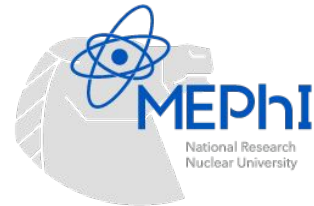
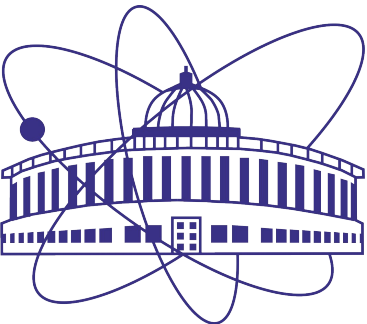


# Review of methods for measuring collective flow and global polarization of $\Lambda$ hyperons

Troshin V.<sup>1,2</sup>, Parfenov P.<sup>1,2</sup>, Taranenko A.<sup>1,2</sup>

(1- JINR, 2 - MEPHI)

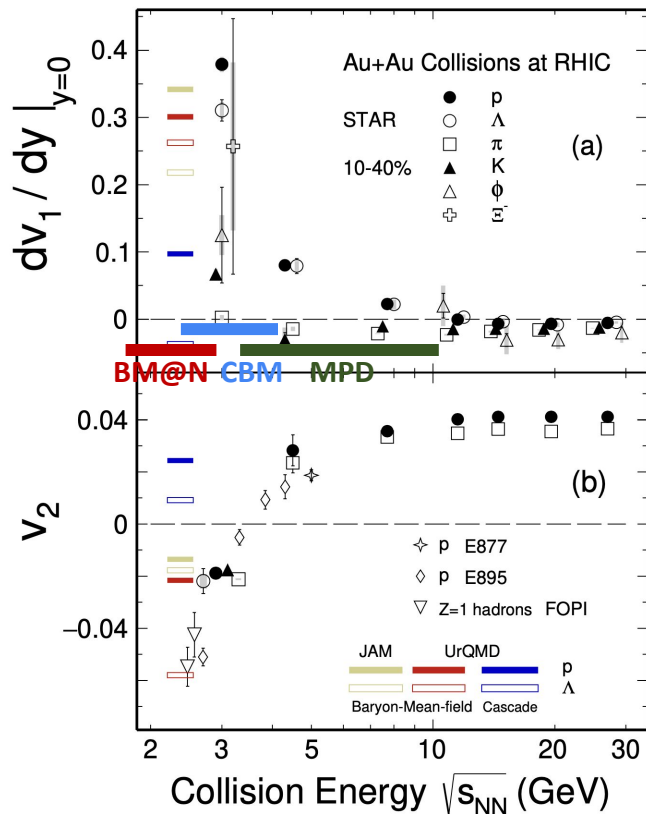
12th Collaboration Meeting of the BM@N Experiment at the NICA Facility



# Outline

- Introduction
- Anisotropic flow and global polarization measurements
- Track crossing
- Reconstructed efficiency
- Radial distance asymmetry
- Detector occupancy
- Summary

# Anisotropic transverse flow in heavy-ion collisions at Nuclotron-NICA energies



Strong energy dependence of  $dv_1/dy$  and  $v_2$  at  $\sqrt{s_{NN}} = 4-11$  GeV.

Anisotropic flow at FAIR/NICA energies is a delicate balance between:

- The ability of pressure developed early in the reaction zone
- Long passage time (strong shadowing by spectators).

Differential flow measurements  $v_n(\sqrt{s_{NN}}, \text{centrality}, \text{pid}, p_T, y)$  will help to study:

- effects of collective (radial) expansion on anisotropic flow
- interaction between collision spectators and produced matter
- baryon number transport

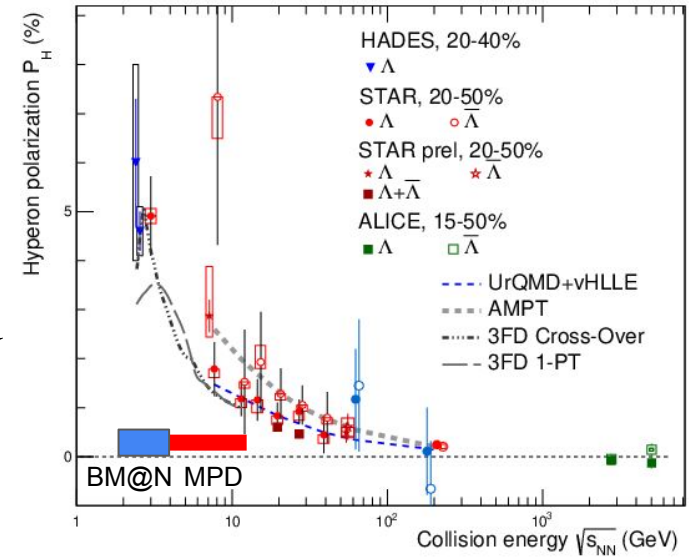
Several experiments (MPD, BM@N, STAR FXT, CBM, HADES, NA61/SHINE) aim to study properties of the strongly-interacted matter in this energy region.

