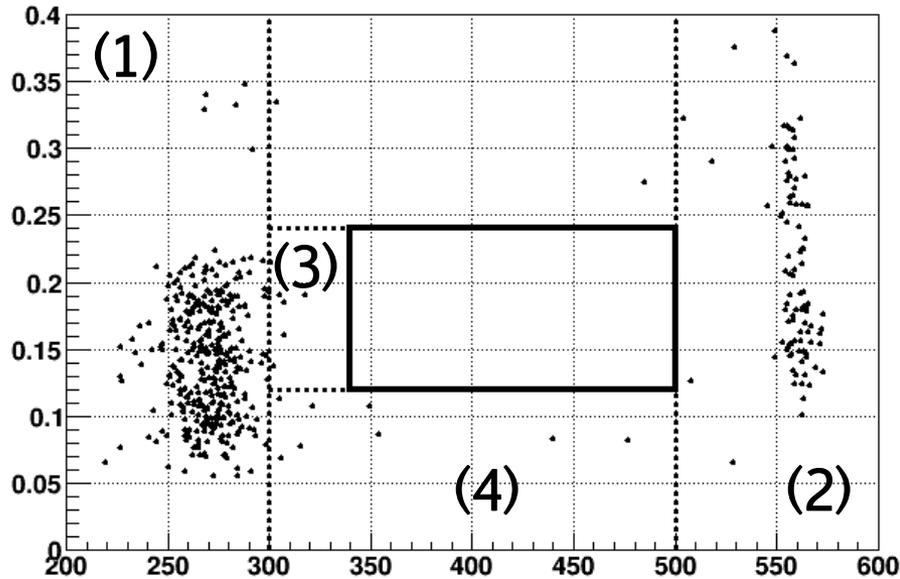
In box: 640383 ev.



Total BG: the same level
Acceptance : increased on 65%
(In comparison with E391 final result)

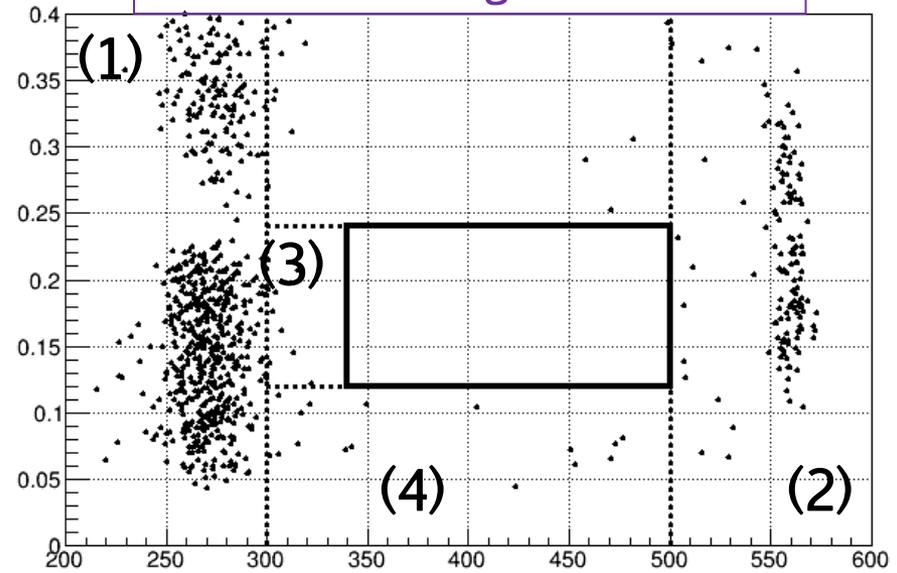
Results: Final Plot (Run2+Run3 data)