# Global Polarization at Nuclotron-NICA energies

- Predicted and observed global polarization signals rise as the collision energy is reduced:

NICA energy range will provide new insight

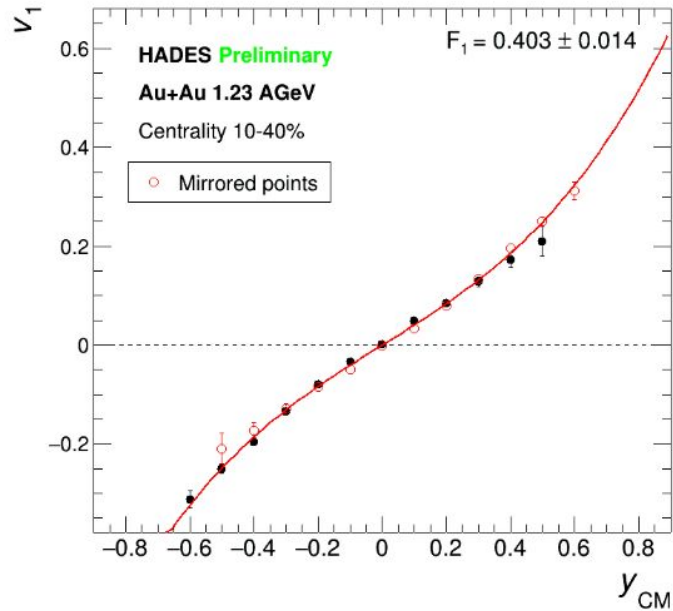
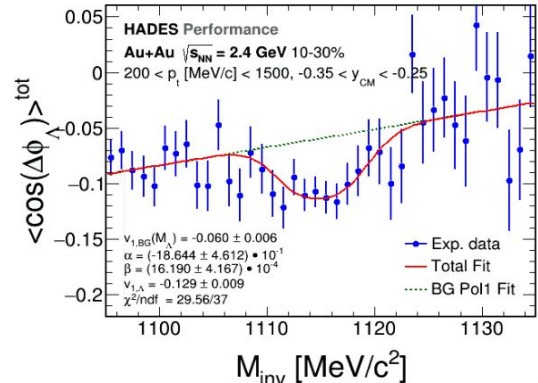
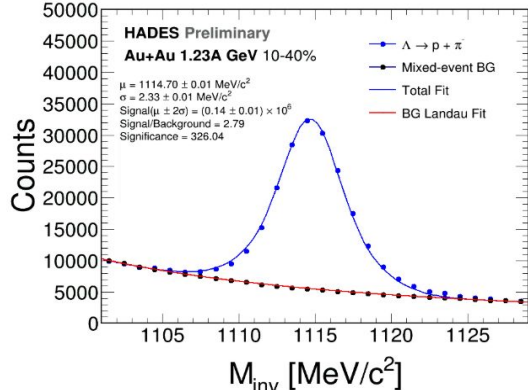
- $\Lambda(\bar{\Lambda})$  - splitting of global polarization
- Comparison of models, detailed study of energy and kinematical dependences, improving precision
- Probing the vortical structure using various observables



S. Singha, EPJ Web Conf. 276 (2023)  
06012

J. Adam et al. (STAR Collaboration), Phys. Rev. C 98, 014910 (2018)  
O. Teryaev and R. Usubov, Phys. Rev. C 92, 014906 (2015)

# $v_n$ of $V_0$ particles: invariant mass fit method



Reasonable directed flow measurements for reconstructed  $\Lambda$

$$v_2^{SB}(\mathbf{m}_{inv}, \mathbf{p}_T) = v_2^S(\mathbf{p}_T) \frac{N^S(\mathbf{m}_{inv}, \mathbf{p}_T)}{N^{SB}(\mathbf{m}_{inv}, \mathbf{p}_T)} + v_2^B(\mathbf{m}_{inv}, \mathbf{p}_T) \frac{N^B(\mathbf{m}_{inv}, \mathbf{p}_T)}{N^{SB}(\mathbf{m}_{inv}, \mathbf{p}_T)}$$

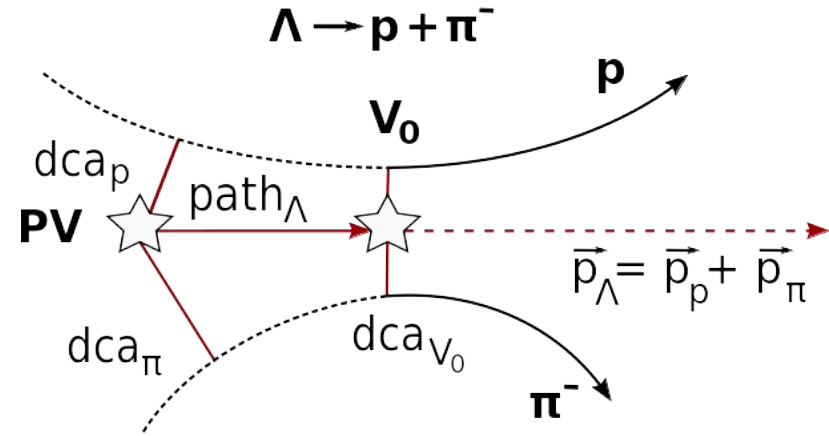
Frédéric Julian Kornas Thesis: PhD Dortmund U. (2021)

# Measurements of global hyperon polarization

- Polarization can be measured using the azimuthal angle of proton in Lambda rest frame  $\phi^*$

$$\bar{P}_{\Lambda/\bar{\Lambda}} = \frac{8}{\pi\alpha} \frac{1}{R_{EP}^1} \langle \sin(\Psi_{EP}^1 - \phi^*) \rangle$$

- ➔ Determine centrality
- ➔ Determine event plane  
( $\Psi_{EP}^1, R_{EP}^1$ )
- ➔ Reconstruct Lambda
- ➔ Measure global polarization

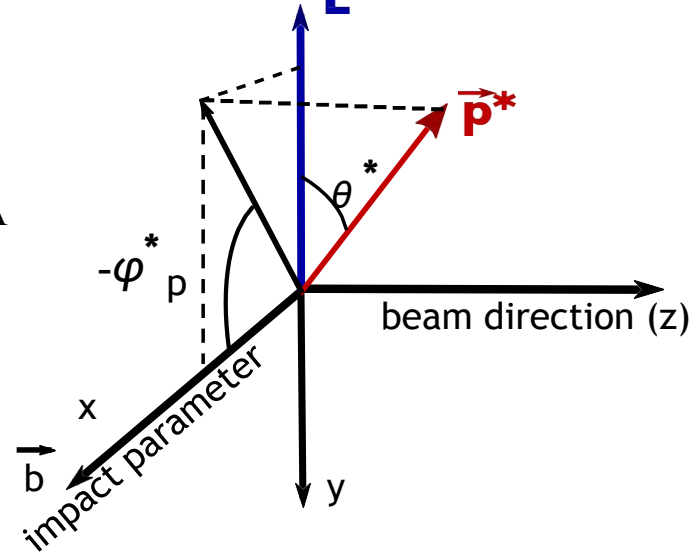
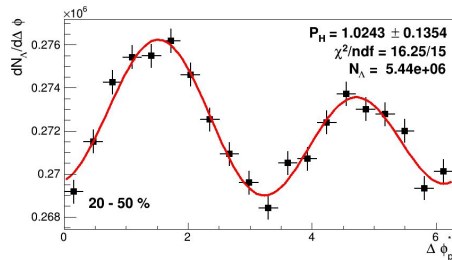


- PV — primary vertex
- $V_0$  — vertex of hyperon decay
- dca — distance of closest approach
- path — decay length

# $\Delta\phi$ -method

- Obtain invariant mass distribution in bins of  $\Delta\phi_p^* = \Psi_{EP}^1 - \phi_p^*$ 
  - Net amount of  $\Lambda$  in each bin
  - Distribution of  $N_\Lambda(\Delta\phi_p^*)$
- Fit of the distribution to get  $\langle \sin(\Delta\phi_p^*) \rangle \rightarrow P_\Lambda$