E391 analysis



E391 reanalysis

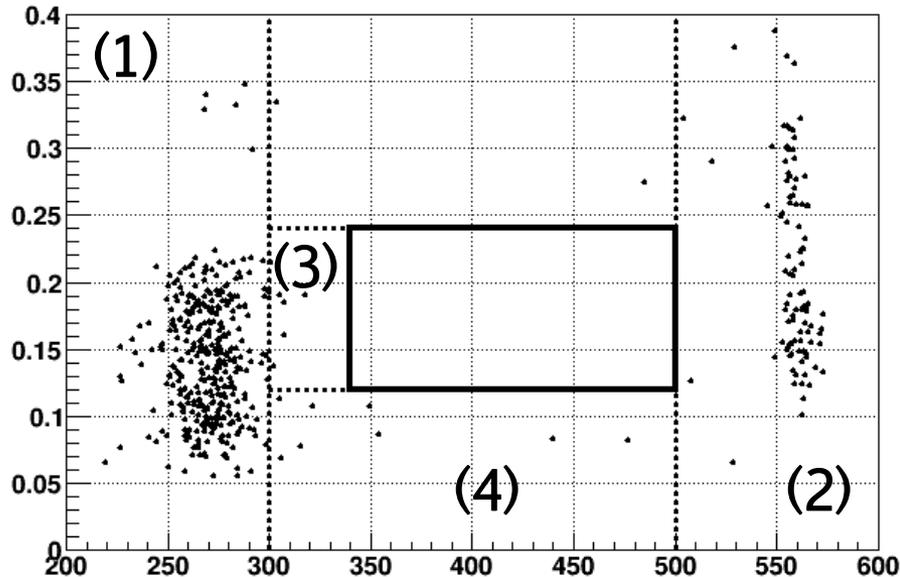
No events in signal box!!



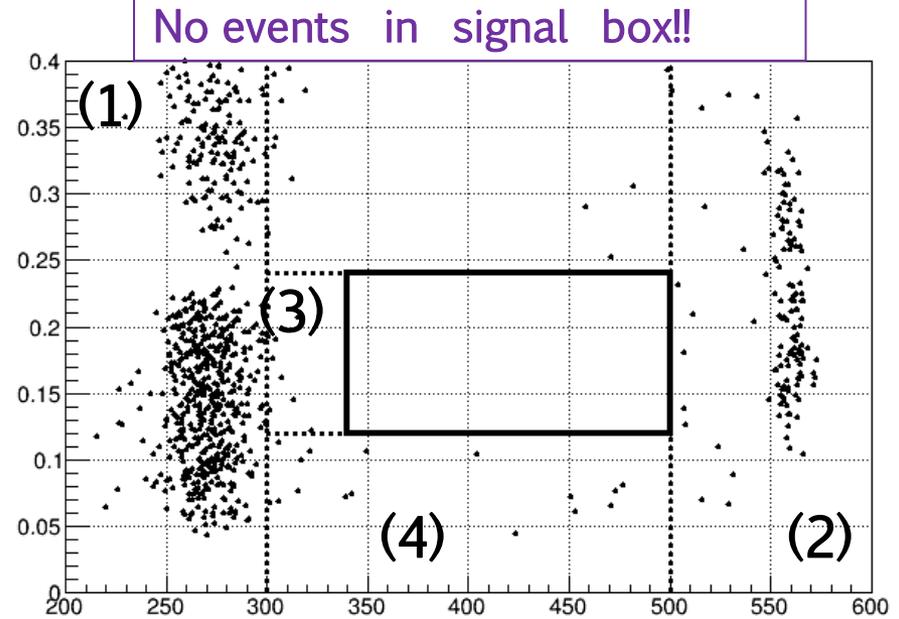
	Region-1	Region-2	Region-3	Region-4	Signal box
Data	752 (360)	151 (101)	9 (8)	16 (8)	0 (0)
MC BG	752 (360)	127.5 (77.2)	8.1 (5.9)	5.3 (2.9)	0.87 (0.87)

Results: Final Plot (Run2+Run3 data)

E391 analysis



E391 reanalysis



Total BG: the same level
Acceptance : increased on 65%
Data : No events in signal box!!
 (In comparison with E391 final result)

	Signal box
Data	0 (0)
MC BG	0.87 (0.87)

	Signal box
Data	0 (0)
MC BG	0.87 (0.87)

Thank you for attention!