- $dN/d\Delta\phi_p^*$
- $P_\Lambda = \frac{8}{\pi\alpha_\Lambda} \frac{p_1}{R_{EP}^1}$



$$\bar{P}_{\Lambda/\bar{\Lambda}} = \frac{8}{\pi\alpha} \frac{1}{R_{EP}^1} \langle \sin(\Psi_{EP}^1 - \phi_p^*) \rangle$$

$$\frac{dN}{d\Delta\phi_p^*} = p_0(1 + 2p_1 \sin \Delta\phi_p^* + 2p_2 \cos \Delta\phi_p^* + 2p_3 \sin 2\Delta\phi_p^* + 2p_4 \cos 2\Delta\phi_p^* + \dots)$$

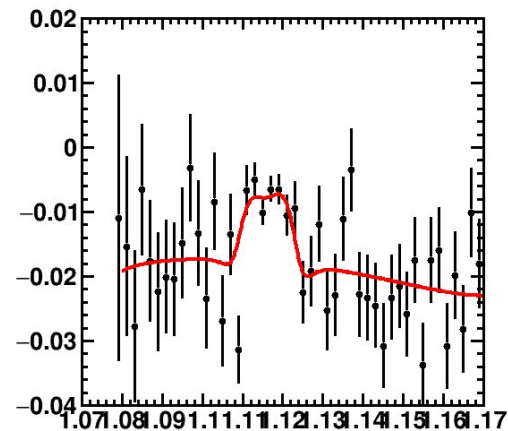
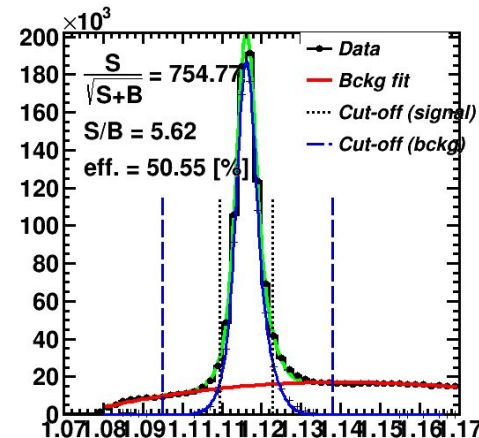
# Inv. mass fit method

- Use invariant mass distribution
- Calculate Sig/All, Bg/All ratios
- Fit  $\langle \sin(\Psi_{EP} - \phi_p^*) \rangle$  as a function of inv. mass:

$$P^{SB}(m_{inv}, p_T) = P^S(p_T) \frac{N^S(m_{inv}, p_T)}{N^{SB}(m_{inv}, p_T)} + P^B(m_{inv}, p_T) \frac{N^B(m_{inv}, p_T)}{N^{SB}(m_{inv}, p_T)}$$

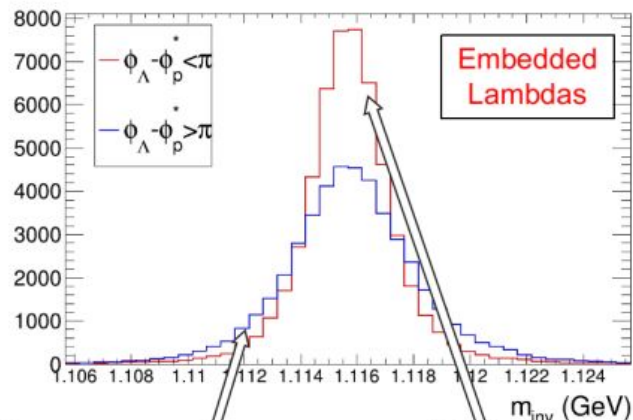
- Use  $P^S(p_T) = \langle \sin(\Psi_{RP} - \phi_p^*) \rangle^S$  to find  $P_H$ :

$$\bar{P}_{\Lambda/\bar{\Lambda}} = \frac{8}{\pi\alpha} \frac{1}{R_{EP}^1} \langle \sin(\Psi_{EP}^1 - \phi_p^*) \rangle$$



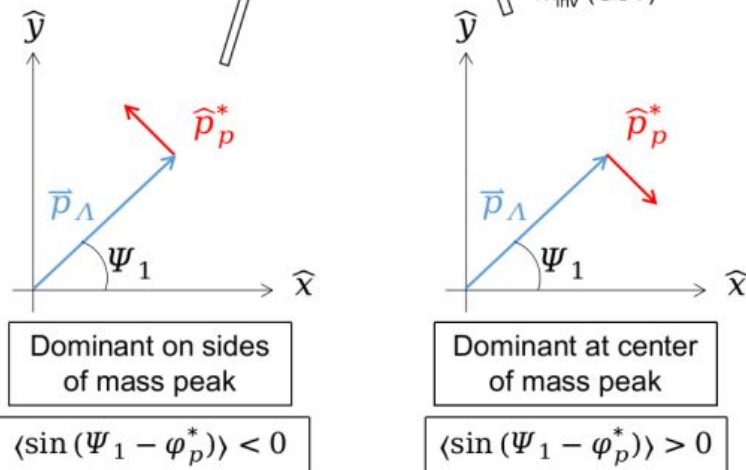


# Track crossing and $v_1$ contribution



**Problem:** daughter particles tracks with opposite charges are bended in the opposite directions in the magnetic field, and these tracks may cross each other that leads 2 peaks distribution.

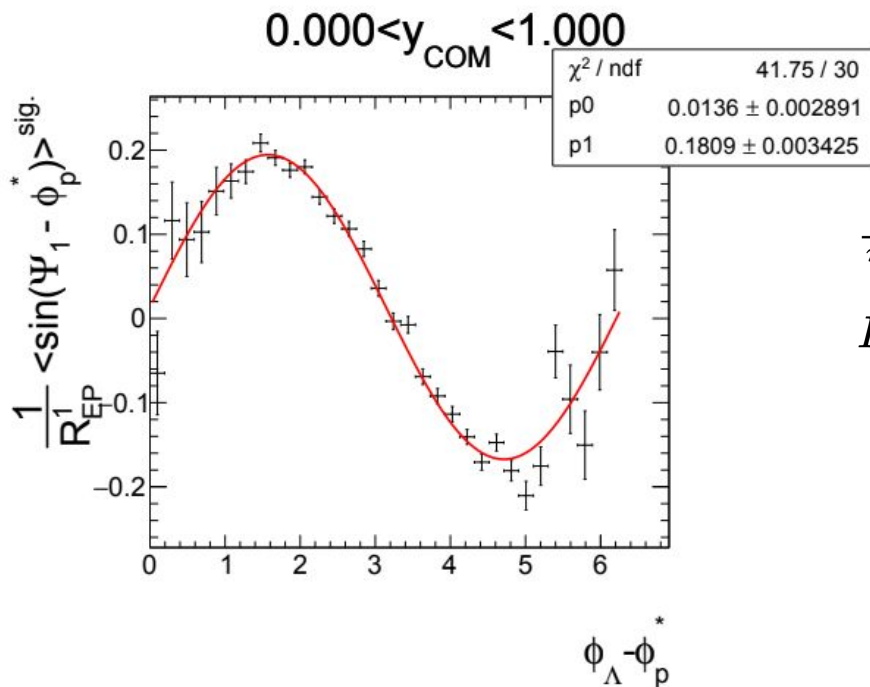
**Solution:** fit signal with 2 gaussses



**Warning:** with detector asymmetry it would provide the effect of  $v_1$  on the polarization measurements and odd pseudorapidity dependence

M.S. Abdallah et al. (STAR Collaboration),  
Phys. Rev. C 104, L061901 (2021)

# Generalized inv. mass fit method



Fit  $P^S = \langle \sin(\Psi_{\text{RP}} - \phi_p^*) \rangle^S$   
 in bins of  $\phi_\Lambda - \phi_p^*$  for  $\eta > 0$ ,  $\eta < 0$  using  
 formula:

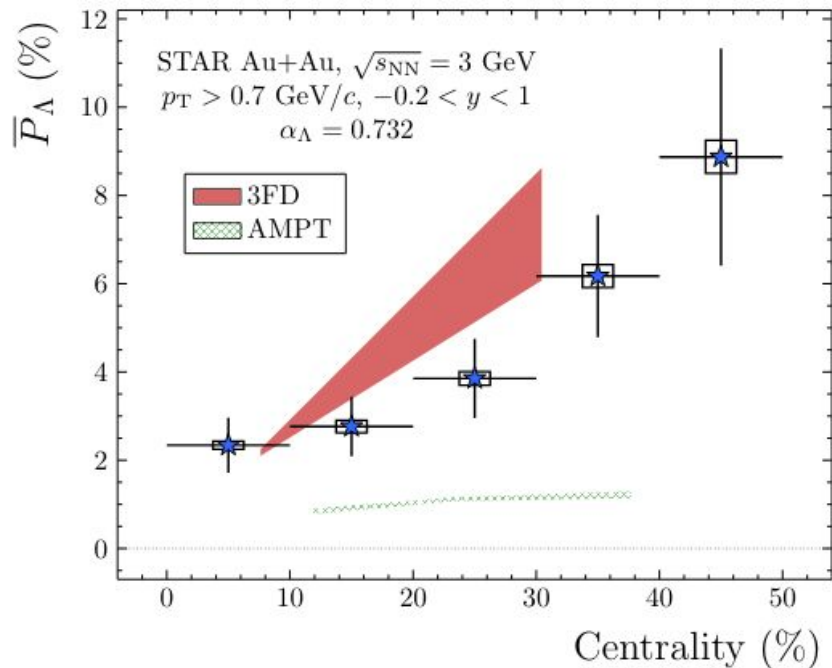
$$\frac{8}{\pi\alpha_\Lambda} \frac{1}{R_{EP}^{(1)}} \langle \sin(\Psi_1 - \phi_p^*) \rangle^{\text{sig}} = \bar{P}_\Lambda^{\text{true}} + cv_1 \sin(\phi_\Lambda - \phi_p^*)$$

$$\bar{P}_H = \frac{1}{2} [\bar{P}_H(\eta > 0) + \bar{P}_H(\eta < 0)]$$

This fit corrects effects of directed flow and  
 acceptance contributions to  $P_H$

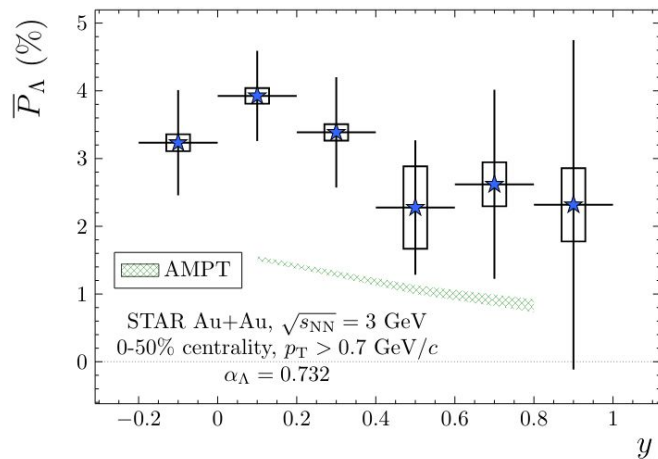
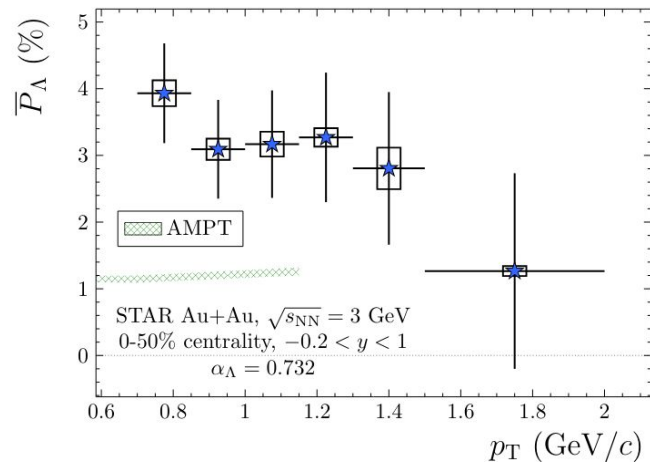
M.S. Abdallah et al. (STAR Collaboration),  
 Phys. Rev. C 104, L061901 (2021)

# Global polarization: STAR results



M.S. Abdallah et al. (STAR Collaboration),  
 Phys. Rev. C 104, L061901 (2021)

No dependence within uncertainties



# Corrections for reconstruction efficiency

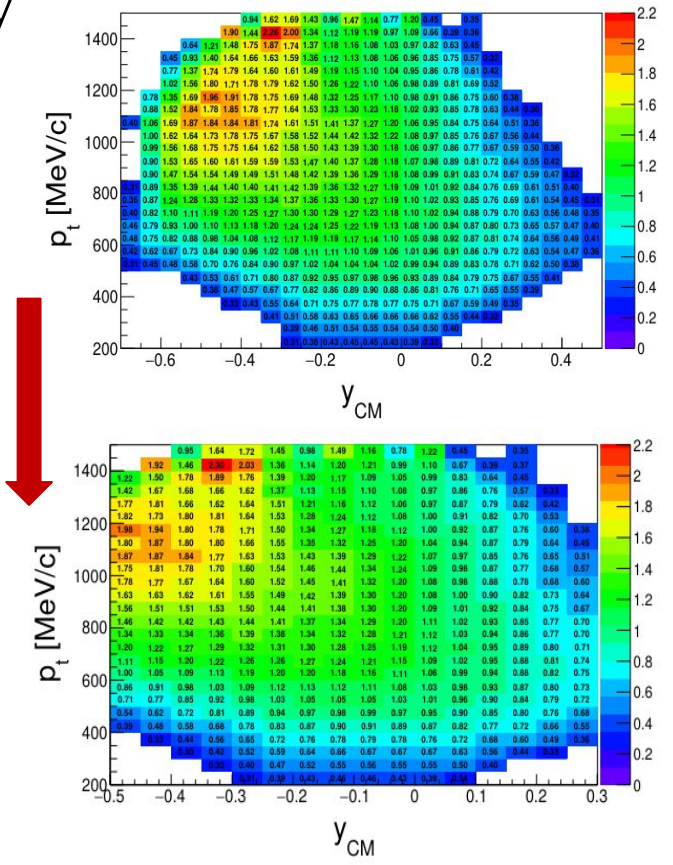
**Problem:** collective flow and global polarization are the observables with amplitude  $\sim 10^{-1}$ - $10^{-2}$  and  $10^{-3}$  correspondingly

Very limited acceptance leads to increasing the fluctuations of the mean due to low efficiency

**Solution:** weighting with relative reconstruction efficiency

$$\bar{\epsilon} = \frac{\int dy \int dp_t \frac{dN_{Reco}}{dy dp_t} \epsilon(p_t, y)}{\int dy \int dp_t \frac{dN_{Reco}}{dy dp_t}},$$

- Avoiding the shift of the mean
- Do not facing with the increasing of fluctuations

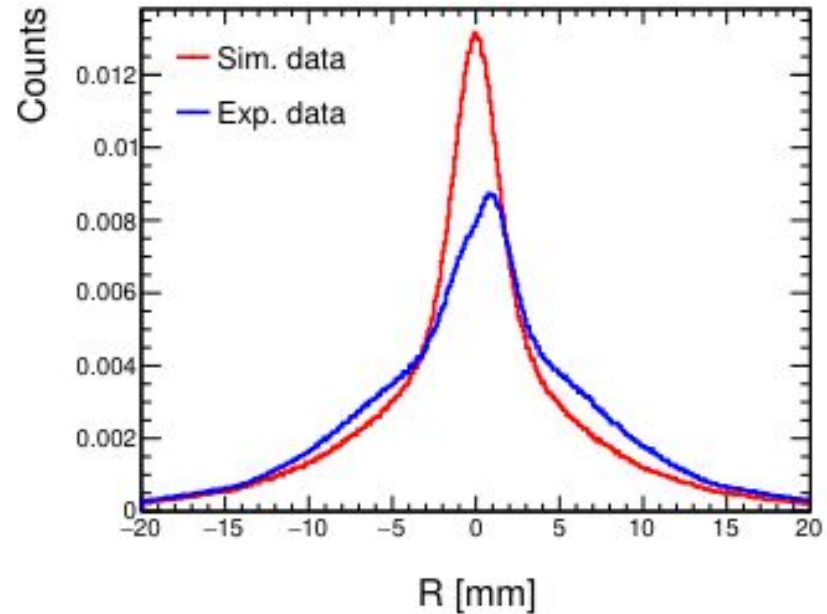


# Corrections for the radial distance asymmetry

Radial distance  $R$  - is the minimum distance of the reconstructed track to the beam axis

**Problem:** asymmetry of the radial distance wrt. vertex.

**Solution:** take the  $R$  distribution in the inv. mass range under the peak of  $\Lambda$  and calculate the weights that do this distribution flat after the correction



# Corrections for detector occupancy

**Problem:** efficiency loss due to strong varying track densities

**Result:** effect on  $v_1$  pseudorapidity dependence

Solution:

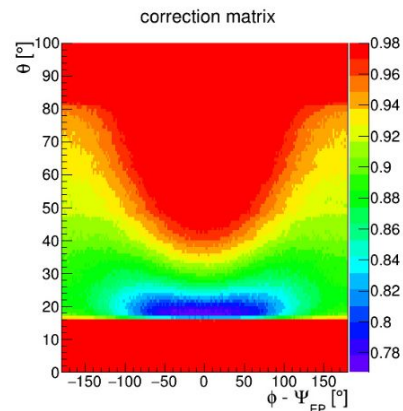
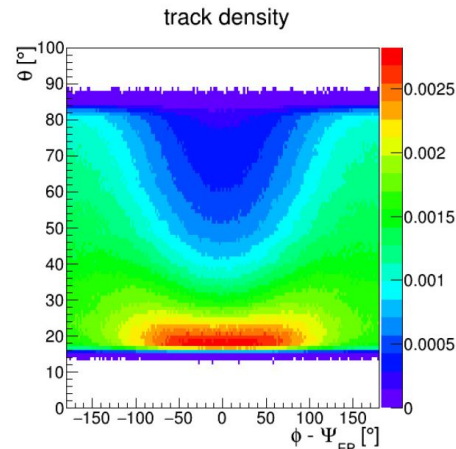
- centrality bins for occupancy

- $\epsilon(N_{\text{track}}) = \epsilon_0(1 - k \cdot N_{\text{track}})$

To obtain corrections due to occupancy for  $\Lambda$  the multiplication of proton and pion occupancy is used:

$$\epsilon_{\Lambda} = \epsilon_p \cdot \epsilon_{\pi^-}$$

- Very high effect on  $v_1$  slope that cannot be explained with systematics
- Occupancy corrections for  $\Lambda$  is not working correctly



# Summary

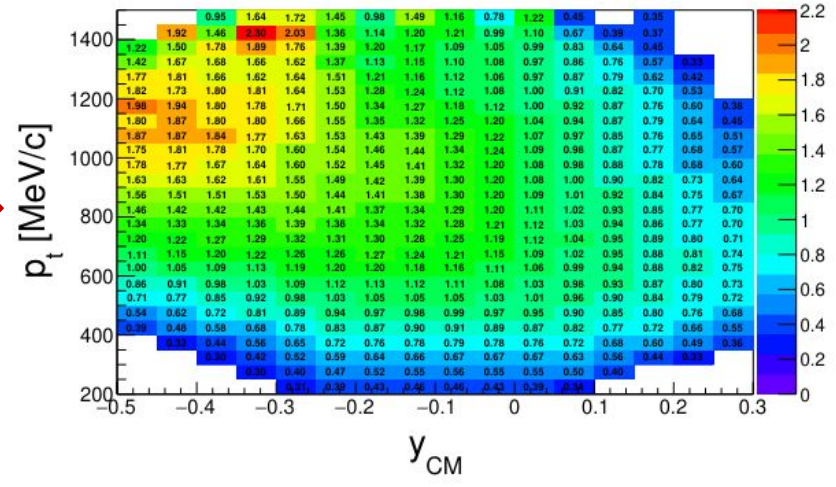
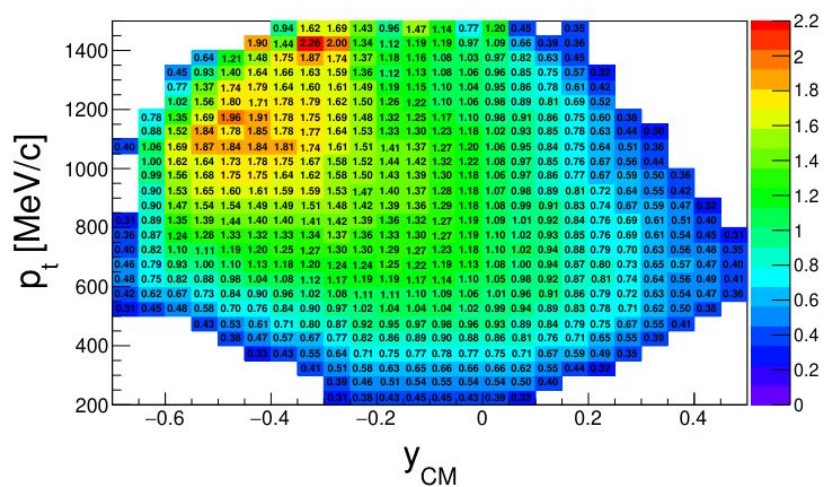
- Inv. mass fit method is a standard method for  $v_n$  measurements of V0 particles
- $\Delta\phi$ -method and inv. mass fit method gives reasonable result for global polarization measurements
  - Generalized inv. mass fit method is possible to correct acceptance effects and directed flow contribution
- Corrections reconstructed efficiency and radial distance asymmetry provides a reasonable effects
- Corrections for detector occupancy are still important to be studied

Thank you for your attention!

BACKUP



# Corrections for reconstruction efficiency



- cut efficiency  $< 0.3$
- Provide a relative efficiency
- Smooth it by Savitzky-Golay filter